

First exam Fall 2018

problem 1. solve the following short problems

[A] If $(212)_z = (38)_{10}$ then $z = \dots$

لو دوطرنا
ديجيتال

$$2z^0 + 1z + 2z^2 = 38$$

decimal

$$2z^2 + z + 2 = 38$$

ع ا لصين

$$2z^2 + z - 36 = 0$$

تكون

الرحصين

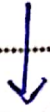
decimal

$z = 4$ or $\left(\frac{-9}{2}\right) \rightarrow$ this is ignored.

answer is $z = 4$

SUBJECT:

[B] $(7706)_8$ is equal to $(3F18)_{16}$



00111 111 - 00011000

↓
3

F

1

8

[C] $(73)_{10}$ is equal to $(243)_5$

$73/5$ 3



$14/5$ 4

$2/5$ 2

0

[D] $(1293)_{10}$ is equal to $(00100101010011)_{BCD}$

\swarrow \swarrow \swarrow \swarrow
 0001 0010 1001 0011

[E] dual expression for function

$$F(A, B, C, D) = (\bar{A} + A(\bar{C} + D)) \cdot A$$

dual $F = (\bar{A} \cdot (A + (\bar{C} \cdot D))) + A$

[F] simplified complement expression for

$$F(A, B, C) = \bar{A} + C + \bar{A} \cdot C$$

dual $F = \overline{A \cdot C} \cdot (\bar{A} + C)$

$$\bar{F} = A \cdot C \cdot (A + \bar{C})$$

then: simplify

dual simplification
 \Downarrow
 K-map
 (\bar{A}, A, B, C)

but for better answer

$$F(A, B, C) = \bar{A}\bar{C} + \bar{A}C \rightarrow \text{first simplify (F)}$$

$$= \bar{A}(\bar{C} + C)$$

$$= \bar{A} \rightarrow \text{then } \bar{F} = A$$

$$F(A, B, C) = \overline{A} + C + \overline{A} \cdot C = \overline{A} \cdot \overline{C} + \overline{A} \cdot C$$

11/15/2019, 10:00

K-map

	000	001	0100

[G] Assume N is a 3-digit number represented in octal, minimum number of digits need when N in decimal is ()?

octal (radix 8) \rightarrow 3 digits.

$8^3 = 512$ combinations to reach the maximum possible combination of 3 digits ($N = 777$)₈

so $\log_{10} 512 = 2.7$

so you need 3 digits.

[H] The even parity bit for the following:

