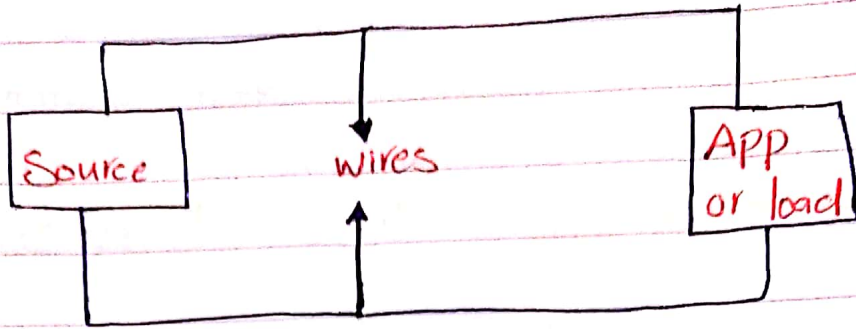
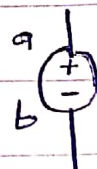


* Chapter "1" →



* Sources generator
battery

1- Voltage source 

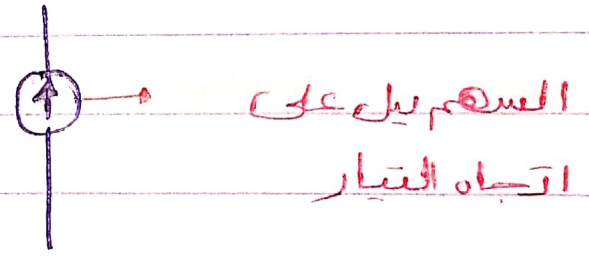
$$V_{ab} = \Delta V = V_a - V_b$$

* Voltage of source is DC or Independent Source
Direct Current

الفولتية تكون ثابتة

* PV طاقة شمسية
* AC فولتية متغيرة

2. Current Source (C.S)



* إذا كانت قيمة التيار 5A - نحافظ على نفس الاتجاه ونعوض
الشارة

* Loads →

(R) Resistance \rightarrow (يقاس بالأوم Ω)

(L) inductor (يقاس بالهنري H) \rightarrow

(C) Capacitor $\frac{1}{\text{T}}$ (يقاس بالفاراد F)

* Quantities →

* V (Volt) الجهد

* Power (watt) القدرة

* I (Ampere) التيار

$$P = \pm I \cdot V$$

لإشارة التيار

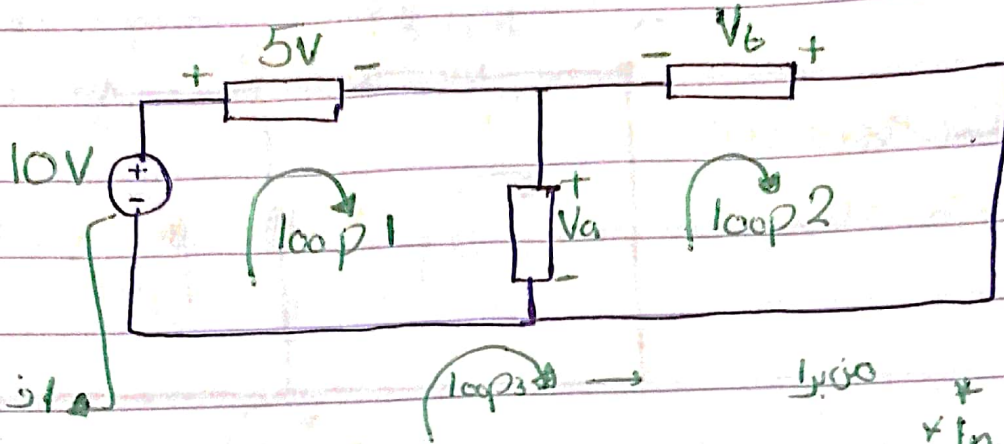
* Power (P) ⇒ $\begin{cases} + \rightarrow \text{Consume, absorb} \\ - \rightarrow \text{generate, deliver} \end{cases}$

* Energy = Power . time

↳ (Kw.h)

كيلوواط ساعة

* KVL (Kirchhoff's voltage law)



وإذا دخلت
بالسلك بوضوح
القوة سالبة

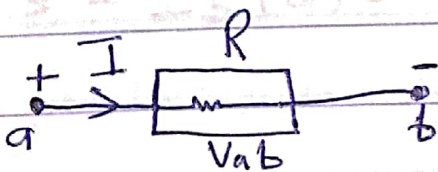
In a the loop
 $\sum V = 0$

وإذا دخلت بالسلك
بوضوح القوة موجبة

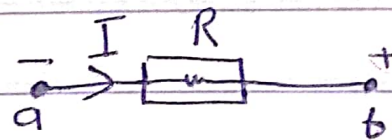
From loop 1 $\Rightarrow -10 + 5 + V_a = 0$
 $V_a = 5V$

From loop 2 $\Rightarrow -V_a - V_b = 0$
 $-5V = V_b \Rightarrow V_b = -5V$

* $V = IR$

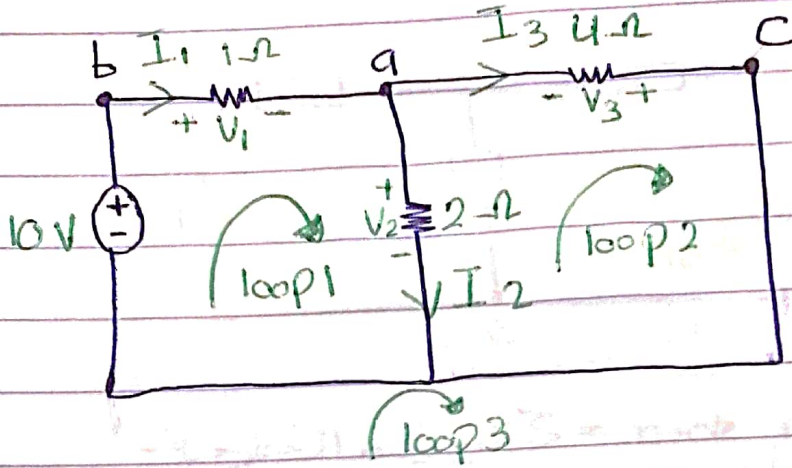


$V_{ab} = +IR$



$V_{ba} = -IR$

* Example:



* إذا ما شئ مع التيار بوضوه (4)
 * إذا ما شئ مع التيار بوضوه (-)

$$\text{loop 1} \Rightarrow -10 + I_1(1) + I_2(2) = 0$$

$$\text{loop 2} \Rightarrow -2I_2 + 4I_3 = 0$$

$$\text{loop 3} \Rightarrow -10 + I_1(1) + 4I_3 = 0$$

$$\text{at node a} \Rightarrow I_1 = I_2 + I_3$$

بكل حل 100 =

$$\text{* Assume } I_1 = 10, I_2 = -3, I_3 = 13$$

$$V_1 = +I_1(1) = 10 \text{ V}$$

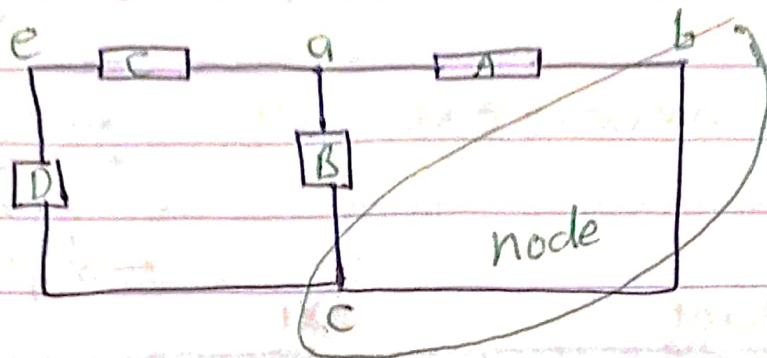
$$V_2 = +(-3)(2) = -6 \text{ V}$$

$$V_3 = -I_3(4) = -52 \text{ V}$$

$$\text{Energy} = P \cdot \Delta t$$

$$= 2 \times 3 = 6 \text{ W}$$

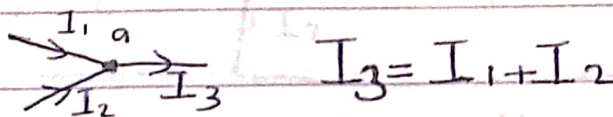
* KCL (Kirchhoff's Current Law)



* node

هي النقطة التي يلتقي فيها أكثر من element

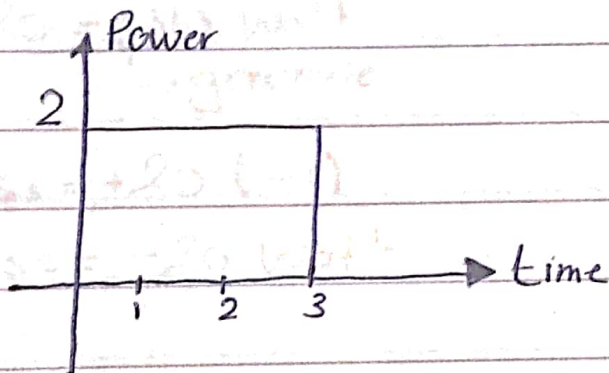
* \sum التيارات الداخلة = node أي خلافتي أي التيارات الخارجة



