

Rotating Field of Ac Machines

Both types of Ac machines (Induction & Synchronans) have ~~the~~ identical stator (Armature), where power generated or developed

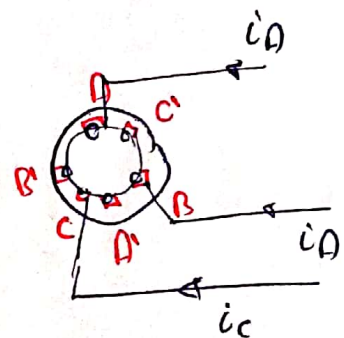
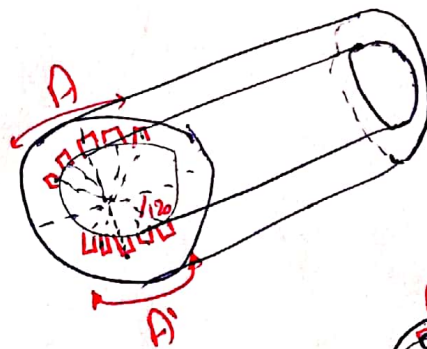
● Armature Structure :-

1) Ferromagnetic Core

- ⊕ to provide low-reluctance path for the magnetic field
- ⊕ to hold the windings of the armature

2) 3-ph windings:-

- ⊗ 3-different sets of coils physically displaced by 120° (Mech) (usually in slots)



3) 3-phase Power Supply (Balance) (certain sequences) \rightarrow the rotating direction

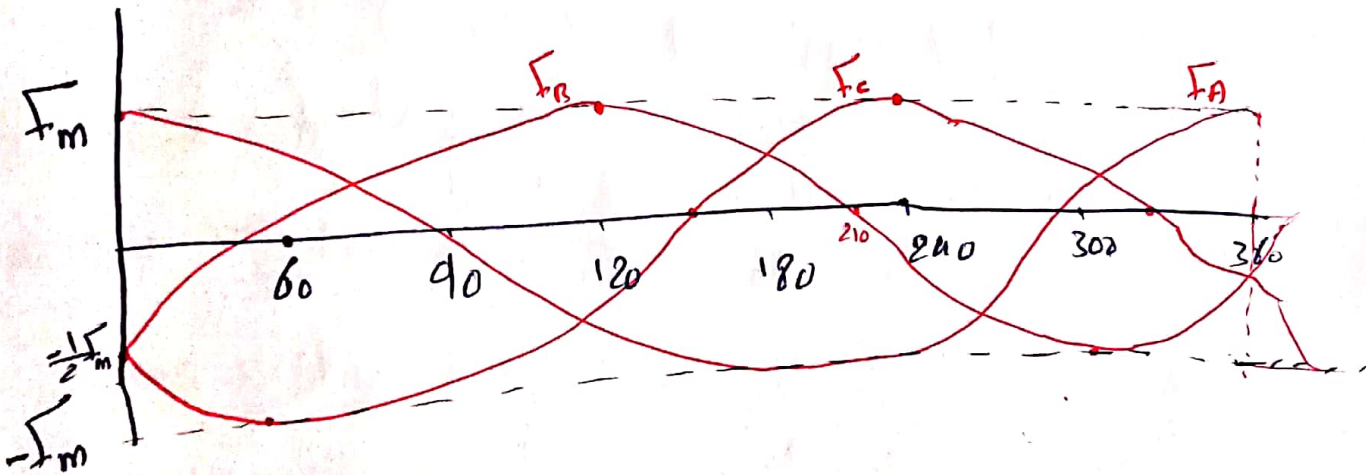
the machine is [Motor]

3-Ph Balanced Supply

$$\begin{aligned}
 i_A &= I_m \cos(\omega t) \Rightarrow \text{MMF } F_A = N_{ph} \times i_A \\
 i_B &= I_m \cos(\omega t - 120^\circ) \Rightarrow F_B = N_{ph} \times i_B \\
 i_C &= I_m \cos(\omega t + 120^\circ) \Rightarrow F_C = N_{ph} \times i_C
 \end{aligned}$$

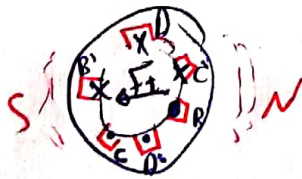
MMF Sets

$$\begin{aligned}
 F_A &= N_{ph} I_m \cos(\omega t) = F_m \cos(\omega t) \\
 F_B &= N_{ph} I_m \cos(\omega t - 120^\circ) = F_m \cos(\omega t - 120^\circ) \\
 F_C &= N_{ph} I_m \cos(\omega t + 120^\circ) = F_m \cos(\omega t + 120^\circ)
 \end{aligned}$$

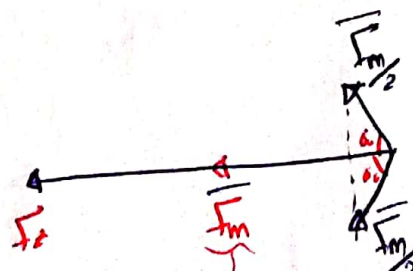


⊗ at $t=0$

$$\begin{aligned}
 F_A &= F_m \cos 0 = F_m \\
 F_B &= F_m \cos(120) = -\frac{1}{2} F_m \\
 F_C &= \frac{1}{2} F_m
 \end{aligned}$$



$$F_A + F_B + F_C = F_R$$



$$\begin{aligned}
 F_B + F_C &= \sqrt{F_B^2 + F_C^2} = \frac{1}{2} F_B F_C \cos(120) \\
 &= \frac{1}{2} F_m
 \end{aligned}$$

$F_R = 1.5 F_m$

The rotating field has same Amplitude as the previous one $\frac{3}{2}$
 i.e. $\frac{3}{2} F_m$

The Field Vector rotates in a certain direction decided by the phase sequence of the supply & if the direction is to be reversed phase sequence should be reversed

$\omega t = 90$

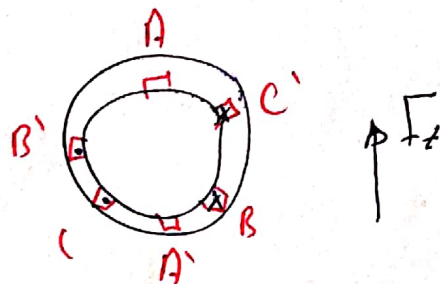
$F_A = 0 \Rightarrow \cos(90)$

$F_B = \frac{\sqrt{3}}{2} F_m \Rightarrow \cos(-30)$

$F_C = -\frac{\sqrt{3}}{2} F_m \Rightarrow \cos(210)$

The Mech speed of the rotating field vector is referred to as the Synchronous speed which is a two-pole machine is same as that of the electric currents

$\omega_m = \omega_e$



The speed of the rotating field is known as N_s : synchronous speed $\frac{4}{1}$
 (rpm) (Ws) rad/sec

$$N_s = \frac{60 \times f}{P}$$

where f frequency in Hz or cycles/sec

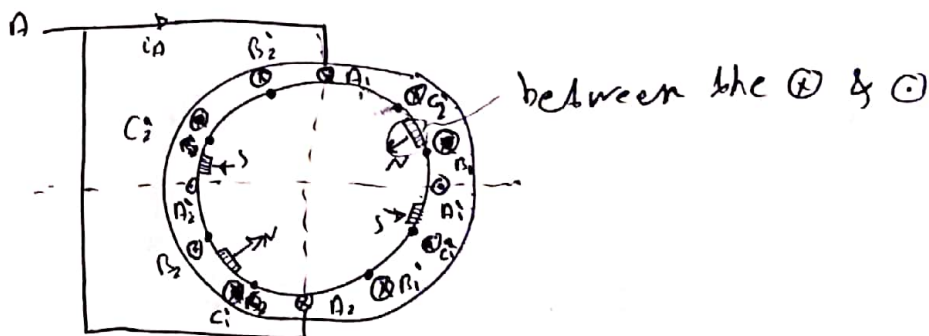
P :- No of pole pairs of the stator

50 Hz Sys \Rightarrow 3000 1500 1000 750 600 500 - - - -

60 Hz Sys \Rightarrow 3600 1800 1200 900 720 600 - - - -

Induction Asynchronous $N_m \neq N_s$

Synchronous $N_m = N_s$



$$\omega = 0$$

ω : electric freq (or speed)

To change N_s : the No of poles is to be changed from the (Design point of view)

But

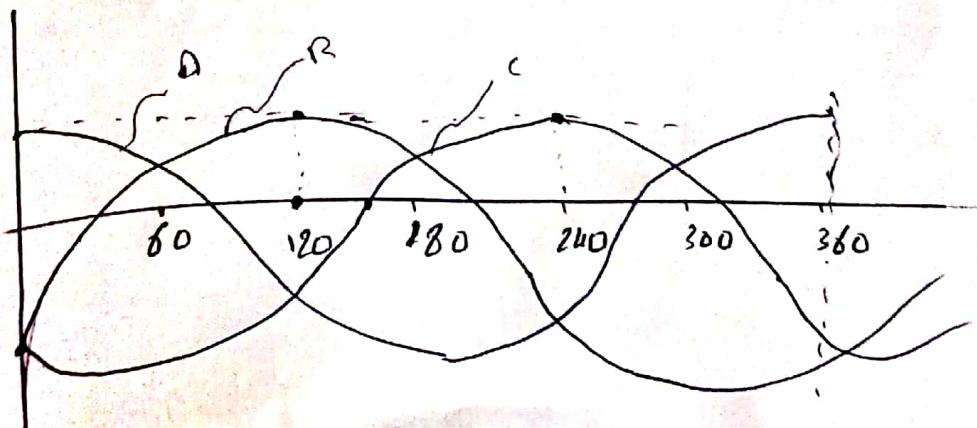
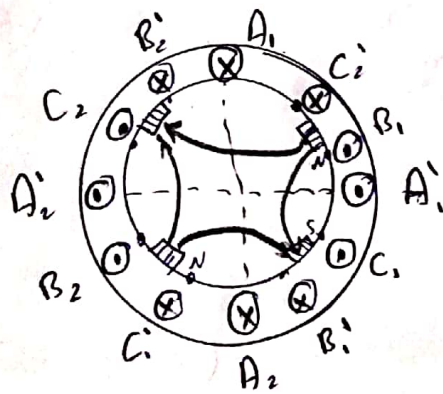
In Generators N_s can be decided by the prime mover speed

(thermal or Hydraulic)

- High speed
- low speed
- low No of poles
- High No of poles

In motors: N_s can be controlled easily by frequency

Irrespective of $\frac{P}{2}$. Amplitude of the rotating field $\frac{3}{2} I_m / \text{ph}$



* In motor N_s can be controlled easily by frequency Irrespective of P the amplitude of the rotating field still

$$\frac{3}{2} \frac{f_m}{p} \text{ph}$$

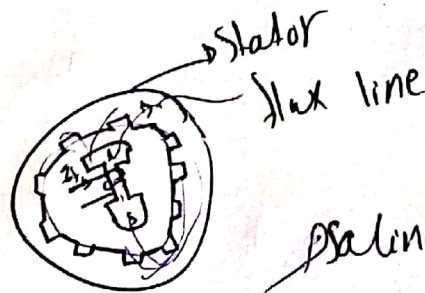
Synchronous Generators

* Two major types:-

- Salient-pole machine
 - round (or cylindrical) rotor machine
- } in both the stator in the same

~~stator~~ Rotor:

- a) permanent Magnet (small power)
- b) Electric pole (large power)



Salient-pole Machines

* I_f : the DC Field current

that usually supplies ~~current~~ the rotor to create the flux

* The stator is providing the close path for the flux ϕ

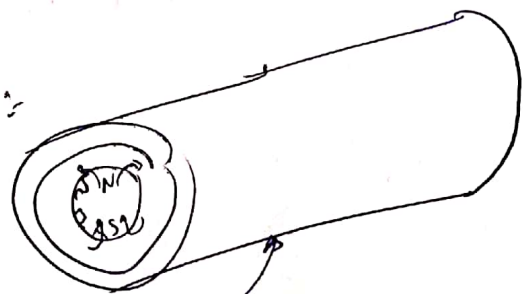
It is usually laminated to reduce Eddy current losses

* The core (Rotor) is not laminated?

Because there is no change of the flux at the rotor
(Rotates with the stator fields)

\Rightarrow No eddy current

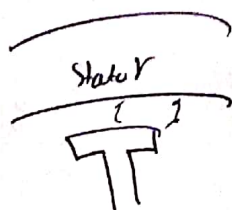
* The airgap should be as small as possible:
to reduce the reluctance of the flux path



Stator + cylindrical rotor

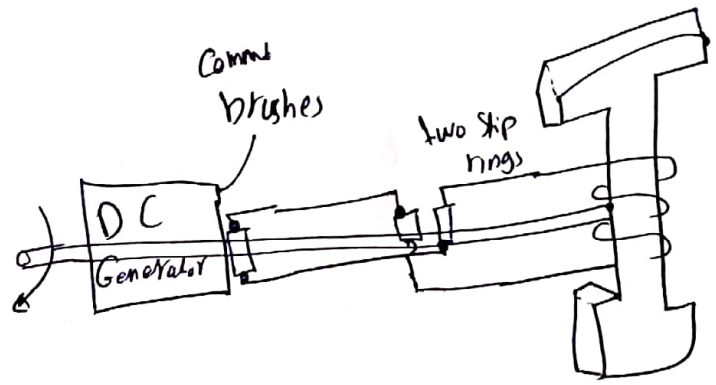
* The airgap is usually not uniform. This
will help in creating pure sine function

(only in sine)

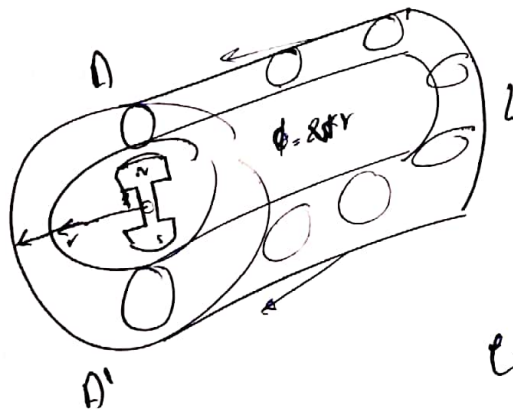


Excitation

Shaft
prime mover
(Steam or hydraulic turbine)



EMF



the field power is 2% of the total power

$$e = 4.44 N_{ph} \phi_m f$$

$$e = (\vec{v} \times \vec{B}) L$$

$$e = v \cdot B_m \cdot L \cdot \sin \omega t$$



$$L = v_m \cdot r \cdot B_m \cdot L \cdot \sin \omega t \Rightarrow e_{cal} = \underbrace{2r}_{\text{two sides}} \cdot \underbrace{L}_{N \text{ turns}} \cdot \underbrace{N_{ph}}_{\phi_m = \frac{W_e}{P}} \cdot B_m \cdot \sin \omega t$$

$$= 2rL N_p \frac{W_e}{P} \cdot B_m \cdot \sin \omega t$$

$$= \frac{2rL}{P} B_m \cdot N_{ph} \cdot W_e \cdot \sin \omega t$$

$$e_{cal} = N_{ph} \cdot 2\pi f \cdot \phi \sin \omega t \Rightarrow E_m = N_{ph} \cdot 2\pi f \phi$$

$\frac{2rL}{P} \Rightarrow$ area under pole

So $W_e \cdot A = \phi$

$$E_{rms} = \frac{E_m}{\sqrt{2}} = 4.44 N_{ph} \phi f$$

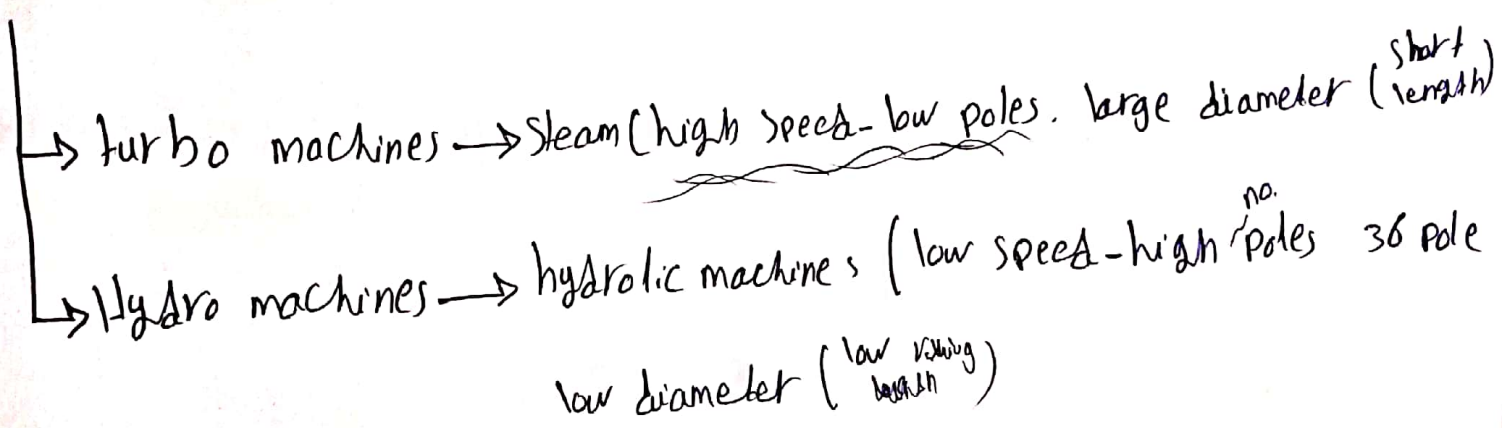
K_w

the winding factor

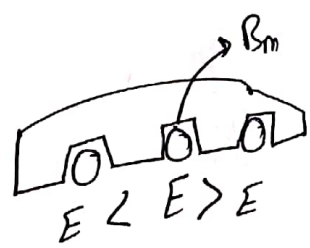
$$0.95 \leq K_w < 1$$

$$E_{rms} = 4.44 K_w N_{ph} \phi \omega$$

Synch machines can be



why K_w ??



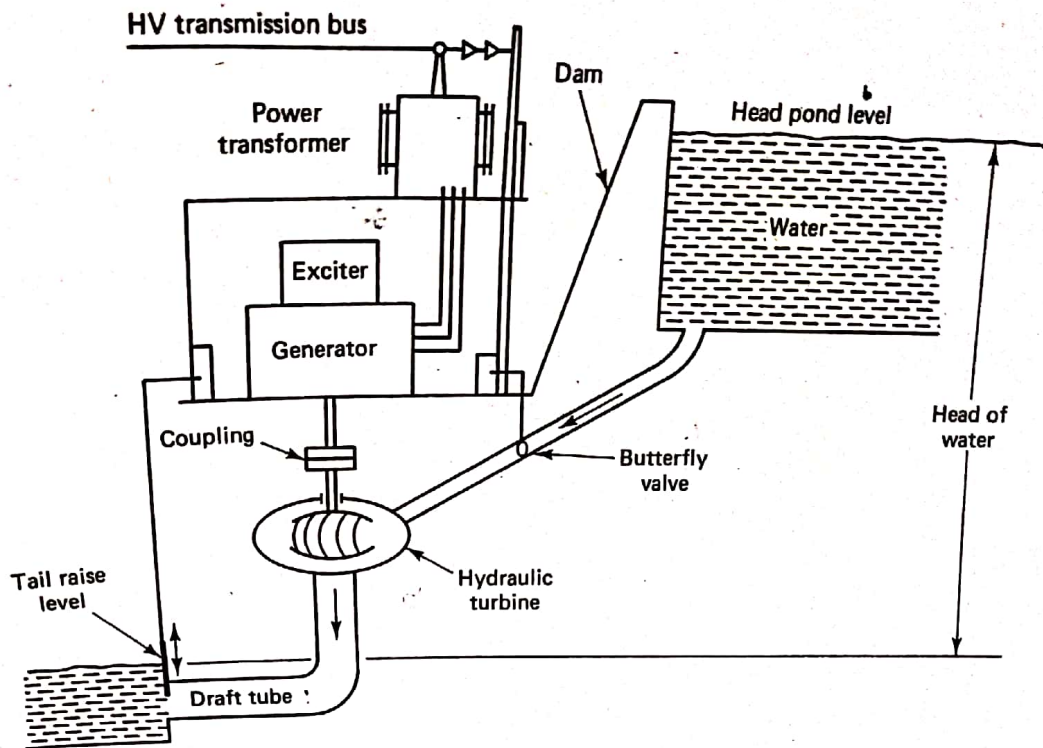


Figure 6-7 Typical hydrogenerating plant. Hydrogenerator is vertically constructed.

6-4 THREE-PHASE GENERATED VOLTAGES AND FREQUENCY

Rotor speed and frequency of the generated voltage are directly related. Let us now determine how. Consider the elementary two-pole ac generator of Fig. 6-9. To simplify things, there is only one coil shown, made up of two conductors in series, a and a' . When we have a single coil like this, we talk of a concentrated

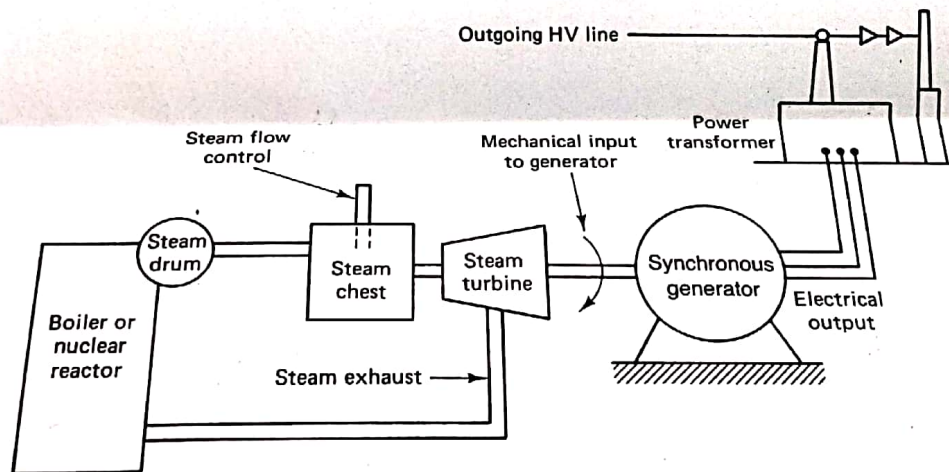


Figure 6-8 Simplified electric generating plant using horizontal construction of steam turbine generator.

Speed → control the freq of the output
 → control the real power

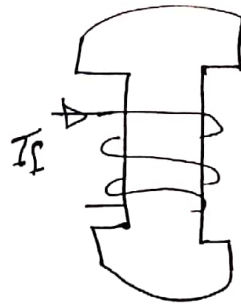
Field current ϕ → control the reactive power

Excitation system:

I_f ⇒ excitation current.

Now, to get it:

1) Isolated DC supply: (isolated DC Generator)



through slip rings and brushes → field circuit

2) Isolated AC supply + Rectifier →

through slip rings + brushes → ^{Controlled} field circuit

I_f التيار بتيار

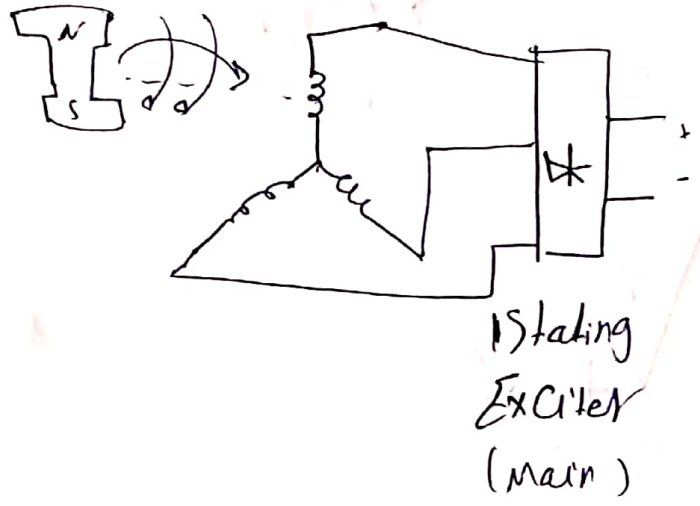
3) Brushless Excitation system.

Commutator → to convert ac to DC

Brush → تجميع التيار

Brushless excitation:

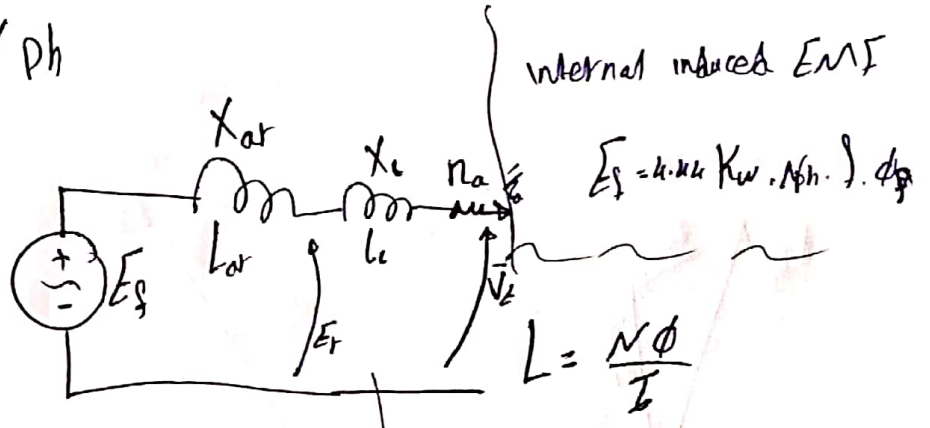
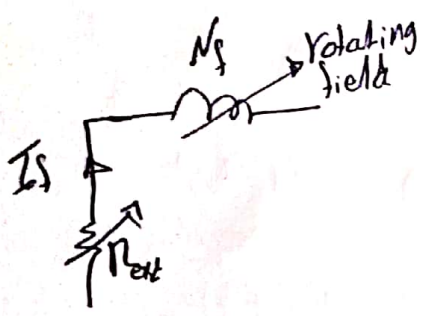
• Pilot exciter $\xrightarrow{3\phi}$ AC Generator (connected to the turbine shaft)



Rectifier

Rotating Exciter (main)

Equivalent Circuit / Ph



internal induced EMF

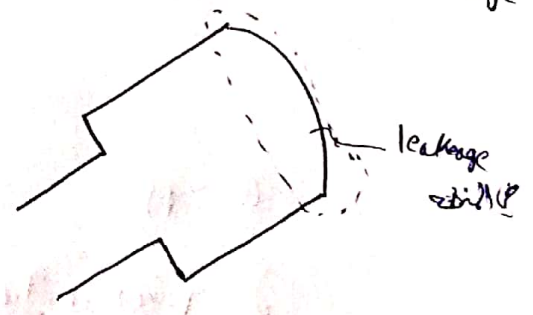
$$E_g = k_w \cdot \omega \cdot N \cdot \phi$$

$$L = \frac{N\phi}{I}$$

$X_{ar} \Rightarrow$ Armature Reaction Reactance

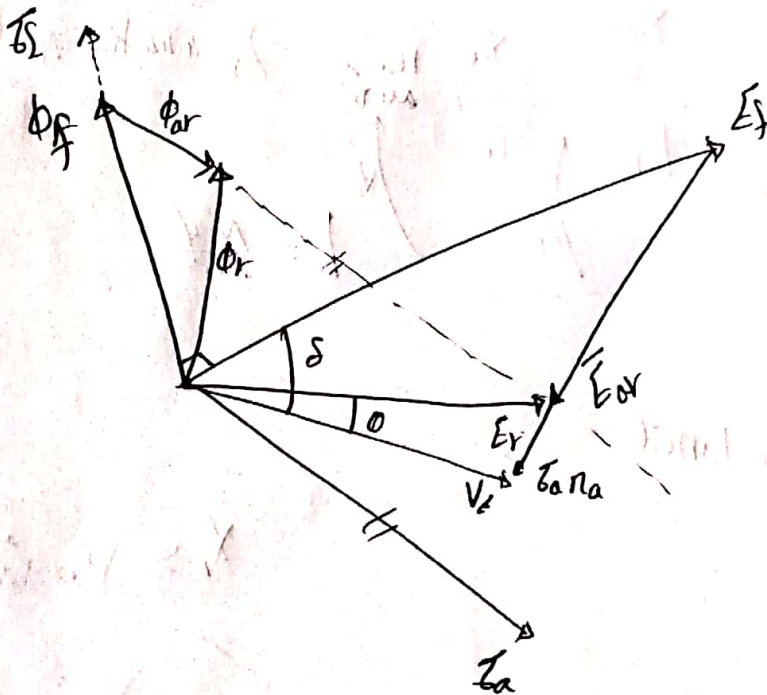
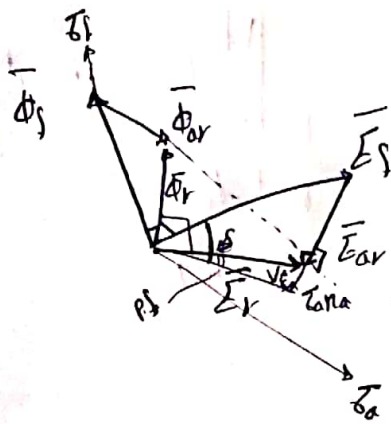
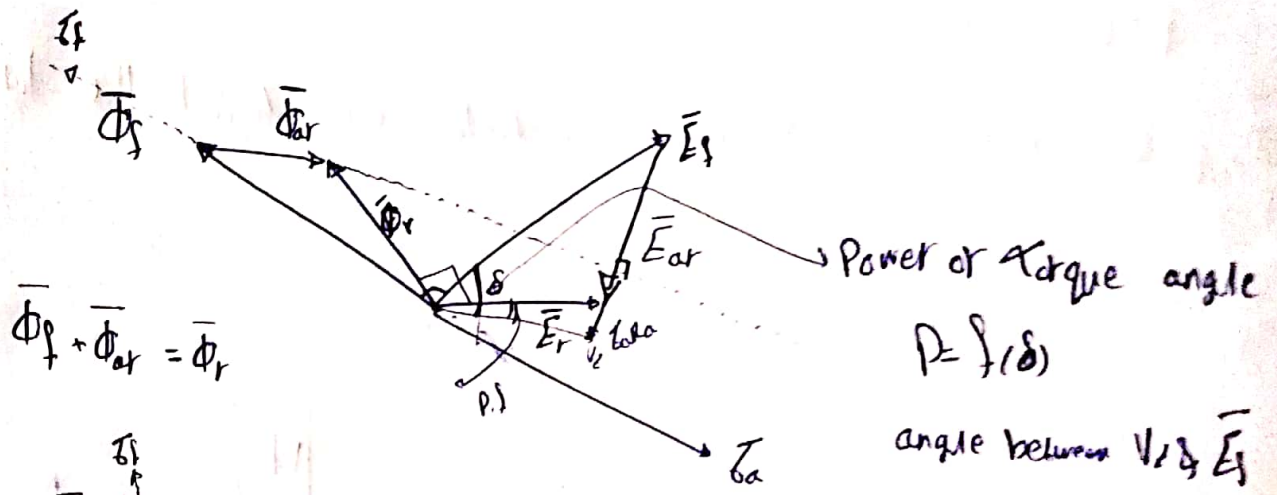
$$X_{ar} = 2\pi f \cdot L_{ar}$$

