# COMPUTER AND NETWORI SECURITY 

Jonathan Katz

Modified by: Dr. Ramzi Saifan

## "SECURITY"

- Most of computer science is concerned with achieving desired behavior
- Security is concerned with preventing undesired behavior
- Different way of thinking!
- An enemy/opponent/hacker/adversary who is actively and maliciously trying to circumvent any protective measures you put in place


## ONE ILLUSTRATION OF THE DIFFERENCE

- Software testing determines whether a given program implements a desired functionality
- Test I/O characteristics
- Q/A
- How do you test whether a program does not allow for undesired functionality?
- Penetration testing helps, but only up to a point


## SECURITY IS INTERDISCIPLINARY

- Draws on all areas of CS
- Theory (especially cryptography)
- Networking
- Operating systems
- Databases
- AI/learning theory
- Computer architecture/hardware
- Programming languages/compilers
- HCI, psychology


## FORTUNATELY, WE ARE WINNING THE SECURITY BATTLE

- Strong cryptography
- Firewalls, intrusion detection, virus scanners
- Buffer overflow detection/prevention
- User education


## REALLY??!



## Top 50 Products By Total Number Of "Distinct" Vulnerabilities in 2017

Go to year: $1999 \underline{2000} \underline{2001} \underline{2002} \underline{2003} \underline{2004} \underline{2005} 2006 \underline{2007} 2008 \underline{2009} 2010 \underline{2011} 2012 \underline{201 \Xi}$ Time Leaders

|  | Product Name | Vendor Name | Product Type | Number of Vulnerabilities |
| ---: | :--- | :--- | :--- | :--- | :--- |
| 1 | Android | $\underline{\text { Google }}$ | OS | $\underline{842}$ |
| 2 | Linux Kernel | $\underline{\text { Linux }}$ | OS | $\underline{453}$ |
| 3 | $\underline{\text { Iphone Os }}$ | $\underline{\text { Apple }}$ | OS | $\underline{387}$ |
| 4 | $\underline{\text { Imagemagick }}$ | $\underline{\text { Imagemagick }}$ | Application | $\underline{357}$ |
| 5 | Mac Os X | $\underline{\text { Apple }}$ | OS | $\underline{299}$ |
| 6 | Windows 10 | $\underline{\text { Microsoft }}$ | OS | $\underline{268}$ |
| 7 | $\underline{\text { Windows Server 2016 }}$ | $\underline{\text { Microsoft }}$ | OS | $\underline{252}$ |
| 8 | $\underline{\text { Windows Server 2008 }}$ | $\underline{\text { Microsoft }}$ | OS | $\underline{243}$ |
| 9 | Windows Server 2012 | $\underline{\text { Microsoft }}$ | OS | $\underline{235}$ |
| 10 | Debian Linux | $\underline{\text { Debian }}$ | OS | $\underline{230}$ |
| 11 | $\underline{\text { Windows 7 }}$ | $\underline{\text { Microsoft }}$ | OS | $\underline{229}$ |
| 12 | Windows 8.1 | $\underline{\text { Microsoft }}$ | OS | $\underline{225}$ |

source: https://www.cvedetails.com/top-50-products.php?year=2017

# VULNERABLE APPLICATIONS BEING EXPLOITED 



Source: Kaspersky Security Bulletin 2017

## PHILOSOPHY OF THIS COURSE

- We are not going to be able to cover everything
- We are
- Main goa You will not be a security expert after this class
- A samp (after this class, you should realize why it
- The sed would be dangerous to think you are)
- Becom
 "buzzworde" (nhiahiner
- Becom
- Try to 1 You should have a better appreciation of security, project issues after this class


## Course Organization

## a naive view

- Computer security is about CIA:
- Confidentiality, integrity, and availability
- These are important, but security is about much more...


## A NAİVe VIEW



## IN REALITY...

- Where does security end?



## ONE GOOD ATT'ACK

- Use public records to figure out someone's password
- Or, e.g., their SSN, so can answer security question...
- The problem is not (necessarily) that SSNs are public
- The problem is that we "overload" SSNs, and use them for more than they were intended


## A NAÏVE VIEW

" Achieve "absolute" security

## IN REALITY...

- Absolute security is easy to achieve!
- How...?
- Absolute security is impossible to achieve!
- Why...?
- Good security is about risk management


## SECURITY AS A TRADE-OFF

- The goal is not (usually) "to make the system as secure as possible"...
" ...but instead, "to make the system as secure as possible within certain constraints" (cost, usability, convenience)
- Must understand the existing constraints
- E.g., passwords...


## COST-BENEFIT ANALYSIS

- Important to evaluate what level of security is necessary/appropriate
- Cost of mounting a particular attack vs. value of attack to an adversary
- Cost of damages from an attack vs. cost of defending against the attack
- Likelihood of a particular attack
- Sometimes the best security is to make sure you are not the easiest target for an attacker...


## "MORE" SECURITY NOT ALWHYS BETTER

- "No point in putting a higher post in the ground when the enemy can go around it"
- Need to identify the weakest link
- Security of a system is only as good as the security at its weakest point...
- Security is not a "magic bullet"
- Security is a process, not a product


## COMPUTER SECURITY IS NOT JUST ABOUT SECURITY <br> Detection, response, audit

- How do you know when you are being attacked?
- How quickly can you stop the attack?
- Can you identify the attacker(s)?
- Can you prevent the attack from recurring?
- Recovery
- Can be much more important than prevention
- Economics, insurance, risk management...
- Offensive techniques


## COMPUTER SECURITY IS NOT JUST ABOU'T COMPUTERS

- What is "the system"?
- Physical security
- Social engineering
- Bribes for passwords
- Phishing
- "External" means of getting information
- Legal records
- Trash cans


## SECURITY MINDSET

- Learn to think with a "security mindset" in general
- What is "the system"?
- How could this system be attacked?
- What is the weakest point of attack?
- How could this system be defended?
- What threats am I trying to address?
- How effective will a given countermeasure be?
- What is the trade-off between security, cost, and usability?


## SUMMARY

- "The system" is not just a computer or a network
- Prevention is not the only goal
- Cost-benefit analysis
- Detection, response, recovery
- Nevertheless...in this course, we will focus on computer security, and primarily on prevention
- If you want to be a security expert, you need to keep the rest in mind


## COMPUTERS ARE EVERYWHERE...

- ...and can always be attacked
- Electronic banking, social networks, e-voting
- iPods, iPhones, PDAs, RFID transponders
- Automobiles
- Appliances, TVs
- (Implantable) medical devices
- Cameras, picture frames(!)
- See http://www.securityfocus.com/news/11499


## "TRUSTING TRUST"

- Consider a compiler that embeds a trapdoor into anything it compiles
- How to catch?
- Read source code? (What if replaced?)
- Re-compile compiler?
- What if the compiler embeds the trojan code whenever it compiles a compiler?
- (That's nasty...)


## "TRUSTING TRUST"

- Whom do you trust?
- Does one really need to be this paranoid??
- Probably not
- Sometimes, yes
- Shows that security is complex...and essentially impossible
- Comes back to risk/benefit trade-off


## Next time: begin cryptography

# COMPUTER AND NETWORI SECURITY 

## LECTURE 2

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## A high-level survey of cryptography

## GOALS OF CRYPTOGRAPHY

- Crypto deals primarily with three goals:
- Confidentiality
- Integrity (of data)
- Authentication (of resources, people, systems)
- Other goals also considered
- E.g., non-repudiation
- Accountability
- Anonymity
" ...


## CRYPTOGRAPHIC SYSTEMS

- Characterized along three independent dimensions:


The way in which the plaintext is processed


## PRIVATE- VS. PUBLIC-KEY SETTINGS

- For the basic goals, there are two settings:
- Private-key / shared-key / symmetric-key / secret-key
- Public-key
- The private-key setting is the "classical" one (thousands of years old)
- The public-key setting dates to the 1970s


## PRIVATE-KEY CRYPTOGRAPHY

- The communicating parties share some information that is random and secret
- This shared information is called a key
- Key is not known to an attacker
- This key must be shared (somehow) in advance of their communication



## TO EMPHASIZE

- Alice and Bob share a key K
- Must be shared securely
- Must be completely random
- Must be kept completely secret from attacker
- We don't discuss (for now) how they do this
- You can imagine they meet on a dark street corner and Alice hands a USB device (with a key on it) to Bob


## CANONICAL APPLICATIONS

- Two (or more) distinct parties communicating over an insecure network
- E.g., secure communication
" A single party who is communicating "with itself" over time
- E.g., secure storage




## SECURITY THROUGH OBSCURITY?

- Always assume that the full details of crypto protocols and algorithms are public
- Known as Kerckhoffs' principle
- The only secret information is a key
- "Security through obscurity" is a bad idea...
- True in general; even more true in the case of cryptography
- Home-brewed solutions are BAD!
- Standardized, widely-accepted solutions are GOOD!


## SECURITY THROUGH OBSCURITY?

- Why not?
- Easier to maintain secrecy of a key than an algorithm
- Reverse engineering
- Insider attacks
- Easier to change the key than the algorithm
- In general setting, much easier to share an algorithm than for everyone to use their own


## Private-key encryption

## Functional definition



Encryption: $\mathrm{c} \leftarrow \mathrm{E}_{\mathrm{K}}(\mathrm{m})$ possibly randomized!
Decryption algorithm: $\mathrm{m}=\mathrm{D}_{\mathrm{K}}(\mathrm{c})$
Correctness: for all K , we have $\mathrm{D}_{\mathrm{K}}\left(\mathrm{E}_{\mathrm{K}}(\mathrm{m})\right)=\mathrm{m}$

## Encryption scheme security

- Unconditionally secure
- No matter how much time an opponent has, it is impossible for him or her to decrypt the ciphertext simply because the required information is not there
- Computationally secure
- The cost of breaking the cipher exceeds the value of the encrypted information
- The time required to break the cipher exceeds the useful lifetime of the information



## MODEL OF SYMMETRIC CRYPTOSYSTEM



Figure 2.2 Model of Symmetric Cryptosystem

## CRYPTANALYSIS AND BRI 'T-FORCE ATTACK

Cryptanalysis

- Attack relies on the nature of the algorithm plus some knowledge of the general characteristics of the plaintext
- to attempt to deduce a specific plaintext or to deduce the key being used


## Brute-force attack

- Attacker tries every possible key on a piece of ciphertext until an intelligible translation into plaintext is obtained
- On average, half of all possible lkeys must be tried to achieve success.
- To supplement the brute-force approach, some degree of knowledge about the expected plaintext is needed,

Type of Attack
Known to Cryptanalyst

| Ciphertext Only | - Encryption algorithm <br> - Ciphertext |
| :---: | :---: |
| Known Plaintext | - Encryption algorithm <br> - Ciphertext <br> - One or more plaintext-ciphertext pairs formed with the secret key |
| Chosen Plaintext | - Encryption algorithm <br> - Ciphertext <br> - Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key |
| Chosen Ciphertext | - Encryption algorithm <br> - Ciphertext <br> - Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key |
| Chosen Text | - Encryption algorithm <br> - Ciphertext <br> - Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key <br> - Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key |

TABLE 2.1 TYPES OF<br>hTTHCKS<br>ON<br>ENCRYPTIED<br>MESSAGES

## A CLASSIC EXAMPLE: SHIFT CIPHER

- Assume the English uppercase alphabet (no lowercase, punctuation, etc.)
- View letters as numbers in $\{0, \ldots, 25\}$
- The key is a random letter of the alphabet
- Encryption done by addition modulo 26
- Is this secure?
- Exhaustive key search
- Automated determination of the key

| KEY | PHHW PH DIWHU WKH WRJD SDUWB |
| ---: | :--- |
| 1 | oggv og chvgt vjg vqic rctva |
| 2 | nffu nf bgufs uif uphb qbsuz |
| 3 | meet me after the toga party |
| 4 | ldds ld zesdq sgd snfz ozqsx |
| 5 | kccr kc ydrcp rfc rmey nyprw |
| 6 | jbbq jb xcqbo qeb qldx mxoqv |
| 7 | iaap ia wbpan pda pkcw lwnpu |
| 8 | hzzo hz vaozm ocz ojbv kvmot |
| 9 | gyyn gy uznyl nby niau julns |
| 10 | fxxm fx tymxk max mhzt itkmr |
| 11 | ewwl ew sxlwj lzw lgys hsjlq |
| 12 | dvvk dv rwkvi kyv kfxr grikp |
| 13 | cuuj cu qvjuh jxu jewq fqhjo |
| 14 | btti bt puitg iwt idvp epgin |
| 15 | assh as othsf hvs hcuo dofhm |
| 16 | zrrg zr nsgre gur gbtn cnegl |
| 17 | yqqf yq mrfqd ftq fasm bmdfk |
| 18 | xppe xp lqepc esp ezrl alcej |
| 19 | wood wo kpdob dro dyqk zkbdi |
| 20 | vnnc vn jocna cqn cxpj yjach |
| 21 | ummb um inbmz bpm bwoi xizbg |
| 22 | tlla tl hmaly aol avnh whyaf |
| 23 | skkz sk glzkx znk zumg vgxze |
| 24 | rjjy rj fkyjw ymj ytlf ufwyd |
| 25 | qiix qi ejxiv xli xske tevxc |

Figure 2.3 Brute-Force Cryptanalysis of Caesar Clipeer

## MONOALPHABETIC CIPHER

- The key is a random permutation of the alphabet
- Note: key space is huge!
- Encryption done in the natural way
- Is this secure?
- Frequency analysis
- A large key space is necessary, but not sufficient, for security


Figure 2.5 Relative Frequency of Letters in English Text

## MONOALPHABETIC CIPHERS

- Easy to break because they reflect the frequency data of the original alphabet
- Countermeasure is to provide multiple substitutes (homophones) for a single letter
- Digram
- Two-letter combination
- Most common is th
- Trigram
- Three-letter combination

- Most frequent is the



## ANOTHER EXAMPLE: VIGENERE CIPHER

- More complicated version of shift cipher
- Believed to be secure for over 100 years
- Is it secure?


## POLYALPHABETIC CIPHERS

- Polyalphabetic substitution cipher
- Improves on the simple monoalphabetic technique by using different monoalphabetic substitutions as one proceeds through the plaintext message


## All these techniques have the following features in common:

- A set of related monoalphabetic substitution rules is used
- A key determines which particular rule is chosen for a given transformation


## VIGENÈRE CIPHER

- Best known and one of the simplest polyalphabetic substitution ciphers
- In this scheme the set of related monoalphabetic substitution rules consists of the 26 Caesar ciphers with shifts of 0 through 25
- Each cipher is denoted by a key letter which is the ciphertext letter that substitutes for the plaintext letter a


## EXAMPLE OP VIGENÈRE CIPHER

- To encrypt a message, a key is needed that is as long as the message
- Usually, the key is a repeating keyword
- For example, if the keyword is deceptive, the message "we are discovered save yourself" is encrypted as:
key:
deceptivedeceptivedeceptive
plaintext: wearediscoveredsaveyourself ciphertext: ZICVTWQNGRZGVTWAVZHCQYGLMGJ


## VIGenère autorey system

- A keyword is concatenated with the plaintext itself to provide a running key
- Example:
key: deceptivewearediscoveredsav
plaintext: wearediscoveredsaveyourself ciphertext: ZICVTWQNGKZEIIGASXSTSLVVWLA
- Even this scheme is vulnerable to cryptanalysis
- Because the key and the plaintext share the same frequency distribution of letters, a statistical technique can be applied


## ATTACKING THE VIGENERE CIPHER

- Let $p_{i}($ for $i=0, \ldots, 25)$ denote the frequency of letter $i$ in Englishlanguage text
- Known that $\Sigma \mathrm{p}_{\mathrm{i}}{ }^{2} \approx 0.065$
- For each candidate period $t$, compute frequencies $\left\{q_{i}\right\}$ of letters in the sequence $\mathrm{c}_{0}, \mathrm{c}_{\mathrm{t}}, \mathrm{c}_{2 \mathrm{t}}, \ldots$
- For the correct value of $t$, we expect $\Sigma q_{i}^{2} \approx 0.065$
- For incorrect values of $t$, we expect $\Sigma q_{i}{ }^{2} \approx 1 / 26$
- Once we have the period, can use frequency analysis as in the case of the shift cipher


## MORAL OF THE STORY?

- Don't use "simple" schemes
- Don't use schemes that you design yourself
- Use schemes that other people have already designed and analyzed...


## A FUNDAMENTAL PROBLEM

" A fundamental problem with "classical" cryptography is that no definition of security was ever specified
" It was not even clear what it meant for a scheme to be "secure"

- As a consequence, proving security was not even an option
- So how can you know when something is secure?
- (Or is at least based on well-studied, widely-believed assumptions)


## SECURITY COALS?

- Adversary unable to recover the key
- Necessary, but meaningless on its own...
- Adversary unable to recover entire plaintext
- Good, but is it enough?
- Adversary unable to determine any information at all about the plaintext
- Formalize?
- Sounds great!
- Can we achieve it?


# CMSC 414 <br> Computer and Network Security 

## Lecture 3

## Jonathan Katz

Modified by: Dr. Ramzi Saifan

Perfect secrecy

## Defining secrecy (take 1)

- Even an adversary running for an unbounded amount of time learns nothing about the message from the ciphertext
- (Except the length)
- Perfect secrecy
- Formally, for all distributions over the message space, all $m$, and all $c$ :

$$
\operatorname{Pr}[\mathrm{M}=\mathrm{m} \mid \mathrm{C}=\mathrm{c}]=\operatorname{Pr}[\mathrm{M}=\mathrm{m}]
$$

## Properties of the one-time pad?

- Achieves perfect secrecy
- No eavesdropper (no matter how powerful) can determine any information whatsoever about the plaintext
- was developed by Gilbert Vernam in 1918.
- Stream cipher: The message is represented as a binary string.
- The key is a truly random sequence of 0's and 1's of the same length as the message.
- The encryption is done by XOR the key and the message.


