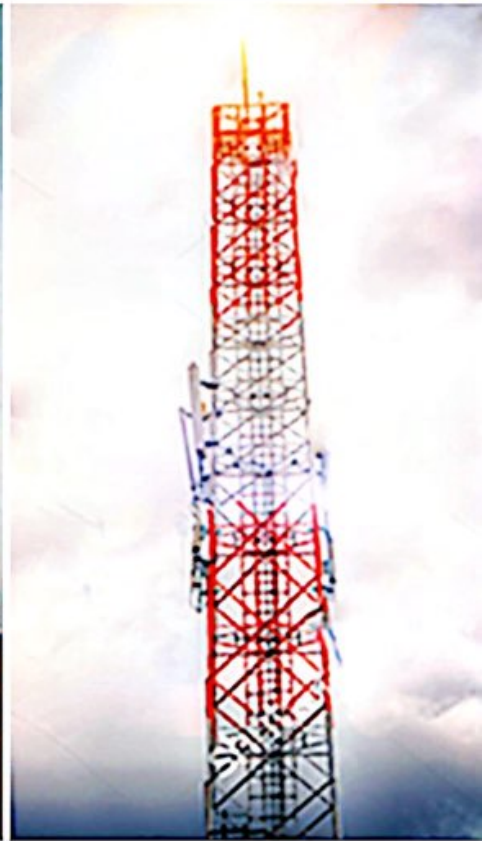


POWER ELECTRONICS

DR. MHMD HAJ-AHMAD
BY: ANOUD AL-HALLAQ



POWERUNIT-JU.COM



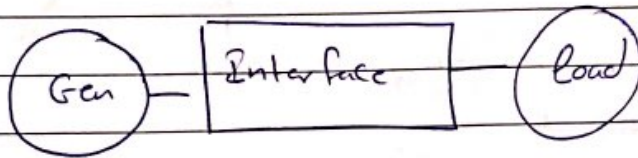
POWER ELECTRONIC

30/11 Tue

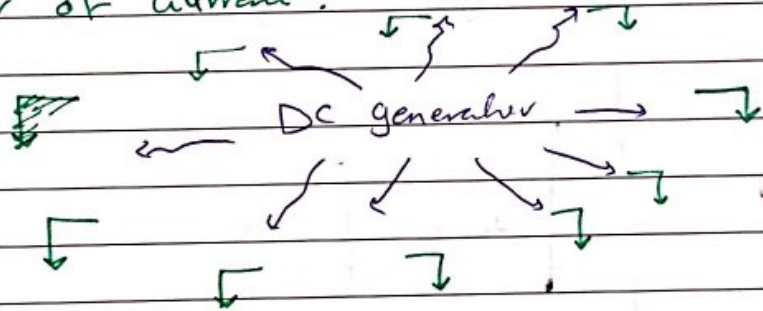
* Power electronics :- is about to convert and monitor electric power from one shape to another.

* 4 - types of conversion :-

- 1- DC to DC conversion
- 2- DC to AC . Inversion
- 3- AC to DC Rectification.
- 4- AC to AC control.



⇒ war of current.



Tesla :-



* Microgrid
→ DC microgrid
→ AC "

* Applications

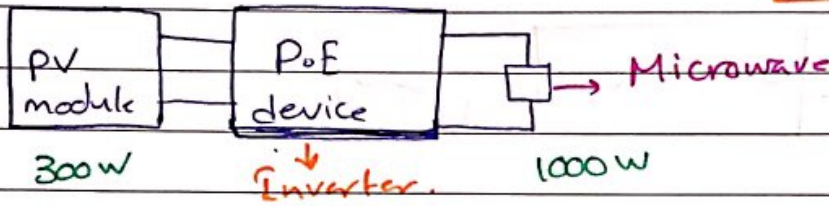
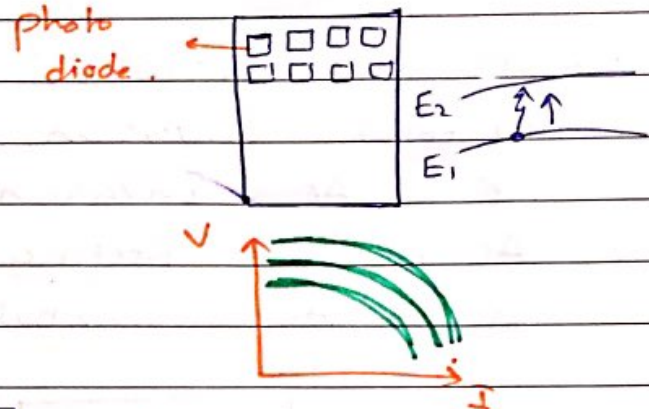
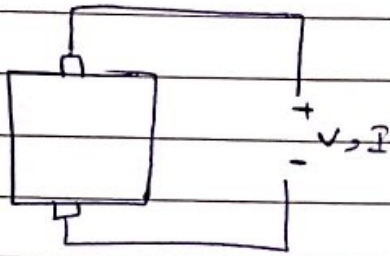
□ Renewables → Solar system
→ wind energy

□

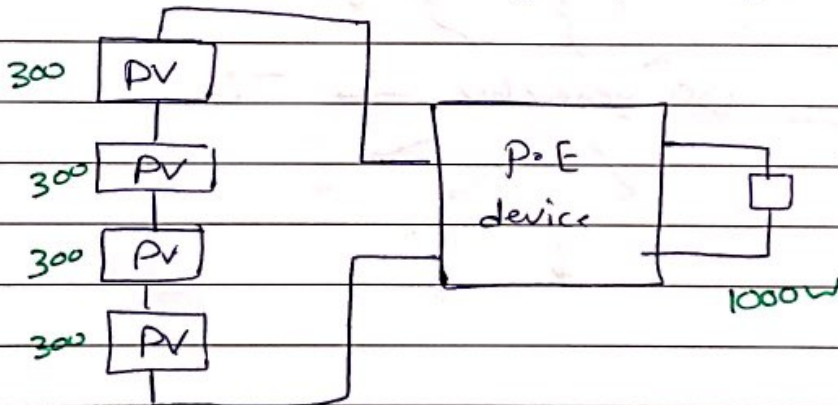
Solar System → PV System
 → CSP System.

⇒ PV System :-

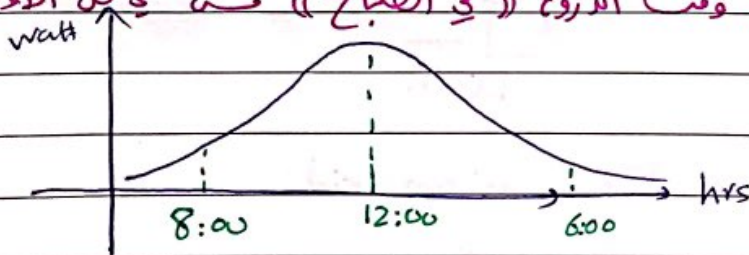
* PV module / 300 W



* في صاير اقاليم الميكرويف ما بيت نقل



* نقل الميكرويف وقت الترويح ((في الصباح)) من في كل الاوقات



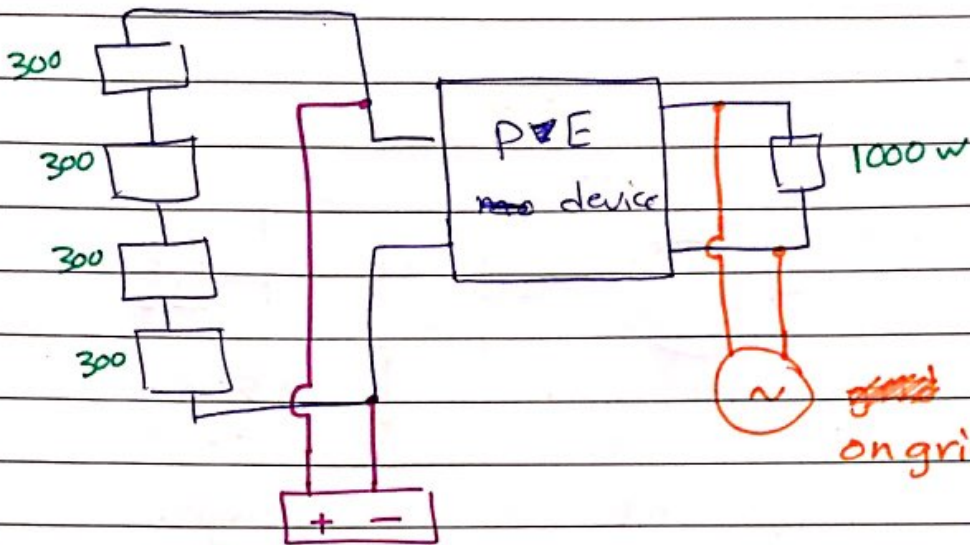
curve = energy

* في صاير اقاليم الميكرويف ما بيت نقل كده لانه ال PV بيحطها بزوايه 45° زيها

* 7 دونم ⇒ 1 Mwatt

* في صاير اقاليم الميكرويف ما بيت نقل كده لانه ال PV بيحطها بزوايه 45° زيها

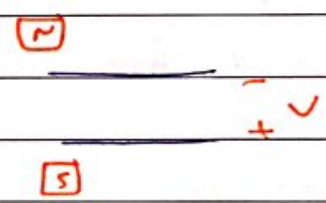
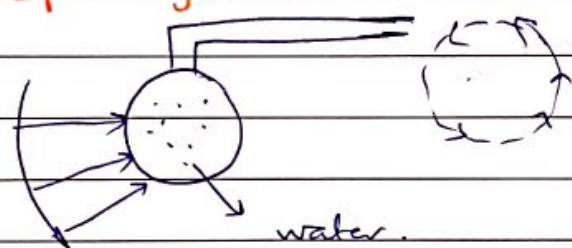
load ← كل الصاير ← اي ايف ongrid ← System.



sol 1 → ١٠/١٥
1 kWh

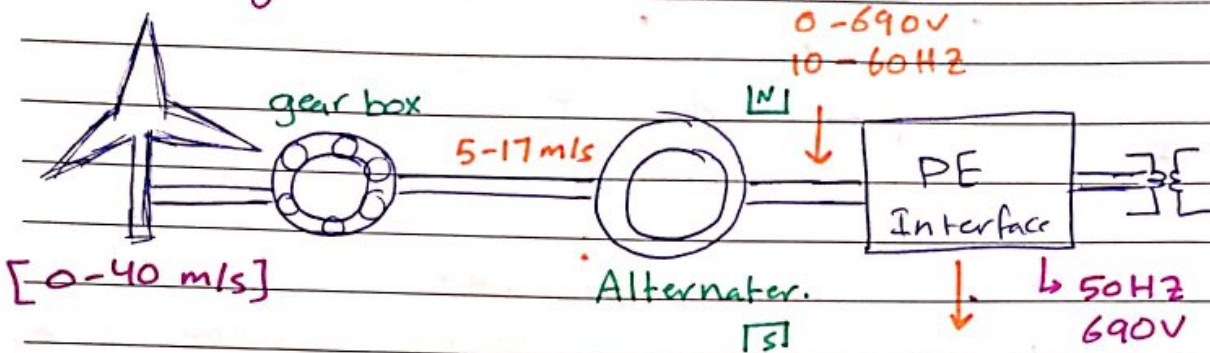
on grid system ← sol 2
ل١ ل٢

* CSP system :-



س١ س٢ س٣ س٤ س٥ س٦ س٧ س٨ س٩ س١٠
س١١ س١٢ س١٣ س١٤ س١٥ س١٦ س١٧ س١٨ س١٩ س٢٠

Wind generators :-



توليد volt الجهد من اليا c الرياح

Alternator :-

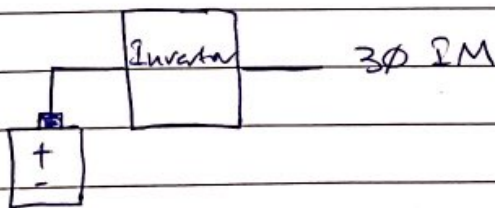
- 1 SG \equiv Synchronous generator.
- 2 IG \equiv Induction generator.
- 3 DFIG \equiv doubly fed Induction generator.
- 4 FCG \equiv full converter gen.

application \Rightarrow

2 Electronic devices.

3 Trans portation :-
(electric cars and trains)

\hookrightarrow 3 ϕ Induction motor.



ex \Rightarrow Tesla cars are 3phase Induction motor

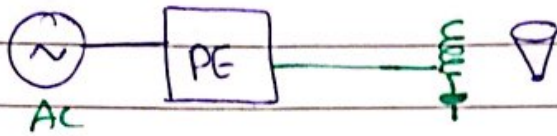
4

4 Efficiency Improvement

* transformer mean there is losses.

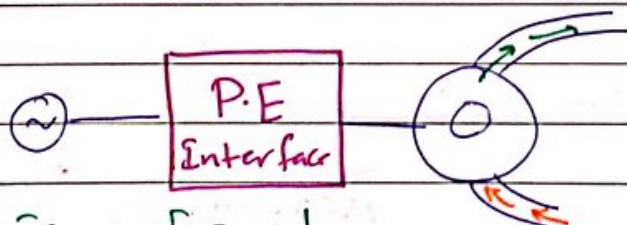
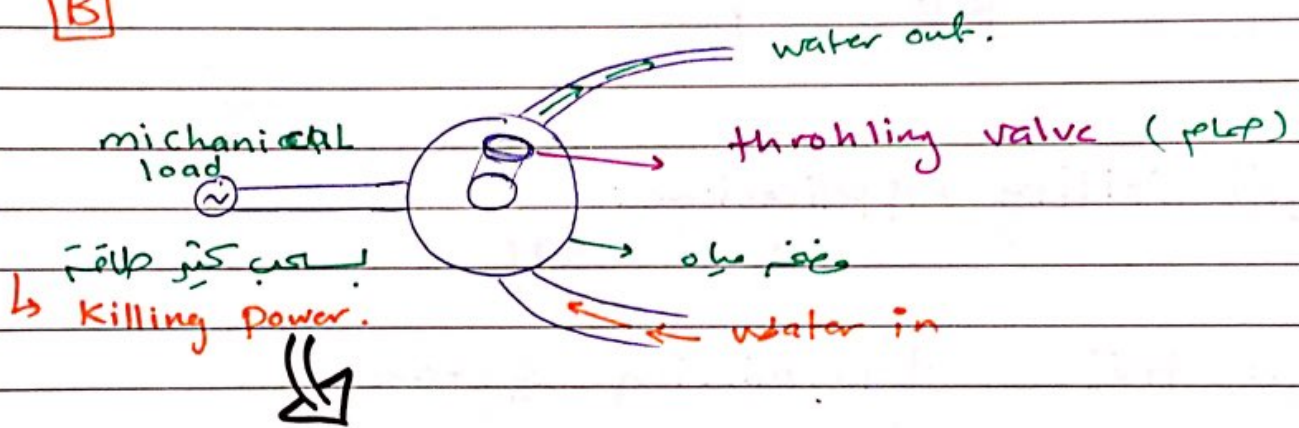
A LED, CFL

CFL = Compact fluorescent.



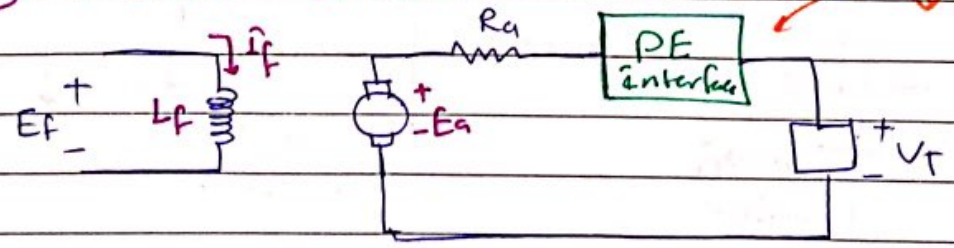
Efficacy "candela/w" better than efficiency.

B



المحرك يتركه يعمل في النظام
 في الارتفاع \uparrow والضغط \uparrow أكثر

5 Motor Drive :-



" $\downarrow \uparrow V_t$: $\uparrow \downarrow$ "

$$I_a = \frac{E_a - V_T}{R_a}$$

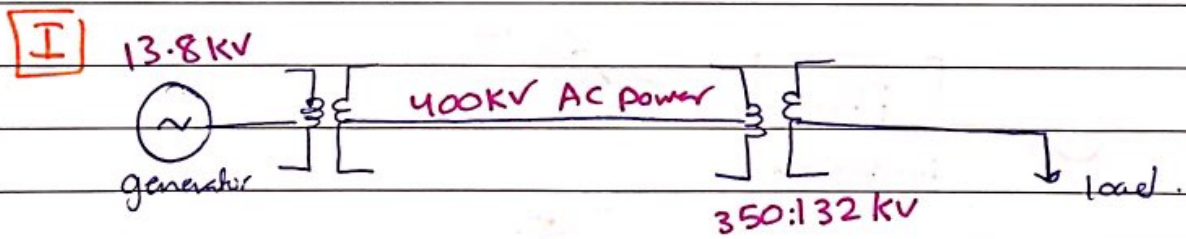
$$E_a = K \phi \omega$$

$$I_a = \frac{K \phi \omega - V_T}{R_a}$$

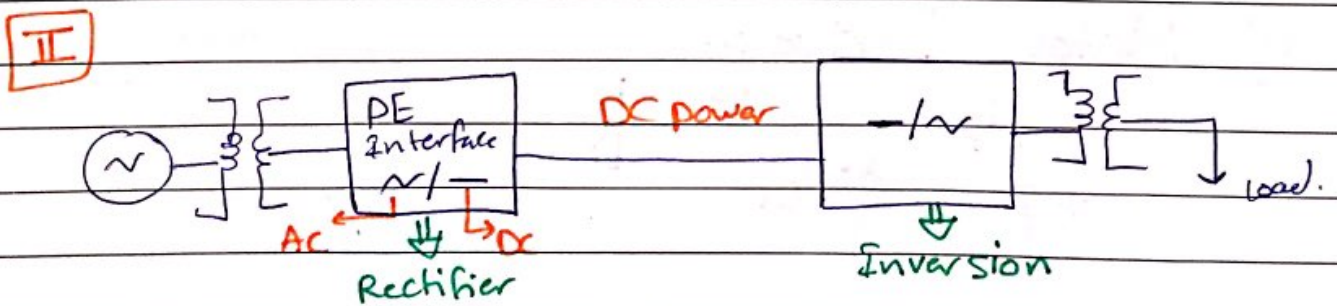
$$\omega = \frac{I_a R_a + V_T}{K \phi}$$

6 Utility Applications:-

A HVDC transmission Systems:-



((سے الی (طرف)) R_{ac} loss in AC is more than in DC



AC no. DC power \Rightarrow effe. \Rightarrow E_b \Rightarrow V_T \Rightarrow V_a \Rightarrow V_L \Rightarrow V_T \Rightarrow V_a \Rightarrow V_L *

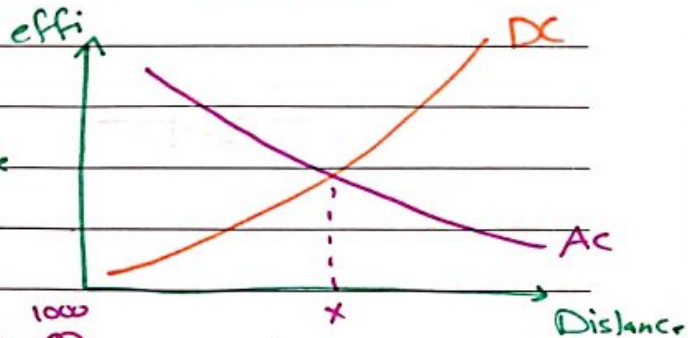
R_{DC} 

$$\delta = \frac{1}{\sqrt{M \sigma T f}}$$

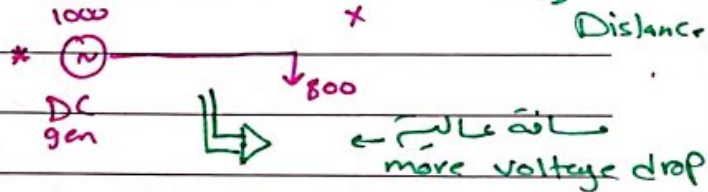
$$R_{AC} > R_{DC}$$

* losses AC \rightarrow losses DC because of skin effect.

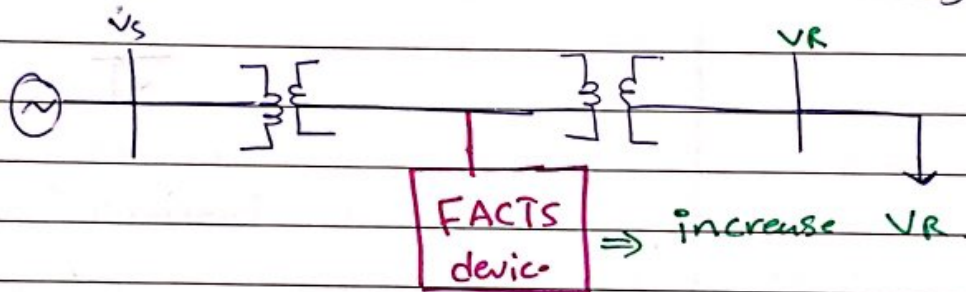
* $f \uparrow \rightarrow$ ~~losses AC~~ \rightarrow ~~losses DC~~



B FACTS :-



FACTS = flexible AC transmission system.



