

Chapter 1 **DC**: due to linear function of time referring to charges.

current = $\frac{dq}{dt} = A$ $\rightarrow \frac{dq}{dt} = \alpha = \frac{\Delta q}{\Delta t}$ $I = \frac{\Delta q}{\Delta t}$

charge = $\int_0^t i(t) dt = c = \text{number of electrons} \times \text{electron charge}$

Voltage

$V_{ab} = \frac{dW}{dq} = \frac{\Delta W}{\Delta q}$ $\rightarrow W$: energy in joules. **knowing that**

$V_{ab} = (V_a - V_b) \rightarrow$ lowest polarity, highest polarity

Power

$P = \frac{dW}{dt} = \text{watts} = \text{rate}$

$\Delta W = P \Delta t \rightarrow$ it can be taken by hours for unit (Wh)

$P = i(t) \cdot v(t) = \text{Instantaneous}$

$W = \int P dt$

Passive Sign convention

- i through, $(+)$ term
- $\rightarrow +i \cdot v = P$
- $+P$: absorbed by element.
- $-P$: supplied by element.
- i through, $(-)$ term
- $\rightarrow -i \cdot v = P$
- $+P$: absorbed.
- $-P$: supplied.

law of conservation of energy

total supplied power = total absorbed power

$\sum_{k=1}^n P_k = 0 \rightarrow k$ is an element.

$(y - y_0)$ slope $(x - x_0)$

Chapter (2)

① $R = \frac{V}{i}$ → Voltage $V = +iR$ (through +ve term)
 $V = -iR$ (" -ve term).

Basic Resistance

Note :- short circuit + open circuit are described in my notebook.

② $R = \frac{\rho L}{A}$

↳ Conductance :- $G = \frac{1}{R} = S$.

22 problem

Power (dissipated) by a resistor :-

$$P = +i \cdot v = i^2 R = \frac{v^2}{R}$$

KCL + current source replacement :-

$$\sum I_n = \sum I_{out} \rightarrow \text{remember } I = \frac{V}{R}$$

Replacement use kcl to replace currents in parallel (revise notebook)
↓
sources.

KVL + voltage source replacement :-

$$\sum V_k = 0 \rightarrow \text{remember } v = iR. \text{ (take care of passive sign convention)}$$

Replacement use kvl to replace (revise notebook).

Series Resistors :-

→ The current stays the same for them all ✓
(all resistors)

→ ① Apply (KVL) to determine how it goes ✓ (it gives V_{eq})

→ ② $R_{eq} = R_1 + R_2 + \dots + R_n$

Then ① $i = \frac{V}{R_{eq}}$

Then ② $V_1 = \pm i \cdot R = \frac{R_1}{R_{eq}} V$

$V_2 = \pm i \cdot R = \frac{R_2}{R_{eq}} V$

Voltage divider rule

Parallel Resistors :-

→ The voltage stays the same for them all ✓
(all resistors)

→ You can apply (KCL) to see more details.

$$\rightarrow \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}$$

$$\text{then } R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$

A special case when

$N=2$

$$\rightarrow R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{R_1 R_2}{R_1 + R_2}$$

Using Conductance :-

$$G_k = \frac{1}{R_k} \rightarrow G_{eq} = \frac{1}{R_{eq}}$$

$$G_{eq} = G_1 + G_2 + \dots + G_n$$

Then we substitute that:-

$$i_k = \frac{\frac{1}{R_k} \cdot i}{\frac{1}{R_{eq}}} = \frac{G_k \cdot i}{G_{eq}}$$