* Power \rightarrow watt (w)

$$E_{\text{energy}} = \int_0^{\Delta t} P(t) dt$$

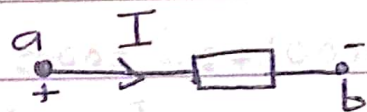
(Joule)



$$E_{\text{energy}} = P \cdot \Delta t$$

$$= 2 \times 3 = 6 \text{ Kw.h}$$

$$* P = V \cdot I$$

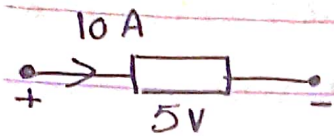


$$P = +VI$$

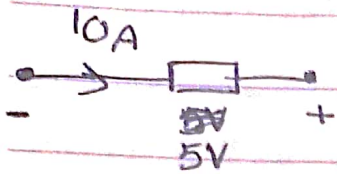
إذا تيار داخل موجب

$$P = -VI$$

إذا تيار دخل سالب

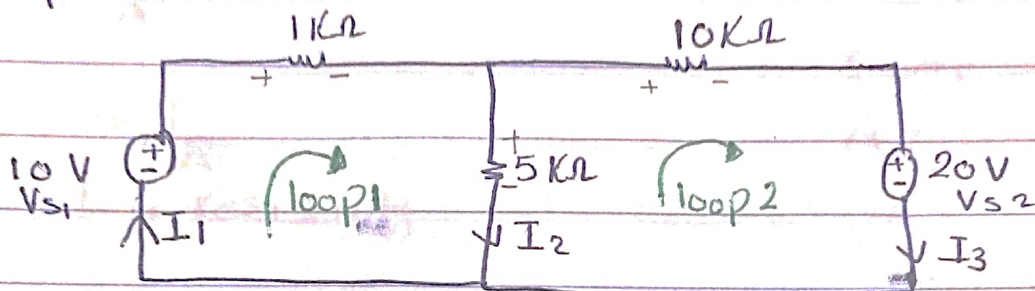


$$P = +10 \times 5 = 50 \text{ watt (absorbs, consumes Power)}$$



$$P = -10 \times 5 = -50 \text{ watt (generates, delivers, produce power)}$$

* Example \rightarrow



- find ① power absorbed/generated in V_{s1} and V_{s2}
 ② power absorbed by $5k\Omega$

$$\textcircled{1} P = +VI$$

$$P_{s1} = -1 \times 10$$

$$P_{s1} = -10 \text{ watt}$$

\hookrightarrow generate

$$P_{s2} = +20(-1)$$

$$P_{s2} = -20 \text{ watt}$$

$$-10 + I_1(1k) + I_2(5k) = 0$$

$$-I_2(5k) + I_3(10k) + 20 = 0$$

$$I_1 = I_2 + I_3$$

$$-10 + (I_2 + I_3)1000 + 5000I_2 = 0$$

$$20 - 5000I_2 + 10000I_3 = 0$$

$$-10 + 6000I_2 + 1000I_3 = 0$$

$$20 - 5000I_2 + 10000I_3 = 0$$

$$100 - 60000I_2 - 10000I_3 = 0$$

$$20 - 5000I_2 + 10000I_3 = 0$$

$$120 - 65000I_2 = 0$$

$$I_2 = 2 \text{ mA}$$

$$I_3 = -1 \text{ mA} / I_1 = 1 \text{ mA}$$

$$\textcircled{2} P_{5k\Omega} = I^2 R$$

$$= (2)^2 \times 5k$$

$$= +20 \text{ watt}$$

* Resistance \rightarrow

Cross section area (A) = πR^2

$$R = \rho \frac{L}{A}$$

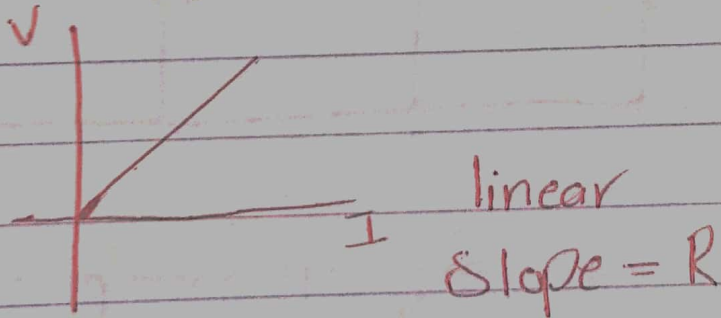
ρ resistivity

word = Ω

* The resistance absorbs power ($P > 0$)

* Ohm's law \rightarrow

$$V = IR$$



* Conductivity

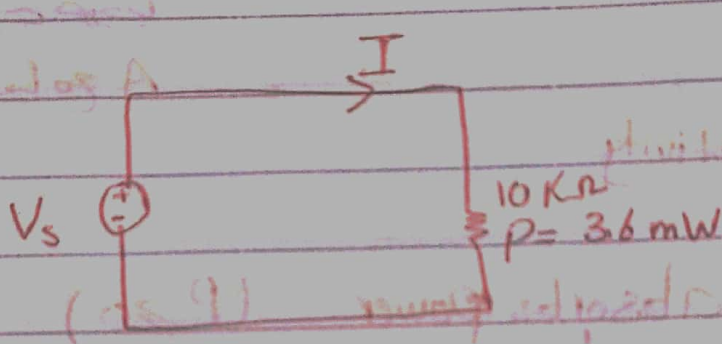
$$G = \frac{1}{R} \quad (\text{S/V})$$

$$* P = VI = \frac{V^2}{R} = RI^2$$

* Short and open Circuits

- ↳ infinite resistance ($I=0$)
- ↳ a device with zero resistance ($V=0$)

* The power absorbed by the $10\text{-k}\Omega$ resistor in the following circuit is 3.6 mW . Determine the voltage and the current.



$$P = I^2 R$$

$$3.6 = I^2 \times 10$$

$$I^2 = \frac{3.6}{10}$$

$$I = 0.6\text{ mA}$$

$$V = IR$$

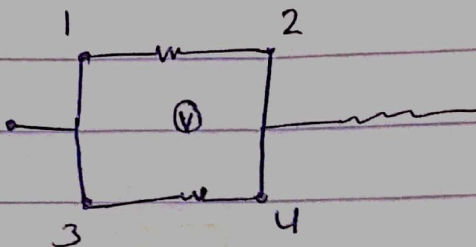
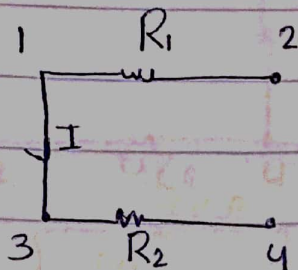
$$V = 6 \times 10^{-4} \times 10$$

$$V = 6\text{ V}$$

* Connection between Resistance →

① Series

② parallel (//)



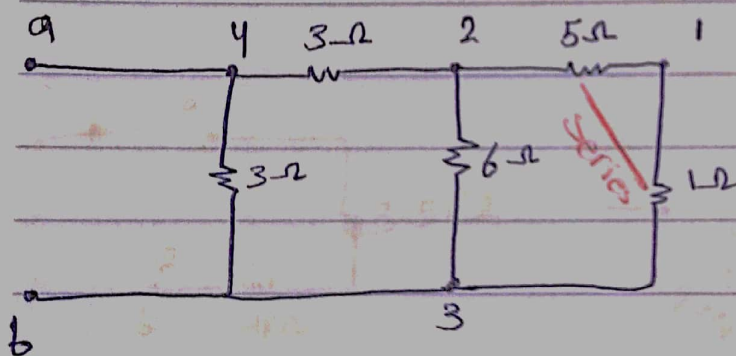
فقط من طرف واحد
مشتركين

$$R_{eq} = R_1 + R_2$$

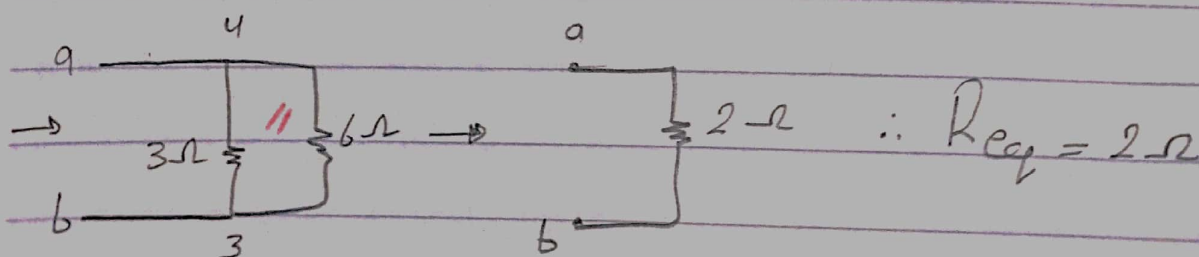
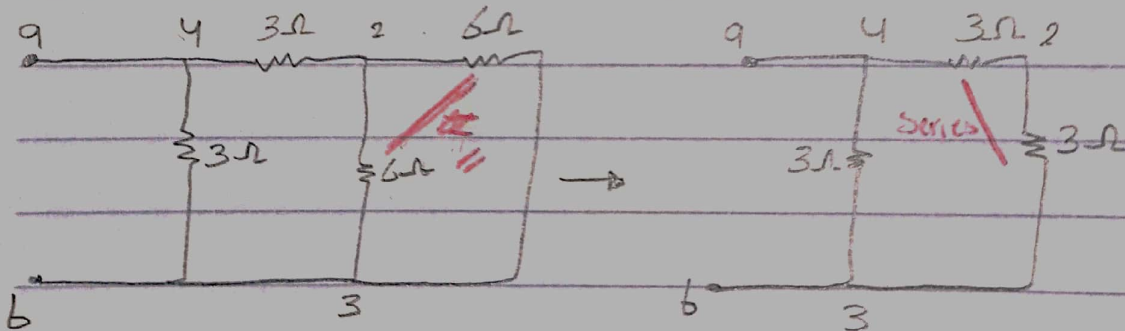
$$R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