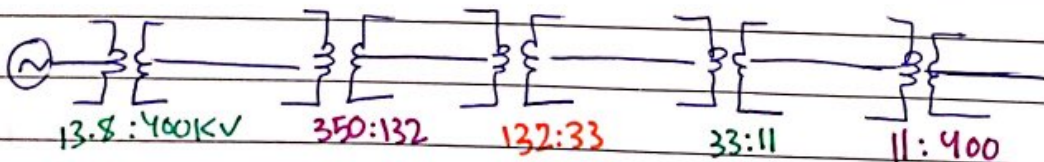
Power bank	\rightarrow	cell phone
3%		80%
3-4%		76%

\Rightarrow Essence of Power electronics \Rightarrow switching transistor, mosfet, diodes

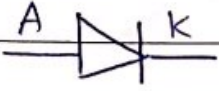
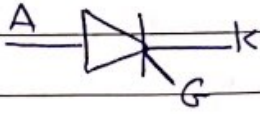



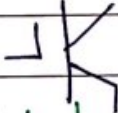
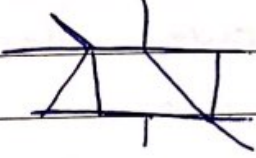
Switching device categorization

\rightarrow Contrallability and Direction.

* AC in Aqaba

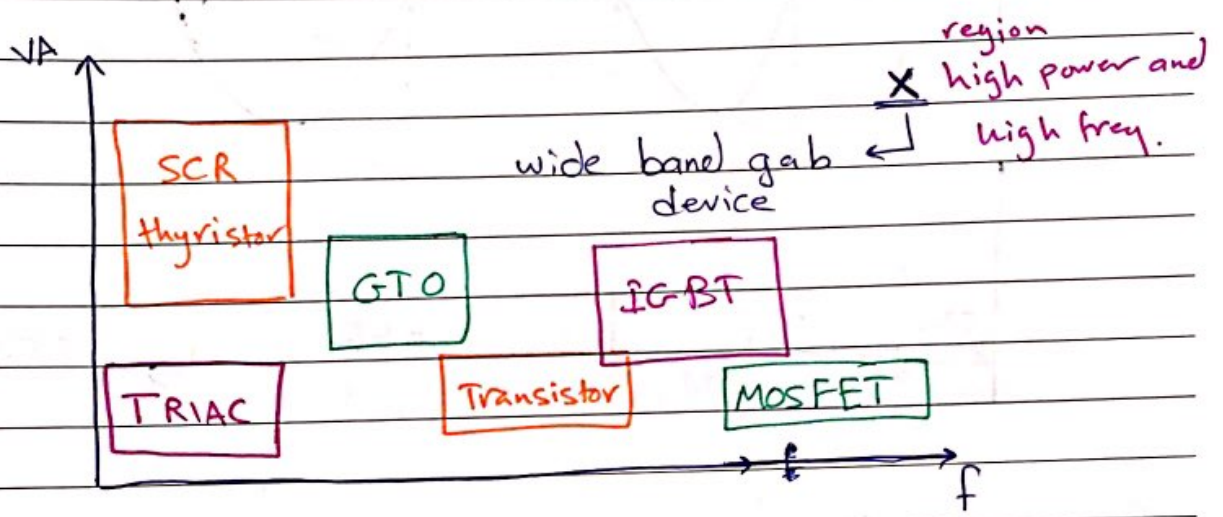


7

	UNcontrollable	Controllable ON	fully controlled
UNI - direction	 <p>diode</p>	 <p>G = gain Thyristor (SCR) OFF ← ON \overline{w} \overline{d} \overline{s}</p>	 <p>transistor.</p>  <p>MOSFET</p>  <p>Gate turn OFF Thyristor (GTO)</p>  <p>Insulated gate Bipolar transistor (IGBT) OFF \overline{w} ON \overline{w} \overline{d} \overline{s}</p>
BI - direction.		 <p>Triac</p>	

Power electronics Switches Categories :-

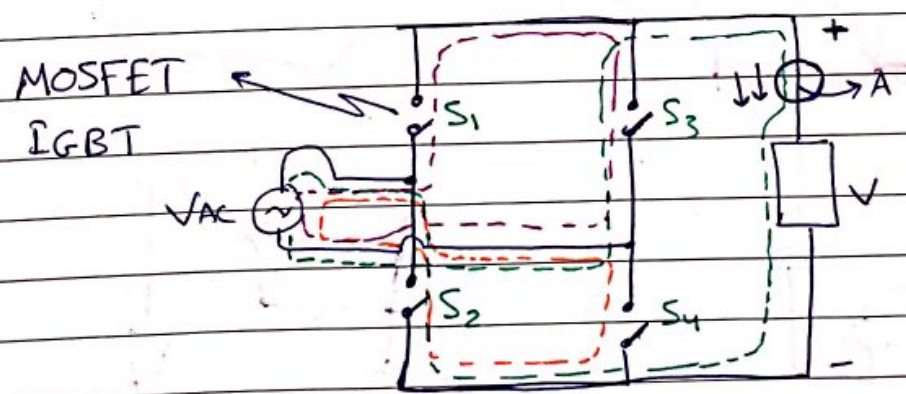
Power and frequency



* SCR thyristor ⇒ Power System في دوائر الـ AC

* في اصول الـ AC و الـ DC بين الـ الجهد والـ تيار

#1 Principle of AC-DC Conversion :- [Rectification]

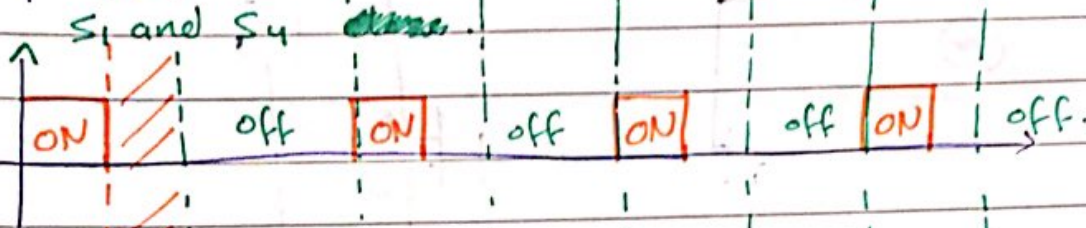
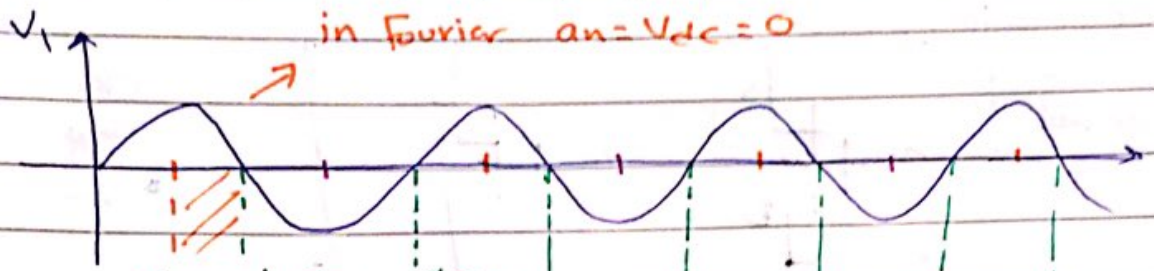


- * S1 and S3 close → S.C
- * S2 and S4 close → S.C
- S3 ON S4 OFF

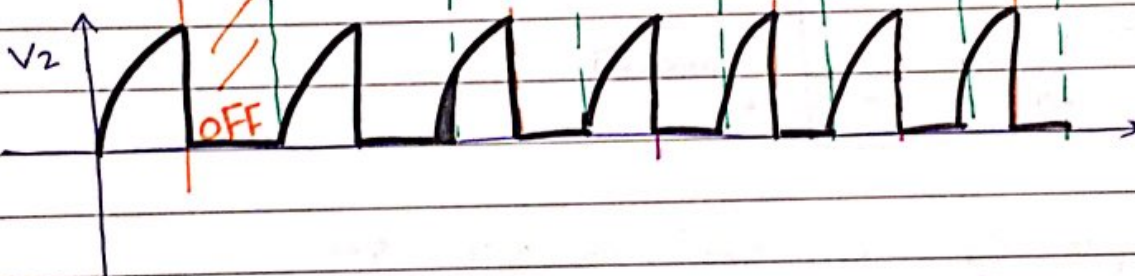
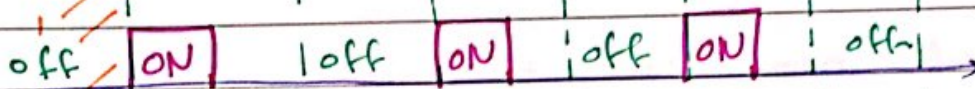
Switching function

$$V_2 = (S_1 - S_3) V_1 = (S_4 - S_2) V_1$$

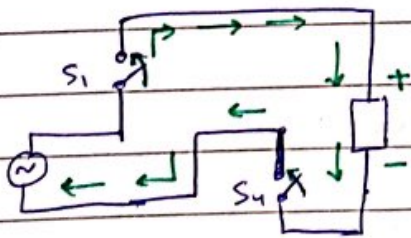
9



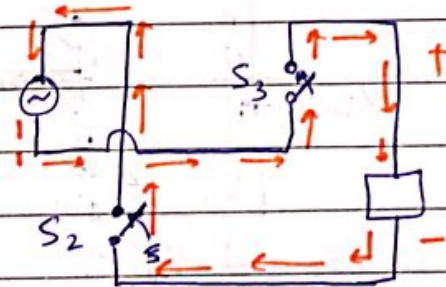
S_2 and S_3 open



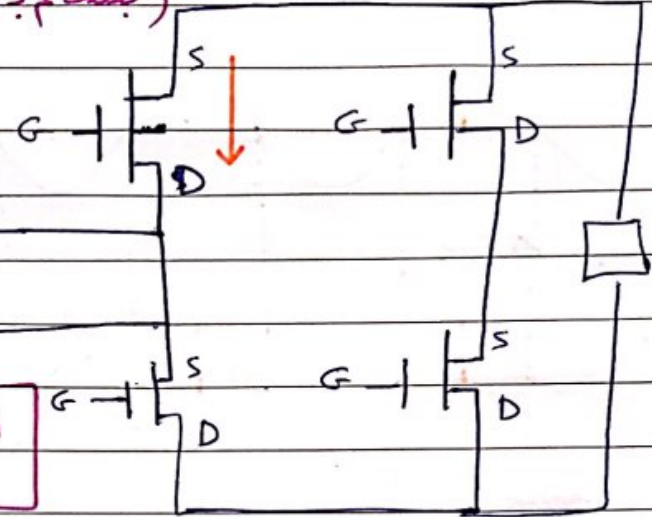
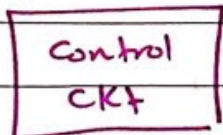
* S_1 and S_4 close.



S_3 and S_2 closed.

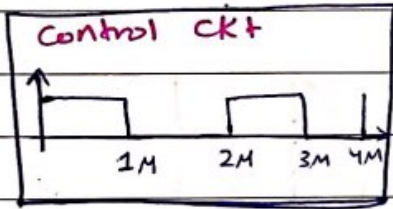


gate drive (switch, f_{drive})



CKT
* V_{dc}
|||

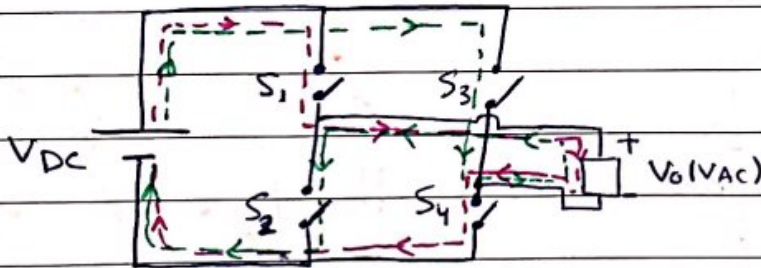
↓ current from source to drain



MOSFET

Principle of DC-AC converter : Δ

[Inverter] using in solar system.



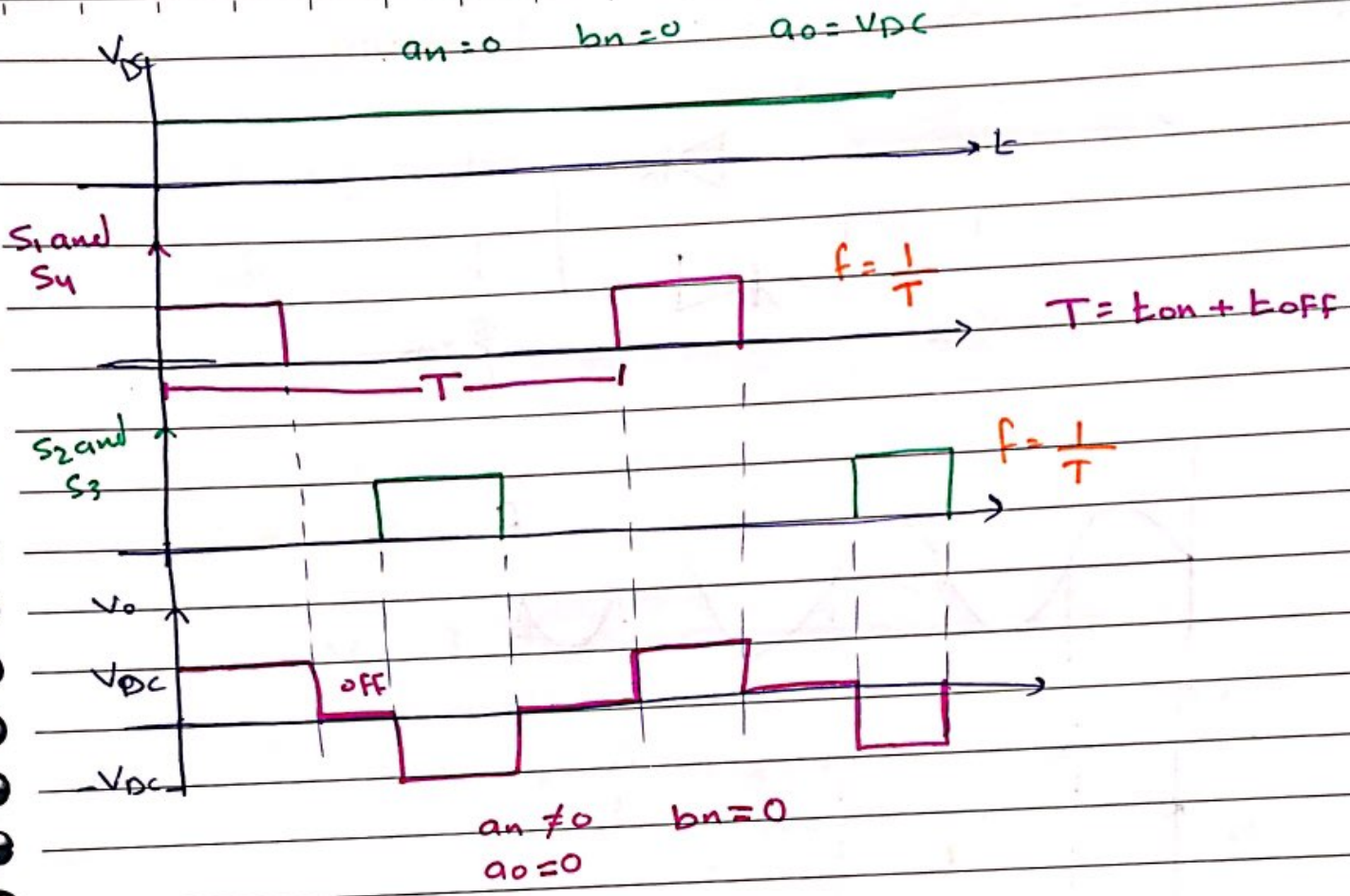
case 1: (S_1 and S_4) ON

$$-V_{DC} + V_o = 0 \Rightarrow V_o = +V_{DC}$$

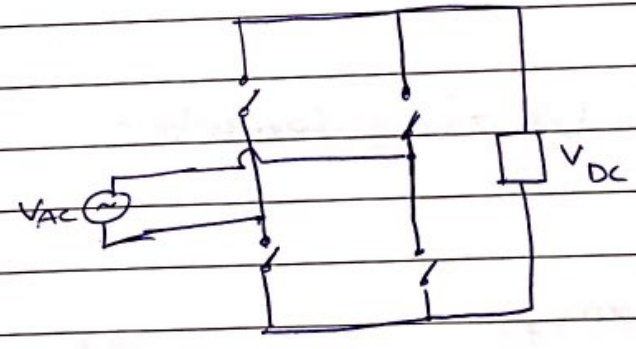
case 2: (S_3 and S_2) ON

$$-V_{DC} + -V_o = 0 \Rightarrow V_o = -V_{DC}$$

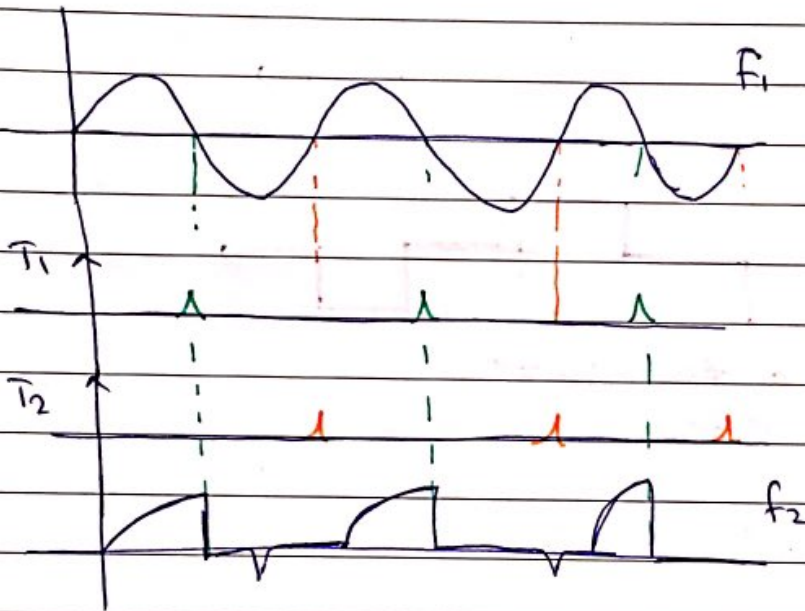
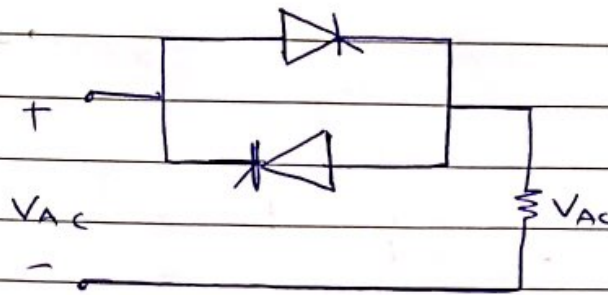




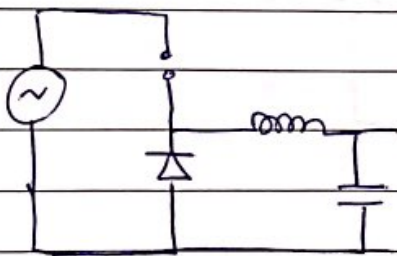
$$V_{AC} = (S_1 - S_2) V_{DC}$$



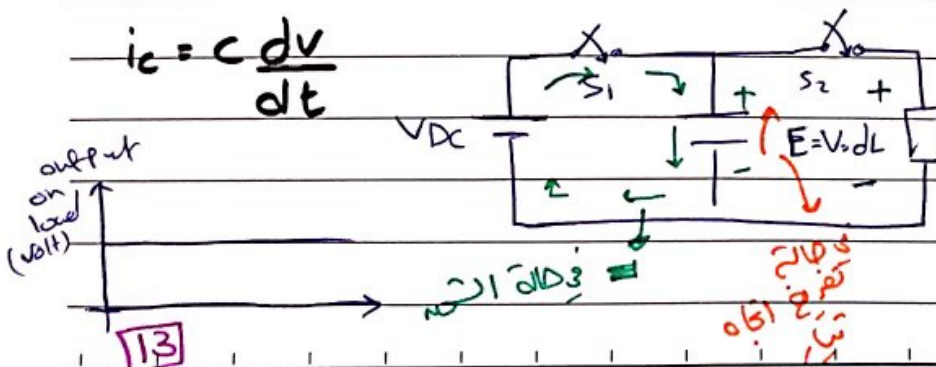
Principle of AC-AC Conversion [Controllers] :-



Principle of DC-DC Converter.



$$i_c = C \frac{dv}{dt}$$



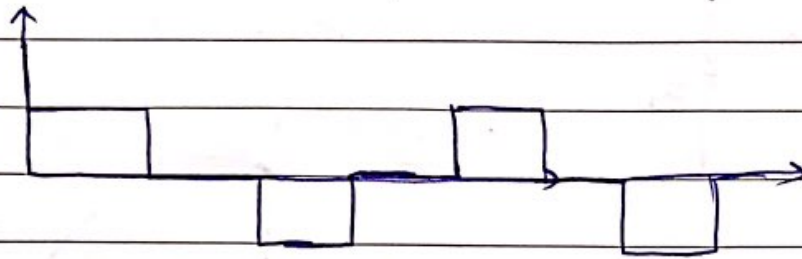
* close $S_1 \rightarrow$ Cap charge.
 \rightarrow open $S_1 \rightarrow$ close S_2
 output on load.

