

\* Power =  $I \times V$       unit :- watt.

⊕ sign → the element absorbs power.

⊖ sign → the element generates power.

+ Power absorbed = - Power generated.

\* Current should enter through the positive polarity of the voltage.

\*  $\sum P = 0$  → total power absorbed = total power generated.

Circuit elements :-

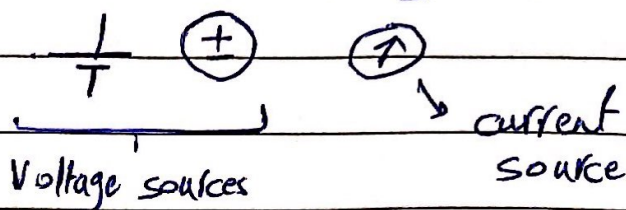
- 1) active element :- Capable of generating energy
- 2) passive element :- doesn't generate energy

ex. active elements → batteries

ex. passive elements → resistors, capacitors, inductors.

\* Current and Voltage sources :-

↳ independent → completely independent of other circuit elements.



2) dependent, controlled by another voltage or current



"diamond shape"

$$V = IR$$

$I$  :- current

$R$  :- resistance

$V$  :- Voltage.

\* short circuit  $\rightarrow V = 0, R = 0$

\* open circuit  $\rightarrow I = 0$

$$* P = VI = I^2 R = \frac{V^2}{R}$$

\* number of branches in a circuit = number of element

\* Node :- where elements connect together

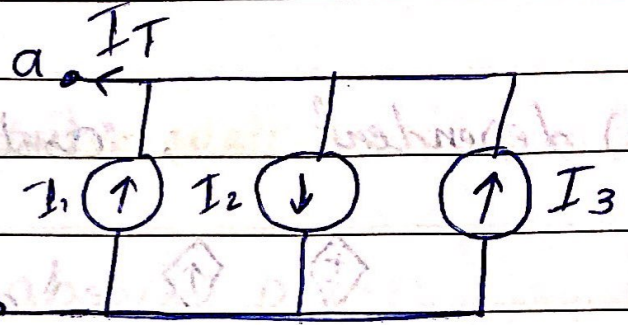
\* Loop :- closed path.

\* KCL "Kirchhoff's current law"

$$\sum I \text{ "entering a node"} = 0$$

\*  $I_{in} \rightarrow (+)$  and  $I_{out} = (-)$   
or vice versa.

$$I_T + I_2 = I_1 + I_3$$

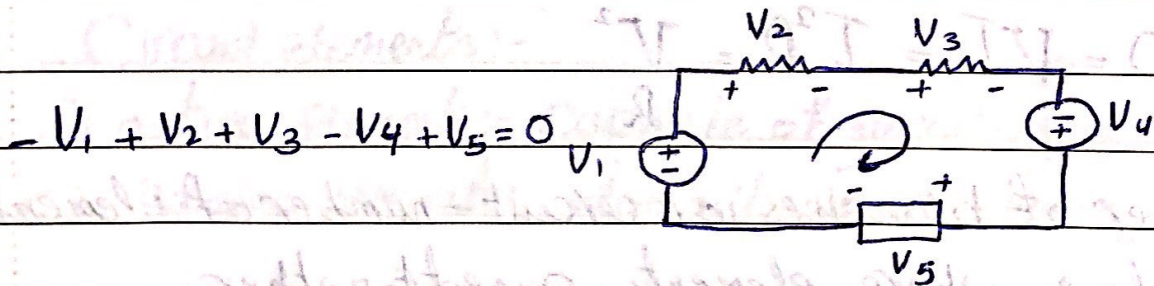


\* When the current sources are connected in parallel

\* KVL "Kirchhoff's Voltage law"

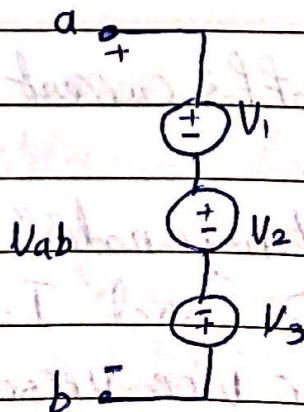
$$\sum V \text{ "around loop" } = \text{zero}$$