* equivalent Resistance

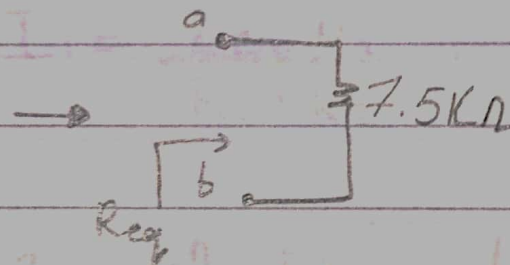
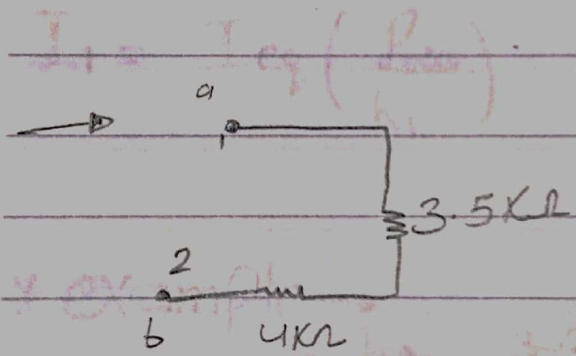
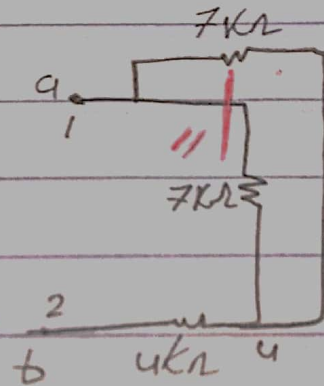
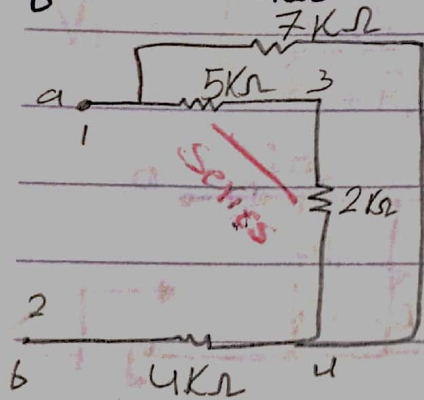
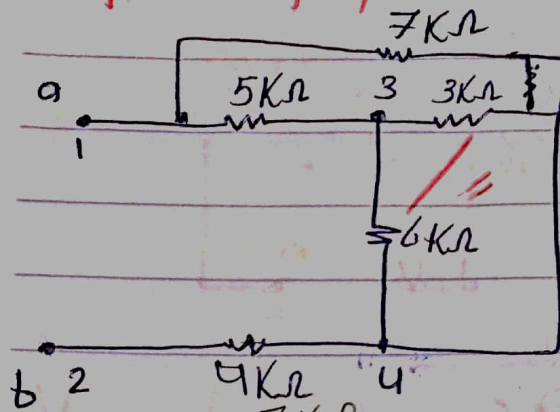
$$= \frac{R_1 R_2}{R_1 + R_2}$$



find Req

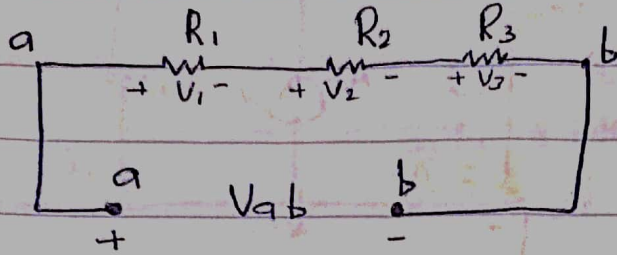


* Past paper (2019)

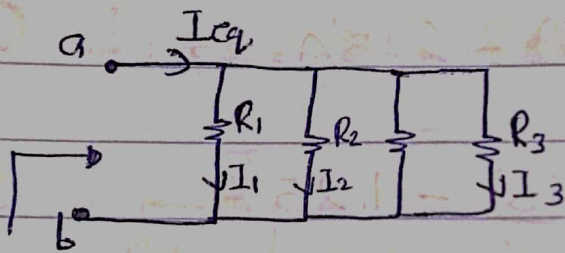


* Voltage division, Current division

Series



$$V_1 = \left(\frac{V_{ab}}{R_1 + R_2 + R_3} \right) R_1$$

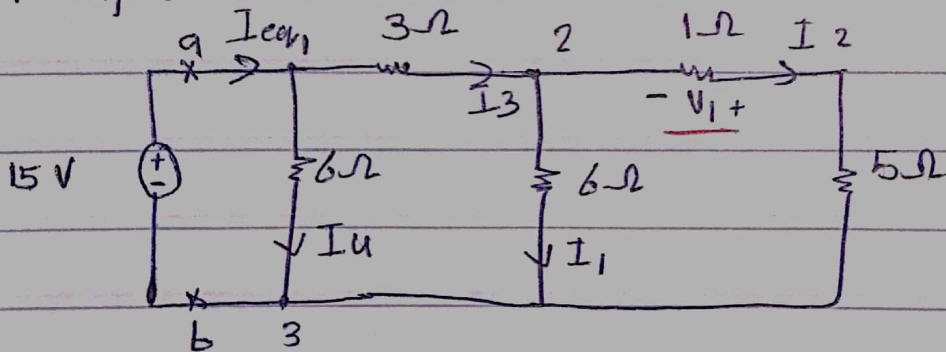


$$I_1 = I_{eq} \left(\frac{R_{eq}}{R_1} \right)$$

for 2 resistance

$$I_1 = \frac{I_{eq} R_2}{R_1 + R_2}$$

* example →



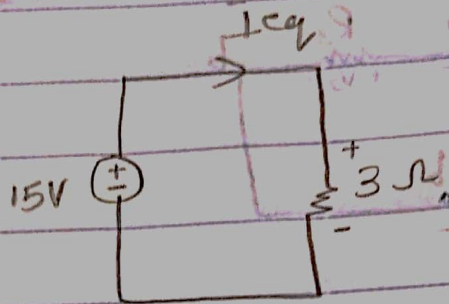
find \$I_{eq}\$ and
 \$I_1\$ and
 power absorbed
 by \$5\Omega\$ and \$V_1\$

