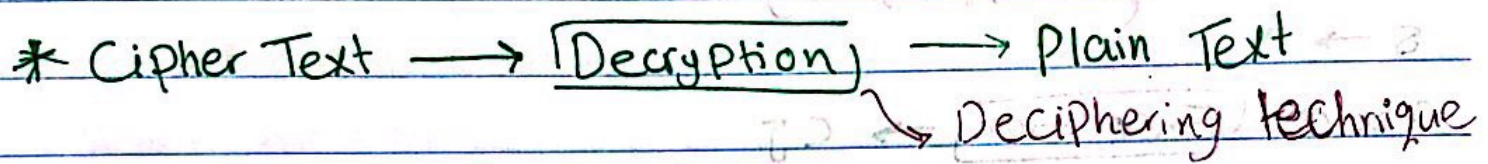
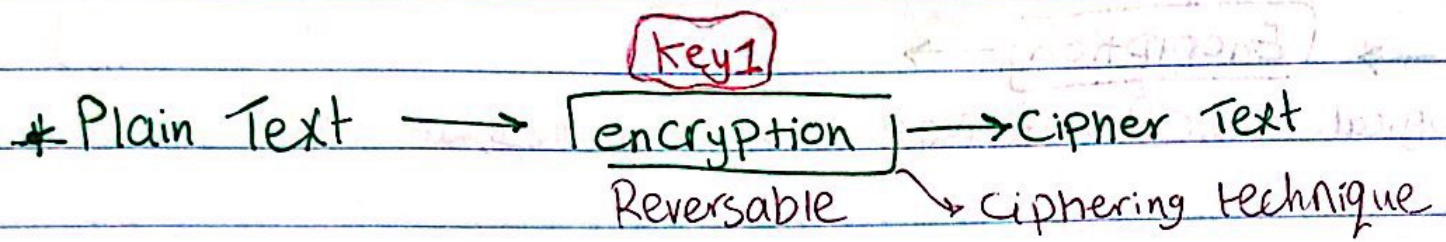


• Cryptology : encryption and decryption



• Cryptanalysis : Try to guess the key or the plaintext based on the algorithm and the cipher text

\* We always assume that the encryption and decryption algorithm is known to everybody

\* The only secure thing is the key

• Symatric encryption  $\Rightarrow$  Key 1 = Key 2

• Asymatric encryption  $\Rightarrow$  Key 1  $\neq$  Key 2

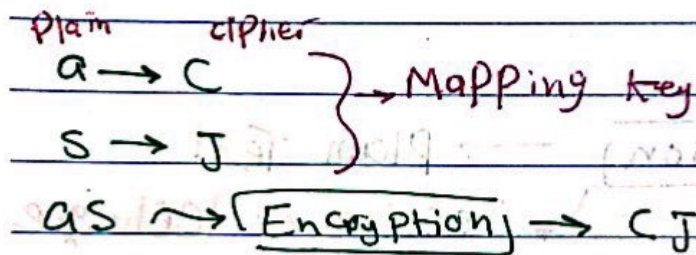
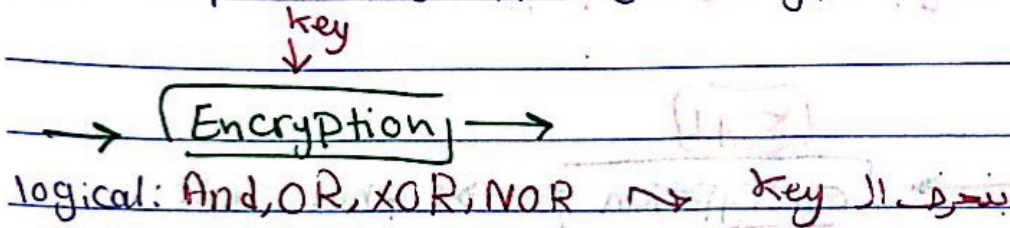
• senario: Alice message  $\rightarrow$  Bob

eve

Active attack : Try to manipulate the data

Passive attack : Will not destroy or change the data, only interrupt (sniff or collect) the ~~data~~ <sup>data</sup>

## \* Simple and naive encryption techniques:



## ~~Popular~~ Popular algorithms 8 2001

Symmetric	<del>DES</del>	- Diffie-Hellman	Asymmetric
	<del>3DES</del>	- ElGamal	
	AES	- Elliptic Curve	
	<del>RSA</del>	- RSA	

It is a bad idea to design your own encryption technique

\* Any algorithm should be secured against two things of

(1) cryptanalysis

(2) brute force attack: try every possible key or every

possible plain-text to guess the key

Problems with asymmetric: They need high processing memory and time

## \* Hash Function:

Variable size text → hash Function → Fixed length hash value

→ Satisfies the data integrity

• Data integrity: make sure that the data was not manipulated or change

↳ by encryption

• Data confidentiality make sure that only legitimate users can use the data

↳ by hashing

• Authentication: make sure that you talk to the claimed side

## • Risk management

- ↳ How possible a risk will happen?
- ↳ What is the cost to prevent this risk?
- ↳ What is the cost if the risk happened?
- ↳ In case the risk happened, how long will take to recover from it? and what is the cost to recover -
- ↳ Cost-benefit-analysis

## • Passwords Design very strong password system

- ↳ Password is sent encrypted
- ↳ Minimum length is 15 characters
- ↳ Small & Capital letters
- ↳ Special characters
- ↳ Cant put 3 consecutive numbers or letters

## • Detect trial of attack? check logs

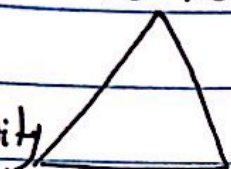
## • Physical security :

\* Social engineering : based on social information about the victim , try to do some attacks

\* Phishing : send an email to somebody with fake links to make the victim open malicious web sites or files.

Confidentiality

availability



integrity

- Cryptographic: Solves Problems related to:
  - Confidentiality
  - Integrity
  - Availability
  - Non-Repudiation: To prevent somebody from denying his actions.

• Accountability: know who is responsible about each action

• Anonymity: Nobody knows where I am by just seeing my buy order

\* Cryptographic:

1- Substitution: Replace "a" by "c"  
Replace "lol" by "lll"

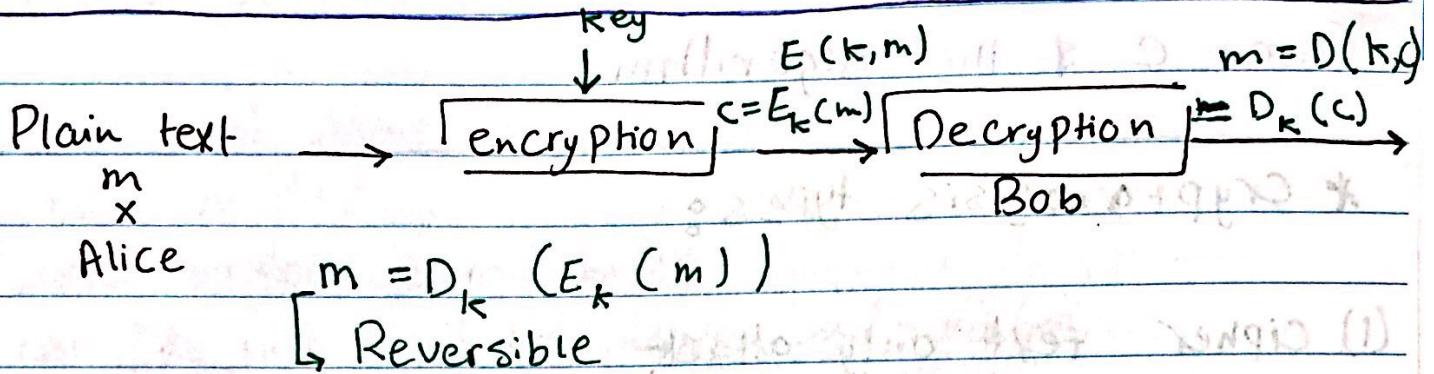
2- Transposition: Replace letter with position "x" by letter with position "y"