$(1100110011110111)_2$ code word

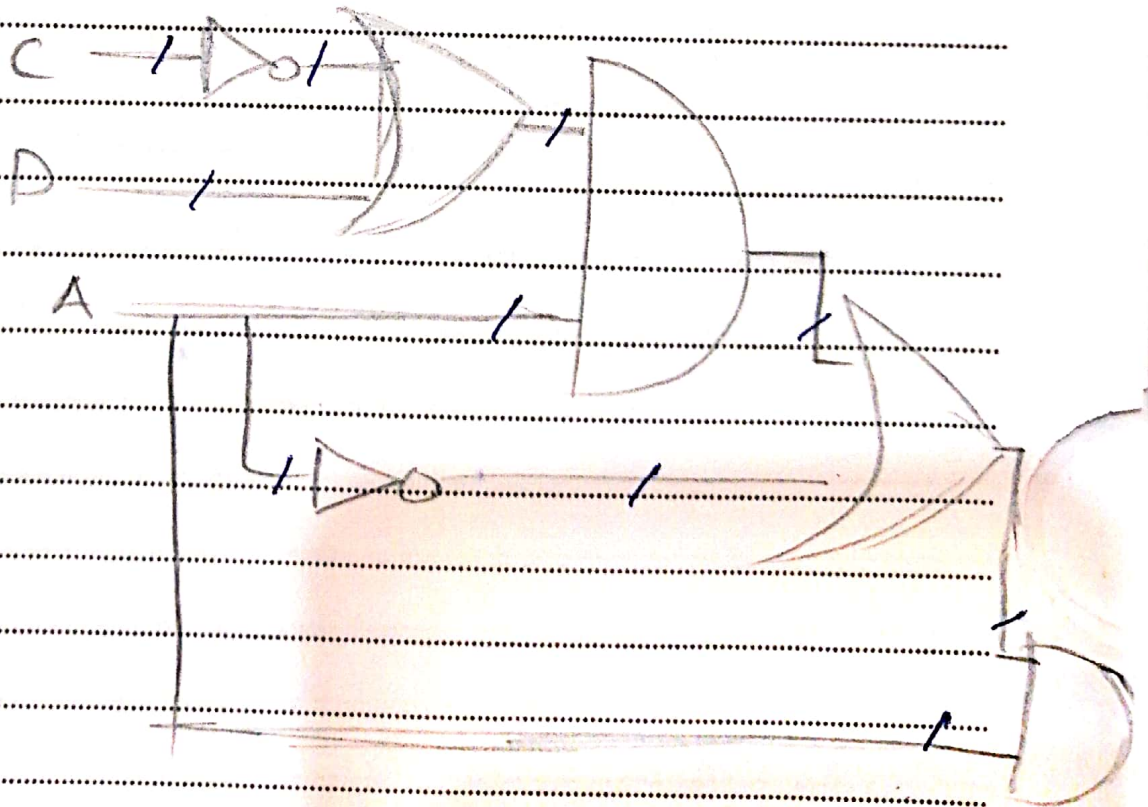
is: 1

[E] The gate input cost with inverters counted of

$F(A, B, C, D) = (\bar{A} + A(C + D)) \cdot A$ is

GN: (10)

دالة الترميز المفضل



Problem 2:

Fill-in the following k-map for function
 $F(A, B, C, D) = (\bar{B}\bar{D} + BC\bar{D} + A\bar{B}\bar{C}D)$

	\bar{C}		C		
\bar{A}	1			1	\bar{B}
A			1		B
A			1		\bar{B}
	\bar{D}		D		
	1	1		1	\bar{D}

Problem 3 use boolean algebra only, prove that:

$$\overline{x+z} + \overline{xy}z + \overline{y}z = \overline{x} + \overline{y}z$$