$X_l \Rightarrow$ flux leakage



$\vec{E}_r = \vec{E}_g + \vec{E}_{ar}$
 resultant (Dirgap EMF)
 main field
 Armature Reaction

$$X_s = X_{ar} + X_l$$



$\theta \Rightarrow \text{PS}$

$\delta \Rightarrow \text{power or Torque angle}$

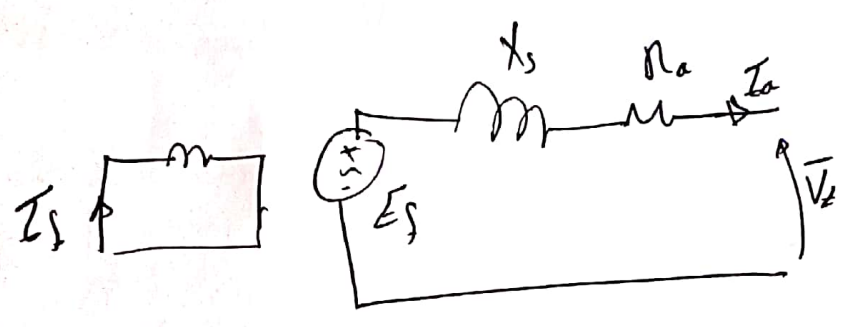
$$X_s = X_{ar} + X_l$$

↳ Synchronous reactance

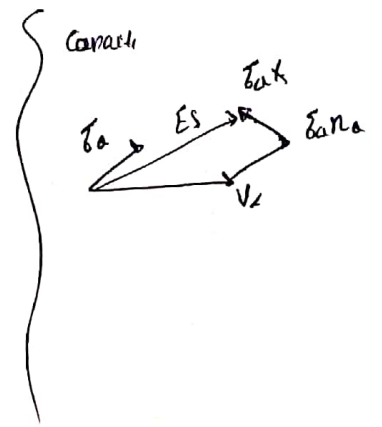
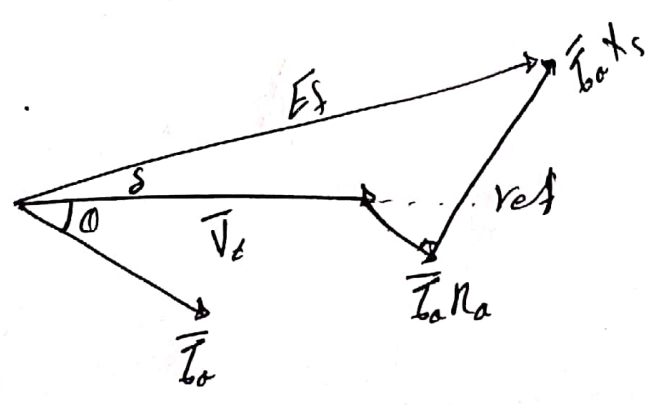
$$X_{ar} \gg X_l$$

$X_s \rightarrow$ Constant unless core saturation

$$R_a \ll X_s$$



inductive



δ — + Generators
 — - Motors

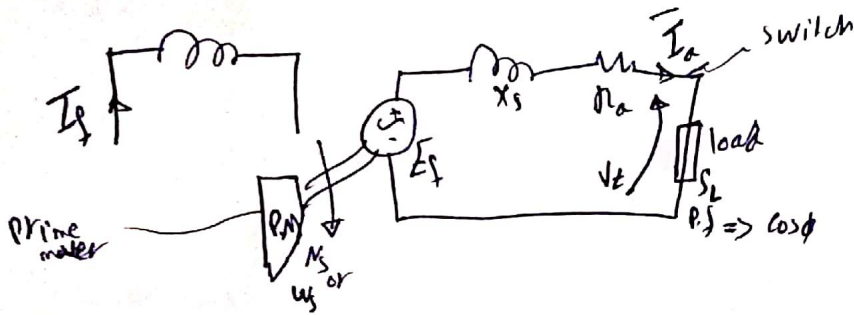
$$\begin{aligned} \vec{V}_t &= 200 \angle 30^\circ \\ \vec{E}_s &= 180 \angle 15^\circ \end{aligned}$$

leading p.f. $E_s < V_t$
 Generators

$$\delta = \theta_{V_t} - \theta_{E_s}$$

Developed power by a synch. Generator:

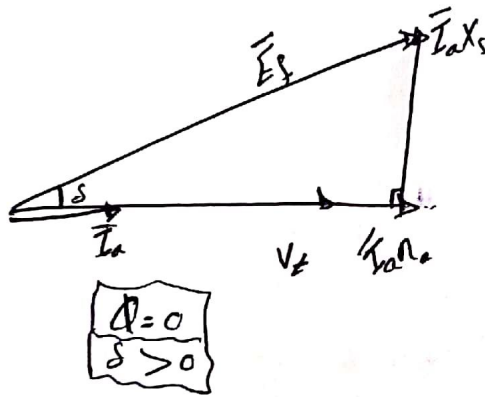
Start with phasor Diagram



a) Unity P.F load

δ angle between \bar{V}_t and \bar{E}_f

ϕ angle between \bar{V}_t and \bar{I}_a



$$\bar{E}_f = \bar{V}_t + \bar{I}_a (R_a + jX_s)$$

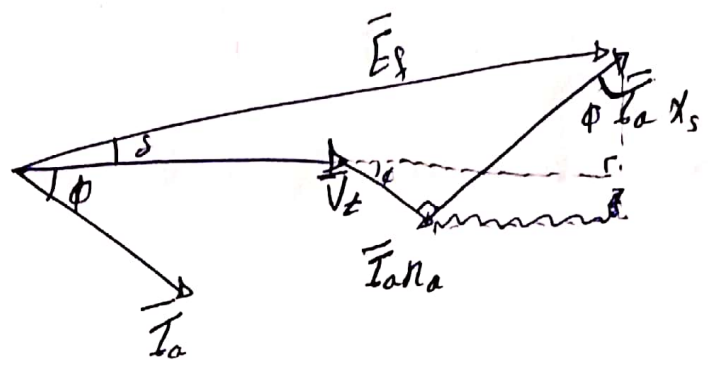
$R_a \ll X_s$

Voltage Regulation :-

$$\frac{|E_f - V_t|}{V_t} \times 100\%$$

17 M
 Synch machine Voltage is around 20KV then ~~to~~ To rise voltage to
 Transmission

h) Inductive loads



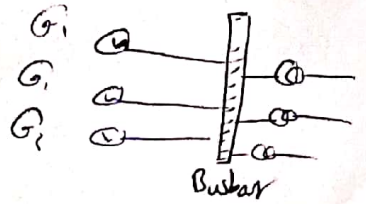
$$S = 3 V_{rms} I_{rms}$$

$P_d \Rightarrow$ developed power transferred to the load

$$P_d = 3 V_t(\text{ph}) I_a(\text{ph}) \cos \phi = \sqrt{3} V_t(\text{L}) I_a(\text{L}) \cos \phi$$

⊛ Synch. Generator are usually connected to a large power system or Network.

(Network is connected to an Infinite Busbar)

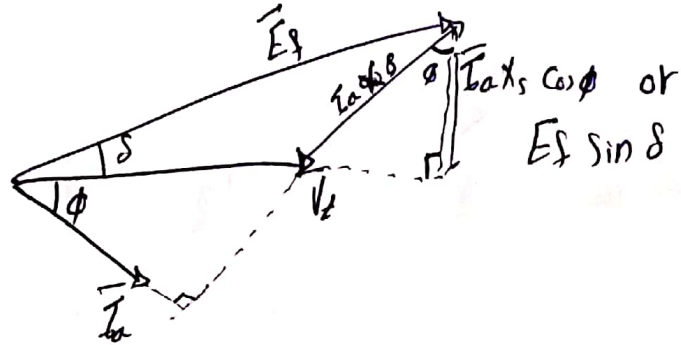


It means \Rightarrow constant voltage and frequency irrespective of load variations

Assuming $V_f = \text{const}$

$$P_d \propto I_a \cos \phi$$

With $R_a \rightarrow$ neglected



$$I_a X_s \cos \phi = E_f \sin \delta$$

$$I_a \cos \phi = \frac{E_f \sin \delta}{X_s}$$

$$P_d = 3 V_f I_a \cos \phi$$

$$P_d = \frac{3 V_f E_f}{X_s} \sin(\delta)$$

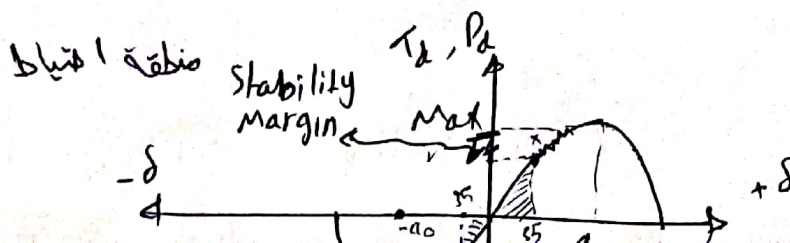
$$P_d = \frac{3 V_f E_f}{X_s} \sin(\delta)$$

δ is defined as the power angle since P_d is function of δ

developed Torq

$$T_d = \frac{P_d}{\omega_s} = \frac{P_d}{\text{const}} = \left(\frac{3 V_f E_f}{\omega_s X_s} \right) \sin(\delta)$$

δ can be referred to as the Torque angle



From the Theoretical point of view, δ is changing in the Range 17

$$0^\circ \leq \delta \leq 90^\circ \text{ Generator}$$

Practically

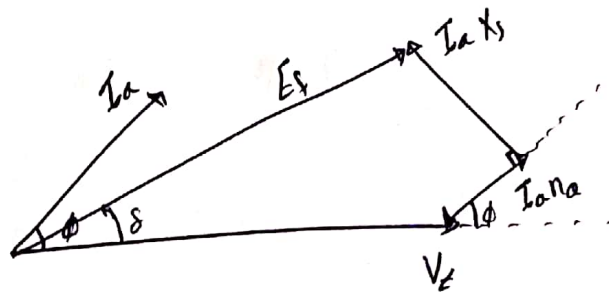
$$10^\circ \leq \delta \leq 35^\circ$$

$\delta > 90^\circ$
 اذا تعدى ال 90 درجة يصبح Motor

If $\delta = 90^\circ \rightarrow P_d = P_{max} = \frac{3 V_t E_s}{X_s}$

Stability margin \Rightarrow
 في حالة زيادة الحمل ال Generator وينقل ال
 ونفس الشيء ينطبق ال Motor

Leading P.F



δ still \oplus

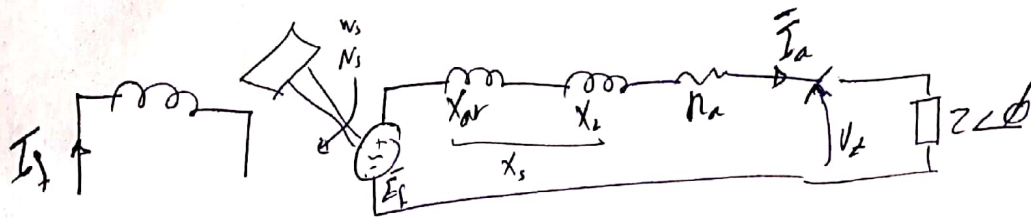
Reactive power depends on

$$I_a \sin \phi$$

$$Q = 3 V_t I_a \sin \phi$$

in Generators $\delta \rightarrow \oplus$

Synchronous Machines parameters

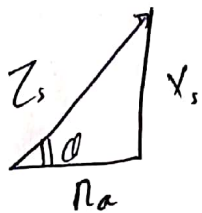


$\bar{E}_f, V_t, \bar{I}_a$ are per phase values

$R_a \rightarrow$ Armature Resistance ≈ 0.01 pu

$X_l \approx 0.1 - 0.2$ pu

$X_s \approx 1$ pu



$$Z_s = \sqrt{R_a^2 + X_s^2} \angle \theta$$

$$\theta \leq 90^\circ$$

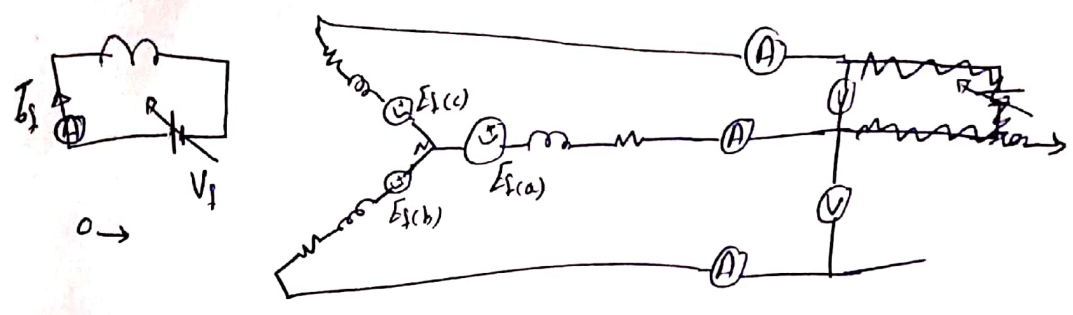
$$\theta = \tan^{-1} \frac{X_s}{R_a}$$

This is why R_a is neglected in the general analysis of S.M
for η calculation it is taken into account

ex) $P_a = \frac{3 V_t E_f \sin \delta}{X_s} \rightarrow R_a \rightarrow \infty$

$P_a (R_a \neq 0) = K + K'$ later on

S.M testing



DC test

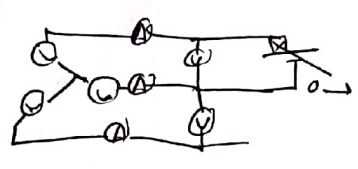
To Evaluate R_a

$N_s = 0$
 $I_f = 0$

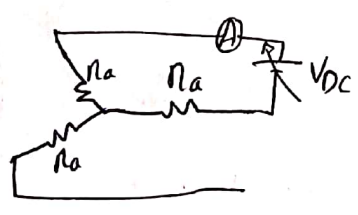
V_{DC}	V_{DC1}	V_{DC2}	V_{DC3}	V_{DC4}
I_{DC}	I_{DC1}	I_{DC2}	I_{DC3}	$I_{a(r)}$

→ I_{DC4}

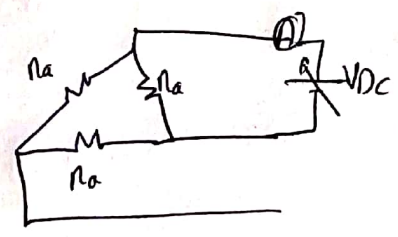
$I_{DC4} \leq I_{a(r)}$



eq



$R_a = \frac{V_{DC} (av)}{2 I_{DC} (av)}$, \downarrow - connected



$2R_a // R_a = \frac{2}{3} R_a$

$R_a = \frac{3 V_{DC} (av)}{2 I_{DC} (av)}$

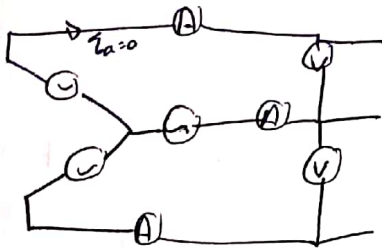
. If Δ -connected Armature

SEF \rightarrow skin effect factor

$$N_a(AC) = SEF * N_a(DC)$$

to correct for skin effect

open circuit test \rightarrow No load



1) set $I_s = 0$

$$\vec{E}_s = \vec{V}_s + \vec{I}_s \vec{Z}_s$$

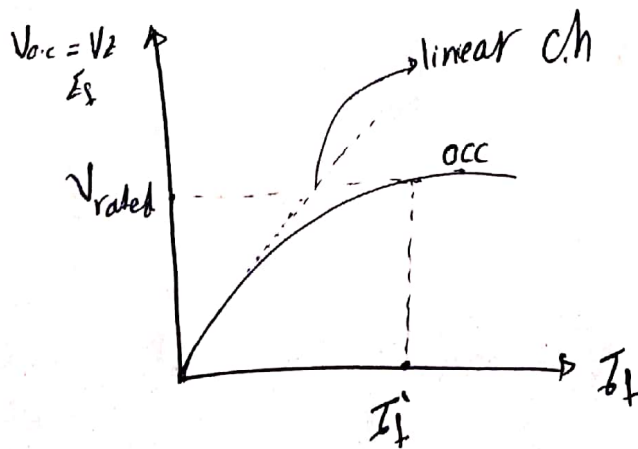
2) Run P.M at $N = N_s$

I_1	0	I_{s1}	I_{s2}	...
E_s	$V_{o.c}$	0		

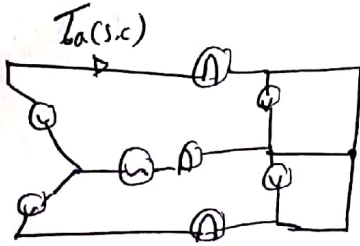
120% V_{r1}

$I_a = 0$

P.M \Rightarrow Prime mover

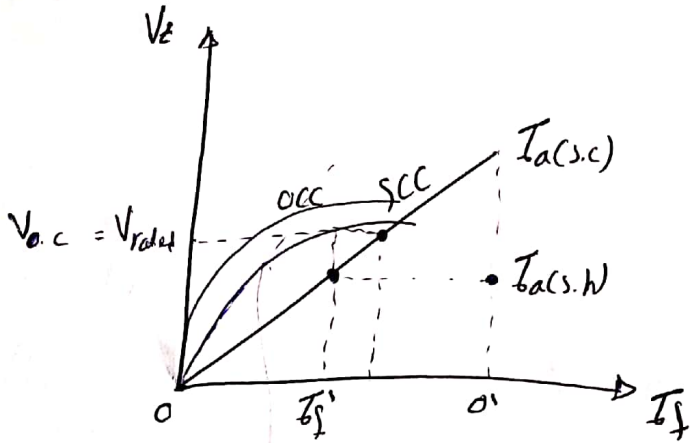


Short circuit test



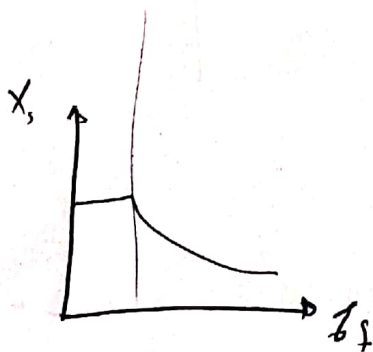
I_f at starting = 0
 Run P.M at N_s

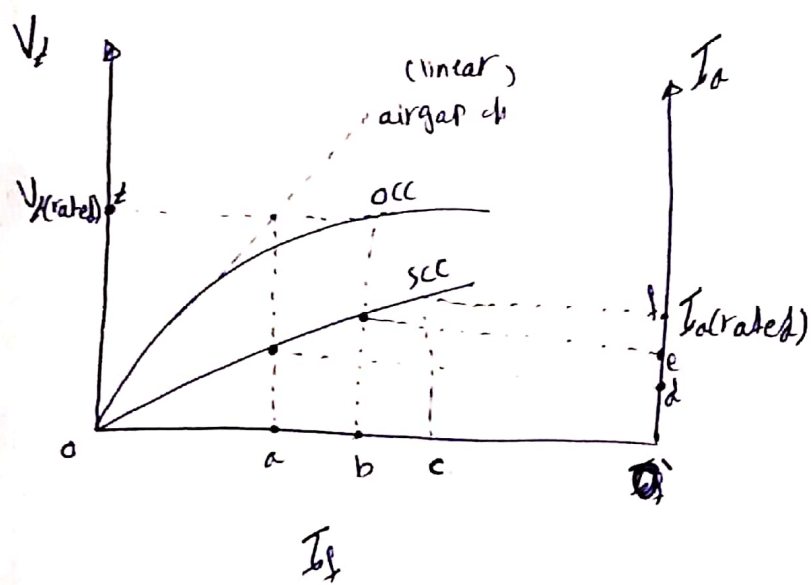
I_a (A.V)	I_f	I_f	I_f	I_f	I_f
I_{a1}	0				150% $I_{a(c.r)}$
I_{a2}	0				
I_{a3}	0				



$$Z_s = \frac{V_{(o.c)}}{I_{a(s.c)}} \approx X_s$$

$$X_s = \frac{V_{o.c}}{I_{a(s.c)}}, \quad X_s = \sqrt{Z_s^2 - R_a^2}$$





$$X_s \approx Z_s(\text{sat}) = \frac{o_e (V/\text{ph})}{o_e (A/\text{ph})}$$

$$Z_s(\text{sat}) < Z_s(\text{unsat})$$

$$X_s(\text{unsat}) = Z_s(\text{unsat}) = \frac{o_d (V/\text{ph})}{o_d (A/\text{ph})}$$

Define the SCR (short circuit ratio)

SCR = $\frac{\text{field current that gives } V_t(\text{rated}) \text{ at OCC}}{\text{field current that gives } I_a(\text{rated}) \text{ at SCC}}$

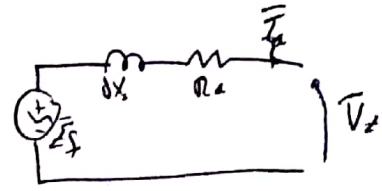
$$\text{SCR} = \frac{ob}{oc}$$

Prove $\text{SCR} = \frac{1}{X_s(\text{sat}) (pu)}$

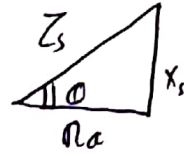
it can be proved that

$$S = \bar{V}_t \times \bar{I}_a^*$$

$$\bar{I}_t = \frac{\bar{E}_f - \bar{V}_t}{Z_s \angle \theta}$$



$$\bar{I}_t = \frac{\bar{E}_f \angle \delta - \bar{V}_t \angle 0}{Z_s \angle \theta}$$



$$Z_s = R_a + jX_s$$

$$= \sqrt{R_a^2 + X_s^2}$$

$$\theta = \tan^{-1} \left(\frac{X_s}{R_a} \right) \leq 90^\circ$$

$$= \frac{E_f}{Z_s} \angle \delta - \theta - \frac{V_t}{Z_s} \angle -\theta$$

$$= \frac{E_f}{Z_s} (\cos(\delta - \theta) + j \sin(\delta - \theta)) - \frac{V_t}{Z_s} (\cos \theta - j \sin \theta)$$

$$= \left(\frac{E_f}{Z_s} \cos(\delta - \theta) - \frac{V_t}{Z_s} \cos \theta \right) + j \left(\frac{E_f}{Z_s} \sin(\delta - \theta) + \frac{V_t}{Z_s} \sin \theta \right)$$

$$S = P + jQ = \bar{V}_t \times \bar{I}_a^*$$

$$= \left(\frac{V_t E_f}{Z_s} \cos(\delta - \theta) - \frac{V_t^2}{Z_s} \cos \theta \right) - j \left(\frac{V_t E_f}{Z_s} \sin(\delta - \theta) + \frac{V_t^2}{Z_s} \sin \theta \right)$$

$$\therefore P = \text{Real power} = \frac{V_t E_f}{Z_s} \cos(\delta - \theta) - \frac{V_t^2}{Z_s} \cos \theta$$

$$Q = \text{Reactive power} = - \frac{V_t E_f}{Z_s} \sin(\delta - \theta) - \frac{V_t^2}{Z_s} \sin \theta$$

lets assume that $\pi_a \rightarrow 0$, $Z_s = X_s$, $\theta = 90^\circ$

$$P = \frac{V_t E_f}{X_s} \cos(\delta - 90^\circ) - \frac{V_t^2}{X_s} \cos(90^\circ)$$

$$P = \frac{V_t E_f}{X_s} \sin(\delta)$$

δ Generator $\rightarrow P$
Motor $\rightarrow P$

$$Q = -\frac{V_t E_f}{X_s} \sin(\delta - \theta) - \frac{V_t^2}{X_s} \sin(90^\circ)$$

$$Q = \frac{V_t E_f}{X_s} \cos(\delta) - \frac{V_t^2}{X_s}$$

Two cases of Interests:-

when the Gen is connected to Infinite Busbar

($V_t = \text{const}$, $f = \text{const}$ respective of the load variations)

$V_t \rightarrow$ can be controlled through T_f Governor.

$$\bar{V}_t = \bar{E}_f - j\bar{I}_a X_s$$

$f \rightarrow$ can be controlled through $\overset{\text{the}}{\text{input energy}}$ Governor (to the turbine)

Case 1

Infinite Busbar + constant real power
P

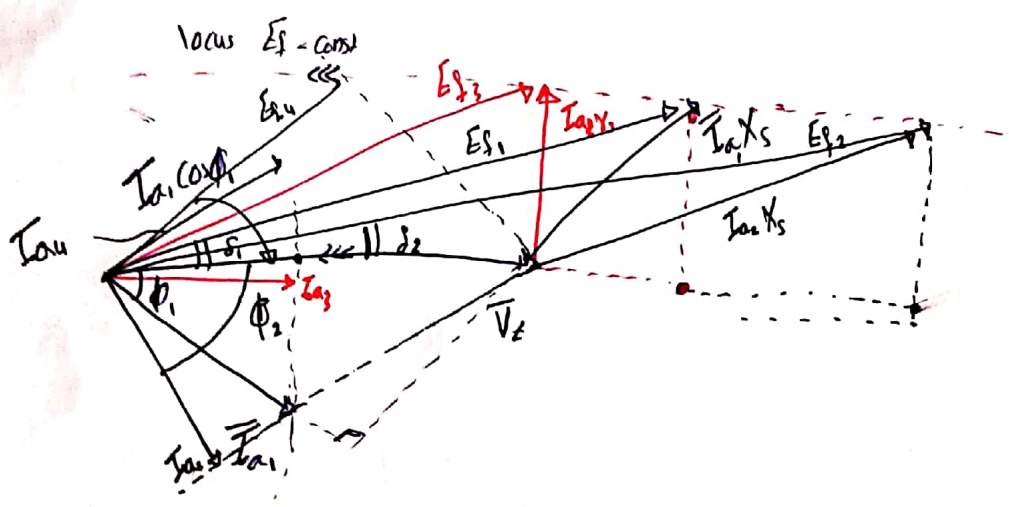
$P_m \xrightarrow{\text{Johar convert}} P$ real power

To keep $P = \text{const}$

$$P = \frac{E_f V_t}{X_s} \sin \delta$$

$$P = V_t I_a \cos \phi$$

$$P = \text{const} \rightarrow I_a \cos \phi = \text{const}$$



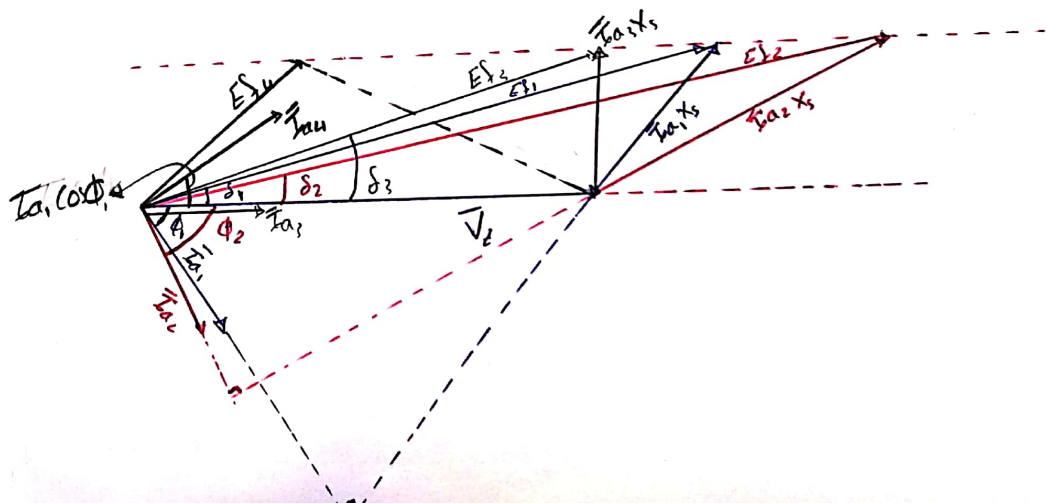
Unity p.f., lagging, leading, constant

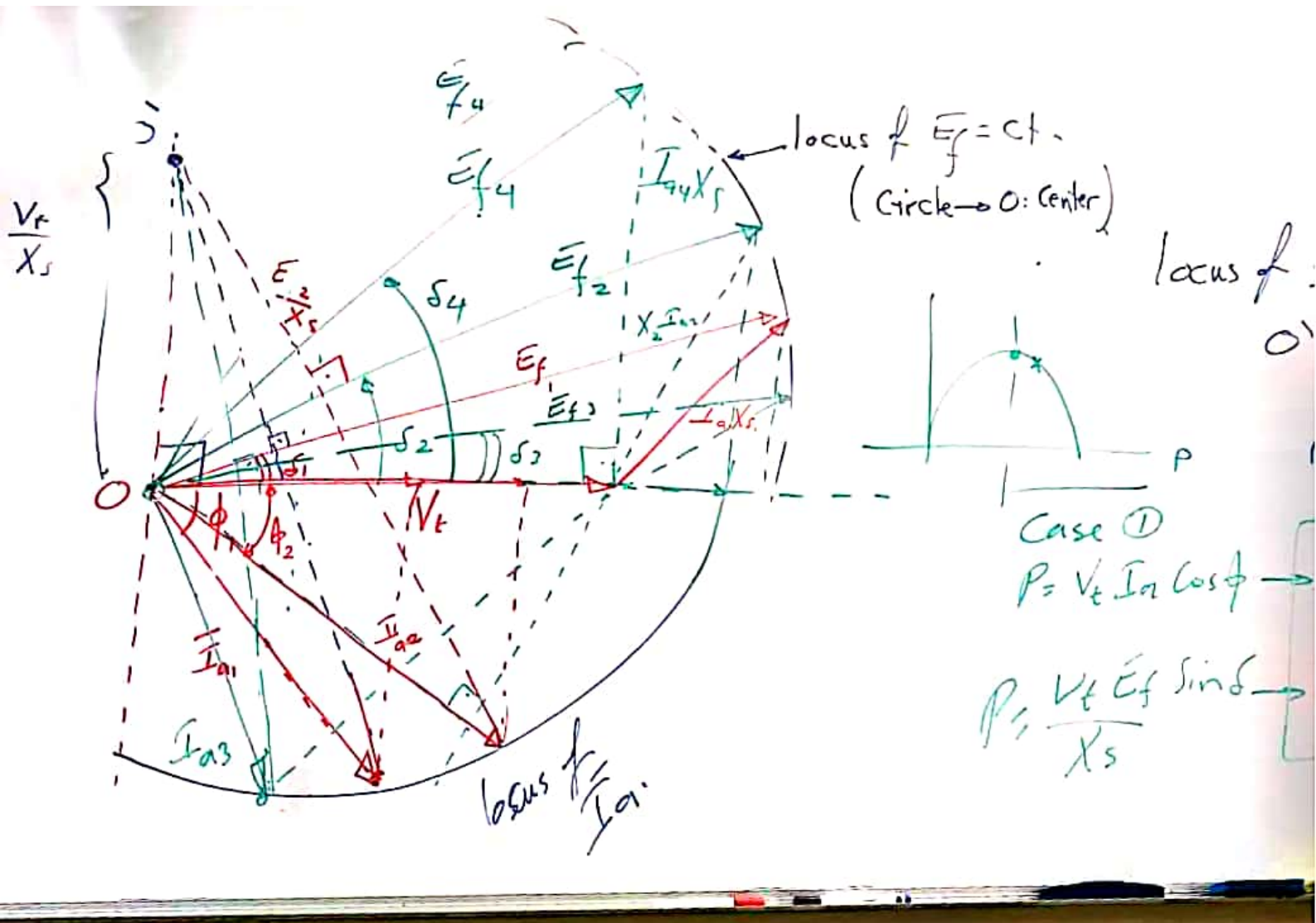
$$P = \frac{E_s - V_t \sin \delta}{x_s}$$

$$P = V_t I_a \cos \phi$$

$P \rightarrow \text{constant}$

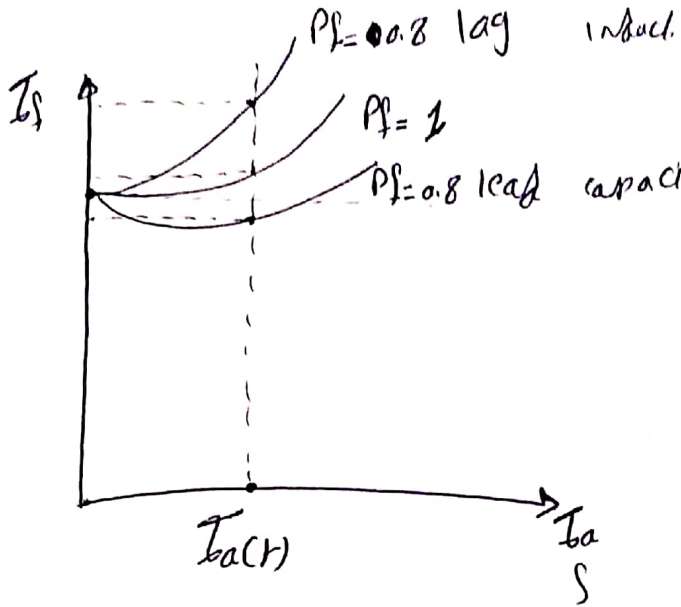
$I_a \cos \phi \rightarrow \text{constant}$





Compound Curve of S.G

S.G \Rightarrow Relationship between I_a and I_f such that $V_t = \text{const}$ and at constant P.f



change I_f
 $V_t = \text{const}$

Voltage regulation
unity P.f is $V_{t0} - V_t$
P.f

Parallel operation of Generators:

$G_1 \rightarrow G_2 \Rightarrow$ Isolated system

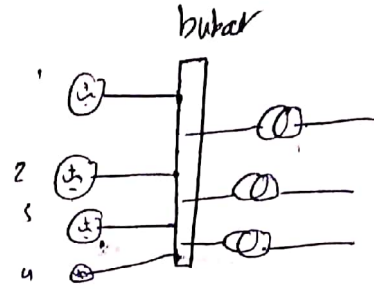
$G \rightarrow$ Infinite busbar

conditions to be satisfied for connections in parallel?