Key : Secret part  $\rightarrow$  Not easy task

Random

$\rightarrow$  For totally random secret each bit ( $b_i$ )

Should equal 0 or 1 with Probability  $\frac{1}{2}$



- The standard solutions are well tested and not subject to reverse engineering

- it is easier to share a key than an algorithm

\*insider attack : Changing the key is much easier than changing the algorithm

\*Any cryptographic algorithm must be secure. However it could be

$\rightarrow$  only one example : one-time - Pad

(1) Unconditionally secure : whatever money, processing, memory (resource) you have, you can't break it

$\rightarrow$  most of algs are :

(2) Computational secure : you can break it if you have enough resources. However the required resources are more expensive than the secret data

\* The cryptanalysis: Tries to find  $m'$  or  $k'$  such that

$$m' = m$$

$$k' = k$$

or part of them

Given  $C$  & the algorithm:

\* Cryptanalysis types:

(1) Cipher text only attack

Pair of

(2) Known Plain text: Ciphertext, algorithm, plaintext, try to guess the key or ~~subsequence~~ Subsequent messages

(3) Chosen Plain text: The attacker chooses the plaintext and asks one Party to encrypt using the shared key with the second Party

→ attacker knows the ciphertext of a chosen plaintext and the algorithm





- If you can do  $10^6$  decryption per second  
how long we need to break it on average?

$$\frac{4 * 10^{26}}{10^6} / 2$$

$$= 2 * 10^{20} \text{ seconds}$$

$$= 5.5 * 10^{16} \text{ hours}$$

$$= 2.3 * 10^{15} \text{ days}$$

$$= 6.3 * 10^{12} \text{ years}$$

\* Frequency analysis :

For each letter in the cipher text, find its  
frequency

\* Poly-alphabetic encryption: each letter may be represented by multiple letters

→ We need a way for reverting it

aa	CX
ab	Cd
ac	⋮
⋮	⋮

• Diagrams: The frequency of 2 letters are the same in Plain text & cipher text: ex: Th, is, io

• Example of Poly-alphabetic encryption:

Vigener cipher: another version of Shift cipher & Poly-alphabetic cipher.

Shift cipher

→ ~~Encryption~~:  $(P_i + Key) \bmod 26$

→ Vigener cipher:  $(P_i + k_i) \bmod 26$ , key size = message size

\* key word: repeat it

as many times as you want

ex: Plain text length = 1000 letter

Key word = Key

→ key word word word ... 250 times

word عدد احرف

$$1000 \div 4 \approx 250$$

• Assuming we know the key size  $\rightarrow$  Frequency analysis

$(P_1, P_{10}, P_{19}, P_{28}, P_{37}, \dots)$

$P_2, P_{11}, P_{20}, P_{29}, P_{38}, \dots$  Freq will be as in

Plain text

$$\sum_{i=1}^{26} (P_i)^2 = 0.065$$

• For key size: 1 to 20

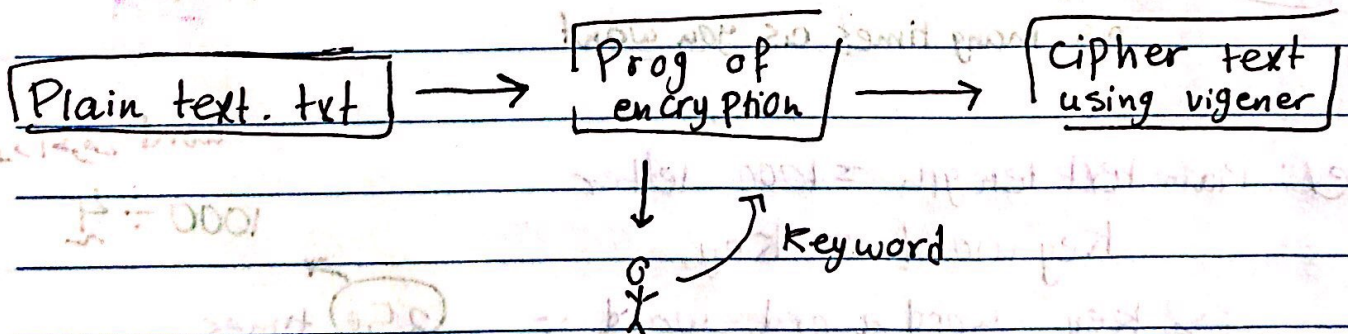
~~do freq~~

do Freq analysis on  $\{(P_i \text{ \# key size})\}$

where  $i$  in  $\frac{\text{Plain text size}}{\text{key size}}$

if  $\sum (P_i)^2 \approx 0.065$  return key size

• Assignment: 2 Parts encryption, decryption (5 marks)



• bonus: ~~find~~ return at least letters (+2)

Cipher text.txt  $\rightarrow$  Hacking  $\rightarrow$  Size of key

• Defining Secrecy:

$P(m' = m | C) = P(m' = m) \Rightarrow$  cipher text gives you no information about the plaintext

where  $\alpha = 0.00000001 \Rightarrow$  not perfectly secure <sup>u</sup>

if  $\alpha = 0$  Perfect secure

## Properties of one time pad

- The key is truly random & of the same length of message

$$0 \neq 1: P(K_i) = \frac{1}{2}$$

$$P(K_i=0 | K_j) = \frac{1}{2} \quad \forall j < i$$

If you know all previous bits of the key, probability of the next bit = 1 or 0 =  $\frac{1}{2}$

• Encryption in OTP :  $C_i = m_i \oplus k_i$

$$\begin{aligned} \text{• Decryption in OTP : } m_i &= c_i \oplus k_i \\ &= (m_i \oplus k_i) \oplus k_i \\ &= m_i \oplus (k_i \oplus k_i) \\ &= m_i \oplus 0 \\ &= m_i \end{aligned}$$

• Pure random :  $P(K_i=0) = \frac{1}{2}$  ,  $P(K_i=1) = \frac{1}{2}$

$$P(m_i=0) = x$$

$$P(m_i=1) = 1-x$$

$m_i$	$P(m_i)$	$k_i$	$P(k_i)$	$c_i$
0	$x$	0	0.5	0
0	$x$	1	0.5	1
1	$1-x$	0	0.5	1
1	$1-x$	1	0.5	0

$$P(E_1 \cup E_2) = P(E_1) + P(E_2) - P(E_1 \cap E_2)$$

$$P(E_1 \cap E_2) \text{ if } E_1 \text{ \& } E_2 \text{ are independent} = P(E_1) \times P(E_2)$$

$$P(c_i = 0) = P[(m_i = 0 \text{ \& } k_i = 0) \cup (m_i = 1 \text{ \& } k_i = 1)]$$

$$= P(m_i = 0 \text{ \& } k_i = 0) + P(m_i = 1 \text{ \& } k_i = 1)$$

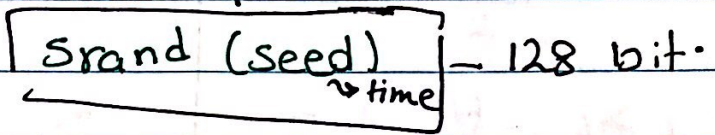
$$= x \cdot \frac{1}{2} + (1-x)$$

rand() → Random Value between (0, 1)

For random value between (0,  $10^{19}$ )

~~rand~~

(int) rand \*  $10^{19}$



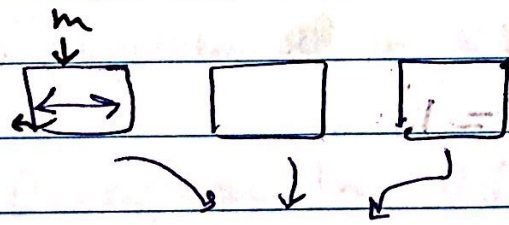
Alice & Bob agreed on the seed (initial key)