$$R_{eq} = 3 \Omega$$

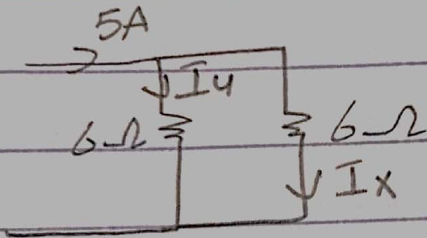
$$\textcircled{1} V = IR$$

$$15 = +I \times 3$$

$$I = +5A$$



$\textcircled{2}$



$$I_x = \frac{5(6)}{12} = 2.5A = I_x$$

$$I_1 = \frac{2.5(6)}{12} = 1.25A$$

$$\textcircled{3} P = I^2 R$$

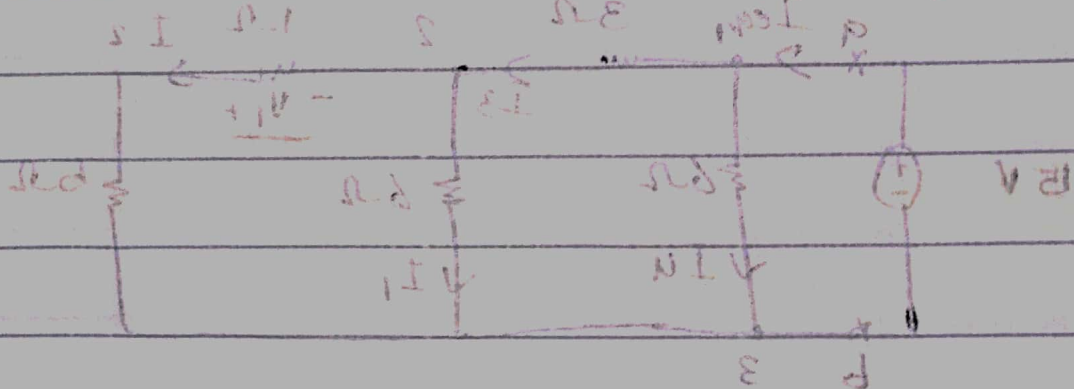
$$= (1.25)^2 \times 5$$

$$= 12.5 \text{ watt}$$

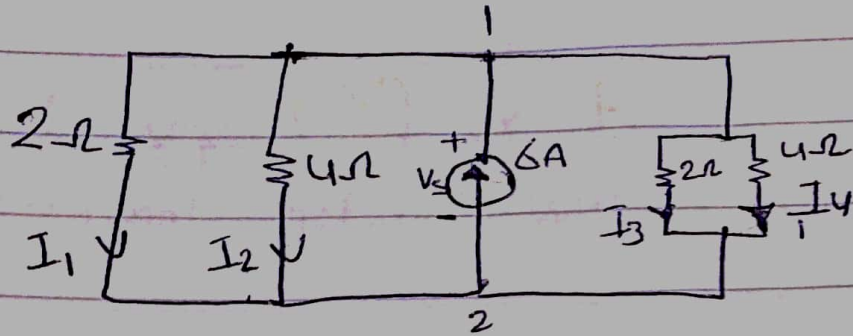
$$\textcircled{4} V_1 = -IR$$

$$= -1.25 \times 1$$

$$= -1.25V$$



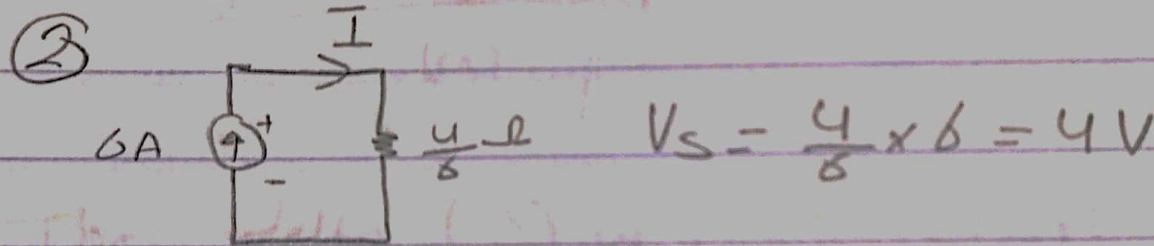
* example →



find I_1 and the power generated by the current source

$$R_{eq} = \frac{4}{6} \Omega$$

$$\textcircled{1} \quad I_1 = \frac{6 \left(\frac{4}{6} \right)}{2} = 2A$$



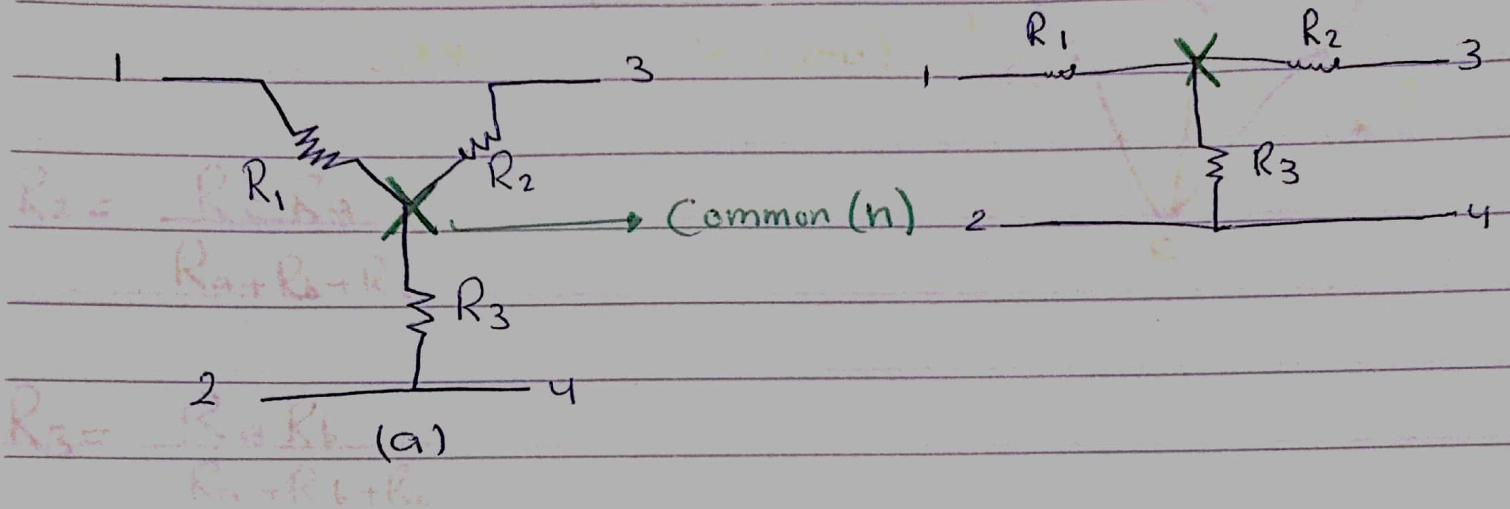
$$P = \pm VI$$

$$= -VI$$

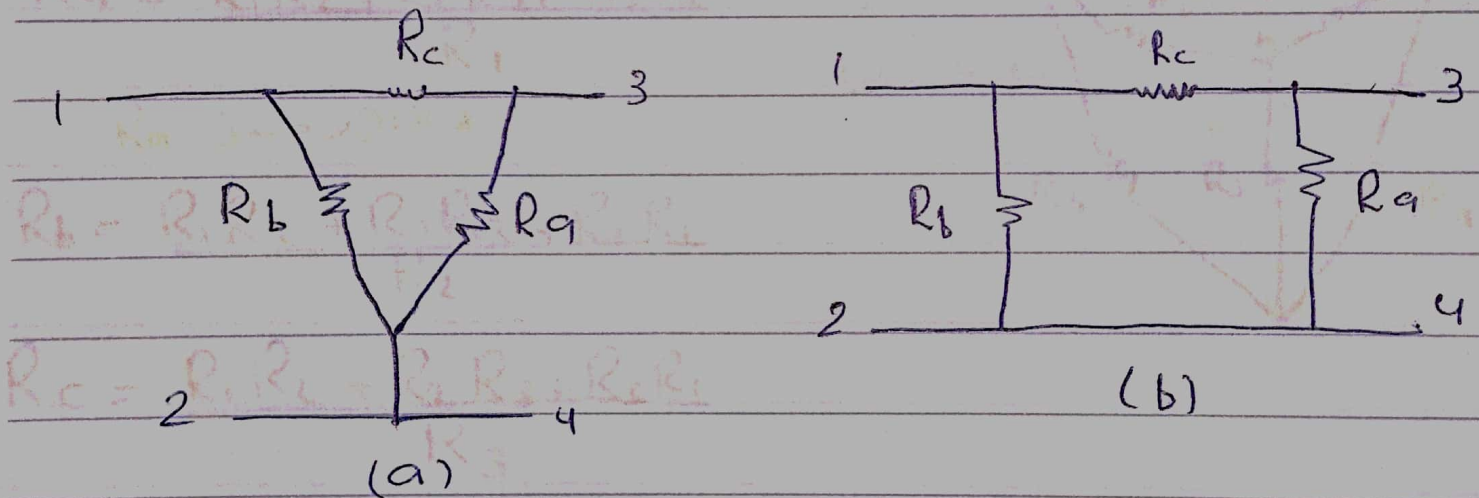
$$= -4(6) = -24 \text{ watt}$$

* Wye and Delta Networks →

• A wye (Y) or Tee (T) network is a three-terminal network with the following general form:



• The delta (Δ) or Pi (Π) network has the following general form:

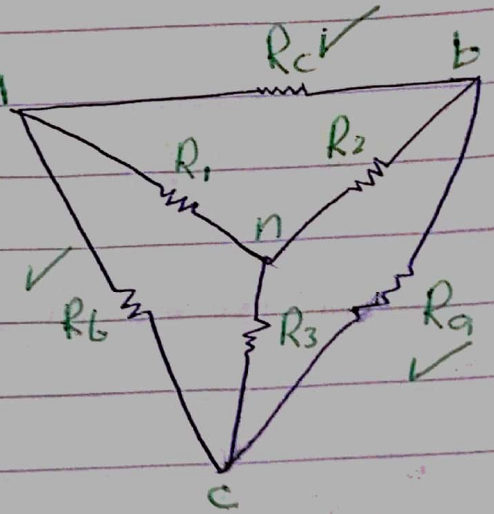


* Delta - Wye conversion

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

→ (ما يصل بين المقاومتين التي تأتيين مع المقاومة R_1)

دالة مجموع (مجموع مقادير Delta)



$$R_2 = \frac{R_c R_a}{R_a + R_b + R_c}$$

$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

* Wye - Delta conversion

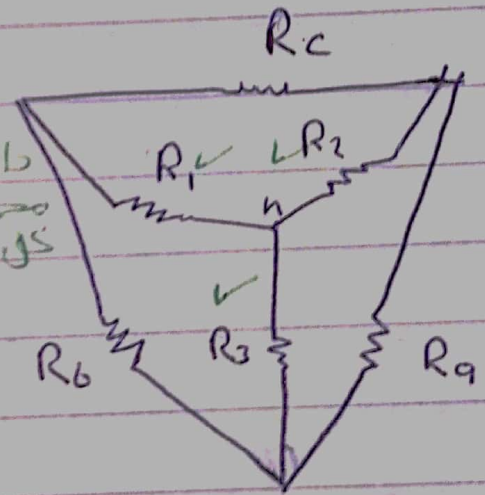
$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

