

Answers should be written in ink

Exam Duration: 70 min

Useful information : for silicon,  $\mu_n = 1350 \text{ cm}^2/\text{V}\cdot\text{s}$  and  $\mu_p = 480 \text{ cm}^2/\text{V}\cdot\text{s}$ .  
 $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ ,  $V_T = 0.026 \text{ V}$  at 300K.

Use the linearized diode model with  $r_f = 0 \text{ ohm}$  unless otherwise mentioned.

Q1 a) Consider n-type <sup>silicon</sup> ~~GaAs~~ at  $T = 300 \text{ K}$  doped to a concentration of  $N_d = 5 \times 10^{15} \text{ cm}^{-3}$ . Assume mobility values of  $\mu_n = 1350 \text{ cm}^2/\text{V}\cdot\text{s}$  and  $\mu_p = 480 \text{ cm}^2/\text{V}\cdot\text{s}$ . Determine the conductivity of the material.

$$\sigma = en\mu_n + ep\mu_p$$

$$n_i^2 = BT^{3/2} \cdot e^{-E_g/kT}$$

$$n_i^2 = n_0 p_0$$

because of  $N_d \gg n_i$   
 $N_d = P_0 = 5 \times 10^{15}$

$$n_0 = \frac{n_i^2}{p_0} = \frac{(2.25 \times 10^{20})}{5 \times 10^{15}}$$

$$n = 45 \times 10^3$$

~~Ans  $\sigma = (1.6 \times 10^{19}) (45 \times 10^3) (1350) + (1.6 \times 10^{19}) (5 \times 10^{15}) (480)$~~

$$\sigma = (1.6 \times 10^{19}) (45 \times 10^3) (1350) + (1.6 \times 10^{19}) (5 \times 10^{15}) (480)$$

$$= 9.72 \times 10^{12} + 384 \times 10^{-3} = 0.384 \text{ (cm}^{-2}\text{)}$$

Determine the applied electric field that induces a drift current density of  $175 \text{ A/cm}^2$ .

$$J = \sigma E$$

$$\frac{175}{0.384} = E \Rightarrow E = 455.72 \frac{\text{A} \cdot \Omega}{\text{cm}^3}$$

b) A silicon pn junction at  $T = 300 \text{ K}$  is doped with  $N_d = 10^{16} \text{ cm}^{-3}$  and  $N_a = 10^{15} \text{ cm}^{-3}$ . The junction capacitance is to be  $0.8 \text{ pF}$  when a reverse bias voltage of  $13 \text{ V}$  is applied. Find the zero-biased junction capacitance.

$$C_j = 0.8 \text{ pF}$$

$$V_{bi} = 13 \text{ V}$$

$$C_j = C_{j0} \left(1 + \frac{V_R}{V_{bi}}\right)^{-1/2}$$

$$0.8 = C_{j0} \left(1 + \frac{13}{V_{bi}}\right)^{-1/2}$$

$$0.8 = C_{j0} \left(1 + \frac{13}{0.637}\right)^{-1/2}$$

$$\frac{0.8}{0.216} = \frac{C_{j0} (0.216)}{0.216}$$

$$V_{bi} = V_T \ln\left(\frac{N_a N_d}{n_i^2}\right)$$

$$V_{bi} = 0.026 \ln\left(\frac{10^{16} \cdot 10^{15}}{(1.5 \times 10^{10})^2}\right)$$

$$= 0.026 \ln\left(\frac{1 \times 10^{31}}{2.25 \times 10^{20}}\right)$$

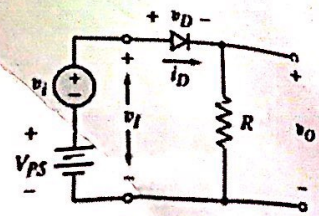
$$= 0.637$$

final answer

$$C_{j0} = 3.70 \text{ pF}$$

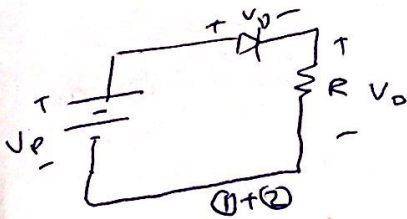


Q3 a) The circuit and diode parameters for the circuit shown are  $V_{PS} = 9.7 \text{ V}$ ,  $R = 9.9 \text{ K ohm}$ ,  $V_Y = 0.7 \text{ V}$ ,  $r_f = 100 \text{ ohm}$  and  $v_i = 0.2 \sin \omega t \text{ V}$ .