$k_1 = \text{Srand}(\text{seed}) \rightarrow 128 \text{ bits}$

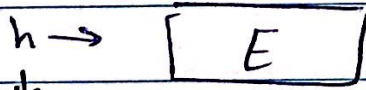
$k_2 = \text{Srand}(k_1)$

$k_i = \text{Srand}(k_{i-1})$

# Block Ciphers



Block size is determined by enc algorithm



large : To prevent brute force attack

64  
128 bits

DES block size = 64 bits

DES key = 56 bits out of 64 bits

\* Feistel network: A general architecture can be used by anybody to design his own encryption algorithm

\* DES used Feistel network

\* Same block repeated many times (iteration)

\* Avalanche effect: Change in any bit of the inputs (key & message) will change approximately half of the output (cipher text)

\* Repetition of some block  $\rightarrow$  reduce code size that can be deployed on tiny devices and makes HW implementation easier

\* Each round uses a key that is designed from original key

~~RE<sub>i</sub> = LE<sub>i-1</sub>  $\oplus$  F(k<sub>i</sub>, RE<sub>i-1</sub>)~~

$$RE_i = LE_{i-1} \oplus F(k_i, RE_{i-1})$$
$$LE_i = RE_{i-1}$$

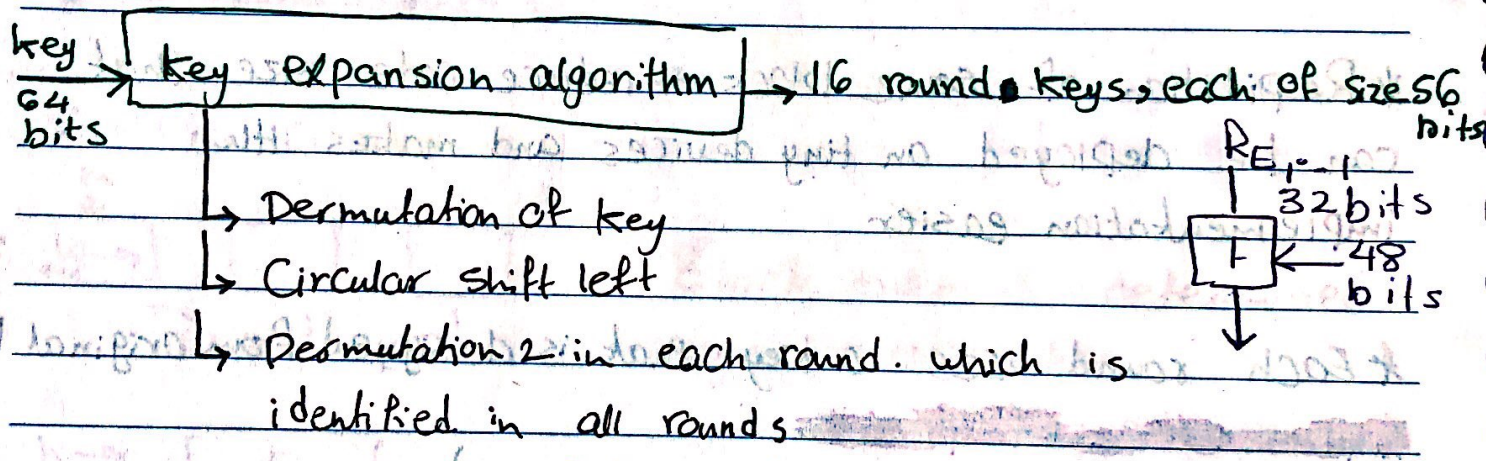
\* Parameters of Feistel:

- Key size, trade off between security and efficiency
- Round function: non-linear function & non piece-wise linear function
- # of rounds: trade of security & time
- Block size: trade of security & time
- Round key generation algorithm



Ⓔ Same for encryption and decryption  
 no need for  $F^{-1}$  for decryption

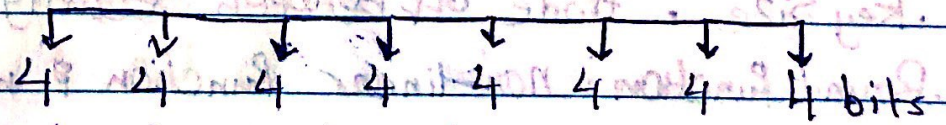
\* Same code for encryption and decryption  
 \* Other than the first permutation and last inverse permutation, DES has exactly Feistel structure



\* Round function is composed of 4 steps:

~~1- Expansion~~

1- Half block expansion: input is half block of size 32 bits  
 → output (48 bits)



48 bits

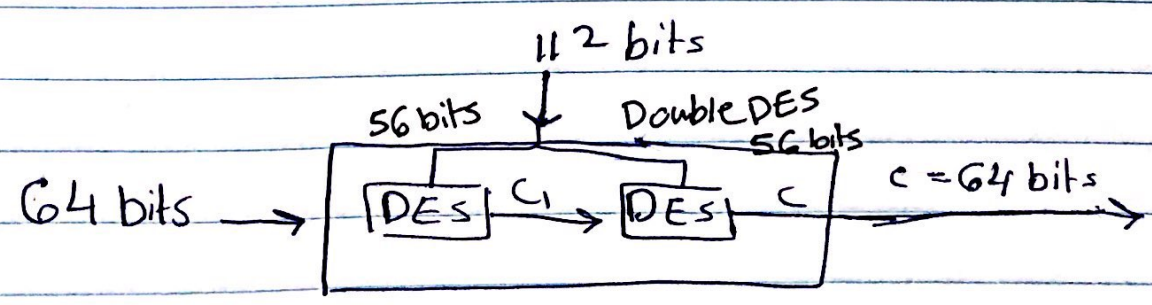
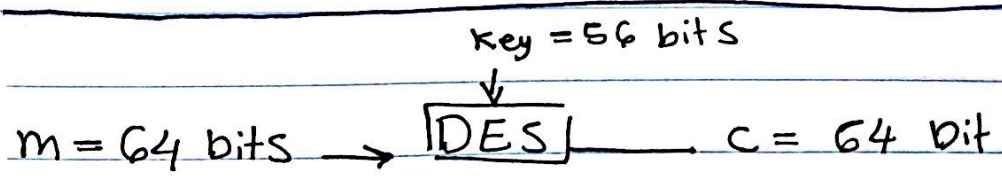
- 2) XOR 48 expanded word and the round key
- 3) apply S-boxes on the generated 48 bits to generate 32 bits

S-Box: A Look up table (16 columns)  
 makes round function non-linear

0000	4) permutation
0000	
64 rows	
⋮	
1111	

● Avalanche effect

- ↳ SAC :
- ↳ BIC :



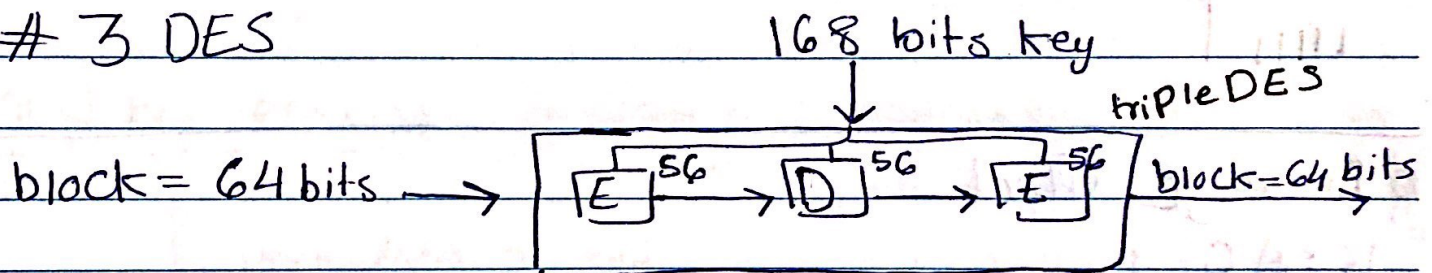
Theoretically = Brute force attack  $\Rightarrow$  on average we need  $2^{111}$  decryption