↓
for a
branch

The current divider rule

A special case when $N=2$:-

$$i_1 = \frac{R_2}{R_1 + R_2} \cdot i$$

$$i_2 = \frac{R_1}{R_1 + R_2} \cdot i$$

So :-

i_1 is $\propto \frac{1}{R_1}$ and $\propto R_2$

i_2 is $\propto \frac{1}{R_2}$ and $\propto R_1$

→ See the open and short circuits in the note book ✓

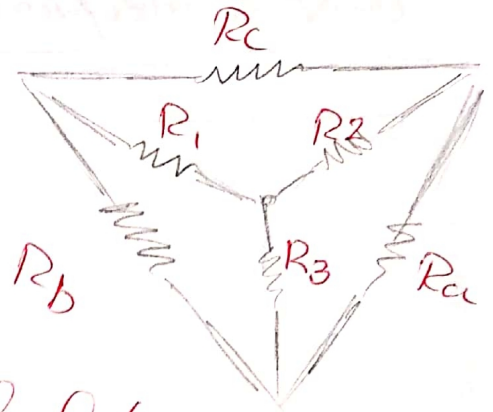
Delta - Wye Connections :-

∇ -Y conversion:-

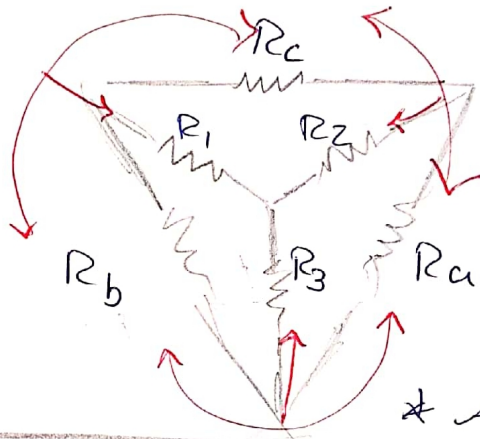
$$① R_1 = \frac{R_b \cdot R_c}{R_a + R_b + R_c}$$

$$② R_2 = \frac{R_a \cdot R_c}{R_a + R_b + R_c}$$

$$③ R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$



So you can find it this way :-



* And for a special case:-

A Balanced ∇ connection
 $R_a = R_b = R_c = R$
 So you have a balanced Y connection:-
 $R_1 = R_2 = R_3 = \frac{R}{3}$ ✓

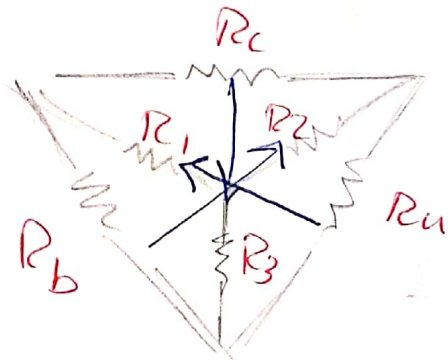
Y- ∇ conversion:-

$$R_a = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_2}$$

$$R_c = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_3}$$

→ The Trick:-



chapter 3

[1] Nodal Analysis

- select reference node.
- ~~assign~~ assign voltages v_1, v_2, v_3 .
- Apply KCL to nonreference nodes.
(ohm's law applied.)
- solve equations. ($Av=b$)

[2] Nodal Analysis with voltage sources.

[case 1] → voltage source connected between reference and nonreference node. (put nonreference to voltage source)

[case 2] → Apply KVL to super node.

- then treat super node wire with anything in parallel with it, and then continue as usual.

[3] Mesh Analysis.

- assign mesh currents
- Apply KVL / Ohm's law applied.
- Solve equations $AI=b$

[4] Mesh Analysis with current sources.

[case 1] I source only in one mesh → set mesh current to current source. consider directions

[case 2] I source between 2 meshes. (supermesh)

Exclude the current source and any elements connected in series with it.

*Cramer's Rule:
Example $Av=b$
 $\text{Det}(A)=X$
 $v_i = \frac{\text{Det}_i}{\text{Det}(A)}$ (replace b in i 's column)
 $v_2 = \frac{\text{Det}_2}{\text{Det}(A)}$ (replace b in 2nd column)
 $\text{Det}(A)$

Linear property:-

function of transformation:-

to be linear:-

$$T\{\alpha_1 x_1(t) + \alpha_2 x_2(t)\} = \alpha_1 T\{x_1(t)\} + \alpha_2 T\{x_2(t)\}.$$

For:- $T\{i(t)\} = R \cdot i(t).$

→ linear circuit:-

output is linearly related to its input.