Calculate the time-varying diode current and voltage.

First kill  $V_i$  source: we get a DC-circuit



$$V_D = I_D \cdot R + V_D$$

$$9.7 = 9.9 I_D + V_D \quad \text{--- (1)}$$

$$V_D = I_D r_f + V_Y$$

$$V_D = 100 I_D + 0.7$$

$$-0.7 = 100 I_D - V_D \quad \text{--- (2)}$$

$$9.7 = 9.9 I_D + V_D$$

$$-0.7 = 100 I_D - V_D$$

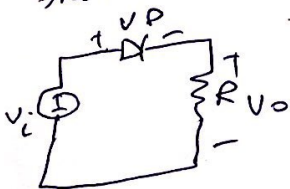
$$9 = \frac{109.9 I_D}{109.9} \Rightarrow I_D = 8.18 \times 10^{-5} \text{ A}$$

$$V_D = 11.97 \text{ V}$$

2.5

then when we switch on  $v_i$

$$V_d = \frac{V_i}{I_D} = \frac{0.026}{0.08} = 317.48 \text{ mV}$$



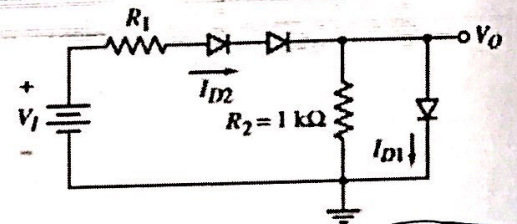
$$V_d = I_D (R + r_d)$$

$$i_D = \frac{v_i}{R + r_d} = \frac{0.2 \sin(\omega t)}{9.9 + 0.325} = 1.957 \times 10^{-5} \sin(\omega t) \text{ A}$$

time varying current

$$v_d = r_d i_d$$

b) Assume each diode in the circuit shown has a cut-in voltage of  $V_Y = 0.7 \text{ V}$ ,  $r_f = 50 \text{ ohm}$  and  $V_I = 6.1 \text{ V}$ . Determine the value of  $R_1$  required such that  $I_{D1}$  is one-half the value of  $I_{D2}$ .



$$V_Y = 0.7 = V_{D1} \text{ because of the sign } V_D \text{ "forward bias"}$$

$$I_{R2} = \frac{V_{D1}}{R_2} = \frac{0.7}{1 \times 10^3} = 7 \times 10^{-4} \text{ A} = I_{D2} \times \frac{1}{2} \rightarrow \text{then } V_{D2} = \frac{I_{D2} r_f}{1} = 7 \times 10^{-4} \times 50 = 1.4 \times 10^{-2} \text{ V}$$

if we apply KVL

$$-V_I + V_{R1} + V_{D2} + V_{R2} = 0$$

$$-6.1 + V_{R1} + 1.4 \times 10^{-2} + 0.7 = 0$$

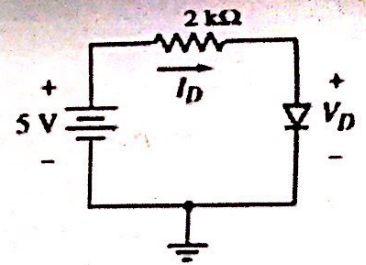
$$V_{R1} = 5.39 \text{ V}$$

$$\text{then } R_1 = \frac{V_{R1}}{I_{D2}} = \frac{5.39}{7 \times 10^{-4}} = 7700 \text{ } \Omega$$

$$\text{and } V_{R2} = \frac{V_A}{R_2} = 0.7$$

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Q2 a) Consider the following circuit, where  $I_s = 10^{-12}$  A. Determine  $V_D$ , and  $I_D$ , using the diode equation and the trial and error method.