Parallel operation of synch. Machines 2

Network

$G + \infty$ Infinite Busbar



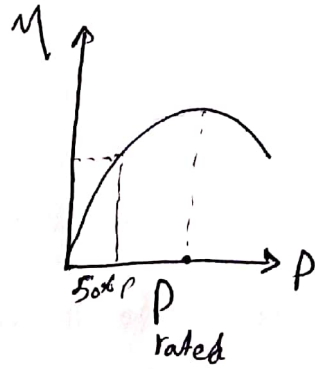
Isolated

$G_1 + G_2$

busbar (∞ Infinite $\rightarrow V = \text{fixed}, f = \text{fixed}$
irrespective of load power flow)

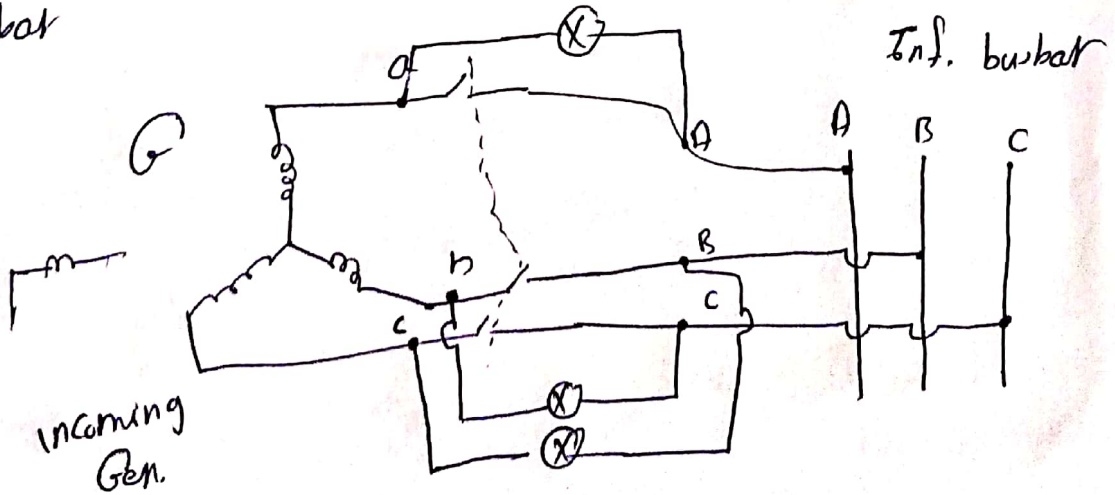
Why networks (parallel-connection Generator)?

- 1) More Reliable
- 2) More (higher) efficiency
(~~expense~~ especially when the generator is under load)
- 3) More National security



Gen. \rightarrow 30 W/s

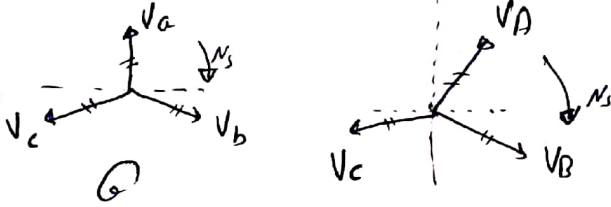
Conditions to be satisfied before connecting a new Generator to the infinite busbar



Condition:-

1) $E_f(G) = V_L(G) = V_{ab} \approx V_{AB}$, Equal Voltages

2) Same phase sequence



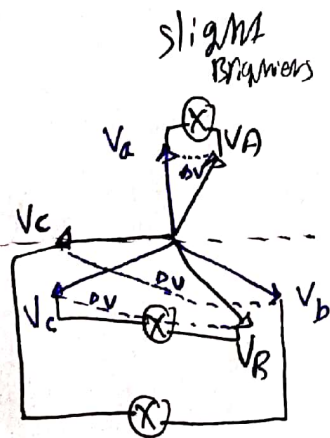
- Using small 3-ph induction motor
- Lamps
- Synchroscope

3) Freq. of the Incoming Gene. should be equal or slightly higher than that of the busbar

4) Connection at the Instant at which the two voltages are in phase



المرحلتين مع الشرط الرابع
In phase

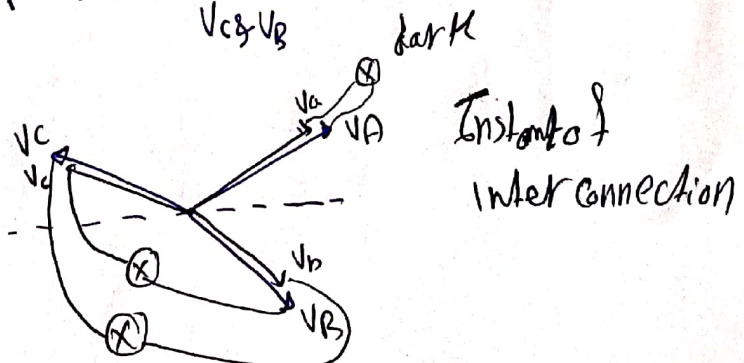


بعد فترة عندما يصبح in phase

التي بين V_{ab} و V_A كبرى

phase shift 120° V_{bc} و V_C

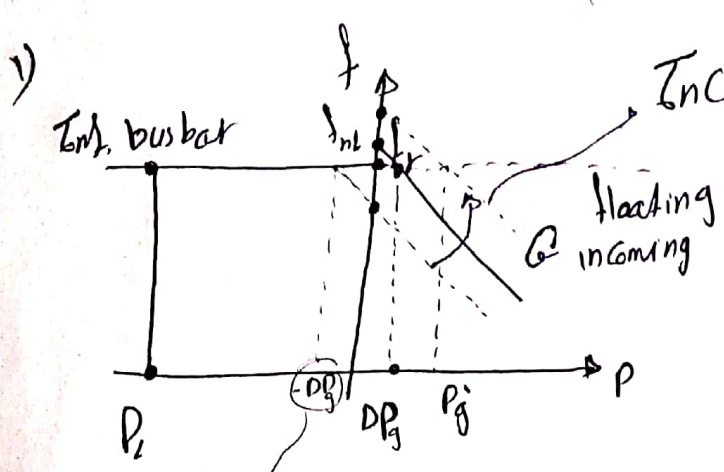
V_C و V_B



Instant of Interconnection

1) freq/Power curve
Active

2) f/Q / Reactive power curve

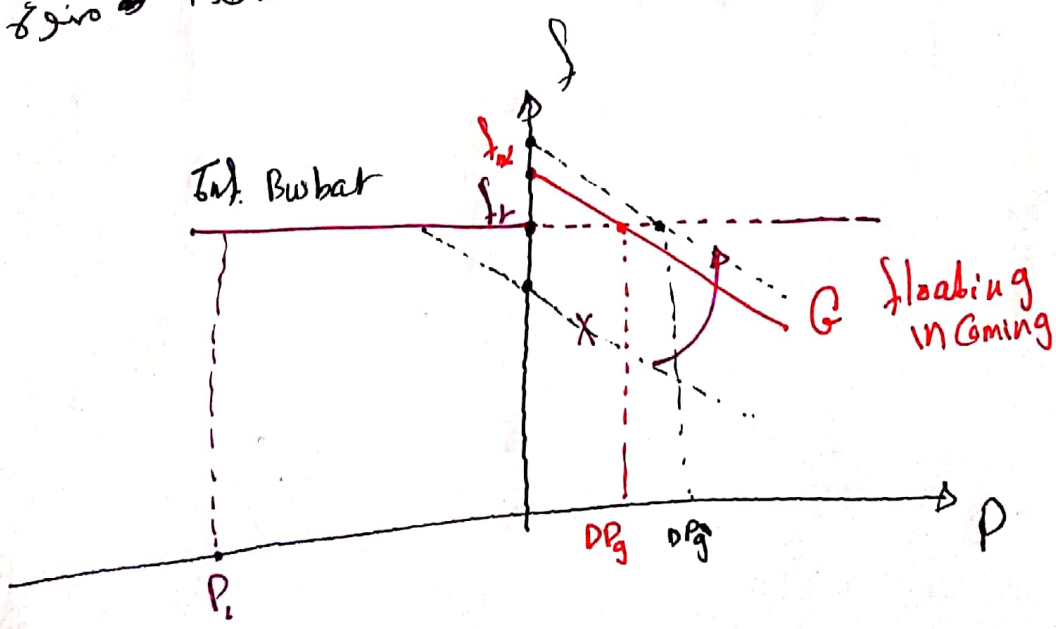


تفتح الصمام و
تزيد السرعة

Gover
set point

تغير موقع

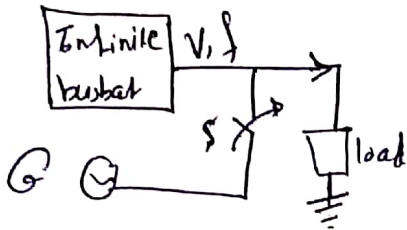
freq. ω زياد
في ω زياد



Parallel connections:

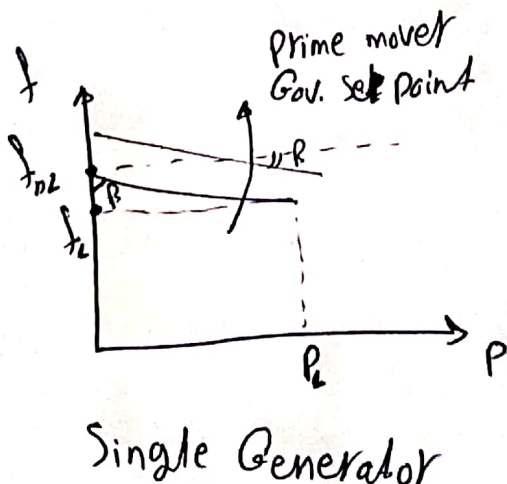
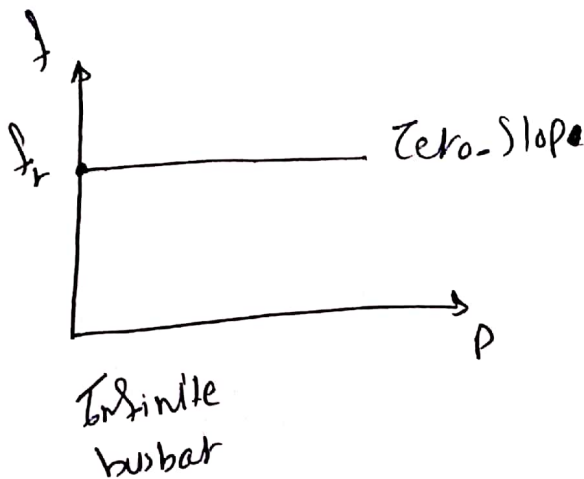
Ⓐ Case 1:

Generator to Infinite busbar



when S is closed, G is said to be floating. Raising Diagram:

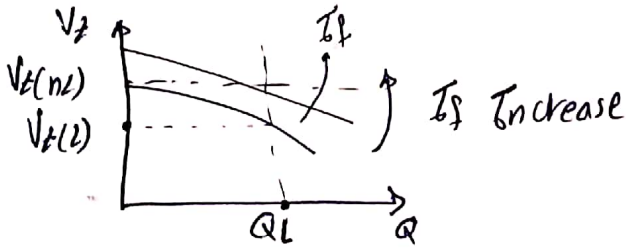
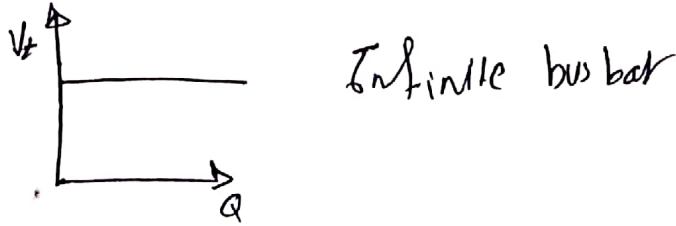
$f = \text{Function of } P$



$$P = \text{slope} * (f_{n2} - f_r) \quad , \text{slope} = \tan B$$

Single Generator

$$V_L = f(Q)$$



V_L can be controlled through I_f

After Loading,

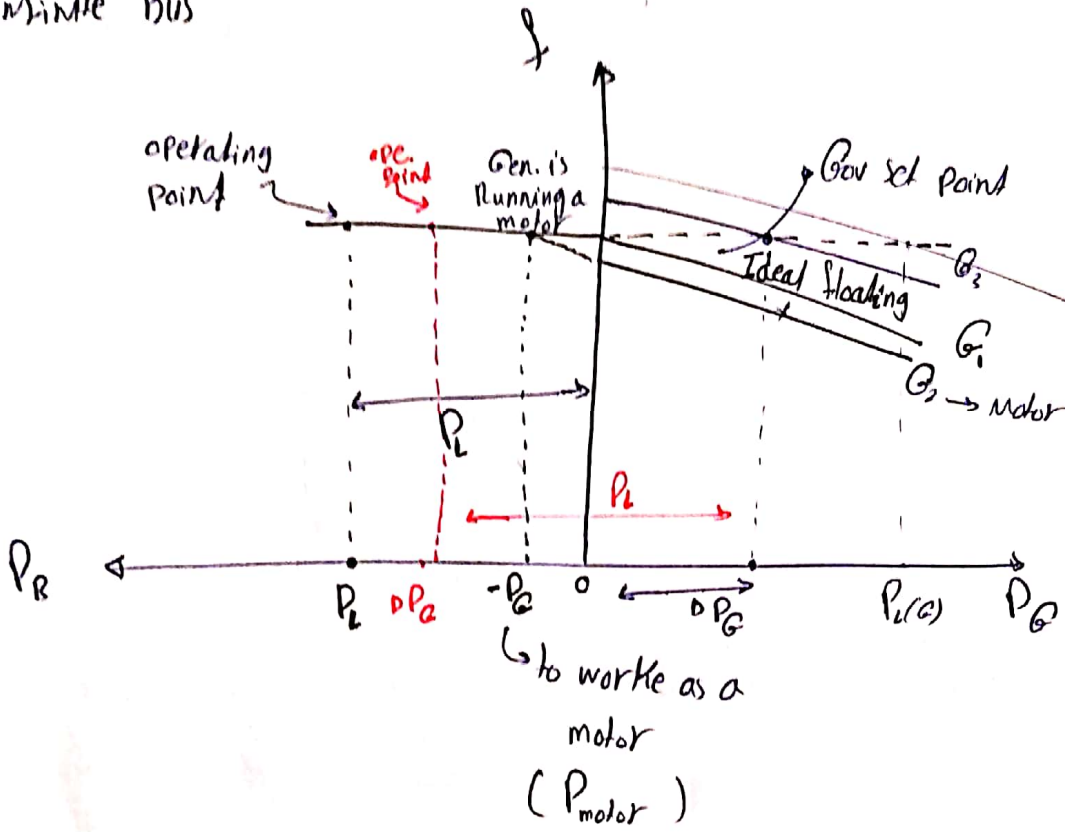
1) prime mover set point control to control the Real power the Gen. should share.

2) Generator field current set point, to control the Reactive power

*) To make sure that the Incoming Machine is not working as a motor when S is closed, the freq of the Gen. output should be slightly greater than that Infinite bus

Infinite bus

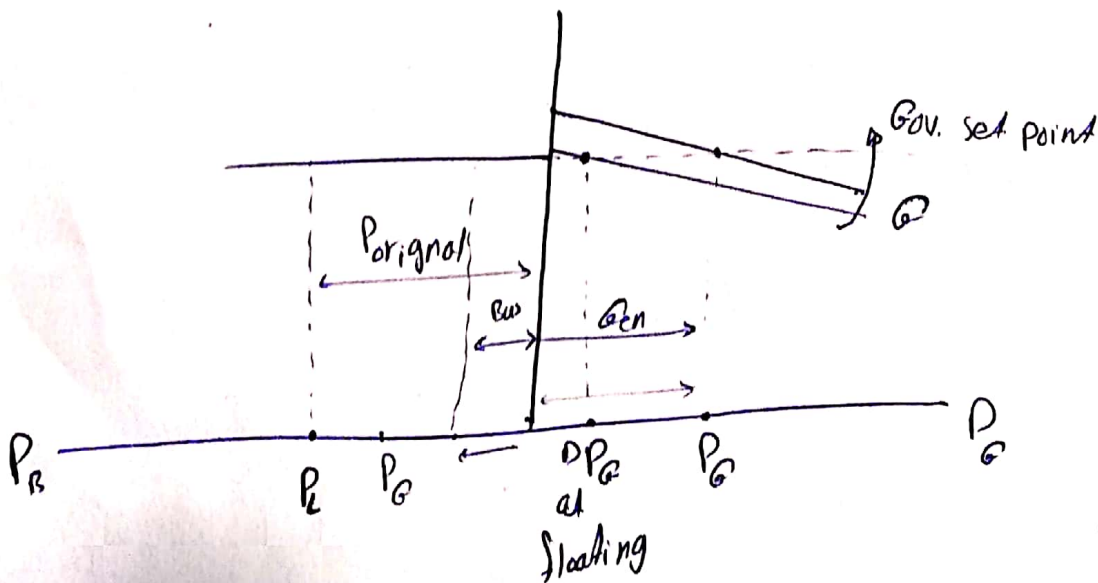
Incoming machine



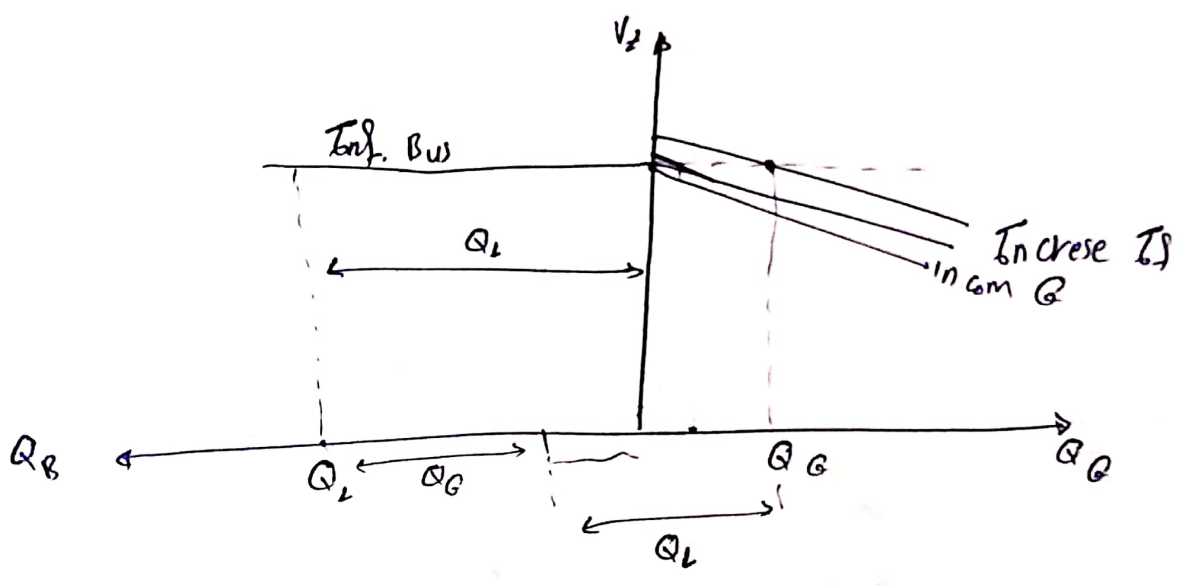
*) If this is not the case, a reverse-Power Trip facilitates with open the switch Σ to avoid Motoring Action of the Gen.

*) In case (3) (Normal case) in practical life, G will share load power by DP_G .
 (Infinite bus) power will be $P_L - DP_G$

*) If the ^{real} power to be shared by G is to be increased, the P.M. Governor set point is increased.

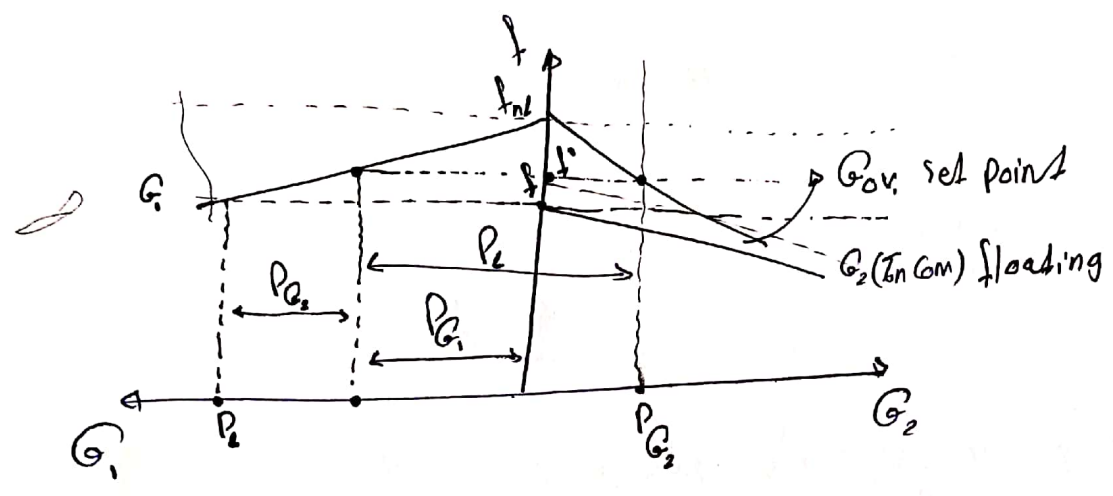


To control reactive power Q (and the power factor), the field current is to be controlled to maintain the ~~Req.~~ Req. Q (PF)



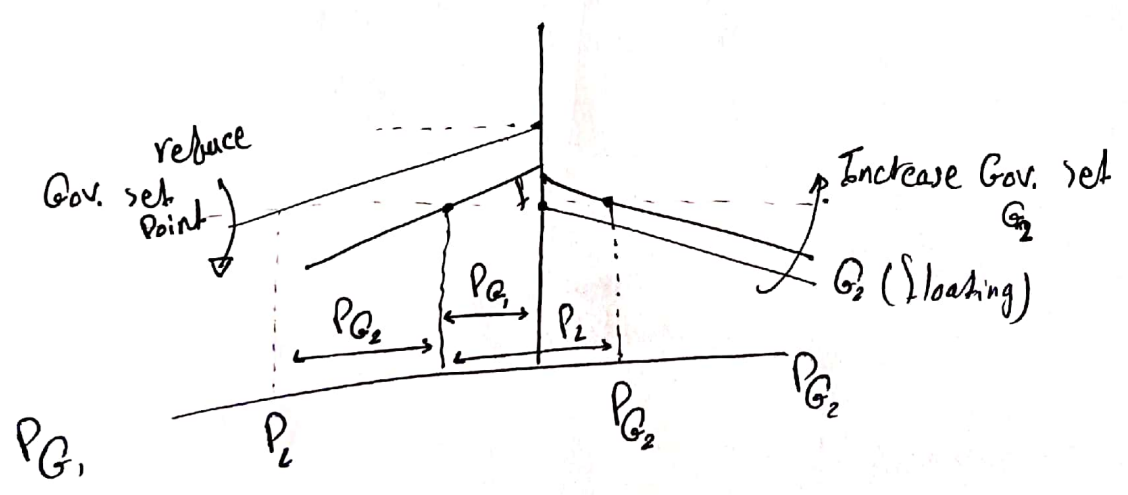
Case 2:

G_1 to G_2 in parallel V_L and $f \neq \text{const.}$



How to keep freq constant??!

- 1) when connecting G_2 , freq of the system frequency increase (after load sharing)
- 2) If the freq is to be fixed at its original value

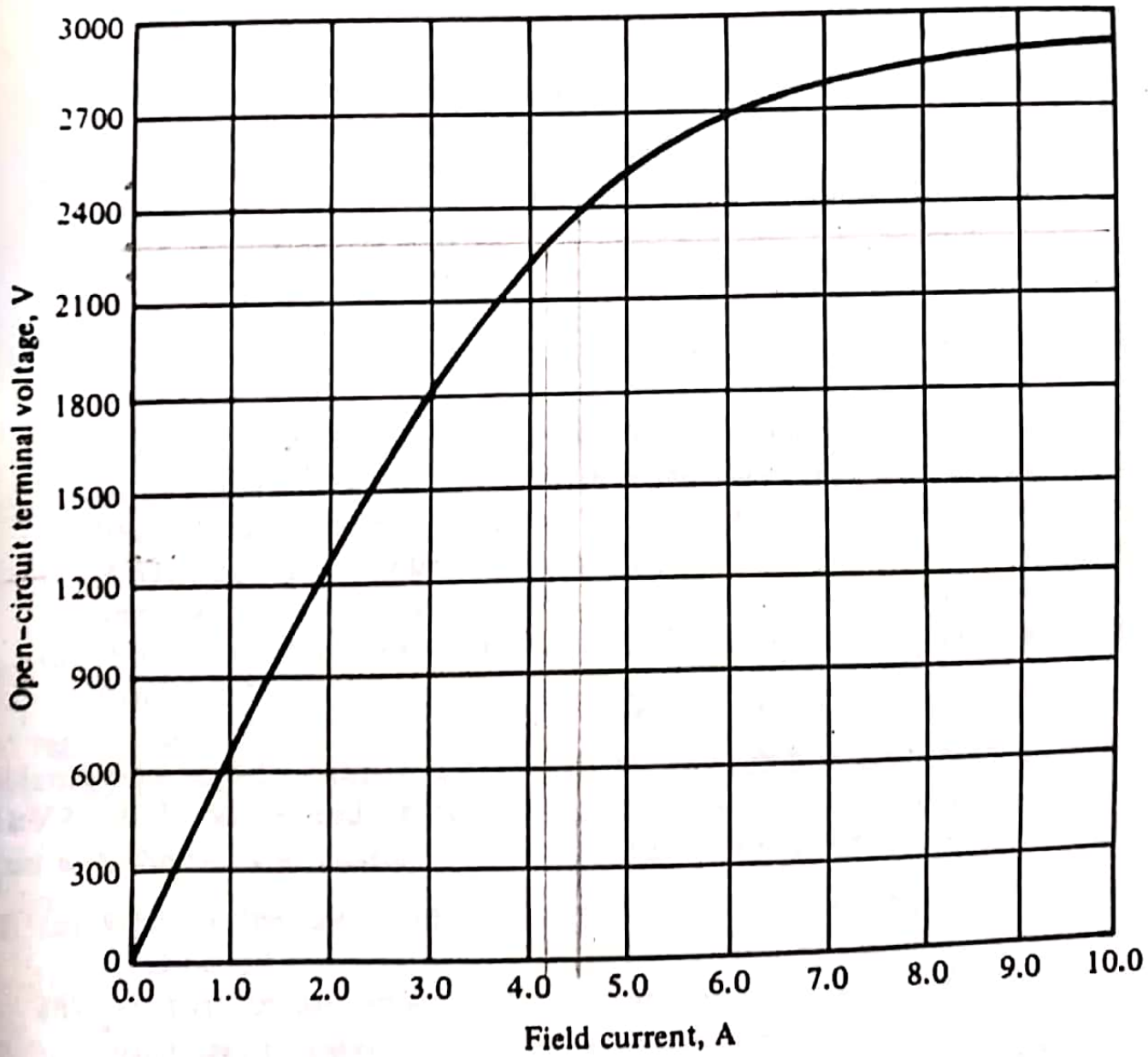


- 3) the Gov set point of G_1 is to be reduced and Gov. set point of G_2 should be increased.