* $\uparrow \Delta V_{cap} \rightarrow$ Jav Voltage Source.

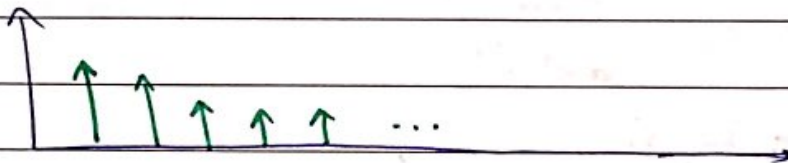
13

* Problem 584

1 Harmonics and ripple :-



full of harmonics



... Filter $b > 1$... not pure ...

2 NO Over load capabilities



Fouriers Series 84

$$v(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos(n\omega t) + b_n \sin(n\omega t)$$

$$a_0 = \frac{2}{T} \int_0^T v(t) dt = \frac{1}{\pi} \int_0^{2\pi} v(\omega t) d\omega t$$

$$a_n = \frac{2}{T} \int_0^T v(t) \cos(n\omega t) dt$$

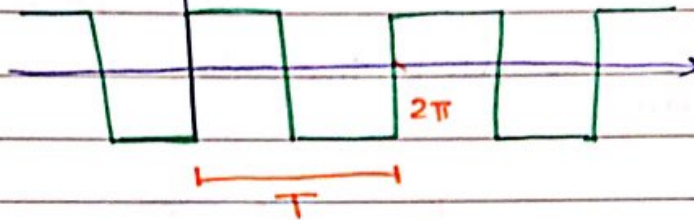
$$= \frac{1}{\pi} \int_0^{2\pi} v(\omega t) \cos(n\omega t) d\omega t$$

$$b_n = \frac{2}{T} \int_0^T v(t) \sin(n\omega t) dt = \frac{1}{\pi} \int_0^{2\pi} v(\omega t) \sin(n\omega t) d\omega t$$

Ex Find the 1st and 3rd Harmonic For

Rest of harmonic

! low AC signal



$$\Rightarrow a_0 = \frac{1}{\pi} \int_0^{2\pi} v(\omega t) d\omega t$$

$$a_0 = \frac{1}{\pi} \left[\int_0^{\pi} 1 d\omega t + \int_{\pi}^{2\pi} -1 d\omega t \right]$$

$$= 0$$

pure DC signal

$$\Rightarrow a_n = \frac{1}{\pi} \int_0^{2\pi} v(\omega t) \cos(n\omega t) d\omega t$$

$a_n = 0 \rightarrow$ odd signal

$$= \frac{1}{\pi} \int_0^{\pi} \cos n\omega t d\omega t + \frac{1}{\pi} \int_{\pi}^{2\pi} -\cos n\omega t d\omega t$$

$$= \frac{1}{n\pi} \left[\sin n\omega t \right]_0^{\pi} - \frac{1}{n\pi} \left[\sin n\omega t \right]_{\pi}^{2\pi} = 0$$

$$b_n = \frac{1}{\pi} \int_0^{\pi} \sin n\omega t d\omega t + \frac{1}{\pi} \int_{\pi}^{2\pi} -\sin n\omega t d\omega t$$

$$= -\frac{1}{\pi n} \left[\cos(n\omega t) \right]_0^{\pi} + \frac{1}{\pi n} \left[\cos(n\omega t) \right]_{\pi}^{2\pi}$$

$$b_n = \frac{2}{n\pi} - \frac{2}{n\pi} \cos n\pi$$

First harmonic $n=1 \Rightarrow b_1 = \frac{4}{\pi} \Rightarrow$ Fundamental.

$$v(t) = \sum_{n=1}^{\infty} \left(\frac{2}{n\pi} - \frac{2}{n\pi} \cos n\pi \right) \sin n\omega t$$

2nd harmonic $n=2 \Rightarrow b_2 = 0$

3rd " $n=3 \Rightarrow b_3 = \frac{4}{3\pi}$

$$b_4 = 0$$

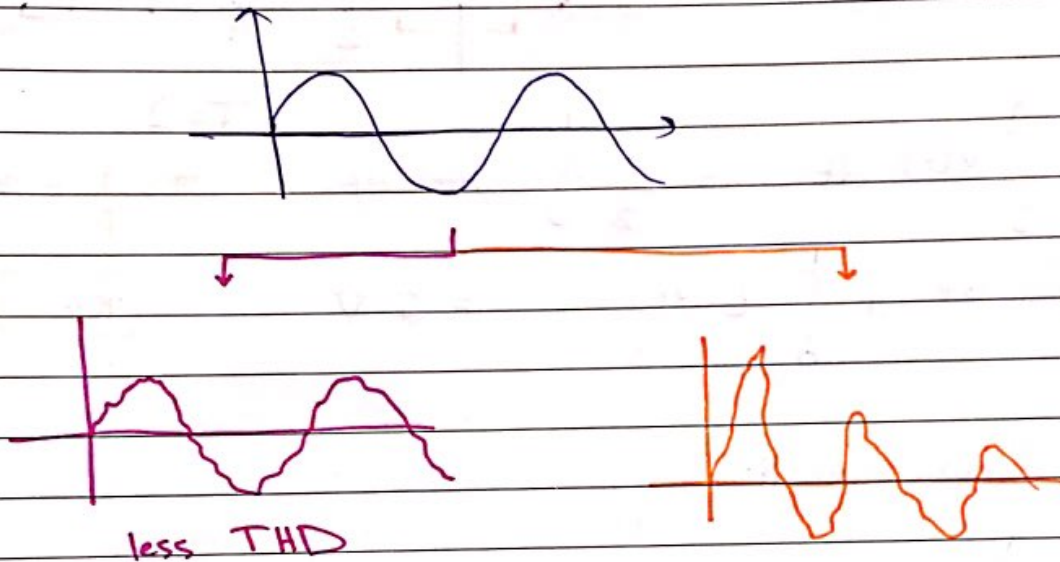
$$b_5 = \frac{4}{5\pi}$$

Energy Power لا تتغير في 1st har

harmonic

* Total Harmonic Distortion :-

THD: is a measure of the closeness in shape between a waveform and its fundamental component :-



$$\text{THD}_I = \frac{\sqrt{\sum_{n=2}^{\infty} I_n^2}}{|I_1|}$$

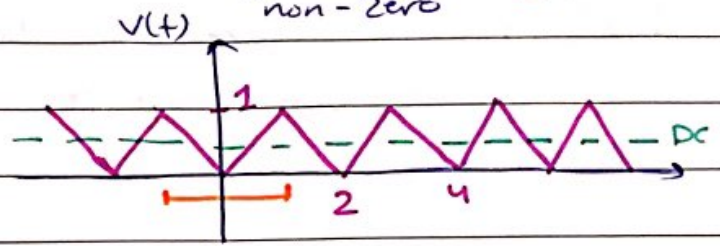
$$\text{THD}_V = \frac{\sqrt{\sum_{n=2}^{\infty} V_n^2}}{|V_1|}$$

For DC-signal: $\frac{a_0}{2} \rightarrow$ value of intercept

$\rightarrow a_n, b_n = 0$

Ex Find the total Harmonic distortion for the signal [consider the first 5 Harmonic]!?

$$v(t) = \begin{cases} -t & -1 < t < 0 \\ t & 0 < t < 1 \end{cases}$$



Sol:-

$$\begin{aligned} \Rightarrow a_0 &= \frac{2}{T} \int_0^T v(t) dt = \frac{2}{2} \int_{-1}^1 v(t) dt & T=2 \\ &= \int_{-1}^0 -t dt + \int_0^1 t dt = 1 \text{ V} & T = \frac{1}{f} = \frac{2\pi}{\omega} \\ & & \boxed{\pi = \omega} \end{aligned}$$

$\Rightarrow b_n = 0$ [even function]

$$\begin{aligned} \Rightarrow a_n &= \frac{2}{T} \int_0^T v(t) \cos(n\omega t) dt \\ &= \frac{2}{T} \int_{-1}^1 v(t) \cos(n\omega t) dt \\ &= 2 \int_0^1 v(t) \cos(n\omega t) dt \end{aligned}$$

$$\begin{aligned} u &= t & du &= \cos n\omega t dt \\ du &= dt & v &= \frac{1}{n\omega} \sin n\omega t \end{aligned}$$

$$= 2 \left(\left[\frac{t \sin n\omega t}{n\omega} \right]_0^1 - \int_0^1 \frac{1}{n\omega} \sin n\omega t dt \right)$$

$$= \frac{2}{n^2 \omega^2} \left[\cos n\omega t \right]_0^1 = \frac{2}{n^2 \pi^2} [\cos n\pi - 1]$$

$$a_n = \begin{cases} 0 & n \text{ is even} \\ \frac{-4}{n^2 \pi^2} & n \text{ is odd} \end{cases}$$

Fundamental at $n=1 \rightarrow \frac{-4}{\pi^2}$

$n=2, n=4, n=6, n=8, \dots = 0$

3rd $n=3 \rightarrow a_3 = \frac{-4}{9\pi^2}$

$n=5 \rightarrow a_5 = \frac{-4}{25\pi^2}$

$n=7 \rightarrow a_7 = \frac{-4}{49\pi^2}$

$n=9 \rightarrow a_9 = \frac{-4}{81\pi^2}$

$$\text{THD} = \frac{\sqrt{\sum_{n=2}^{\infty} v_n^2}}{|V_1|}$$

$$\text{THD} = \frac{\sqrt{\left(\frac{4}{9\pi^2}\right)^2 + \left(\frac{4}{25\pi^2}\right)^2 + \left(\frac{4}{49\pi^2}\right)^2 + \left(\frac{4}{81\pi^2}\right)^2}}{4/\pi^2} = 12\%$$

if $b_n = \frac{2\pi}{3n} \Rightarrow c_n = \sqrt{a_n^2 + b_n^2}$

skip

$$\text{THD} = \frac{\sqrt{c_3^2 + c_5^2 + c_7^2}}{c_1^2}$$

DC-DC Converters

- PV system
- Switched mode regulated DC power supplies
- Electric / Hybrid / ~~EV~~ ~~VE~~ Vehicles

Non-Isolated.

Isolated

→ Buck [steps down]

→ Fly back

→ Boost [steps up]

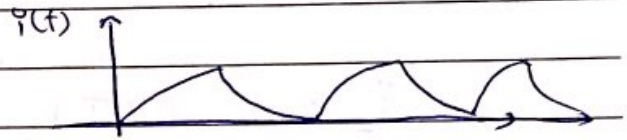
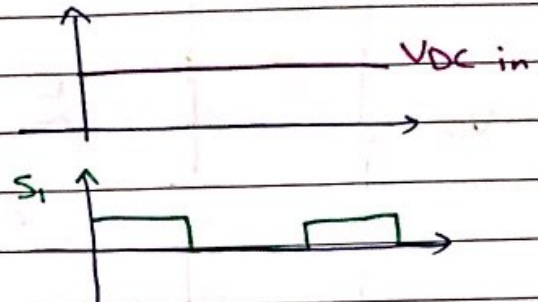
→ Forward

→ Buck/Boost [up/down]

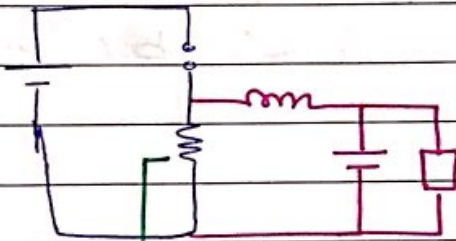
→ full and half bridge.

* Origin of Buck Converter:-

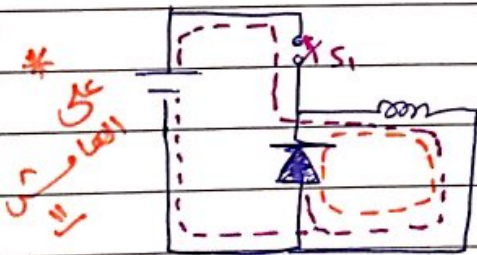
First stage:-



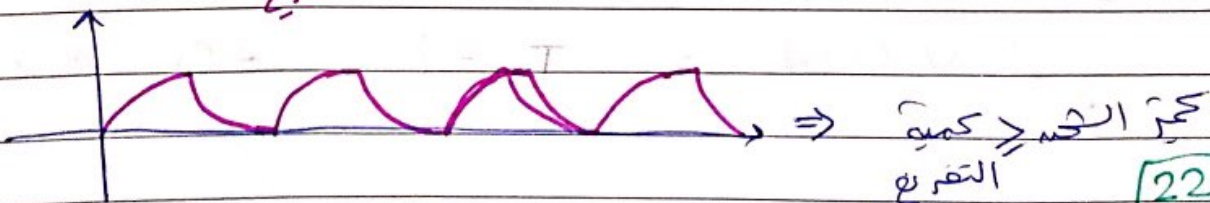
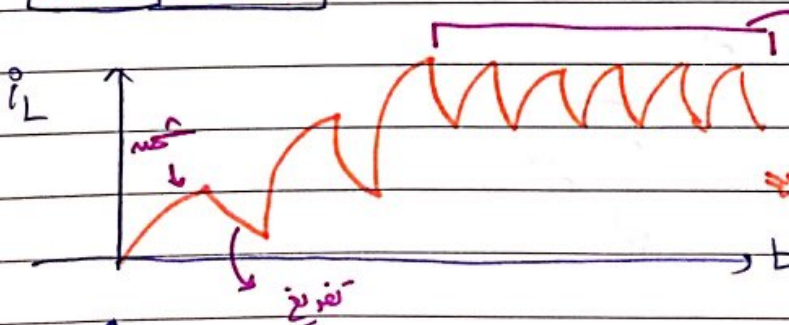
Next stage:-



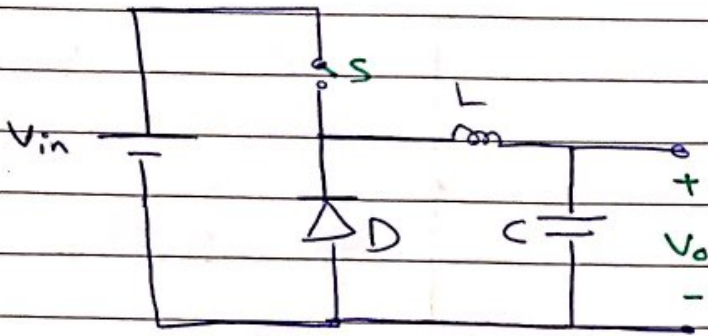
→ Kill s the efficiency.



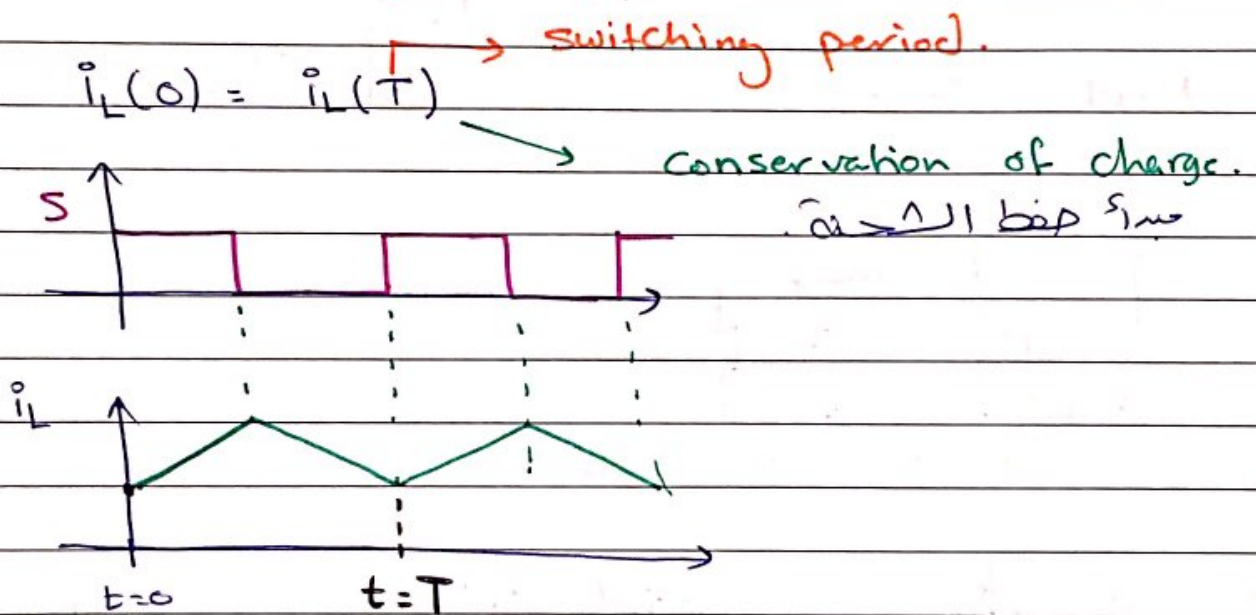
switch ON
S1 OFF



Final version of Buck converter :-



* In steady state the average voltage across the inductor is zero !!