## Why OTP is perfect secure?

- The security depends on the randomness of the key.
- In cryptographic context, we seek two fundamental properties in a binary random key sequence:
- Unpredictability: the probability of a certain bit being 1 or 0 is exactly equal to $1 / 2$ even if you have all previous bits.
- Balanced (Equal Distribution):
- The number of 1's and 0's should be equal.


## Mathematical Proof

- the probability of a key bit being 1 or 0 is exactly equal to $1 / 2$.
- The plaintext bits are not balanced. Let the probability of 0 be $x$ and then the probability of 1 turns out to be 1-x.
- Let us calculate the probability of ciphertext bits.


## Mathematical Proof

| $m_{i}$ <br> prob. |  | $k_{i}$ | prob. | $c_{i}$ | prob. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | $x$ | 0 | $1 / 2$ | 0 | $1 / 2 x$ |
| 0 | $x$ | 1 | $1 / 2$ | 1 | $1 / 2 x$ |
| 1 | $1-x$ | 0 | $1 / 2$ | 1 | $1 / 2(1-x)$ |
| 1 | $1-x$ | 1 | $1 / 2$ | 0 | $1 / 2(1-x)$ |

- We find out the probability of a ciphertext bit being 1 or 0 is equal to $(1 / 2) x+(1 / 2)(1-x)=1 / 2$. Ciphertext looks like a random sequence.


## Disadvantages

- (Essentially) useless in practice...
- Long key length
- Can only be used once (hence the name!)
- Insecure against known-plaintext attacks
- Key distribution \& Management difficult.
- These are inherent limitations of perfect secrecy


## A computationally secure scheme

- A pseudorandom (number) generator (PRNG) is a deterministic function that takes as input a seed and outputs a string
- If seed chosen at random, output of the PRNG should "look random" (i.e., be pseudorandom)


## Notes

- Pseudo-randomness must be indistinguishable from random for all efficient algorithms
- General-purpose PRNGs not sufficient for crypto
- Pseudorandomness of the PRNG depends on the seed being chosen "at random"
- Note in particular that if a seed is re-used then the output of the PRNG remains the same!
- In practice: from physical processes and/or user behavior


## Computational secrecy

## Computational secrecy

- We can overcome the limitations of perfect secrecy by (slightly) relaxing the definition
- Instead of requiring total secrecy against unbounded adversaries, require secrecy against time-bounded adversaries except with some small probability
- E.g., secrecy for 100 years, except with probability 2-80


## The take-home message

- Weakening the definition slightly allows us to construct much more efficient schemes!
- Strictly speaking, no longer 100\% absolutely guaranteed to be secure
- Security of encryption now depends on security of building blocks (which are analyzed extensively, and are believed to be secure)
- Given enough time and/or resources, the scheme can be broken

Block Ciphers and the Data Encryption Standard (DES)

Modified by: Dr. Ramzi Saifan

## Block ciphers

- Keyed, invertible
- Large key space, large block size
- A block of plaintext is treated as a whole and used to produce a ciphertext block of equal length
- Typically a block size of 64 or 128 bits is used
- The majority of network-based symmetric cryptographic applications make use of block ciphers


## Data Encryption Standard (DES)

- Developed in 1970s by IBM / NSA / NBS
- Non-public design process
- Block size $=64$-bit input/output
- Key size $=56$ bits out of a 64 bits
- One bit in each octet is a parity-check bit
- Was the most widely used encryption scheme until the introduction of the Advanced Encryption Standard (AES) in 2001


## Feistel Cipher

- Proposed the use of a cipher that alternates substitutions and permutations


## Substitutions

- Each plaintext element or group of elements is uniquely replaced by a corresponding ciphertext element or group of elements
- No elements are added or deleted or replaced in the sequence, rather the order in which the elements appear in the sequence is changed


## Is the structure used by many significant symmetric block ciphers currently in use.

Feistel Cipher Structure




Figure 3.3 Feistel Encryption and Decryption (16 rounds)

## Feistel Cipher Design Features

- Block size
- Larger block sizes mean greater security but reduced encryption/decryption speed for a given algorithm
- Key size
- Larger key size means greater security but may decrease encryption/decryption speeds
- Number of rounds
- The essence of the Feistel cipher is that a single round offers inadequate security but that multiple rounds offer increasing security
- Subkey generation algorithm
- Greater complexity in this algorithm should lead to greater difficulty of cryptanalysis
- Round function F
- Greater complexity generally means greater resistance to cryptanalysis
- Fast software encryption/decryption
- In many cases, encrypting is embedded in applications or utility functions in such a way as to preclude a hardware implementation; accordingly, the speed of execution of the algorithm becomes a concern
- Ease of analysis
- If the algorithm can be concisely and clearly explained, it is easier to analyze that algorithm for cryptanalytic vulnerabilities and therefore develop a higher level of assurance as to its strength


## Feistel Example



Figure 3.4 Feistel Example


## DES <br> Encryption Algorithm

Figure 3.5 General Depiction of DES Encryption Algorithm

## Round Function



## Average Time Required for Exhaustive Key

## Search

| Key size (bits) | Cipher | Number of Alternative Keys | Time Required at 109 decryptions/s | Time Required at 1013 decryptions/s |
| :---: | :---: | :---: | :---: | :---: |
| 56 | DES | $\begin{aligned} & 256 \approx 7.2 \times \\ & 1016 \end{aligned}$ | $255 \mathrm{~ns}=1.125$ years | 1 hour |
| 128 | AES | $\begin{aligned} & 2128=3.4 \times \\ & 1038 \end{aligned}$ | $\begin{aligned} & 2127 \mathrm{~ns}=5.3 \times 1021 \\ & \text { years } \end{aligned}$ | $\begin{aligned} & 5.3 \times 1017 \\ & \text { years } \end{aligned}$ |
| 168 | Triple DES | $\begin{aligned} & 2168=3.7 \times \\ & 1050 \end{aligned}$ | $2167 \mathrm{~ns}=5.8 \times 1033$ <br> years | $\begin{aligned} & 5.8 \times 1029 \\ & \text { years } \end{aligned}$ |
| 192 | AES | $\begin{aligned} & 2192 \approx 6.3 \times \\ & 1057 \end{aligned}$ | $\begin{aligned} & 2191 \mathrm{~ns}=9.8 \times 1040 \\ & \text { years } \end{aligned}$ | $\begin{aligned} & 9.8 \times 1036 \\ & \text { years } \end{aligned}$ |
| 256 | AES | $\begin{aligned} & 2256 \approx 1.2 \times \\ & 1077 \end{aligned}$ | $\begin{aligned} & 2255 \mathrm{~ns}=1.8 \times 1060 \\ & \text { years } \end{aligned}$ | $\begin{aligned} & 1.8 \times 1056 \\ & \text { years } \end{aligned}$ |
| 26 characters (permutation) | Monoalphabetic | $26!=4 \times 1026$ | $\begin{aligned} & 2 \times 1026 \mathrm{~ns}=6.3 \times \\ & 109 \text { years } \end{aligned}$ | $6.3 \times 106$ years |

## Block Cipher Design Principles: Design of Function F

- The heart of a Feistel block cipher is the function F
- The more nonlinear F , the more difficult any type of cryptanalysis will be
- The SAC and BIC criteria appear to strengthen the effectiveness of the confusion function

The algorithm should have good avalanche properties

## Strict avalanche criterion (SAC)

States that any output bit $\mathbf{j}$ should change with probability $\mathbf{1 / 2}$ when any single input bit $i$ is inverted for all $\mathbf{i}, \mathbf{j}$


States that output bits $j$ and $k$ should change independently when any single input bit $i$ is inverted for all $\mathbf{i}, \mathbf{j}$, and $k$

## Concerns about DES

- Short key length
- DES "cracker", can break DES in days
- Computation can be distributed to make it faster
- Does not mean "DES is insecure"; depends on desired security
- Short block length
- Repeated blocks happen "too frequently"
- Some (theoretical) attacks have been found
- Claimed known to DES designers 15 years before public discovery!


## Double DES


(a) Double Encryption

## Meet-in-the-Middle Attack

The use of double DES results in a mapping that is not equivalent to a single DES
encryption


The meet-in-the-middle attack algorithm will attack this scheme and does not depend on any particular property of DES but will work against any block encryption cipher

## Triple-DES with Two-Keys

Obvious counter to the meet-in-the-middle attack is to use three stages of encryption with three different keys

- This raises the cost of the meet-in-the-middle attack to $2^{112}$, which is beyond what is practical
- Has the drawback of requiring a key length of $56 \times 3=168$ bits, which may be somewhat unwieldy
- As an alternative Tuchman proposed a triple encryption method that uses only two keys
3DES with two keys is a relatively popular alternative to DES and has been adopted for use in the key management standards ANSI X9.17 and ISO 8732


## Multiple Encryption


(b) Triple Encryption

Figure 6.1 Multiple Encryption

## Triple DES with Three Keys

## Many researchers now feel that three-key 3DES is

 the preferred alternativeThree-key 3DES has
an effective key
length of 168 bits and is defined as:

Backward
compatibility with
DES is provided by putiting:

- $C=\mathrm{E}\left(K_{3}, \mathrm{D}\left(K_{2}, \mathrm{E}\left(K_{1}, P\right)\right)\right)$
- $\mathrm{K}_{3}=\mathrm{K}_{2}$ or $\mathrm{K}_{1}=\mathrm{K}_{2}$

A number of Internet-based applications have adopted three-key 3DES including PGP and S/MIME

Next is AES

(a) Two-key Triple Encryption with Candidate Pair of Keys

(c) Table of intermediate values and candidate keys
(b) Table of $\mathbf{n}$ known plaintext-ciphertext pairs, sorted on $\mathbf{P}$

Figure 6.2 Known-Plaintext Attack on Triple DES

## Advanced Encryption Standard

Modified by: Dr. Ramzi Saifan

## Why AES?

- Symmetric block cipher, published in 2001
- Intended to replace DES and 3DES

DES is vulnerable to multiple attacks
3DES has slow performances

## NIST Criteria to Evaluate Potential Candidates

- Security: The effort to crypt analyze an algorithm.
- Cost: The algorithm should be practical in a wide range of applications.
- Algorithm and Implementation Characteristics : Flexibility, simplicity etc.

5 final candidates have been chosen out of 15


Figure 5.1 AES Encryption Process

## AES Data Structures

| in ${ }_{0}$ | $\mathrm{in}_{4}$ | $\mathrm{in}_{8}$ | $\mathrm{in}_{12}$ | $s_{0,0}$ | $s_{0,1}$ | $s_{0,2}$ | $s_{0,3}$ | $s_{0,0}$ | $s_{0,1}$ | $s_{0,2}$ | $s_{0,3}$ | out $_{0}$ | out $_{4}$ | out $_{8}$ | out $_{12}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{in}_{1}$ | $\mathrm{in}_{5}$ | $\mathrm{in}_{9}$ | $\mathrm{in}_{13}$ | $s_{1,0}$ | $s_{1,1}$ | $s_{1,2}$ | $s_{1,3}$ | $s_{1,0}$ | $s_{1,1}$ | $s_{1,2}$ | $s_{1,3}$ | out $_{1}$ | out ${ }_{5}$ | out ${ }_{9}$ | out $_{13}$ |
| $\mathrm{in}_{2}$ | $\mathrm{in}_{6}$ | in 10 | in ${ }_{14}$ | $s_{2,0}$ | $s_{2,1}$ | $S_{2,2}$ | $s_{2,3}$ | $s_{2,0}$ | $s_{2,1}$ | $s_{2,2}$ | $s_{2,3}$ | out $_{2}$ | out $_{6}$ | out ${ }_{10}$ | out $_{14}$ |
| $\mathrm{in}_{3}$ | $i n_{7}$ | $\mathrm{in}_{11}$ | $\mathrm{in}_{15}$ | $s_{3,0}$ | $s_{3,1}$ | $s_{3,2}$ | $s_{3,3}$ | $s_{3,0}$ | $s_{3,1}$ | $s_{3,2}$ | $s_{3,3}$ | out $_{3}$ | out $_{7}$ | out 11 | out $_{15}$ |

(a) Input, state array, and output

(b) Key and expanded key

## Convert to State Array

Input block:

|  | 0 | 4 | 8 | 12 |  | $\mathrm{S}_{0,0} \mathrm{~S}$ | $\mathrm{S}_{0,1}$ | $\mathrm{S}_{0,2}$ | $\mathrm{S}_{0,3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 5 | 9 | 13 | 6-7 8 | $\mathrm{S}_{1,0} \mathrm{~S}$ | $\mathrm{S}_{1,1}$ | $\mathrm{S}_{1,2}$ | $\mathrm{S}_{1,3}$ | 15 |
| 0 | 2 | 6 | 10 | 14 |  | $\mathrm{S}_{2,0}$ | $\mathrm{S}_{2,1}$ | $\mathrm{S}_{2,2}$ | $\mathrm{S}_{2,3}$ |  |
|  | 3 | 7 | 11 | 15 |  | $\mathrm{S}_{3,0} \mathrm{~S}$ | $\mathrm{S}_{3,1}$ | $\mathrm{S}_{3,2}$ | $\mathrm{S}_{3,3}$ |  |

## Table 5.1 AES Parameters

| Key Size (words/bytes/bits) | $4 / 16 / 128$ | $6 / 24 / 192$ | $8 / 32 / 256$ |
| :--- | :---: | :---: | :---: |
| Plaintext Block Size (words/bytes/bits) | $4 / 16 / 128$ | $4 / 16 / 128$ | $4 / 16 / 128$ |
| Number of Rounds | 10 | 12 | 14 |
| Round Key Size (words/bytes/bits) | $4 / 16 / 128$ | $4 / 16 / 128$ | $4 / 16 / 128$ |
| Expanded Key Size (words/bytes) | $44 / 176$ | $52 / 208$ | $60 / 240$ |

## AES Encryption and Decryption



Figure 5.3 AES Encryption and Decryption

## Detailed Structure

The key that is provided as input is expanded into an array of forty-four 32-bit words, $w[i]$

## Four different stages are used:

- Substitute bytes - uses an S-box to perform a byte-by-byte substitution of the block
- ShiftRows - a simple permutation
- MixColumns - a substitution that makes use of arithmetic
- AddRoundKey - a simple bitwise XOR of the current block with a portion of the expanded key

Can view the cipher as alternating operations of XOR encryption (AddRoundKey) of a block, followed by scrambling of the block (the other three stages), followed by XOR encryption, and so on
Each stage is easily reversible
The decryption algorithm makes use of the expanded key in reverse order, however the decryption algorithm is not identical to the encryption algorithm

- Final round of both encryption and decryption consists of only three stages

SubBytes

State

State

MixColumns

State

AddRoundKey


Figure 5.4 AES Encryption Round

## AddRoundKey

- XOR each byte of the round key with its corresponding byte in the state array



## SubBytes

- Replace each byte in the state array with its corresponding value from the $S$-Box

|  | Y |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | a | b | C | d | e | f |
| 0 | 63 | 7c | 77 | 7b | f2 | 6b | 6 f | c5 | 30 | 01 | 67 | 2b | fe | d7 | ab | 76 |
| 1 | ca | 82 | c9 | 7d | fa | 59 | 47 | f0 | ad | d4 | a2 | af | 9c | a 4 | 72 | c0 |
| 2 | b7 | fd | 93 | 26 | 36 | 31 | f7 | CC | 34 | a5 | e5 | f1 | 71 | d8 | 31 | 15 |
| 3 | 04 | c7 | 23 | c3 | 18 | 96 | 05 | 9a | 07 | 12 | 80 | e2 | eb | 27 | b2 | 75 |
| 4 | 09 | 83 | 2c | 1a | 1b | 6e | 5a | a0 | 52 | 3b | d6 | b3 | 29 | e3 | 2 f | 84 |
| 5 | 53 | d1 | 00 | ed | 20 | fc | b1 | 5b | 6 a | cb | be | 39 | 4 a | 4 C | 58 | Cf |
| 6 | d0 | ef | aa | fb | 43 | 4d | 33 | 85 | 45 | f9 | 02 | 7f | 50 | 3c | 9f | a8 |
| 7 | 51 | a3 | 40 | 8f | 92 | 9d | 38 | f5 | bc | b6 | da | 21 | 10 | ff | f3 | d2 |
| 8 | cd | 0c | 13 | ec | 5 f | 97 | 44 | 17 | c4 | a7 | 7e | 3d | 64 | 5d | 19 | 73 |
| 9 | 60 | 81 | 4f | dc | 22 | 2a | 90 | 88 | 46 | ee | b8 | 14 | de | 5 e | 0b | db |
| a | e0 | 32 | 3a | 0a | 49 | 06 | 24 | 5c | c2 | d3 | ac | 62 | 91 | 95 | e4 | 79 |
| b | e7 | c8 | 37 | 6d | 8d | d5 | 4e | a9 | 6 c | 56 | f4 | ea | 65 | 7a | ae | 08 |
| c | ba | 78 | 25 | 2e | 1c | a6 | b4 | c6 | e8 | dd | 74 | 1f | 4b | bd | 8b | 8 a |
| d | 70 | 3e | b5 | 66 | 48 | 03 | f6 | 0e | 61 | 35 | 57 | b9 | 86 | c1 | 1d | 9e |
| e | e1 | f8 | 98 | 11 | 69 | d9 | 8e | 94 | 9b | 1e | 87 | e9 | ce | 55 | 28 | df |
| f | 8 c | a1 | 89 | 0d | bf | e6 | 42 | 68 | 41 | 99 | 2d | 0f | b0 | 54 | bb | 16 |