• Meet in the middle attack

- if you have a single pair of plain text / cipher text  
I will build a table of  $2^{56}$  rows, each row contains the enc of the plain text using the possible keys [ $2^{56}$  keys]

$E_{k_i} \cdot (P)$	$2^{56}$	→ on avg $\frac{2^{56}}{2}$ to break it
---------------------	----------	--

# 3 DES



168  $\xrightarrow{2^{167}}$  as efficient as 112  
↳ not efficient, regarding key size  
↳ Slow

# Rijenaal

↳ AES :

128 bits block size

128 bits cipher text

AES

128 bits

44 words

Key Size

16 bytes

round 0 +

[10 rounds] ↳ 128 bits (16 bytes) (4 words) initial state ↓

52 round 0 + [12 rounds] ↳ 192 bits (24 bytes) (6 words)

round 0 + [14 rounds] ↳ 256 bits (32 bytes) (8 words)

60 words

0	4	8	12
1	5	9	13
2	6	10	14
3	7	11	15

\* Several rounds

\* Key expansion algorithm: takes as input the original key, and it expands it to several round keys

• Round 0 is just add round key

• Each round has 4 steps, except for the last round 3 steps

↳ substitute bytes: Lookup table → 8 bits input → 8 bits output } non-linearity

↳ Shift rows

↳ Mix Columns: Matrix multiplication  $a_{ij} = \sum_{row}^{4 \times 4} * Column_j$

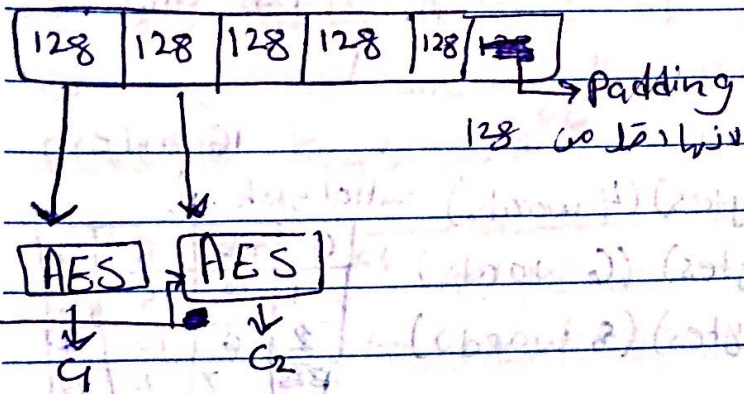
↳ Add round keys: Bitwise XOR operation

• DES: Same code for enc & dec

• AES: not same code for enc & dec, you need inverse function

\* Modes of encryption: when you have large text and you want to encrypt using block cipher algorithm, how you divide it

ECB



\* Adv:

- 1) Parallel encryption & Dec
- 2) If one block was damaged, lost you can retrieve the remain (loss and noise tolerance)

# Dis: similar blocks will be encrypted to the same cipher

Don't use ECB for long texts  
Sol: if one block was repeated in the plaintext, it should give different cipher texts

- CBC: No parallelism (you can't encrypt block  $i$  before block  $i-1$ )
  - Not tolerant to loss or noise
  - The initialization vector should be kept secret & you may exchange it using ECB encryption
- adv: you can use it to achieve data integrity

• You can ~~choose~~ use any of the block cipher as stream cipher.

## # Cipher Feedback mode [CFM]

**Adv:** you can use it as stream cipher regardless of the plain text size

→ Same blocks will be ~~encrypted~~ encrypted differently

→ Same Code

**Disadv:** IV "Initialization vector"

↳ should be unpredictable

→ No parallelism

→ loss and noise effect

→ known plain text attack if same initialization vector

For multiple messages

## # Output Feed back mode [OFM]

nonce → A value that keeps changed

[Counter, timer, Date]

⊕ can be used as stream cipher

⊕ Pre-Processing

⊕ loss and noise tolerance

⊕ Same Code

- ⊖ Keep changing nonce
- ⊖ Known Plaintext attack (same nonce)  
retrieve all subsequent messages that are encrypted using same nonce

# Counter mode [CTR] the simplest

⊕ HW and SW efficient

⊕ Parallel

⊕ different cipher for same block

⊕ Same code for enc/dec

⊕ Pre processing

⊖ Counter

⊖ moderate affect for noise or loss

• Message authentication (2 solutions)

↳ Data integrity: the message was not changed by unlegitimate user

↳ Data origin authentication: the message was created by the claimed person

Solutions:

① Add MAC = Function (M, k)

② Add digital signature

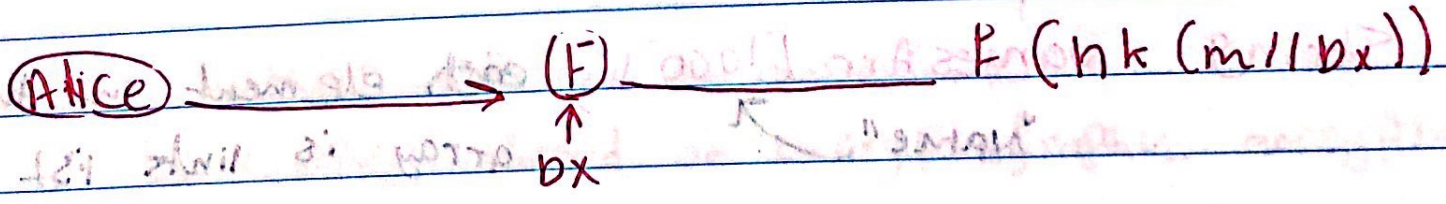
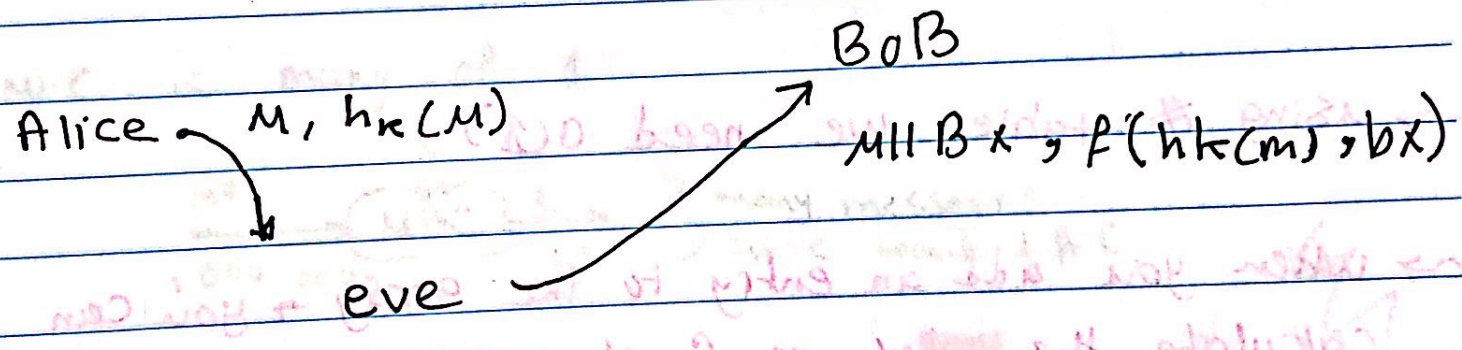
M, MAC (M, k)

- Collision: To Find 2 messages  $m \neq m'$  such that  $H(m) = H(m')$

Pre-Image  $\rightarrow$  Much more difficult

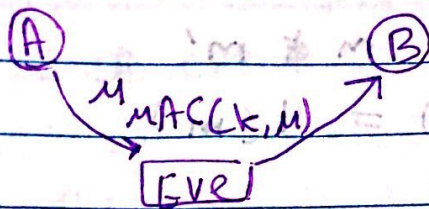
if hash value is of length  $n$  we need to check on average  $\frac{2^n}{n}$  messages to find pre-Image

However, to find collision we need to check  $2^{n/2}$  messages



# much faster  
 $k' = k ||$  [zeros to generate one block]  
 $H(k' || M)$





Can eve generate this?