دالة حاصل مجموع ضربين كل مقادير

له البيرة عن R_a

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$



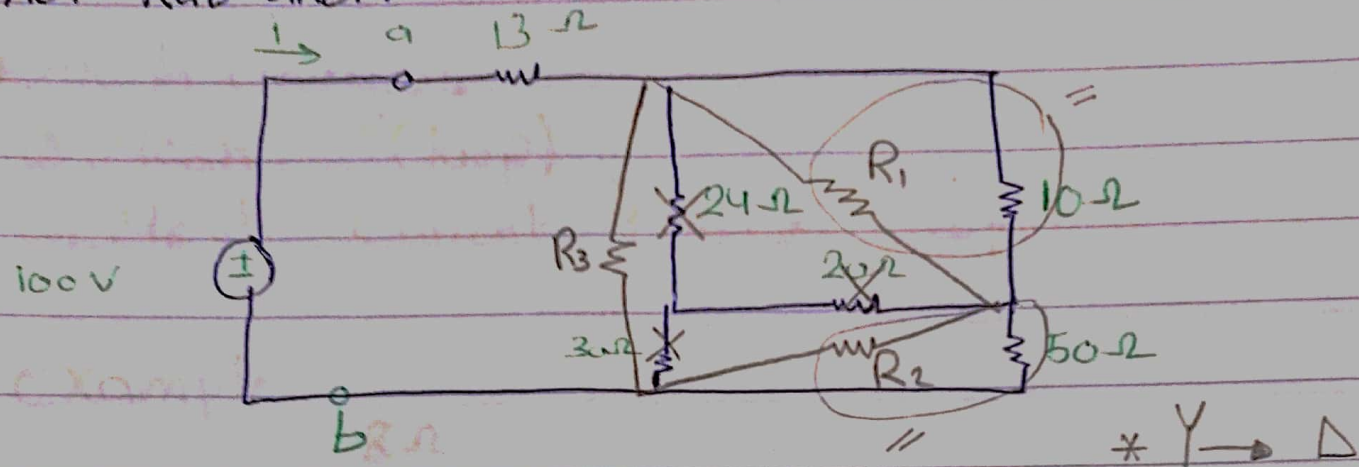
* Y and Δ networks are said to be balanced when :

$$R_1 = R_2 = R_3 = R_Y \text{ and } R_a = R_b = R_c = R_\Delta$$

* For balanced Y and Δ networks the conversion formulas become :

$$R_Y = \frac{R_\Delta}{3} \text{ and } R_\Delta = 3R_Y$$

* example: for the following bridge network find R_{ab} and i.



$$R_1 = \frac{20 \times 24 + 24 \times 30 + 20 \times 30}{30} = 60 \quad \rightarrow \text{نقطة اللمة}$$

$$R_2 = \frac{20 \times 24 + 24 \times 30 + 20 \times 30}{24} = 75$$

$$R_3 = \frac{20 \times 24 + 24 \times 30 + 20 \times 30}{20} = 90$$

* $(R_3 \parallel (R_1 \parallel 10\Omega + R_2 \parallel 50\Omega))$ Series with 13Ω

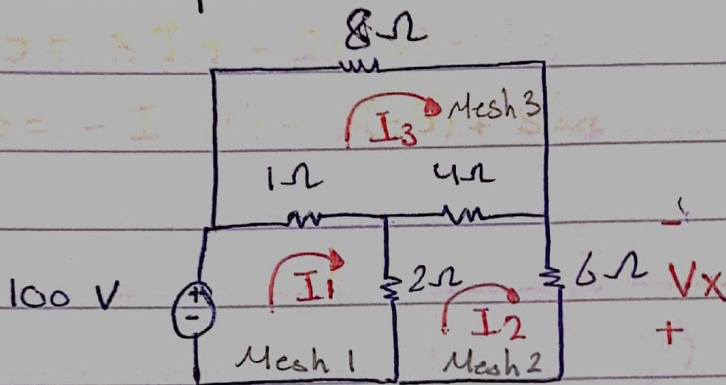
* Chapter "3" →

* Mesh analysis

① Mesh (loop)

② Mesh Current (قسطور الجهد)

* Example



4 loops / 3 Meshes

$$-100 + 1(I_1 - I_3) + 2(I_1 - I_2) = 0 \quad \text{from Mesh 1}$$

$$3I_1 - 2I_2 - I_3 = 100 \quad \text{--- (1)}$$

$$4(I_2 - I_3) + 6I_2 + 2(I_2 - I_1) = 0 \quad \text{from Mesh 2}$$

$$-2I_1 + 12I_2 - 4I_3 = 0 \quad \text{--- (2)}$$

$$8I_3 + 4(I_3 - I_2) + 1(I_3 - I_1) = 0 \quad \text{from Mesh 3}$$

$$-I_1 - 4I_2 + 13I_3 = 0 \quad \text{--- (3)}$$

* Inspection →

Mesh 1

$$+I_1(3) - I_2(2) - I_3(1) = 100$$

Mesh 2

$$-I_1(2) + I_2(12) - I_3(4) = 0$$

$$\text{Mesh 3} \rightarrow -I_1(1) - I_2(4) + I_3(13) = 0$$

$$* V_x = I_x R$$

$$V_x = -I_x(6)$$

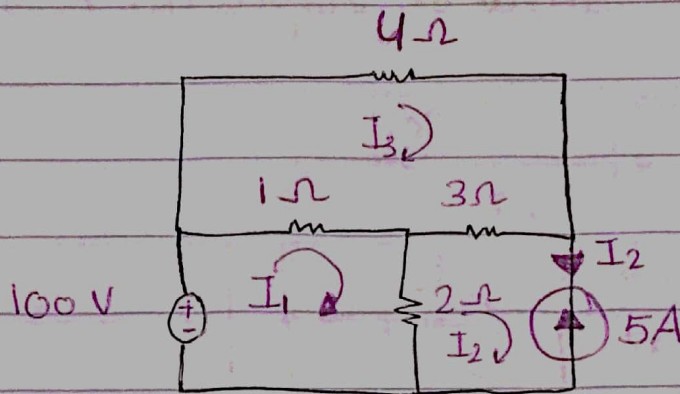
* Power in 2Ω

$$P = I^2(2)$$

$$P = (I_1 - I_2)^2(2) \text{ watt}$$

* Mesh \Rightarrow KVL

* C.S



$$I_2 = -5A$$

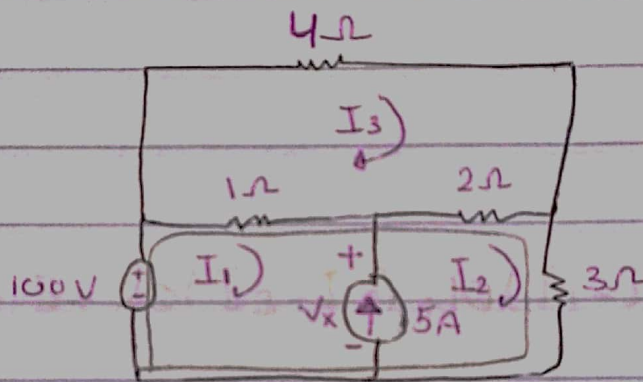
لأنه متجه

$$100 = 3I_2 - 2(-5) - I_3$$

$$0 = -I_1(1) - 3(-5) + 8I_3$$

* لا تطبق طريقة Mesh

في حال وجود C.S



$$5 = I_2 - I_1$$

$$\text{Mesh 3} \rightarrow -I_1 - 2I_2 + 7I_3 = 0$$

* في الحل الذي loop لا يأخذ Current Source وتطبق KVL

(Super Mesh)

$$-100 + 1(I_1 - I_3) + 2(I_2 - I_3) + 3I_2 = 0$$

OR

$$-100 + 4I_3 + 3I_2 = 0 \rightarrow \text{loop ظاهري}$$

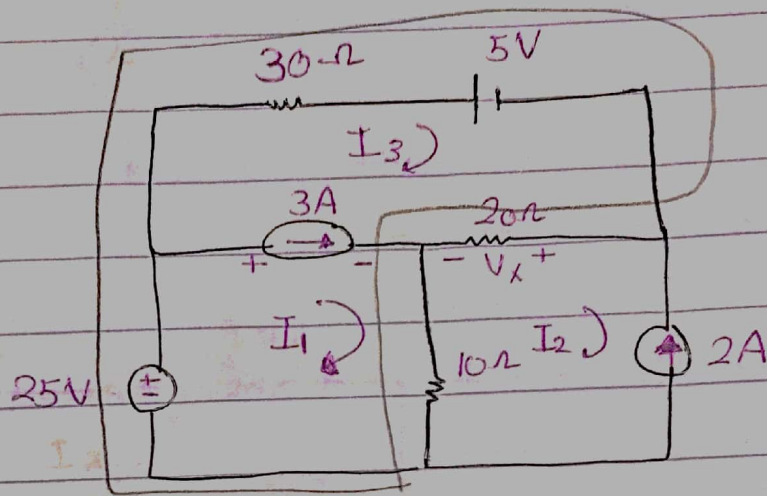
* power delivered / consumed in the current source

$$P = \pm V \cdot I = -V \cdot I = -5V_x$$

$$\rightarrow -100 + 1(I_1 - I_3) + V_x = 0$$

*Past paper

Use Mesh analysis to write the mesh equations



$$I_2 = -2A$$

$$I_1 - I_3 = 3$$

KVL (loop)