## (a) S-box

|  |  | $y$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | A | B | C | D | E | F |
| $x$ | 0 | 63 | 7C | 77 | 7B | F2 | 6B | 6 F | C5 | 30 | 01 | 67 | 2B | FE | D7 | AB | 76 |
|  | 1 | CA | 82 | C9 | 7D | FA | 59 | 47 | F0 | AD | D4 | A2 | AF | 9C | A4 | 72 | C0 |
|  | 2 | B7 | FD | 93 | 26 | 36 | 3F | F7 | CC | 34 | A5 | E5 | F1 | 71 | D8 | 31 | 15 |
|  | 3 | 04 | C7 | 23 | C3 | 18 | 96 | 05 | 9A | 07 | 12 | 80 | E2 | EB | 27 | B2 | 75 |
|  | 4 | 09 | 83 | 2 C | 1A | 1B | 6 E | 5A | A0 | 52 | 3B | D6 | B3 | 29 | E3 | 2F | 84 |
|  | 5 | 53 | D1 | 00 | ED | 20 | FC | B1 | 5B | 6A | CB | BE | 39 | 4A | 4C | 58 | CF |
|  | 6 | D0 | EF | AA | FB | 43 | 4D | 33 | 85 | 45 | F9 | 02 | 7F | 50 | 3C | 9F | A8 |
|  | 7 | 51 | A3 | 40 | 8F | 92 | 9D | 38 | F5 | BC | B6 | DA | 21 | 10 | FF | F3 | D2 |
|  | 8 | CD | 0C | 13 | EC | 5F | 97 | 44 | 17 | C4 | A7 | 7E | 3D | 64 | 5D | 19 | 73 |
|  | 9 | 60 | 81 | 4F | DC | 22 | 2 A | 90 | 88 | 46 | EE | B8 | 14 | DE | 5E | 0B | DB |
|  | A | E0 | 32 | 3A | 0A | 49 | 06 | 24 | 5C | C2 | D3 | AC | 62 | 91 | 95 | E4 | 79 |
|  | B | E7 | C8 | 37 | 6D | 8D | D5 | 4E | A9 | 6 C | 56 | F4 | EA | 65 | 7A | AE | 08 |
|  | C | BA | 78 | 25 | 2E | 1 C | A6 | B4 | C6 | E8 | DD | 74 | 1F | 4B | BD | 8B | 8A |
|  | D | 70 | 3E | B5 | 66 | 48 | 03 | F6 | 0E | 61 | 35 | 57 | B9 | 86 | C1 | 1D | 9E |
|  | E | E1 | F8 | 98 | 11 | 69 | D9 | 8E | 94 | 9B | 1E | 87 | E9 | CE | 55 | 28 | DF |
|  | F | 8C | A1 | 89 | 0D | BF | E6 | 42 | 68 | 41 | 99 | 2D | 0F | B0 | 54 | BB | 16 |

## (b) Inverse S-box

|  |  | $y$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | A | B | C | D | E | F |
| $x$ | 0 | 52 | 09 | 6A | D5 | 30 | 36 | A5 | 38 | BF | 40 | A3 | 9E | 81 | F3 | D7 | FB |
|  | 1 | 7 C | E3 | 39 | 82 | 9B | 2F | FF | 87 | 34 | 8E | 43 | 44 | C4 | DE | E9 | CB |
|  | 2 | 54 | 7B | 94 | 32 | A6 | C2 | 23 | 3D | EE | 4C | 95 | 0B | 42 | FA | C3 | 4E |
|  | 3 | 08 | 2 E | A1 | 66 | 28 | D9 | 24 | B2 | 76 | 5B | A2 | 49 | 6D | 8B | D1 | 25 |
|  | 4 | 72 | F8 | F6 | 64 | 86 | 68 | 98 | 16 | D4 | A4 | 5C | CC | 5D | 65 | B6 | 92 |
|  | 5 | 6 C | 70 | 48 | 50 | FD | ED | B9 | DA | 5 E | 15 | 46 | 57 | A7 | 8D | 9D | 84 |
|  | 6 | 90 | D8 | AB | 00 | 8C | BC | D3 | 0A | F7 | E4 | 58 | 05 | B8 | B3 | 45 | 06 |
|  | 7 | D0 | 2C | 1E | 8 F | CA | 3F | 0F | 02 | C1 | AF | BD | 03 | 01 | 13 | 8A | 6B |
|  | 8 | 3A | 91 | 11 | 41 | 4 F | 67 | DC | EA | 97 | F2 | CF | CE | F0 | B4 | E6 | 73 |
|  | 9 | 96 | AC | 74 | 22 | E7 | AD | 35 | 85 | E2 | F9 | 37 | E8 | 1C | 75 | DF | 6 E |
|  | A | 47 | F1 | 1A | 71 | 1D | 29 | C5 | 89 | 6F | B7 | 62 | 0E | AA | 18 | BE | 1B |
|  | B | FC | 56 | 3E | 4B | C6 | D2 | 79 | 20 | 9A | DB | C0 | FE | 78 | CD | 5A | F4 |
|  | C | 1 F | DD | A8 | 33 | 88 | 07 | C7 | 31 | B1 | 12 | 10 | 59 | 27 | 80 | EC | 5 F |
|  | D | 60 | 51 | 7F | A9 | 19 | B5 | 4A | 0D | 2D | E5 | 7A | 9F | 93 | C9 | 9C | EF |
|  | E | A0 | E0 | 3B | 4D | AE | 2A | F5 | B0 | C8 | EB | BB | 3C | 83 | 53 | 99 | 61 |
|  | F | 17 | 2B | 04 | 7E | BA | 77 | D6 | 26 | E1 | 69 | 14 | 63 | 55 | 21 | 0C | 7D |

## S-Box Rationale

- The S-box is designed to be resistant to known cryptanalytic attacks
- The Rijndael developers sought a design that has a low correlation between input bits and output bits and the property that the output is not a linear mathematical function of the input


## Shift Row Transformation


(a) Shift row transformation

AES Row and Column Operations

## ShiftRows

- Last three rows are cyclically shifted

|  |  |  | $\mathrm{S}_{0,0}$ | $\mathrm{S}_{0,1}$ | $\mathrm{S}_{0,2}$ | $\mathrm{S}_{0,3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{S}_{1,0}$ | $\mathrm{S}_{1,0}$ | $\mathrm{S}_{1,1}$ | $\mathrm{S}_{1,2}$ | $\mathrm{S}_{1,3}$ |
|  | $\mathrm{S}_{2,0}$ | $\mathrm{S}_{2,1}$ | $\mathrm{S}_{2,0}$ | $\mathrm{S}_{2,1}$ | $\mathrm{S}_{2,2}$ | $\mathrm{S}_{2,3}$ |
| $\mathrm{S}_{3,0}$ | $\mathrm{S}_{3,1}$ | $\mathrm{S}_{3,2}$ | $\mathrm{S}_{3,0}$ | $\mathrm{S}_{3,1}$ | $\mathrm{S}_{3,2}$ | $\mathrm{S}_{3,3}$ |

## Shift Row Rationale

On encryption, the first 4 bytes of the plaintext are copied to the first column of State, and so on

The round key is applied to State column by column

- Thus, a row shift moves an individual byte from one column to another, which is a linear distance of a multiple of 4 bytes
Transformation ensures that the 4 bytes of one column are spread out to four different columns


## MixColumn Transformation


(b) Mix column transformation

Figure 5.7 AES Row and Column Operations

## MixColumns

- Apply MixColumn transformation to each column


## Mix Columns Rationale

- Coefficients of a matrix based on a linear code with maximal distance between code words ensures a good mixing among the bytes of each column
- The mix column transformation combined with the shift row transformation ensures that after a few rounds all output bits depend on all input bits


## AddRoundKey Transformation

The 128 bits of State are bitwise XORed with the 128 bits of the round key

Operation is viewed as a columnwise operation between the 4 bytes of a State column and one word of the round key

- Can also be viewed as a byte-level operation


## Rationale:

Is as simple as possible and affects every bit of State

The complexity of the round
key expansion plus the complexity of the other stages of AES ensure security

## Inputs for Single AES

 Round

Figure 5.8 Inputs for Single AES Round

## AES Key Expansion

Takes as input a four-word (16 byte) key and produces a linear array of 44 words (176) bytes

- This is sufficient to provide a four-word round key for the initial AddRoundKey stage and each of the 10 rounds of the cipher
Key is copied into the first four words of the expanded key
- The remainder of the expanded key is filled in four words at a time

Each added word $w[i]$ depends on the immediately preceding word, $w[i-1]$, and the word four positions back, w[i-4]

- In three out of four cases a simple XOR is used
- For a word whose position in the $w$ array is a multiple of $4, \mathrm{a}$ more complex function is used

(a) Overall algorithm

Figure 5.9 AES Key Expansion

## Key Expansion Rationale

The Rijndael developers designed the expansion key algorithm to be resistant to known cryptanalytic attacks

Inclusion of a round-dependent round constant eliminates the symmetry between the ways in which round keys are generated in different rounds

| Key Words | Auxiliary Function |
| :---: | :---: |
| w0 $=0 \mathrm{f} 1571 \mathrm{c} 9$ | RotWord(w3) $=7 \mathrm{f} 6798$ af $=\mathrm{x} 1$ |
| $\mathrm{w} 1=47 \mathrm{~d} 9$ e8 59 | SubWord(x1) $=$ d2 $854679=y 1$ |
| $\mathrm{w} 2=0 \mathrm{c}$ b7 ad d6 | $\operatorname{Rcon}(1)=01000000$ |
| w3 = af 7f 6798 | $\mathrm{y} 1 \oplus \operatorname{Rcon}(1)=\mathrm{d} 3854679=\mathrm{z} 1$ |
| $\mathrm{w} 4=\mathrm{w} 0 \oplus \mathrm{z} 1=\mathrm{dc} 9037 \mathrm{~b} 0$ | RotWord(w7) $=8115$ a7 38 = x2 |
| $\mathrm{w} 5=\mathrm{w} 4 \oplus \mathrm{w} 1 \times 9 \mathrm{~b} 49 \mathrm{df}$ e9 | SubWord (x4) = 0c $595 \mathrm{c} 07=\mathrm{y} 2$ |
| $\mathrm{w} 6=\mathrm{w} 5 \oplus \mathrm{w} 2=97 \mathrm{fe} 723 \mathrm{f}$ | Rcon(2) = 02000000 |
| $\mathrm{w} 7=\mathrm{w} 6 \oplus \mathrm{w} 3=388115 \mathrm{a7}$ | y2 $\oplus \operatorname{Rcon}(2)=0 \mathrm{~L} 595 \mathrm{c} 07=\mathrm{z} 2$ |
| $\mathrm{w} 8=\mathrm{w} 4 \oplus \mathrm{z} 2=\mathrm{d} 2 \mathrm{c} 9 \mathrm{6b} \mathrm{~b} 7$ | RotWord(w11) $=$ ff d3 c6 e6 = x3 |
| w9 = w8 $\oplus$ w5 $=4980 \mathrm{~b} 45 \mathrm{e}$ | SubWord(x2)= $1666 \mathrm{~b} 4 \mathrm{8e}=\mathrm{y} 3$ |
| $\mathrm{w} 10=\mathrm{w} 9 \oplus \mathrm{w} 6=$ de 7 e c6 61 | Rcon(3) $=04000000$ |
| $\mathrm{w} 11=\mathrm{w} 10 \oplus \mathrm{w} 7=$ e6 ff d3 c6 | y 3 ¢ $\operatorname{Rcon}(3)=1266 \mathrm{~b} 48 \mathrm{e}=\mathrm{z} 3$ |
| w12 = w8 $\oplus \mathrm{z} 3=\mathrm{c} 0$ af df 39 | RotWord(w15) $=$ ae 7e c0 b1 $=\mathrm{x} 4$ |
| $\mathrm{w} 13=\mathrm{w} 12$ ( $\dagger \mathrm{w} 9=892 \mathrm{f} 6 \mathrm{~b} 67$ | SubWord(x3) $=$ e4 f3 ba c8 $=$ y 4 |
| $\mathrm{w} 14=\mathrm{w} 13 \oplus \mathrm{w} 10=5751$ ad 06 | Rcon(4) = 08000000 |
| $\mathrm{w} 15=\mathrm{w} 14 \oplus \mathrm{w} 11=\mathrm{b} 1$ ae 7 e c 0 | $\mathrm{y} 4 \oplus \operatorname{Rcon}(4)=$ ec $\mathrm{f} 3 \mathrm{ba} \mathrm{c} 8=4$ |
| $\mathrm{w} 16=\mathrm{w} 12$ ( $+\mathrm{z4}=2 \mathrm{c} 5 \mathrm{c} 65 \mathrm{f} 1$ | RotWord(w19) $=8 \mathrm{c}$ dd $5043=\mathrm{x} 5$ |
| $\mathrm{w} 17=\mathrm{w} 16$ ( $+\mathrm{w} 13=\mathrm{a} 5730 \mathrm{e} 96$ | SubWord (x4) $=64$ c1 $531 \mathrm{l}=\mathrm{y} 5$ |
| $\mathrm{w} 18=\mathrm{w} 17 \oplus \mathrm{w} 14=\mathrm{f} 222 \mathrm{a3} 90$ | Rcon(5) = 10 000000 |
| $\mathrm{w} 19=\mathrm{w} 18$ ( $\mathrm{w} 15=438 \mathrm{c}$ dd 50 | $\mathrm{y} 5 \oplus \operatorname{Rcon}(5)=74 \mathrm{c} 1531 \mathrm{l}=\mathrm{z5}$ |
| $\mathrm{w} 20=\mathrm{w} 16$ ( $+\mathrm{z5}=58$ 9d 36 eb | RotWord(w23) $=4046 \mathrm{bd} 4 \mathrm{c}=\mathrm{x} 6$ |
| $\mathrm{w} 21=\mathrm{w} 20$ ( $\mathrm{w} 17=\mathrm{fd}$ ee 38 7d | SubWord (x5) = 09 5a 7a 29 = y6 |
| $\mathrm{w} 22=\mathrm{w} 21$ ( $\mathrm{w} 18=0 \mathrm{f} \mathrm{cc} 9 \mathrm{~b}$ ed | Rcon(6) $=20000000$ |
| $\mathrm{w} 23=\mathrm{w} 22$ ( $\mathrm{w} 19=4 \mathrm{c} 4046 \mathrm{bd}$ | $\mathrm{y} 6 \oplus \operatorname{Rcon}(6)=29$ 5a 7a $29=\mathrm{z6}$ |
| $\mathrm{w} 24=\mathrm{w} 20$ ( $\mathrm{z}^{\prime}=71 \mathrm{c} 7 \mathrm{4c} \mathrm{c} 2$ | RotWord(w27) $=$ a5 a9 ef cf = x7 |
| $\mathrm{w} 25=\mathrm{w} 24$ ( $\mathrm{w} 21=8 \mathrm{c} 2974 \mathrm{bf}$ | SubWord(x6) $=06$ d3 df 8a = y7 |
| w26 = w25 $\dagger$ w22 = 83 e5 ef 52 | $\operatorname{Rcon}(7)=40000000$ |
| $\mathrm{w} 27=\mathrm{w} 26$ ( $\mathrm{w} 23=\mathrm{cf}$ a5 a9 ef | $\mathrm{y} 7 \oplus \operatorname{Rcon}(7)=46 \mathrm{~d} 3 \mathrm{df} 8 \mathrm{a}=\mathrm{z7}$ |
| $\mathrm{w} 28=\mathrm{w} 24 \oplus \mathrm{z7}=37149348$ | RotWord(w31) $=7 \mathrm{~d}$ a1 4a f7 $=\mathrm{x} 8$ |
| w29 = w28 $\oplus$ w25 = bb 3d e7 f7 | SubWord(x7) $=$ ff $32 \mathrm{~d} 668=\mathrm{y} 8$ |
| w30 = w29 $\dagger$ w26 = 38 d8 08 a5 | Rcon(8) = 80 000000 |
| $\mathrm{w} 31=\mathrm{w} 30 \oplus \mathrm{w} 27=\mathrm{f} 7 \mathrm{7d} \mathrm{a} 1 \mathrm{4a}$ | $\mathrm{y} 8 \oplus \operatorname{Rcon}(8)=7 \mathrm{f} 32 \mathrm{~d} 668=\mathrm{z} 8$ |
| w32 = w28 $\dagger$ z8 = 48 264520 | RotWord(w35) = be 0b 38 3c = x9 |
| w33 $=\mathrm{w} 32$ ( $\mathrm{w} 29=\mathrm{f} 3 \mathrm{1b}$ a2 d7 | SubWord (x8) = ae $2 \mathrm{~b} 07 \mathrm{eb}=\mathrm{y} 9$ |
| w34 $=$ w33 $\oplus$ w30 $=$ cb c3 aa 72 | $\operatorname{Rcon}(9)=1 \mathrm{~B} 000000$ |
| w35 $=\mathrm{w} 34 \oplus \mathrm{w} 32=3 \mathrm{c}$ be 0b 38 | y9 $\oplus \operatorname{Rcon}(9)=\mathrm{b} 52 \mathrm{~b} 07 \mathrm{eb}=\mathrm{z} 9$ |
| w36 $=$ w32 $\dagger \mathrm{z} 9=\mathrm{fd} 0 \mathrm{~d} 42 \mathrm{cb}$ | RotWord(w39) $=6 \mathrm{bb} 4156 \mathrm{f9}=\mathrm{x} 10$ |
| w37 = w36 $\dagger$ w33 = 0e 16 e0 1c | SubWord (x9) $=7 \mathrm{f} 83 \mathrm{~b} 199=\mathrm{y} 10$ |
| w38 $=\mathrm{w} 37$ ( $\mathrm{w} 34=\mathrm{c} 5 \mathrm{~d} 54 \mathrm{a} 6 \mathrm{e}$ | $\operatorname{Rcon}(10)=36000000$ |
| $\mathrm{w} 39=\mathrm{w} 38$ ( $\mathrm{w} 35=\mathrm{f} 96 \mathrm{~b} 4156$ | $\mathrm{y} 10 \oplus \operatorname{Rcon}(10)=4983 \mathrm{~b} 199=\mathrm{z} 10$ |
| $\mathrm{w} 40=\mathrm{w} 36 \oplus \mathrm{zl0}=\mathrm{b} 48 \mathrm{fe}$ f3 52 |  |
| $\mathrm{w} 41=\mathrm{w} 40 \oplus \mathrm{w} 37=$ ba 98134 e |  |
| $\mathrm{w} 42=\mathrm{w} 41 \oplus \mathrm{w} 38=7 \mathrm{f} 4 \mathrm{~d} 5920$ |  |
| $\mathrm{w} 43=\mathrm{w} 42 \oplus \mathrm{w} 39=86261876$ |  |