PROBLEMS

- 8-1. At a location in Europe, it is necessary to supply 300 kW of 60-Hz power. The only power sources available operate at 50 Hz. It is decided to generate the power by means of a motor-generator set consisting of a synchronous motor driving a synchronous generator. How many poles should each of the two machines have in order to convert 50-Hz power to 60-Hz power?
- 8-2. A 2300-V 1000-kVA 0.8-power-factor-lagging 60-Hz two-pole Y-connected synchronous generator has a synchronous reactance of 1.1Ω and an armature resistance of 0.15Ω . At 60 Hz, its friction and windage losses are 24 kW, and its core losses are 18 kW. The field circuit has a dc voltage of 200 V, and the maximum I_f is 10 A. The resistance of the field circuit is adjustable over the range from 20 to 200 Ω . The OCC of this generator is shown in Fig. P8-1.
- (a) How much field current is required to make V_f equal to 2300 V when the generator is running at no load?

- (b) What is the internal generated voltage of this machine at rated conditions?
- (c) How much field current is required to make V_T equal to 2300 V when the generator is running at rated conditions?
- (d) How much power and torque must the generator's prime mover be capable of supplying?
- (e) Construct a capability curve for this generator.



Special assumption

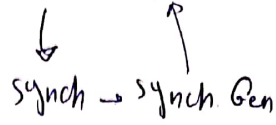
FIGURE P8-1
The open-circuit characteristic for the generator in Prob. 8-2.

(c)

3000 kW at 60 Hz

Available freq is 50 Hz

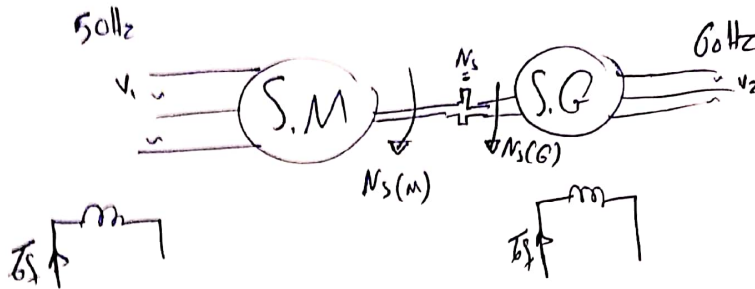
Power to be Gen by Motor-Generator set



$P_G, P_m = ??$

How many poles should be convert from 50 to 60 Hz?

Conventional M-G set



$$N_s(m) = N_s(G)$$

$$N_{s(m)} = \frac{60 f_m}{P_m}$$

$$N_{s(G)} = \frac{60 f}{P_G} = \frac{60 \times 60}{P_G}$$

P_m	$N_{s(m)}$
1	3000
2	1500
3	1000
4	750
5	600
6	500
...	...

P_G	$N_{s(G)}$
2	3600
2	1800
3	1200
4	900
5	720
6	600
...	...

$P_G = 6 \Rightarrow 12$ Poles

$P_m = 5 \Rightarrow 10$ Poles

Problem 2

A 2300V, 1000KVA, 0.8 pf lag, 60Hz, 2-pole

y-connected synch. Generator



Nameplate Data	
Nominal Value	Rated Value

$V_L = 2300V / \text{line}$

$S_r = 1000KVA \Rightarrow \text{output}$

Prime mover $S = S_r + \text{losses}$

$pf = 0.8 \rightarrow$

حساب التيار \rightarrow rated current

* $w_s = \frac{2\pi N_s}{60}$

$I_{act} = \frac{S_r}{\sqrt{3} V_L} = \frac{1000K}{\sqrt{3} \times 2300} = 251 A$

$I_{act} = I_{act} = 251A$

$V_r \approx S_r \Rightarrow \Phi_r (V_r = 4.44 N_s \Phi_r)$

same example at 60Hz, $P_{mech} = 24KW$, $P_{core} = 18KW$

field $V = 200V$, $I_m = 10A$, $R_f = 20 - 200 \Omega$

OCC - given

$R_a = 0.15 \Omega / \text{ph}$, $r_s = 1.1 \Omega / \text{ph}$

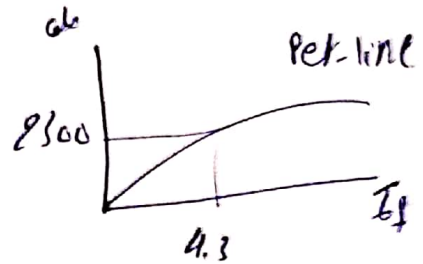
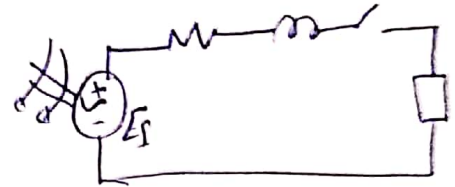
a) $I_f = ?$ such that $V_L = 2300$ at no-load ($I_a = 0$)

at no load $I_a = 0$

So $V_L = E_f \Rightarrow E_f = 2300 \text{ V/line}$

From the curve

$I_f = 4.3 \text{ A}$



b) internal generated voltage at rated loading conditions

$E_{f(1)\text{ph}} = V_{L(1)\text{ph}} + I_{a(1)\text{ph}} Z_s \rightarrow \text{always per line}$

$V_{L(1)\text{ph}} = \frac{2300}{\sqrt{3}} \angle 0, I_{a(1)\text{ph}} = 251 \angle -\cos^{-1} 0.8$

$I_{a(1)\text{line}} = \frac{S_{(3\text{ph})}}{\sqrt{3} V_{L(1)\text{L}}} = \frac{10^6}{\sqrt{3} V_{L(1)\text{L}}} = 251 \text{ A}$

$S_L = \sqrt{3} V_L I_L$

$E_{f(1)\text{ph}} = 1536.6 \angle 7.41 \text{ V}_{\text{ph}}$

$Z_s = \sqrt{0.15^2 + 1.1^2} \angle \tan^{-1} \frac{1.1}{0.15}$

$E = \sqrt{3} E_f \quad 1536 - \frac{2300}{\sqrt{3}}$

$E_f = 1536.6 \angle 7.47 \text{ } \circ \delta$

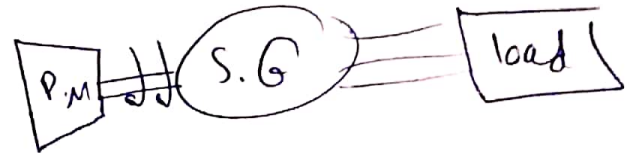
3) Find P_{PM}

$$P_{PM} = 24 \text{ kW} + 18 \text{ kW} + P_{cu} + P_{load}$$

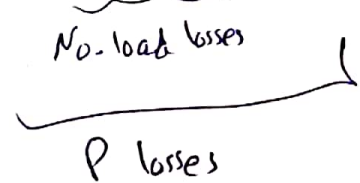
$$P_{cu} = 3 I_{a(cph)}^2 R_a = 28.35 \text{ kW}$$

$$P_{PM} = 870.35 \text{ kW}$$

$$4) \eta = \frac{P_{out}}{P_{in}} = \frac{800 \text{ kW}}{870.35 \text{ kW}}$$



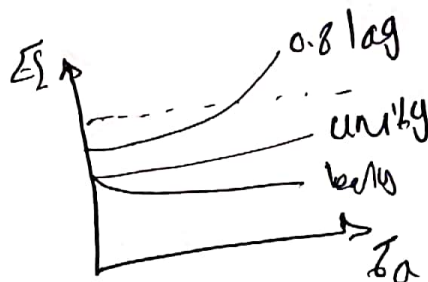
$$P_{P.M.} = P_{mech} + P_{core} + P_{cu} + P_{load}$$



$$Q = 600 \text{ kVAR}$$

S.P.F
100% P.F
 $P_L = 800 \text{ kW}$

5) capability curve



6) Torque by the prime mover $\Rightarrow T_g = \frac{P_{P.M.}}{\omega_m} = \frac{P_{P.M.}}{\omega_s}$

$$\omega_s = \frac{2\pi N_s}{60}, N_s = \frac{60f}{P} = 3600 \text{ (poles)}$$

$$T_g = 2308$$

7) the voltage regulation at rated conditions

$$V.R. = \frac{V_L(\text{line or phase})_{no-load} - V_L(\text{load})}{V_L(\text{load})}$$

V.R. i can use ~~the~~ line or phase

* Leading PF, rated condition

$V_{ph} + Z_{0/3} (Z_L)$

$$E_f = \frac{2300 \angle 0}{\sqrt{3}} + 251 \angle 82.2$$

leading P.F

$$Z_s \angle 82.2$$

$$E_f = 1217.43 \angle 11.5 \text{ New } S$$

$$1217.43 \angle \frac{2300}{\sqrt{3}}$$

$$V_{Reg} = \frac{2108 - 2300}{2300} = -8.3\%$$

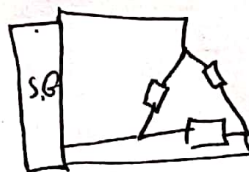
Unity P.F

$$E_f = \frac{2500 \angle 0}{\sqrt{3}} + 251 \angle 0 + Z_s \angle 82.2$$

ex) $I_f = 4.5 A \xrightarrow{\text{from curve}} E_f = 2400 V$ (the curve always use the line)

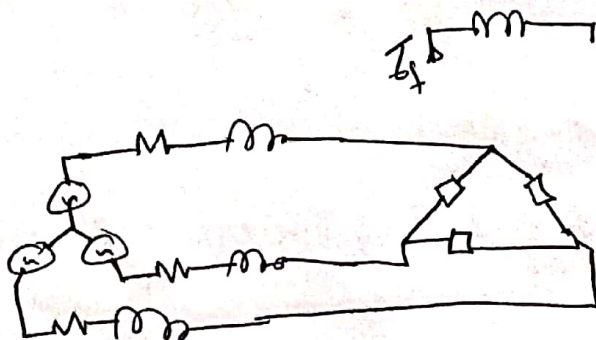
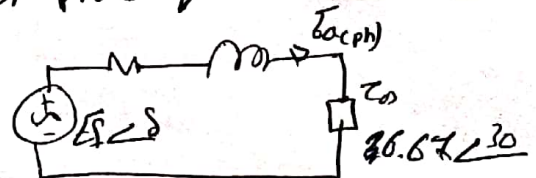
$$\bar{V}_L = \bar{V}_L \angle 0 = ??$$

Per 2s, 6

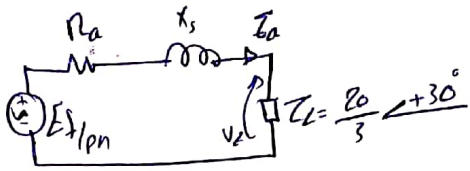


$$Z_D = Z_0 \angle 30^\circ \Omega$$

Per phase eq



$$Z_D = Z_0/3 \text{ (balanced)}$$



no V_s fixed
V ← D

ES curve always
Per-line

$I_s = 4.5 \text{ A}$ from curve $\rightarrow E_f = 2100 \text{ V}$

$$V_t = E_f - I_a Z_s$$

$$V_t \angle 0 = E_f \angle \delta - 187.377 \angle \delta - 36.8^\circ * Z_s$$

~~V_t = 1356.773~~

$$V_t + j0 = 1356.773 \cos \delta + j 1356.773 \sin \delta - \frac{(187.377 \angle \delta - 36.8^\circ * 1.11 \angle 82.2^\circ)}{20 \angle 1.88 \angle \delta + 45.4^\circ}$$

Per-phase

$$I_a = \frac{E_f / \sqrt{3}}{Z_s + Z_L}$$

$$Z_s = \sqrt{R_a^2 + X_s^2} \angle \tan^{-1} \frac{X_s}{R_a} = 1.11 \angle 82.2^\circ \Omega / \text{ph}$$

$$V_t + j0 = [1356.773 \cos \delta + 20 \angle 1.88 \cos(\delta + 45.4^\circ)] + j [1356.773 \sin \delta + 20 \angle 1.88 \sin(\delta + 45.4^\circ)] \quad I_a = \frac{1356.773 \angle \delta}{1.11 \angle 82.2^\circ + \frac{20 \angle 30^\circ}{3}}$$

$$I_a = 187.377 \angle \delta - 36.8^\circ \text{ A}$$

~~$$j0 = 20 \angle 1.88 (\delta + 45.4^\circ)$$~~

$$j0 = j [1356.773 \sin \delta + 20 \angle 1.88 \sin(\delta + 45.4^\circ)]$$

$$\sin \delta \cos 45.4^\circ - \cos \delta \sin 45.4^\circ$$

$$0 = 1356.773 \sin \delta + 20 \angle 1.88 (\sin \delta \cos 45.4^\circ - \cos \delta \sin 45.4^\circ)$$

Divided by $\cos \delta$

$$\cos 45.4^\circ = 0.7$$

$$\sin 45.4^\circ = 0.71$$

$$0 = 1356.773 \tan \delta + 145.516 \tan \delta - 147.594$$

$$\tan \delta = 0.524$$

$$\delta = 5.4^\circ$$

Rat part
 $V_L = 1 \sqrt{3} 401 \text{ V/ph}$

$V_L = 2667.6 \text{ V/line}$

13.8 KV, 10 MVA, 0.8 p.f lag, 60 Hz, 2-pole, Y-connected, st. turbine

$X_s = 18 \Omega/\text{ph}$ $R_a = 2 \Omega/\text{ph}$

G → connected to Busbar (V, $V_L = \text{constant}$)

1) $E_f = ???$
 2) δ } rated condition

3) $E_f = \text{const}$, $P_{\text{max}} = ??$, P_{reserve} at full load.
 $\alpha = ??$

$I_a(\text{cr}) = \frac{S_r}{\sqrt{3} V_L(\text{cr})}$
 $= \frac{10 \times 10^6}{\sqrt{3} \times 13.8 \times 10^3} = 418.37 \angle -36.87^\circ$ (lag)

$E_f = \frac{13800}{\sqrt{3}} \angle 0^\circ + 418.37 \angle -36.87^\circ \times 18.1107 \angle 83.66^\circ$

$E_f = 13863 \angle 25.53^\circ \text{ V/ph}$

$E_f = 24011.87 \text{ V/line}$

$\delta = +25.53^\circ$

$E_{f \text{ line}} = \sqrt{3} E_{f \text{ ph}}$

at any load
 $I_a = \frac{S}{\sqrt{3} V_L(\text{cr})}$ (infinite bus)

$I_a = 170 \angle \alpha$ (lead, lag, or unity)

$Z_s = \sqrt{2^2 + 18^2} \angle \tan^{-1} \left(\frac{18}{2} \right) \text{ } \Omega/\text{ph}$
 $Z = |Z_s| \angle 0^\circ$

$$P = \frac{3V_t E_f}{X_s} \sin \delta \longrightarrow P_a = 0 \Rightarrow P_{\max} \Rightarrow \text{when } \delta = 90$$

$$P = \frac{3V_t E_f}{Z_s} \cos(\delta - \theta) - \frac{3V_t^2}{Z_s} \cos \theta \longrightarrow P_a \neq 0$$

P_{\max} if $P_a \neq 0$

$$\frac{dP}{d\delta} = 0 = -\frac{3V_t E_f}{X_s} \sin(\delta - \theta)$$

$$\sin(\theta - \delta) = 0$$

$$\therefore \theta - \delta = 83.66^\circ$$

$$P_{\max} = \frac{3V_t E_f}{Z_s} \cos(83.66 - 83.66) - \frac{3V_t^2}{Z_s} \cos(83.66) = 17.6717 \text{ MW}$$

$$P_{\max} \text{ at } P_a = 0 \Rightarrow P_{\max} = 18.9 \text{ MW}$$

$P_a \rightarrow 0$

$$P_{\max} = 18.9 \text{ M}$$

$$P_{\text{reserve}} = 18.9 - \frac{10(0.8)}{\text{step}} = 10.9 \text{ MW} \rightarrow \text{Power rated}$$

$P_a \neq 0$

$$P_{\text{reserve}} = 9.67 \text{ MW}$$

Synchronous Motor's SM non self starting motor

*Reasons for each current cycle from the supply the rotor vibrates with zero average torque, and since $E_f = 0 \rightarrow$ large armature current $\approx I_{sc}$
 $V_t - E_f \approx V_t$

which can destroy the motor if runs for a relatively long period of time.

*SM can be controlled to run at any pf (unity, leading or lagging).

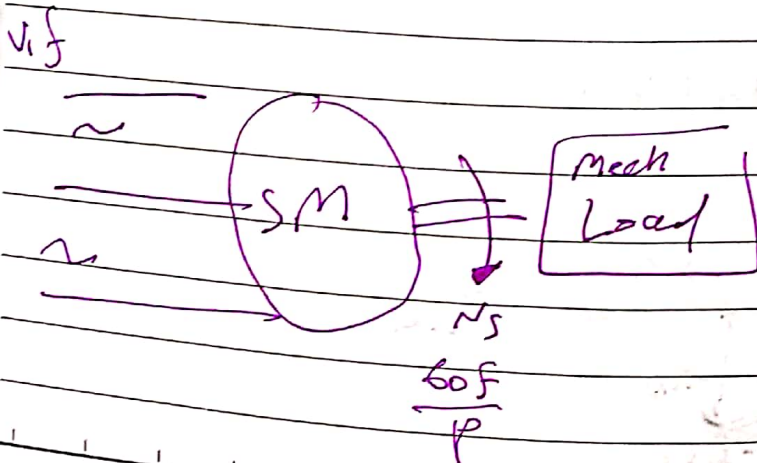
This can be done by field control. (pf correction).

*SM is expensive motor (2-3) same size induction motor.

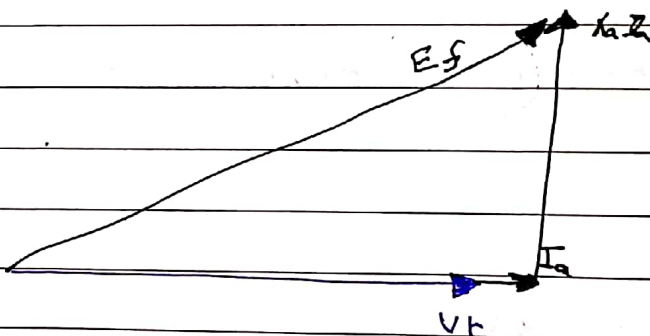
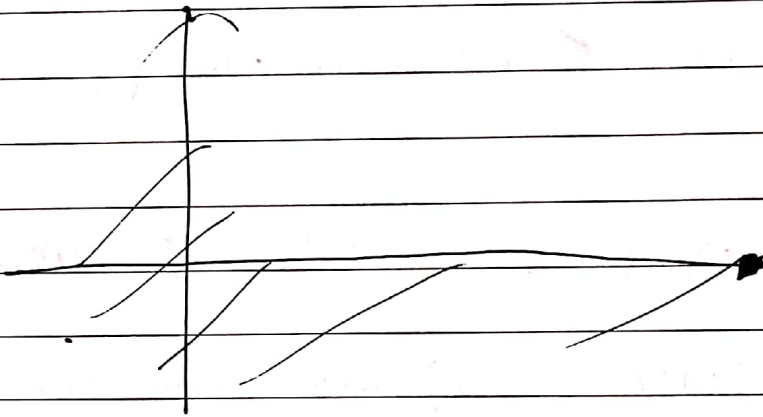
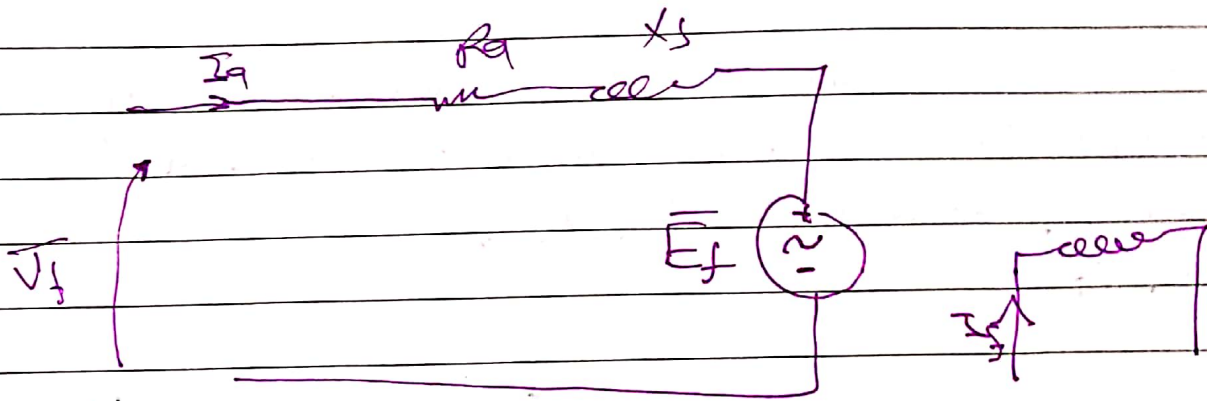
*the only motor that has zero speed regulation

$$N_m = N_{syn}$$

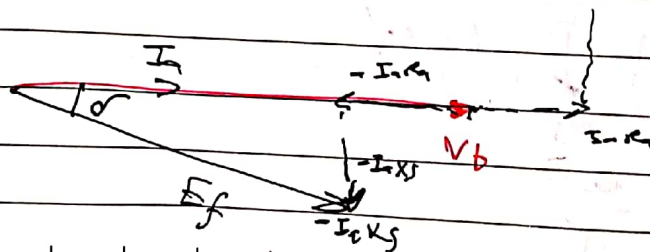
$$\text{Speed Reg} = \frac{N_{syn} - N_{mech}}{N_{syn}} \approx 0$$



Open CKT

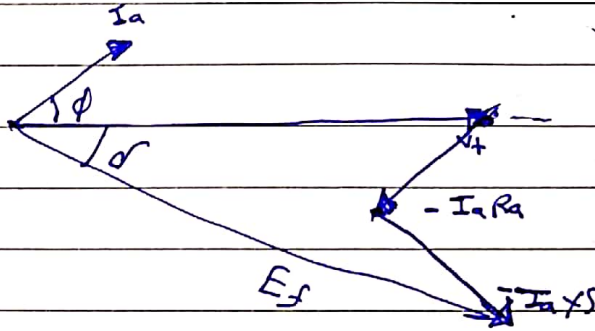


Normal excitation

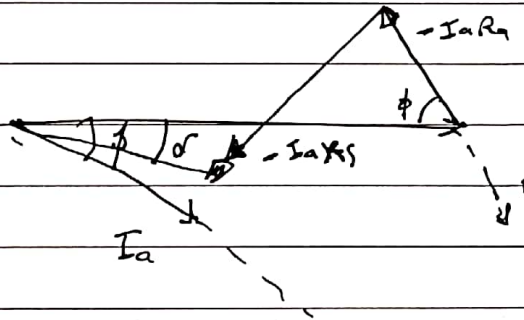


Leading pf =

over excitation

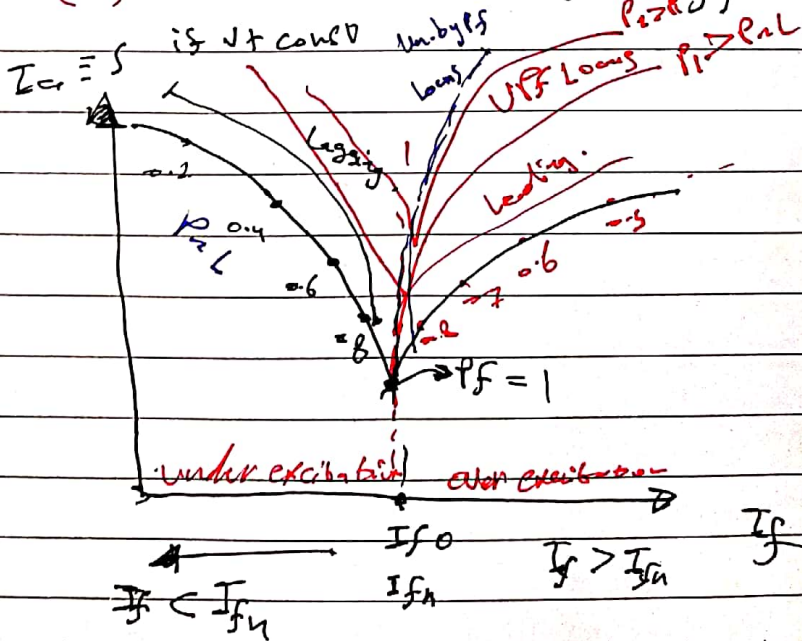


Lagging pf



small Emf under excitation

(W) or (V) curve $I_a = f(I_f)$



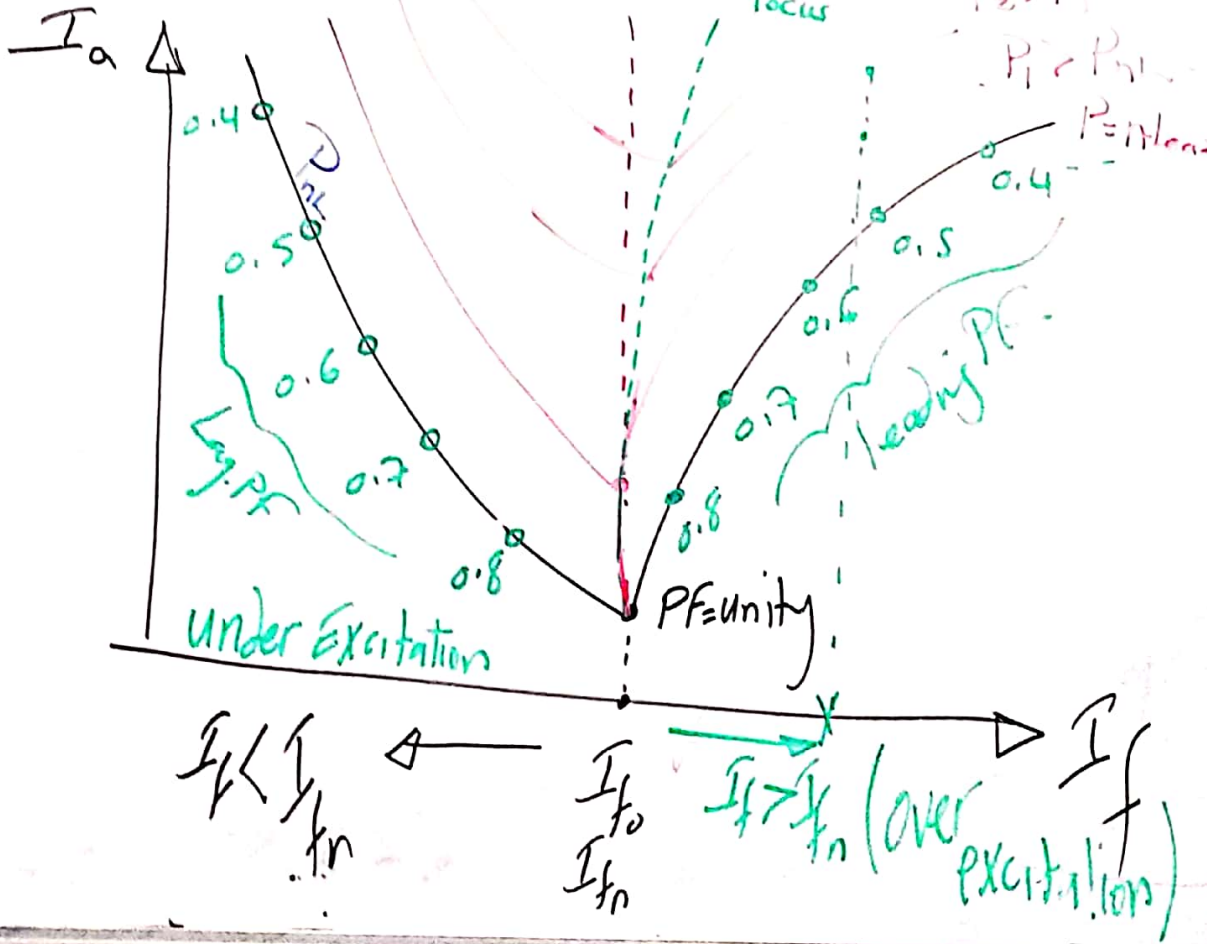
$$I = \frac{P}{V \cos \phi}$$

IPFL

V_s and $P = \text{const}$

V or (V) Curve

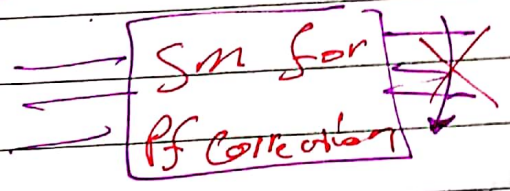
$$I_a = f(I_f)$$



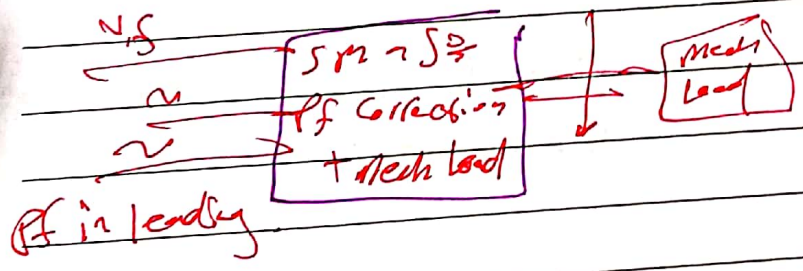
SMG can supply reactive power only $P=0, Q > 0 (+)$
 The motor in this case is known as synchronous capacitor, "Condenser".

reactive power

if



This motor can also be used to supply mech power to Mech. Loads while its power factor is leading (over excitation).