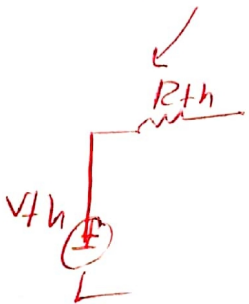
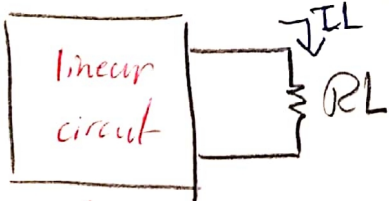
Superposition principle:-

principle of killing sources:-

- ① Turn off all sources, except one, and find the required thing.
- ② repeat it for all sources
- ③ find total.

Thevenin Theorem

steps of finding R_{th} and V_{th} is in the notebook.



$$I_L = \frac{V_{th}}{R_{th} + R_L}$$

$$V_L = \frac{R_L}{R_L + R_{th}} \cdot V_{th}$$

Chapter 4 Analyzing circuit with each independent source
OR POSITION acting alone, then use algebraic sum.

⊙ - voltage sources are replaced by (short circuit)
 - current sources are replaced by (open circuit).

⊕ Dependent sources are left intact.

Chapter 4

Source Transformation

replacing a voltage source in series with R by current source in parallel with R
 and vice versa.

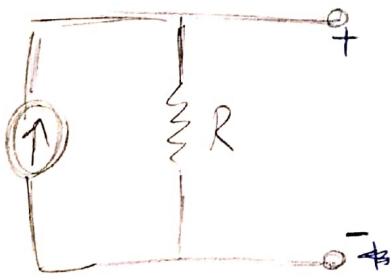
$$\left. \begin{aligned} U_s &= I_s R \\ I_s &= \frac{U_s}{R} \end{aligned} \right\} \text{for transformation.}$$

→ Applicable for independent and dependent sources.

Remember

→ we can combine 2 voltage sources additionally in series.
 → we can combine 2 current sources additionally in parallel.

Open Circuit

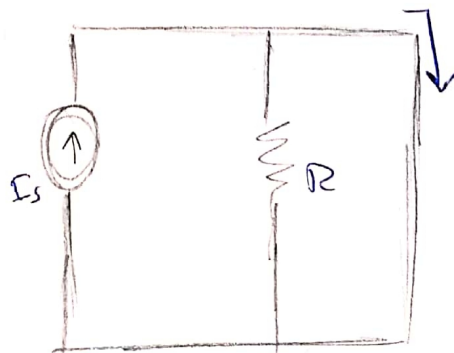


$$I_{op} = 0$$

$$V_{op} = U_s$$

$$U_s = I_s R$$

Short Circuit



$$I_{sh} = I_s$$

$$V_{sh} = 0$$

$$V_s = I_s R$$

Chapter 6 summarization:-

§ 6.2 : capacitors (open circuits to dc)
voltage cannot change suddenly.

Basic

→ How to find capacitance:-

$$C = \frac{q}{V} \quad \text{or} \quad C = \frac{\epsilon d}{A} \quad \begin{matrix} (A \text{ of one plate}) \\ (q \text{ " " "}) \end{matrix}$$

C is measured in Farad = 1 coulomb / volt.

① i through a capacitor:-

$$i = \frac{C \, dv}{dt} \rightarrow \text{you'll find } i(t) / \text{function of } t \text{ until they give you } t$$

② $v(t)$ of capacitor:-

$$v(t) = \frac{1}{C} \int_{t_0}^{+} i(\tau) \, d\tau + v(t_0) \\ = \frac{1}{C} \int_{t_0}^{+} i(t) \, dt + v(t_0)$$

[Power and Energy:-

* Power

$$\rightarrow p(t) = i(t) \cdot v(t)$$

$$P(t) = C \frac{dv(t)}{dt} \cdot v(t)$$

* Energy stored in capacitor:

$$\rightarrow w = \frac{1}{2} C v^2$$

convert using $C = \frac{q}{V}$

$$\rightarrow \text{or } w = \frac{1}{2} \frac{q^2}{C}$$

voltage-division rule (capacitors in series)

$$v_1 = \frac{C_2}{C_1 + C_2} v_S, \quad v_2 = \frac{C_1}{C_1 + C_2} v_S$$

current-division rule (capacitors in parallel)

$$i_1 = \frac{C_1}{C_1 + C_2} i_S, \quad i_2 = \frac{C_2}{C_1 + C_2} i_S$$

:-
to do
only.