→ NO, except if she knows  $k$

array of elements [1000] elements  
 to find the index of an element, we need  $n/2$   
 of average  $O(n)$  worst case  
 if the array is sorted, we need  $O(\log n)$   
 using binary search

→ using # table we need  $O(1)$

→ when you add an entry to the array → you can calculate the index as function of array entry

String Names Arr [1000]; each element in this array is link list  
 "name" →

hash Function of element =  $\sum$  (ASCII codes of elements) mode 1000

- Esraa → 213
- Ali → 217
- Khalid → 300

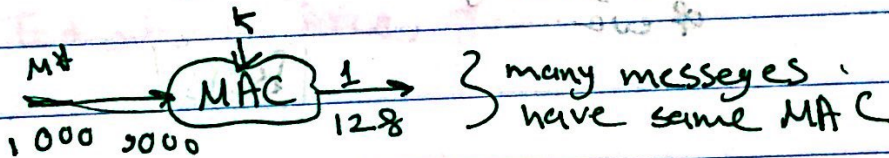
→ A good hash function, should be collision resistant  
it is not easy to find 2 values  
( $v_1 \neq v_2$ ) with  $H(v_1) = H(v_2)$

MAC  $\rightarrow$  Uses mainly hash function

\*One characteristic of hash functions that must be achieved to be one way

[Irreversible] given  $H(M)$ , you can't find  $M$

MAC is many of 1



$\infty \rightarrow 1$

MAC  $\rightarrow$  HMAC : Based on hash function

$\rightarrow$  CMAC : Based on cryptographic encryption

→ Pre-Image: if you have a message  $m$  &  $y = H(m)$   
to find another message ( $m'$ ) such that  $m' \neq m$   
while  $H(m') = y$

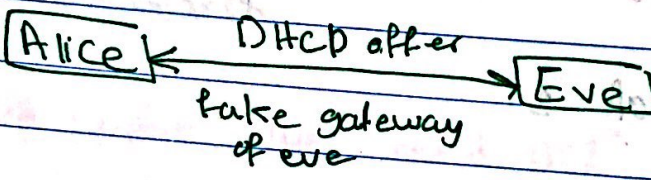
Alice Bob

eve

man in the middle attack

can be easily done

- IP-address
- subnet mask
- Local DNS IP address
- Default gateway IP address



Bob

Alice

(x) gateway

MAC of gateway

→ ARP of message broadcasted

src MAC	
Dst MAC	
src IP	
Dst IP	

↓  
Algo Cn)

if complexity =  $O(n^a)$  where  $a$  is constant

→ Feasible

→ can be solved in Polynomial time

if complexity =  $O(2^n)$  or  $(n^n)$

→ ~~is~~ NP Complete

→ None Polynomial time complex

Mike, Ted, Bob, Alice, John

EPRB (CP) → ~~is~~ (cant be implemented because  
~~not~~ PRB not available

Printed  
Alice

→ Bob

Alice knows :

- Plain text
- PRA
- RUA
- PU<sub>M</sub>
- PU<sub>T</sub>
- PU<sub>J</sub>
- PUB

EPUB (CP)  
EPUB (CP)  
EPRA (CP)

→ no benefit (useless)

because Bob does not  
know the Private key of Alice

→ Bob can decrypt

the msg because he  
knows PRB (Confidentially)

Bob can retrieve the msg

because he has the Public  
key of Alice

→ Data integrity and  
authenticity

→ Part 8 "Public key encryption"

1977 → Diffie and Hellman → for key exchange

\* Public Key encryption: everyone maintain 2 keys  
= a Public Key (PU) and a Private Key (PR)

→ The Public Key:

↳ Known to everyone → you can publish it on website

→ The Private Key:

↳ Only known by the owner → kept locally no one should have access to it

**PU PR** They should have mathematical relationship  
↳ encryption operation is a mathematical ~~operation~~ equation

any (int) ~~is~~ number (n) can be represented by the form

$$a = p_1^{a_1} * p_2^{a_2} * \dots * p_L^{a_L}$$

where  $p_i < p_{i+1}$

• Ex:  $48/2 \rightarrow 24/2 \rightarrow 12/2 \rightarrow 6/2 \rightarrow 3/3 \rightarrow 1$   
 $= 2^4 * 3$

→ The idea is based on finding large prime numbers  
 ex: (2048 or 4096 bit)

\* There is no mathematical proof that a number is  
 prime or not → there is no such function that

Fun (A) → if prime → True  
 ↳ if not prime → False

$$\frac{1}{410}$$

\* Miller-Rubin Algorithm:

↳ Takes as input integer (n) and returns:  
 in conclusion: no conclusion → probability prime →

→ if the int n is not prime → with probability  $\leq \frac{1}{4}$   
 it returns inconclusive

• composite: Definitely not prime

it will be invoked several times → if I invoked  
 it 10 times with different values of parameter "a"  
 and it returned in 10 times inclusive →

with  $(1 - \frac{1}{410})$  the number is prime

ex:  $n = 57$

$$\hookrightarrow n-1 = 2^k * q$$

$$\textcircled{1} \quad 56 = 2^3 * 7$$

$$\textcircled{2} \quad 1 < q < n-1$$

$$\textcircled{3} \quad \text{if } 3^7 \bmod 56 = 1$$

return "incomplete"

$\textcircled{4}$  for  $j = 0$  to  $k = -1$  do

$$\text{if } (3^{2^j * 0 * 7} \bmod 56 = 56)$$

return ("incomplete")

return ("complete")

→ all public encryption protocols need trap-door one way function.

\* one way function:-

it is easy to calculate  $y = f(x)$  given  $x$   
it is infeasible to calculate  $x = f^{-1}(y)$  given  $y$

\* trap door one way function:-

$y = f_K(x)$  easy given  $x \in K$

$x = f_K^{-1}(y)$  infeasible given only  $y$

$x = f_K^{-1}(y)$  easy given  $y \in K$

→ trap door one way function like factoring function.  
if you have  $a \in b$ .

is it easy to find  $n = a * b$  ✓  
given  $n$  is it easy to find  $a$  or  $b$  ✗  
is it easy to find  $a$  given  $n \in b$ .

→ RSA:- is based on factoring trap door one function.

EL-gamal & Diffie Helman they are based on discrete log trap door one way function.



$e = 7$   
 $n = 187$   
 $d = 23$   
 $m = 38$

Ex in slides.