$$\overline{x+z} + \overline{xy}z + \overline{y}z =$$

$$\overline{xz} + z(\overline{xy} + \overline{y}) =$$

$$\overline{xz} + z(\overline{x} + \overline{y}) =$$

$$\overline{xz} + \overline{x}z + \overline{y}z$$

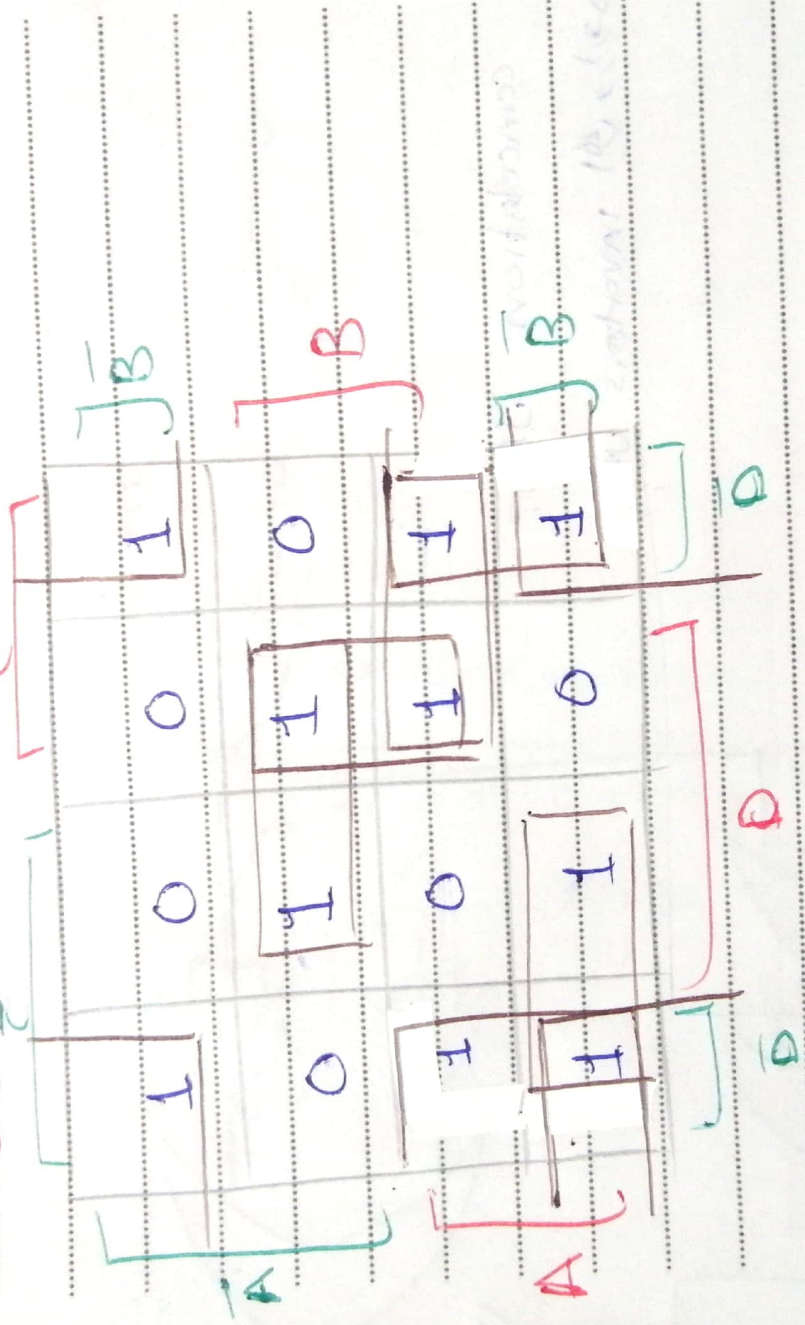
$$\overline{x}(z+z) + \overline{y}z$$

$$\overline{x} + \overline{y}z$$

SUBJECT:

Problem 4: Consider the following K-map for the function $F(A, B, C, D)$. Identify its prime implicants and determine which are essential.

QWC Essential:



Implicants:

$B\bar{C}$ → essential

$A\bar{D}$ → essential

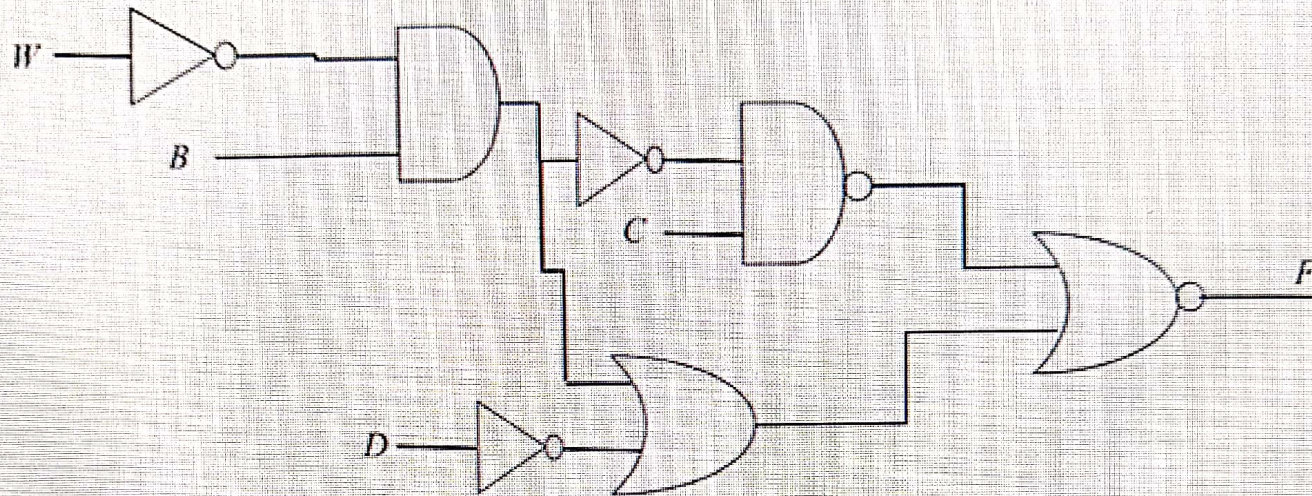
$A\bar{B}\bar{C}$ → essential

$A\bar{B}C$

$B\bar{C}D$

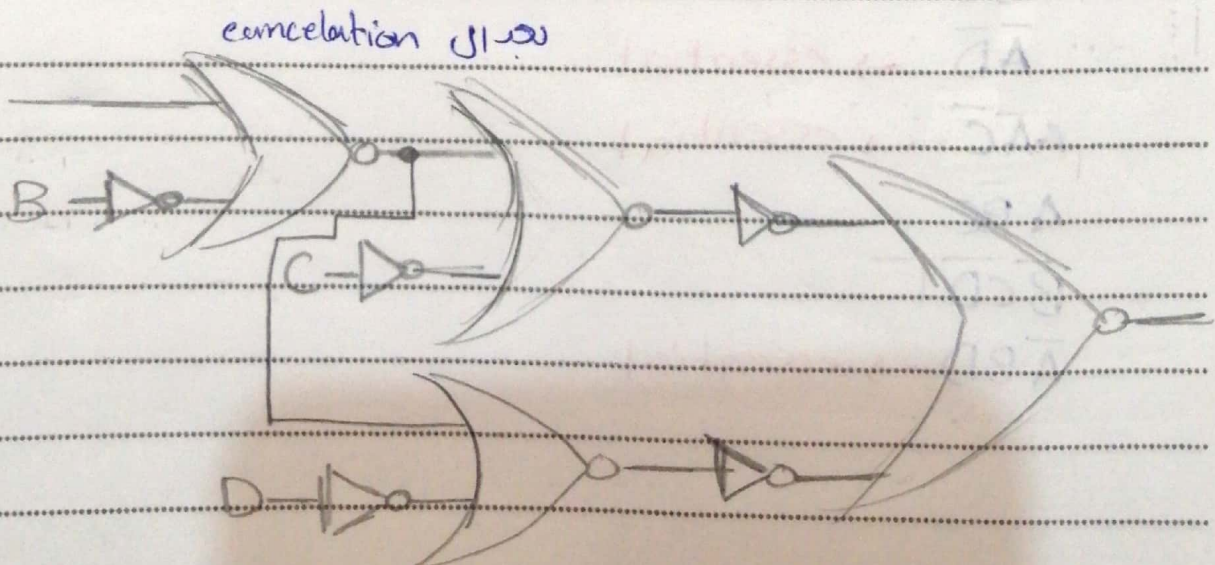
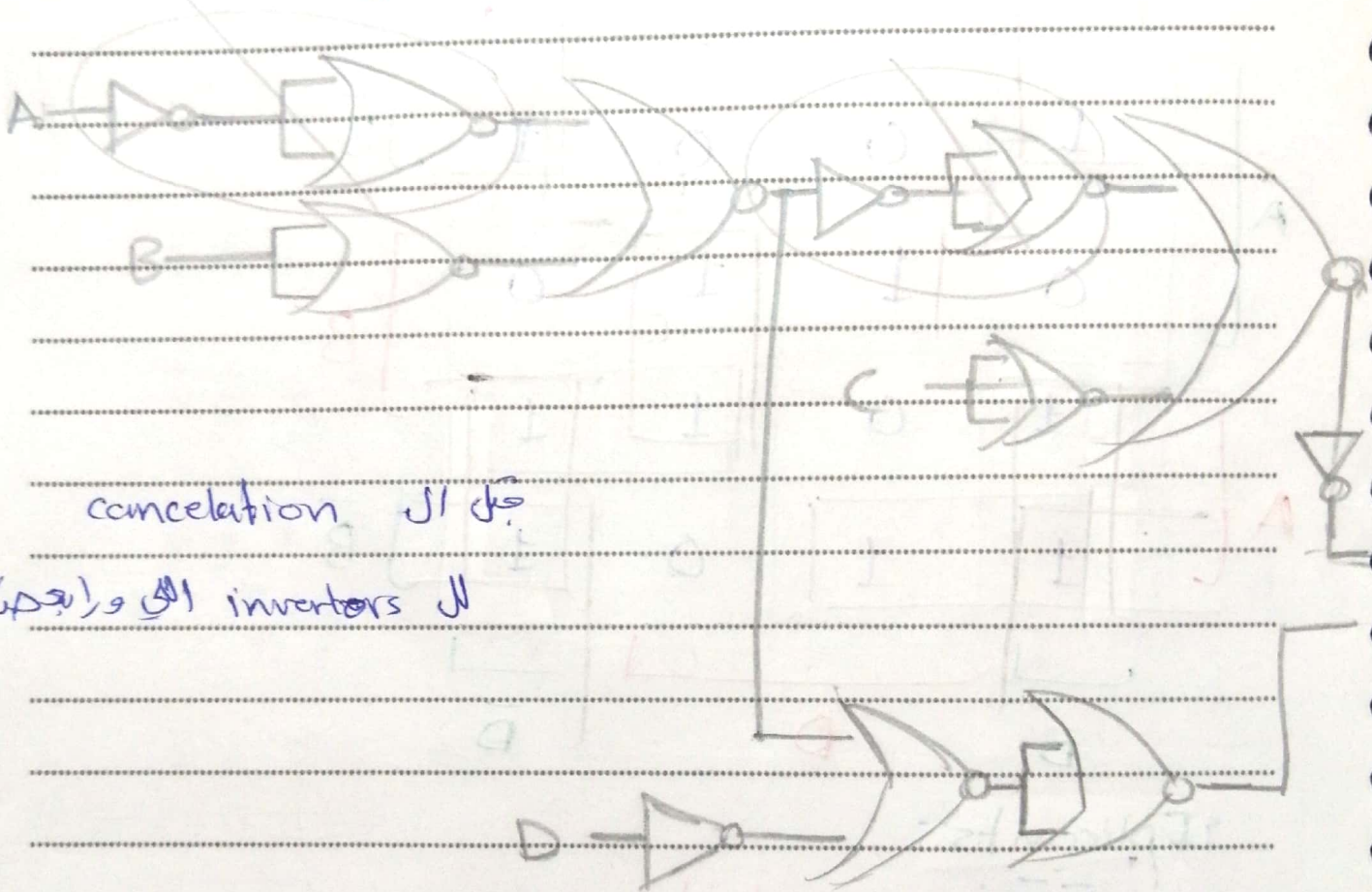
$\bar{A}BD$ → essential