→ How to find capacitance:-

$$C = \frac{q}{V} \quad \text{or} \quad C = \frac{\epsilon d}{A} \quad \begin{matrix} (A \text{ of one plate}) \\ (q \text{ " " "}) \end{matrix}$$

C is measured in Farad = 1 coulomb / volt.

① → i through a capacitor:-

$$i = c \frac{dv}{dt} \rightarrow \text{you'll find } i(t) / \text{function of } t \text{ until they give you } t$$

② → $v(t)$ of capacitor:-

$$v(t) = \frac{1}{c} \int_{t_0}^+ i(\tau) d\tau + v(t_0) \\ = \frac{1}{c} \int_0^+ i(t) dt + v(t_0)$$

[Power and Energy:-

* Power

$$\rightarrow p(t) = i(t) \cdot v(t)$$

$$P(t) = c \frac{dv(t)}{dt} \cdot v(t)$$

* Energy stored in capacitor:

$$\rightarrow w = \frac{1}{2} c v^2$$

convert using $c = \frac{q}{v}$

→ Series and parallel ~~resistors~~ capacitors:

~~Parallel resistors:~~

→ Parallel capacitors:

$$C_{eq} = C_1 + C_2 + C_3 + C_4$$

→ they share same voltage:

→ charge is distributed.

→ Series capacitors:

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \frac{1}{C_4}$$

→ they share same q

→ voltage is distributed.

special:

for $N=2$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} \quad \equiv \quad C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

Inductors: - a short circuit for dc.
→ current cannot change suddenly.

Basics: -

→ Inductance: $L = \frac{N^2 \mu A}{l}$

⊙ voltage: $v = L \frac{di}{dt}$

⊙ current $i = \frac{1}{L} \int_{t_0}^t v(t) dt + i(t_0)$

for special case:

$t_0 = -\infty \rightarrow i(t_0) = 0$

Then $i(t) = \frac{1}{L} \int_{-\infty}^t v(t) dt = \frac{1}{L} \left[\int_{-\infty}^t v(t) dt + \int_0^t v(t) dt + i(t_0) \right]$

power and energy: -

→ $p = vi = \left(L \frac{di}{dt} \right) i$

series + parallel
are like resistors

→ $w = \frac{1}{2} Li^2$

We say under dc conditions, then:

$w_e = \frac{1}{2} CV^2 / w_L = \frac{1}{2} Li^2$

✓ voltage division principle (inductors in series)

$$v_1 = \frac{L_1}{L_1 + L_2} \times v_S, \quad v_2 = \frac{L_2}{L_1 + L_2} v_S$$

for dc.
? slowly.

Current division principle (inductors in parallel)

$$i_1 = \frac{L_2}{L_1 + L_2} i_S, \quad i_2 = \frac{L_1}{L_1 + L_2} i_S$$

⊖ voltage: $v = L \frac{di}{dt}$

⊖ current $i = \frac{1}{L} \int_{t_0}^t v(t) dt + i(t_0)$

for special case:

$$t_0 = -\infty \rightarrow i(t_0) = 0$$

$$\text{Then } i(t) = \frac{1}{L} \int_{-\infty}^t v(t) dt = \frac{1}{L} \left[\int_{-\infty}^0 v(t) dt + \int_0^t v(t) dt \right]$$

power and energy:-

$$\rightarrow p = w \dot{i} = \left(L \frac{di}{dt} \right) i$$

series + parallel
are like resistors

$$\rightarrow w = \frac{1}{2} L i^2$$

we say under dc conditions, then:

$$w_c = \frac{1}{2} C v^2 / w_L = \frac{1}{2} L i^2$$

Chapter 7

First Order
Circuit

a circuit characterized by a first-order differential Equation.