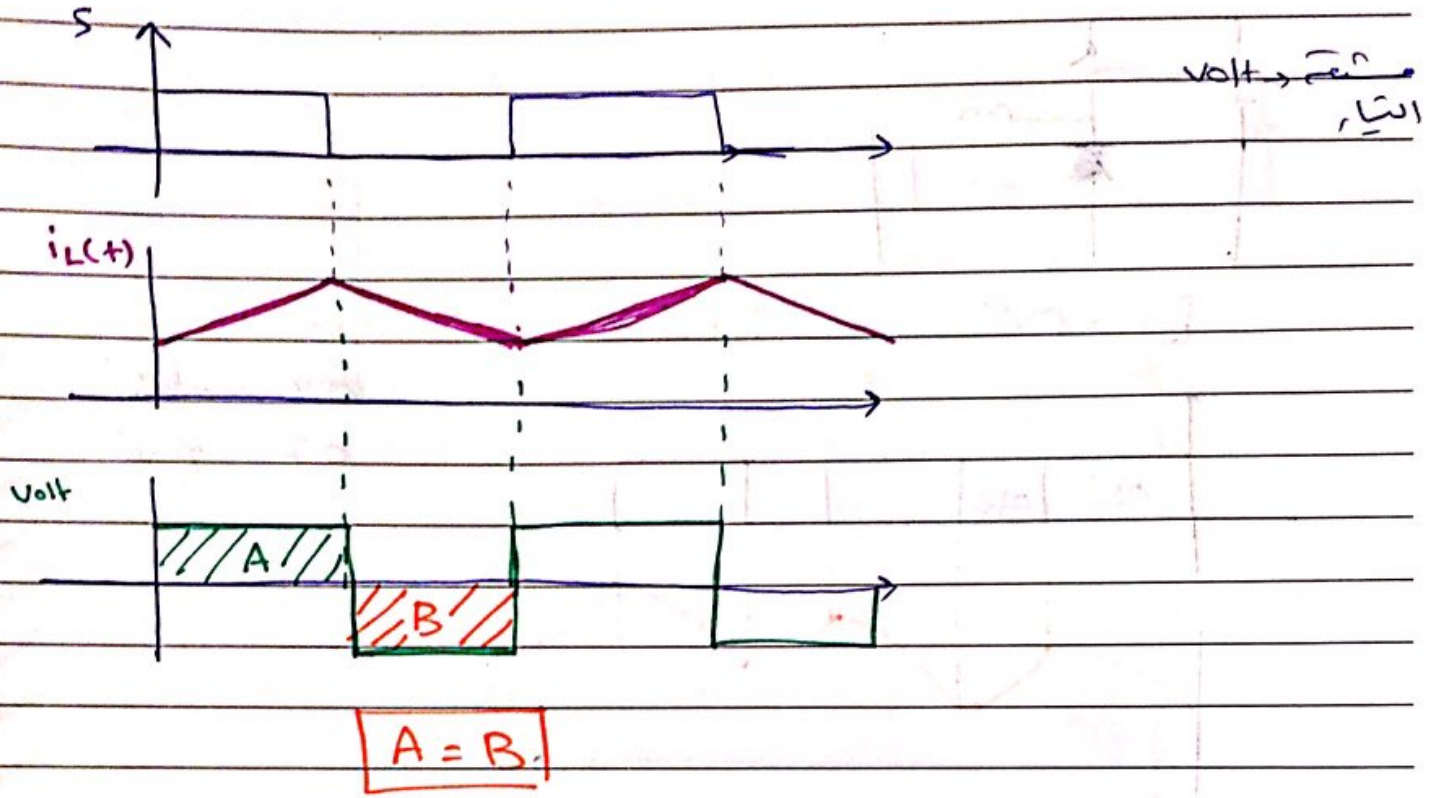


$$V_L(t) = L \frac{di(t)}{dt}$$

$$\frac{1}{L} V_L(t) dt = di$$

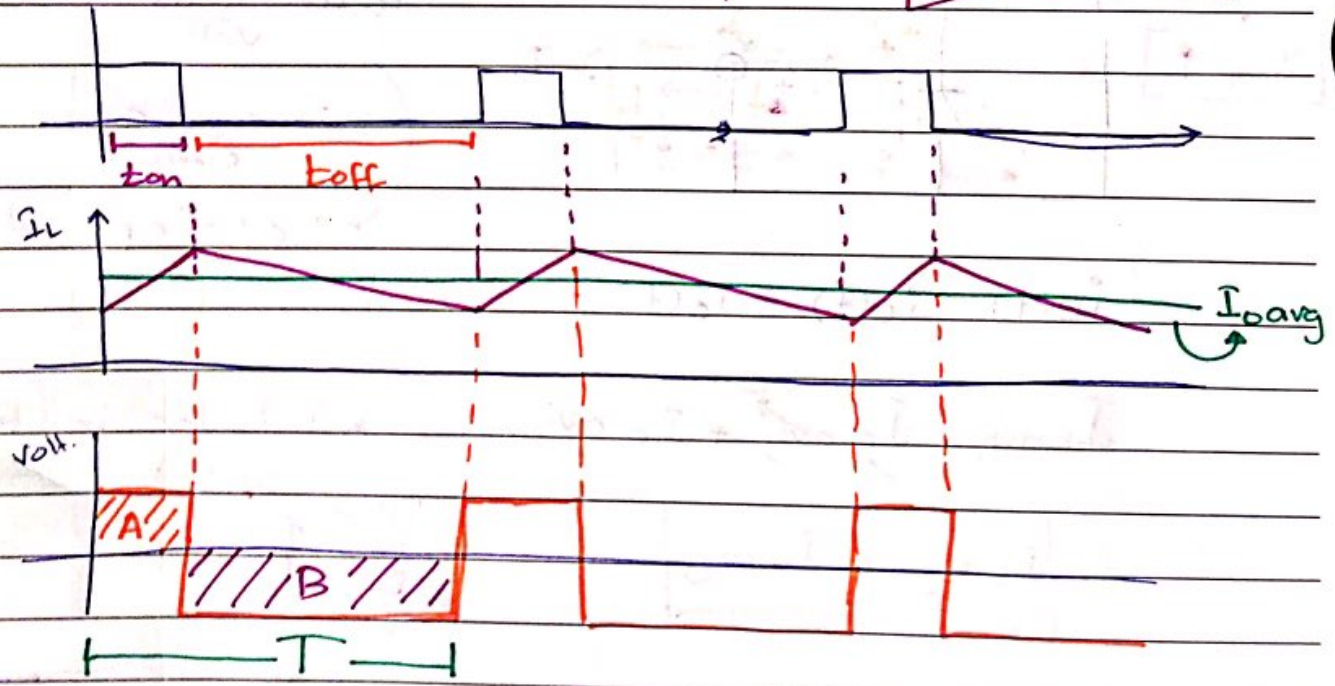
$$\int_0^T \frac{1}{L} V_L(t) dt = \int_{i(0)}^{i(T)} di$$

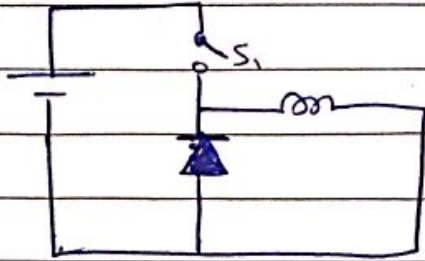
$$\int_0^T \frac{1}{L} V_L(t) dt = i(T) - i(0) = 0 \quad (\text{average = volt})$$



$T = t_{on} + t_{off}$

$D \triangleq$ Duty cycle $= \frac{t_{on}}{T}$ $0 \leq D \leq 1$



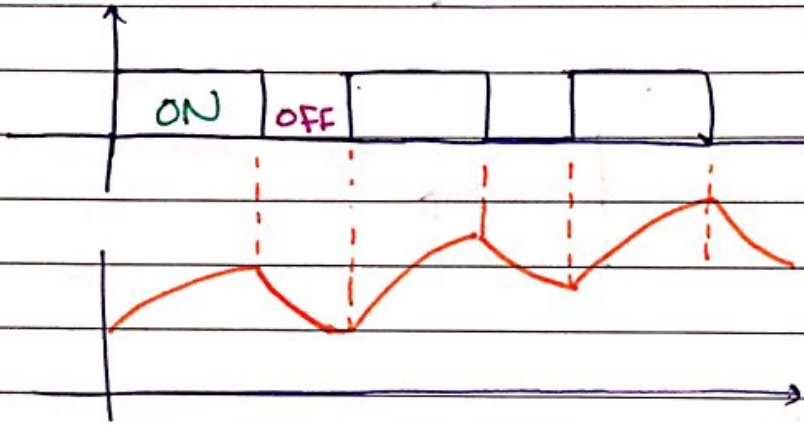


$$D = 0.8$$

$$T = 1s$$

$$0.8 = \text{مُدَّة}$$

$$0.2 = \text{زمن قف}$$

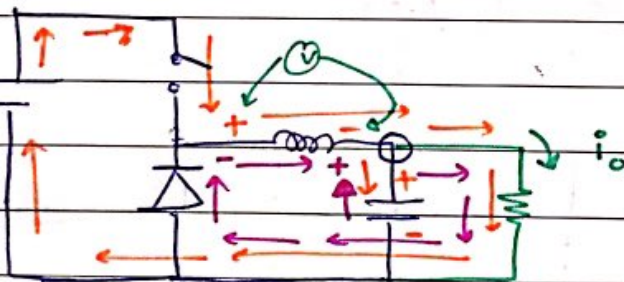


if $D=0.2 \rightarrow$ يعني قفي وبتفرغ كبر

ON state.

OFF state

$I_{cap} \uparrow$



\rightarrow average inductor = 0 volt

\rightarrow average capacitor = 0 current

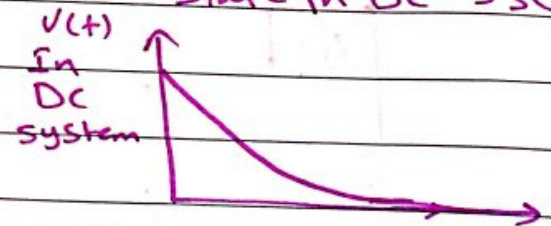
over a period.

$$i_L(t) = i_c(t) + i_o(t)$$

$$I_{L \text{ avg}} = I_{c \text{ avg}} + I_{o \text{ avg}}$$

$$I_{L \text{ avg}} = I_{o \text{ avg}}$$

* Inductor in Steady State in DC \rightarrow short



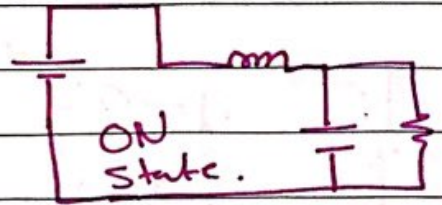
Switch ON \rightarrow OFF \Rightarrow Inductor \Rightarrow Top to go to steady state \rightarrow

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ON state :-

$$V_{in}(t) = V_L(t) + V_o(t)$$

$$-V_{in}(t) + V_L(t) + V_o(t) = 0$$



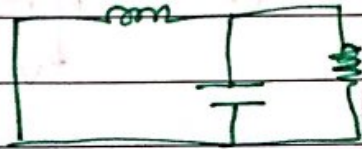
OFF state :-

* diode short ckt.

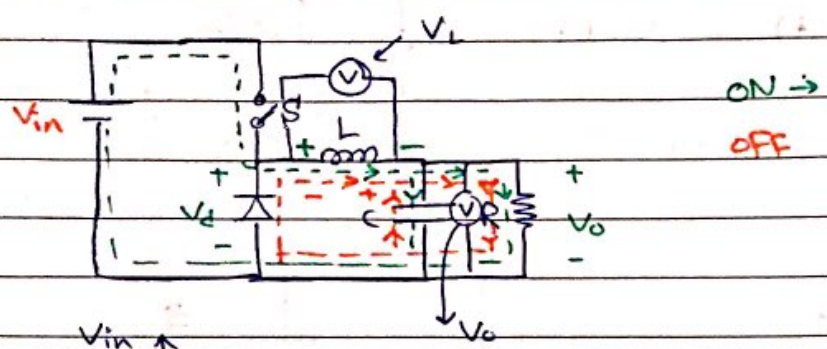
$$-V_L(t) = V_o(t)$$

$$V_L(t) + V_o(t) = 0$$

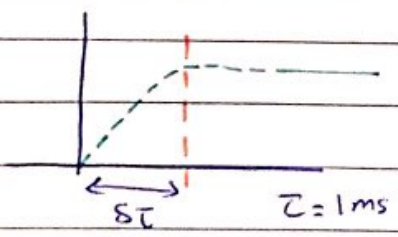
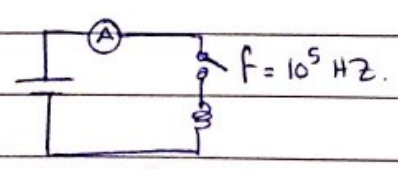
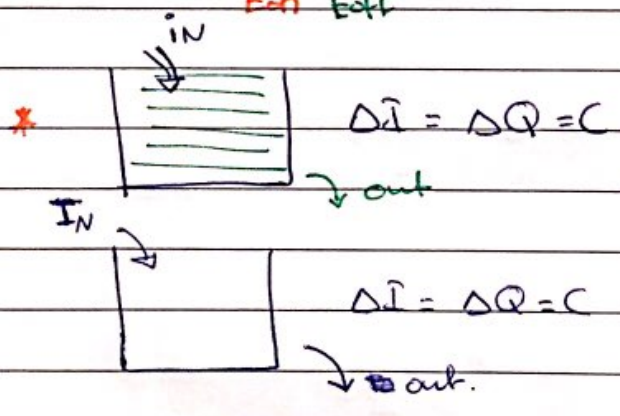
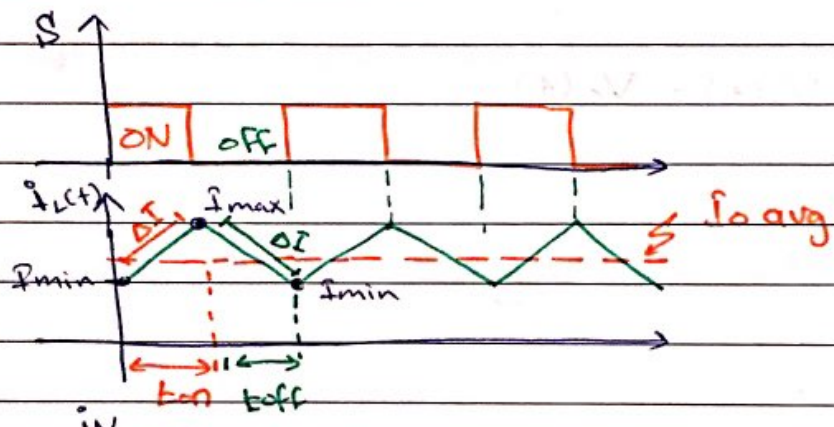
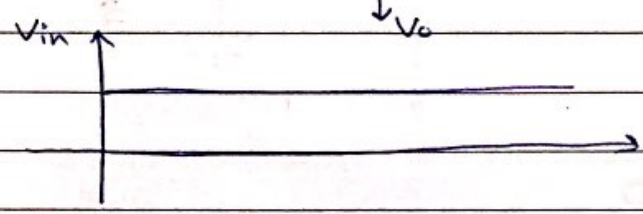
$$-V_L(t) = V_o(t) = V_c(t)$$



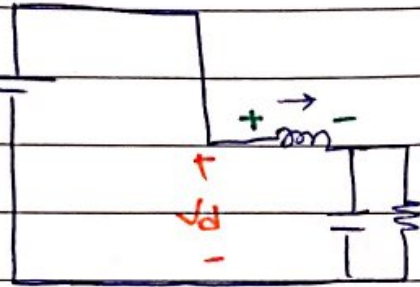
BUCK Converter



ON →
OFF

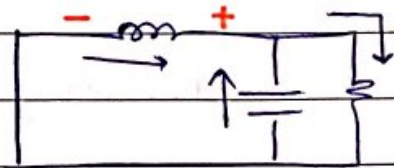


ON :-



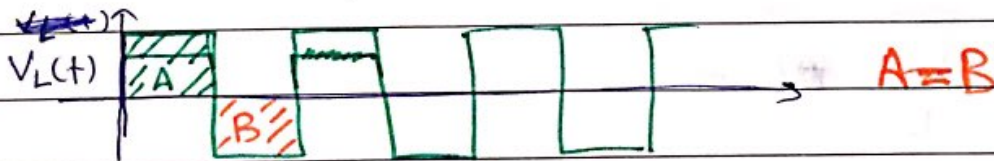
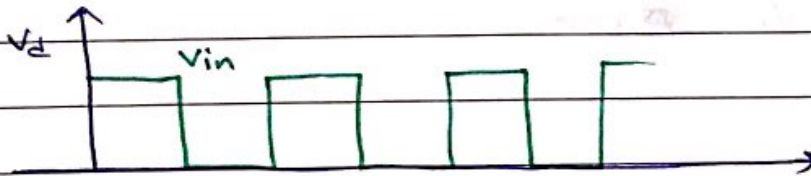
$$i_L(t) = i_C(t) + i_R(t)$$

OFF :-



change its direction $\Rightarrow (i_C(t))$

$$i_L(t) = i_C(t) + i_R(t)$$



IN ~~Steady~~ Steady State :-

$$I_{L avg} = I_o avg$$

S is ON :-

$$-V_{in} + V_L + V_o = 0$$

$$V_L = L \frac{di}{dt} = V_{in} - V_o \quad \dots \textcircled{1}$$

$$L \Delta \bar{I}_1 = V_{in} - V_o \quad \dots \textcircled{1}$$

t_{ON}

S is OFF

$$V_L = -V_o$$

$$|V_L| = |V_o|$$

V_L is $-V_o$ because the inductor changes polarity.

$$V_o = -V_L = -L \frac{\Delta \bar{I}_2}{t_{OFF}} \quad \dots \textcircled{2}$$

$$\Delta \bar{I}_2 = -\Delta \bar{I}_1$$

from (1) :-

$$\Delta \bar{I}_1 = \frac{V_{in} - V_o}{L} t_{ON}$$

from (2) :-

$$\Delta \bar{I}_1 = \frac{V_o}{L} t_{OFF}$$

$$\frac{V_{in} - V_o}{L} t_{ON} = \frac{V_o}{L} t_{OFF}$$

$$V_{in} t_{ON} - V_o t_{ON} = V_o t_{OFF}$$

$$V_{in} t_{ON} = V_o (t_{ON} + t_{OFF})$$

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$$T = t_{on} + t_{off}$$

$$D = \frac{t_{on}}{T}$$

duty cycle.

$$0 \leq D \leq 1$$

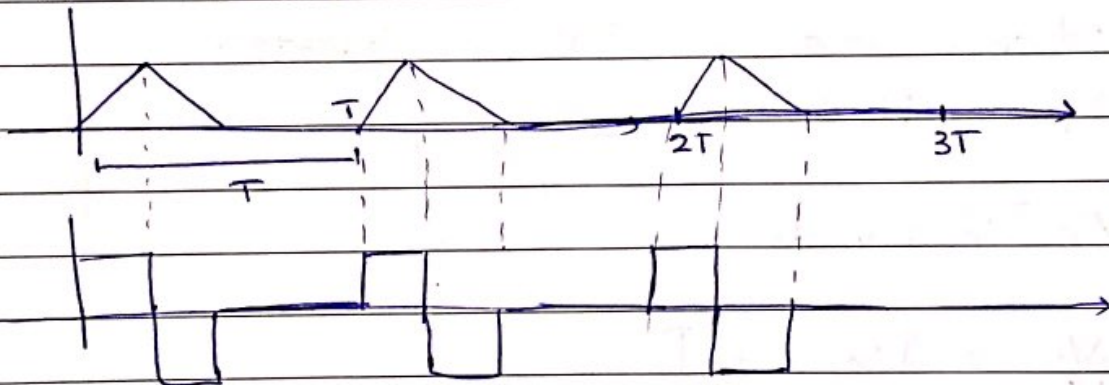
$$V_{in} t_{on} = V_o T$$



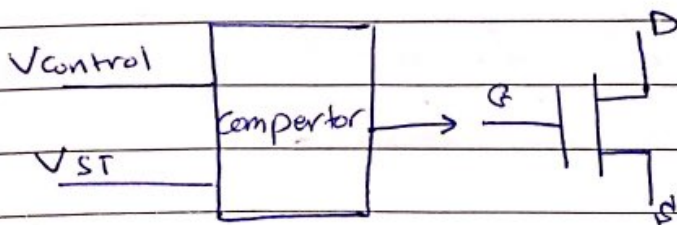
$$V_o = V_{in} \frac{t_{on}}{T}$$

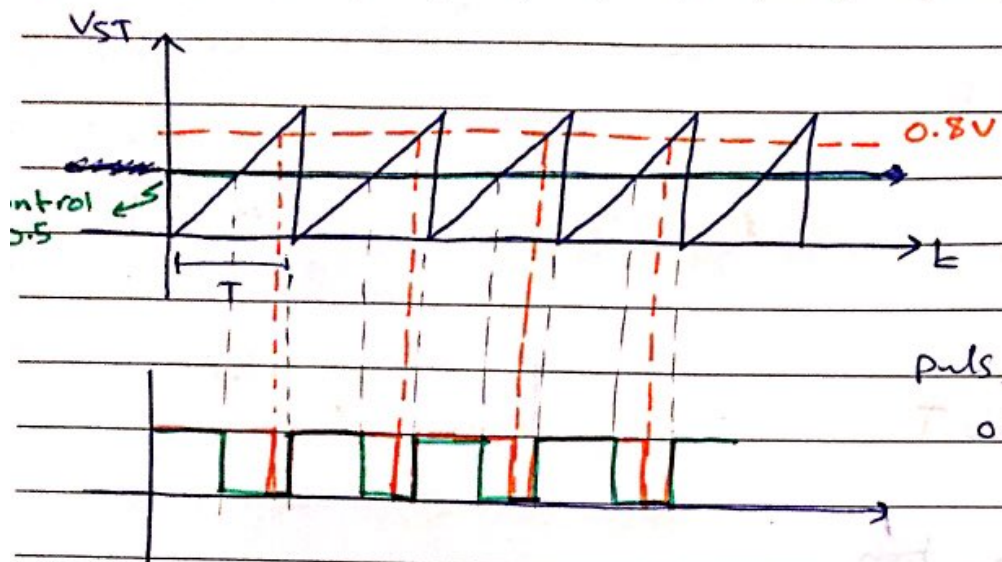
$$V_o = D V_{in}$$

average output voltage.