Problem 5: In the space give below redesign the following function using NOR gates and inverters only. **(2 Points)**



Problem 5

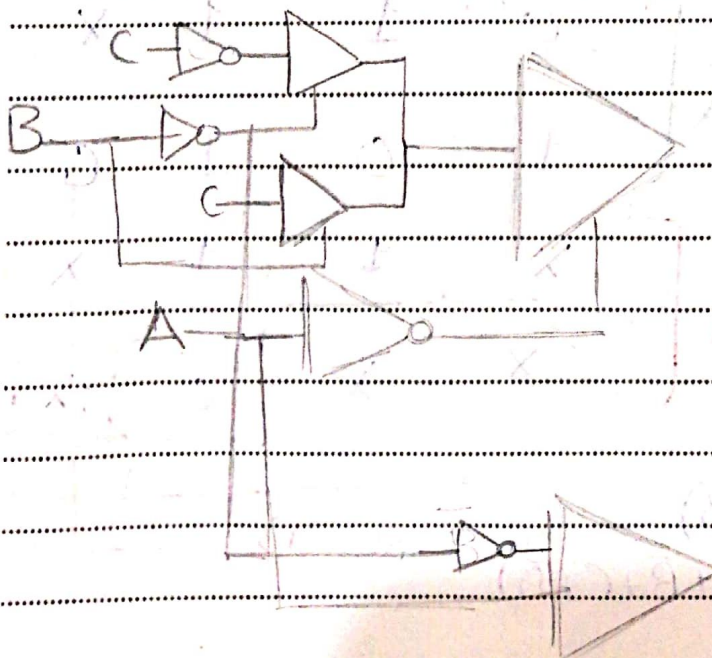
redesign the following function using NOR gates and inverters only.



problem 6

the truth table for $F(A, B, C)$, draw the implementation of the function using tri-state buffers and inverters only.