| Start of round | After SubBytes | After ShiftRows | After MixColumns | Round Key |
| :---: | :---: | :---: | :---: | :---: |
| 0189 fe 76 |  |  |  | 0f 47 0c af |
| 23 ab dc 54 |  |  |  | 15 d9 b7 7f |
| 45 cd ba 32 |  |  |  | 71 e8 ad 67 |
| 67 ef 9810 |  |  |  | c9 59 d6 98 |
| 0 e ce f2 d9 | ab 8b 8935 | ab 8b 8935 | b9 945775 | dc 9b 9738 |
| 3672 6b 2b | 0540 7f f1 | 40 7f f1 05 | e4 8e 1651 | 9049 fe 81 |
| $\begin{array}{lllll}34 & 25 & 17 & 55\end{array}$ | 18 3f f0 fc | f0 fc 18 3f | 47 20 9a 3f | 37 df 7215 |
| ae b6 4e 88 | e4 4e 2f c4 | c4 e4 4e 2f | c5 d6 f5 3b | b0 e9 3f a7 |
| 65 0f c0 4d | 4 d 76 ba e3 | 4 d 76 ba e3 | 8 e 22 db 12 | d2 49 de e6 |
| 74 c7 e8 do | 92 c6 9b 70 | c6 9b 7092 | b2 f2 dc 92 | c9 80 7e ff |
| 70 ff e8 2a | $51 \quad 16$ 9b e5 | 9b e5 5116 | $\mathrm{df} 80 \mathrm{f7} \mathrm{c} 1$ | 6b b4 c6 d3 |
| 75 3f ca 9c | 9d 7574 de | de 9d 7574 | 2d c5 le 52 | b7 5e 61 c6 |
| 5 c 6b 05 f 4 | 4a 7f 6b bf | 4a 7f 6b bf | b1 c1 0b cc | c0 8957 b 1 |
| 7b 72 a2 6d | 21403 a 3 c | 40 3a 3c 21 | ba f3 8b 07 | af 2 f 51 ae |
| b4 343112 | 8d 18 c7 c9 | c7 c9 8d 18 | f9 1f 6a c3 | df 6b ad 7e |
| 9a 9b 7f 94 | b8 14 d2 22 | 22 b 814 d 2 | 1 d 19245 c | $3967 \quad 06$ c0 |
| 7148 5c 7d | a3 $52 \mathrm{4a}$ ff | a3 52 4a ff | d4 11 fe 0 f | 2c a5 f2 43 |
| 15 dc da a9 | 598657 d3 | 8657 d3 59 | 3b 440673 | 5 c 73228 c |
| 2674 c7 bd | f7 92 c6 7a | c6 7a f7 92 | cb ab 6237 | 65 0e a3 dd |
| 247 e 229 c | 36 f3 93 de | de 36 f3 93 | $\begin{array}{llll}19 & \text { b7 } & 07 & \text { ec }\end{array}$ | f1 969050 |
| f8 b4 0c 4c | 41 8d fe 29 | 41 8d fe 29 | 2a 47 c4 48 | 58 fd 0f 4c |
| 673724 ff | 85 9a 3616 | 9a 361685 | 83 e8 18 ba | 9d ee cc 40 |
| ae a5 c1 ea | e4 4067887 | $\begin{array}{llllll}78 & 87 & \text { e4 } & 06\end{array}$ | $\begin{array}{lllll}84 & 18 & 27 & 23\end{array}$ | $36 \quad 38$ 9b 46 |
| e8 2197 bc | 9 b fd 8865 | 65 9b fd 88 | eb 1000 f 3 | eb 7d ed bd |
| 72 ba cb 04 | 40 f4 1f f2 | 40 f4 1f f2 | 7b 05424 a | 71 8c 83 cf |
| 1e 06 d 4 fa | 72 6f 48 2d | 6f 48 2d 72 | 1 e d0 2040 | c7 29 e5 a5 |
| b2 20 bc 65 | 37 b7 654 d | 65 4d 37 b7 | $\begin{array}{lllll}94 & 83 & 18 & 52\end{array}$ | 4 c 74 ef a9 |
| 00 6d e7 4e | 63 3c 942 f | 2 f 63 3c 94 | 94 c 443 fb | c2 bf 52 ef |
| 0a 89 c1 85 | $\begin{array}{llll}67 & \text { a7 } & 78 & 97\end{array}$ | 67 a7 7897 | ec 1a c0 80 | $37 \mathrm{bb} 38 \mathrm{f7}$ |
| d9 f9 c5 e5 | 3599 a6 d9 | 99 a6 d9 35 | 0c 5053 c 7 | 14 3d d8 7d |
| d8 f7 f7 fb | 616868 0f | 68 0f 6168 | 3b d7 00 ef | 93 e7 08 a1 |
| $\begin{array}{lllll}56 & 7 b & 11 & 14\end{array}$ | b1 2182 fa | fa b1 2182 | b7 $22 \begin{array}{llll} & 72 & \text { e0 }\end{array}$ | 48 f7 a5 4a |
| db a1 f8 77 | b9 3241 f 5 | b9 3241 f5 | b1 1a 4417 | $48 \mathrm{f3} \mathrm{cb} 3 \mathrm{c}$ |
| 18 6d 8b ba | ad 3c 3d f4 | 3c 3d f4 ad | $3 \mathrm{~d} 2 \mathrm{f} \mathrm{ec} \mathrm{b6}$ | 26 1b c3 be |
| a8 30084 e | c2 04302 f | 30 2f c2 04 | 0a 6b 2f 42 | 45 a2 aa 0b |
| ff d5 d7 aa | 16030 eac | ac 16030 e | 9 f 68 f 3 b 1 | $\begin{array}{lllll}20 & \text { d7 } & 72 & 38\end{array}$ |
| f9 e9 8f 2b | 99 1e 73 f1 | 99 1e 73 f1 | 31303 ac | fd 0e c5 f9 |
| 1b 342 f 08 | af 181530 | 181530 af | ac 7188 c 4 | 0d 16 d5 6b |
| 4 f c9 8549 | 84 dd 97 3b | 97 3b 84 dd | 466548 eb | 42 e0 4a 41 |
| bf bf 8189 | $08080 c a 7$ | a7 $0808080 c$ | 6 a 1c 3162 | cb 1c 6e 56 |
| cc 3e ff 3b | 4 b b2 16 e2 | 4 b b2 16 e2 | 4 b 868 a 36 | b4 ba 7f 86 |
| a1 6759 af | 3285 cb 79 | 85 cb 7932 | b1 cb 27 5a | 8 e 98 4d 26 |
| 048502 aa | f2 9777 ac | 77 ac f2 97 | fb f2 f2 af | f3 13135918 |
| a1 0005 ff 34 | 3263 cf 18 | 183263 cf | cc 5a 5b cf | $52 \quad 4 \mathrm{e} \quad 20 \quad 76$ |
| ff 086964 |  |  |  |  |
| Ob $\begin{array}{lllll}53 & 34 & 14\end{array}$ |  |  |  |  |
| 84 bf ab 8 f |  |  |  |  |
| 4 a 7 c 43 b 9 |  |  |  |  |



## Avalanche

Effect
in AES:
Change in Key

| Round |  | Number of Bits that Differ |
| :---: | :---: | :---: |
|  | 0123456789 abcdeffedcba9876543210 0123456789 abcdeffedcba9876543210 | 0 |
| 0 | 0e3634aece7225b6f26b174ed92b5588 0f3634aece7225b6f26b174ed92b5588 | 1 |
| 1 | 657470750 fc7ff3fc0e8e8ca4dd02a9c c5a9ad090ec7ff3fc1e8e8ca4cd02a9c | 22 |
| 2 | 5c7bb49a6b72349b05a2317ff46d1294 90905fa9563356d15f3760f3b8259985 | 58 |
| 3 | $7115262448 d c 747 e 5 c d a c 7227 d a 9 b d 9 c$ 18aeb7aa794b3b66629448d575c7cebf | 67 |
| 4 | f867aee8b437a5210c24c1974cffeabc f81015f993c978a876ae017cb49e7eec | 63 |
| 5 | 721 eb200ba06206dcbd4bce704fa654e 5955c91b4e769f3cb4a94768e98d5267 | 81 |
| 6 | 0ad9d85689f9f77bc1c5f71185e5fb14 dc60a24d137662181e45b8d3726b2920 | 70 |
| 7 | db18a8ffa16d30d5f88b08d777ba4eaa fe8343b8f88bef66cab7e977d005a03c | 74 |
| 8 | f91b4fbfe934c9bf8f2f85812b084989 da7dad581d1725c5b72fa0f9d9d1366a | 67 |
| 9 | ccal04a13e678500ff59025f3bafaa34 0ccb4c66bbfd912f4b511d72996345e0 | 59 |
| 10 | ff0b844a0853bf7c6934ab4364148fb9 fc8923ee501a7d207ab670686839996b | 53 |

## Implementation Aspects

- AddRoundKey is a bytewise XOR operation

ShiftRows is a simple byte-shifting operation
SubBytes operates at the byte level and only requires a table of 256 bytes

- MixColumns requires matrix multiplication
- MixColumns only requires multiplication by $\{02\}$ and $\{03\}$, which can be converted to shifts and XORs.
- Designers believe this very efficient implementation was a key factor in its selection as the AES cipher.

Modes of Operation

Modified by: Dr. Ramzi Saifan

## Modes of Operation

To apply a block cipher in a variety of applications, five modes of operation have been defined by NIST.

- The five modes are intended to cover a wide variety of applications of encryption for which a block cipher could be used
- These modes are intended for use with any symmetric block cipher, including triple DES and AES


Codebook Mode (ECB)

(b) Decryption
$\mathrm{C}_{\mathrm{i}}=\mathrm{E}_{\mathrm{K}}\left(\mathrm{P}_{\mathrm{i}}\right)$; the cipher text is $\left(\mathrm{C}_{1}, \ldots, \mathrm{C}_{\mathrm{n}}\right)$

## Security?

- ECB should not be used
- Why?


## The effect of ECB mode


*Images from Wikipedia

## Cipher Block Chaining (CBC)


(a) Encryption

(b) Decryption

IV; $\mathrm{C}_{\mathrm{i}}=\mathrm{E}_{\mathrm{K}}\left(\mathrm{m}_{\mathrm{i}} \oplus \mathrm{C}_{\mathrm{i}-1}\right) ;$ the ciphertext is $\left(\mathrm{IV}, \mathrm{C}_{1}, \ldots, \mathrm{C}_{\mathrm{n}}\right)$

## Cipher Feedback Mode

- For AES, DES, or any block cipher, encryption

There are three modes that make it possible to convert a block cipher into a stream cipher:

Cipher feedback (CFB) mode

Output feedback (OFB) mode

Counter (CTR) mode

## $s$-bit Cipher Feedback (CFB) Mode


(a) Encryption


## Output Feedback (OFB)Mode


(a) Encryption

(b) Decryption

Nonce; $\mathrm{z}_{\mathrm{i}}=\mathrm{E}_{\mathrm{K}}\left(\mathrm{z}_{\mathrm{i}-1}\right) ; \mathrm{C}_{\mathrm{i}}=\mathrm{z}_{\mathrm{i}} \oplus \mathrm{m}_{\mathrm{i}} ;$ the ciphertext is (Nonce, $\left.\mathrm{C}_{1}, \ldots, \mathrm{C}_{\mathrm{n}}\right)$

## Counter (CTR) Mode


(a) Encryption

(b) Decryption

Counter $1 ; \mathrm{z}_{\mathrm{i}}=\mathrm{F}_{\mathrm{K}}(\mathrm{IV}+\mathrm{i}) ; \mathrm{C}_{\mathrm{i}}=\mathrm{z}_{\mathrm{i}} \oplus \mathrm{m}_{\mathrm{i}} ;$ the ciphertext is (Counter1, $\mathrm{C}_{1}, \ldots, \mathrm{C}_{\mathrm{n}}$ )

- Hardware efficiency
- Software efficiency


## Advantages of CTR

- Preprocessing
- Random access
- Provable security
- Simplicity



## Security

- CBC, OFB, and CTR modes are secure against chosen-plaintext attacks

*Images from Wikipedia


## Table 6.1 Block Cipher Modes of Operation

| Mode | Description | Typical Application |
| :--- | :--- | :--- |
| Electronic Codebook (ECB) | Each block of plaintext bits is <br> encoded independently using the <br> same key. | $\bullet$ Secure transmission of <br> single values (e.g., an <br> encryption key) |
| Cipher Block Chaining (CBC) | The input to the encryption <br> algorithm is the XOR of the next <br> block of plaintext and the <br> preceding block of ciphertext. | •General-purpose block- <br> oriented transmission <br> $\bullet$ Authentication |
| Cipher Feedback (CFB) | Input is processed $s$ bits at a time. <br> Preceding ciphertext is used as <br> input to the encryption algorithm <br> to produce pseudorandom output, <br> which is XORed with plaintext to <br> produce next unit of ciphertext. | $\bullet$ General-purpose stream- <br> oriented transmission <br> $\bullet$ Authentication |
| Output Feedback (OFB) | Similar to CFB, except that the <br> input to the encryption algorithm <br> is the preceding encryption <br> output, and full blocks are used. | $\bullet$ Stream-oriented <br> transmission over noisy <br> channel (e.g., satellite <br> communication) |
| Counter (CTR) | Each block of plaintext is XORed <br> with an encrypted counter. The <br> counter is incremented for each <br> subsequent block. | $\bullet$ General-purpose block- <br> oriented transmission <br> $\bullet$ Useful for high-speed <br> requirements |

## Data Integrity

Modified by: Dr. Ramzi Saifan

## Encryption/Decryption

- Provides message confidentiality.
- Does it provide message authentication?


## Message Authentication

- Bob receives a message $m$ from Alice, he wants to know
$\square$ (Data origin authentication) whether the message was really sent by Alice;
$\square$ (Data integrity) whether the message has been modified.
- Solutions:
$\square$ Alice attaches a message authentication code (MAC) to the message.
$\square$ Or she attaches a digital signature to the message.


## Communication without authentication

Very easy..

## Eve

Eve can simply change the message

## Integrity Protection with MAC



MAC (k,M)
Eve
Eve can not forge MAC when $k$ is unknown

## Alice

Key : k
Key : k

Shared key $k$ to generate authenticate message

## MAC Authentication (I)

- MAC allows two or more mutually trusting parties to authenticate messages sent between members

> Only Alice and me know $k$, one of us sent M .

## MAC Authentication (II)

- MAC allows two or more mutually trusting parties to authenticate messages sent between members



## Integrity with Hash



Can we simply send the hash with the message to serve message authentication ?
Ans: No, Eve can change the message and recompute the hash.
Using hash needs more appropriate procedure to guarantee integrity

## Message Authentication Code

$>$ A function of the message and a secret key that produces a fixed-length value that serves as the authenticator
$>$ Generated by an algorithm :
$>$ generated from message + secret key : MAC $=\mathbf{F}(\mathbf{K}, \mathbf{M})$
$>$ A small fixed-sized block of data
$>$ appended to message as a signature when sent
$>$ Receiver performs same computation on message and checks it matches the MAC


## MAC and Encryption

$>$ As shown the MAC provides authentication
$>$ But encryption can also provides authentication!
> Why use a MAC?

- sometimes only authentication is needed
- sometimes need authentication to persist longer than the encryption (eg. archival use)


## MAC Properties

$>$ A MAC is a cryptographic hash

$$
\mathrm{MAC}=\mathrm{C}_{\mathrm{K}}(\mathrm{M})
$$

- condenses a variable-length message M
- using a secret key K
- to a fixed-sized authenticator
$\rightarrow$ A many-to-one function
- potentially many messages have same MAC
- but finding these needs to be very difficult

|  | Bit 1 | Bit 2 | - | Bit n |
| :---: | :---: | :---: | :---: | :---: |
| Block 1 | $b_{11}$ | $b_{21}$ |  | $b_{n 1}$ |
| Block 2 | $b_{12}$ | $b_{22}$ |  | $b_{n 2}$ |
|  | - | - | $\stackrel{\bullet}{\bullet}$ | - |
| Block m | $b_{1 m}$ | $b_{2 m}$ |  | $b_{n m}$ |
| Hash code | $C_{1}$ | $C_{2}$ |  | $C_{n}$ |

Figure 21.1 Simple Hash Function Using Bitwise XOR

## Keyed Hash Functions as MACs

$>$ Want a MAC based on a hash function

- because hash functions are generally faster
- crypto hash function code is widely available
- But hashing is internally has no key!
> Original proposal:
KeyedHash = Hash (Key|Message)
- some weaknesses were found with this
> Eventually led to development of HMAC


## Security requirements

- Pre-image: if $h(m)=y, m$ is a pre-image of $y$.
- Each hash value typically has multiple pre-images.
- Collision: a pair of $\left(m, m^{\prime}\right), m \neq m^{\prime}$, s.t. $h(m)=h\left(m^{\prime}\right)$.

A hash function is said to be:

- Pre-image resistant if it is computationally infeasible to find a pre-image of a hash value.
- Collision resistant if it is computationally infeasible to find a collision.
- A hash function is a cryptographic hash function if it is collision resistant.


## To be useful for message authentication, a hash function H must have the following properties:



## Birthday Problem

- Birthday problem: In a group of $k$ people, what is the probability that at least two people have the same birthday?
$\square$ Having the same birthday is a collision?
- Birthday paradox: $p \geq 1 / 2$ with $k$ as small as 23 .
- Consider a hash function $h:\{0,1\}^{*} \rightarrow\{0,1\}^{n}$.
- If we randomly generate $k$ messages, the probability of having a collision depends on $n$.
- To resist birthday attack, we choose $n$ to be sufficiently large that it will take an infeasibly large $k$ to have a non-negligible probability of collision.


## Collision-resistant hash functions

- Collision-resistant hash functions can be built from collision-resistant compression functions using Merkle-Damgard construction.