* How to realize duty cycle control of Switch [PWM]





puls width 0.8 = Vcont

0.5V
1 bit
0.5 model
0 bit

$$V_{control} > V_{st} \Rightarrow \text{Comp at } = 1$$

$$V_{control} < V_{st} \Rightarrow \text{Comp at } = 0$$

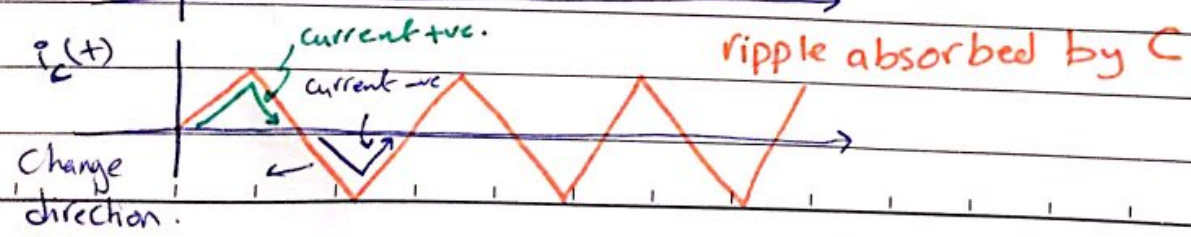
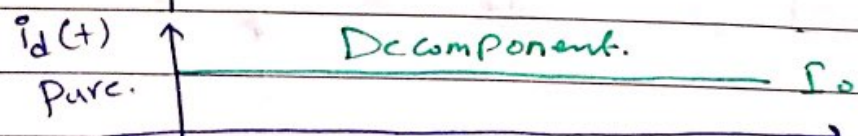
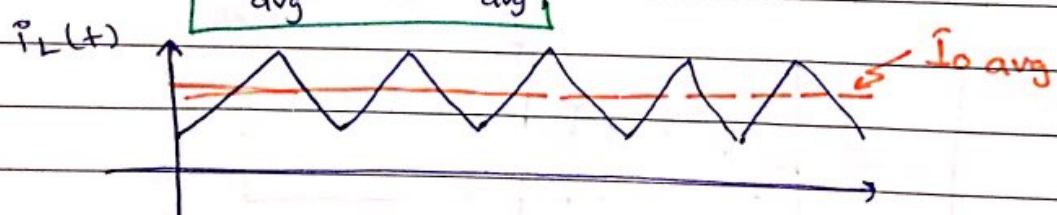
Considering lossless DC-DC Converter.

$$P_{in} = P_{out}$$

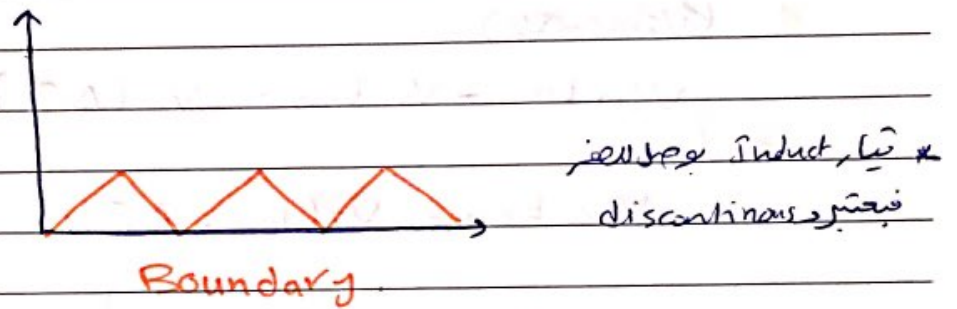
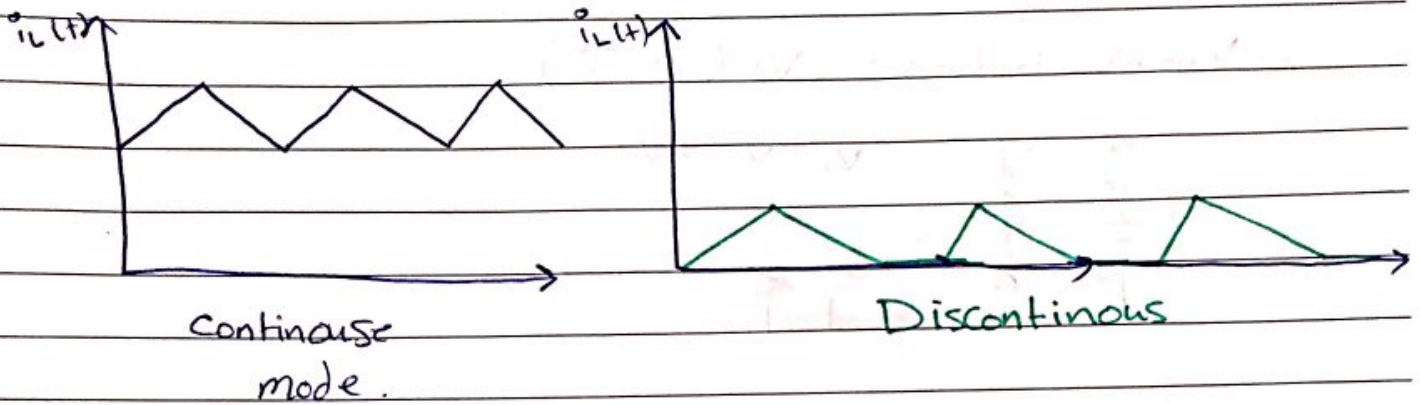
$$V_{in} I_{in} = V_o I_o$$

$$\frac{V_o}{V_{in}} = \frac{I_{in}}{I_o} = D$$

$$I_{in, avg} = D I_{o, avg}$$



2 mode of operation for a ~~DC~~ DC/DC Buck Converter.

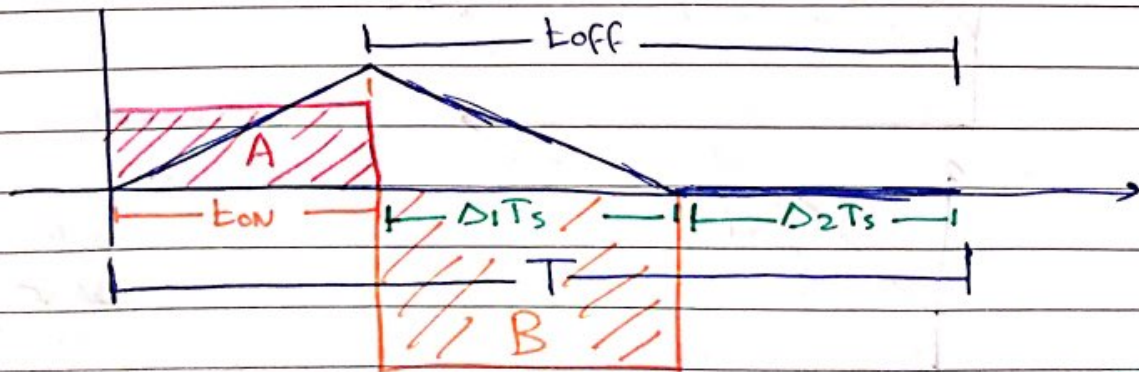


* Continuous mode $\Rightarrow \frac{L}{R} = \tau \gg T$

$V_o = D V_{in} = \frac{t_{on}}{t_{on} + t_{off}} V_{in}$

* Discontinuous \Rightarrow - large of time (D small)
- Low frequency

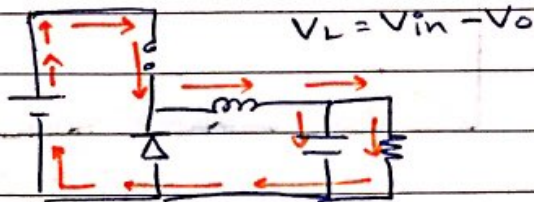
\Rightarrow Find which mode will be having higher output voltage! [with same duty ratio] the



Voltage - Second ~~balance~~ balance

$$|A| = |B|$$

$$(V_{in} - V_o) \cdot t_{on} = V_o (\Delta_i T)$$



~~Voltage~~

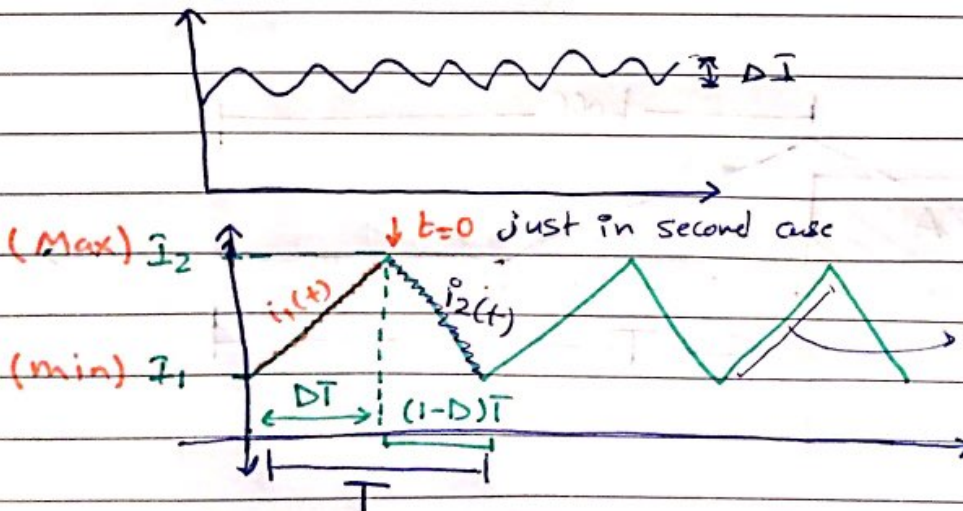
$$V_{in} t_{on} - V_o t_{on} = V_o (\Delta_i T)$$

$$V_{in} t_{on} = V_o (t_{on} + \Delta_i T)$$

$$V_o = \left(\frac{t_{on}}{t_{on} + \Delta_i T} \right) V_{in}$$

⇒ Discontinuous mode will produce higher output voltage for the same duty cycle.

$\Delta I \downarrow \rightarrow$ calc loss, L_o

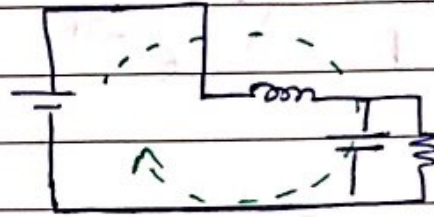


exponential i_D
 به جابجایی
 نیز می شود
 منتهی

[33]

⇒ Find I_1 and I_2 in continuous mode

ON State :-



$t: 0 \leq t \leq DT$

$$V_s(t) = R i_1(t) + L \frac{di_1(t)}{dt}$$

$$i_1(t) = \underbrace{\bar{I}_1 e^{-\frac{tR}{L}}}_{\text{natural}} + \underbrace{\frac{V_s}{R} (1 - e^{-\frac{tR}{L}})}_{\text{forced}}$$

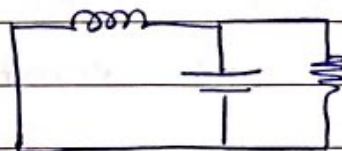
$$i_1(DT) = \bar{I}_2$$

at $t = DT$

$$\bar{I}_2 = \bar{I}_1 e^{-\frac{DTR}{L}} + \frac{V_s}{R} (1 - e^{-\frac{DTR}{L}}) \dots \textcircled{1}$$

OFF State <

$$R i_2(t) + L \frac{di_2(t)}{dt} = 0$$



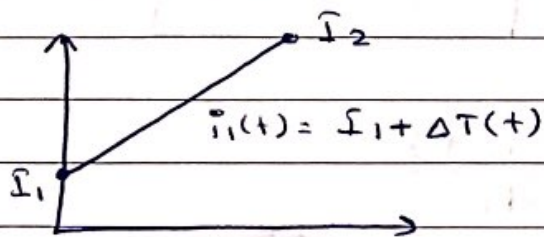
$$i_2(t) = \bar{I}_2 e^{-\frac{tR}{L}}$$

$$i_2((1-D)T) = \bar{I}_1$$

$$\bar{I}_1 = \bar{I}_2 e^{-\frac{R(1-D)T}{L}} \dots \textcircled{2}$$

$$\bar{I}_1 = \frac{V_{in}}{R} \begin{pmatrix} e^{\frac{DTR}{L}} & -1 \\ e^{\frac{TR}{L}} & -1 \end{pmatrix}$$

$$\hat{I}_2 = \frac{V_{in}}{R} \left(\frac{e^{-\frac{DT}{L}} - 1}{e^{-\frac{TR}{L}} - 1} \right)$$



The Peak-to-Peak ripple ΔI

$$\Delta I = \hat{I}_2 - \hat{I}_1$$

$$= \frac{V_{in}}{R} \left[\frac{(e^{-\frac{DT}{L}} - 1) \cdot e^{\frac{TR}{L}}}{(e^{-\frac{TR}{L}} - 1) \cdot e^{\frac{TR}{L}}} \cdot \frac{(e^{\frac{DT}{L}} - 1)}{(e^{\frac{TR}{L}} - 1)} \right]$$

$$= \frac{V_{in}}{R} \left[\frac{1 + e^{\frac{TR}{L}} - e^{\frac{DT}{L}} - e^{\frac{(1-D)TR}{L}}}{e^{\frac{TR}{L}} - 1} \right]$$

The Maximum ripple occurs:-

[which D will maximize the ripple. \Rightarrow when $\frac{d\Delta I}{dD} = 0$

$$\frac{d\Delta I}{dD} = \frac{V_{in}}{R[e^{\frac{TR}{L}} - 1]} \left[\frac{TR}{L} e^{\frac{(1-D)TR}{L}} - \frac{TR}{L} e^{\frac{DTR}{L}} \right] \stackrel{!}{=} 0$$

$$(1-D) = D$$

$D = 0.5$ will make maximum ripple on Buck DC/DC converter.

to find ΔI_{max} but $D = 0.5$

$$\Delta I_{max} = \frac{V_{in}}{R} \left[\frac{1 + e^{\frac{TR}{L}} - e^{\frac{0.5TR}{L}} - e^{\frac{0.5TR}{L}}}{e^{\frac{TR}{L}} - 1} \right]$$

$$= \frac{V_{in}}{R} \left[\frac{(1 - e^{\frac{0.5TR}{L}})^2}{e^{\frac{0.5TR}{L}} - 1} (e^{\frac{0.5TR}{L}} + 1) \right]$$

$$= \frac{V_{in}}{R} \left[\frac{(1 - e^{\frac{0.5TR}{L}})^2}{(1 - e^{\frac{0.5TR}{L}})(1 + e^{\frac{0.5TR}{L}})} \right]$$

$$\Delta I_{max} = \frac{V_{in}}{R} \left[\frac{e^{\frac{0.5TR}{L}} - 1}{e^{\frac{0.5TR}{L}} + 1} \right]$$

$$= \frac{V_{in}}{R} \tanh \frac{TR}{4L}$$

$$\tanh x = \frac{e^{2x} - 1}{e^{2x} + 1}$$

$$\Delta I = \frac{V_{in}}{R} \left[\frac{1 + e^{\frac{TR}{L}} - e^{(1-D)\frac{TR}{L}} - e^{-\frac{DTR}{L}}}{e^{\frac{TR}{L}} - 1} \right]$$

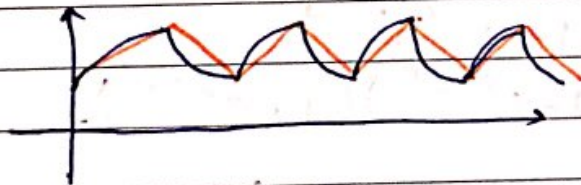
$$\Delta I_{max} \Big|_{D=0.5} = \frac{V_{in}}{R} \tanh \frac{TR}{4L} \xrightarrow{4LF} \frac{R}{4LF} \rightarrow \text{High Frequency.}$$

Since $\tanh \Theta = \Theta$ for very small value.

$$\Delta I_{max} = \frac{V}{4FL}$$

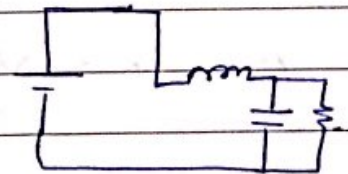


Approximate solution:-



ON State:-

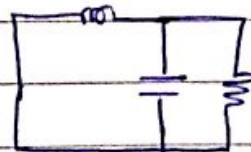
$$t_{on} = L \frac{\Delta I_L}{V_{in} - V_o} \left[V_L = L \frac{\Delta I_L}{t_{on}} \right]$$



$$(V_{in} - V_{out}) = L \frac{\Delta I_L}{t_{on}}$$

OFF State:-

$$t_{off} = \frac{\Delta I_L \times L}{V_o}$$



$$T = \frac{1}{f} = t_{on} + t_{off}$$

$$= \frac{L \cdot \Delta \bar{I} \cdot V_o}{(V_{in} - V_o) V_o} + \frac{\Delta \bar{I} \cdot L \cdot (V_{in} - V_o)}{V_o \cdot (V_{in} - V_o)}$$

$$\frac{1}{f} = \frac{V_{in} \Delta \bar{I} \cdot L}{(V_{in} - V_o) V_o}$$

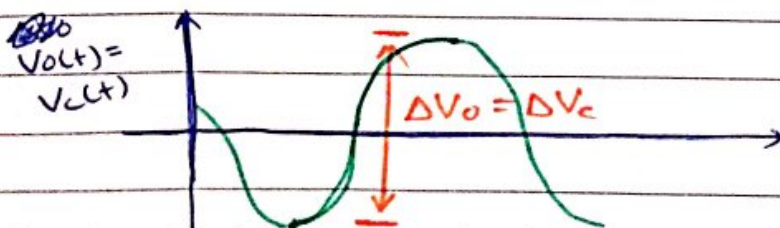
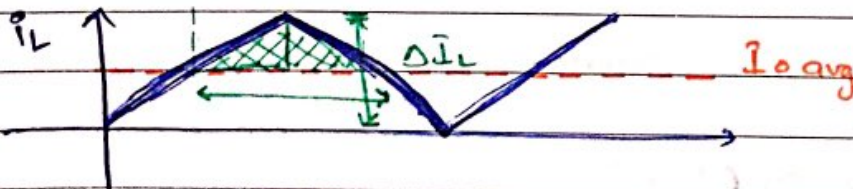
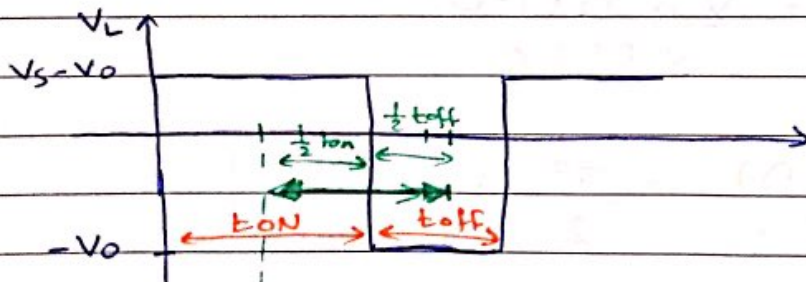
$$\Delta \bar{I} = \frac{(V_{in} - V_o) V_o}{V_{in} L f}$$

$$V_o = D V_{in}$$

$$\Delta \bar{I} = \frac{V_{in} (1-D) D}{L f}$$

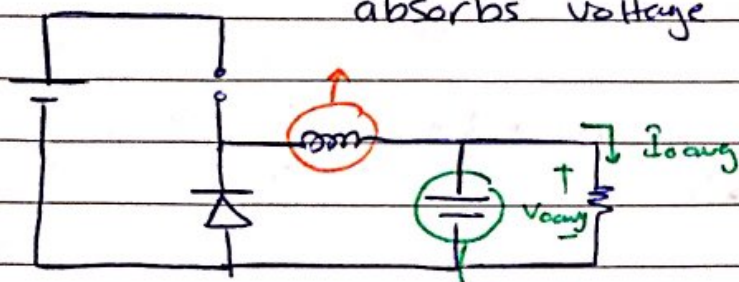
$$\Delta \bar{I}_{max} \Big|_{D=0.5} = \frac{V_{in}}{L f}$$

* Output voltage ripple (capacitor voltage ripple) :-



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absorbs voltage fluctuation.



absorbs current fluctuation.

cap → ripple الـ voltage

Ind → voltage الـ ripple current الـ

$$\Delta V_o = \Delta V_c = \frac{\Delta Q}{C} \rightarrow \text{الـ ripple الـ voltage}$$

$$= \frac{1}{2} * \frac{1}{2} \Delta I_L * \frac{1}{2} T$$

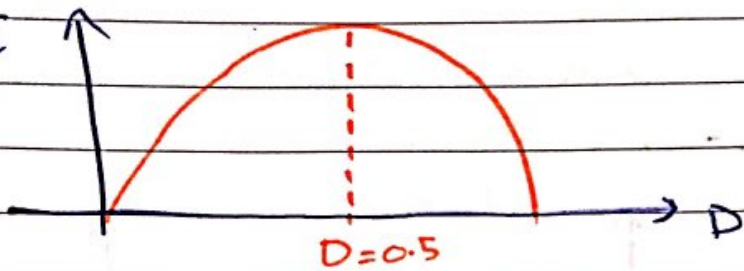
$$= \frac{\Delta I_L}{8 f C} = \frac{V_{in} D (1-D)}{8 f^2 L C}$$

$$\frac{\Delta V_o}{V_o} = \frac{(1-D)}{8 f^2 L C} = \frac{\pi^2}{2} (1-D) \left(\frac{f_c}{f} \right)^2$$

where $f_c = \frac{1}{2\pi \sqrt{LC}}$, corner frequency

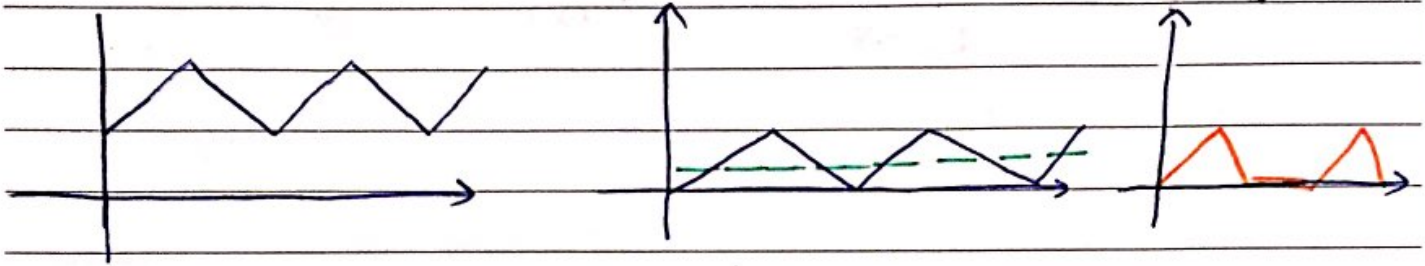
$$\Delta I = \frac{V_{in} D (1-D)}{f L}$$

ΔI



ΔI as a function of D

Boundaries between cont. and discont. modes of operation (DC-DC Buck)



$$I_2 - I_1$$

$$I_{o\text{avg}} = \frac{1}{2} \Delta I = \frac{1}{2} \frac{V_{in} (D)(1-D)}{fL}$$

$$\text{but } I_{o\text{avg}} = \frac{V_o}{R} = \frac{DV_{in}}{R}$$

$$\frac{DV_{in}}{R} = \frac{V_{in} D(1-D)}{2fL}$$

$$L_c = \frac{R(1-D)}{2f}$$

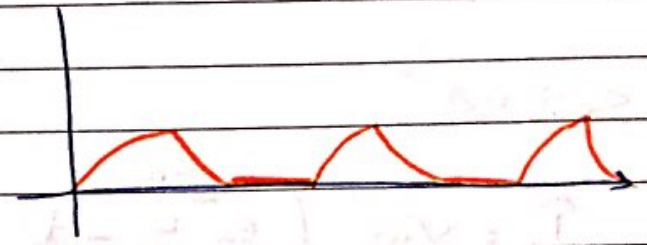
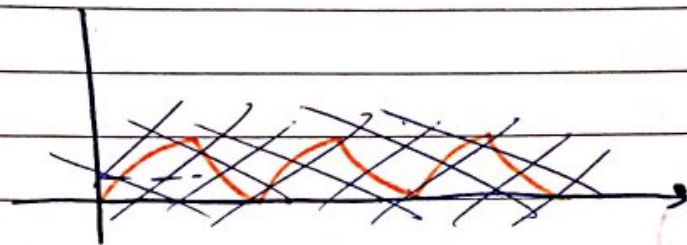
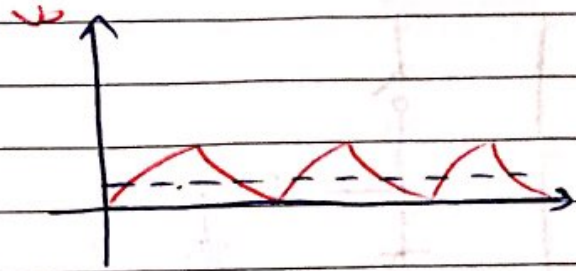
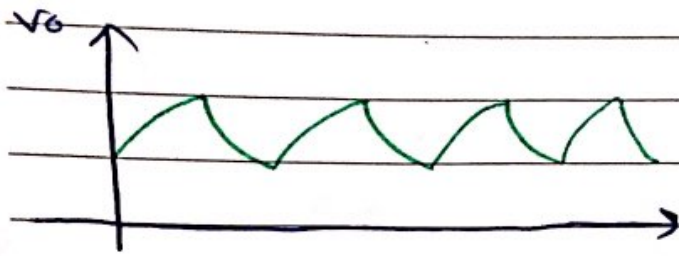
↳ critical value

$L > L_c \Rightarrow$ continuous mode.