Ex: $V_t = 2300V, f = 50 Hz, S = 500 kW, 2 pole$
 Synchronous motor $R_a = 0.1 \Omega, X_s = 1.2 \Omega$
 If the motor is to supply rated power at $\cos \phi$ lead
 find I_f (Given curve see)

if

to find $I_1 \rightarrow E_1$

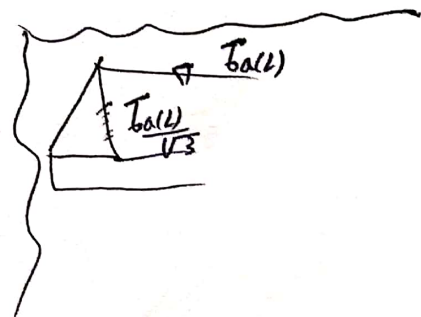
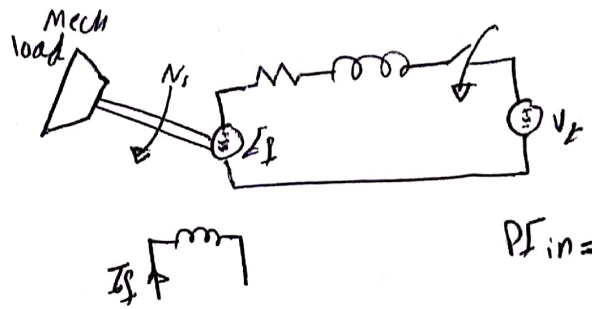
$$\vec{E}_1 = \vec{V}_1 - \vec{I}_1 (R_a + jX_s)$$

$$Z_s = (R_a + jX_s) = 0.1 + j1.0$$

$$= 1.01 \angle 84^\circ \text{ } \Omega/\text{ph}$$

$$I_{a2} = \frac{P_{in}}{\sqrt{3} V_L \cos \phi} = \frac{500 \text{ kW}}{\sqrt{3} \times 2300 \times 0.8} = 156.8 \text{ A/ph (A/line)}$$

$$\vec{I}_a = 156.8 \angle +\cos^{-1} 0.8 = 156.8 \angle 36.87^\circ \text{ A}$$



Per phase $\frac{V_L}{\sqrt{3}}$

$$E_f = \frac{2300}{\sqrt{3}} \angle 0 - 156.8 \angle 53.13^\circ (1.01 \angle 84.1)$$

$$E_f = 1448 \angle -4.24^\circ \text{ V/ph} \Rightarrow \boxed{\delta = -4.24}$$

$$E_f = 1448 \text{ V/ph}$$

$$E_f = 1448\sqrt{3} = 2508 \text{ V/line}$$

curve
 \rightarrow from OCC $\Rightarrow I_f = 4.6 \text{ A}$

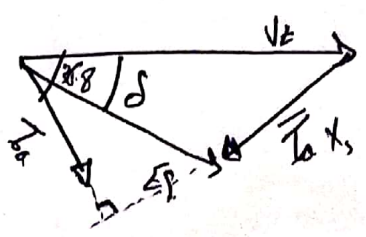
$$S_{in(rated)} = \frac{P}{P.f} = \frac{500 \text{ kW}}{0.8} = 625 \text{ KVA} \angle +36.87^\circ$$

$$= 500 + j375 \text{ KVA}$$

$$S_L = \frac{500}{0.6} = 833.33 \text{ KVA} \angle 53.13$$

$$= 500 - \underbrace{j666}_{Q_{new}} \text{ KVA}$$

neglected R_a



$$E_f = \frac{2300}{\sqrt{3}} - 156 \angle -36.8 \times 1.01 \angle 84.0$$

3 Identical S. Gen are running in parallel.

Rated 3 MW at 0.78 P.F. lag

G_A: $f_{no} = 61 \text{ Hz}$, speed Droop (A) = SD(A) = 3.4%

$$SD = \frac{\text{speed no} - \text{speed Hz}}{\text{speed Hz}}$$

G_B: $f_{no} = 61.5 \text{ Hz}$, speed Droop (B) = SD(B) = 3%

$$= \frac{N_{no} - N_L}{N_L} \%$$

G_C: $f_{no} = 60.5 \text{ Hz}$, speed Droop (C) = SD(C) = 2.6%

$$\text{freq. Droop} = \frac{f_{no} - f_L}{f_L} \%$$

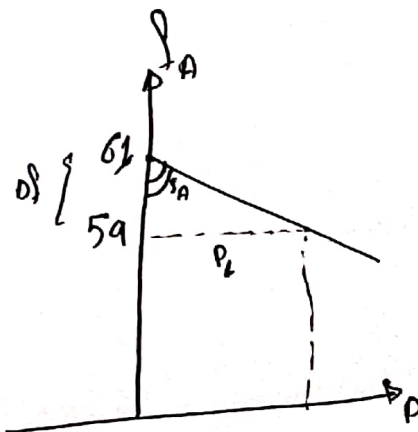
$P_L = 2 \text{ MW} \rightarrow I_{L??}$ then

$P_D = ?$, $P_B = ?$, $P_C = ?$

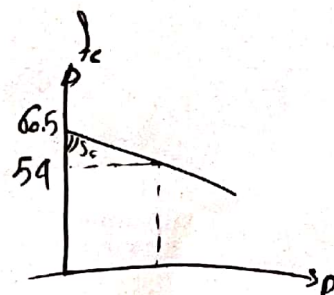
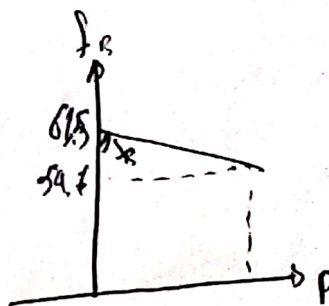
$$N = \frac{60 \text{ f}}{P}$$

S.D = freq Droop

G_A
 $0.034 = \frac{61 - f_L}{f_L} \Rightarrow f_{L(A)} = 58.9 \approx 59 \text{ Hz}$



G_B
 $0.03 = \frac{61.5 - f_L}{f_L} \Rightarrow f_{L(B)} = 59.7 \text{ Hz}$



G_C
 $0.026 = \frac{60.5 - f_L}{f_L} \Rightarrow f_{L(C)} = 59 \text{ Hz}$

ترتيب فقط واحد

S_A : Slope of P/f ch. of Gen. A

$$S_A = \frac{3 \text{ MW}}{61.59} = \frac{3}{2} = 1.5 \text{ MW/Hz}$$

$$S_B = \frac{3 \text{ MW}}{61.5 - 59.1} = 1.67 \text{ MW/Hz}$$

$$S_C = \frac{3 \text{ MW}}{60.5 - 59} = 2 \text{ MW/Hz}$$

$$P_L = P_A + P_B + P_C$$

$$x \text{ MW} = 1.5 [61 - f] + 1.67 [61.5 - f] + 2 [60.5 - f]$$

$$f = 59.6 \text{ Hz}$$

$$P_A = 1.5 [61 - 59.6] = P_A$$

$$P_B = 1.67 [61.5 - 59.6]$$

$$P_C = 2 [60.5 - 59.6]$$

$$P_A = 2 \text{ MW}$$

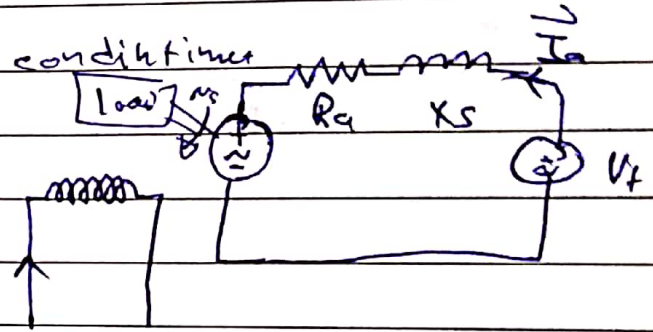
$$P_B = 3.12 \text{ MW} \Rightarrow \text{over load}$$

$$P_C = 1.8 \text{ MW}$$

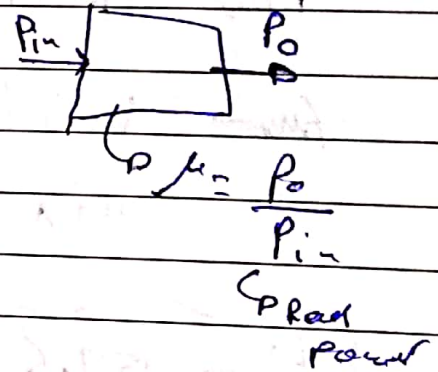
440 V, 50 Hz, 100 HP, 0.89 PF, 89% efficiency ^{↑ disconnected} synchronous motor
 has $R_a = 0.22 \Omega/\text{ph}$, $X_s = 3.14 \Omega/\text{ph}$, $V_t = \text{fixed}$

a) Input current, P_{in} at rated conditions

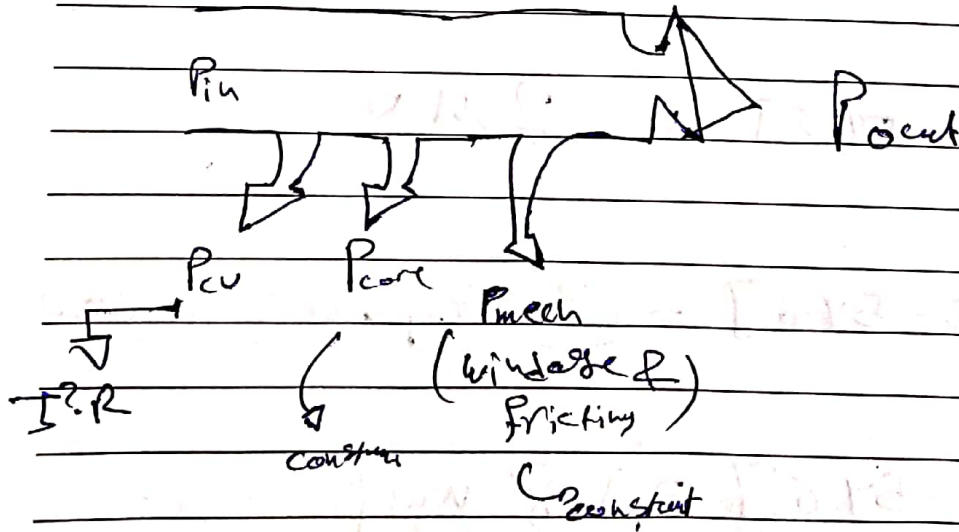
$T_g(\omega) = ?!$



$$P_o = \frac{100 \times 746}{\text{HP}} = 74.6 \text{ kW}$$



$$P_{in} = \frac{P_o}{\eta} = \frac{74.6}{0.89} = 83.82 \text{ kW}$$



* $P_{mech} \Rightarrow$ constant since $N_s \Rightarrow$ constant *

* $P_{core} \Rightarrow$ constant since V_t & f are fixed.

* $P_{cu} = 3 \cdot I_{ph}^2 \cdot R_a$ " variable or load-dependent losses"

$$P_{in} = \sqrt{3} I_{a(L)} * V_{t(L)} \cos \phi$$

$$I_{a(L)} = \frac{83.82 \times 10^3}{\sqrt{3} * 440 * 0.8} = 137.5 \text{ A/line}$$

$$I_a (M) = \frac{137.5}{\sqrt{3}} = 79.375 \text{ A}$$

$$P_{converted} = P_{in} - (P_{cu} + P_{core}) \neq (P_{out} + P_{mech})$$

$$T_g(\omega) = \frac{P_o}{\omega_m} = \frac{P_o}{\omega_s}$$

$$\omega_m = \omega_s \frac{2\pi}{60} \text{ rad/s}$$

$$N_m = N_s = \frac{60 f}{P} = \frac{60 * 50}{2}$$

$$= 1500 \text{ RPM}$$

$$T_g(\text{conv}) = \frac{P_{conv}}{\omega_s}$$

$$Q = \sqrt{3} I_{a(L)} * V_{t(L)} * \sin \phi$$

$$= \frac{2\pi}{60} * \frac{60 f}{P} = \boxed{2\pi f}$$

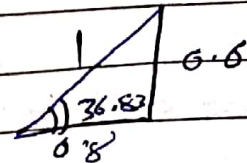
at full load

$$\phi = \cos^{-1}(0.8) = 36.87^\circ$$

$$= \sqrt{3} * 137.5 * 440 * 0.8$$

$$= 62,865 \text{ kVA}$$

$$\omega_m = P \omega_s$$



$$S = 82.83 - j 62.865$$

b) \vec{I} at rated conditions

$$P = \frac{3 V_t E_f}{X_s} \cos \phi \quad \& \quad E_f = I_f L_s$$

$$E_f = V_t - I_a (R_a) Z_s$$

$$3008 \angle 85.8^\circ$$

$$= 440 \angle 0^\circ - 79.375 \angle +36.87^\circ (0.22 + j3)$$

$$I_f R_a = 0$$

$$L_s \angle 3 \angle 90^\circ$$

$$E_f = 603.34 \angle -19.46^\circ \text{ V/ph}$$

motor

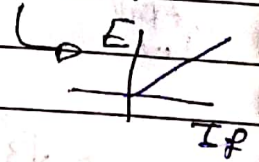
$$\phi = -19.46^\circ$$

c) If I_f is reduced by 10% (No sat)

$$\vec{E}_f = 90\% \vec{E}_f$$

$$E_f = K \cdot I_f$$

$$(I_f = 90\% I_f)$$



new \vec{E}_f
new I_f

$$E_f = 0.9 * 603.34 = 543 \text{ V/ph}$$

$$\vec{I}_a = \frac{\vec{V}_t - \vec{E}_f}{Z_s} = \frac{440 \angle 0^\circ - 543 \angle -21.8^\circ}{3008 \angle 85.8^\circ} = 70.35 \angle +22.42^\circ$$

$$PF = \cos(22.42^\circ) \text{ leading} = 0.924 \text{ lead P.f}$$

* Criteria P_r ($P = \text{ct}$) (neglect R_a)

$$E_f \sin(\delta) = \text{constant}$$

$$E_f \cdot \sin(\delta) = E'_f \cdot \sin(\delta')$$

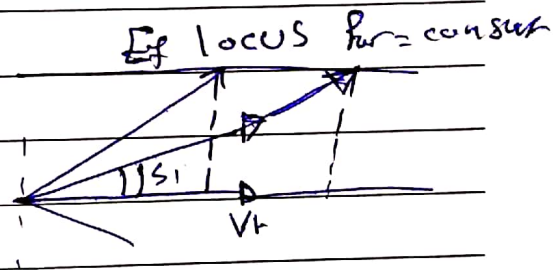
$$\sin \delta' = \left(\frac{E_f / 1}{E'_f} \right) \sin(\delta)$$

$$= \left(\frac{E_f}{0.9 E_f} \right) \sin(-19.1^\circ)$$

$$\delta_2 = -21.7^\circ$$

$$Q = -3 \times 440 \times 70.35 \times \sin(22.4)^\circ$$

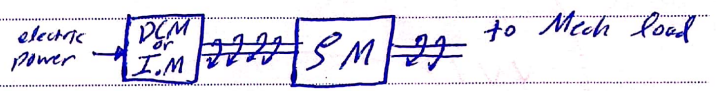
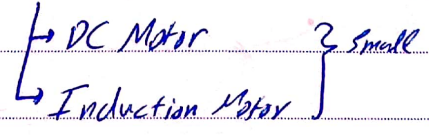
$$= -34.37 \text{ KVA}$$



* Starting of Synchron Motors (why?? \Rightarrow S-M is non-self starting)

How to start the Motor??

1) Use a prime mover



steps (A) disconnect the Mech-load B) I.P.S.V.

c) Start the prime mover up to (almost) Synchron-speed

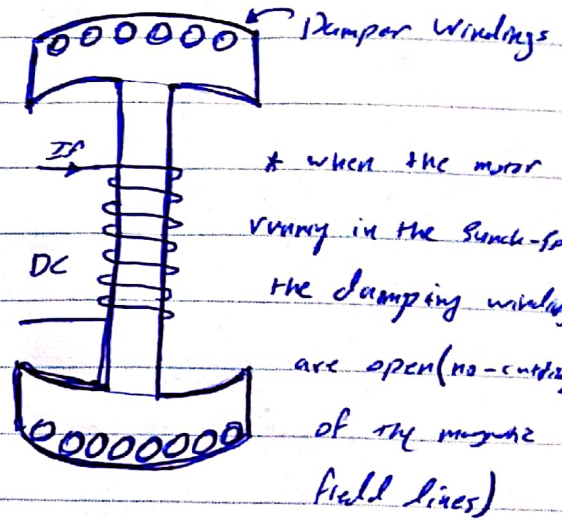
d) connect the field circuit (DO Synchronization) \rightarrow [Connect 3ph-Source \rightarrow Run as motor \rightarrow disconnect the small motor]

2) Damper Windings:

* If $I_f > 0$, stator connected to 3-ph supply
it's run as an induction motor
(unloaded)!!

then connect the I_f

* it also serves as a damping tool
to any disturbance of motor speed
(stability-tool)



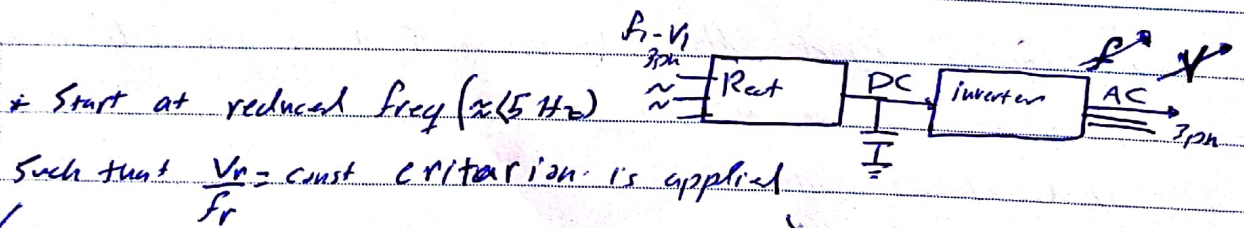
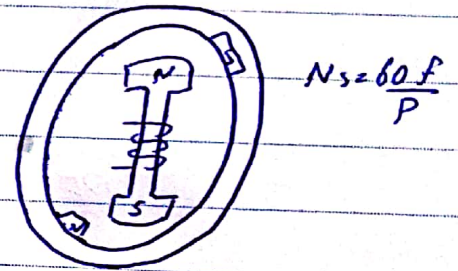
3) Starting by means of frequency control

* why the S-M is non self-starting

↳ the Rotating Field is faster than the
mech load → every cycle the rotor is rotate
then return every 2ms

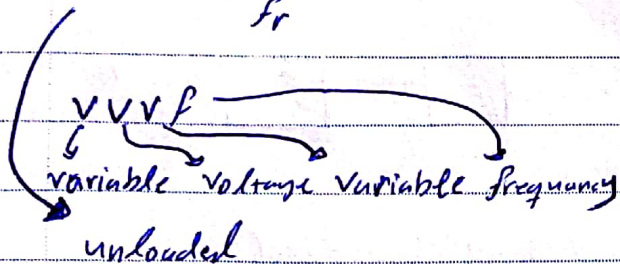
because of the mech loss the rotor is slipping and can't rotate with the field

* Freq-control can be done by the inverter



* Start at reduced freq (5 Hz)

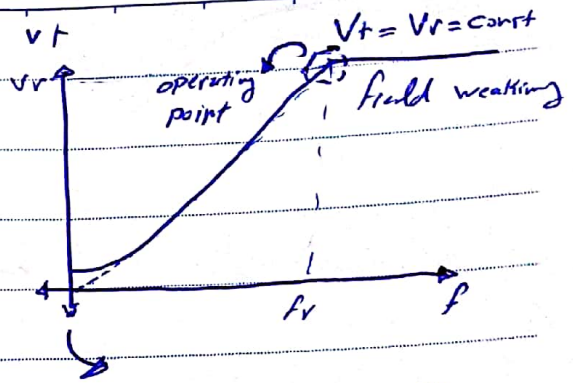
Such that $\frac{V_r}{f_r} = \text{const}$ criterion is applied



Note:
lower freq → lower X_s
So, need to lower the voltage

*) --

* If I want to increase the freq \rightarrow seem't increase V_t than V_r
 \rightarrow So use field weakening method



the curve is not linear because R don't change with the frequency

$$V_t \approx E_f = 4.44 * k * N_p h * f * \phi$$

$$\text{If } V_t \rightarrow \text{constant} \rightarrow f \uparrow \rightarrow \phi \downarrow$$

$$\downarrow$$

$$f \downarrow \rightarrow \phi \uparrow$$

Ex: 11-16 Y-connected $S = 300 \text{ kVA}$

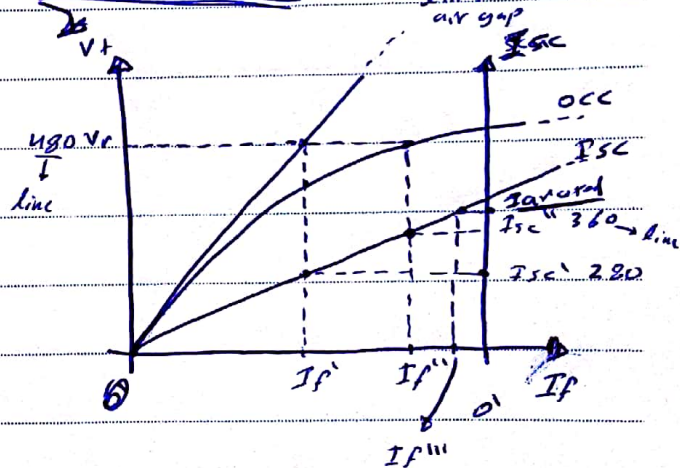
Find $Z_s(\text{sat})$

$Z_s(\text{unsat})$ SCR

$$* Z_s(\text{unsat}) = \frac{V_r(\text{pu})}{(I_{sc}(\text{pu}))} = \frac{480/\sqrt{3}}{280}$$

$$+ Z_s(\text{sat}) = \frac{480/\sqrt{3}}{360}$$

given line voltage



* SCR (Short Circuit Ratio)

$$\hookrightarrow I_{\text{rated}} = \frac{S}{\sqrt{3} V_{rL}} = \frac{300 \text{ kVA}}{\sqrt{3} 480} = 360.8$$

$$SCR = \frac{I_{f''}}{I_{f'''}} \rightarrow (I_f \text{ from the sat-curve with } V_r)$$

$$I_{f'''}$$

$$\rightarrow (I_f \text{ from the } I(r) \text{ with } I_{sc}\text{-Test})$$

$$(pu) \rightarrow Z_{\text{base}} = \frac{V_{r(\text{pu})}}{I_{r(\text{pu})}} (\Omega), \quad Z(\text{sat})_{pu} = \frac{Z_{\text{sat}} (\Omega)}{Z_{\text{base}} (\Omega)}$$

Ex) in max power $\delta = 90^\circ$ / when $R \neq 0$ $\theta_s = \delta$ (must be $< 90^\circ$)

Ex) const power varied field \Rightarrow Ef sin $\delta = \text{const}$

$$E_f \sin(\theta_s + \delta) \rightarrow < 90^\circ$$



3-ph Induction Motors (Asynchronous) / المصغري / المصغري

* Invented by Tesla

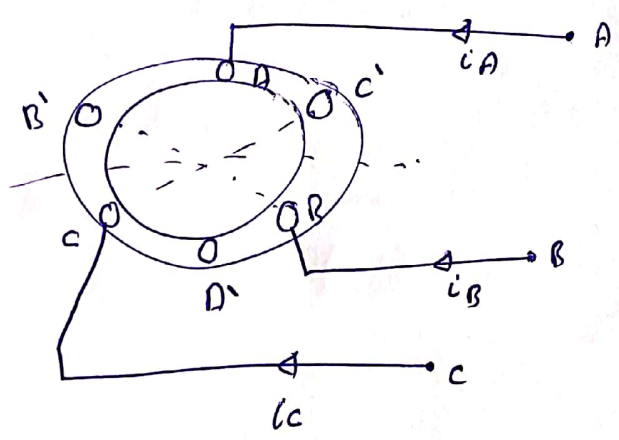
* Construction =>

two Types:

- 1) Squirrel-Cage
- 2) Wound-Rotor

In both cases = stator (where the 3-ph power supply is connected) called the Armature. The stator winding and construction is exactly identical to that of a synth. Machine.

3-ph balanced windings connected to create the required No. Poles.



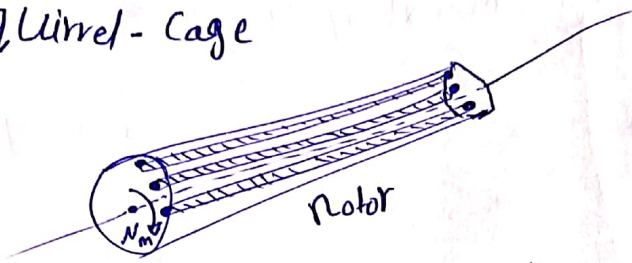
3-ph Power Supply
(f, v)

The supply to the windings creates the Rotating Field at the synchronous speed

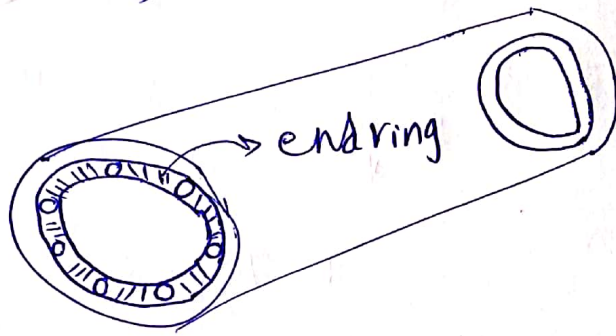
$$N_s = \frac{60 f}{P}$$

$$\omega_s = \frac{2\pi N_s}{60} = \frac{2\pi \frac{60 f}{P}}{60} = \frac{2\pi f}{P}$$

Rotor: Squirrel-Cage

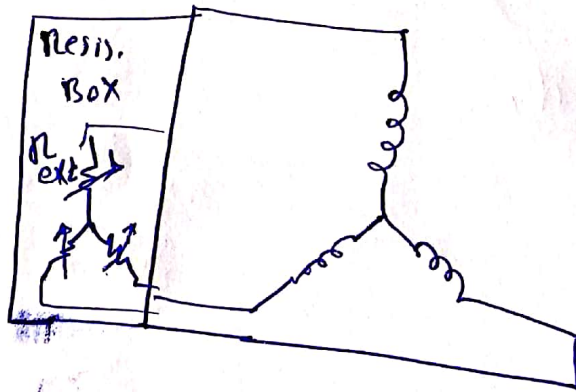


في قيمة المقاومة
منه لبدأ

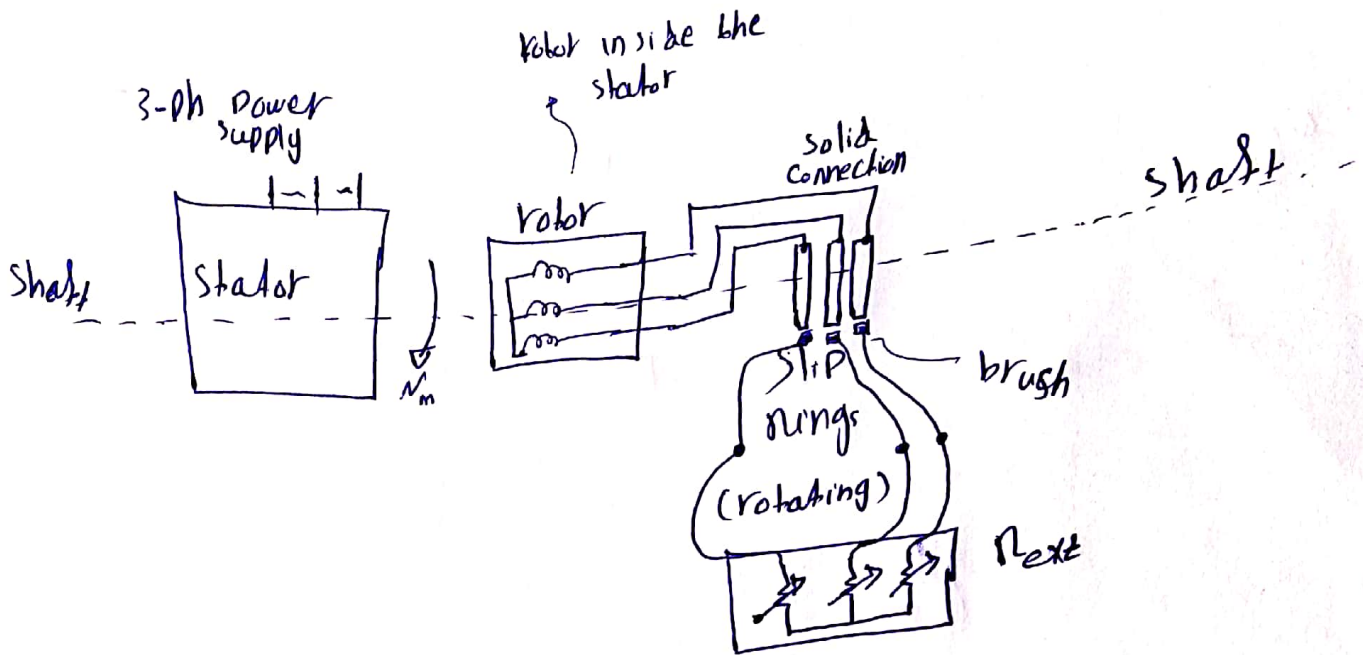


Wound-Rotor Machines

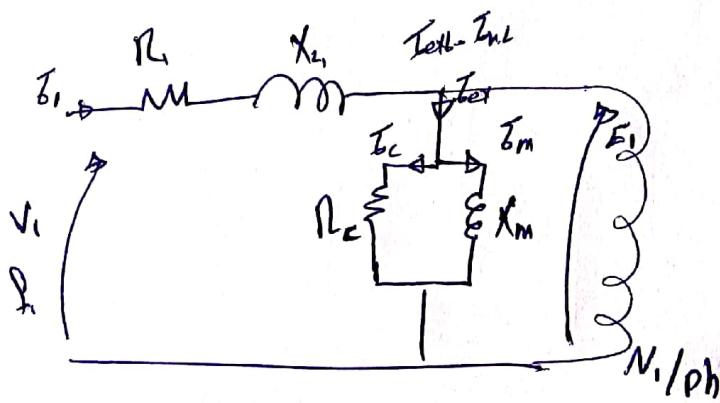
The rotor is wound exactly as the stator, but the ends of these windings are short-circuited through Resistance Box 3-ph external



Wound Rotor



This machine is referred to as (Rotating Transformer).
 The equivalent circuit of the stator of this machine is exactly the same (in terms of its shape) to that of the transformer.