## Merkle-Damgard Construction



Compression function $f:\{0,1\}^{n+b} \rightarrow\{0,1\}^{n}$

- Insecure: $M A C_{k}(m)=h(m)$ with $\mathrm{IV}=k$.
(For simplicity, without padding)

- Easy to forge:
( $\left.m^{\prime}, h_{k}\left(m^{\prime}\right)\right)$,
where $m^{\prime}=m \square m_{s+1}$



## CMAC (Cipher-based MAC)

- "Hashless" MAC
- Uses an encryption algorithm (DES, AES, etc.) to generate MAC
- Based on same idea as cipher block chaining
- Compresses result to size of single block (unlike encryption


## CBC CMAC Overview



## CMAC Facts

- Advantages:
- Can use existing encryption functions
- Encryption functions have properties that resist preimage and collision attacks
- Most exhibit strong avalanche effect - minor change in message gives great change in resulting MAC
- Disadvantage:
- Encryption algorithms (particularly when chained) can be much slower than hash algorithms


## HMAC

- Interest in developing a MAC derived from a cryptographic hash code
- Cryptographic hash functions generally execute faster
- Library code is widely available
- SHA-1 was not deigned for use as a MAC because it does not rely on a secret key
- Issued as RFC2014
- Has been chosen as the mandatory-toimplement MAC for IP security
- Used in other Internet protocols such as Transport Layer Security (TLS) and Secure Electronic Transaction (SET)


## HMAC

- $\operatorname{HMAC}(K, m)=H\left(\quad\left(K^{\prime} \oplus\right.\right.$ opad $) \| \quad H\left(\left(K^{\prime} \oplus\right.\right.$ ipad $\left.\left.) \| m\right) \quad\right)$, where
- $H$ : is a cryptographic hash function, composed of multiple rounds with operations AND, OR, XOR, NOT, and SHIFT. Very efficient to compute.
- $K$ : is the secret key,
- $M$ : is the message to be authenticated,
- $K^{\prime}$ : is another secret key, derived from the original key $K$ (by padding $K$ to the right with extra zeroes to the input block size of the hash function, or by hashing $K$ if it is longer than that block size,
- || denotes concatenation,
- opad is the outer padding ( $0 x 5 \mathrm{c} 5 \mathrm{c} 5 \mathrm{c} \ldots 5 \mathrm{c} 5 \mathrm{c}$, one-block long constant), and
- ipad is the inner padding ( $0 \times 363636 \ldots 3636$, one-block long constant).



## Hash functions in practice

- MD5
- 128-bit output
- Introduced in 1991...collision attacks found in 2004...several extensions and improvements since then
- Still widely deployed(!)
- SHA-1
- 160-bit output
- No collisions known, but theoretical attacks exist
- SHA-2
- 256-/512-bit outputs


## Secure Hash Algorithm (SHA)

- SHA was originally developed by NIST
- Published as FIPS 180 in 1993
- Was revised in 1995 as SHA-1
- Produces 160-bit hash values
- NIST issued revised FIPS 180-2 in 2002
- Adds 3 additional versions of SHA
- SHA-256, SHA-384, SHA-512
- With 256/384/512-bit hash values
- Same basic structure as SHA-1 but greater security
- The most recent version is FIPS 180-4 which added two variants of SHA-512 with 224-bit and 256-bit hash sizes


## Comparison of SHA Parameters

| SHA-1 | SHA-224 | SHA-256 | SHA-384 | SHA-512 | SHA- <br> $\mathbf{5 1 2 / 2 2 4}$ | SHA- <br> $\mathbf{5 1 2 / 2 5 t}$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Message <br> size | $<2^{64}$ | $<2^{64}$ | $<2^{64}$ | $<2^{128}$ | $<2^{128}$ | $<2^{128}$ | $<2^{128}$ |
| Word <br> size | 32 | 32 | 32 | 64 | 64 | 64 | 64 |
| Block <br> size | 512 | 512 | 512 | 1024 | 1024 | 1024 | 1024 |
| Message <br> digest <br> size | 160 | 224 | 256 | 384 | 512 | 224 | 256 |
| Number <br> of steps | 80 | 64 | 64 | 80 | 80 | 80 | 80 |
| Security | 80 | 112 | 128 | 192 | 256 | 112 | 128 |

1. All sizes are measured in bits.
2. Security refers to the fact that a birthday attack on a message digest of size $n$ produces a collision with a work factor of approximately $2^{n / 2}$.


Figure 21.2 Message Digest Generation Using SHA-512


Figure 21.3 SHA-512 Processing of a Single 1024-Bit Block

## SHA-3

$\checkmark$ SHA-2 shares same structure and mathematical operations as its predecessors and causes concern
$\checkmark$ Due to time required to replace SHA-2 should it become vulnerable, NIST announced in 2007 a competition to produce SHA-3

## Requirements:

- Must support hash value lengths of $224,256,384$, and 512 bits
- Algorithm must process small blocks at a time instead of requiring the entire message to be buffered in memory before processing it


## Hash Function

- The ideal cryptographic hash function has four main properties:

1) it is quick to compute the hash value for any given message
2) it is infeasible to generate a message from its hash value except by trying all possible messages
3) a small change to a message should change the hash value so extensively
4) it is infeasible to find two different messages with the same hash value

## Encryption + integrity

$>$ simultaneously protect confidentiality and authenticity of communications

- often required but usually separate
$>$ approaches
- Hash-then-encrypt: $\mathrm{E}_{\mathrm{K}}(\mathrm{M} \| \mathrm{H}(\mathrm{M}))$
- MAC-then-encrypt: $\mathrm{E}_{\mathrm{K} 2}\left(\mathrm{M} \| \mathrm{MAC}_{\mathrm{K} 1}(\mathrm{M})\right)$
- Encrypt-then-MAC: $\left(\mathrm{C}=\mathrm{E}_{\mathrm{K} 2}(\mathrm{M}), \mathrm{T}=\mathrm{MAC}_{\mathrm{K} 1}(\mathrm{C})\right.$
- Encrypt-and-MAC: $\left(\mathrm{C}=\mathrm{E}_{\mathrm{K} 2}(\mathrm{M}), \mathrm{T}=\mathrm{MAC}_{\mathrm{K} 1}(\mathrm{M})\right.$
> decryption/verification straightforward
> but security vulnerabilities with all these


## Replay attacks

- A MAC inherently cannot prevent replay attacks
- Replay attacks must be prevented at a higher level of the protocol!
- (Note that whether a replay is ok is applicationdependent.)
- Replay attacks can be prevented using nonces, timestamps, etc.


# Public Key Encryption 

Modified by: Dr. Ramzi Saifan

## Prime Numbers

Prime numbers only have divisors of 1 and itself

- They cannot be written as a product of other numbers

Any integer a > 1 can be factored in a unique way as

$$
\mathrm{a}={ }_{\mathrm{p} 1}{ }^{\mathrm{a} 1} * \mathrm{p}_{2}{ }^{\mathrm{a} 2} * \ldots * \mathrm{p}_{\mathrm{p} 1}{ }^{\mathrm{a} 1}
$$

where $\mathrm{p}_{1}<\mathrm{p}_{2}<\ldots<\mathrm{p}_{\mathrm{t}}$ are prime numbers and where each $\mathrm{a}_{\mathrm{i}}$ is a positive integer

This is known as the fundamental theorem of arithmetic

## Table 8.1

## Primes Under 2000

| 2 | 101 | 211 | 307 | 401 | 503 | 601 | 701 | 809 | 907 | 1009 | 1103 | 1201 | 1301 | 1409 | 1511 | 1601 | 1709 | 1801 | 1901 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 103 | 223 | 311 | 409 | 509 | 607 | 709 | 811 | 911 | 1013 | 1109 | 1213 | 1303 | 1423 | 1523 | 1607 | 1721 | 1811 | 1907 |
| 5 | 107 | 227 | 313 | 419 | 521 | 613 | 719 | 821 | 919 | 1019 | 1117 | 1217 | 1307 | 1427 | 1531 | 1609 | 1723 | 1823 | 1913 |
| 7 | 109 | 229 | 317 | 421 | 523 | 617 | 727 | 823 | 929 | 1021 | 1123 | 1223 | 1319 | 1429 | 1543 | 1613 | 1733 | 1831 | 1931 |
| 11 | 113 | 233 | 331 | 431 | 541 | 619 | 733 | 827 | 937 | 1031 | 1129 | 1229 | 1321 | 1433 | 1549 | 1619 | 1741 | 1847 | 1933 |
| 13 | 127 | 239 | 337 | 433 | 547 | 631 | 739 | 829 | 941 | 1033 | 1151 | 1231 | 1327 | 1439 | 1553 | 1621 | 1747 | 1861 | 1949 |
| 17 | 131 | 241 | 347 | 439 | 557 | 641 | 743 | 839 | 947 | 1039 | 1153 | 1237 | 1361 | 1447 | 1559 | 1627 | 1753 | 1867 | 1951 |
| 19 | 137 | 251 | 349 | 443 | 563 | 643 | 751 | 853 | 953 | 1049 | 1163 | 1249 | 1367 | 1451 | 1567 | 1637 | 1759 | 1871 | 1973 |
| 23 | 139 | 257 | 353 | 449 | 569 | 647 | 757 | 857 | 967 | 1051 | 1171 | 1259 | 1373 | 1453 | 1571 | 1657 | 1777 | 1873 | 1979 |
| 29 | 149 | 263 | 359 | 457 | 571 | 653 | 761 | 859 | 971 | 1061 | 1181 | 1277 | 1381 | 1459 | 1579 | 1663 | 1783 | 1877 | 1987 |
| 31 | 151 | 269 | 367 | 461 | 577 | 659 | 769 | 863 | 977 | 1063 | 1187 | 1279 | 1399 | 1471 | 1583 | 1667 | 1787 | 1879 | 1993 |
| 37 | 157 | 271 | 373 | 463 | 587 | 661 | 773 | 877 | 983 | 1069 | 1193 | 1283 |  | 1481 | 1597 | 1669 | 1789 | 1889 | 1997 |
| 41 | 163 | 277 | 379 | 467 | 593 | 673 | 787 | 881 | 991 | 1087 |  | 1289 |  | 1483 |  | 1693 |  |  | 1999 |
| 43 | 167 | 281 | 383 | 479 | 599 | 677 | 797 | 883 | 997 | 1091 |  | 1291 |  | 1487 |  | 1697 |  |  |  |
| 47 | 173 | 283 | 389 | 487 |  | 683 |  | 887 |  | 1093 |  | 1297 |  | 1489 |  | 1699 |  |  |  |
| 53 | 179 | 293 | 397 | 491 |  | 691 |  |  |  | 1097 |  |  |  | 1493 |  |  |  |  |  |
| 59 | 181 |  |  | 499 |  |  |  |  |  |  |  |  |  | 1499 |  |  |  |  |  |
| 61 | 191 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 67 | 193 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 71 | 197 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 73 | 199 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 79 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 83 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 89 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 97 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Miller-Rabin Algorithm

Typically used to test a large number for primality
Algorithm is: TEST ( $n$ )

- Find integers $k$, $q$, with $k>0, q$ odd, so that $(n-1)=2^{k} q$;
- Select a random integer $a, 1<a<n-1$;
- if $a^{q} \bmod n=1$ then
- return ("inconclusive");
$-\mathbf{f o r} j=0$ to $k-1$ do
- if $\left(a^{2 j q} \bmod n=n-1\right)$ then
- return ("inconclusive") ;
- return ("composite") ;


## Miller Rabin Usage

- It can be shown that given an odd number $n$ that is not prime and a randomly chosen integer, a with $1<a<n-1$, the probability that TEST will return inconclusive (i.e., fail to detect that $n$ is not prime) is less than 1/4.
- Thus, if $t$ different values of $a$ are chosen, the probability that all of them will pass TEST (return inconclusive) for $n$ is less than $(1 / 4)^{\mathrm{t}}$. For example, for $t=10$, the probability that a nonprime number will pass all ten tests is less than $10^{-6}$.
- Thus, for a sufficiently large value of $t$, we can be confident that $n$ is prime if Miller's test always returns inconclusive .
- invoke TEST ( $n$ ) using randomly chosen values for a . If, at any point, TEST returns composite, then $n$ is determined to be nonprime. If TEST continues to return inconclusive for $t$ tests, then for a sufficiently large value of $t$, assume that $n$ is prime.


## Deterministic Primality Algorithm

Prior to 2002 there was no known method of efficiently proving the primality of very large numbers

All of the algorithms in use produced a probabilistic result

In 2002 Agrawal, Kayal, and Saxena developed an algorithm that efficiently determines whether a given large number is prime

- Known as the AKS algorithm
- Does not appear to be as efficient as Miller-Rabin algorithm



Figure 9.1 Public-Key Cryptography

## Public-Key Cryptosystem: Confidentiality



## Public-Key Cryptosystem: Authentication



## Public-Key Cryptosystem: Authentication and Confidentiality

Source A


## Public-Key Requirements

Conditions that these algorithms must fulfill:

- It is computationally easy for a party B to generate a pair (public-key $P U_{b}$, private key $\mathrm{PR}_{b}$ )
- It is computationally easy for a sender A, knowing the public key and the message to be encrypted, to generate the corresponding ciphertext
- It is computationally easy for the receiver B to decrypt the resulting ciphertext using the private key to recover the original message
- It is computationally infeasible for an adversary, knowing the public key, to determine the private key
- It is computationally infeasible for an adversary, knowing the public key and a ciphertext, to recover the original message
- The two keys can be applied in either order


## Public-Key Requirements

- Need a trap-door one-way function
- A one-way function is one that maps a domain into a range such that every function value has a unique inverse, with the condition that the calculation of the function is easy, whereas the calculation of the inverse is infeasible
- $Y=f(X)$ easy
- $\mathrm{X}=\mathrm{f}^{-1}(\mathrm{Y})$ infeasible
- A trap-door one-way function is a family of invertible functions $\mathrm{f}_{\mathrm{k}}$, such that
- $Y=f_{k}(X)$ easy, if $k$ and $X$ are known
- $\mathrm{X}=\mathrm{f}_{\mathrm{k}}{ }^{-1}(\mathrm{Y})$ easy, if k and Y are known
$-X=f_{k}^{-1}(Y)$ infeasible, if $Y$ known but $k$ not known
- A practical public-key scheme depends on a suitable trap-door one-way function


## Rivest-Shamir-Adleman (RSA) Scheme

- Developed in 1977 at MIT by Ron Rivest, Adi Shamir \& Len Adleman
- Most widely used general-purpose approach to public-key encryption
- Is a cipher in which the plaintext and ciphertext are integers between 0 and $n-1$ for some $n$
- A typical size for $n$ is 1024 bits, or 309 decimal digits


## Table 8.2

Some Values of Euler's Totient Function $\phi(n)$

| $n$ | $\phi(n)$ |
| :---: | :---: |
| 1 | 1 |
| 2 | 1 |
| 3 | 2 |
| 4 | 2 |
| 5 | 4 |
| 6 | 2 |
| 7 | 6 |
| 8 | 4 |
| 9 | 6 |
| 10 | 4 |


| $n$ | $\phi(n)$ |
| :---: | :---: |
| 11 | 10 |
| 12 | 4 |
| 13 | 12 |
| 14 | 6 |
| 15 | 8 |
| 16 | 8 |
| 17 | 16 |
| 18 | 6 |
| 19 | 18 |
| 20 | 8 |


| $n$ | $\phi(n)$ |
| :---: | :---: |
| 21 | 12 |
| 22 | 10 |
| 23 | 22 |
| 24 | 8 |
| 25 | 20 |
| 26 | 12 |
| 27 | 18 |
| 28 | 12 |
| 29 | 28 |
| 30 | 8 |

## RSA Algorithm

- RSA makes use of an expression with exponentials
- Plaintext is encrypted in blocks with each block having a binary value less than some number $n$
- Encryption and decryption are of the following form, for some plaintext block $M$ and ciphertextblock C

$$
\begin{aligned}
& C=M^{e} \bmod n \\
& M=C^{d} \bmod n=\left(M^{e}\right)^{d} \bmod n=M^{e d} \bmod n
\end{aligned}
$$

- Both sender and receiver must know the value of $n$
- The sender knows the value of $e$, and only the receiver knows the value of $d$
- This is a public-key encryption algorithm with a public key of $P U=\{e, n\}$ and a private key of $P R=\{d, n\}$


## Algorithm Requirements

For this algorithm to be satisfactory for publickey encryption, the following requirements must be met:

1. It is possible to find values of $e, d, n$ such that $M^{e d} \bmod n=M$ for all $M<n$
2. It is relatively easy to calculate $M^{e} \bmod$ $n$ and $C^{d} \bmod n$ for all values of $M<n$
3. It is infeasible to determine $d$ given $e$ and $n$


## Key Generation by Alice



| $\quad$ Key Generation by Alice |  |
| :--- | :--- |
| Select $p, q$ | $p$ and $q$ both prime, $p \neq q$ |
| Calculate $n=p \times q$ |  |
| Calculate $\phi(n)=(p-1)(q-1)$ |  |
| Select integer $e$ | $\operatorname{gcd}(\phi(n), e)=1 ; 1<e<\phi(n)$ |
| Calculate $d$ | $d=e^{-1}(\bmod \phi(n))$ |
| Public key | $P U=\{e, n\}$ |
| Private key | $P R=\{d, n\}$ |

## Encryption by Bob with Alice's Public Key

| Plaintext: | $M<n$ |
| :--- | :--- |
| Ciphertext: | $C=M^{e} \bmod n$ |

## Decryption by Alice with Alice's Private Key

Ciphertext:

Plaintext:

$$
M=C^{d} \bmod n
$$

## Example of RSA Algorithm



Figure 9.6 Example of RSA Algorithm

(a) General approach

(b) Example

Figure 9.7 RSA Processing of Multiple Blocks

## Fermat's Theorem

- States the following:
- If $p$ is prime and $a$ is a positive integer not divisible by $p$ then

$$
\mathrm{a}^{\mathrm{p}-1}=1(\bmod p)
$$

- Sometimes referred to as Fermat's Little Theorem

An alternate form is:

- If $p$ is prime and $a$ is a positive integer then

$$
a^{\mathrm{p}}=a(\bmod p)
$$

Plays an important role in public-key cryptography

## Euler's Theorem

- States that for every $a$ and $n$ that are relatively prime:

$$
a^{\phi(\mathrm{n})}=1(\bmod n)
$$

- An alternative form is:

$$
a^{\phi(\mathrm{n})+1}=a(\bmod n)
$$

## Chinese Remainder Thm

- If $p$ and $q$ are prime, then for all $x$ and $a$ :
$-x=a(\bmod p)$ and $x=a(\bmod q)$ iff $x=a \bmod (p q)$
- Example:
- Suppose that $\mathrm{n}=2501=61 * 41$
- To calculate $V \bmod 2501$ :
- $V \bmod 61$
- $V \bmod 41$


## Correctness of RSA

- To show RSA is correct, we must show that encryption and decryption are inverse functions:
$-\operatorname{En}(\operatorname{De}(M))=\operatorname{De}(\operatorname{En}(M))=M=M^{\text {ed }}(\bmod n)$
- Since d and e are multiplicative inverses $\bmod \phi(n)$, there is a $k$ such that:
- $e d=1+k * \phi(\mathrm{n}),=1+\mathrm{k}(\mathrm{p}-1)(\mathrm{q}-1)$
- $M^{e d}=M^{1+k(p-1)(q-1)}=M^{*}\left(M^{p-1}\right)^{k(q-1)}$
- By Fermat: $\mathrm{M}^{\mathrm{p}-1}=1(\bmod p)$
- $\mathrm{M}^{\text {ed }}=\mathrm{M}(1)^{\mathrm{k}(\mathrm{q}-1)}(\bmod \mathrm{p})=\mathrm{M}(\bmod \mathrm{p})$


## Correctness of RSA

- $\mathrm{M}^{\mathrm{ed}}=\mathrm{M}(1)^{\mathrm{k}(\mathrm{q}-1)}(\bmod \mathrm{p})=\mathrm{M}(\bmod \mathrm{p})$
- $\mathrm{M}^{\mathrm{ed}}=\mathrm{M}(1)^{\mathrm{k}(\mathrm{q}-1)}(\bmod \mathrm{q})=\mathrm{M}(\bmod \mathrm{q})$
- By Chinese Remainder Thm, we get:
- $\mathrm{M}^{\wedge}\{\mathrm{ed}\}=\mathrm{M}(\bmod \mathrm{p})=\mathrm{M}(\bmod \mathrm{q})=$ $\mathrm{M}(\bmod \mathrm{pq})=\mathrm{M}(\bmod \mathrm{n})$
- Therefore, RSA reproduces the original message and is correct.