Fermat thm: if  $P$  is prime then for all  $a$

$$a^{P-1} \equiv 1 \pmod{P}$$

$$a^{P-1} \pmod{P} = 1$$

C.R.T

$$x \equiv a \pmod{P}$$

$$x \equiv a \pmod{Q}$$

$$x \equiv a \pmod{(P \times Q)}$$

→ For correctness of R.S.A

$$M \pmod{n} = M$$

for this to be correct

$$e \times d \pmod{\phi(n)} = 1$$

$$e \times d = k \times \phi(n) + 1$$

eg.  $e = 7$ ,  $d = 11$ ,  $\phi(n) = 19$

$$e \times d \pmod{\phi(n)} = 1$$

$$e \times d = k \times \phi(n) + 1$$

$$7 \times 11 = k \times 19 + 1$$

$$k = 4 \#$$

$$x \pmod{n} = a \rightarrow x = k \times n + a$$

constant

$$x = 60, n = 8, a = 4$$

→ for correctness:-

$$M = (M^e)^d \pmod n.$$

$$M = M^{ed} \pmod n.$$

\* To Calculate Keys in RSA :-

① Choose  $p, q$  to be large prime numbers.  
[3000, 4000 bits]

$$\text{if } n = p * q$$

Prime numbers.

$$\phi(n) = (p-1) * (q-1).$$

$$p = 3, q = 7$$

$$n = 3 * 7 = 21$$

$$\phi(21) = 12.$$

1, 2, 4, 5, 8, 10, 11, 13, 16, 17, 19, 20

② calculate  $n = p * q$ .

$$\text{③ } \phi(n) = (p-1)(q-1)$$

④ select  $e$ , with  $e$  is relatively prime to  $\phi(n)$ .

⑤ calculate  $d = e^{-1} \pmod{\phi(n)}$  } there is algorithm to calculate  $d$  }  
 $d * e \pmod{\phi(n)} = 1$  }  
Given  $e \in \phi(n)$ .

$p, q, n, \phi(n), e, d$

Private.

Private.

$p, q, \phi(n) \rightarrow$  only needed only @ Key calculation then they are discarded.

RSA:- is a block cipher.

→ each block will be handled as an integer between  $0 \leq (n-1)$ , where  $n$  is typically 4096 bits

Euler Totient function  $\phi$

$\phi(n)$ :- number of integers  $< n$  that are relatively prime to  $n$ .

$x$  &  $a$  are relatively prime,  $\text{gcd}(x, a) = 1$

18, 5 ✓

12, 7 ✓

18, 6 X.

By convention

$$\phi(1) = 1$$

$\phi(p) = p - 1$ , if  $p$  is prime.

Enc in RSA :-

$$C = M^e \pmod n \quad (e, n) \text{ Public}$$

Dec :-  $(d, n)$  Private

$$M = C^d \pmod n$$

\* the only secure thing is  $d$ .

Public  $e, n$

$P, q$

Private  $d, n$

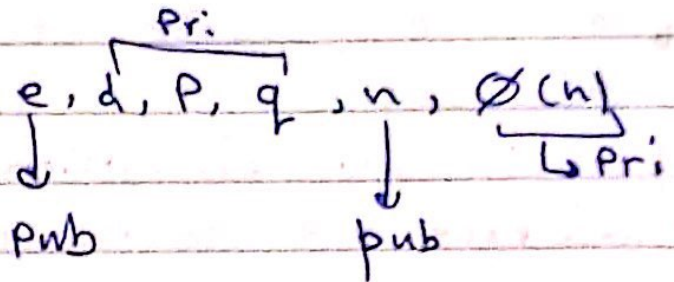
$n = P * q$

$$C = M^e \pmod n$$

$$\phi(n) = (P-1) * (q-1)$$

$$M = C^d \pmod n$$

Find  $\begin{bmatrix} e \\ d \end{bmatrix}$  st  $\text{gcd}(e, \phi(n)) = 1$   
 $d = e^{-1} \pmod{\phi(n)}$



$e, n \rightarrow d$

$\rightarrow n = P * q$

If you can factor  $n$  to  $P * q \rightarrow$  you discover the private key.

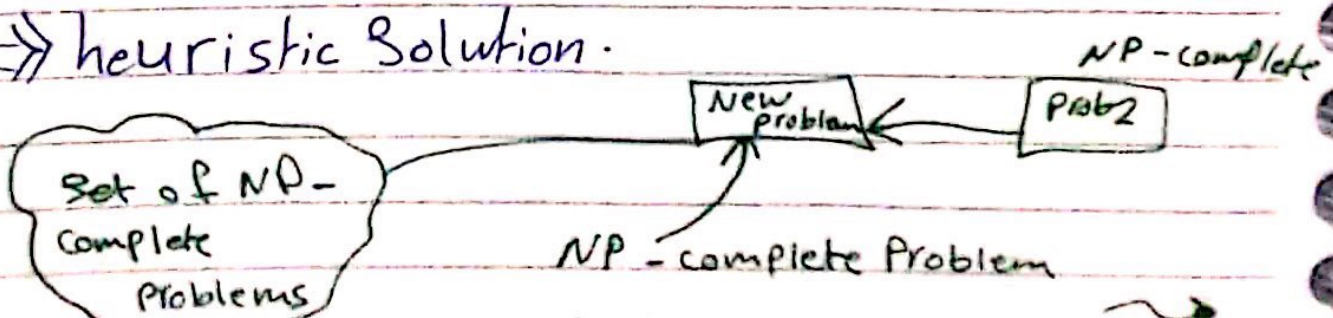
# NP-complete Problem :-

$P \rightarrow$  complexity  $O(n^a)$

NP  $\rightarrow$  complexity  $(a^n), (2^n)$

$\rightarrow$  once you prove that the problem is NP problem  $\rightarrow$  no optimal solution

$\Rightarrow$  heuristic solution.



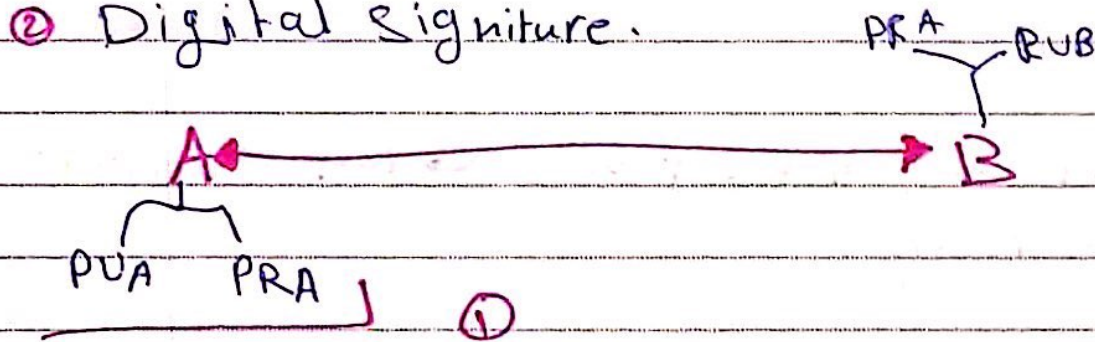
128 bits key of AES almost equivalent to 2048 bits, key of RSA

from security perspective.

4096 key size still much slower than AES Enc.

# Public Key Encryption is too slow to Enc data  
Therefore we use them only :-

- 1 Key exchange.
- 2 Digital signature.



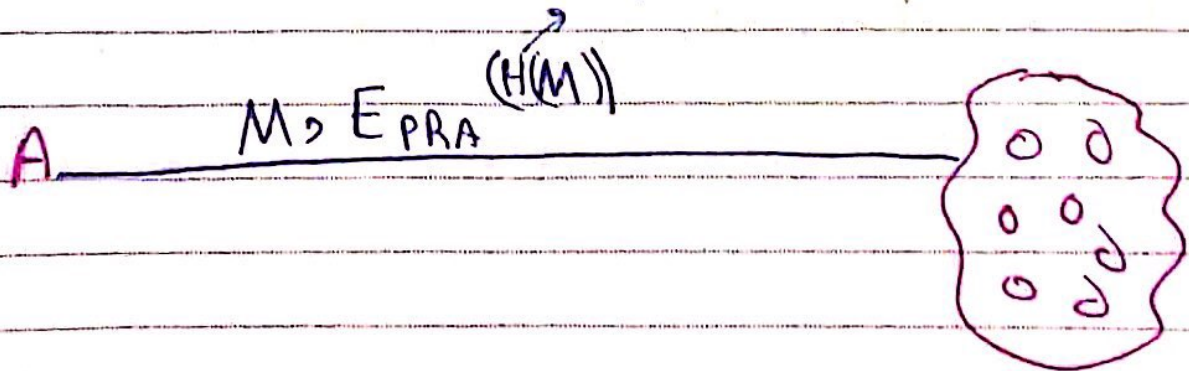
128 bits AES Key.

$$E_{PUB} ( E_{PRA} (K) )$$

(3)                      (2)

its calculation is very fast.