$$-25 + 30I_3 + 5 + 20(I_3 - I_2) + 10(I_1 - I_2) = 0$$

$$-20 - 40 + 20 = 50I_3 + 10I_1$$

$$-40 = 50I_3 + 10I_1$$

$$-40 = 50I_3 + 10(3 + I_3)$$

$$I_1 = 3 - \frac{7}{6}I_3$$

$$I_2 = -2$$

$$I_3 = -\frac{7}{6}$$

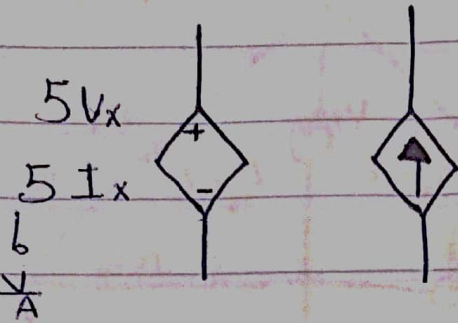
$$* V_x = -20(I_x) \quad * P_{3A} = VI$$

$$= -20(I_2 - I_3) \quad = +3V_y$$

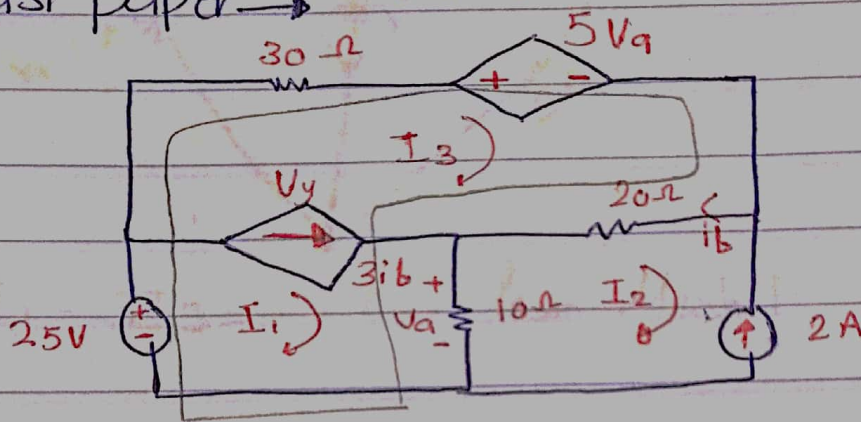
$$\hookrightarrow -25 + V_y + 10(I_1 - I_2) = 0$$

* Dependent Source

element کی تیار



* Past paper



$$I_2 = -2A$$

$$3i_b = I_1 - I_3$$

$$i_b = I_3 - I_2$$

$$3(I_3 - I_2) = I_1 - I_3$$

$$4I_3 - 3I_2 - I_1 = 0$$

$$4I_3 - I_1 = -6$$

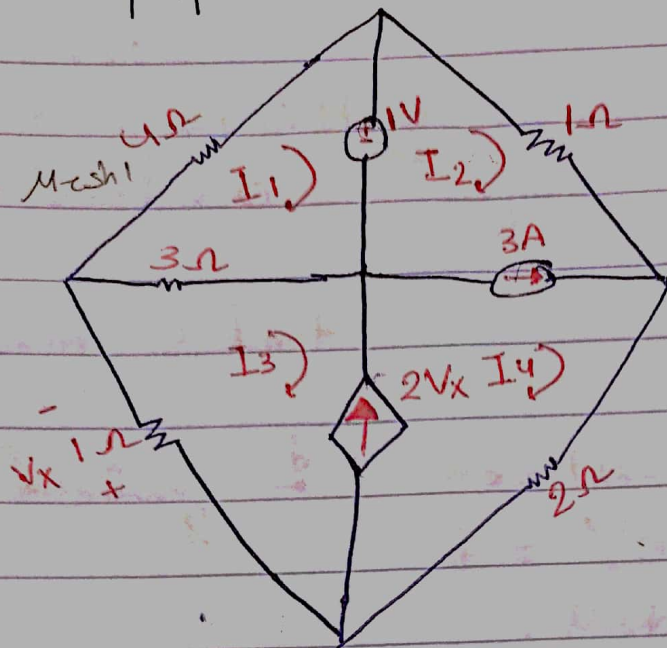
$$-25 + 30I_3 + 5V_a + 20(I_3 - I_2) + 10(I_1 - I_2) = 0$$

$$* V_a = + (I_1 - I_2)(10)$$

$$* P_{3i_b} = + V_y (3i_b)$$

$$\begin{matrix} \text{L} \\ \text{L} \end{matrix} \quad -25 + V_y + 10(I_1 - I_2) = 0$$

* past paper



$$7I_1 - 3I_3 = -1 \quad \text{from Mesh 1}$$

$$3 = I_4 - I_2 \quad \text{--- (2)}$$

$$2V_x = I_4 - I_3$$

$$2(+I_3(1)) = I_4 - I_3$$

$$2I_3 = I_4 - I_3$$

$$I_4 - 3I_3 = 0 \quad \text{--- (3)}$$

$$I_3 + 4I_1 + I_2 + 4I_4 = 0 \quad \text{--- (4)}$$

* Nodal analysis

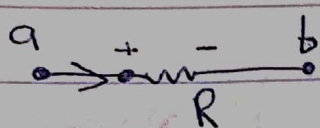
* Nodes

* KCL \Rightarrow Voltage

* $V_{ref} = 0$

$$\underline{I} = V = 0$$

$$\sum I_{in} = \sum I_{out}$$



$$V_{ab} = V_a - V_b = +IR$$

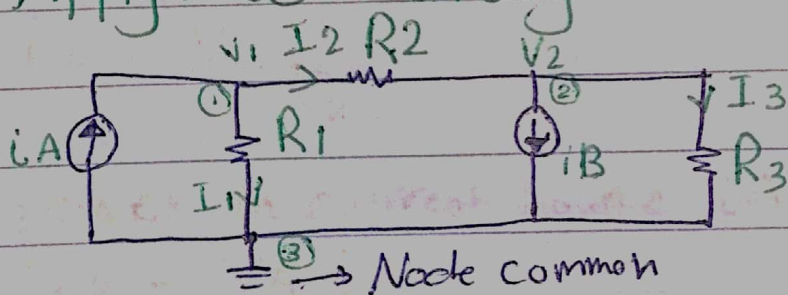
$$I = \frac{V_a - V_b}{R}$$

* جميع التيارات تكون Node out من Node R

$$* \frac{I}{R} = G(V, S)$$

$$I = G(V_a - V_b)$$

* Apply Nodal analysis to write Nodal equations.



at node 1 $\Rightarrow \frac{V_1 - V_3}{R_1} + \frac{V_1 - V_2}{R_2} = iA$

$$V_1 \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - V_2 \left(\frac{1}{R_2} \right) - V_3 \left(\frac{1}{R_1} \right) = iA$$

$\hookrightarrow = 0$

at node 2

$$\frac{V_2 - V_1}{R_2} = \frac{V_2 - V_3}{R_3} + i_B = 0$$

$$V_2 \left(\frac{1}{R_2} + \frac{1}{R_3} \right) - \frac{V_1}{R_2} + i_B = 0$$

* inspection

Current source i_B *
source

at node 1

$$+ V_1 \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - V_2 \left(\frac{1}{R_2} \right) - V_3 \left(\frac{1}{R_1} \right) = i_A$$

at node 2

$$- V_1 \left(\frac{1}{R_2} \right) + V_2 \left(\frac{1}{R_2} + \frac{1}{R_3} \right) + \frac{V_3}{3} + i_B = 0$$

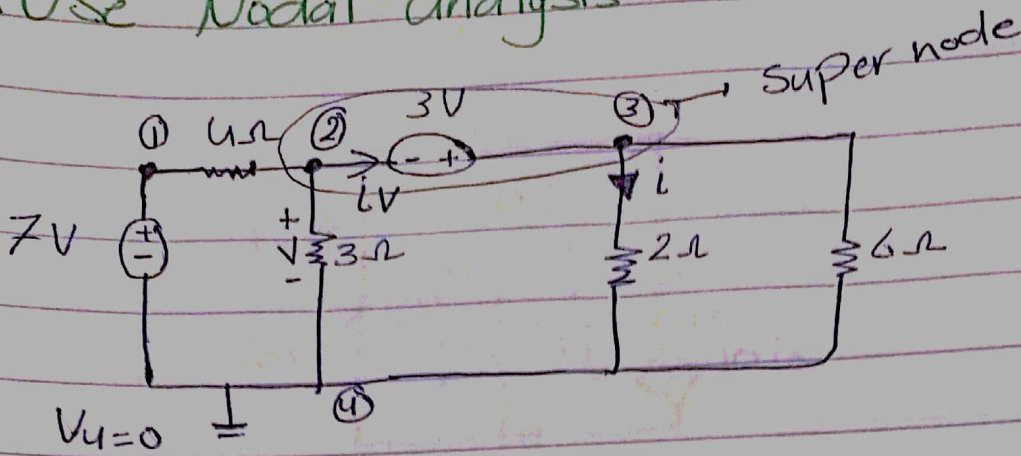
$$* i_2 = \frac{V_1 - V_2}{R_2}$$

* Power in current source i_A

$$P = - V_A i_A$$

$$= - (V_1 - V_3) i_A$$

*Use Nodal analysis



$$7 = V_1 - V_4$$

$$\boxed{V_1 = 7V}$$

$$3 = V_3 - V_2 \quad \text{--- (1)}$$

at node 2

$$-V_1 \left(\frac{1}{4} \right) + V_2 \left(\frac{1}{4} + \frac{1}{3} \right) + iV = 0$$