$$E_1 = 4.44 * K_w * N_{1/ph} * f * \phi$$

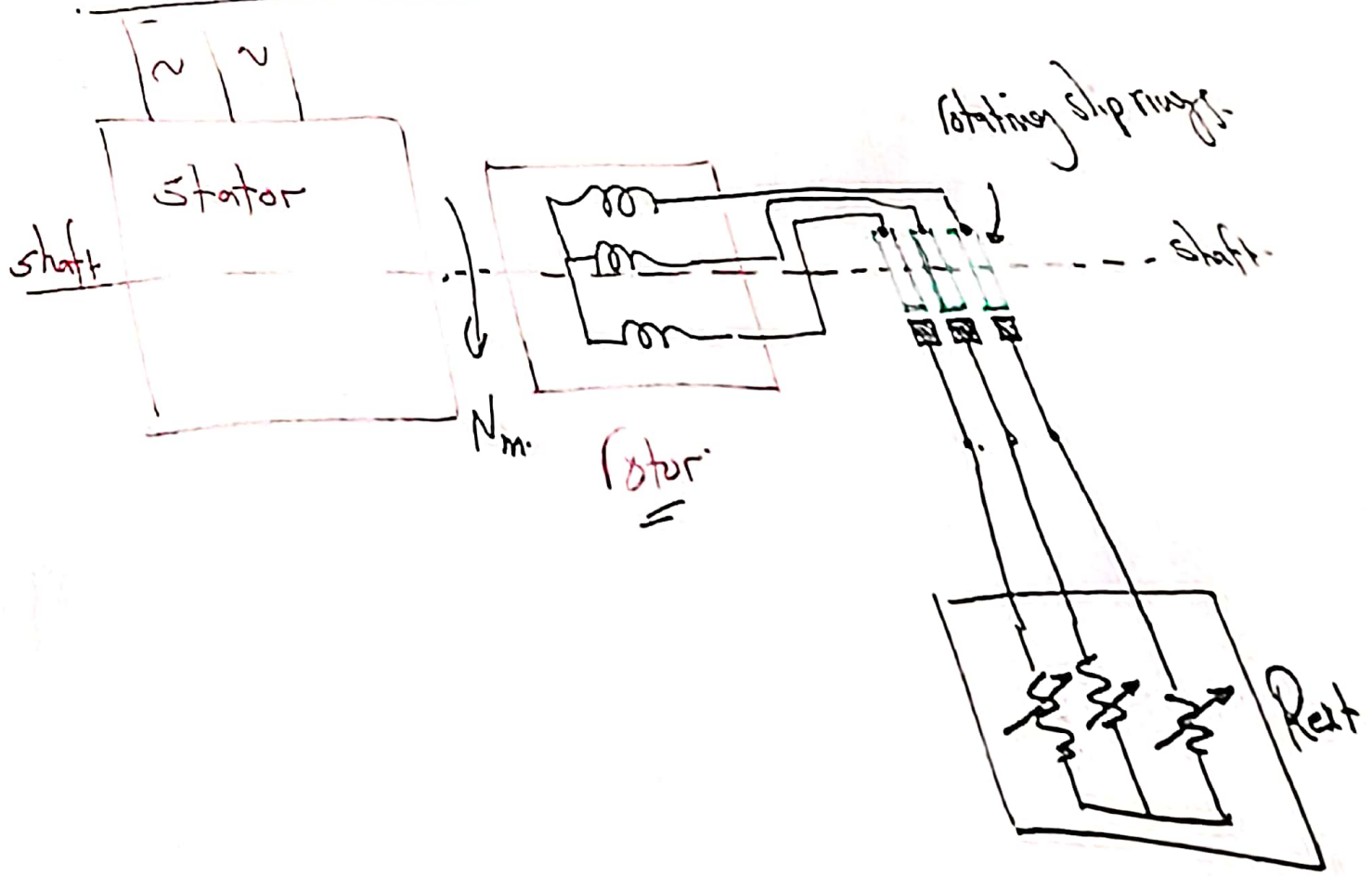
$K_w \Rightarrow$ Winding Factor
 $0.95 \leq K_w < 1$

(Stator winding)

P.F. \rightarrow lag

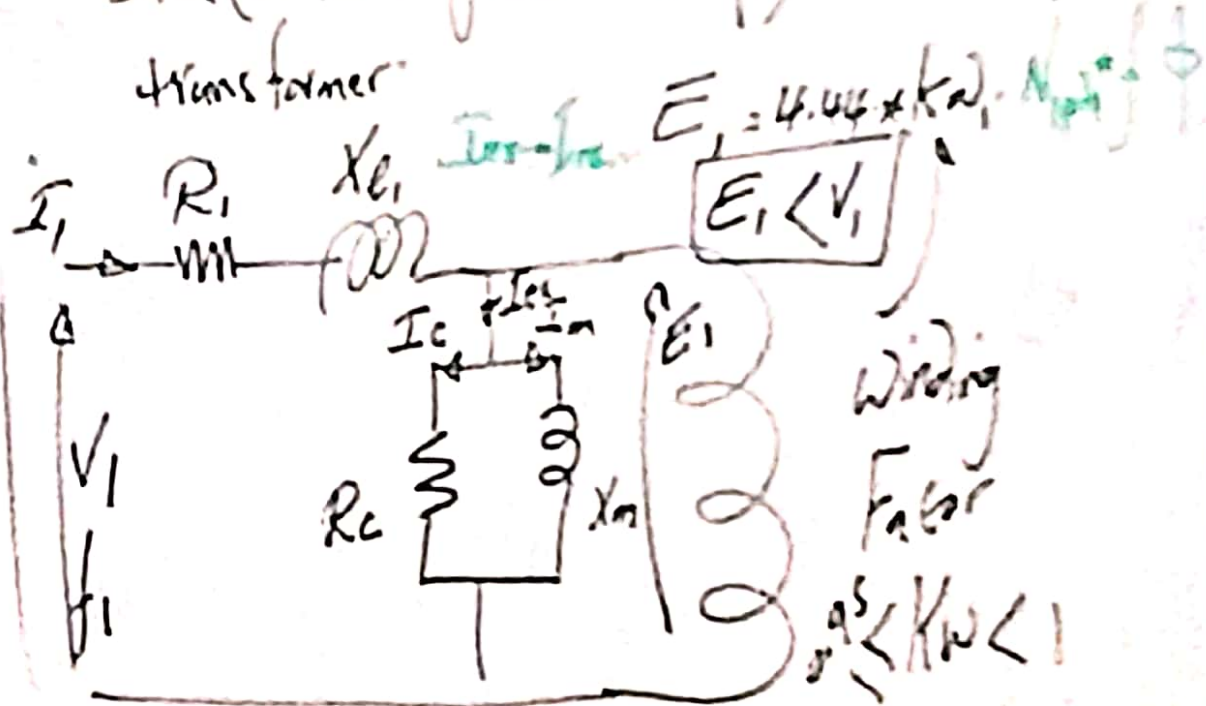
always $E_1 < V_1$

Wound-Rotor Machine



This Machine is referred to as
 (Rotating Transformer).

The equivalent circuit of the
 stator of this Machine is exactly the
 same (in terms of its shape) to that of the
 transformer.



$X_m \rightarrow$ Transformer $X_m(T.R)$

$X_m \rightarrow$ Induction Motor $X_m(I.M)$

The airgap in the induction motor makes all differences

prove $X_m(I.M) \ll X_m(T.R)$

Due to airgap:

$$R_m(I.M) \gg R_m(T.R)$$

$$L_m(I.M) \ll L_m(T.R)$$

$$I_{n2}(T.R) \approx (1-5)\% I_{rated}$$

$$I_{n2}(I.M) \approx (15-40)\% I_{rated}$$

Induction Motors:-

* Equivalent Circuit Development

$N_s \Rightarrow$ the synchronous speed (RPM)
(speed of the rotating field)



$$N_s = \frac{60f}{P}$$

The rotor will move following the stator field at speed N_m (Mech. speed)

$$N_m < N_s$$

Reason:-

friction and windage (Mech. losses),
with no source compensat for these losses.

The rotor is slipping behind the stator field

* Define S as the slip, where

$S \Rightarrow$ relative speed of rotor compare that of the stator field:

$$S = \frac{N_s - N_m}{N_s} \quad (\text{pu or \%})$$

$$0 < S < 1$$

$S=0 \Rightarrow N_m = N_s$ (Impossible)

$S \neq 0 \Rightarrow$ No rotation

Min. Slip at No load

$$s_{nl} = 0.005 \rightarrow 0.01$$

$S=1 \Rightarrow$ at $N_m=0$ (at starting or when the rotor is Blocked)

(equivalent to short circuit in transformer)

$$s_{\text{normal}} = s = 0.03 \rightarrow 0.06$$

In some cases s can reach 15% or 0.15

$$N_s = \frac{60f}{P}, \quad S = \frac{N_s - N_m}{N_s} \Rightarrow f = \frac{P}{60} N_s$$

$f \Rightarrow$ stator freq.
(supply freq.)

$$DN = N_s - N_m$$

$$\text{Rotor } f_{\text{req}} = f_{\text{rotor}} = f_r = \frac{P}{60} (N_s - N_m) = \frac{P}{60} (N_s \times S)$$

$$f_r = S \times f_s$$

\therefore Rotor $f_{\text{req}} = \text{Slip} \times \text{Stator } f_{\text{req}}$

$$E_1 = \text{Stator EMF/ph} = 4.44kV \times N_{ph} \times \phi \times f$$

$$E_2 = \text{Rotor EMF/ph} = 4.44kV \times N_{ph} \times \phi \times f_r$$

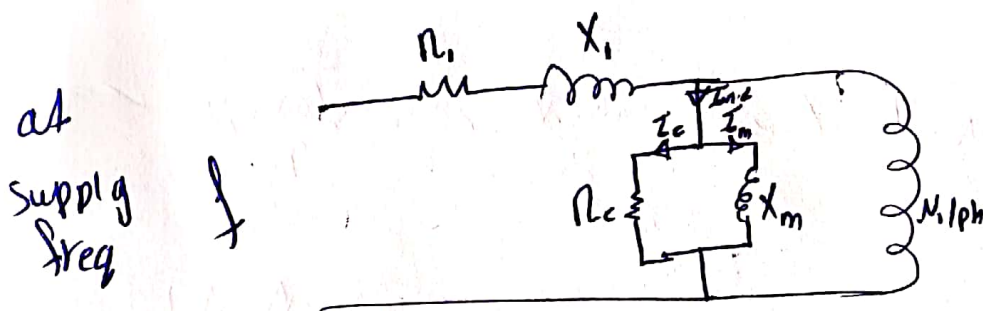
$$\therefore E_{2s} = 4.44 k W_2 \times N_2 / p_h \times \phi \times S \text{ } \}$$

$$E_{2s} = S (4.44 k W_2 \times N_2 / p_h \times \phi \text{ } \})$$

$E_{2s} \Rightarrow$ Motor EMF /ph at Motor } req

$E_{2s} = S \times E_2$, $E_2 \Rightarrow$ Motor EMF at supply } req.

Stator Eq. Circuit



$X_m \Rightarrow$ Magnetization Reactance /ph

$X_1 \Rightarrow$ Stator leakage flux /ph

$R_1 \Rightarrow$ Stator resistance /ph

$R_c \Rightarrow$ core-loss equivalent R_{sis}

$I_{nl} \Rightarrow$ No load current

at

$$T.R \quad X_m < R_c$$

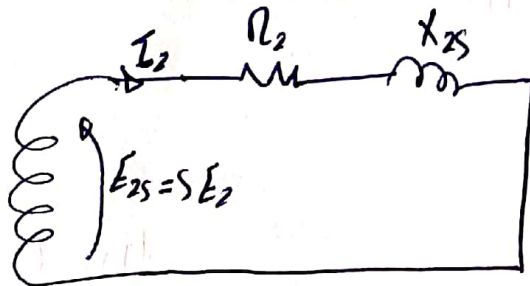
$$T.M \quad X_m \ll R_c$$

at

T.r $I_{0.c} = I_{n.l} \approx (1-5)\% I_{rated}$

I.M $I_{n.l} \approx (15\% - 40\%) I_{rated}$

Rotor Eq. Circuit



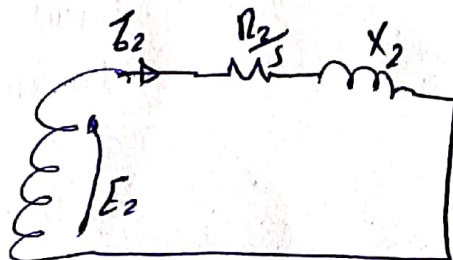
$$I_2 = \frac{E_{2s}}{R_2 + jX_{2s}}$$

$$X_{2s} = 2\pi f_r L_2 = 2\pi f_s L_2$$

$X_{2s} = s \times X_2$ \Rightarrow reactance at supply freq

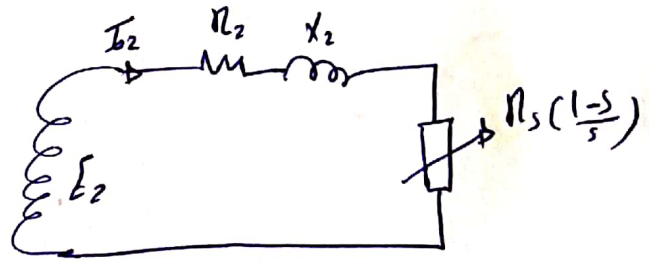
$$I_2 = \frac{s E_2}{R_2 + jX_2 s} = \frac{E_2}{\frac{R_2}{s} + jX_2} = I_2$$

at supply freq



$$\therefore) \frac{R_2}{s} = R_2 + ??$$

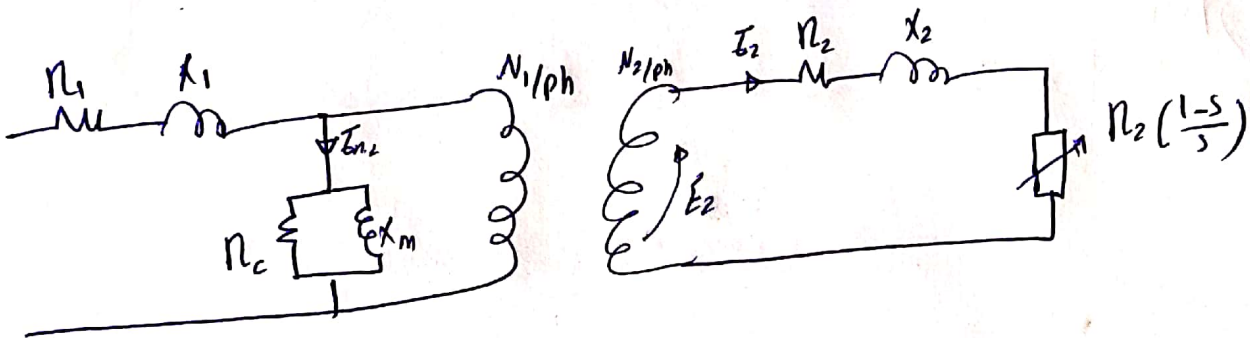
$$\begin{aligned} ?? &= \frac{R_2}{s} - R_2 \\ &= R_2 \left(\frac{1}{s} - 1 \right) \\ &= R_2 \left(\frac{1-s}{s} \right) \end{aligned}$$



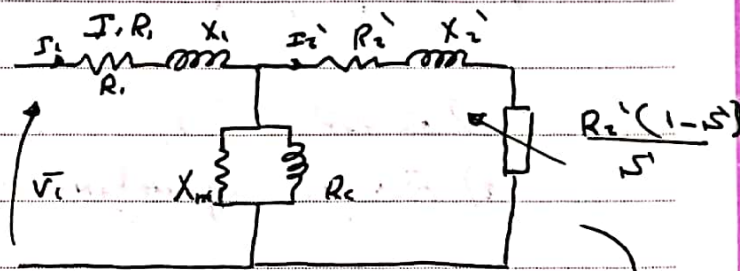
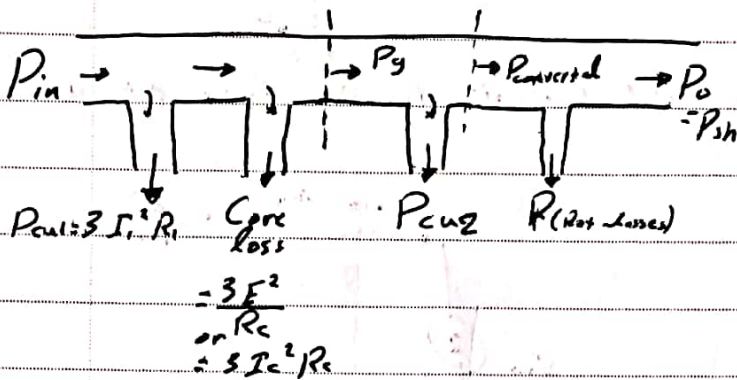
$R_2 \left(\frac{1-s}{s} \right) \Rightarrow$ Mech load Equivalent Resistance

Now

at supply freq.



* Power Flow Diagram



eq. circuit Ref to Source side

eq. Mech Power

* $P_{in} = 3 V_{1ph} I_{1ph} \cos \phi$

phase shift V & I

* $P_{conv} = P_g - P_{cu2}$

$I_2^2 R_2'$

* P_{sh} : useful shaft power

* P_g : Air Gap Power

or: Electromagnetic power

or: Developed power

* $\eta = \frac{P_{in} - P_{out}}{P_{out}}$

$P_g = 3 I_2'^2 \left(R_2' + \frac{R_2'(1-s)}{s} \right)$

* $T_g = T_{div} = T_{ind} = T_{electromagnetic}$

$P_g = 3 I_2'^2 \frac{R_2'}{s}$

$T_g = \frac{P_g}{\omega_s}$, $\omega_s = \frac{2\pi N_s}{60}$

* ~~$P_{converted} = P_g - P_{cu2}$~~

$T_g = \frac{3 I_2'^2 R_2'}{\omega_s s}$

* or $P_{conv} = 3 I_2'^2 \left(\frac{1-s}{s} \right)$
 $= \frac{3 I_2'^2 R_2'}{s} (1-s)$

* $T_{conv} = \frac{P_{conv}}{\omega_m}$, $\omega_m = \frac{2\pi N_s}{60}$
 $\omega_m = \omega_s (1-s)$

$P_{cont} = P_g (1-s)$

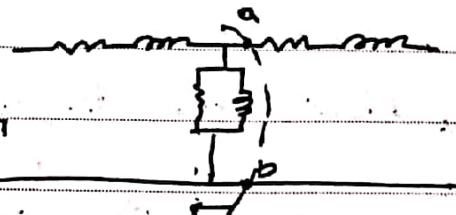
$\frac{P_g(1-s)}{\omega_s(1-s)}$

So $T_{conv} = \frac{P_g}{\omega_s} = T_g$

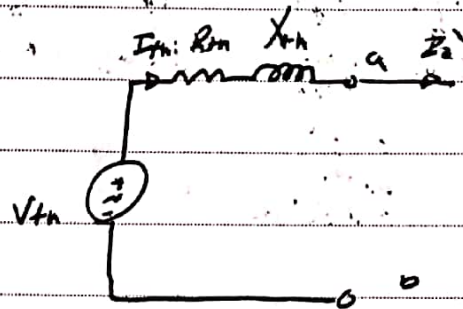
* Torque / Speed char

1) $R_c \gg X_m$

2) Find the equivalent thevenin's circuit to the left of 'ab'



$$* \bar{V}_{th} = V_1 * \frac{j X_m}{R_1 + j X_1 + j X_m}$$



$$= \frac{X_m \angle 90^\circ}{\sqrt{R_1^2 + (X_1 + X_m)^2}} \angle \tan^{-1} \frac{X_1 + X_m}{R_1} V_1$$

Since $R_1 \ll (X_1 + X_m)$

$$\bar{V}_{th} \approx \frac{j X_m}{j (X_1 + X_m)} \bar{V}_1 \Rightarrow \boxed{V_{th} = \frac{X_m}{X_1 + X_m} \bar{V}_1}$$

$$* Z_{th} = \frac{j X_m \parallel (R_1 + j X_1)}{j X_m + R_1 + j X_1} \xrightarrow{\text{let } R_1 = 0}$$

$$\frac{X_m}{X_1 + X_m} (R_1 + j X_1) = R_{th} + j X_{th}$$

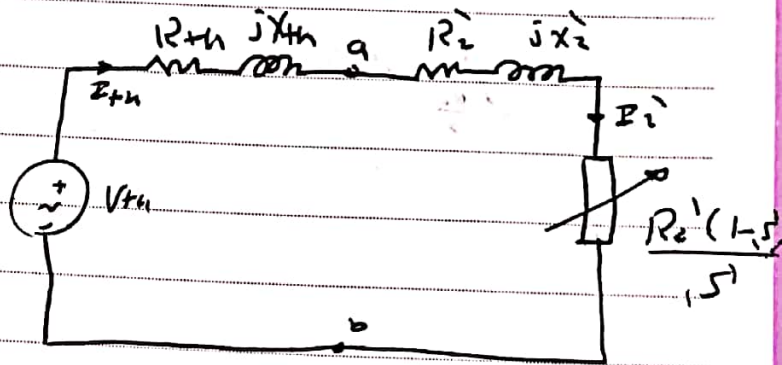
$$\boxed{R_{th} = \frac{R_1 X_m}{X_1 + X_m}}$$

$$\boxed{X_{th} = \frac{X_m X_1}{X_1 + X_m}}$$

* Modified Thevenin's Eq. Circuit

So

$$I_2' = \frac{V_{th}}{\left(\frac{R_{th} + R_2'}{s'}\right) + j(X_{th} + X_2')}$$



$$I_2' = \frac{V_{th}}{\sqrt{\left(\frac{R_{th} + R_2'}{s'}\right)^2 + (X_{th} + X_2')^2}} \angle \tan^{-1} \frac{X}{R}$$

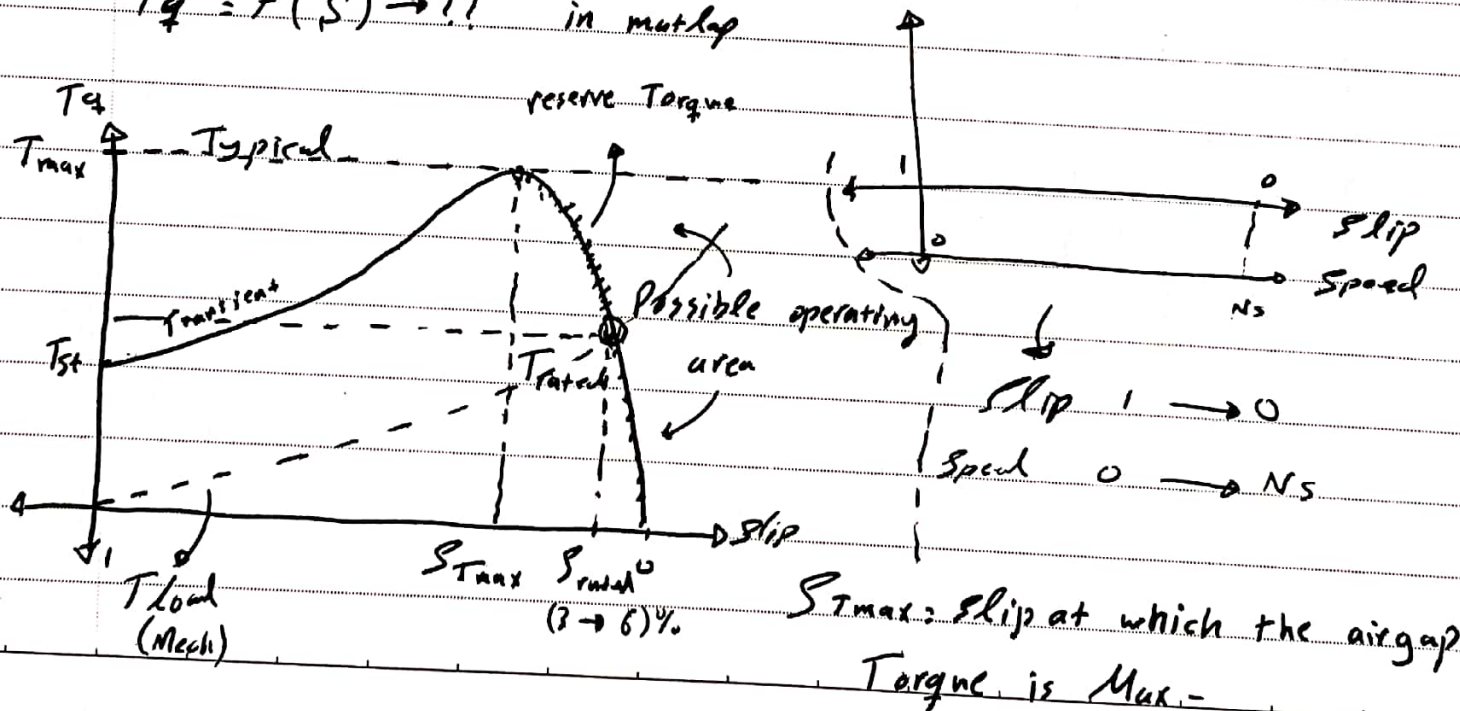
For the Torque & power i need the amplitude

$$R_2' + \frac{R_2'(1-s')}{s'} = \frac{R_2'}{s'}$$

$$* P_g = 3 I_2'^2 \frac{R_2'}{s'} = 3 \frac{V_{th}^2 R_2' / s'}{\left[\left(\frac{R_{th} + R_2'}{s'}\right)^2 + (X_{th} + X_2')^2\right]}$$

$$* T_g = \frac{P_g}{\omega_s} = \frac{3 V_{th}^2 R_2' / s'}{\omega_s \left[\dots \right]}$$

$T_g = f(s') \rightarrow ??$ in matlab

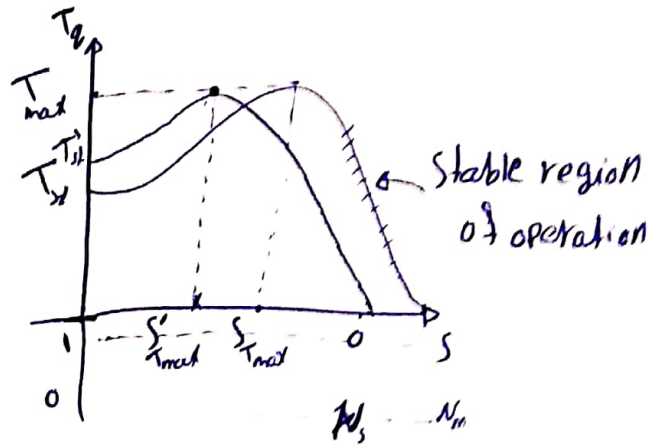


T_{max} = Maximum Developed Torque

$$T_g = \frac{3 V_{th}^2 \times R_2' / s}{\omega_s [(R_{th} + \frac{R_2'}{s})^2 + (X_{th} + X_2')^2]}$$

$$\frac{dT_g}{d(\frac{R_2'}{s})} = \sqrt{R_{th}^2 + (X_{th} - X_2')^2}$$

$$* s_{T_{max}} = \frac{R_2'}{\sqrt{R_{th}^2 + (X_{th} - X_2')^2}}$$



what does mean?

Slip at which the developed is Max depends on R_2' , when R_2' is increased

(Next for the wound-rotor motor)

By adding Next \rightarrow

$$s'_{T_{max}} = \frac{R_2' + R_{ext}}{\sqrt{R_{th}^2 + (X_{th} + X_2')^2}} \Rightarrow s'_{T_{max}} > s_{T_{max}}$$

(Stable region of operation is increased)

Substit in T_g equation

$$T_{max} = \frac{3 V_{th}^2}{2 \omega_s [R_{th} + \sqrt{R_{th}^2 + (X_{th} + X_2')^2}]}$$

T_{max} is dependent on ??

T_{max} is dependent on

1) $V_{th}^2 \rightarrow (V_i)^2 \rightarrow$ square of the applied voltage.

2) R_1, X_1, X_2' \rightarrow by external components

it reduced T_{max}

3) f req control \rightarrow almost $T_{max} = \text{constant}$ if $f < f_r$

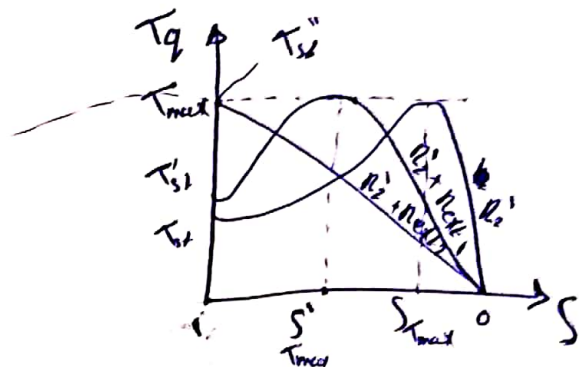
$T_{max} < T_{max}(r)$ if $f > f_r$

* T_{max} Independent of R_2'

$\lambda_{T_{max}} = 1 \rightarrow$ possible

$$\lambda = \frac{R_2' + R_{ext}}{\sqrt{R_{th}^2 + (X_{th} + X_2')^2}}$$

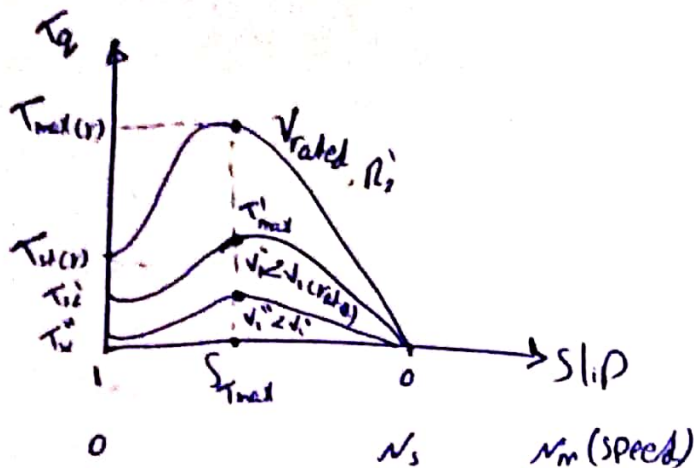
$$R_{ext} = \sqrt{R_{th}^2 + (X_{th} + X_2')^2} - R_2'$$



At such a condition, the motor starts at max torque (required for traction system).

Motors with high T_{st} and wide stability region should be designed with higher R_2' . Solid-Rotor motor is an example (No copper or Al. bus in the rotor)

T_q versus Voltage

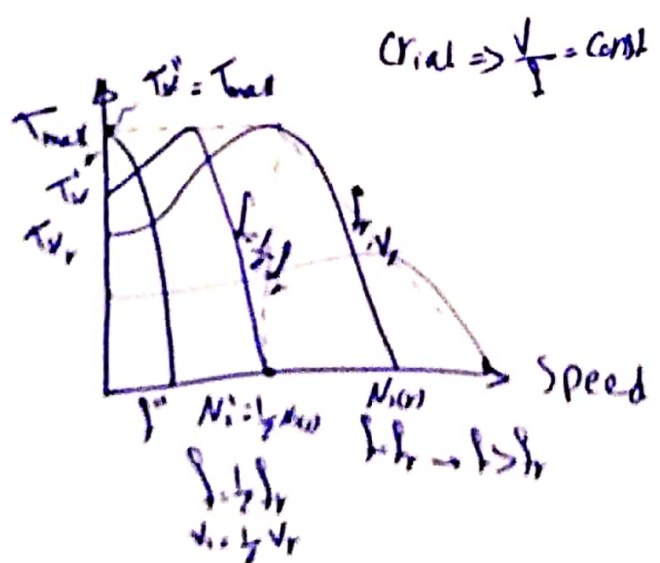


* V₁ can be less than V_{1(rated)}

* S_{max} is independent of V₁
 S_{max} = constant

* T_{max} = f(V₁²)

T_q versus ^{supply} f_{req.} (Modern speed control)



Cr₁ ⇒ V/f = const

N₁ = 60/p f

* T_{max} is reduced

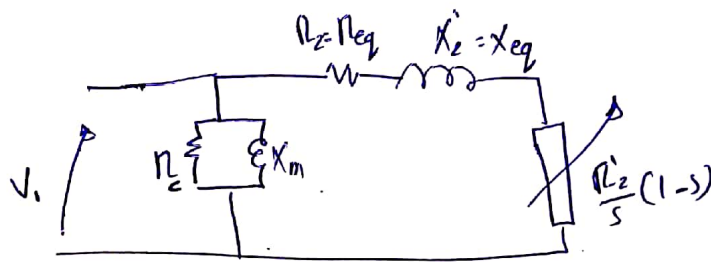
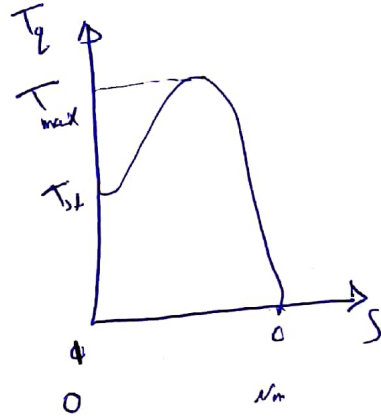
at f < f_r to keep φ = const (No saturation)
 V₁/f = constant to keep φ = const.

