

Relation	R	C	L	$u(t) = \begin{cases} 0 & t < 0 \\ 1 & t \geq 0 \end{cases}$
<u>Voltage</u>	$V = IR$	$V = \frac{1}{C} \int_{t_0}^t i(t) dt + V_0$	$V = L \frac{di}{dt}$	$u(t-t_0) = \begin{cases} 0 & t < t_0 \\ 1 & t \geq t_0 \end{cases}$
<u>Current</u>	$I = \frac{V}{R}$	$I = C \frac{dV}{dt}$	$I = \frac{1}{L} \int_{t_0}^t V(t) dt + I_0$	$u(t-t_0) = \begin{cases} 0 & t < t_0 \\ 1 & t \geq t_0 \end{cases}$
<u>P/w</u>	$P = \frac{V^2}{R}, I^2 R, IV$	$W = \frac{1}{2} CV^2$	$W = \frac{1}{2} LI^2$	

Chapter 70

RC-circuit

- Discharge $V(t) = V_0 e^{-t/\tau}$
- V is the voltage of capacitor
- Charge $V(t) = V_{\infty} + [V_0 - V_{\infty}] e^{-t/\tau}$

$\tau = RC$

RL-circuit

- Discharge $I(t) = I_0 e^{-t/\tau}$
- I is the current of inductor
- Charge $I(t) = I_{\infty} + [I_0 - I_{\infty}] e^{-t/\tau}$

$\tau = \frac{L}{R}$

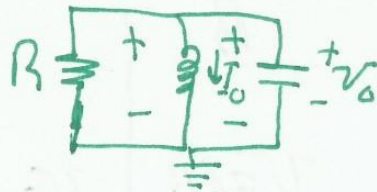
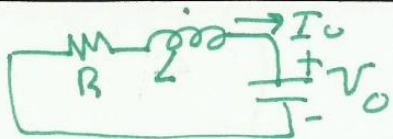
If the C or L charge or discharge at $t \neq 0$

Then $e^{-t/\tau} \Rightarrow e^{-(t-c)/\tau}$

c is the time when it charge or discharge

Tip: The Rules at Top of the Page are for current going from t to $-$

Ch 80 -



Series RLC circuit

$$\alpha = \frac{R}{2L}, \omega_0 = \frac{1}{\sqrt{LC}}, s_1 = -\alpha + \sqrt{\alpha^2 - \omega_0^2}$$

$$s_2 = -\alpha - \sqrt{\alpha^2 - \omega_0^2}$$

$\left. \begin{matrix} \alpha > \omega_0 & \text{over} \\ \alpha = \omega_0 & \text{critical} \\ \alpha < \omega_0 & \text{under} \end{matrix} \right\} \text{Damping}$

$$\omega_d = \sqrt{\omega_0^2 - \alpha^2}$$

$$u(-t) = \begin{cases} 0 & t > 0 \\ 1 & t \leq 0 \end{cases}$$

Discharging

$i(t)$ is the current of inductor

$$\alpha > \omega_0 \quad i(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t}$$

$$\alpha = \omega_0 \quad i(t) = (A_2 + A_1 t) e^{-\alpha t}$$

$$\alpha < \omega_0 \quad i(t) = e^{-\alpha t} (B_1 \cos(\omega_d t) + B_2 \sin(\omega_d t))$$

$$\left(\frac{di(0)}{dt} = -\frac{1}{L} (R I_0 + V_0) \right)$$

Always check polarity of capacitor here

Charging

$v(t)$ is the voltage of capacitor

$$\alpha > \omega_0 \quad v(t) = V_{\infty} + A_1 e^{s_1 t} + A_2 e^{s_2 t}$$

$$\alpha = \omega_0 \quad v(t) = V_{\infty} + (A_1 + A_2 t) e^{-\alpha t}$$

$$\alpha < \omega_0 \quad v(t) = V_{\infty} + (A_1 \cos \omega_d t + A_2 \sin \omega_d t) e^{-\alpha t}$$

$$i(0) = C \left(\frac{dv(0)}{dt} \right)$$

Parallel RLC circuit $\alpha = \frac{1}{2RC}, \omega_0 = \frac{1}{\sqrt{LC}}, \frac{dv(0)}{dt} = -\frac{(V_0 + R I_0)}{RC}$

Discharging

voltage of capacitor

$$\alpha > \omega_0 \quad v(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t}$$

$$\alpha = \omega_0 \quad v(t) = (A_1 + A_2 t) e^{-\alpha t}$$

$$\alpha < \omega_0 \quad v(t) = e^{-\alpha t} (A_1 \cos(\omega_d t) + A_2 \sin(\omega_d t))$$

Charging $i(t) = I_{\infty} + A_1 e^{s_1 t} + A_2 e^{s_2 t} \quad (\alpha > \omega_0)$

$$i(t) = I_{\infty} + (A_1 + A_2 t) e^{-\alpha t} \quad (\alpha = \omega_0)$$

$$i(t) = I_{\infty} + (A_1 \cos \omega_d t + A_2 \sin \omega_d t) e^{-\alpha t} \quad (\alpha < \omega_0)$$

current of inductor

$$v(0) = L \left(\frac{di(0)}{dt} \right)$$