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	0



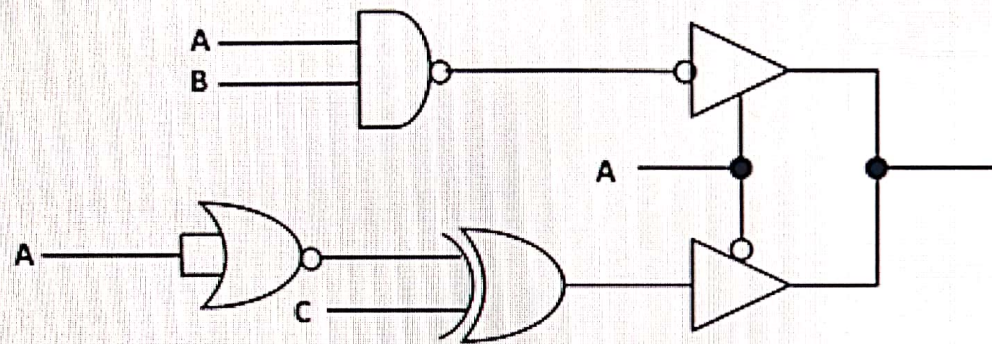
buffers = 3

inverters = 3

3

Problem 7. Given the logic diagram of function F Fill in the table on the right for the given combinations
(2 Points)

I



A	B	C	F
1	0	0	
1	1	1	
0	1	0	
0	1	1	

Problem 8: Given the Kmap for function F write the Boolean expression of F as a POS. (2 Points)

C

Problem 8: Given the Kmap for function F write the Boolean expression of F as a POS.

(2 Points)

I

		C		
		0	1	X
		1	0	0
A	B	X	1	X
		X	X	0
		D		

F (A, B, C, D) =

Problem 7

Given the logic diagram of function F

Fill in the table the given combinations:

A	B	C	F
1	0	0	0
1	1	1	1
0	1	0	1
0	1	1	0

Problem 8

Given K-map for function F, write boolean expression of F as a POS

$$F = CD + AB + \bar{B}D + \bar{A}\bar{B}\bar{C}D$$

dual $F =$

$$(C + \bar{D}) \cdot (A + \bar{B}) \cdot (\bar{B} + \bar{D}) \cdot (\bar{A} + B + \bar{C} + D)$$

	C		C		
	0	1	1	X	B
A	1	0	1	0	B
	X	1	1	X	
	X	X	0	X	B
	B		D		

$$F \text{ as POS} = (\bar{C} + \bar{D}) \cdot (\bar{A} + B) \cdot (B + D) \cdot (A + \bar{B} + \bar{C} + \bar{D})$$

problem 9

Box 1 J

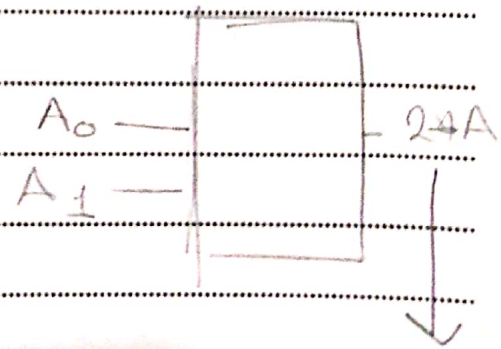
Box 2 0 or 1

Box 3 X

Box 4 1 or x or y

Problem 10 write the truth table for a combinational logic circuit that takes as an input a 2 bit binary number A and produces as an output the multiplication of A by 2.

$A \times 2$	$A_1 A_0$	$O_2 O_1 O_0$
0	← 0 0	0 0 0
2	← 0 1	0 1 0
4	← 1 0	1 0 0
6	← 1 1	1 1 0



2 bits ← out of $A_1 A_0$

output 3 bits ← out of $A_1 A_0$