Hash of message.



$$M^{ed} = M^{k \times (p-1)(q-1) + 1}$$

$$\equiv M * M^{k(p-1)(q-1)}$$

$$\equiv M * [M^{(p-1)}]^{k(q-1)}$$

$$\equiv M * [1]$$

$$\equiv M \pmod{p}$$

$$M^{ed} = M^{k(p-1)(q-1) + 1}$$

$$\equiv M * [M^{(q-1)}]^{k(p-1)}$$

$$\equiv M * [1] \pmod{q}$$

$$M * 1 \pmod{q}$$

$$M^{ed} = M \pmod{q}$$

$$\rightarrow M^{ed} = M \pmod{n}$$

$$M^{ed} = M \pmod{n} \quad \#$$

message → DEC → ciphertext?

$$A^b \stackrel{?}{=} B^a$$

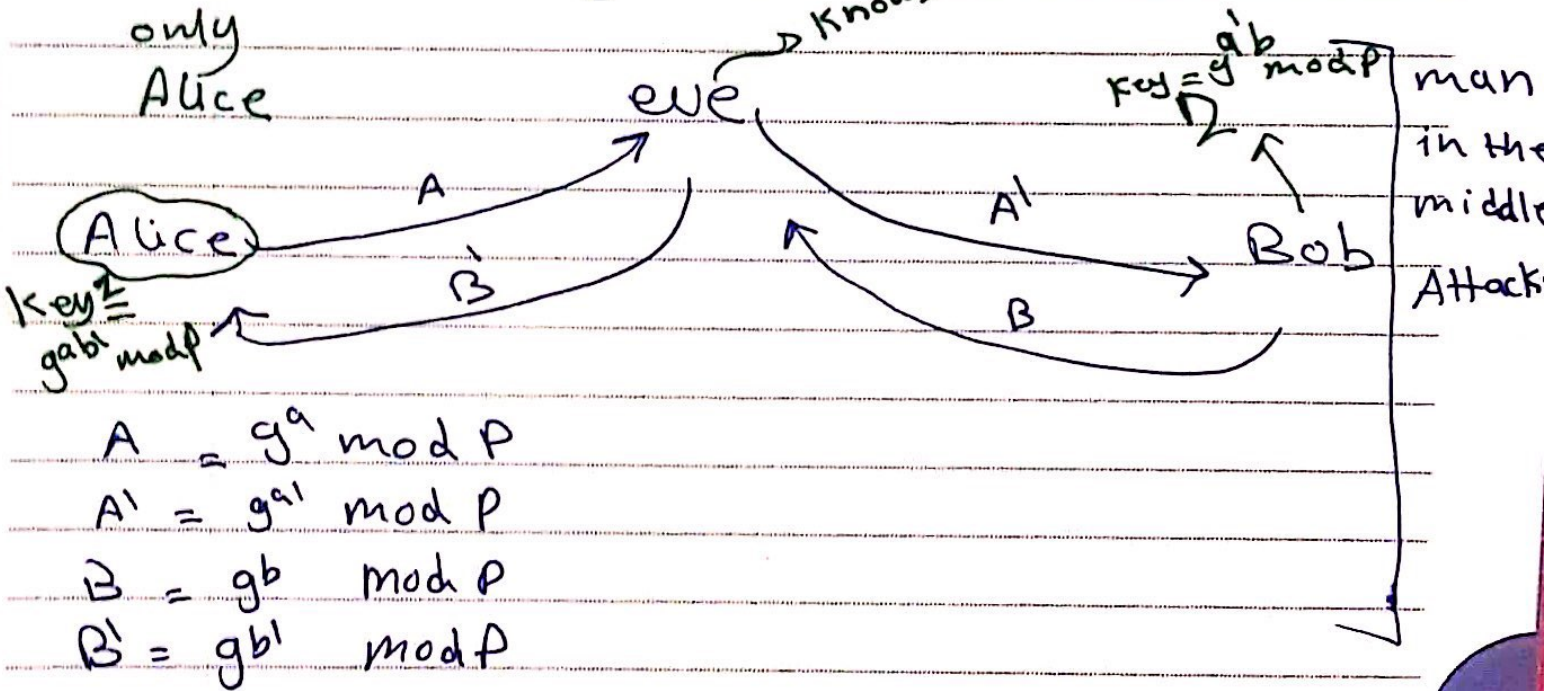
$$(g^a \text{ mod } P)^b \stackrel{?}{=} (g^b \text{ mod } P)^a$$

$$g^{a \times b} \text{ mod } P \stackrel{?}{=} g^{a \times b} \text{ mod } P$$

→ any Body knows  $g, P, A, B$  but

not  $a$  &  $b$

only Alice  
 only Bob.  
 Eve knows  $K_1, K_2$ .



each message sent from Alice to Bob will be decrypted using  $\text{Key}_1$  and then encrypted using  $\text{Key}_2$ .

$$\text{Key}_2 = g^{a'b'} \text{ mod } P$$

→ to prove that a public belongs to me I need a digital certificate signed by the private key of the CA.

✿ for anybody to verify my signature, they need to know their public key of the CA.

# usually it is embedded in the OS.

# Digital certificate has cost & expiration date.

### Diffie AND Hellman.

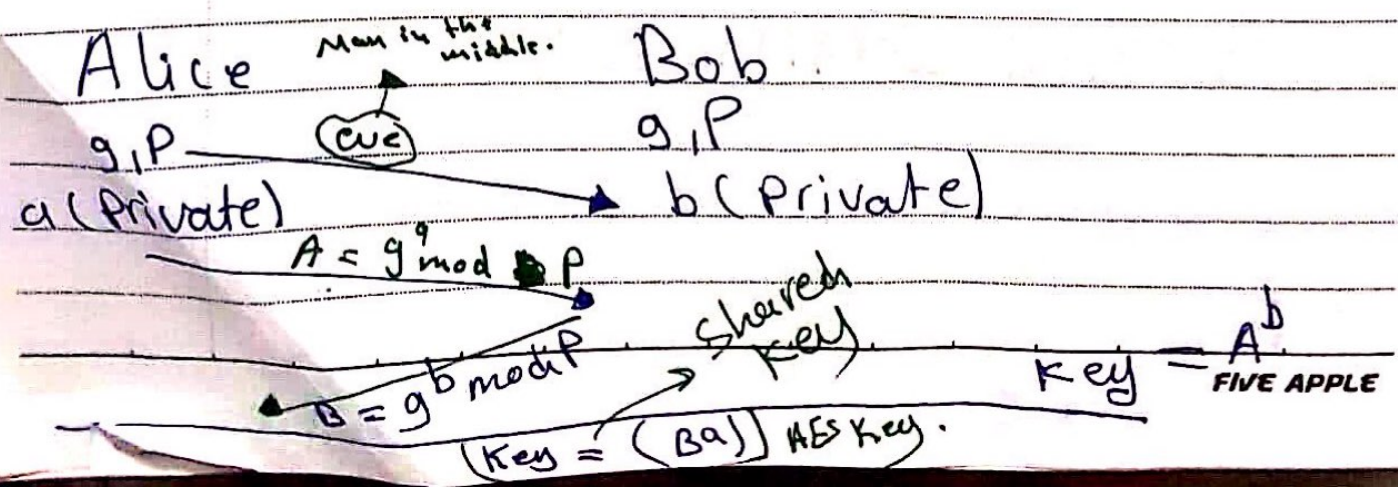
✿ No shared information between A & B.