$L < L_c \Rightarrow$ Discontinuous.

Condition for critical value of capacitor to keep the output voltage in continuous mode

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$$V_o \approx \frac{1}{2} \Delta V_o = \frac{1}{2} \Delta V_c$$

$$\Delta V_{in} = V_o > \frac{1}{2} \frac{V_{in} D(1-D)}{8 f^2 LC}$$

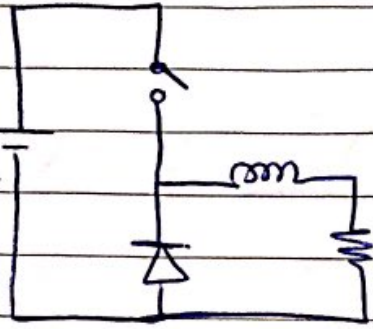
$$C_c > \frac{1-D}{16 f^2 L}$$

* $C > C_c \Rightarrow$ Continuous mode.

* $C < C_c \Rightarrow$ Discontinuous mode.

[Ex] DC-DC Buck converter is feeding a load [RL load] with $V_{in} = 220V$, $R = 5\Omega$, $L = 7.5mH$, $f = 1KHz$, $D = 0.5$.

[1] Find the min and max load currents $I_{1,0}$ & $I_{2,0}$?



Sol 84

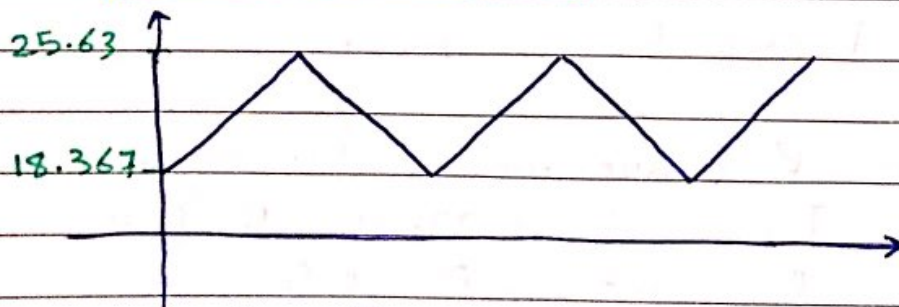
$$\hat{I}_1 = \frac{V_{in}}{R} \left(\frac{e^{\frac{DTR}{L}} - 1}{e^{\frac{TR}{L}} - 1} \right)$$

$$= \frac{220}{5} \left(\frac{e^{\frac{0.5 \times 10^{-3} \times 5}{7.5 \times 10^{-3}}} - 1}{e^{\frac{10^{-3} \times 5}{7.5 \times 10^{-3}}} - 1} \right)$$

$$\hat{I}_1 = 18.367 \text{ A}$$

$$\hat{I}_2 = \frac{V_{in}}{R} \left(\frac{e^{-\frac{DTR}{L}} - 1}{e^{\frac{TR}{L}} - 1} \right)$$

$$\hat{I}_2 = 25.63 \text{ A}$$



Continuous.

$$\Rightarrow \Delta I = \hat{I}_2 - \hat{I}_1 = 7.26 \text{ A} \rightarrow \text{exact number.}$$

$$\Rightarrow \Delta \hat{I} = \frac{V_{in} D(1-D)}{FL} = \frac{220 \times 0.5(1-0.5)}{7.5} = 7.33 \text{ A}$$

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FL

7.5

approximate number.

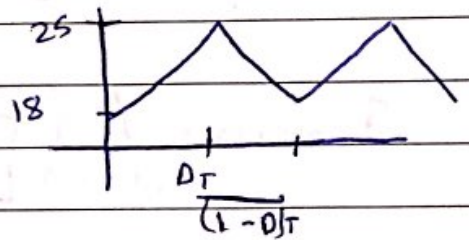
$$I_1 = I_0 - \frac{1}{2} \Delta I$$

$$= \frac{0.5 \times 220}{5} - \frac{1}{2} \times 7.33$$

$$I_0 = \frac{I_1 + I_2}{2} = \frac{V_0}{R} = \frac{D V_{in}}{R} = 22 \text{ A}$$

2 Find the RMS value of output current ?!

$$i_1(t) = \frac{V_{in}}{R} \left(1 - e^{-\frac{TRt}{L}} \right) + I_1 e^{-\frac{TRt}{L}}$$

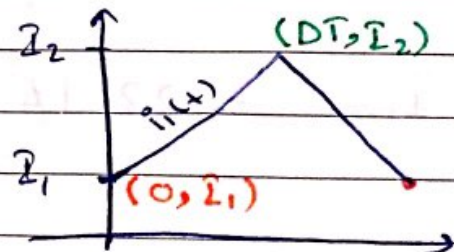


$$i_2(t) = I_2 e^{-\frac{TRt}{L}}$$

$$I_{rms\ out} = \sqrt{\frac{1}{T} \left[\int_0^{DT} i_1(t)^2 dt + \int_0^{(1-D)T} i_2(t)^2 dt \right]}$$

Approximate solution:-

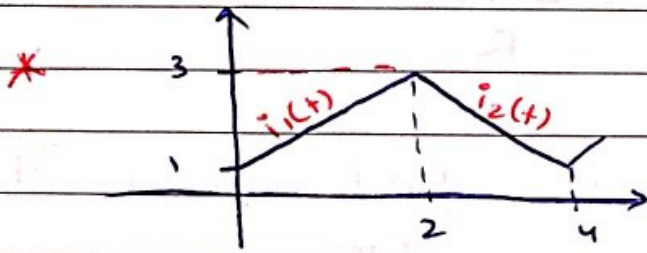
$$i_1(t) = I_1 + \frac{\Delta I}{DT} t$$



$$I_{rms\ out} = \sqrt{\frac{1}{DT} \int_0^{DT} \left(I_1 + \frac{\Delta I}{DT} t \right)^2 dt}$$

$$i_2(t) = I_2 - \frac{\Delta I}{(1-D)T} t$$

$$I_{rms(s)} = \sqrt{\frac{1}{T} \left[\int_0^{DT} \left(I_1 + \frac{\Delta I}{DT} t \right)^2 dt + \int_0^{(1-D)T} \left(I_2 - \frac{\Delta I}{(1-D)T} t \right)^2 dt \right]}$$



$$\begin{cases} i_1(t) & 0 < t < 2 \\ i_2(t) & 2 < t < 4 \end{cases}$$

$$I_{rms(s)} = \sqrt{\frac{1}{4} \left[\int_0^2 i_1(t)^2 dt + \int_2^4 i_2(t)^2 dt \right]}$$

$$= \sqrt{\frac{1}{2} \int_0^2 i_1(t)^2 dt}$$

Sol 2:

$$I_{rms} = \sqrt{\frac{1}{0.5 \times 10^{-3}} \int_0^{0.5 \times 10^{-3}} \left(18.367 + \frac{7.26}{0.5 \times 10^{-3}} t \right)^2 dt}$$

$$I_{rms} = 22.1 \text{ A}$$

[3] Find the average source current?!

sol:-

$$I_{in} = D I_o = 22 \times 0.5 = 11 \text{ A}$$

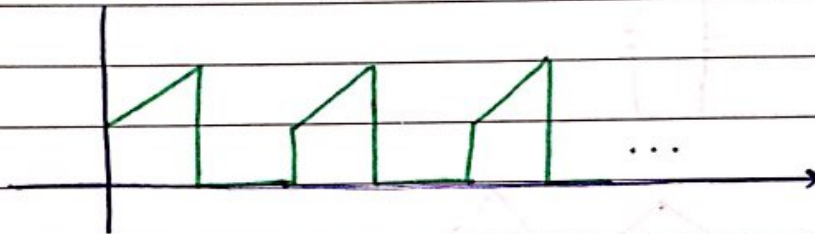
45

4] the effective input resistor ?!

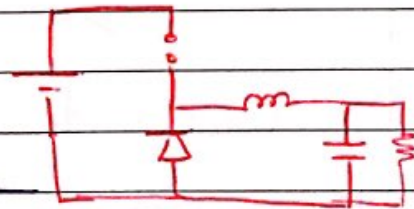
$$R_{in} = \frac{V_{in}}{I_{in}} = \frac{220}{11}$$

$$R_{in} = 20 \Omega$$

5] The RMS value of the input current ?!



$I_{in} = I_{out} \rightarrow$ ON state
OFF state $\Rightarrow I = 0$



$$I_{rms(in)} = \sqrt{\frac{1}{T} \int_0^{DT} \left(I_1 + \frac{\Delta I}{DT} t \right)^2 dt}$$

~~$I_{rms(in)} = \sqrt{D \cdot I_{rms(out)}^2}$~~

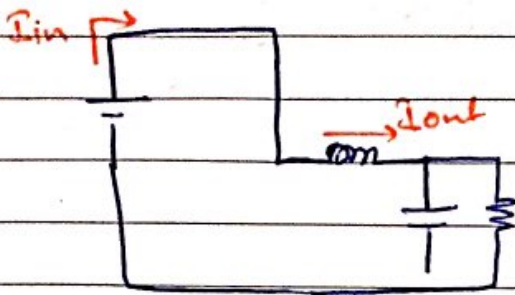
$$= \sqrt{D} \cdot I_{rms(out)}$$

$$= \sqrt{0.5} \cdot 220$$

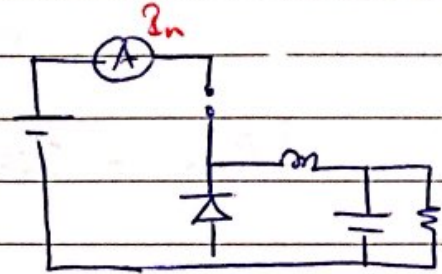
$$= 15.63$$

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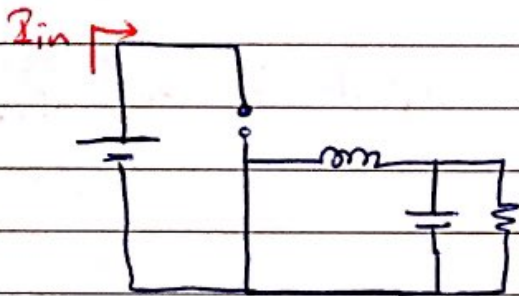
ON state :



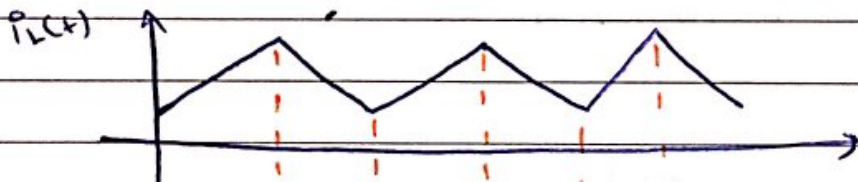
$i_{in} = i_{out}$



OFF state:-



$i_{in} = 0$



$i_{rms(in)} = \sqrt{D} * i_{rms(o)}$

$i_{rms(o)} = \sqrt{\frac{1}{DT} \int_0^{DT} (i_1 + \frac{\Delta i}{DT} t)^2 dt} \rightarrow i_L(t)$

$i_{rms(in)} = \sqrt{\frac{1}{T} \int_0^{DT} (i_1 + \frac{\Delta i}{DT} t)^2 dt} \rightarrow i_{in}(t)$

Ex DC-DC Buck Converter. $V_s = 550 \text{ V}$, $R_{\text{load}} = 25 \Omega$
 $I_0(\text{avg}) = 200 \text{ A}$, $f = 50 \text{ Hz}$ Find the value of
 L (inductor) which limit the load current
 ripple to 10% of I_0 ?!!

Sol:- $I_0 = 200 \text{ A}$
 10% of $I_0 = 20 \text{ A}$
 $\Delta I_{\text{max}} = 20 \text{ A}$

$$\Delta I_{\text{max}} = \frac{V_{\text{in}}}{4 \times 50 \times L} \Rightarrow \frac{550}{4 \times 50 \times L} = 20$$

~~XXXXXXXXXX~~

$$L = 20 \text{ mH}$$

Ex Buck Converter with $V_s = V_{\text{in}} = 12 \text{ V}$,
 $V_0 = V_a = 5 \text{ V}$, $R = 500$, $\Delta V_c = 20 \text{ mV}$
 $f = f_s = 25 \text{ kHz}$, $\Delta I = 0.8 \text{ A}$?!

1) Find D ?!

$$D = \frac{V_0}{V_{\text{in}}} = \frac{5}{12} = 0.4167$$

2) Find L ?!

$$\Delta I = \frac{V_{\text{in}}(D)(1-D)}{fL} \Rightarrow L = \frac{V_{\text{in}} D(1-D)}{f \Delta I}$$

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$$L = 145.83 \text{ mH}$$

3] Find C ?!

$$\Delta V_C = \Delta V_O = \frac{V_{in}(D)(1-D)}{8f^2LC}$$

$$C = 200 \text{ MF}$$

4] L_c and C_c ?!

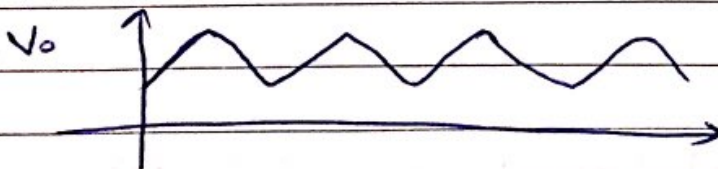
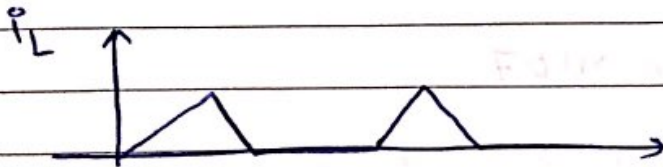
$$\Rightarrow L_c = \frac{(1-D)R}{2f}$$

$$L_c = 5.83 \text{ mH}$$

$$\Rightarrow C_c = \frac{(1-D)}{16Lf^2}$$

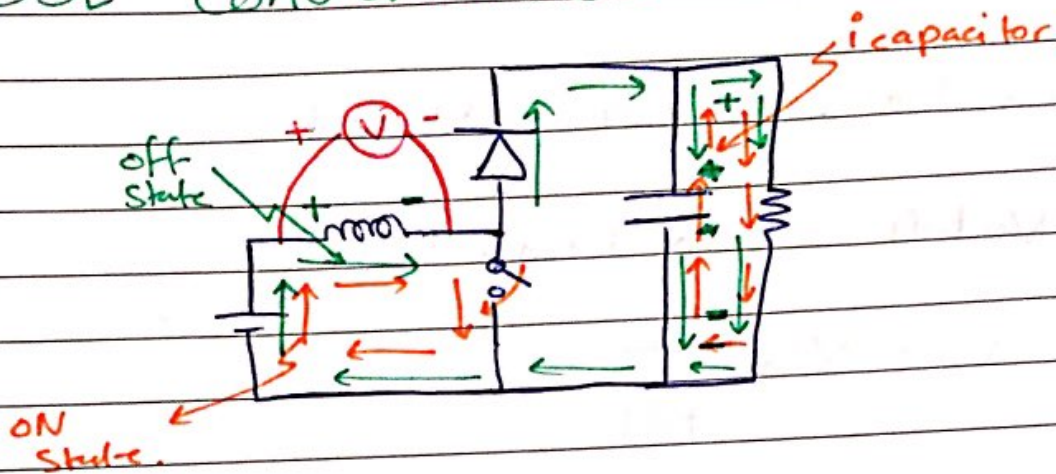
$$C_c = 0.4 \text{ MF}$$

$L, L_c \Rightarrow L_c > L \Rightarrow$ Discontinuous
 $C, C_c \Rightarrow C > C_c \Rightarrow$ Continuous capacitor voltage.



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* Boost converters 84



* OFF State



* ON State:



$$-V_{in} + V_L = 0 \quad , \quad V_L = V_{in} = L \frac{\Delta I}{\Delta t}$$

$$V_L = V_{in}$$

$$\Delta t = t_{ON}$$

OFF state :-

$$-V_{in} + V_L + V_o = 0 \quad , \quad V_L = V_{in} - V_o = -L \frac{\Delta I}{\Delta t}$$

$$V_L = V_{in} - V_o$$

$$\Delta t = t_{OFF}$$

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$$V_{in} t_{on} = (V_o - V_{in}) t_{off}$$

$$V_{in} t_{on} = V_o t_{off} - V_{in} t_{off}$$

$$V_o t_{off} = V_{in} (t_{on} + t_{off})$$

$$V_o = V_{in} \frac{T}{t_{off}}$$

$$V_o = V_{in} \frac{T}{(1-D)T}$$

$$V_o = \frac{V_{in}}{1-D}$$

works as a boost converter
voltage ال، هو أعلى!

→ $D=1$ in Buck means → switch is ~~on~~ always off

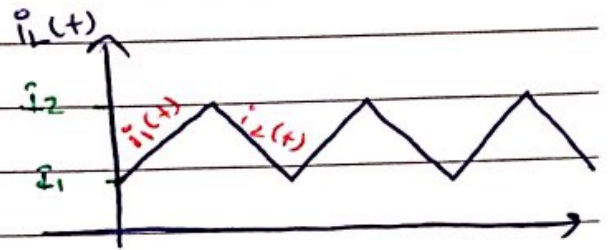
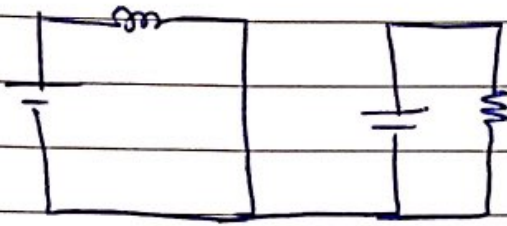
→ D is an unstable condition. ⇒ $D=1$ in Boost.
لا يعمل في حالة $D=1$ ، قريب من هنا.