\* The sign on each voltage is the polarity of the terminal encountered first as we travel around the loop

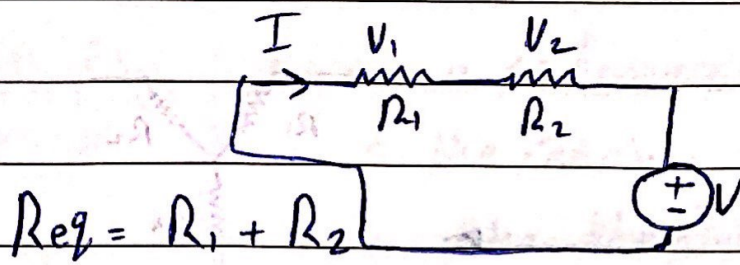


\* When the voltage sources are connected in series, KVL can be applied to obtain the total voltage source.

$$V_{ab} = V_1 + V_2 - V_3$$



Req. in series = the sum of the individual resistance



\* current division "for resistors in series"

$$V_1 = V \frac{R_1}{R_1 + R_2}, \quad V_2 = V \frac{R_2}{R_1 + R_2}$$

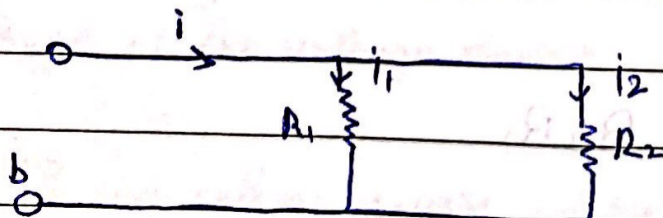
\* The larger resistance  $\rightarrow$  the larger voltage drop.

$$R_{eq} \text{ in parallel} = \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots \dots \dots \text{etc.}$$

\* for two resistors in parallel :-

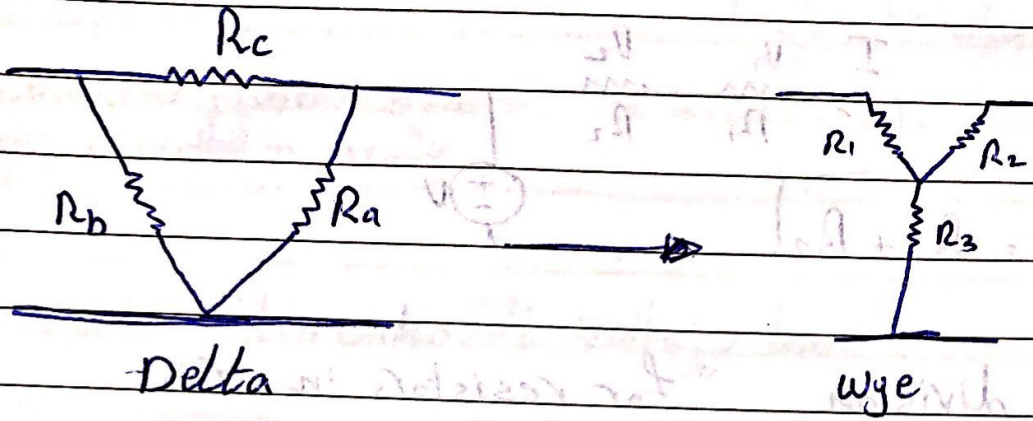
$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

\* current division "for resistors in parallel"