Alice | Bob • Diffie and Hellman is based on discrete logarithm one way trapdoor function.

share a key

$$A = g^a \text{ mod } P$$

it is infeasible to know  $a$  given  $A, g, P$   
it is easy to calculate  $A$  given  $a, g, P$ .

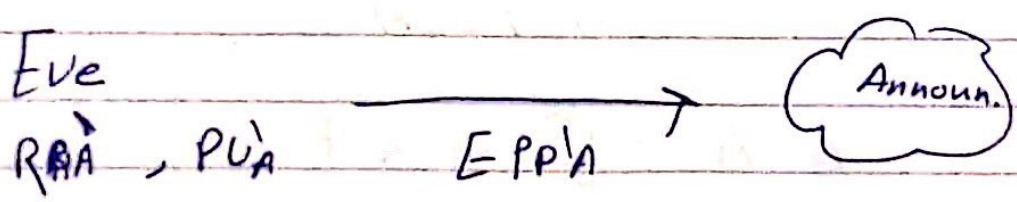
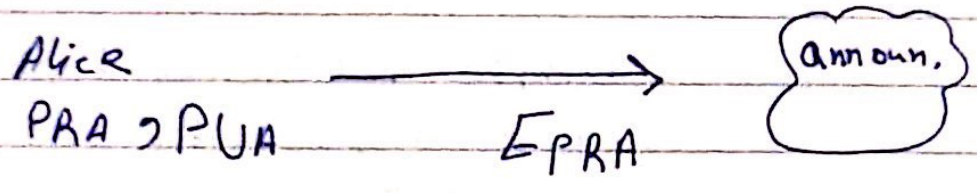
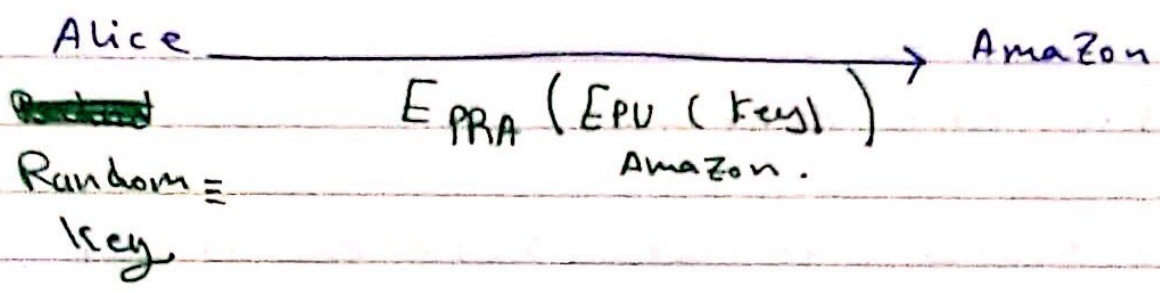




→ If you can find any polynomial time solution to one of the NP comp problems →

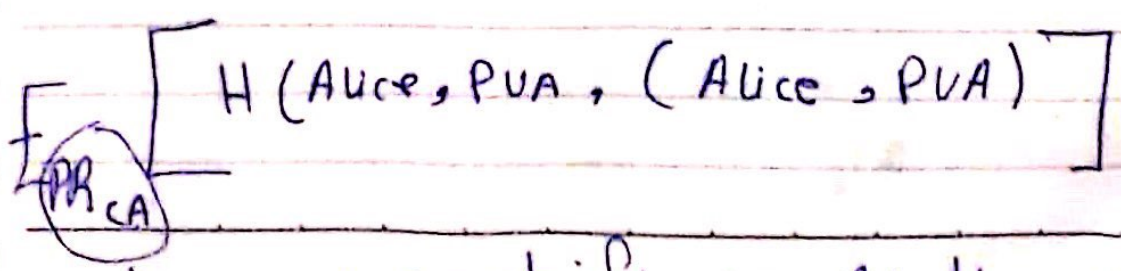
You can solve ~~NP complete~~ all of them.

$M, C$   
→ if they are very small, large.



# I need certificate for my Public Key

[ Digital certificate ]



→ certificate Authority

## \* Authentication

- Mutual authentication: The two parties don't know each other, and want to make sure of identity of each other
- Unidirectional authentication: A knows B, But not the inverse. Like log in to a website
- Sign-up: Identification to register yourself
- Verification: Introduce something to be compared with the evidence you submitted at identification phase

## \* Types of authentication:

- Something you know : Password, Pin code, Key
- " " are : Fingerprint, Face, iris, DNA, voice
- " " have : Cards (ATM, student), Dongles
- " " do : Key stroke dynamics : type behavior, mouse movements

~~Shoulder surfing~~  
~~+ easy to install & use~~  
~~Strong password need more rest~~  
~~used many times~~

## ~~Passwords & shoulder surfing~~

- know : ⊖ shoulder surfing, sticky note, stored passwords  
Strong Pass, can be guessed or ~~stated~~ stolen, used many times
- ⊕ easy to install & use
  - ⊕ suitable for remote authentication

are: ⊕ Hard to guess or steal ⊖ Not convenient

⊖ False positive or negative

⊖ Need special HW (cost)

Have: ⊖ Can be lost or stolen

⊖ Cost

⊖ Special HW

DO: ⊕ Active authentication

⊕ No need for special HW

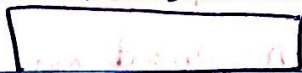
⊖ Pulse positive & negative

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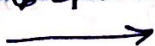
• Online attack:

• Offline attack: you can brute force attack against a password file and compare them

unix Password



64 bit



DES

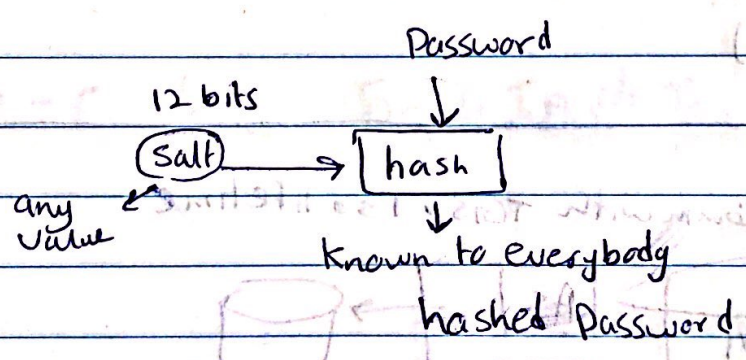


25 lines

• SysKey: you can encrypt the SAM file, and the key can be on a USB disk

• Dictionary attack: you download a dictionary  
- it may include all popular passwords  
- english words  
- you can add information about the user to it

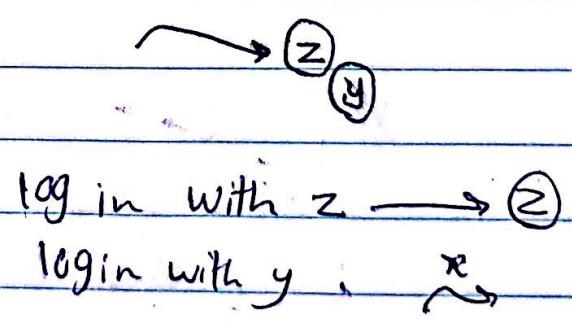
• Rainbow table: contains ~~all~~ hashes of all passwords



Rainbow table is much larger with 12 bits  
 $\Rightarrow 2^{12} \times$  old rainbow table size

• One time password: Password that can be used only once

a = random  
b = hash(a)  
c = hash(b)  
!  
z = hash(y)



• Two parties want to communicate with each other  
 Securely. Mutual authentication

↳ Public Key

↳ Trusted third Party (Symmetric Key)