First order circuit \leftrightarrow 1st ODE \equiv RC / RL circuits.

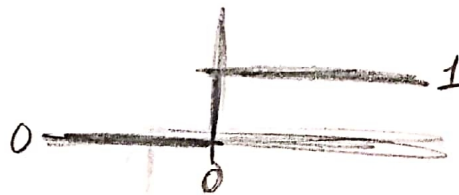
1st ODE $\begin{cases} \rightarrow \text{Homo} \\ \rightarrow \text{NonHomo (external force / source of power incl. current)} \end{cases}$

Unit Step Function - [Singularity Functions]

* We use it to model Electric circuits with switches.

* we'll be interested in the case $t > 0$

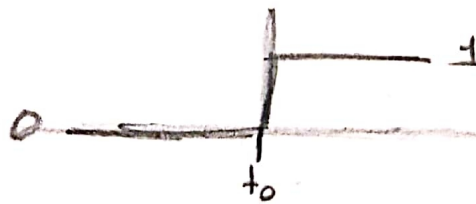
$$u(t) = \begin{cases} 1, & t > 0 \\ 0, & t < 0 \end{cases}$$



$$u(t) = \begin{cases} 1, & t < 0 \\ 0, & t > 0 \end{cases}$$



$$u(t-t_0) = \begin{cases} 1, & t > t_0 \\ 0, & t < t_0 \end{cases}$$



$$u(t-2) \rightarrow$$



$$u(t+2) \rightarrow$$



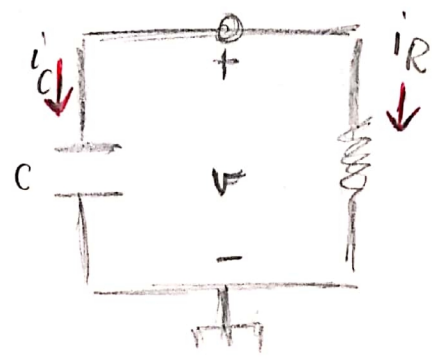
source-free RC Circuit

Objective: Determine circuit response.

starting from the initially charged capacitor.

→ $v(0) = v_0$
 → $w(0) = \frac{1}{2} C v_0^2$

v cannot change suddenly,
 nothing restricts i to do so



After disconnecting DC source:-

circuit response:-

① $v(t) = v_0 e^{-t/RC}$

→ for which $v(t) = v_0 e^{-t/\tau}$

$RC = \tau$ (time constant).

Notes:-

→ response is only due to the initial energy stored and the circuit characteristics, with no external excitations. (Natural response)

time constant:-

the time required for the response to decay to a factor of 1/e or 36.8 percent of its initial value.

Notes:-

- ① it takes 5τ for the circuit to reach its final ~~value~~ ^{state}, or steady state, when no changes take place with time.
- ② But at any constant time small or large the circuit reaches the steady state at 5τ
- ③ The smaller τ , the more rapidly voltage decrease (faster response), and vice versa

② $i_R(t) = \frac{v(t)}{R} = \frac{v_0}{R} e^{-t/\tau}$

resistor response

③ $P_R(t) = v i_R = \frac{v_0^2}{R} e^{-2t/\tau}$

Note that P_{eq} voltage

④ $w_R(t) = \frac{1}{2} C v_0^2 (1 - e^{-2t/\tau})$

is the same equation above

Target:-

→ get $v_c(t)$ so you can find i_c , v_R , i_R .

keys:-

- initial voltage across C is $v(0) = v_0$
- time constant τ

Source-free RL circuit

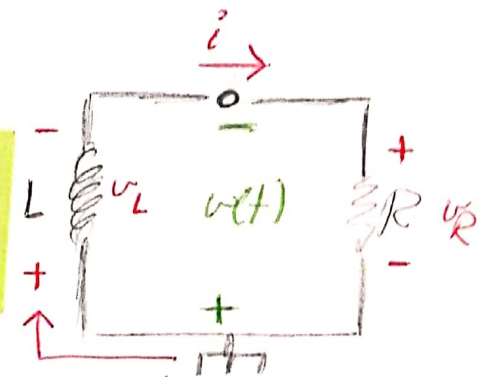
Objective: Determine circuit response.

starting from the initially have a current.