Induction Motor Starting

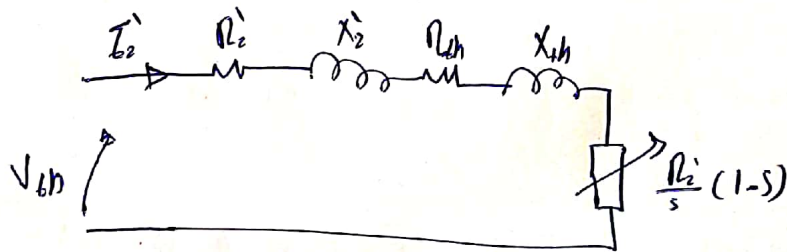
at starting

$$s = 1 \Rightarrow s = \frac{N_s - N_m}{N_s}$$

$$= \frac{N_s - 0}{N_s}$$



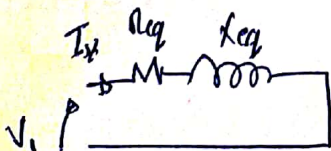
⇓



at starting

$R_2' \left(\frac{1-s}{s} \right) \rightarrow 0$ [equivalent to short circuit] condition in Tr

$$Z_{eq} \ll Z_{o.e}$$



$$I_{sc} = \frac{V_1}{\sqrt{R_{eq}^2 + X_{eq}^2}}$$

$$T_s = \frac{3 I_{sc}^2 \cdot R_2'}{W_s}$$

, 3-ph

$$P = 3 I_{sc}^2 R_2', \quad T = \frac{P}{W_s}$$

$$T_g = \frac{3 I_2' R_2'}{W_s}$$

$$I_{sc} = \frac{V_1}{\sqrt{(R_1 + R_2')^2 + (X_1 + X_2')^2}}$$

$$\frac{I_{sc}}{I_2'(cr)} = (5 \rightarrow 20)$$

$$I_2' = \frac{V_1}{\sqrt{(R_{th} + \frac{R_2'}{s})^2 + (X_{th} + X_2')^2}}$$

$$\frac{T_{sc}}{T_{rated}} = \left(\frac{I_{sc}}{I_2'(cr)} \right) \cdot S_{rated}$$

ex)

$$\frac{I_{sc}}{I_2'(cr)} = 5 \quad \leftarrow \text{from disin}$$

$$S_{rated} = 0.05$$

$$\frac{T_{sc}}{T_{rated}} = 25 \times 0.05 = 1.25$$

ex)

$$\frac{I_{sc}}{I_{rated}} = 10 \quad , \quad S_{rated} = 0.05$$

$$\frac{T_{sc}}{T_{rated}} = 100 \times 0.05 = 5 \quad \text{Not Acceptable}$$

ex)

$$\frac{I_{sc}}{I_{rated}} = 5 \quad , \quad S_{rated} = 0.03$$

$$\frac{T_{sc}}{T_{rated}} = 25 \times 0.03 = 0.75$$

Starting:

The starting is large (up to 20 times rated current)

* If frequent starting this is not acceptable. (burden motor)

* If $P_{rated} > 10 \text{ Kw} \rightarrow$ Not acceptable

T_{sc} is affected by starting current!

Motors should start carefully such that

$$I_{sc} \approx I_{rated}$$

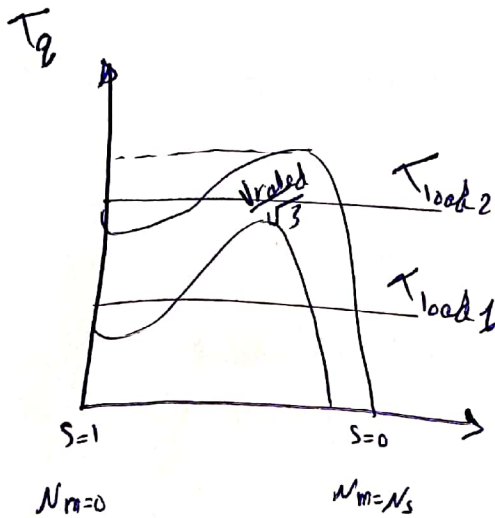
How to reduce I_{s2} ?!

1) Δ normally D-connected, start the motor as Δ (Δ -D starting)

This imply that

$$\frac{I_{s2}(\Delta)}{I_{s2}(D)} = \frac{1}{\sqrt{3}} = 58\%$$

$$\frac{T_{s2}(\Delta)}{T_{s2}(D)} = \left(\frac{V_{(\Delta)}}{V_{(D)}}\right)^2 = \frac{1}{3}$$



$$I_{s2} = \frac{V_1}{Z_{eq}}$$

$$I_{s2}(\Delta) = \frac{V_r/\sqrt{3}}{Z_{eq}}$$

$$I_{s2}(D) = \frac{V_r}{Z_{eq}}$$

$$T_{s2} = \frac{3V_1^2}{Z_{eq}}$$

$$T_{s2}(\Delta) = \frac{3(V_r/\sqrt{3})^2}{Z_{eq}}$$

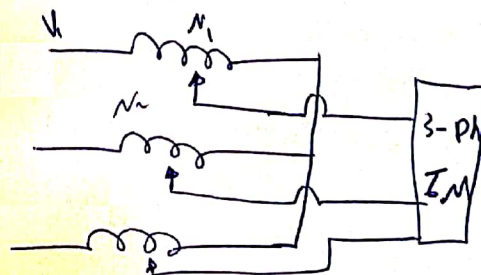
$$T_{s2}(D) = \frac{3V_r^2}{Z_{eq}}$$

2) Starting at reduced voltage using

Auto transformer

$$a = \frac{N_1}{N_2} > 1$$

$$V_{s2} = \frac{V_{rated}}{a}$$



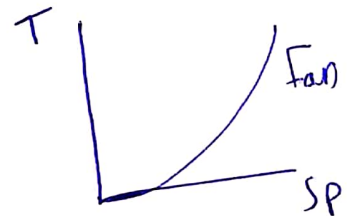
Same side effect same as (1-p)

$\alpha \rightarrow$ variable (not $\sqrt{3}$ only as 1 to)

* load \Rightarrow fan type

Can the reduced voltage apply ~~of~~ efficiently?!

Since T_{st} is very small.



③ Add X_{ext} to the stator

$$I_{st(New)} = \frac{V_1}{\sqrt{(R_{th} + R_{eq} + R_2')^2 + (X_{th} + X_2')^2}}$$

$$I_{st(New)} < I_{st}$$

* but this is inefficient due to copper losses in R_{ext} .

④ Add X_{ext} to the stator circuit

$$I_{st(New)} = \frac{V_1}{\sqrt{(R_1 + R_2')^2 + (X_1 + \underbrace{X_{ext}}_{\text{external}} + X_2')^2}}$$

$$I_{st(New)} < I_{st(Old)}$$

$$T_{st(New)} < T_{st(Old)}$$

$$I_{st(New)} < I_{st}$$

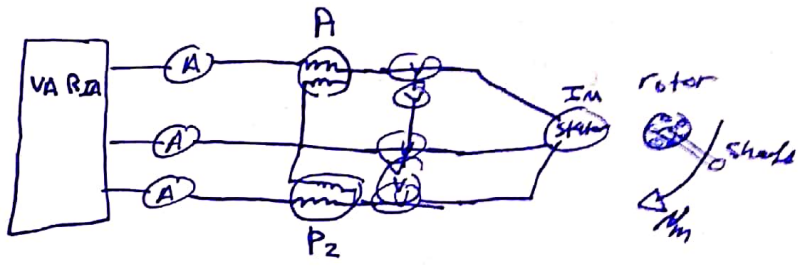
$$T_{st(New)} < T_{st(r)}$$

* but
much lower P.f at starting

* Inducting Motor Testing :-

- 1) No load test
- 2) Blocked-Rotor Test

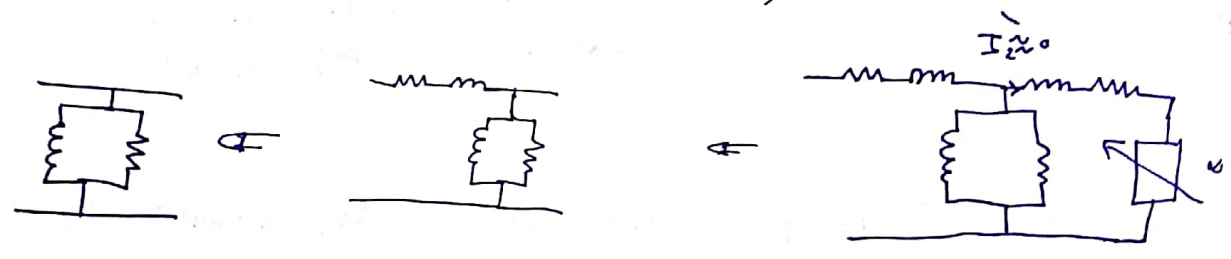
* Wiring diagram



* No load test :- eq val to open circuit Test
 rotor is free to run without mech load

$N_m \approx N_s \rightarrow S=0$

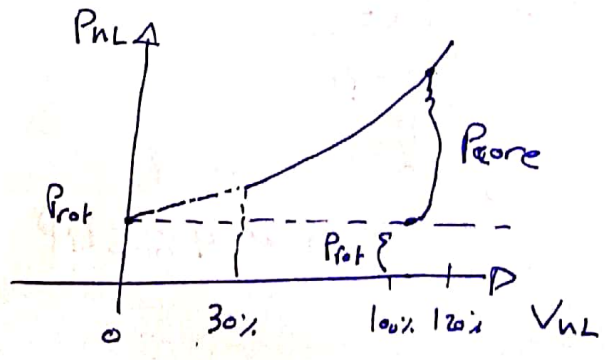
$R_2' \left(\frac{1-s}{s} \right) \rightarrow \infty$ (rotor open circuit)



From this Test, X_m & R_c can be evaluated $P_{core} + P_{rot loss} = P_o$

* To separate P_{core} & P_{rot}

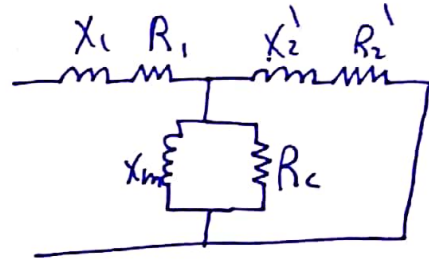
V_{NL}	30%	40	50	60/...	120%
P_{NL}					



Blocked-Rotor Test:-

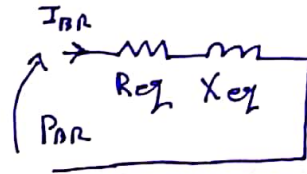
$$N_m = 0 \rightarrow s = \frac{N_s - 0}{N_s} = 1$$

$$R_2' \left(\frac{1-s}{s} \right) \rightarrow \infty$$



$$Z_{oc} \gg R_2' + jX_2' \rightarrow Z_2'$$

* Z_0 can be omitted



* can be calculated $\left\{ \begin{array}{l} R_{eq} = R_1 + R_2' \\ X_{eq} = X_1 + X_2' \end{array} \right.$



Ex: 400 V, 6-pole, 50 Hz Δ -connected 3-ph IM, Running light (No-load) at rated voltage:- 7.5 A, 700 W

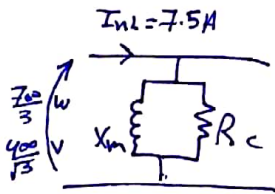
* Blocked-Rotor :- 150 V, 35 A, 400 W
(stator & rotor copper loss are equal)
 $R_1 = R_2'$

$$\frac{X_1}{X_2'} = \frac{1}{0.5}$$

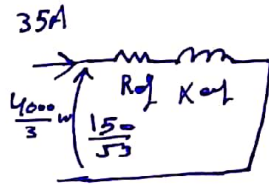
* اذا ما اعطاني بغيرها ارفعها
مساويات

- find :-
- 1) $P_{sh} = ?!$
 - 2) $P_o = ?!$
 - 3) $T_g = ?!$, $T_o = ?!$
 - 4) $s = ?!$ - at 4% slip

No-load Test



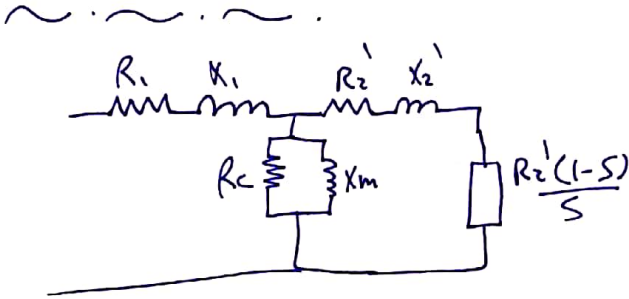
Blocked-Rotor



$$R_1 = R_2' = R_{eq} / 2$$

$$X_{eq} = X_1 + X_2' = X_1 + 0.5X_1 = 1.5X_1$$

$$X_1 = \frac{X_{eq}}{1.5}, \quad X_2' = X_{eq} - X_1$$



$$s = 0.04$$

$$Z_{in} = Z_{oc} \parallel \left(\frac{R_2'}{s} + jX_2' \right)$$

$$I_1 = \frac{V_1}{Z_{in}}, \quad I_2 = \frac{I_1(Z_0)}{Z_0 + \left(\frac{R_2'}{s} + jX_2' \right)}$$

Ex) 460 V, 25 hp, 60 Hz, 4-pole, Y-connected 3-ph induction motor

$$R_1 = 0.641 \Omega/\text{ph}, R_2' = 0.332 \Omega/\text{ph}, X_1 = 1.106 \Omega/\text{ph}, X_2' = 0.464 \Omega/\text{ph}$$

$$X_m = 26.3 \Omega/\text{ph}, R_c \rightarrow \text{large enough (can be omitted)} \quad \underline{1750 \text{ RPM}}$$

$$P_{rot} = 1100 \text{ W} = \text{const}$$

Find 1) T_{st}, I_{st}, T_{max}

2) If R_2 is doubled Recalculate T_{st}, I_{st}, T_{max}

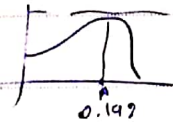
by using the exact eq

Sol) 1)

$$V_{th} = \frac{V}{\sqrt{3}} \frac{X_m}{X_m + X_1} = \frac{460}{\sqrt{3}} \left(\frac{26.3}{26.3 + 1.106} \right) = 254.8 \text{ V}$$

$$X_{th} = X_1 = 1.106 \Omega/\text{ph} \quad R_{th} = R_1 \left(\frac{X_m}{X_m + X_1} \right)^2 = 0.59 \Omega/\text{ph}$$

$$s_{T_{max}} = \frac{R_2'}{\sqrt{R_{th}^2 + (X_{th} + X_2')^2}} = 0.198 \text{ pu or } 19.8\%$$



$$s_{T_{max}} = \frac{N_s - N_m}{N_s} = N_m = N_s (1 - s)$$

$$N_m = 1443 \text{ RPM}$$

$$s = \frac{N_s - N_m}{N_s}$$

$$T_{y_{max}} = \frac{3 V_{th}^2}{\omega_s (R_{th} + \sqrt{R_{th}^2 + (X_{th} + X_2')^2})^2} = 229 \text{ N.m}$$

$$N_s = \frac{60 f}{P} = 1800 \text{ RPM}$$

$$T_{st} = \frac{3 V_{th}^2 R_2'}{\omega_s [(R_{th} + R_2')^2 + (X_{th} + X_2')^2]} = 104 \text{ N.m}$$

$T_{st} < T_{max}$

$$\omega_s = \frac{2\pi N_s}{60}$$

$$I_{st} = \frac{V_{th}}{\sqrt{(R_{th} + R_2')^2 + (X_{th} + X_2')^2}} =$$

$$T_{st} = \frac{3 I_{st}^2 R_2'}{w_s}$$

$$T_{FL} = 3 I_2'(FL)^2 R_2' / S_{PL}$$

Full load \Rightarrow rated value

$S_{PL} \Rightarrow$ at rated speed 1710

$$S_{PL} = \frac{N_s - 1710}{N_s}$$

$$T_{st} = \frac{3 I_{st}^2 R_2'}{w_s}$$

$$\frac{T_{FL}}{T_{st}} = \left(\frac{I_2'(FL)}{I_{st}} \right)^2 \times \frac{1}{S_{PL}}$$

* after adding R_{ext} ($R_{ext} = R_2$)

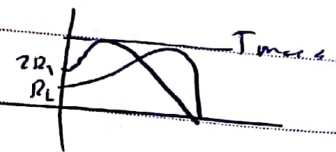
$$* S_{Tmax}' = \frac{R_2' + R_{ext}}{\sqrt{R_{th}^2 + (X_{th} + X_2')^2}} = \frac{2R_2'}{\sqrt{R_2'^2 + (X_{th} + X_2')^2}} = 2 * S_{Tmax} = 0.396$$

$$* N_m = N_s (1 - S_{Tmax}') = 1800 (1 - 0.396) = \dots$$

* T_{max} = the same = 229 constant T_{max} is independent of R_2'

$$* T_{st}' = \frac{3 V_{th}^2 (R_2' + R_{ext})}{w_s \left[R_{th} + R_2' + R_{ext} \right]^2 + (X_{th} + X_2')^2}$$

$$= 170 \text{ Nm}$$



$$I_{st}' = \frac{V_{th}}{\sqrt{(R_{th} + R_2' + R_{ext}')^2 + (X_{th} + X_2')^2}}$$

Q) $R_{ext} = ?$ If $I_{st} = I_{max} ??$

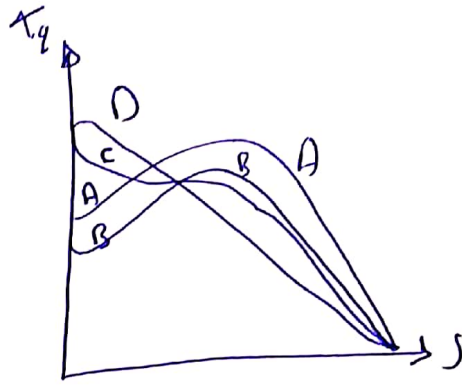
$S = 1$

$$1 = R_2' + R_{ext}'$$

$$\sqrt{R_{th}^2 + (X_{th} + X_2')^2}$$

Classes of T.M :-

- Class A
- Class B
- Class C
- Class D



Differences :

$$\frac{T_{st}}{T_{rated}}, \quad \frac{T_{max}}{T_{rated}}, \quad \frac{I_{st}}{I_{rated}}, \quad S_{T_{max}}, \quad S_{rated}$$

Class A \Rightarrow Classic Motor

$$\frac{T_{st}}{T_r} \approx 1.75 - 2.00 \%, \quad \frac{T_{max}}{T_r} \approx 250 - 300 \%, \quad S_r \leq 0.05$$

$$\frac{I_{st}}{I_r} \approx 500 - 1000 \%, \quad S_{T_{max}} \approx 15 - 20 \%$$

Class B

$$\frac{T_{st}}{T_r} \approx 100 - 150 \%, \quad \frac{T_{max}}{T_r} \approx 200 \%, \quad S_r \leq 0.05$$

$$\frac{I_{st}}{I_r} \approx 700 - 1200 \%, \quad S_{T_{max}} \approx 15 - 20 \%$$

Class c

(Special Design of Squirrel-cage Motor)

[Deep bars or Double-cage I.M]

$$\frac{I_{sk}}{I_r} \approx 275-300\%$$

$$\frac{T_{max}}{T_r} \approx 300\%$$

$$S_r \approx 5\% - 7\%$$

$$S_{T_{max}} \approx \text{up to } 25\%$$

$$\frac{I_{sk}}{I_r} \approx 300\% - 500\%$$

Class D

Mostly wound rotor I.M, with high R_2 . Next can be added to achieve the goal or the more is basically designed with high R_2 .

ex) use Al instead of copper in the rotor bars or use solid rotor without copper or Al bars

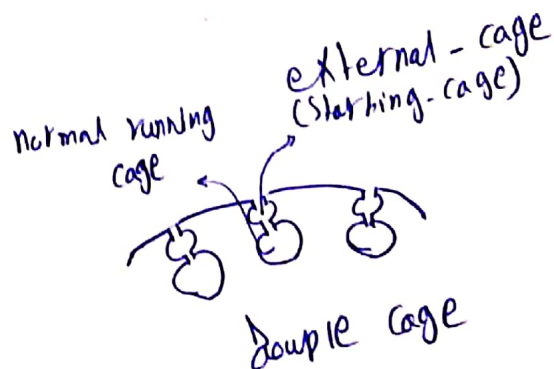
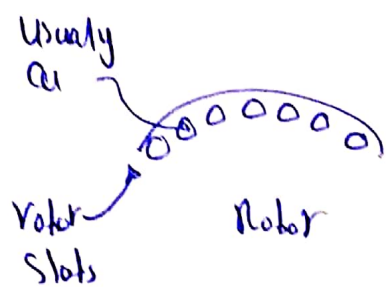
$$S_{T_{max}} \approx 100\%$$

$$S_r \approx \text{upto } 7-11\% \text{ [less efficient]}$$

$$\frac{I_{sk}}{I_r} \approx \frac{T_{max}}{T_r} \approx 275-350\% \text{ [useful for Tranche Application]}$$

$$\frac{I_{sk}}{I_r} \approx 300\% - 500\%$$

Deep bar or double-cage motor



Starting cage \Rightarrow Small cross-sectional area
made of high resistivity material

Normal running cage \Rightarrow large cross-sectional area
made of low resistivity material

At starting $s=1 \Rightarrow \rho_r = s \rho = \rho$

* at starting rotor reactance is much larger than its value at normal running.

* rotor bars that is concentrated in the inner part or [the normal-running cage]
 \rightarrow (implying high reactance)

this reactance reduces as we approach the outer part of the rotor
(Near the air gap)

Also, $I_r = I$ [the highest - value ever]

This implies that the rotor current flows in relatively low cross sectional area in the [outer part or starting cage] implying High R_2 , leading to low starting current, High starting torque.

As s_2 reduces to reach $\approx 5\%$ of its starting value, the internal reactance reduces [in the same ratio]

* [In case of double-cage the electric resistance of the cage is much lower than that of starting one], then the rotor current is driven back to the normal running cage [or more uniformly distributed in the deep bar ratio].

This implies that R_2 is ~~beco~~ becoming lower, leading to High efficiency
Normal running

$$I_{st} = \frac{V_{th}}{\sqrt{(R_{th} + R_i)^2 + (X_{th} + X_i)^2}} = \frac{V_{th}}{\sqrt{(R_{th} + R_i)^2 + f^2 (2\pi X_{th} + 2\pi X_i)^2}}$$

Modern Starting Feeding of I.Motor

*Ex 208 V, 60 Hz, 6-pole, Y_{conn} , 2.5hp Design B Ind Machine

tested, consider $X_2' = 0.41 X_{eq}$

No load 208V, 22A, 1200W, 60 Hz

Blocked Rotor 24.6V, 84.5A, 2200W, 15 Hz

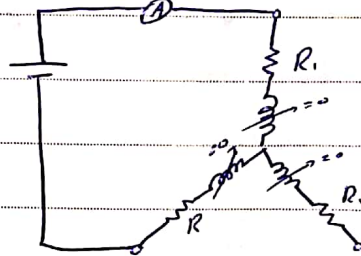
DC Test 13.5V, 64A

Sol

Find every thing

DC test

$$2R_1 = V_{DC} / I_{DC} \Rightarrow R_1 = 0.1055 \Omega/ph$$

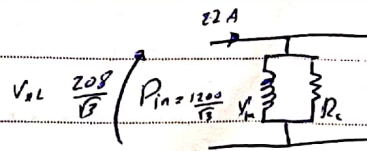


① No-load Test

$$R_c = 41.327 \Omega, X_m = 5.507$$

to find Prot

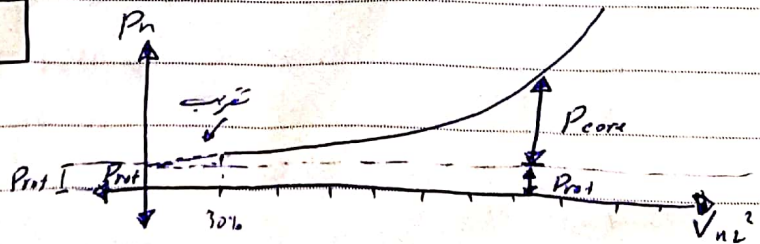
V	30%	40%	50%	...	100%
P_{NL}					



at $V=0$ ($P_{core}=0$)

$$S_0 \Rightarrow P_{NL} = P_{core} + P_{rot}$$

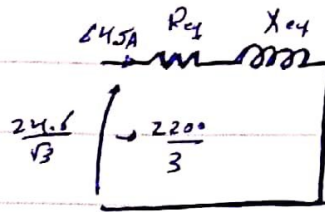
$$P = P_{rot}$$



⊗ Blocked Rotor test

$R_{eq} = 0.1763 \Omega/ph$

$X_{eq} = 0.13147 \Omega/ph$
(15)
Hz



$X_{eq}(60Hz) = 0.13147 * (60/15) = 0.5258$

Why $f \neq f_r$ at BRT??

for more convenient result

So $X_2 = 0.4 X_{eq} \rightarrow$ given

to reduce the (skin effect) Factor

$f \downarrow \rightarrow$ SKIN EFFECT \downarrow
(correction factor)

$X_2 = 0.3167 \Omega/ph, X_1 = 0.2112 \Omega/ph$

ex) 208 V, 4 pole, 10HP, 60 Hz, Y-conn, 3-ph IM

Full load Torque at 3.2% slip at 60Hz and 208

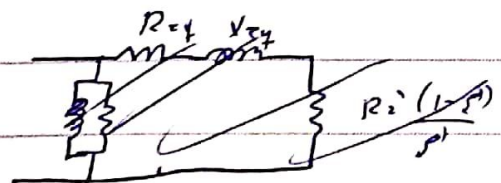
$R_1 = 0.38 \Omega, X_1 = 0.47 \Omega, X_2 = 0.47 \Omega, X_m = 15.5$

$P_{mech} \rightarrow 0$

Find $R_2' = ?$, T_{max} , N_m (T_a (max torque) $T_{st} > ?$)

$R_{th} = R_1 \left(\frac{X_m}{X_m + X_1} \right)^2$

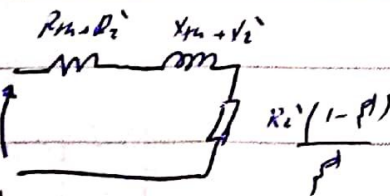
$V_{th} = V_1$



$V_{th} = \frac{V_1 X_m}{X_1 + X_m} = 128.9 V$

$Z_{th} = 0.379 + j 0.464$

$P_{mech} = P_o (P_{mech}(rot) \rightarrow 0) = 10.1746 = 7.46 kW$



$T_g = \frac{P_g}{\omega_s} = \frac{P_{mech}}{\omega_m}$

$\omega_m = \frac{2\pi f}{2} \Rightarrow \omega_s (1-s) = \omega_m$

$= \frac{P_o}{\omega_s (1-s)} = \frac{P_o}{\omega_m} = 41.1 N_m$

$$T_g = \frac{3 V_{th}^2 R_2' / s}{\omega_s \left[R_{th} + \frac{R_2'}{s} \right]^2 + (X_{th} + X_2')^2}$$

Solve

$R_2' = 0.195 \checkmark$
 $R_2' = \dots$



208 V, 4-pole, 10 hp, 60 Hz, X_{conn.} J-FLIM

Full Load Torque at 3.8% slip at 60 Hz and 208 V
 $R_1 = 0.336 \Omega$, $X_1 = 0.47 \Omega$, $X_2 = 0.47 \Omega$, $X_m = 15.5 \Omega$

$P_{mech} \rightarrow 0$

- ① $R_2 = ??$
- ② T_{max} , $S_{Tmax} = ??$ Nm (at Max Torque)
- ③ $T_{st} = ??$

$$T_g = \frac{P_g}{\omega_s} = \frac{P_{conv}}{\omega_m} = \frac{P_o}{\omega_m}$$

$P_{int} = 0$

$$P_o = 10 * 746 = 7.46 \text{ kW}$$

$$\omega_s = \frac{2\pi f}{2} = 377 \text{ rad/s}$$

$$\omega_m = (1-s)\omega_s$$

$$T_g = \frac{P_g}{\omega_s} = \frac{P_{conv}}{\omega_m} = \frac{P_o}{\omega_m} = 41.1 \text{ Nm}$$

$$T_g = \frac{3V_{th}^2 R_2' / s}{\omega_s [(R_{th} + \frac{R_2'}{s})^2 + (X_{th} + X_2')^2]}$$

$$V_{th} = 125.9 \text{ V}$$

$$Z_{th} = 0.339 + j0.164$$

$$R_2' = 0.195$$

$$S_{Tmax} = 0.196$$

$$T_{max} = 99.2 \text{ Nm}$$

$$T_{st} = 44.5 \text{ Nm}$$

$$X_1 = 0.2112 \Omega$$

$$X_2 = 0.2167 \Omega$$

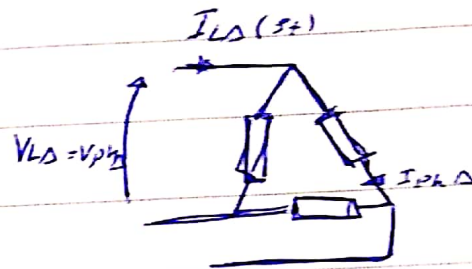
* $Y \rightarrow \Delta$ Starting

Motor: 208V, Δ Connected, $2P=2$, 25hp, 60Hz, 3ph IM

in Δ

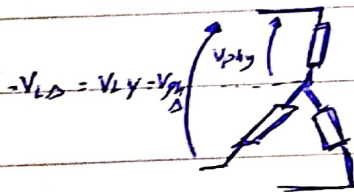
$$I_{ph\Delta}(st) = \frac{V_{ph\Delta}}{Z_{eq}}$$

$$I_{L\Delta}(st) = \frac{V_{ph\Delta}}{Z_{eq}} \times \sqrt{3}$$



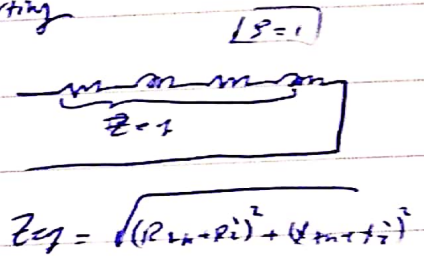
at starting

* Starting at Y



$$I_{LY}(st) = I_{phY}(st) = \frac{V_{ph\Delta}}{Z_{eq} \sqrt{3}}$$

$$V_{phY} = \frac{V_{ph\Delta}}{\sqrt{3}}$$



* Motor Side

$$\frac{I_{phY}(st)}{I_{ph\Delta}(st)} = \frac{V_{ph\Delta}/\sqrt{3}}{Z_{eq} \cdot \frac{V_{ph\Delta}}{Z_{eq}}} = \frac{1}{\sqrt{3}} \quad \left(\frac{1}{3} \text{ less losses } P_{cu} = I^2 R \right)$$

* Line Side

$$\frac{I_{LY}(st)}{I_{L\Delta}(st)} = \frac{V_{ph\Delta}/\sqrt{3}}{Z_{eq} \sqrt{3} \frac{V_{ph\Delta}}{Z_{eq}}} = \frac{1}{3} \quad \left(\frac{1}{9} \text{ less losses} \right)$$

* Starting torque

$$T_{st} = \frac{3 V^2 R_2'}{\omega_s Z_{eq}^2} = \frac{3}{\omega_s} I_{phY}(st)^2 R_2'$$

$$T_{st(\Delta)} = \frac{3}{\omega_s} I_{ph\Delta}(st)^2 R_2'$$

$$\frac{T_{stY}}{T_{st\Delta}} = \left(\frac{I_{phY}(st)}{I_{ph\Delta}(st)} \right)^2 = \frac{1}{3}$$

Ex) 450, 50 HP, 6-poles, Δ -connected, 3-ph IM

$S_r = 4\%$, $\eta_r = 91\%$, $PF = 0.87$ *leading lagging*

at starting, $T_{st} \approx 1.75 T_{rated}$ / $I_{st} = 7 I_{rated}$
 phase values

An auto Transformer is to be used to start the motor such that

$$T_{st}' = T_{rated} \Rightarrow a = ??, \frac{I_{st}'}{I_{rated}} = ?, I_{st}' = ??$$

Primary

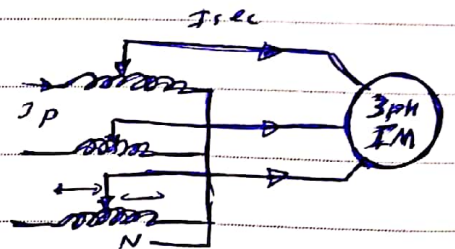
Sol

$$I_{rated} = \frac{P_{in}}{\sqrt{3} V_L \cos \phi} = \frac{40.98 \text{ kW}}{\sqrt{3} \times 480 \times 0.87}$$

$$P_{in} = \frac{P_{out}}{\eta} = \frac{40.98 \text{ kW}}{0.91}$$

$$= 59 \text{ A/line}$$

$$T_{pk} = \frac{59}{\sqrt{3}} = 34.1 \text{ A/line}$$



$$\frac{T_{st}}{T_r} = 1.75, \quad \frac{T_{st}'}{T_r} = 1 \quad (T_{rated} = I_{st})$$

per phase auto transformer

$$\frac{V_c}{V'} = a$$

$$\frac{T_{st}'}{T_{st}} = \frac{1}{1.75}$$

$$\frac{I_{st}'}{I_{st}} = \sqrt{\frac{T_{st}'}{T_{st}}} \Rightarrow I_{st}' = \frac{I_{st}}{\sqrt{1.75}} = 0.76 I_{st}$$

$T_{st} = \frac{3 I_{st}^2 R_r'}{s}$

$$a = \frac{1}{0.76} \left(\frac{V}{s} \right)$$

Single-Ph Induction Motors:

This the most important Existing Single-ph Motor.