$$i_1 = i \frac{R_2}{R_1 + R_2}, \quad i_2 = i \frac{R_1}{R_1 + R_2}$$

\* Delta to wye conversion :-

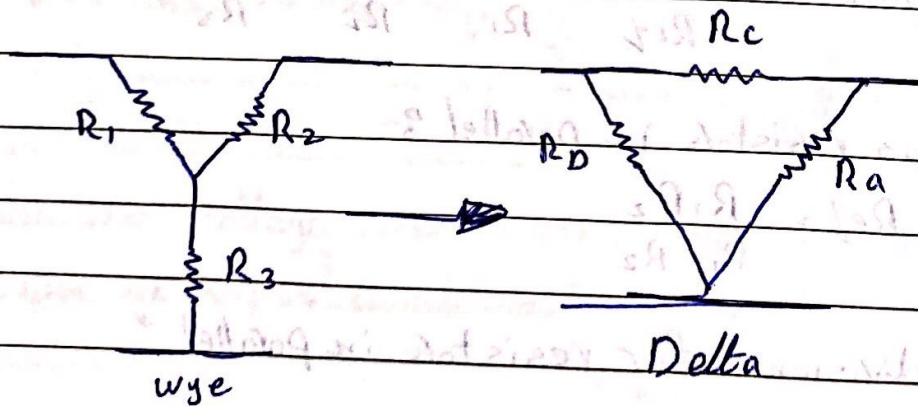


$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

$$R_2 = \frac{R_c R_a}{R_a + R_b + R_c}$$

$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

\* Wye to delta conversion.



$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

→ Nodal analysis → using nodes voltages

1- select a node as a reference node. Assign voltages  $V_1, V_2, \dots, V_{n-1}$  to the remaining  $n-1$  nodes.  
\* reference node → has the highest number of connections

2- Apply KCL to each of  $n-1$ , nonreference nodes.  
Use Ohm's law to express the branch current in terms of node voltages.

3- Solve the resulting simultaneous equations to obtain the unknown node voltages.

\* current flows from a higher potential to a lower potential in a resistor.

$$I = \frac{V_{\text{higher}} - V_{\text{lower}}}{R}$$

\* If a voltage source is connected between the reference node and a nonreference node, we simply set the voltage at the nonreference node equal to the voltage of the voltage source

\* If the voltage source (dependent or independent) is connected between two non-reference nodes, then the two non-reference nodes form one node called supernode.

\* A supernode requires the application of both KCL and KVL

\* Mesh analysis  $\rightarrow$  using mesh currents as a circuit variables.

mesh  $\equiv$  loop  $\rightarrow$  closed path.

$\rightarrow$  we apply ~~KVL~~ KVL to find unknown currents.

Steps:-

1) assign mesh currents  $i_1, i_2, \dots$  to the  $n$  meshes

2) apply KVL to each of the  $n$  meshes. Use Ohm's law to express the voltages in terms of the mesh currents

3) solve the resulting  $n$  simultaneous equations to get the mesh currents.

\* it is conventional to assume that each mesh current flows clockwise.

dependent  
independent.

\* When the current source exists only in one mesh, the mesh current is equal to the current source ~~value~~

"علاقة التفاضل"

\* When a current source exist between two meshes, we create a supermesh, by excluding the current source and any elements connected in series with it.

\* A supermesh requires the application of both KVL and KCL

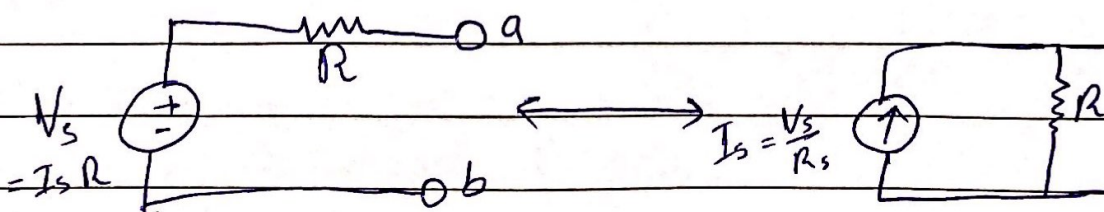
\* if we have two supermeshes then we put them in one large supermesh.

\* in superposition we consider one independent source at a time, while all other independent sources are turned off,

\* we replace every voltage source by short circuit " $V=0$ " and every current source by an open circuit " $I=0$ "

\* Dependent sources are left intact.

\* Source transformation is the process of replacing a voltage source in series with a resistor by a current source in parallel with a resistor, or vice versa. "dependent and independent sources"





## \* Thevenin's Theorem:-

$$V_{Th} = V \text{ "open circuit"}$$

- 1) If the network has ~~no~~ dependent sources, we turn off all independent sources and find  $R_{eq}$  and independent source