$i(0) = I_0$

$w(0) = \frac{1}{2} L I_0^2$

i cannot change suddenly, nothing restricts *v* to do so



We always assume that *i*(*t*) enters through positive terminal of the inductor.

After disconnecting DC source:-

circuit response :-

$i(t) = I_0 e^{-t/\tau}$ for which $\tau = \frac{L}{R}$ (time constant)

Response of R_{eq} , Note that the current is the same above.

$v_R(t) = iR = I_0 R e^{-t/\tau}$

but $v_L(t) = -I_0 R e^{-t/\tau}$

$P_R(t) = v_R i = I_0^2 R e^{-2t/\tau}$

$w_R(t) = \frac{1}{2} L I_0^2 (1 - e^{-2t/\tau})$

Notes :-

- 1) The smaller the τ , the faster the rate of decay of response.
- 2) At any rate, the response decays to less than 1 percent of its initial value after 5τ .

Note that $(v_L = -v_R)$ for same level RL circuit ($v_L(t) = -L \frac{di}{dt}$) different directions of polarity + current

Target:-

→ get $i(t)$ so you can find (v_L, v_R, i_R)

keys:-

- initial current through L is $i(0) = I_0$
- time constant τ .



Step-Response of RC circuit

Note:- the step response of a circuit is its behavior when the excitation is the step function, which may be a voltage or a current source.

Non-Homogeneous:-

remember:

$v(t)$ must be continuous because capacitor will resist any abrupt change in its voltage.

21 April
min 35

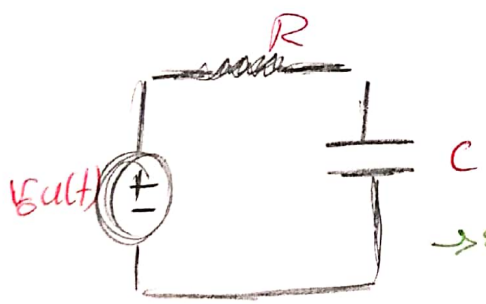
In order to analyze step response RC circuits, you need to:-

1] find v_0 ($t < 0$)

2] find $v(\infty)$ ($t > 0$)

$v(\infty)$ is v of capacitor after $t > 0$

3]



find $\tau = RC$

→ steady state shape.

such that = $\begin{cases} v_0, & t < 0 \end{cases}$

$$\left(v(0) - v(\infty) \right) e^{-t/RC} + v(\infty), \quad t > 0$$

Step-Response of RL circuit

Non-Homogeneous.

remember:-

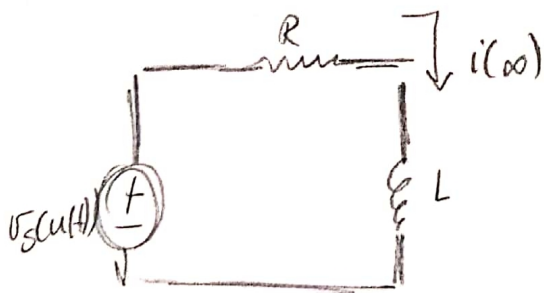
$i(t)$ must be continuous, because inductor will resist any abrupt change in its current.

In order to analyze step response RL circuits, you need to:-

[1] find $i(0) / t < 0$

[2] find $i(\infty) / t > 0$

[3] find $\tau = \frac{L}{R}$



$$\text{such that } = \begin{cases} i(0), & t < 0 \\ i(\infty) + [i(0) - i(\infty)] e^{-t/\tau} \end{cases}$$