## Exponentiation in Modular Arithmetic

- Both encryption and decryption in RSA involve raising an integer to an integer power, $\bmod n$
- Can make use of a property of modular arithmetic:
$[(a \bmod n) x(b \bmod n)] \bmod n=(a x b) \bmod n$
- With RSA you are dealing with potentially large exponents so efficiency of exponentiation is a consideration


## Fast Exponentiation Algorithm

$$
\begin{aligned}
& f=1 \\
& \text { for }(i=k ; i>0 ; i--) \\
& \qquad \begin{array}{l}
f=(f * f) \bmod n ; \\
\\
\quad i f\left(b_{i}==1\right) \\
\\
f=(f * a) \bmod n ;
\end{array}
\end{aligned}
$$

return f;
Algorithm for computing $a^{b} \bmod n, b$ is expressed as a binary

$$
b_{k} b_{k-1} \ldots b_{0}
$$

| $i$ | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $b_{i}$ | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| $c$ | 1 | 2 | 4 | 8 | 17 | 35 | 70 | 140 | 280 | 560 |
| $f$ | 7 | 49 | 157 | 526 | 160 | 241 | 298 | 166 | 67 | 1 |

Result of the Fast Modular Exponentiation Algorithm for $a^{b} \bmod n$, where $a=7, b=560=1000110000$, and $n=561$

## Euclidean Algorithm

Ex: Find $\operatorname{gcd}(421,111)$. use the Euclidean algorithm as follows:

$$
\begin{aligned}
& 421=111 \times 3+88 \\
& 111=88 \times 1+23 \\
& 88=23 \times 3+19 \\
& 23=19 \times 1+4 \\
& 19=4 \times 4+3 \\
& 4=3 \times 1+1 \\
& 3=1 \times 3+0
\end{aligned}
$$

The last non-zero remainder is 1 and therefore $\operatorname{gcd}(421,111)=1$.

## Extended Euclidean Algorithm

The following table can be used to calculate the the Euclidean algorithm and the Extended Euclidean algorithm

| i | Quotient $\mathrm{q}_{\mathrm{i}-1}$ | Remainder $\mathrm{r}_{\mathrm{i}}$ | $\mathrm{S}_{\mathrm{i}}$ | $\mathrm{t}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | - | $\square a$ | $-1$ | $0$ |
| 1 |  | $C^{\mathrm{b}}$ | $10$ | $\int 1$ |
| 2 | $\square \div \square=\square$ | $-\square \star \square=\square$ | $\square-\square * \square=\square$ | $\square-\square * \square=\square$ |
| 3 | $\square$ |  |  |  |
| 4 |  |  |  |  |

## Example

$$
a=31 \quad b=12
$$

| $i$ | Quotient $q_{i-1}$ | Remainder $r_{i}$ | $S_{i}$ | $t_{i}$ |
| :---: | :--- | :--- | :--- | :---: |
| 0 | - | 31 | 1 | 0 |
| 1 | - | 12 | 0 | 1 |
| 2 | $31 \div 12=2$ | $31-2^{*} 12=7$ | $1-0^{*} 2=1$ | $0-1^{*} 2=-2$ |
| 3 | $12 \div 7=1$ | $12-1^{*} 7=5$ | $0-1^{*} 1=-1$ | $1-1^{*}(-2)=3$ |
| 4 | $7 \div 5=1$ | $7-1^{*} 5=2$ | $1-1^{*}(-1)=2$ | $-2-1^{*} 3=-5$ |
| 5 | $5 \div 2=2$ | $5-2^{*} 2=1$ | $-1-2^{*} 2=-5$ | $3-(-10)=13$ |
|  | $2 \div 1=2$ | $2-1^{*} 2=0$ |  |  |

## Efficient Operation Using the Public Key

- To speed up the operation of the RSA algorithm using the public key, a specific choice of $e$ is usually made
- The most common choice is $65537\left(2^{16}+1\right)$
- Two other popular choices are $e=3$ and $e=17$
- Each of these choices has only two 1 bits, so the number of multiplications required to perform exponentiation is minimized
- With a very small public key, such as $e=3$, RSA becomes vulnerable to a simple attack


## Key Generation

- Before the application of the public-key cryptosystem each participant must generate a pair of keys:
- Determine two prime numbers $p$ and $q$
- Select either $e$ or $d$ and calculate the other
- Because the value of $n=p q$ will be known to any potential adversary, primes must be chosen from a sufficiently large set
- The method used for finding large primes must be reasonably efficient


## Public-Key Cryptanalysis

A public-key encryption scheme is vulnerable to a brute-force attack

- Countermeasure: use large keys
- Key size must be small enough for practical encryption and decryption
- Key sizes that have been proposed result in encryption/decryption speeds that are too slow for general-purpose use
- Public-key encryption is currently confined to key management and signature applications

Another form of attack is to find some way to compute the private key given the public key

- To date it has not been mathematically proven that this form of attack is infeasible for a particular public-key algorithm

Finally, there is a probable-message attack

- This attack can be thwarted by appending some random bits to simple messages



## Factoring Problem

We can identify three approaches to attacking RSA mathematically:

- Factor $n$ into its two prime factors. This enables calculation of $\varnothing(n)=(p-1) x(q-1)$, which in turn enables determination of $d=e^{-1}(\bmod \varnothing(\mathrm{n}))$
- Determine $\varnothing(\mathrm{n})$ directly without first determining $p$ and $q$. Again this enables determination of $d=e^{-1}$ $(\bmod \emptyset(\mathrm{n}))$
- Determine $d$ directly without first determining $\varnothing(\mathrm{n})$

| Number of <br> Decimal Digits | Number of Bits | Date Achieved |
| :---: | :---: | :---: |
| 100 | 332 | April 1991 |
| 110 | 365 | April 1992 |
| 120 | 398 | June 1993 |
| 129 | 428 | April 1994 |
| 130 | 431 | April 1996 |
| 140 | 512 | February 1999 |
| 155 | 530 | August 1999 |
| 160 | 676 | December 2003 |
| 174 | 640 | May 2005 |
| 200 | 768 | November 2005 |
| 193 | 232 | $403 b e r ~ 2009$ |

Table 9.5 Progress in RSA Factorization

MIPS-
Years
Needed
to
Factor


Figure 9.9 MIPS-years Needed to Factor

## Timing Attacks

- Paul Kocher, a cryptographic consultant, demonstrated that a snooper can determine a private key by keeping track of how long a computer takes to decipher messages
- Are applicable not just to RSA but to other public-key cryptography systems
- Are alarming for two reasons:
- It comes from a completely unexpected direction
- It is a ciphertext-only attack



## Countermeasures

## Constant

exponentiation time

- Ensure that all exponentiations take the same amount of time before returning a result; this is a simple fix but does degrade performance

Random delay

- Better performance could be achieved by adding a random delay to the exponentiation algorithm to confuse the timing attack

Blinding

- Multiply the ciphertext by a random number before performing exponentiation; this process prevents the attacker from knowing what ciphertext bits are being processed inside the computer and therefore prevents the bit-by-bit analysis essential to the timing attack


# Misconceptions Concerning Public-Key Encryption 

- Public-key encryption is more secure from cryptanalysis than symmetric encryption
- Public-key encryption is a general-purpose technique that has made symmetric encryption obsolete
- There is a feeling that key distribution is trivial when using public-key encryption, compared to the cumbersome handshaking involved with key distribution centers for symmetric encryption


## Terminology Related to Asymmetric Encryption

## Asymetric Keys

Two related keys, a public key and a private key that are used to perform complementary operations, such as encryption and decryption or signature generation and signature verification.

## Public Key Certificate

\& digital document issued and digitally signed by the private key of a Certification authority that binds the name of a subscriber to a public key. The certificate indicates that the subscriber identified in the certificate has sole control and access to the corresponding private key.

Public Key (Asymetric) Cryptographic Algorithm
A cryptographic algorithm that uses two related keys, a public key and a private key. The two keys have the property that deriving the private key from the public key is computationally infeasible.

## Principles of Public-Key Cryptosystems

- The concept of public-key cryptography evolved from an attempt to attack two of the most difficult problems associated with symmetric encryption:


## Key distribution

- How to have secure communications in general without having to trust a KDC with your key


## Digital signatures

- How to verify that a message comes intact from the claimed sender
- Whitfield Diffie and Martin Hellman from Stanford University achieved a breakthrough in 1976 by coming up with a method that addressed both problems and was radically different from all previous approaches to cryptography

End

## Questions

## The Diffie-Hellman Algorithm

Modified by: Dr. Ramzi Saifan

## Introduction

- Discovered by Whitfield Diffie and Martin Hellman - "New Directions in Cryptography"
- The point is to agree on a key that two parties can use for a symmetric encryption, in such a way that an eavesdropper cannot obtain the key.
- Diffie-Hellman key agreement protocol
- Exponential key agreement
- Allows two users to exchange a secret key
- Requires no prior secrets
- Real-time over an un-trusted network


## Introduction

- Based on the difficulty of computing discrete logarithms of large numbers.
- Requires two large numbers, one prime (P), and (G), a primitive root of P


## Implementation

- p and g are both publicly available numbers - P is at least 512 bits
- Alice picks a private value "a" and send to Bob
$-\mathrm{A}=\mathrm{g}^{\mathrm{a}} \bmod \mathrm{p}$
- Bob picks a private value "b" and sends to Alice:
$-\mathrm{B}=\mathrm{g}^{\mathrm{b}} \bmod \mathrm{p}$


## Implementation

- Compute shared, private key:
- Alice received B and knows a, p and g, so she calculates:
- $K_{a}=B^{a} \bmod p$
- Bob received A and knows b, p and g, so he calculates:
- $K_{b}=A^{b} \bmod p$
- Algebraically it can be shown that $\mathrm{K}_{\mathrm{a}}=\mathrm{K}_{\mathrm{b}}=\mathrm{K}$
- Users now have a symmetric secret key to encrypt
Alice

$a, g, p$
$A=g^{a} \operatorname{mood} p$
$A, g, p$

B

$$
K=B^{a} \operatorname{mood} p \quad K=A^{b} \operatorname{mood} p
$$

## Example

- Bob and Alice are unable to talk on the untrusted network.
-Who knows who's listening?



## Example

- Alice and Bob get public numbers

$$
-\mathrm{P}=23, \mathrm{G}=9
$$

- Alice and Bob compute public values
$-\mathrm{A}=9^{4} \bmod 23=6561 \bmod 23=6$
$-\mathrm{B}=9^{3} \bmod 23=729 \bmod 23=16$
- Alice and Bob exchange public numbers


## Example

- Alice and Bob compute symmetric keys
$-\mathrm{k}_{\mathrm{a}}=\mathrm{B}^{\mathrm{a}} \bmod \mathrm{p}=16^{4} \bmod 23=9$
$-\mathrm{k}_{\mathrm{b}}=\mathrm{A}^{\mathrm{b}} \bmod \mathrm{p}=6^{3} \bmod 23=9$
- Alice and Bob now can talk securely!


## Security of DH

- Suppose $\mathbf{p}$ is a prime of around 300 digits,
- and $\mathbf{a}$ and $\mathbf{b}$ at least 100 digits each.
- Discovering the shared secret given $\mathbf{g}, \mathbf{p}, \mathbf{g}^{\mathbf{a}} \mathbf{m o d}$ $\mathbf{p}$, and $\mathbf{g}^{\mathbf{b}} \bmod \mathbf{p}$ would take longer than the lifetime of the universe, using the best known algorithm.
- This is called the discrete logarithm problem.


## Man in the middle attack



## Applications

- Diffie-Hellman is currently used in many protocols, namely:
- Secure Sockets Layer (SSL)/Transport Layer Security (TLS)
- Secure Shell (SSH)
- Internet Protocol Security (IPSec)
- Public Key Infrastructure (PKI)


## User Authentication

Modified By: Dr. Ramzi Saifan

## Authentication

- Verifying the identity of another entity
- Computer authenticating to another computer
- Person authenticating to a local/remote computer
- Important to be clear about what is being authenticated
- The user?
- The machine? A specific application on the machine?
- The data?
- Mutual authentication vs. unidirectional authentication


## Remote User-Authentication Principles

- An authentication process consists of two steps:



## Authentication

- Authentication may be based on

1. What you know
2. What you have
3. What you are
4. What you do

- Examples? Tradeoffs?
- Others?


## Address-based authentication

- Is sometimes used
- Generally not very secure
- Relatively easy to forge source addresses of network packets
- But can be useful if the adversary does not know what IP address to forge
- E.g., IP address of a user's home computer


## Multi-factor Authentication



Figure 3.2 Multifactor Authentication

## Password-based protocols

- Basic idea
- User has a secret password
- System checks password to authenticate user
- Issues
- How is password stored?
- How does system check password?
- How easy is it to guess a password?
- Difficult to keep password file secret, so best if it is hard to guess password even if you have the password file
- Distinguish on-line attacks vs. off-line attacks


## Basic password scheme

## User

## Password file


hash function

$$
\begin{gathered}
\text { exrygbzyf } \\
\text { kgnosfix } \\
\text { ggjoklbsz }
\end{gathered}
$$

## Basic password scheme

- Hash function $\mathrm{h}:$ strings $\rightarrow$ strings
- Given h(password), hard to find password
- No known algorithm better than trial and error
- User password stored as h(password)
- When user enters password
- System computes h(password)
- Compares with entry in password file
- No passwords stored on disk


## Unix password system

- In past UNIX systems, password used modified DES (encryption algorithm) as if it were a hash function
- Encrypts NULL string using password as the key (truncates passwords to 8 characters!)
- Caused artificial slowdown: ran DES 25 times
- Also stored password file in directory: /etc/passwd/
- World-readable (anyone who accessed the machine would be able to copy the password file to crack at their leisure)
- Contained userIDs/groupIDs used by many system programs
- Can instruct modern UNIXes to use MD5 hash function


Figure 3.3 UNIX Password Scheme

## Improved Implementations

Much stronger hash/salt schemes available for

Unix


OpenBSD uses Blowfish block cipher based hash algorithm called Bcrypt

- Most secure version of Unix hash/salt scheme
- Uses 128 -bit salt to create bit hash value

Recommended hash
function is based on MD5
-Salt of up to 48-bits
-Password length is unlimited
-Produces 128 -bit hash
-Uses an inner loop with 1000
iterations to achieve slowdown

## Windows NT/2k/XP/Vista Password

- Uses 2 functions for "hashing" passwords:

1. LAN Manager hash (LM hash)

- Password is padded with zeros until there are 14 characters.
- It is then converted to uppercase and split into two 7-character pieces
- Each half is encrypted using an 8-byte DES (data encryption standard) key
- Result is combined into a 16-byte, one way hash value

2. NT hash (NT hash)

- Converts password to Unicode and uses MD4 hash algorithm to obtain a 16-byte value
- Hashes stored in Security Accounts Manager (SAM)
- Locked within system kernel when system is running.
- Location - C:IWINNT\SYSTEM32\CONFIG
- SYSKEY
- Utility which moves the encryption key for the SAM database off of the computer


## Password Vulnerabilities



## Password selection

- User selection of passwords is typically very poor
- Lower entropy password makes dictionary attacks easier
- Typical passwords:
- Derived from account names or usernames
- Dictionary words, reversed dictionary words, or small modifications of dictionary words
- Users typically use the same password for multiple accounts
- Weakest account determines the security!


## Better password selection

- Non-alphanumeric characters
- Longer phrases
- Can try to enforce good password selection...
- ...but these types of passwords are difficult for people to memorize and type!