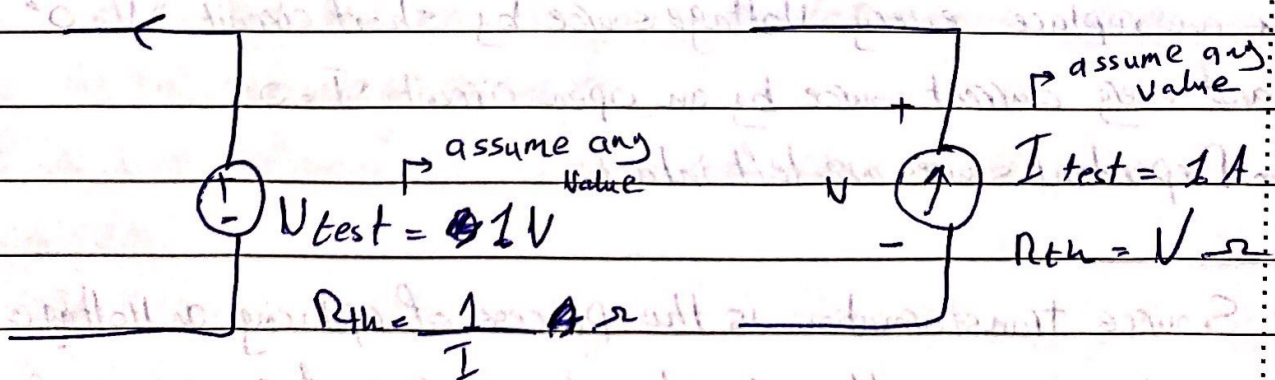
$$R_{Th} = \frac{V_{Th}}{I_{Th}}$$

~~$$R_{Th} = \frac{V_{Th}}{I_{Th}}$$~~

- 2) If the circuit has <sup>no</sup> dependent and <sup>has</sup> independent sources,  
Kill all independent sources the find  $R_{eq}$

$$R_{eq} = R_{Th}$$

- 3) If the circuit has only dependent sources.



\* Norton's theorem :-

$$R_N = R_{th}$$

$$I_N = \frac{V_{th}}{R_{th}}$$

$V_{th}$  = "V" open circuit

$I_N$  = "I" short circuit"

$$R_{Th} = \frac{V_{oc}}{I_{sc}} = R_N$$

\* Maximum power transfer = 0

$$P_{max} = \frac{V_{th}^2}{4R_{th}} \quad \text{or} \quad P_{max} = \frac{I_N^2 R_{th}}{4}$$

\* Capacitor :- Passive element and linear element.

\*  $V_c$  cannot change in zero time.

current

$$I = C \frac{dv}{dt}$$

$$V(t) = \frac{1}{C} \int_{t_0}^t i(\tau) d\tau + V(t_0)$$

stored energy in capacitor

$$W_c(t) = \frac{1}{2} C (V_c^2(t) - V_c^2(t_0)) + W_c(t_0)$$

$$\text{if } w_c(t_0) = 0 \Rightarrow V_c(t_0) = 0$$

$$W_c(t) = \frac{1}{2} C V_c^2(t)$$

\* we replace the capacitor in DC circuits by "open circuit"

\*  $C_{eq}$  for capacitors in parallel is the sum of the individual capacitances

$$C_{eq} = C_1 + C_2 + C_3 \dots$$

in series

\*  $C_{eq}$  for capacitors is the reciprocal of the sum of the reciprocals of the individual capacitances

$$C_{eq} = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots}$$

\* for two capacitors  $\rightarrow C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$

Inductors  $\rightarrow$  linear and passive elements.

$$V = L \frac{di}{dt} = \text{Slope}$$

$$I = \frac{1}{L} \int_{t_0}^t V(\tau) d\tau + i(t_0)$$

$$W_L(t) = \frac{1}{2} L (i^2(t) - i^2(t_0)) + W_L(t_0)$$

if  $w_L(t_0) = 0 \rightarrow i^2(t_0) = 0$

$$w_L(t) = \frac{1}{2} L i^2(t)$$

\* In DC circuits we replace the inductors by short circuit.

$$* \text{Leq in series} = L_1 + L_2 + L_3 + L_4 \dots$$

$$* \text{Leq in parallel} = \frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \frac{1}{L_4} \dots$$

for two inductors in parallel

$$\text{Leq} = \frac{L_1 L_2}{L_1 + L_2}$$

\*  $s \rightarrow y$  transformation can be extended to capacitors and inductors.