Since we consider as lossless converter

$$P_{in} = P_{out}$$
$$V_{in} I_{in} = V_{out} I_{out}$$

$$I_{in} = \frac{I_o}{1-D}$$

* ON State :-

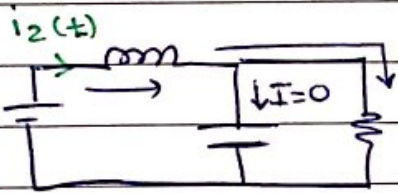


$$V_{in} = L \frac{di_1(t)}{dt}$$

linear curve ?!

$$i_1(t) = \frac{V_{in}}{L} t + I_1$$

* OFF State 8A

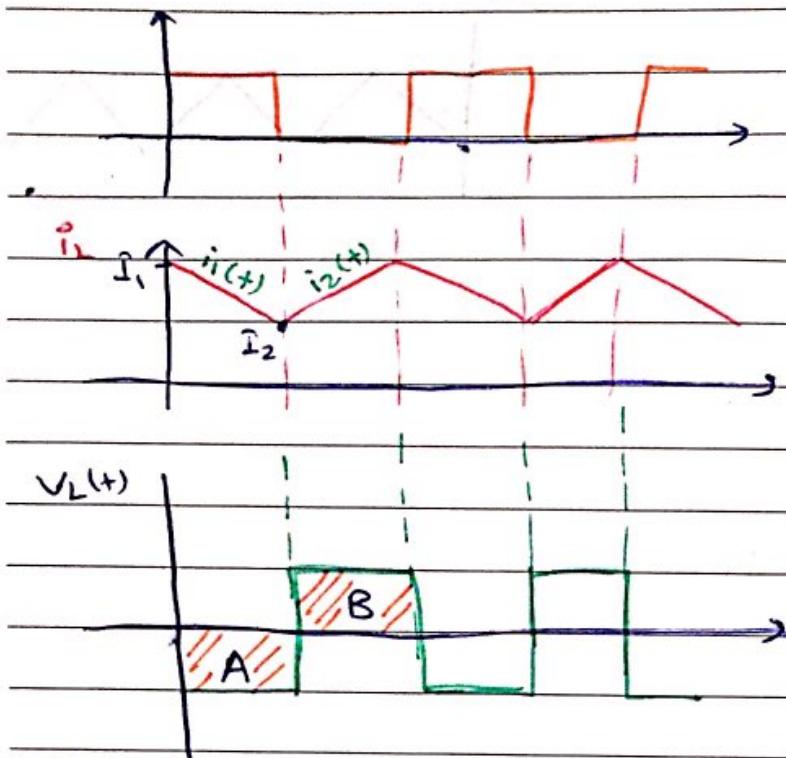


فرض انو حالي في سيارا ، في Capacitor

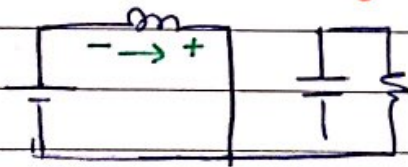
$$V_{in} = L \frac{di_2(t)}{dt} + R i_2(t)$$

$$i_2(t) = \frac{V_{in}}{R} \left(1 - e^{-\frac{Rt}{L}} \right) + \hat{I}_2 e^{-\frac{ER}{L}}$$

Boost Converters 83



ON State :- charge.



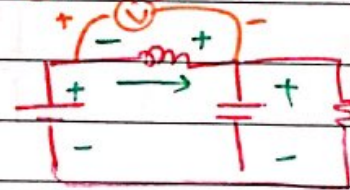
$$V_{in} = L \frac{di_L(t)}{dt}$$

$$i_L(t) = \frac{V_{in}}{L} t + I_1$$

at $t = DT$

$$i_L(t) = I_2 = \frac{V_{in}}{L} (DT) + I_1 \dots \textcircled{1}$$

OFF State :- discharge



$$V_{in} = L \frac{di_L(t)}{dt} + R i_L(t)$$

$$i_L(t) = \frac{V_{in}}{R} (1 - e^{-\frac{tR}{L}}) + I_2 e^{-\frac{tR}{L}}$$

$$-V_{in} + V_L + V_o = 0$$

$$V_L = V_{in} - V_o$$

at $t = (1-D)T$

$$i_2((1-D)T) = \hat{i}_1$$

$$i_2(t) = \frac{V_{in}}{R} \left(1 - e^{-\frac{(1-D)TR}{L}}\right) + \hat{i}_2 e^{-\frac{(1-D)TR}{L}} \dots \textcircled{2}$$

~~scribble~~

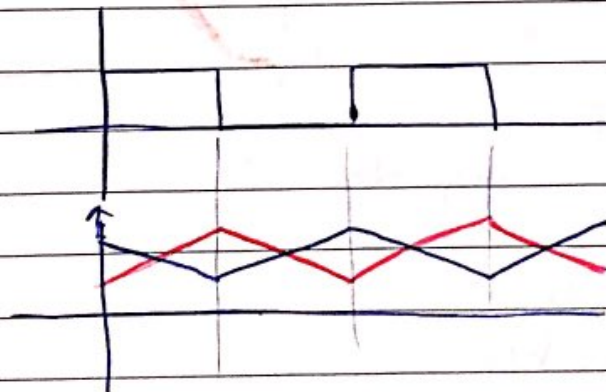
Solving ~~scribble~~ these two equations for \hat{i}_1 and $\hat{i}_2 \Rightarrow$

$$\hat{i}_1 = \frac{V_{in} D \hat{I}}{L} * \frac{e^{-\frac{(1-D)TR}{L}}}{1 - e^{-\frac{(1-D)TR}{L}}} + \frac{V_{in}}{R}$$

$\hookrightarrow \hat{i}_{min}$

$$\hat{i}_2 = \frac{V_{in} D \hat{I}}{L} * \frac{1}{1 - e^{-\frac{(1-D)TR}{L}}} + \frac{V_{in}}{R}$$

$\hookrightarrow \hat{i}_{max}$



~~scribble~~

peak to peak ripple :-

$$\Delta \bar{i} = \bar{i}_2 - \bar{i}_1$$

$$= \frac{V_{in} D T}{L}$$

$$\Delta \bar{i} = \frac{V_{in} D}{fL}$$

The peak to peak capacitor voltage ΔV_c

↳ considering the ON state.

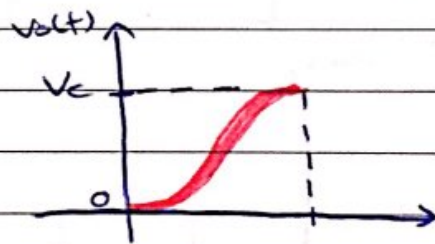
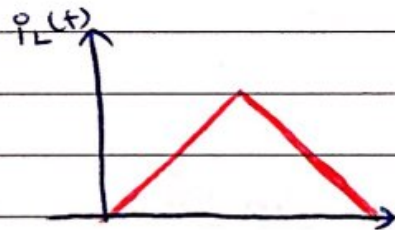
$$\Delta V_o = \Delta V_c$$
$$= V_c - 0$$

$$\frac{1}{C} \int_0^{DT} I_c dt$$

But $I_c = I_o$

$$\Delta V_o = \Delta V_c = \frac{1}{C} \int_0^{DT} I_{o,avg} dt$$

$$= \frac{I_o D T}{C} = \frac{I_o D}{fC}$$



* Condition for continuous mode of operation :-

$$I_1 > 0$$

$$I_{o \text{ avg}} - \frac{1}{2} \Delta I > 0$$

$$\frac{V_{in}}{(1-D)R} - \frac{1}{2} \frac{V_{in} D}{fL} > 0$$

$$L > \frac{RD(1-D)}{2f}$$

$$L_c = \frac{RD(1-D)}{2f}$$

Condition for critical. C :

$$V_o > \frac{1}{2} \Delta V_o = \frac{1}{2} \Delta V_c$$

$$V_o > \frac{1}{2} \frac{I_o D}{fC}$$

$$C > \frac{I_o D}{2f V_o} = \frac{D}{2fR}$$

$$C_c = \frac{D}{2fR}$$

* Reading assignment : Chapter 1

Suggested Problem : 5.1, 5.6

Section ch. 5 → 5.1 → 5.6

5.9.1, 5.9.2, 5.9.3

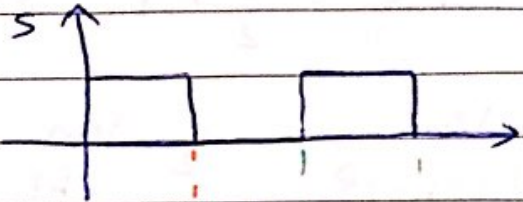
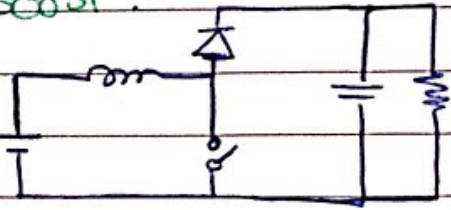
problems → 5.2, 5.3, 5.4, 5.6, 5.7, 5.9, 5.10, 5.11

Mohan → suggested: Section → 7: 7.1 → 7.5

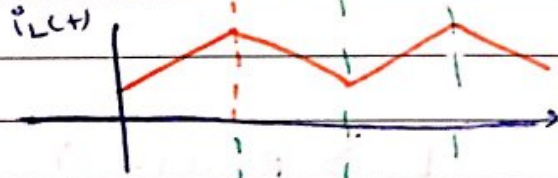
Problem → 7.1, 7.5, 7.7, 7.8, 7.16

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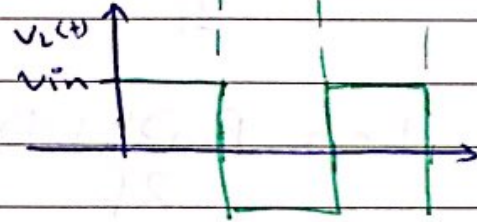
Boost :-



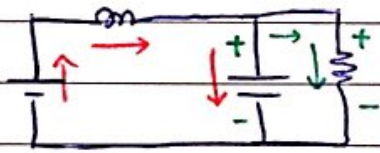
ON state :-



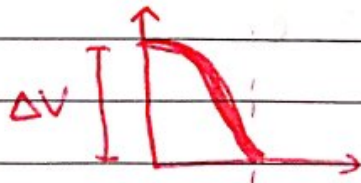
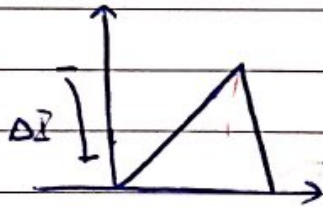
charged.



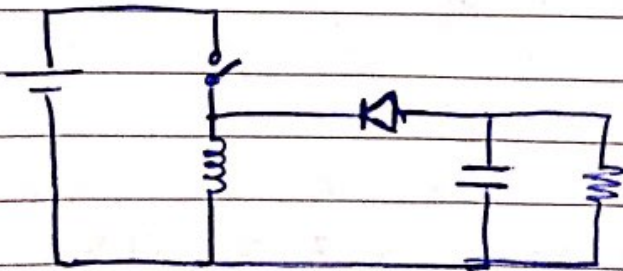
OFF state :-



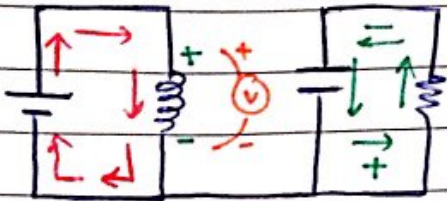
$V_o(p-p)$



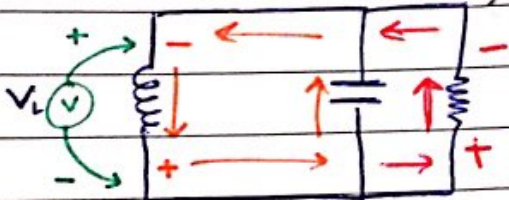
Buck-Boost converter



ON state :-



OFF state :-



ON state :-

$$-V_{in} + V_L = 0$$

$$V_L = V_{in} = L \frac{\Delta I_1}{DT} = L \frac{\Delta I_1}{t_{on}}$$

OFF state :-

$$V_L + V_o = 0$$

$$V_L = -V_o = L \frac{\Delta I_2}{t_{off}} = -L \frac{\Delta I_1}{(1-D)T}$$

$$V_o = L \frac{\Delta I_1}{(1-D)T}$$

$$\Delta I_1 = \frac{V_o (1-D)T}{L} = \frac{V_{in} DT}{L}$$

$$V_o = \frac{D}{1-D} V_{in}$$

$D < 0.5 \Rightarrow$ Buck

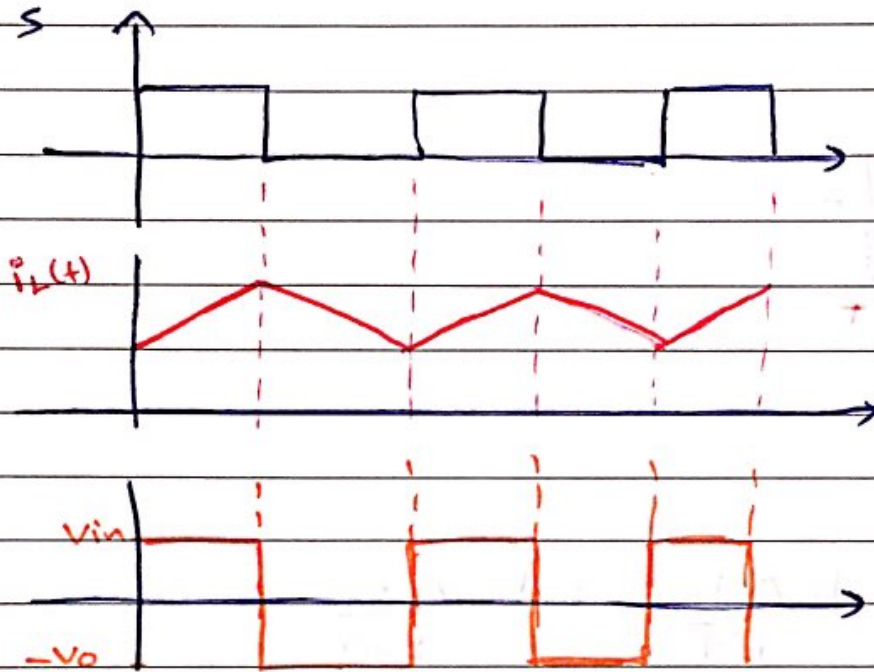
$D > 0.5 \Rightarrow$ Boost

$D \geq 1$ represent instable condition

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Buck $\Rightarrow V_o = D V_{in}$

Boost $\Rightarrow V_o = \frac{1}{1-D} V_{in}$



* considering lossless converter. Δ

Switch Ideal \Rightarrow pure element.

$$V_{in} I_{in} = V_o I_{out}$$

$$I_{in} = \frac{D}{1-D} I_o$$

Peak-peak ripple in inductor current is

$$T = \frac{1}{f} = t_{on} + t_{off}$$

$$= \frac{L \Delta I}{V_{in}} + \frac{L \Delta I}{V_o}$$

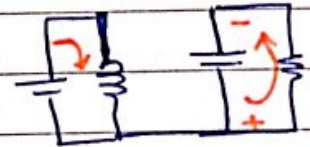
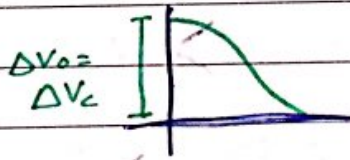
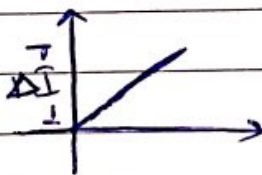
$$\frac{I}{f} = L \frac{\Delta I (V_o + V_{in})}{V_{in} V_o}$$

$$\Delta I = \frac{V_{in} V_o}{fL (V_o + V_{in})}$$

$$\Delta I = \frac{V_{in} V_o}{fL \left(\frac{D}{1-D} + \frac{1+(1-D)}{1+(1-D)} V_{in} \right)}$$

$$\Delta I = \frac{V_o (1-D)}{fL} = \frac{V_{in} D}{fL}$$

Peak-Peak Capacitor ripple voltage ΔV_c
 [on state for the derivation] \Rightarrow off state will hold



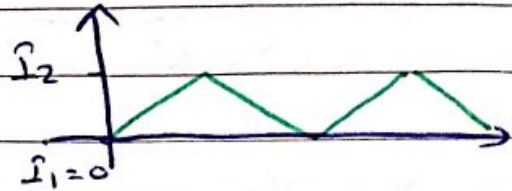
$$\begin{aligned} \Delta V_o = \Delta V_c &= \frac{1}{C} \int_0^{DT} I_c dt \\ &= \frac{1}{C} \int_0^{DT} I_{o,avg} dt \\ &= \frac{I_o DT}{C} \end{aligned}$$

$$\Delta V_o = \frac{I_o D}{CF}$$

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* Critical value of $L \Delta$

$$I_1 > 0$$



$$I_{o\text{avg}} = -\frac{1}{2} \Delta I > 0$$

$$\frac{V_{in} * D}{(1-D)*R} - \frac{1}{2} D \frac{V_{in}}{fL} > 0$$

$$L > \frac{R(1-D)}{2f}$$

$$L_c = \frac{R(1-D)}{2f}$$

* Critical value of $C \Delta$

$$V_{o1} = \frac{1}{2} \Delta V_o > 0$$

$$\frac{V_o}{I_o} - \frac{1}{2} \frac{I_o D}{C f I_o} > 0$$

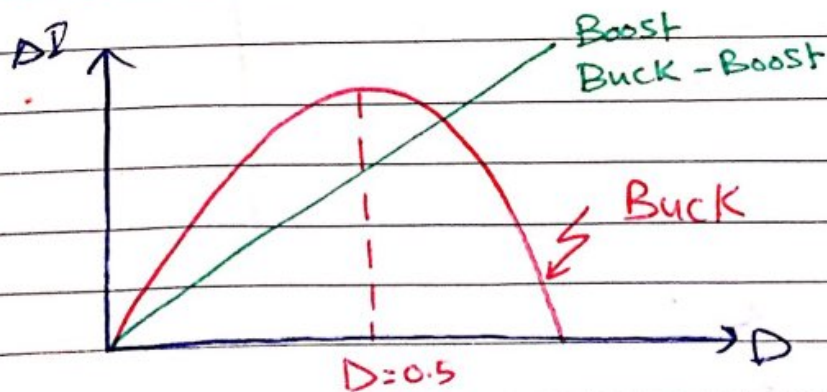
$$R - \frac{D}{2fC} > 0$$

$$C > \frac{D}{2fR}$$

$$C_c = \frac{D}{2fR}$$

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	BUCK	BOOST	BUCK/BOOST
V_o avg	$D V_{in}$	$V_{in}/(1-D)$	$\frac{D}{1-D} V_{in}$
I_o avg	$\frac{I_{in}}{D}$	$I_{in}(1-D)$	$\frac{1-D}{D} I_{in}$
ΔI	$\frac{V_{in} D(1-D)}{fL}$	$\frac{V_{in} D}{fL}$	$\frac{V_{in} D}{fL}$
ΔI_{max}	$\frac{V_{in}}{4fL} \quad (D=0.5)$	$\frac{V_{in}}{fL} \quad D=1$	$\frac{V_{in}}{fL} \quad D=1$
ΔV_o	$\frac{V_{in} D(1-D)}{8f^2 LC}$	$\frac{I_o D}{fC}$	$\frac{I_o D}{fC}$
L_c	$\frac{R(1-D)}{2f}$	$\frac{RD(1-D)}{2f}$	$\frac{R(1-D)}{2f}$
C_c	$\frac{1-D}{16Lf^2}$	$\frac{D}{2fR}$	$\frac{D}{2fR}$



* Homework 184

Design the DC-DC converter in ex 5.2

$V_{in} = 220V$

(Buck)

$R = 5\Omega$

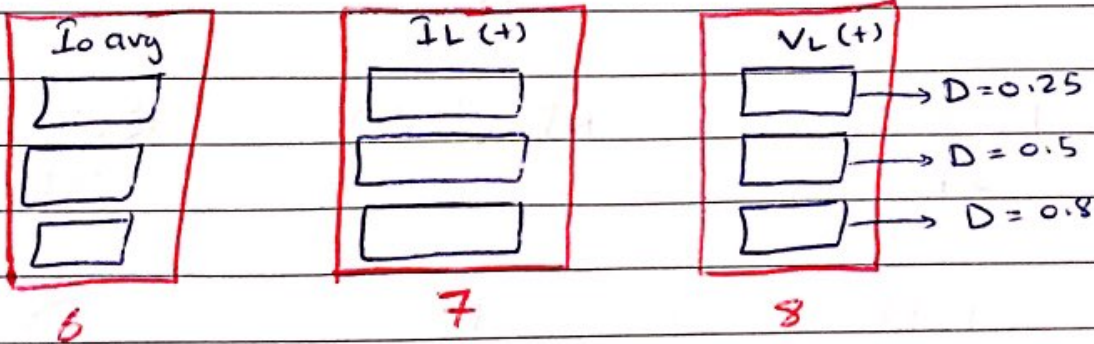
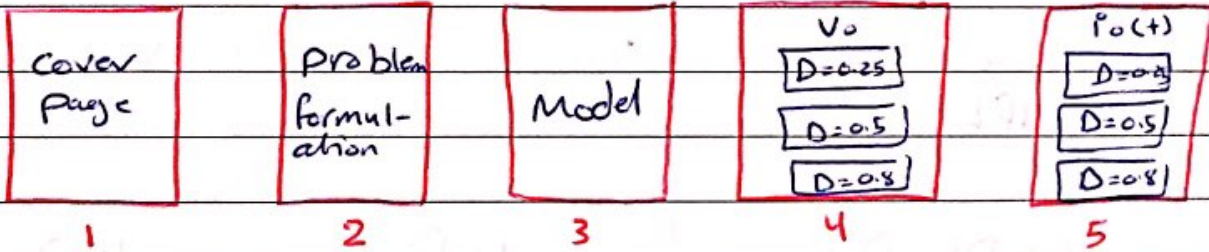
$L = 7.5mH$

$C = 1000\mu F$

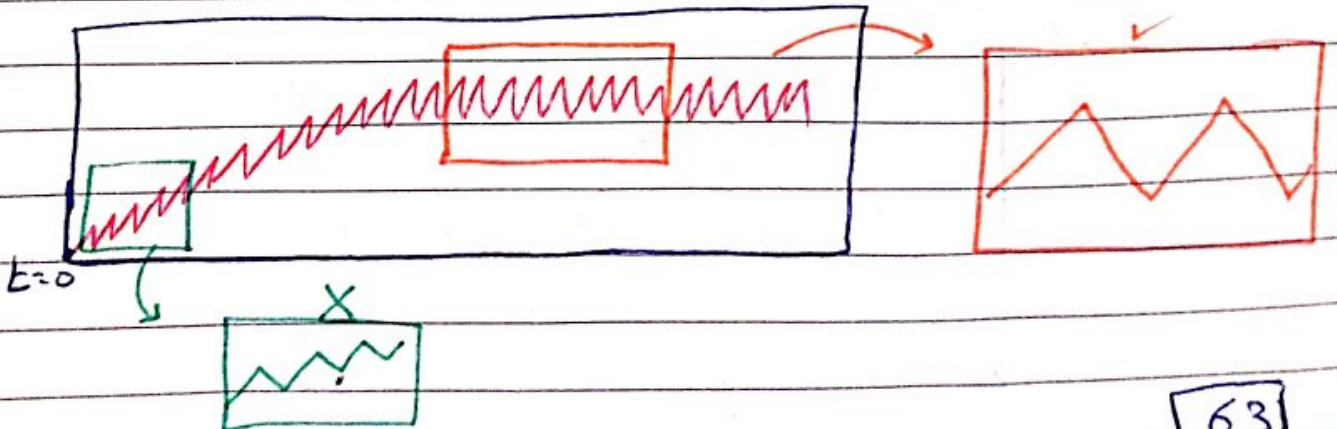
$f = 16KHz$

$D = 0.25, 0.5, 0.8$

Report \Rightarrow 8 Pages 84



ON Matlab $\rightarrow I_L(t)$ at $D = 0.8$



Matlab \rightarrow sys box

new \rightarrow simulink model \rightarrow blank model \rightarrow open the sheet
 \rightarrow draw a system.