at node 3

$$iV = +V_3 \left(\frac{1}{2} + \frac{1}{6} \right)$$

$$-\frac{V_1}{4} + V_2 \left(\frac{1}{4} + \frac{1}{3} \right) + V_3 \left(\frac{1}{2} + \frac{1}{6} \right) = 0 \quad \text{--- (2)}$$

$$V_2 = -0.2V \quad V_3 = 2.8V$$

$$\textcircled{1} V = ??$$

$$V = V_2 = -0.2V$$

$$\textcircled{2} i = \frac{V_3 - V_4}{2} = 1.4A$$

③ Power in 7V

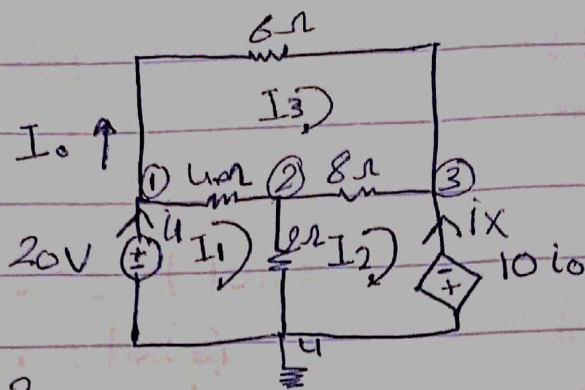
$$P = \pm VI = \pm 7I = -7I_1$$

$$I_1 = \frac{V_1 - V_2}{4} = \frac{7.2}{4}$$

$$P = -7 \times \frac{7.2}{4} \text{ watt}$$

(generate)

* Use Nodal analysis



at node 2

$$-V_1 \left(\frac{1}{4} \right) + V_2 \left(\frac{1}{4} + \frac{1}{8} + \frac{1}{2} \right) - V_3 \left(\frac{1}{8} \right) = 0$$

$$-\frac{V_1}{4} + V_2 \left(\frac{7}{8} \right) - \frac{V_3}{8} = 0 \quad \text{--- (1)}$$

$$V_1 - V_4 = 20$$

$$\boxed{V_1 = 20V}$$

$$40 = 7V_2 - V_3 \quad \text{--- (1)}$$

عند فرض V_1 في (1)

$$10 i_0 = V_4 - V_3$$

$$-V_3 = 10 i_0 \quad \text{--- (2)}$$

$$I_0 = \frac{V_1 - V_3}{6}$$

$$-V_3 = 10 \left(\frac{V_1 - V_3}{6} \right)$$

$$-6V_3 = 10V_1 - 10V_3$$

$$40 = 7V_2 - 50$$

$$4V_3 = 10V_1$$

$$V_2 = \frac{92}{7} V$$

$$V_3 = 50V$$

* find the power in the dependent source and independent

$$P_{ind} = -i_1 (20)$$

KCL

$$\Rightarrow i_1 = V_1 \left(\frac{1}{4} + \frac{1}{8} \right) - V_2 \left(\frac{1}{4} \right) - V_3 \left(\frac{1}{8} \right)$$

$$P_{dep} = + (-i_2) (10i_o)$$

$$= + i_x (10i_o)$$

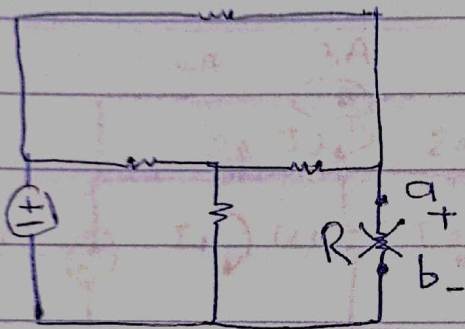
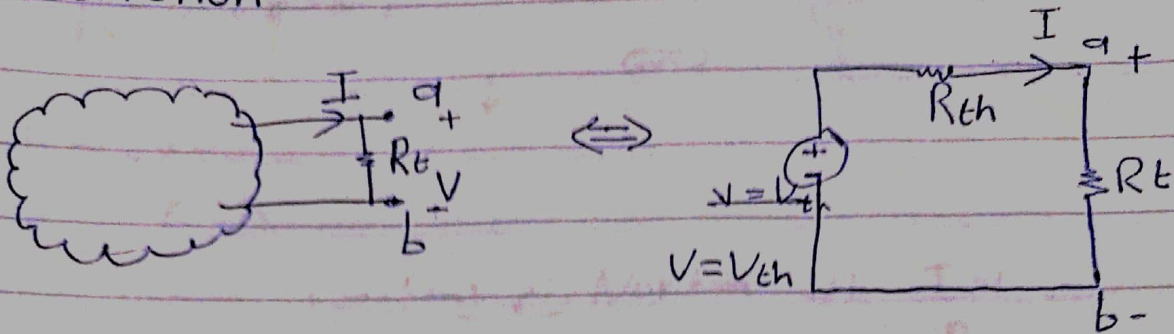
$$\hookrightarrow \frac{V_1 - V_3}{8}$$

$i_x \Rightarrow$ KCL

$$i_x = V_3 \left(\frac{1}{8} + \frac{1}{8} \right) - V_2 \left(\frac{1}{8} \right) - V_1 \left(\frac{1}{8} \right)$$

* Thevenin Eq. CKT

* Reduction



* لا يطلب V_{th}
 لا يزال السؤال يطرح
 القيمة التي اطرح فيها
 لو كان في R فتساها
 ورجب سالتنا
 open circuit

$R_{th} = R_{eq}$ Seen a.b

Kill all the Sources

independent Source

يكون
يسا له

* V.S \Rightarrow zero \Rightarrow S.C

* C.S \Rightarrow O.C
 open circuit

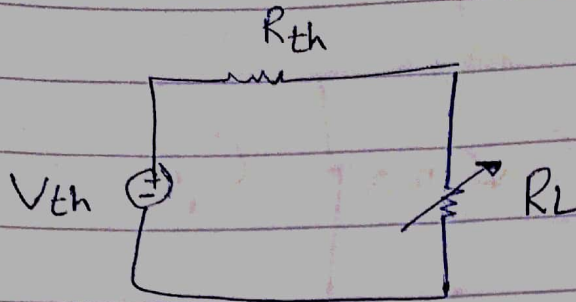
* $L = \text{eff} = \frac{P_{out}}{P_{in}} < 1$

* $P_{in} = P_{lost} + P_{R_{th}}$

* $P_{loss} = I^2 R_{th}$

وخط سالتنا wire ليس، \rightarrow خط سالتنا \rightarrow ليس

* Maximum power transfer



$$P = I^2 R$$

$$P_{RL} = \left(\frac{V_{th}}{R_{th} + R_L} \right)^2 R_L$$

$$I \rightarrow \max$$

$$f(x) = x \dots$$

$$\frac{df(x)}{dx} = 0 \rightarrow x$$

$$\frac{dP}{dR_L} \Rightarrow R_L$$

⊗ R_L ؟؟

① $P_{RL} = \max$

② $P_{transfer}$ from the source max

③ $P_{loss} = \min$

كل ما نضبطه
التي

$$R_L = R_{th}$$

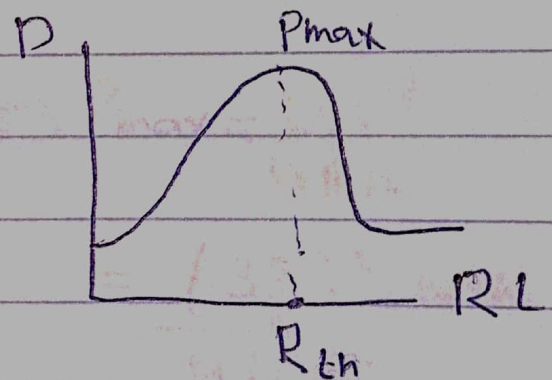
$$P_{max} = \left(\frac{V_{th}}{R_{th} + R_{th}} \right)^2 R_{th}$$

$$P_{max} = \frac{V_{th}^2}{4R_{th}}$$

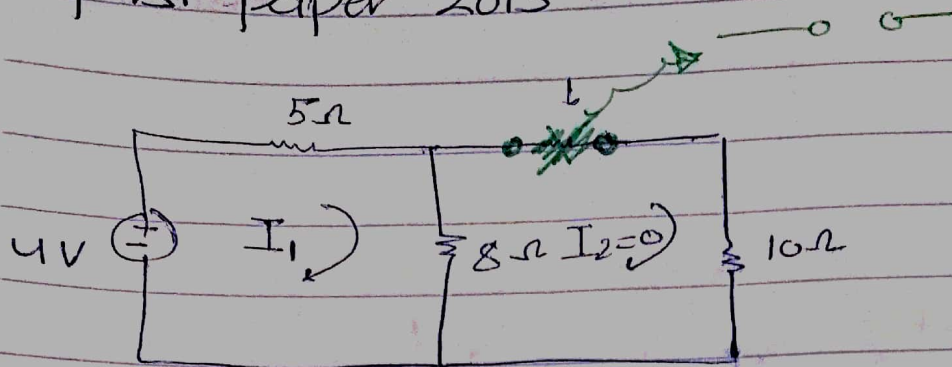
القانون
النقطة

$$R_L = R_{th}$$

$$P_{RL} = \max$$



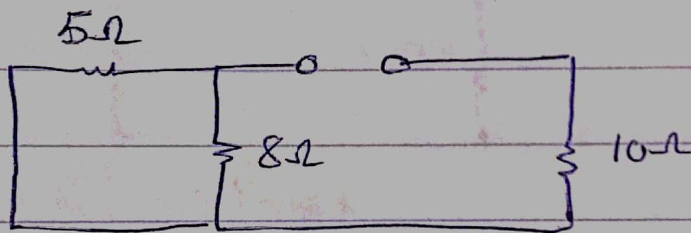
* Past Paper 2013



(A) Select a value for R_L to absorb Max Power from the CKT?