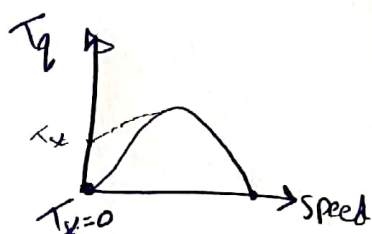
Used in:

Washing machines, ~~fan~~ fans, pumps, Kitchen tools, ...

It is a special Motor.

worst feature: it is a non-self starting motor. $\Rightarrow (T_{st} = 0)$

certain arrangements required to start the motor.



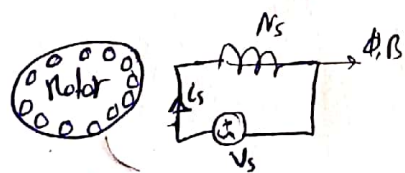
The basic construction features:

Rotor:

usually squirrel-cage [same as that of 3-ph Motors]

Stator:

Single winding supplied by single phase current.



$$B = B_m \cos(\omega_s t - \alpha) \quad \omega = 2\pi f$$

$\alpha \rightarrow$ axis angle of the Rot element

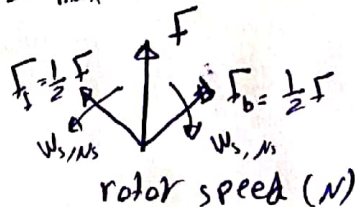
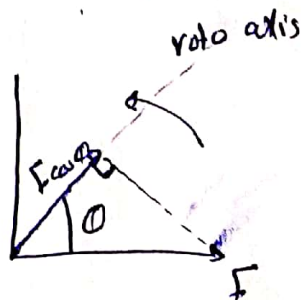
$$F = F_{max} \cos(\omega_s t) \quad \Phi = \Phi_m \cos(\omega_s t)$$

$\Phi, B, F \Rightarrow$ Pulsating, rather than Fixed Rotating Field in 3-ph Motors.

$$F = F_m \cos \omega_s t = F_m \cos(\omega_s t) \cdot \cos 0$$

$$= \frac{F_m}{2} \cos(\omega_s t - 0) + \frac{F_m}{2} \cos(\omega_s t + 0)$$

$$F(\alpha, t) = \frac{1}{2} F_m \cos(\omega_s t - \alpha) + \frac{1}{2} F_m \cos(\omega_s t + \alpha)$$



This implies that the pulsating field can be considered as two components [rotating field rotating opposite to each other.

1) $F_f \Rightarrow$ Forward rotating field (rotor rotates in the same direction as F_f)

define $S_f = \frac{N_s - N}{N_s}$ Forward slip

2) $F_b \Rightarrow$ Back rotating field (in opposite direction of F_f)

define $S_b \Rightarrow$ Slip of the back rot. field F_b

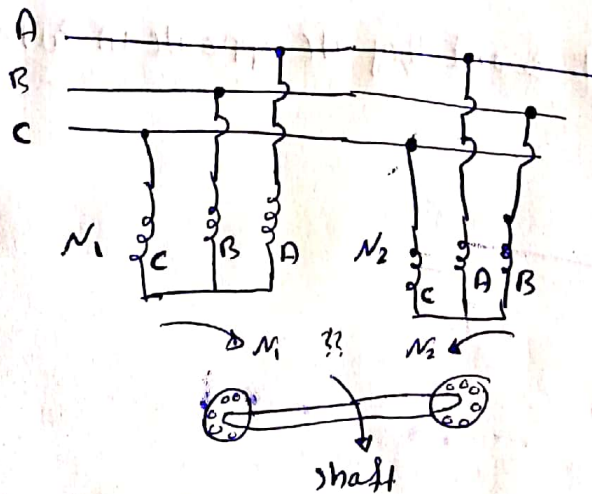
$$S_b = \frac{N_s - (-N)}{N_s} = \frac{N_s + N}{N_s}$$

$$S_b = \frac{N_s + N + N - N_s}{N_s} = \frac{2N - (N_s - N)}{N_s}$$

$$\therefore S_b = 2 - S_f$$

$S_b = S_f \Rightarrow$ This is $S_f = 1 \Rightarrow$ starting instant

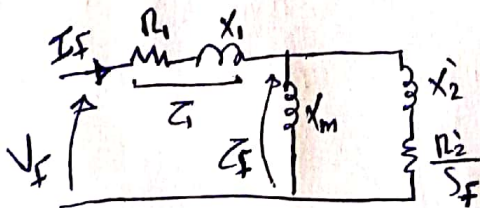
This is equivalent to



This is the two 3-ph equivalent structure of the single-phase Z.M

Equivalent Circuit Development:-

Forward Field:-

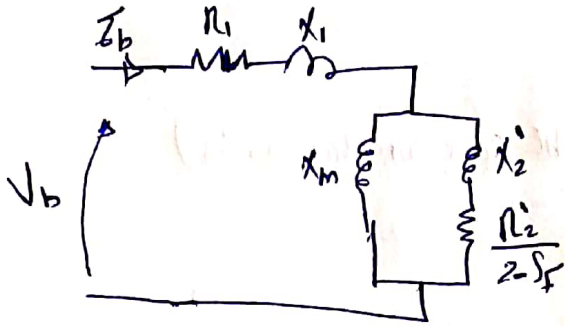


$$\bar{I}_s \Rightarrow \text{stator current [single phase]} = \bar{I}_f + \bar{I}_b$$

$$Z_f = \frac{jX_m \left(\frac{R_2'}{S_f} + jX_2' \right)}{\frac{R_2'}{S_f} + j(X_m + X_2')}$$

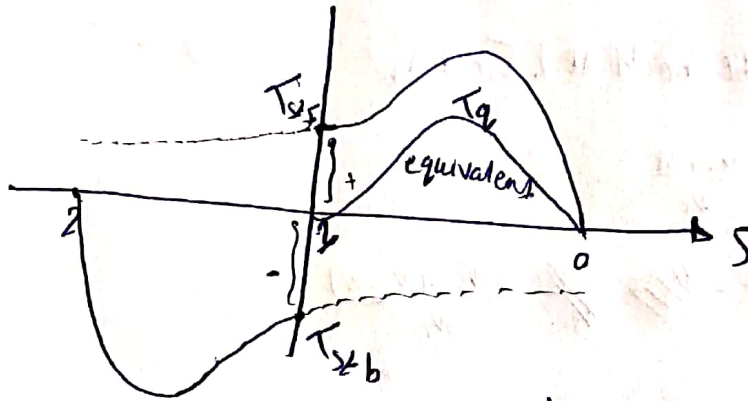
$$\bar{V}_f = \bar{I}_f (Z_1 + Z_f)$$

Backward field:-



$$Z_b = \frac{jX_m(X_2' + \frac{R_2'}{2-s_f})}{\frac{R_2'}{2-s_f} + j(X_m + X_2')}$$

$$\bar{V}_b = \bar{I}_b (\bar{Z}_1 + \bar{Z}_b)$$



→ operating area

Total torque

$$T_g = T_f + T_b$$

$T_z=0 \Rightarrow$ since $T_{sf} = T_{sb} \Rightarrow$ and they are opposite in directions

* Equivalent Circuit

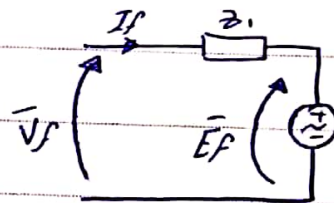
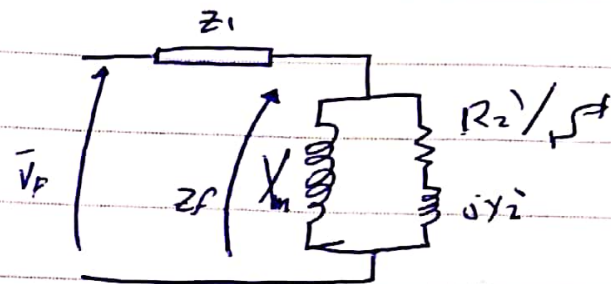
o Forward Field

define $\delta = \delta_F \rightarrow$ hence $\delta_b = 2 - \delta$
 $Z_2 = R_2 + jX_2$

$$* Z_F = jX_m \parallel \left(\frac{R_2}{\delta} + jX_2' \right)$$

$$= R_F + jX_F \quad \bar{V}_F = \bar{I}_F Z_1 + \bar{E}_F$$

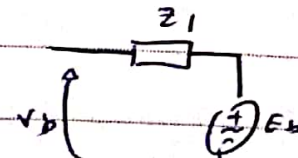
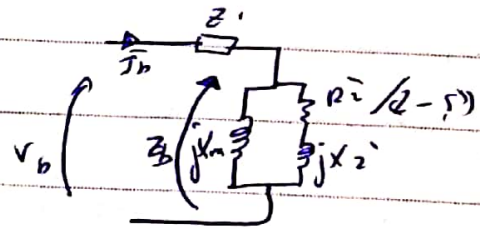
$$\bar{E}_F = \bar{I}_F \times Z_F$$



o Backward

$$Z_b = \omega^2 \parallel 0 \dots$$

$$\bar{V}_b = \bar{I}_b \times Z_1 + \bar{E}_b$$



* the two circuits can be combined into one circuit

$$V_s = I_s Z_1 + \bar{E}_F + \bar{E}_b$$

$$= I_s Z_1 + I_s (Z_F + Z_b)$$

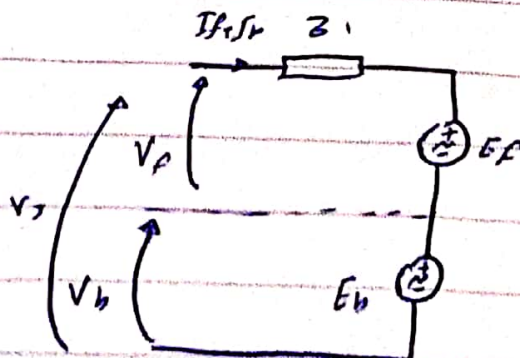
* at stand still

$$\delta_F = \delta_b = \delta \rightarrow Z_F = Z_b$$

$$B(\theta, \dot{\theta})_F = B_{max} (\cos \theta)$$

$$B(\theta, \dot{\theta})_b = B_{max} (\cos \theta)$$

$$\boxed{E_F = E_b}$$



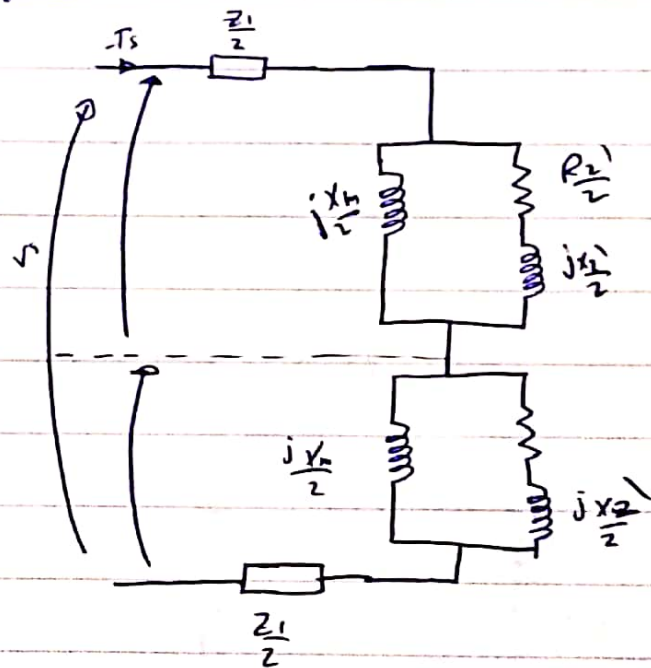
$$Z_f I_f = Z_b + I_b$$

$$\text{Since } Z_f = Z_b \Rightarrow I_f = I_b \Rightarrow I_f = I_b = \frac{I_s}{2} \quad (I_s = I_f + I_b)$$

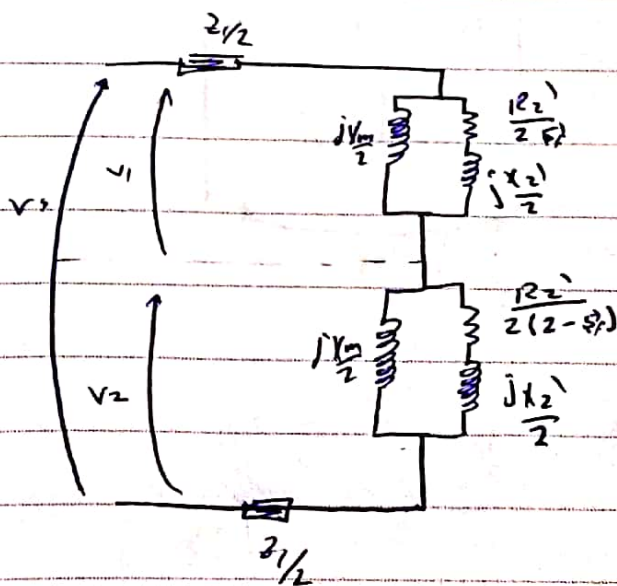
$$V_s = I_s Z_1 + I_s (Z_f + Z_b)$$

$$= \underbrace{Z_1 \frac{I_s}{2}} + \underbrace{Z_1 \frac{I_s}{2}} + \underbrace{\frac{I_s Z_f}{2}} + \underbrace{\frac{I_s Z_b}{2}}$$

only at Start still \Rightarrow



In General



* Starting of Single phase I-M

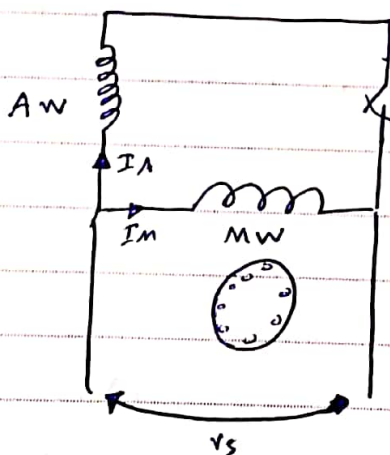
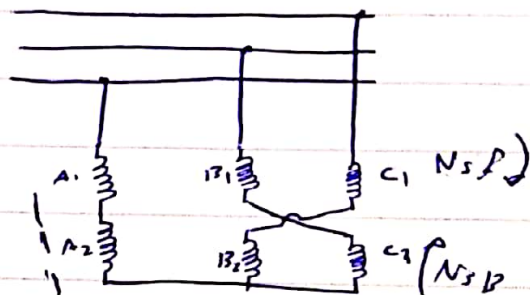
$$T_{gs} = \frac{I_s^2}{\omega_s} \frac{R_f}{2}, \quad T_{gb} = \frac{I_s^2}{\omega_s} * \frac{R_b}{2} \quad Z_f = R_f + j X_{lf}$$

$$T_{overall} = T_f - T_b = \frac{I_s^2}{2\omega_s} (R_f - R_b) \quad \text{at starting}$$

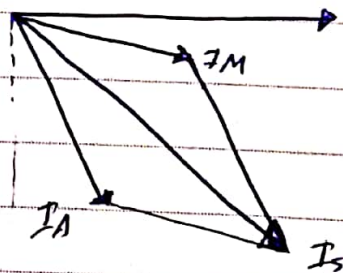
$$\boxed{T_{st} = 0}$$

Problem: Starting Torque = 0

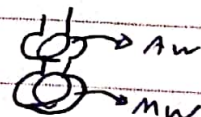
① USE Split-phase IM



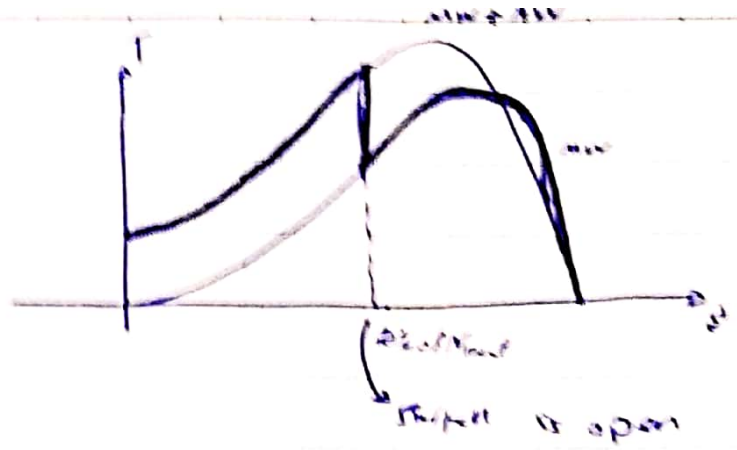
open at 70-80% of NML



AW has $\frac{R_a}{X_A}$ larger than that in MW
 (then wire, outer part of the rotor)
 \downarrow $R \uparrow$ \downarrow $X \downarrow$

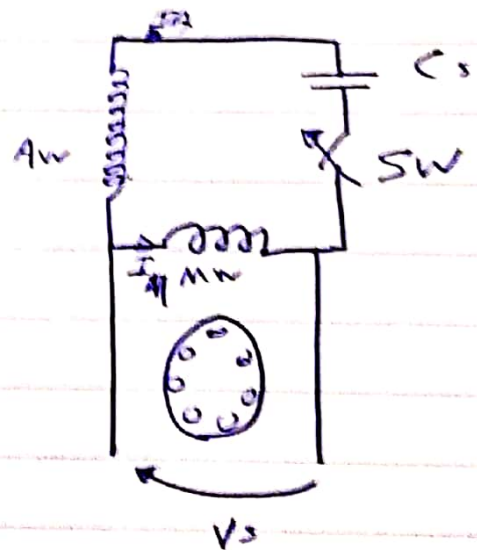
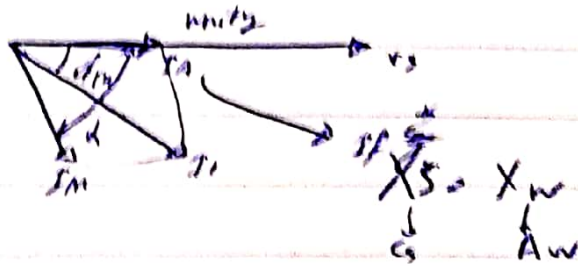


at starting
 ↳ low PF
 ↳ high losses
 ↳ low η



② Capacitor - Start Single phase IM

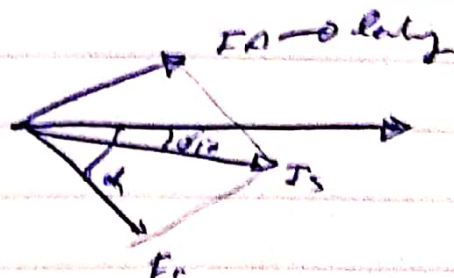
a capacitor C_s is added in series with the AW



For $X_c > X_{AW}$

preval to $\alpha = \frac{\pi}{2}$

SW is open at (70-80)%



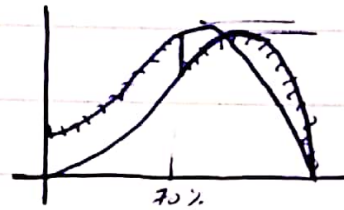
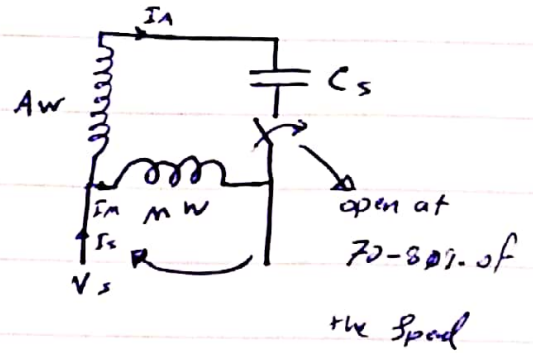
* Capacitor - Run Motor

* with C_s

$$T_{st} > 0$$

$PF_{in} \uparrow$
 at starting

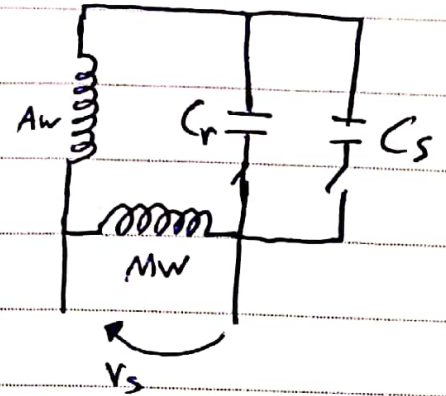
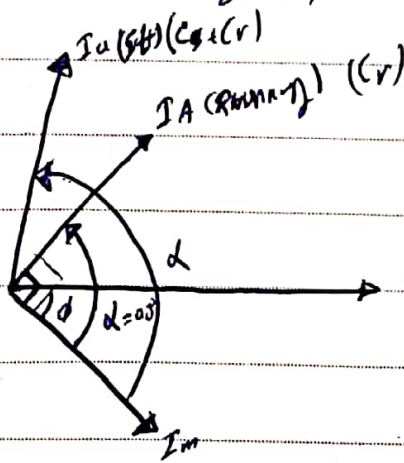
$\eta \uparrow$



③ Capacitor Start, Capacitor Run Motor

C_s : Starting Capacitor

C_r : normal running capacitor * α designed to be greater than 90°



* the parameters are selected such that when C_s is removed $\alpha = 90^\circ$

$PF \uparrow \eta \uparrow \Rightarrow$ normal running

$T_{st} = 2.5 - 3 T_{run} \Rightarrow$ ~~started~~ at starting



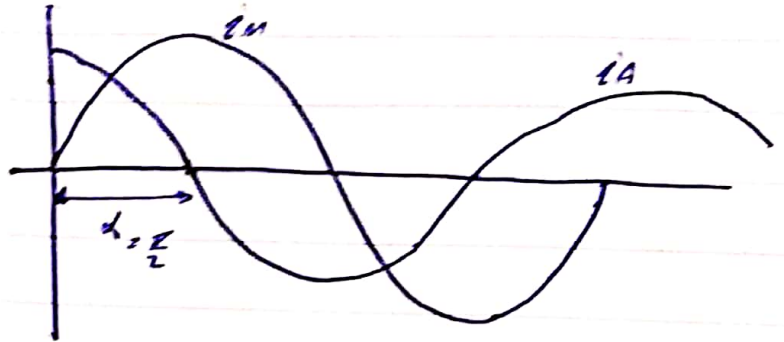
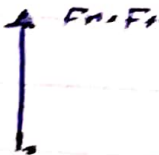
The Rotating Field

@ $t = 0$

$$i_A = I_m \cos(\omega t) \quad F_A \parallel N$$

$$F_A = F_m \cos(\omega t)$$

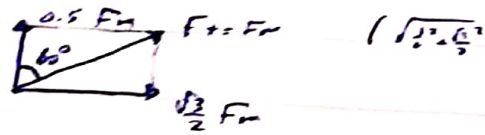
$$F_B = F_m \sin(\omega t)$$



@ $\omega t = 60^\circ$

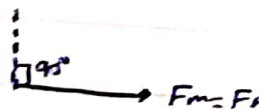
$$F_A = 0.5 F_m \Rightarrow$$

$$F_B = \frac{\sqrt{3}}{2} F_m$$



@ $\omega t = 90^\circ$ $F_A = 0$

$$F_B = F_m \Rightarrow$$



∴ The Field has Fixed amplitude F_m and Rotating is the same speed as ω of the supply current

* Problem

1 kW, 4-pole, 215 V, 50 Hz Single Phase IM

has the parameters $X_m = 10.2 \Omega$, $X_1 = X_2 = 4.02 \Omega$

$R_1 = 1.6 \Omega$, $R_2 = 3.1 \Omega$

- Draw the motor equivalent circuit with all the parameters being shown

- Determine the input current, PF, η , shaft torque, when running at 1440 RPM

$\rightarrow N_m$

Sol

$S_{\text{speed}} = S$ at the value

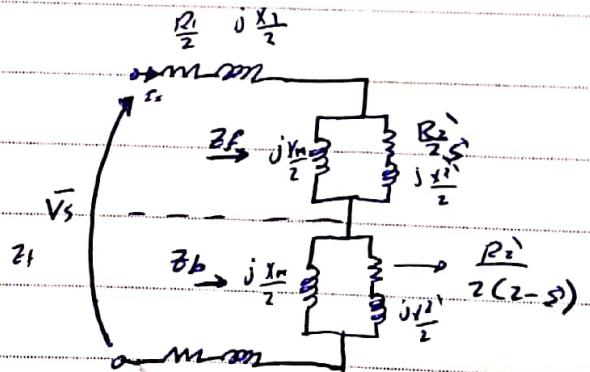
normal n_{mg}

$$S = \frac{1500 - 1440}{1500} = 0.04$$

$$N_s = \frac{60f}{p} = 1500 \text{ RPM}$$

$$\frac{R_2'}{2s} = 38.75 \Omega$$

$$\frac{R_2'}{2(2-s)} = 0.79 \Omega$$



$$Z_f = j \frac{X_m}{2} \parallel \left(\frac{R_2'}{2s} + \frac{jX_2'}{2} \right)$$

$$= \frac{23.73}{\text{RP}} + j \frac{19.63}{\text{XF}} = 32.8 \angle 49.36^\circ \Omega$$

$$Z_b = \dots \parallel \left(\frac{R_2'}{2(2-s)} + \dots \right)$$

$$1.37 + j 3.78 = 4.02 \angle 70.3^\circ \Omega$$

$Z_{\text{motor}} = Z_f + Z_b$, $Z_{\text{series}} = R_1 + jX_1$, $Z_{\text{total}} = Z_{\text{rot}} + Z_{\text{stator}}$

$$Z_{\text{in}} = \dots = 26.7 + j 27.43 = 38.28 \angle 45.77^\circ$$

$$\textcircled{1} \underline{I_s} = \frac{V_s}{Z_{\text{in}}} = \frac{215 \angle 0^\circ}{38.28 \angle 45.77} = 5.62 \angle -45.77^\circ$$

$$\textcircled{2} \text{PF}_{\text{in}} = \cos(\phi_{V_s} - \phi_{I_s}) = (0^\circ - (-45.77)) = 0.7 \text{ lagging}$$

⊗ at starting use the other equ-act
 \rightarrow to find T_{st} , I_{st}

at start $s=1$

$$\frac{R_2'}{2 \times 1} = \frac{R_2'}{2 \times 1} \Rightarrow Z_f = Z_b \text{ at start}$$

* The Torque depends

on \boxed{RP}

* $\eta \Rightarrow$

$$P_{\text{shaft}} = P_o = P_{\text{conv}} - P_{\text{rot}} \rightarrow 0 \\ = 674.9 \text{ watt}$$

$$\eta = \frac{P_o}{P_{\text{in}}} = \frac{674.9}{845.8} = 80\%$$

$$\textcircled{*} T_{\text{sh}} = \frac{P_o}{\omega_m} = \frac{674.9}{4.5} = 150 \text{ Nm}$$

$\omega_m = \frac{2\pi}{60} \times 1500 = 157.08 \text{ rad/s}$

$$T_{\text{gap}} = \frac{P_g}{\omega_s}$$

$$\omega_s = \frac{2\pi}{60} \times 1500 = 157.08 \text{ rad/s}$$

$$P_{\text{in}} = V_s I_s \cos \phi_{\text{in}} \rightarrow 14$$

$$= 215 \times 5.67 \times 0.7 \\ = 845.81 \text{ W}$$

$$P_g = I_s^2 \times (R_f - R_b)$$

or

$$I_s^2 \times R_f \Rightarrow$$



$$P_g = 5.62(23.73 - 1.37) \\ = 706.23 \text{ W}$$

$$P_{\text{conv}} = P_g(1 - s) = 677.9 \text{ W}$$