## Dictionary Attack - some numbers

- Typical password dictionary
- 1,000,000 entries of common passwords
- people's names, common pet names, and ordinary words.
- Suppose you generate and analyze 10 guesses per second
- This may be reasonable for a web site; offline is much faster
- Dictionary attack in at most 100,000 seconds $=28$ hours, or 14 hours on average
- If passwords were random
- Assume six-character password
- Upper- and lowercase letters, digits, 32 punctuation characters
- 689,869,781,056 password combinations.
- Exhaustive search requires 1,093 years on average


## Password-based protocols

- Any password-based protocol is potentially vulnerable to an "on-line" dictionary attack
- On-line attacks can be detected and limited
- How?
- "Three strikes"
- Ratio of successful to failed logins
- Gradually slow login response time
- Potential DoS
- Cache IP address of last successful login


## From passwords to keys?

- Can potentially use passwords to derive symmetric or public keys
- What is the entropy of the resulting key?


## Password-based protocols

- Off-line attacks can never be 'prevented', but protocols can be made secure against such attacks
- Any password-based protocol is vulnerable to offline attack if the server is compromised
- Once the server is compromised, why do we care?


## Password storage

- "Salt"-ed hash of password
- Makes dictionary attacks harder,
- Prevents using 'rainbow tables'


## Advantages of salt

- Without salt
- Same hash functions on all machines
- Compute hash of all common strings once
- Compare hash file with all known password files
- With 12 bits salt
- One password hashed $2^{12}$ different ways
- Precompute hash file?
- Need much larger file to cover all common strings
- Dictionary attack on known password file
- For each salt found in file, try all common strings


## One-time password

- New password obtained by passing user-password through one-way function $n$ times which keeps incrementing
- Protects against replay as well as eavesdropping


## Password Cracking

## Dictionary attacks

- Develop a large dictionary of possible passwords and try each against the password file
- Each password must be hashed using each salt value and then compared to stored hash values

Password crackers exploit the fact that people choose easily guessable passwords

- Shorter password lengths are also easier to crack

Rainbow table attacks

- Pre-compute tables of hash values for all salts
- A mammoth table of hash values
- Can be countered by using a sufficiently large salt value and a sufficiently large hash length


## John the Ripper

- Open-source password cracker first developed in in 1996
- Uses a combination of brute-force and dictionary techniques


Figure 3.4 The Percentage of Passwords Guessed After a Given Number of Guesses

# Passwords Improving Security 

- Password complexity
- Case-sensitivity
- Use of special characters, numbers, and both upper and lower-case letters
- Minimum length requirements
- Security questions
- Ask personal questions which need to be verified
- Some questions are very easy to discover answers
- Virtual keyboard
- Person clicks on-screen keyboard to enter
- password (prevents keylogging)


## Challenge-response Authentication

Goal: Bob wants Alice to "prove" her identity to him

Protocol ap1.0: Alice says "I am Alice"


Failure scenario??

## Authentication

Goal: Bob wants Alice to "prove" her identity to him

Protocol ap1.0: Alice says "I am Alice"

in a network, Bob can not "see" Alice, so Trudy simply declares
herself to be Alice

## Authentication: another try

Protocol ap2.0: Alice says "I am Alice" in an IP packet<br>containing her source IP address



Failure scenario??

## Authentication: another try

## Protocol ap2.0: Alice says "I am Alice" in an IP

 packe $\dagger$ containing her source IP address

Trudy can creat a packet "spoofing" Alice's address

## Authentication: another try

Protocol ap3.0: Alice says "I am Alice" and sends her secret password to "prove" it.


Failure scenario??

## Authentication: another try

## Protocol ap3.0: Alice says "I am Alice" and sends her secret password to "prove" it.


playback attack:


Trudy records Alice's packet and later Alice's Alice's"I'm alicel" it back to Bob IP addr passworat'm Alice"

## Authentication: yet another try

## Protocol ap3.1: Alice says "I am Alice" and sends her

 encrypted secret password to "prove" it.

Failure scenario??

## Authentication: another try

## Protocol ap3.1: Alice says "I am Alice" and sends her

 encrypted secret password to "prove" it.
record and playback still works!

## Authentication: yet another try

Goal: avoid playback attack
Nonce: number (R) used only once -in-a-lifetime ap4.0: to prove Alice "live", Bob sends Alice nonce, R. Alice must return R, encrypted with shared secret key

$E \quad\left(K_{A-B}, R\right)$
Alice is live, and $\rightarrow$ only Alice knows key to encrypt nonce, so it must
Failures, drawbacks? be Alice!

## Authentication: ap5.0

ap4.0 doesn't protect against server database reading

- can we authenticate using public key techniques?
ap5.0: use nonce, public key cryptography



## Biometrics

- Use a person's physical characteristics
- fingerprint, voice, face, ...
- Advantages
- Cannot be disclosed, lost, forgotten
- Disadvantages
- Cost, installation, maintenance
- Reliability of comparison algorithms
- False positive: Allow access to unauthorized person
- False negative: Disallow access to authorized person
- Privacy?
- If forged, how do you revoke?


## Biometric Authentication

- Attempts to authenticate an individual based on unique physical characteristics
- Based on pattern recognition
- Is technically complex and expensive when compared to passwords and tokens
- Physical characteristics used include:
- Facial characteristics
- Fingerprints
- Hand geometry
- Retinal pattern
- Iris
- Signature
- Voice


Figure 3.8 Cost Versus Accuracy of Various Biometric Characteristics in User Authentication Schemes.


User interface
(a) Enrollment

(c) Identification

Figure 3.9 A Generic Biometric System. Enrollment creates an association between a user and the user's biometric characteristics. Depending on the application, user authentication either involves verifying that a claimed user is the actual user or identifying an unknown user.

## Biometrics

- Common uses
- Specialized situations, physical security
- Combine
- Multiple biometrics
- Biometric and PIN
- Biometric and token


## Token-based Authentication Smart Card <br> - With embedded CPU and memory

- Carries conversation w/ a small card reader
- Various forms
- PIN protected memory card
- Enter PIN to get the password
- Cryptographic challenge/response cards
- Computer create a random challenge
- Enter PIN to encrypt/decrypt the challenge w/ the card


## Key Distribution

- given parties A and B have various key distribution alternatives:

1. A can select key and physically deliver to $B$
2. third party can select \& deliver key to A \& B
3. if A \& B have communicated previously can use previous key to encrypt a new key
4. if A \& B have secure communications with a third party C, C can relay key between A \& B
5. Using public key encryption

## Trusted Intermediaries

## Symmetric key problem: Public key problem:

- How do two entities establish * When Alice obtains Bob's shared secret key over network?

Solution: public key (from web site, e-mail, diskette), how does she know it is Bob's public key, not Trudy's?

- trusted key distribution center (KDC) acting as intermediary between entities


## Solution:

- trusted certification authority (CA)


## X. 509 Certificate Use

Unsigned certificate:
contains user ID,


Signed certificate:
Recipient can verify
signature using CA's
public key.

## X. 509 Certificates

- issued by a Certification Authority (CA), containing:
- version V (1, 2, or 3)
- serial number SN (unique within CA) identifying certificate
- signature algorithm identifier AI
- issuer (X. 500 name CA)
- period of validity TA (from - to dates)
- subject X. 500 name A (name of owner)
- subject public-key info Ap (algorithm, parameters, key)
- issuer unique identifier (v2+)
- subject unique identifier (v2+)
- extension fields (v3)
- signature (of hash of all fields in certificate)
- notation $C A \ll A \gg$ denotes certificate for A signed by CA


## X. 509 Certificates



| $\left.\begin{array}{l} \text { Signature } \\ \text { algorithm } \\ \text { identifier } \end{array}\right\}$ | algorithm <br> parameters |
| :---: | :---: |
|  | Issuer Name |
|  | This Update Date |
|  | Next Update Date |
| $\left.\begin{array}{c} \text { Revoked } \\ \text { certificate } \end{array}\right\}$ | user certificate serial \# revocation date |
|  |  |
| $\left.\begin{array}{c} \text { Revoked } \\ \text { certificate } \end{array}\right\}$ | user certificate serial \# revocation date |
| Signature $\{$ | algorithms -- - parameters encrypted |

(b) Certificate Revocation List
(a) X .509 Certificate

## Obtaining a Certificate

$>$ any user with access to CA can get any certificate from it
$>$ only the CA can modify a certificate
$>$ because cannot be forged, certificates can be placed in a public directory

## CA Hierarchy

$>$ if both users share a common CA then they are assumed to know its public key
$>$ otherwise CA's must form a hierarchy
$>$ use certificates linking members of hierarchy to validate other CA's

- each CA has certificates for clients (forward) and parent (backward)
$>$ each client trusts parents certificates
> enable verification of any certificate from one CA by users of all other CAs in hierarchy


## CA Hierarchy Use



## Certificate Revocation

- certificates have a period of validity
- may need to revoke before expiry, eg:

1. user's private key is compromised
2. user is no longer certified by this CA
3. CA's certificate is compromised

- CA's maintain list of revoked certificates
- the Certificate Revocation List (CRL)
- users should check certificates with CA’s CRL


## Kerberos

$>$ trusted key server system from MIT
$>$ provides centralised private-key third-party authentication in a distributed network

- allows users access to services distributed through network
- without needing to trust all workstations
- rather all trust a central authentication server
$>$ two versions in use: $4 \& 5$


## Kerberos v4 Overview

$>$ a basic third-party authentication scheme
$>$ have an Authentication Server (AS)

- users initially negotiate with AS to identify self
- AS provides a non-corruptible authentication credential (ticket granting ticket TGT)
$>$ have a Ticket Granting server (TGS)
- users subsequently request access to other services from TGS on basis of users TGT
$>$ using DES


## Kerberos 4 Overview

2. AS verifies user's access right in database, creates ticket-granting ticket and session key. Results are encrypted using key derived from user's password.
3. User logs on to workstation and requests service on host.

4. Workstation prompts user for password and uses password to decrypt incoming message, then sends ticket and authenticator that contains user's name, network address, and time to TGS.
5. Workstation sends ticket and authenticator to server.

6. Server verifies that ticket and authenticator match, then grants access to service. If mutual authentication is required, server returns an authenticator.

## Kerberos v4 Dialogue

$$
\begin{aligned}
& \text { (1) } \mathrm{C} \rightarrow \mathrm{AS} I D_{c}\left\|I D_{t g s}\right\| T S_{1} \\
& \text { (2) } \mathrm{AS} \rightarrow \mathrm{C} \mathrm{E}\left(K_{c},\left[K_{c, t g s}\left\|I D_{t g s}\right\| T S_{2} \| \text { Lifetime }_{2} \| \text { Ticket }_{\text {tgs }}\right]\right) \\
& \left.\quad{\text { Ticket } t_{t g s}}={\mathrm{E}\left(\mathrm{~K}_{t g s},\right.}\left[\mathrm{K}_{c, g g s}\left\|\mathrm{ID}_{C}\right\| \mathrm{AD}_{C}\left\|\mathrm{I}_{\text {tgs }}\right\| \mathrm{TS}_{2} \| \text { Lifetime }_{2}\right]\right)
\end{aligned}
$$

(a) Authentication Service Exchange to obtain ticket-granting ticket

$$
\begin{aligned}
& \text { (3) } \mathbf{C} \rightarrow \text { TGS } I D_{v} \| \text { Ticket }_{t g^{5}} \| \text { Authenticator }{ }_{c} \\
& \text { (4) TGS } \rightarrow \mathrm{C} E\left(K_{c, 2 g 5^{5}}\left[K_{c, v}\left\|I D_{v}\right\| T S_{4} \| \text { Ticket }_{v}\right]\right) \\
& \text { Ticket }_{t g s}=\mathrm{E}\left(\mathrm{~K}_{\text {tgg }},\left[\mathrm{K}_{c, g \mathrm{gs}}\left\|\mathrm{ID}_{C}\right\| \mathrm{AD}_{C}\left\|\mathrm{D}_{\text {tgs }}\right\| \mathrm{TS}_{2} \| \text { Lifetime }{ }_{2}\right]\right) \\
& \text { Ticket }=\mathrm{E}_{v}\left(\mathrm{~K}_{v},\left[\mathrm{~K}_{c, v}\left\|\mathrm{ID}_{C}\right\| \mathrm{AD}_{C}\left\|\mathrm{ID}_{v}\right\| \mathrm{TS}_{4} \| \text { Lifetime }{ }_{4}\right]\right) \\
& \text { Authenticator }{ }_{c}=\mathrm{E}\left(\mathrm{~K}_{\mathrm{c}, \mathrm{f} g},\left[\mathrm{ID}_{C}\left\|\mathrm{AD}_{C}\right\| \mathrm{TS}_{3}\right]\right)
\end{aligned}
$$

(b) Ticket-Granting Service Exchange to obtain service-granting ticket

$$
\begin{aligned}
& \text { (5) } \mathrm{C} \rightarrow \mathrm{~V} \text { Ticket } \| \text { Authenticator }{ }_{c} \\
& \text { (6) } \mathrm{V} \rightarrow \mathrm{C} \mathrm{E}\left(K_{c, v},\left[T S_{5}+1\right]\right) \text { (for mutual authentication) } \\
& \qquad \begin{aligned}
\text { Ticket }_{v} & \left.=\mathrm{E}_{v},\left[\mathrm{~K}_{c, v}\left\|\mathrm{ID}_{C}\right\| \mathrm{AD}_{C}\left\|\mathrm{ID}_{v}\right\| \mathrm{TS}_{4} \| \text { Lifetime }_{4}\right]\right) \\
\text { Authenticator } & =\mathrm{E}_{c}\left(\mathrm{~K}_{c, v},\left[\mathrm{ID}_{C}\left\|\mathrm{AD}_{C}\right\| \mathrm{TS}_{5}\right]\right)
\end{aligned}
\end{aligned}
$$

(c) Client/Server Authentication Exchange to obtain service

## Kerberos Realms

- a Kerberos environment consists of:
- a Kerberos server
- a number of clients, all registered with server
- application servers, sharing keys with server
- this is termed a realm
- typically a single administrative domain
- if have multiple realms, their Kerberos servers must share keys and trust


## LAN Security

Modified By: Dr. Ramzi Saifan

## LAN

- Many data traffic is available to every node in the LAN zone
- NIC provides physical and logical conversions.
- Every NIC has an address.
- When messages are inserted in the network, the address of the destination NIC is part of the message header.
- As messages flow through an NIC, the destination address is examined.
- If the destination address matches the NIC doing the examining, the message is transmitted to upper layers.
- It is also easy to provide broadcast communication to all NICs by using a special address such as the binary value of all ones.


## LAN simplicity-security tradeoff

- There are many reasons why LANs have become popular,
- the most important is flexibility and cost.
- New NICs may be added to the net or activated,
- or NICs may be removed or deactivated without making a significant change.
- This dynamic flexibility happens without notification and coordination with a central authority.
- A PC can record all the communications traffic. Address filtering can be turned off.
- The NIC can operate in "promiscuous" or "snooper" mode, passing all traffic to the PC, which in turn can record it for some future use.


## Wiretapping

- Wiretapping is conventionally subdivided into passive and active categories.
- In passive, the message traffic is observed but not modified.
- The most obvious objective of passive wiretapping is to learn the contents of messages;
- traffic analysis may provide the adversary with information when message content is not available.
- E.g., sudden change in traffic volume between national central banks, might signal a change in the rate of exchange or some other financial activity that could be turned into a profit by someone.
- In active wiretapping: Messages can be completely deleted, they can be inserted, or their contents can be modified.
- Delay, reordering, duplication, and retransmission are also possible.