$$V_{PS} = R I_D + V_D$$

$$5 = 2 \times 10^3 \cdot \left( I_s \left[ e^{\frac{V_D}{V_T}} - 1 \right] \right) + V_D$$

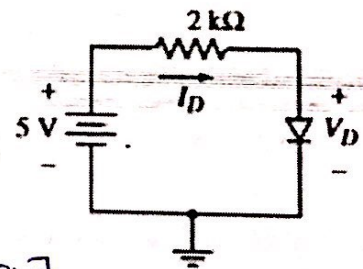
$$5 = 2 \times 10^3 \left( 10^{-12} \left[ e^{\frac{V_D}{0.026}} - 1 \right] \right) + V_D$$

after many trials,

$$V_D = 0.5596 \text{ V}, \quad I_D = 2.2 \text{ mA}$$

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b) Consider the circuit shown. Assume  $V_T = 0.7$  V,  $r_f = 20$  ohm, and  $I_D = 1.2$  mA. Use the piecewise linear model to calculate the voltage drop on the 2 K ohm resistor.



~~$$V_{PS} = I_D R + V_D$$~~

~~$$5 = I_D R + V_D$$~~

~~$$I_D = \frac{5 - V_D}{R}$$~~

~~$$I_D = \frac{5 - V_D}{2000}$$~~

$$V_D = I_D r_f + V_T$$

$$V_D = (1.2 \times 10^{-3})(20) + 0.7$$

$$= 0.724 \text{ V}$$

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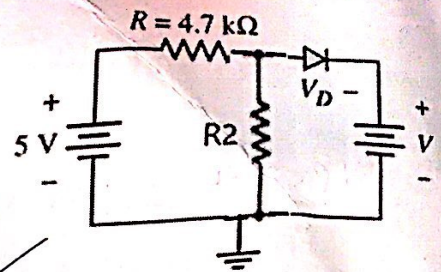
What is the power dissipated in the diode?

$$P = I_D V_D = 8.688 \times 10^{-4} \text{ W}$$



Q4 Consider the circuit shown, where  $V_D = 0.7 \text{ V}$ ,  $r_f = 50 \text{ ohm}$  and  $R_2 = 2 \text{ K ohm}$ .

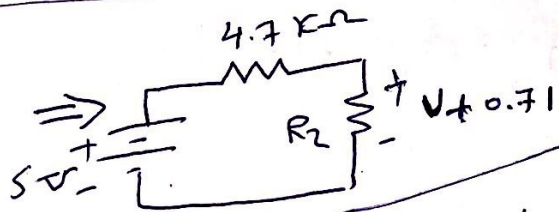
i) Find the supply voltage  $V$  such that the diode current is  $0.2 \text{ mA}$ .



$$V_D = I_D \cdot r_f + V_D$$

$$= (0.2 \times 10^{-3}) (50) + 0.7 = 0.71 \text{ V}$$

$$V_{R_2} = V + 0.71$$



by applying KVL:

$$-5 + 4.7 \times 10^3 I_1 + 2 \times 10^3 I_1 = 0$$

$$\frac{5}{6700} = \frac{6700 I_1}{6700}$$

$$I_1 = 7.46 \times 10^{-4} \text{ A}$$

$$V_{R_2} = \frac{I_1}{R_2} = \frac{7.46 \times 10^{-4}}{2 \times 10^3}$$

$$= 3.73 \times 10^{-7} \text{ V}$$

$$V_{R_2} = V + 0.71$$

$$\Rightarrow V = 0.71 \text{ V}$$

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ii) Calculate the current in the  $R_2$  resistance when  $V = 2 \text{ V}$ .

according to this relation that we determine in the previous question:

$$V_{R_2} = V + 0.71 \Rightarrow V_{R_2} = 1.42 \text{ V}$$

$$I_{R_2} = \frac{V_{R_2}}{R_2} = \frac{1.42}{2 \times 10^3} = 7.1 \times 10^{-4} \text{ A}$$

0

2-5