(B) V_{th} (C) P_{max} (D) $R_L = 10\Omega \Rightarrow P_{RL}??$

(a) $R_L = R_{th}$



$$5 \parallel 8 \Rightarrow \frac{5 \times 8}{5 + 8} = \frac{40}{13} \Omega$$

$$10 + \frac{40}{13} = R_{th}$$

$$R_L = R_{th} = 13\Omega$$

(b) $I_1 = \frac{4}{13} A$

$$+V_{o.c} - 8\left(\frac{4}{13}\right) = 0$$

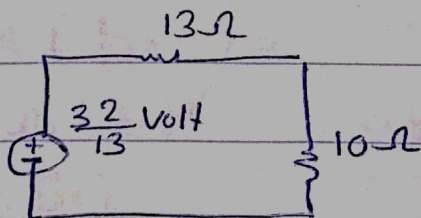
$$V_{o.c} = \frac{32}{13} \text{ Volt} = V_{th}$$

(c) $P_{max} = \frac{V_{th}^2}{4R_{th}}$

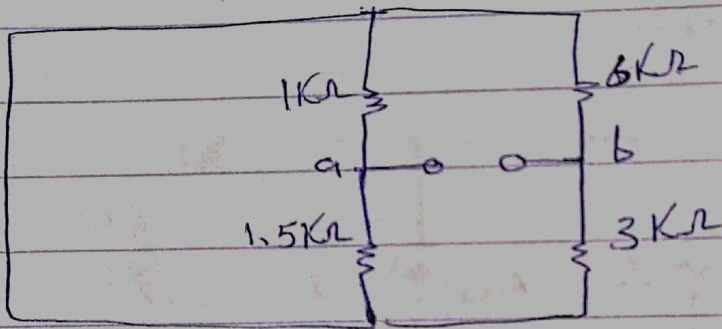
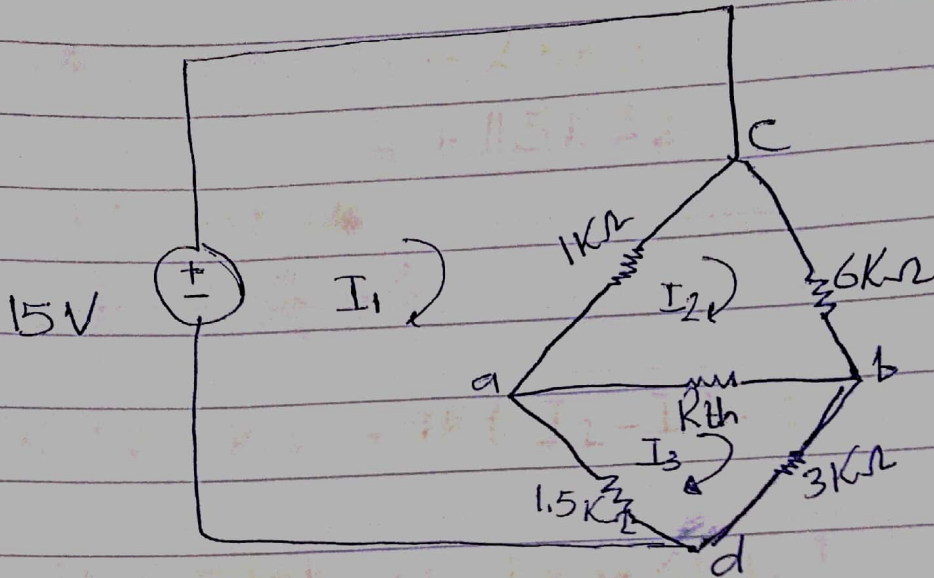
$$= \frac{\left(\frac{32}{13}\right)^2}{4(13)} \text{ watt}$$

$$P_{10\Omega} = I^2(10)$$

$$= \left(\frac{\frac{32}{13}}{13+10}\right)^2 \times 10 \text{ watt}$$



*example

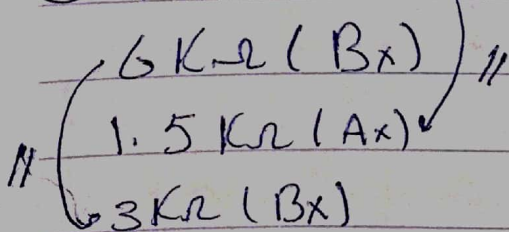


a) $R_L \Rightarrow P_{max}$

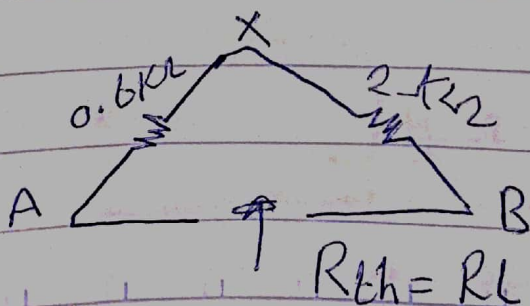
b) P_{max}

c) If the voltage source is replaced with a current source 15A

a) $1k\Omega (Ax)$ $\frac{1 \times 1.5}{1 + 1.5} = 0.6k\Omega (Ax)$



$\frac{6 \times 3}{6 + 3} = 2k\Omega (Bx)$



$R_L = R_{th} = 2 + 0.6 = 2.6k\Omega$

$$\textcircled{b} P_{\max} = \frac{V_{th}^2}{4R_{th}}$$

$$15 = 2.5K I_1 - 2.5K I_2$$

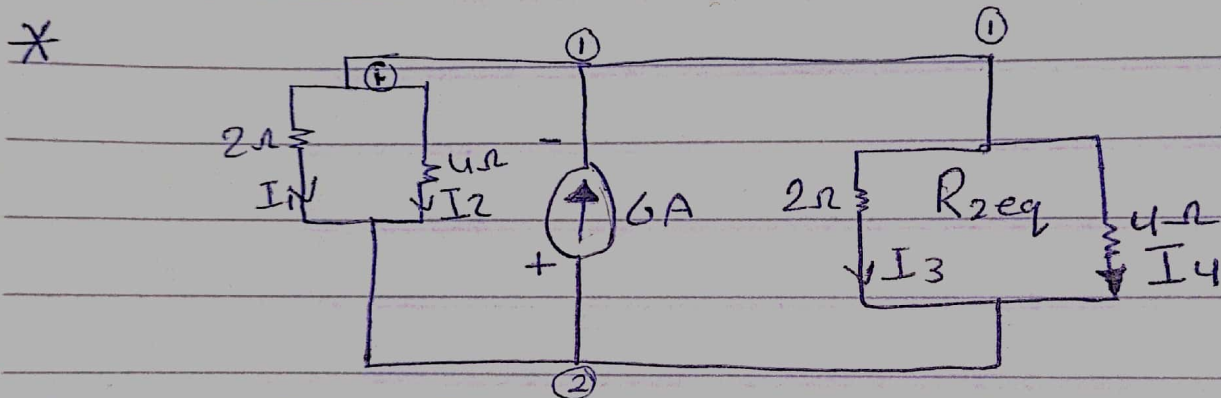
$$0 = -2.5K I_1 + 11.5K I_2$$

$$18 = 9K I_2$$

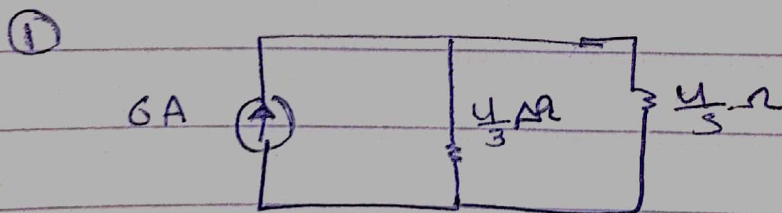
$$I_2 = \frac{5}{3} \text{ mA}$$

$$6K I_2 - V_{oc} + 1K(I_2 - I_1) = 0$$

$$V_{oc} = V_{th} \Rightarrow P_{\max} = \frac{V_{th}^2}{4R_{th}}$$



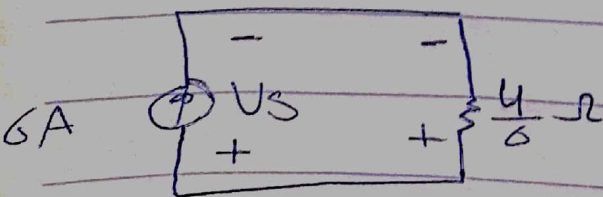
Find ① I_1 ② power generated by the current source



$$I_1 = 6 \left(\frac{4}{8} \right) = 2 \text{ A}$$

$$\textcircled{2} R_{eq} = \frac{4}{6} \Omega$$

$$V_s = \frac{4}{6} \times 6 = 4 \text{ V}$$



$$P = + V_s (6) = 24 \text{ W}$$