## Packet Sniffing

- This works for wireless too!
- In fact, it works for any broadcast-based medium


## Packet Sniffing Countermeasures

- How can we protect ourselves?
- SSH, not Telnet
- Many people are still using Telnet and send their password in the clear (use PuTTY instead!)
- Now that I have told you this, please do not exploit this information
- Packet sniffing is, by the way, prohibited by Computing Services
- HTTP over SSL
- Especially when making purchases with credit cards!
- SFTP, not FTP
- Unless you really don't care about the password or data
- Can also use KerbFTP (download from MyAndrew)
- IPSec
- Provides network-layer confidentiality


## Switch Learning Attacks

- Switch learning is what makes Ethernet scale
- Two key attacks: MAC flooding and spoofing
- Extremely simple to carry out, yet very potent
- Can help attacker collects usernames/passwords, prevent proper operation of LAN, etc
- Can turn a $\$ 50,000$ switch into a $\$ 12$ hub


## Limitations on switch memory

- High end switches can store hundreds of thousands of learning table entries
- What happens if learning table fills up?
- Depends on vendor -
- Most Cisco switches do not replace older entries with new ones.
- Need to "age out" entries (wait for them to time out)
- Other switches circular buffer
- Existing entries get overwritten


## MAC Flooding Attack

- Problem: attacker can cause learning table to fill Generate many packets to varied (perhaps nonexistant) MAC addresses
- This harms efficiency
- Effectively transforms switch into hub
- Wastes bandwidth, and end-host CPU
- This harms privacy
- Attacker can eavesdrop by preventing switch from learning destination of a flow
- Causes flow's packet to be flooded throughout LAN


## MAC Spoofing Attack

- Host pretends to own the MAC address of another host
- Easy to do: most Ethernet adapters allow their address to be modified
- Powerful: can immediately cause complete DoS to spoofed host
- All learning table entries point to the attacker
- All traffic redirected to attacker
- Can enable attacker to evade ACLs set based on MAC information


## Switch Learning Attacks: Countermeasures

- Detecting MAC activity
- Many switches can be config'd to warn administrator about many sudden MAC address moves
- Port Security
- Ties a given MAC address to a port
- On violation, can drop frames, disable port for specified duration, signal alarm, increment violation counter


## Switch Learning Attacks: Countermeasures

- Unicast Flooding Protection
- Send alert when user-defined rate limit is exceeded
- Can also filter traffic or shut down port generating excessive floods


## DHCP



## Attacks on DHCP

- Unfortunately, DHCP was designed without security in mind
- Whoever requests an address is free to receive one
- No authentication fields or any other security-inclined information in protocol


## Attacks against DHCP



- DHCP Scope Exhaustion
- Malicious client attempts to seize entire range of IP addresses
- When legitimate client tries, it is abandoned with no IP connectivity


## Attack: Rogue DHCP Server



- Installation of a Rogue DHCP Server
- Client uses offer or of previously-used IP address, if none then uses first-received response:
- Rogue can compromise all clients "near" itself


## Countermeasures to DHCP Attacks

- Limit number or set of MAC addresses per port
- This is called Port Security
- Limit can be set manually or switch can be instructed to lock down on first dynamically learned address
- Limitations
- DHCP lets you request multiple IP addresses for a single MAC address


## Countermeasures to DHCP Attacks

- Prevent hosts from generating certain DHCP messages (DHCP Snooping)
- Like a stateful firewall for DHCP
- Runs on router's central management processor, to do deep packet inspection
- Learns IP-to-MAC bindings by snooping on DHCP packets
- Rules:
- If port is connected to host, don't allow DHCPOFFER and DHCPACK packets
- Don't allow DHCP packets that don't match learned bindings
- Can also rate-limit DHCP messages per port, etc


## Address Resolution Protocol (ARP)

- Networked applications are programmed to deal with IP addresses
- But Ethernet forwards to MAC address
- How can OS know the MAC address corresponding to a given IP address?
- Solution: Address Resolution Protocol
- Broadcasts ARP request for MAC address owning a given IP address

- ARP: determine mapping from IP to MAC address
- What if IP address not on subnet?
- Each host configured with "default gateway", use ARP to resolve its IP address
- Gratuitous ARP: tell network your IP to MAC mapping
- Used to detect IP conflicts IP address changes; update other machines' ARP tables, update bridges' learned information


## Risk Analysis for ARP

- No authentication
- Hosts do not sign ARP replies
- Information leak
- All hosts in same VLAN learn the advertised <IP,MAC> mapping
- All hosts discover querying host wishes to communicate with replying host
- Availability
- All hosts on same LAN receive ARP request, must process it in software
- Attacker could send high rate of spurious ARP requests, overloading other hosts


## ARP Spoofing Attack



- Attacker sends fake unsolicited ARP replies
- Attacker can intercept forward-path traffic
- Can intercept reverse-path traffic by repeating attack for source
- Gratuitious ARPs make this easy
- Only works within same subnet/VLAN


## Countermeasures to ARP Spoofing

- Ignore Gratuitious ARP
- Problems: gratuitious ARP is useful, doesn't completely solve the problem
- Dynamic ARP Inspection (DAI)
- Switches record <IP,MAC> mappings learned from DHCP messages, drop all mismatching ARP replies
- Intrusion detection systems (IDS)
- Monitor all <IP,MAC> mappings, signal alarms


# SSL and IPSec 

Modified by: Dr. Ramzi Saifan

## Network layers

- Application
- Transport
- Network
- Data link
- Physical


## Example security protocols

- Application layer: PGP
- Transport layer: SSL/TLS
- Network layer: IPsec
- Data link layer: IEEE 802.11
- Security at the physical layer?


## Security in what layer?

- Depends on the purpose...
- What information needs to be protected?
- Who shares keys in advance?
- Should the user be involved?
- E.g., a network-layer protocol cannot authenticate two end-users to each other
- An application-layer protocol cannot protect IP header information
- Also affects efficiency, ease of deployment, etc.


## Generally...

- When security is placed at lower levels, it can provide automatic, "blanket" coverage...
- ...but it can take a long time before it is widely adopted
- When security is placed at higher levels, individual users can choose when to use it...
- ...but users who are not security-conscious may not take advantage of it


## Note...

- The "best" solution is not necessarily to use PGP over IPsec!
- Would have been better to design the Internet with security in mind from the beginning...


## Example: PGP vs. SSL vs. IPsec

- PGP is an application-level protocol for "secure email"
- Can provide security on "insecure" systems
- Users choose when to use PGP; user must be involved
- Alice's signature on an email proves that Alice actually generated the message, and it was received unaltered; also non-repudiation
- In contrast, SSL would secure "the connection" from Alice's computer;
- would need an additional mechanism to authenticate the user
- IPsec is between every two hops in the network


## PGP

## Encrypt



## Decrypt



Encrypted Message


Data

## Example: PGP vs. SSL vs. IPsec

- SSL sits at the transport layer, "above" TCP
- Packet stream authenticated/encrypted
- End-to-end security, best for connection-oriented sessions (e.g., http traffic)
- User does not need to be involved
- The OS does not have to change, but applications do if they want to communicate securely


## Example: PGP vs. SSL vs. IPsec

- IPsec sits at the network layer
- Individual packets authenticated/encrypted
- End-to-end or hop-by-hop security
- Best for connectionless channels
- Need to modify OS
- All applications are "protected" by default, without requiring any change to applications or actions on behalf of users
- Only authenticates hosts, not users
- User completely unaware that IPsec is running


## SSL/TLS

## Brief history...

- SSLv2 deployed in Netscape 1.1 (1995)
- Modified version of SSLv3 standardized at TLS


## Broad overview

- SSL runs on top of TCP
- Provides an API similar to that of TCP
- Technically, SSL runs in the application layer
- Advantage: does not require changes to TCP
- From the programmer's point of view, it is in the transport layer
- Same API as for TCP
- Runs only with TCP, not UDP
- Primarily used for HTTP traffic


## SSL overview

- Three phases
- Handshake
- Key derivation
- Data transfer


## Handshake phase

- Client:
- Establishes TCP connection with server;
- Verifies server's identity
- Obtains server's public key and certificate; verifies certificate
- Sends server a master secret key K
- Encrypted using server's public key


## Key derivation

- Client and server use K to establish four keys: encryption and authentication, for each direction


## Data transfer

- SSL breaks data stream into records; appends a MAC to each record; and then encrypts the result - Mac-then-encrypt...
- The MAC is computed over the record plus a sequence number
- Prevents replay, re-ordering, or dropping packets


## Note...

- As described, SSL only provides one-way authentication (server-to-client)
- Not generally common for clients to have public keys
- Can do mutual authentication over SSL using, e.g., a password
- SSL also allows for clients to have public keys



## HTTPS and the Lock Icon

## Certificates

- How does Alice (browser) obtain $\mathrm{PK}_{\text {Bob }}$ ?

Browser

Bob uses Cert for an extended period (e.g. one year)

## Certificates: example

## Important fields:

Certificate Signature Algorithm
Issuer
$\Delta$ Validity
Not Before
Not After
Subject
$\triangle$ Subject Public Key Info
Subject Public Key Algorithm
Subject's Public Key

## 4 Extensions

## Field Value

Modulus (1024 bits):
ac 731497 b 410 a3 aa f4 c1 15 ed cf 92 f3 9a
$97269 a$ cf 1 b e4 1 b dc d2 c9 372 f d2 e6 07 1d
ad b2 3e f7 8c 2f fa a1 b7 9e e3 544034 3f b9
e2 1c 128 a 306 b 0 c fa 306 a 0161 e 97 c b1 98

6 b 9 c 0 d d0 8e 4 f 390 d 2 b d2 e9 88 cb 2 d 21 a 3
f1 84613 c 3 a aa 801827 e6 7 e f7 b8 6a 0 a 75
e1 bb 147295 cb 6478068481 eb 7 b 078 Cl 49

## Certificate Viewer:"*.gmail.com"

## $x$

Genera Details

This certificate has been verified for the following uses:
SSL Server Certificate

## Issued To

Common Name (CN) *.gmail.com
Organization (O)
Google Inc
Organizational Unit (OU)
Serial Number
<Not Part Of Certificate>

## Issued By

Common Name (CN) Thawte Premium Server CA
Organization (O) Thawte Consulting cc
Organizational Unit (OU) Certification Services Division

## Validity

Issued On $\quad 9 / 25 / 2008$
Expires On
9/25/2010

## Fingerprints

SHA1 Fingerprint
MD5 Fingerprint

B7:A7:89:34:54:5D:C9:6F:41:FD:A9:3E:41:AF:2B:1D:13:C8:CC:AD 55:5F:09:17:24:03:F7:80:2B:B6:90:26:3B:0B:E3:3B

## Certificate Authorities

## Browsers accept certificates from a large number of CAs



## Brief overview of SSL/TLS



Most common: server authentication only

## Why is HTTPS not used for all web traffic?

- Slows down web servers
- Breaks Internet caching
- ISPs cannot cache HTTPS traffic
- Results in increased traffic at web site


## The lock icon: SSL indicator

N Network Security at Stanford - Windows Internet Explorer


Intended goal:

- Provide user with identity of page origin

- Indicate to user that page contents were not viewed or modified by a network attacker


## When is the (basic) lock icon displayed



- All elements on the page fetched using HTTPS
- For all elements:
- HTTPS cert issued by a CA trusted by browser
- HTTPS cert is valid (e.g. not expired)
- CommonName in cert matches domain in URL


## The lock UI: help users authenticate site

Firefox 3: (no SSL)

(SSL)



| d-Mozilla Firefox |
| :--- | :--- | :--- |
| okmarks Iools Help |
| You are connected to |
| stanford.edu |
| which is run by |
| (unknown) |

## The lock UI: help users authenticate site <br> - Firefox 3: clicking on bottom lock icon gives



## The lock UI: Extended Validation (EV) Certs

- Harder to obtain than regular certs
- requires human lawyer at CA to approve cert request
- Designed for banks and large e-commerce sites


Send Money, Money Transfer - PayPal - Mozilla Firefox 3 Beta 3
File Edit View History Bookmarks Tools Help
$-\square x$
$\mathrm{C} \times \boldsymbol{P}$ Paypal Inc. (US) https://www.paypal.com/ \& $\rightarrow$ G- Google $\quad$ Q

## HTTPS and login pages: incorrect version

- Users often land on login page over HTTP:

Type site's HTTP URL into address bar, or

- Google links to the HTTP page



## Invalid certs

$>$ Examples of invalid certificates:

- expired: current-date > date-in-cert
- CommonName in cert does not match domain in URL
- unknown CA (e.g. self signed certs)
- Small sites may not want to pay for cert
> Users Often ignore warning:
- Is it a miss-configuration or an attack? User can't tell.

Accepting invalid cert enables man-in-middle attacks
(see http://crypto.stanford.edu/ssl-mitm )

## Man in the middle attack using invalid certs

GET https://bank.com

$\longleftrightarrow$ ServerCert (Badguy)
attacker

bad cert
warning!


- Attacker proxies data between user and bank. Sees all traffic and can modify data as will.


## Firefox: Invalid cert dialog



## IE: invalid cert URL bar



## IPsec

## Overview

- IPsec can provide security between any two network-layer entities
- host-host, host-router, router-router
- Used widely to establish VPNs
- IPsec encrypts and/or authenticates network-layer traffic, and encapsulates it within a standard IP packet for routing over the Internet


## Overview

- IPsec consists of two components
- IKE --- Can be used to establish a key
- AH/ESP --- Used to send data once a key is established (whether using IKE or out-of-band)
- AH
- Data integrity, but no confidentiality
- ESP
- Data integrity + confidentiality
- (Other differences as well)


## Security policy database

- Nodes maintain a table specifying what is required for each incoming packet
- Drop
- Forward/accept without IPsec protection
- Require IPsec protection
- Auth only
- Enc only
- Both
- As with firewalls, decisions can be based on any information in the packet


## Security associations (SAs)

- When a node receives a packet, needs to know who it is from
- May be receiving IPsec traffic from multiple senders at the same time -- possibly even with the same IP address
- An SA defines a network-layer unidirectional logical connection
- For bidirectional communication, need two SAs
- The IPsec header indicates which security association to use


## Security associations (SAs)

- A tremendous amount of information is kept in the SADB, and we can only touch on a few of them:
- AH: authentication algorithm
- AH: authentication secret
- ESP: encryption algorithm
- ESP: encryption secret key
- ESP: authentication enabled yes/no
- Many key-exchange parameters
- Routing restrictions
- IP filtering policy


## Firewalls...

- Potential problem if upper-layer header data is used for decision-making; this information will be encrypted when using IPsec
- Arguments pro and con as to whether this data should be encrypted or not:
- Pro: This data shouldn't be divulged; get rid of firewalls
- Con: administrators will likely keep firewalls and turn off encryption...


## AH vs. ESP

- Two header types...
- Authentication header (AH)
- Provides integrity only
- Encapsulating security payload (ESP)
- Provides encryption + integrity
- Both provide cryptographic protection of everything beyond the IP headers
- AH additionally provides integrity protection of some fields of the IP header


## Transport vs. tunnel mode

- Transport mode: original IP header not touched; IPsec information added between IP header and packet body
- IP header | IPsec $\underbrace{[\text { [packet ] }}_{\text {protected }}$
- Most logical when IPsec used end-to-end


## Transport vs. tunnel mode

- Tunnel mode: keep original IP packet intact but protect it; add new header information outside
- New IP header | IPsec | [ old IP header | packet ] encrypted
authenticated
- Can be used when IPSec is applied at intermediate point along path (e.g., for firewall-to-firewall traffic)
- Treat the link as a secure tunnel
- Results in slightly longer packet


## More on AH

- AH provides integrity protection on header
- But some fields change en route!
- Immutable fields included in the integrity check
- Mutable but predictable fields are also included in the integrity check
- The final value of the field is used


## More on AH vs. ESP

- ESP can already provide encryption and/or authentication
- So why do we need AH?
- AH also protects the IP header
- Export restrictions
- Firewalls need some high-level data to be unencrypted


## AH Header

# IPSec AH Header 

| next hdr | AH len | Reserved |
| :---: | :---: | :---: |
| SPI (Security Parameters Index) |  |  |
| Sequence Number |  |  |
| Authentication Data <br> (usually MD5 or SHA-1 hash) |  |  |

32 bits

## IPSec in AH Transport Mode



IPSec in AH Tunnel Mode


Original IPv4 Datagram


Protected by AH Auth Data

New IP
New IPv4 Datagram type


TCP payload

## ESP Header

ESP w/o Authentication

| SPI (Security Parameters Index) |
| :---: |
| Sequence Number |
| Encrypted <br> Payload <br> (variable) |
| padding <br> (variable) |
| pad len |
| next hdr |

ESP with Authentication


## IPSec in ESP Transport Mode

Original IPv4 Datagram


Encrypted Data



IPSec in ESP Tunnel Mode


Original IPv4 Datagram


Data


## The future of AH ?

- In the long run, it seems that AH will become obsolete
- Better to encrypt everything anyway
- No real need for AH
- Certain performance disadvantages
- AH is complex...


## IPsec: IKE

## Overview of IKE

- IKE provides mutual authentication, establishes shared key, and creates SA
- Assumes a long-term shared key, and uses this to establish a session key (as well as to provide authentication)
- Supported key types
- Public signature keys
- Public encryption keys
- Symmetric keys


## IKE phases

- Phase 1: long-term keys used to derive a session key (and provide authentication)
- Phase 2: session key used to derive SAs
- Why...?
- In theory, can run phase 1 once, followed by multiple executions of phase 2
- E.g., different flows between same endpoints
- Why not used same key for each? Is there any secure way to do this?
- In practice, this anyway rarely happens


## Key types

- Why are there two PK options?
- Signature-based option
- Efficiency (can start protocol knowing only your own public key, then get other side's key from their certificate)
- Legal reasons/export control
- Encryption-based option
- Can be used to provide anonymity in both directions
- Adds tremendously to the complexity of implementation


## Anonymity

- Protocols can be designed so that identities of the parties are hidden from eavesdroppers
- Even while providing authentication!
- Can also protect anonymity of one side against active attacks
- Whom to protect?
- Initiator: since responder's identity is generally known...
- Responder: since otherwise it is easy to get anyone's identity


## Phase 1 session keys

- Two session keys are defined in phase 1
- One each for encryption/authentication
- These keys are used to protect the final phase 1 messages as well as all phase 2 messages
- These keys are derived from the DH key using hashing
- Details in the book...


## IKE phase 1

- Aggressive mode
- 3 messages
- Main mode
- 6 messages
- Additional features:
- Anonymity
- Negotiation of crypto parameters


## Aggressive mode

- Alice sends $\mathrm{g}^{\mathrm{a}}$, "Alice", crypto algorithms
- Note that choices are restricted by this message
- Bob sends $\mathrm{g}^{\mathrm{b}}$, choice of crypto algorithm, "proof" that he is really Bob
- If Bob does not support any of the suggested algorithms, he simply does not reply
- Note that there is no way to authenticate a refusal, since no session key yet established
- Alice sends "proof" that she is Alice


## Main mode

- Negotiate crypto algorithms (2 rounds)
- Alice and Bob do regular Diffie-Hellman key exchange (2 rounds)
- Alice sends encryption of "Alice" plus a proof that she is Alice, using long-term secret keys plus [keys derived from] $\mathrm{g}^{\text {ab }}$
- Bob does similarly...


## Crypto parameters...

- Choice of:
- Encryption method (DES, 3DES, ...)
- Hash function (MD5, SHA-1, ...)
- Authentication method (e.g., key type, etc.)
- Diffie-Hellman group (e.g., (g, p), etc.)
- A complete set of protocols (a security suite) must be specified


## Negotiating parameters

- Many protocols allow parties to negotiate cryptographic algorithms and parameters
- Allows users to migrate to stronger crypto; increases inter-operability (somewhat)
- But, opens up a potential attack if not authenticated somehow...
- Also makes for more complicated implementations


## "Proofs of identity"

- Depend on which type of long-term shared key is being used
- Similar (in spirit) to the authentication protocols discussed in class
- Details in book...


## Course wrap-up

## What should you take away from this course (after the final)?

- Security mind-set
- Not limited to computers/networks!
- Security is complex
- Draws on many different disciplines
- Need to know what you are doing
- Security is hard, still evolving
- We did not cover some of the most important presentday attacks: spam, phishing, DDos, viruses, ...
- Security is challenging...but fun!


## Thank you!