* library browser (has everything).

SimScop or sym power 3 system \rightarrow power system.

\rightarrow Specialised tech. \rightarrow fund blocks \rightarrow 3 ϕ source.

3 ϕ source (Gen jic) \rightarrow drag and drop.

Elements \rightarrow 3 ϕ transformer \rightarrow connect them

3 ϕ load \rightarrow connect the sys.

double click on Gen \rightarrow freq = 50 Hz

25K phase-phase voltage \rightarrow X/R

on TX change to (250K, 50) \rightarrow (25K the voltage on primary, 50K secondary) \rightarrow local power look.

\rightarrow change time to 1sec. \rightarrow Run \rightarrow error \rightarrow find Power \rightarrow double click in \rightarrow change to discrete.

\rightarrow sample time ($T = \frac{1}{F} = \frac{1}{50} = 20\text{ms}$) we pick

~~20ms~~

sample time = 1×10^{-6}
1M

RUN \rightarrow measurement blocks

current measurement. and voltage measurement.

Series

Parallel

\rightarrow Connect the ~~Ammeter~~ Ammeter to the CKT

\rightarrow " a scope to the ~~Ammeter~~ Ammeter.

RTDS \equiv Real time digital Simulator.

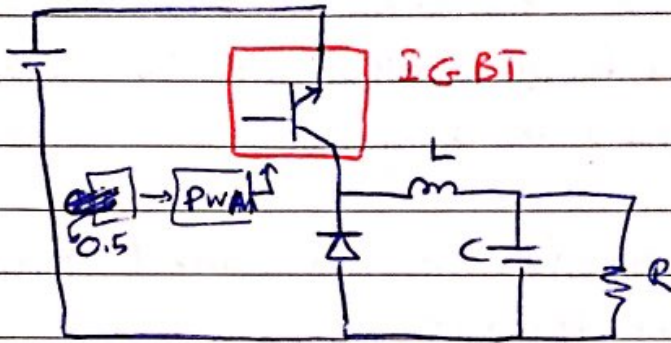
\rightarrow scope \rightarrow file \rightarrow plot. \rightarrow

DC-DC Converter:-

DC Source \rightarrow 100 V \rightarrow library \rightarrow power.

~~element~~. electronics \rightarrow IGBT \rightarrow double click \rightarrow

Show \rightarrow CTRL R (flips) \rightarrow double \rightarrow double click.
 measurement



power GMI.
 discrete
 sample time
 10ms

library \rightarrow elements \rightarrow RLC \rightarrow double click.

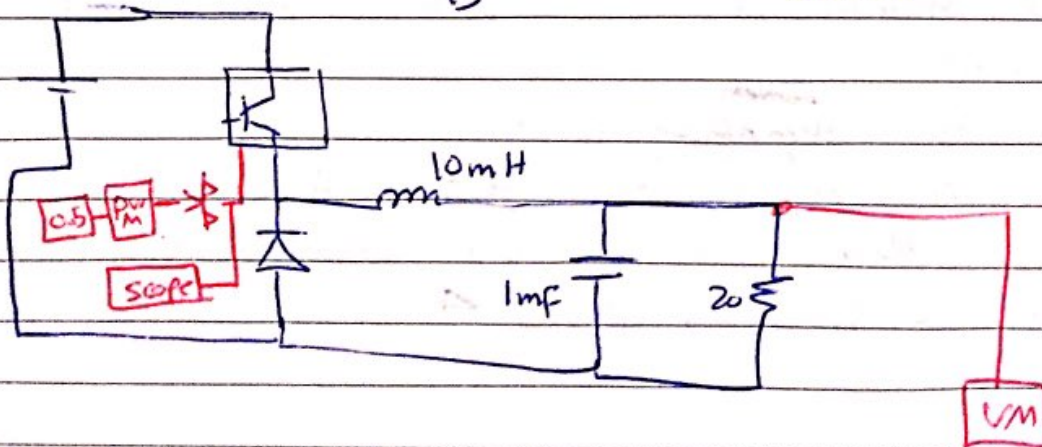
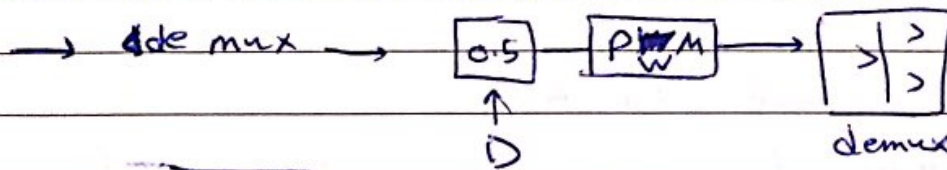
" \rightarrow search PWM \rightarrow D constant.



double click PWM [0,1] freq = 10KHZ.

the constant is the width of the pulse.

(error) \rightarrow PWM \rightarrow double click. \rightarrow 2 puls [check the dimension]



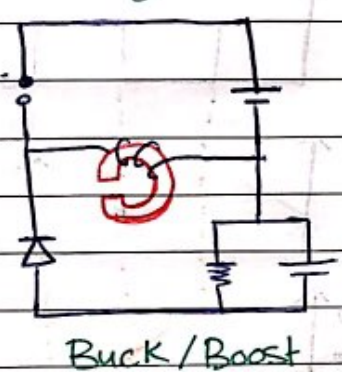
50V \leftarrow

05

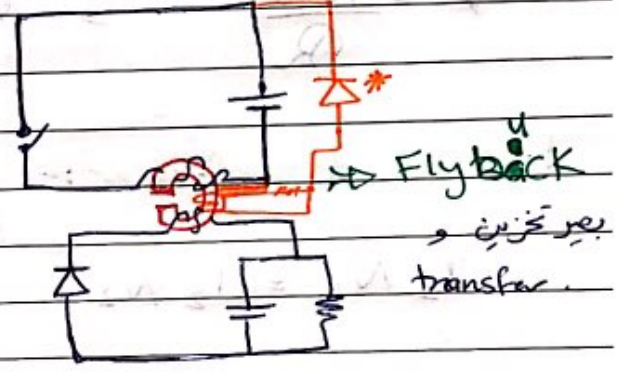
* Electrically Isolated DC-DC Converter 8A

- ⇒ Fly back converter derived from Buck/Boost converter
- ⇒ Forward converter derived from Buck converter.
- ⇒ full and half Bridges derived from Buck converter.

Fly Back converter :-

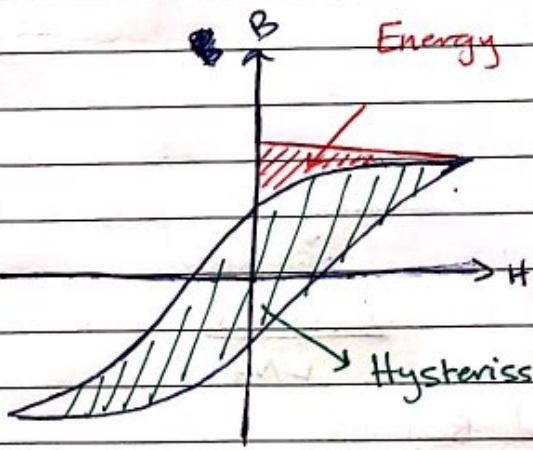


Same winding : μ نچ



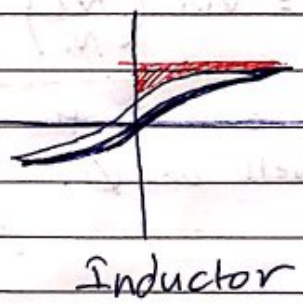
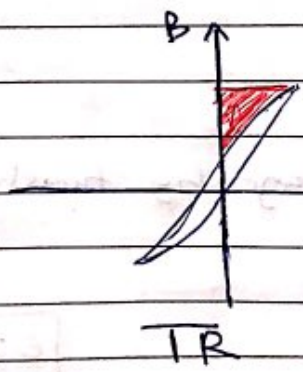
بیر ذخیرین و transfer

transformer (inductor) و ولت *

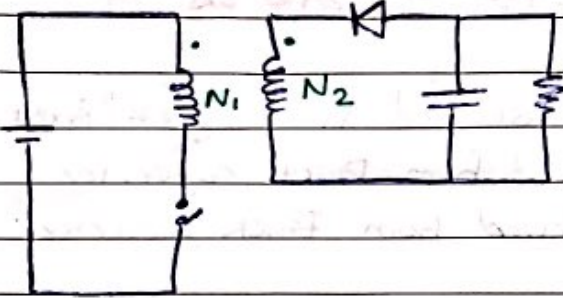


Energy Stored and released.

* winding 3 ⇒ add diode ⇒ to ensure that the TR will not go to saturation (discharging of any accumulating charges)



* energy stored in inductor (bigger) energy stored in TR

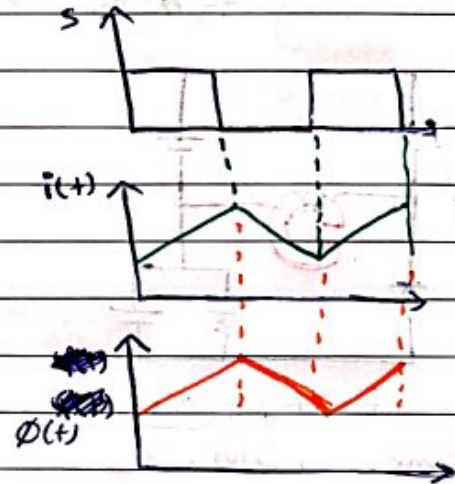


$$\Phi = \frac{NI}{R} \Rightarrow \Phi \propto I$$

For the transformer :-

$$I_1 N_1 = I_2 N_2$$

$$\Delta \Phi_{pp} = N \Delta I$$



$$\Delta I = \frac{\Delta \Phi}{N}$$

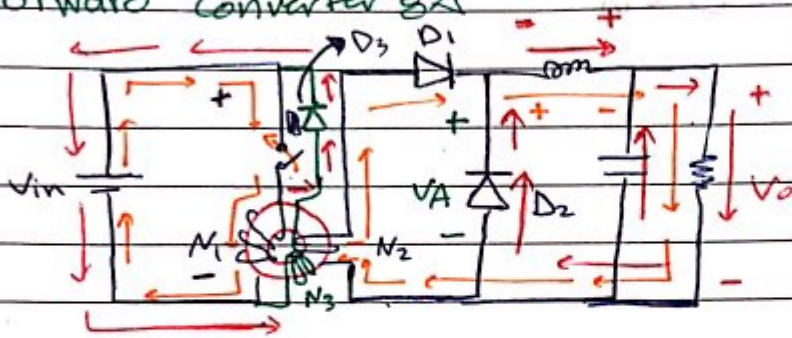
$$\begin{array}{ccc} & \Delta I & \\ \downarrow & & \downarrow \\ \text{ON State} & & \text{OFF State} \\ \frac{V_{in} D T}{L N_1} & = & \frac{V_o (1-D) T}{L N_2} \end{array}$$

according to voltage-second balance

$$V_o = V_{in} \left(\frac{N_2}{N_1} \right) \frac{D}{1-D}$$

⇒ I can now control the output voltage by transformation ratio as well as Φ .

Forward Converter



ON State

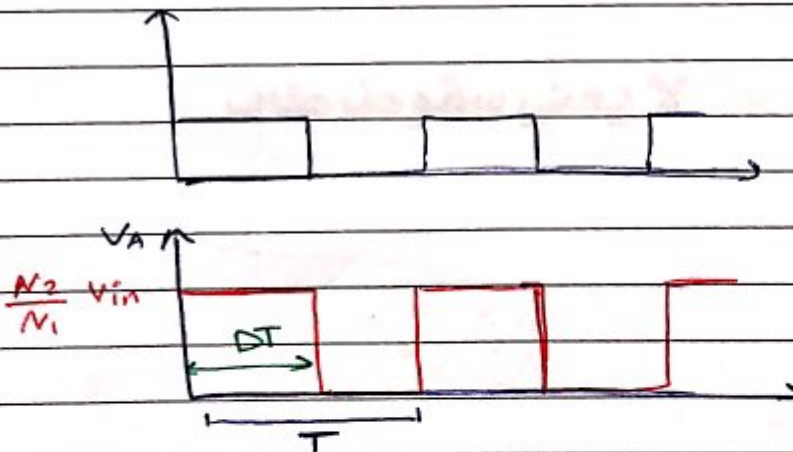
OFF State

ON State :- $D_1 \Rightarrow$ F.B

$D_2 \rightarrow D_3 \Rightarrow$ R.B.

OFF State :- $D_1 \Rightarrow$ R.B

$D_2, D_3 \Rightarrow$ F.B



$$V_A(t) = V_L(t) + V_o(t)$$

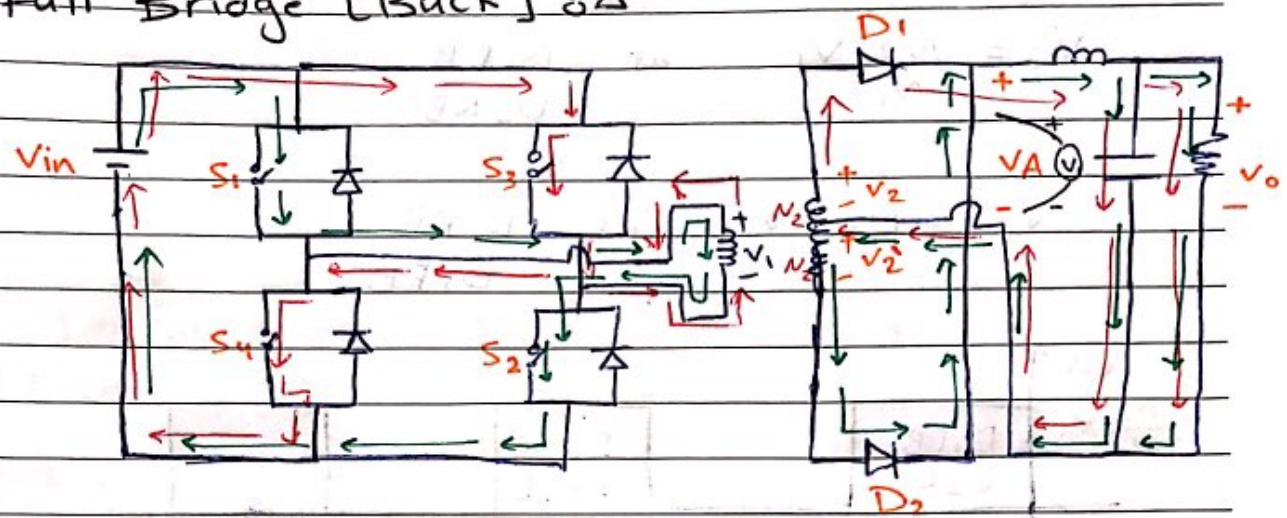
average voltages.

$$V_{A \text{ avg}} = V_{L \text{ avg}} + V_{o \text{ avg}}$$

$$V_{A \text{ avg}} = V_{o \text{ avg}}$$

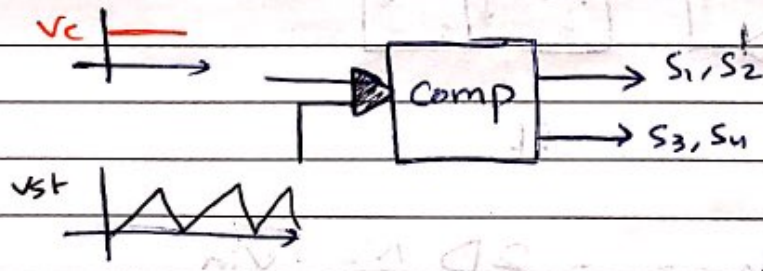
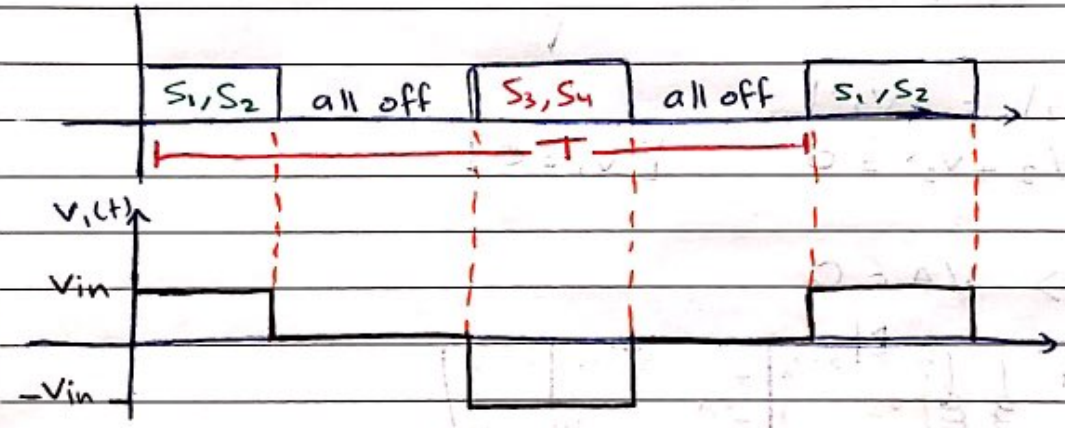
$$V_A = V_o = \frac{N_2}{N_1} D V_{in}$$

* Full Bridge [Buck] 3A



S_1, S_2
 S_3, S_4

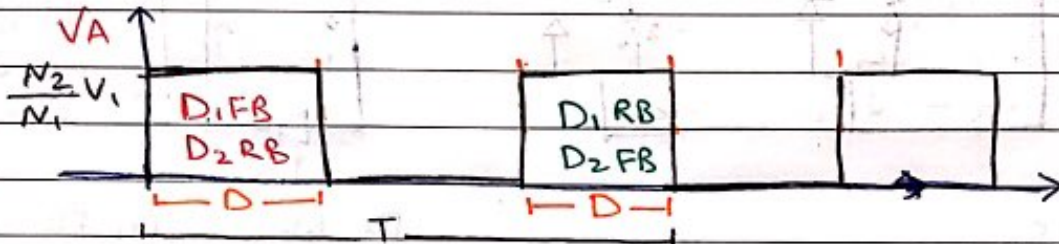
D_1 RB
 D_2 FB
 D_1 FB
 D_2 RB



* 4 switch
even cycle 4S
امرين 4
2 switch
كل T برين امين اعلى
double frequency

$$V_2 = \frac{N_2}{N_1} V_1 \quad \text{at } \begin{matrix} D_1 \text{ FB} \\ D_2 \text{ RB} \end{matrix}$$

$$V_2 = -\frac{N_2}{N_1} V_1 \quad \text{at } \begin{matrix} D_1 \text{ RB} \\ D_2 \text{ FB} \end{matrix}$$

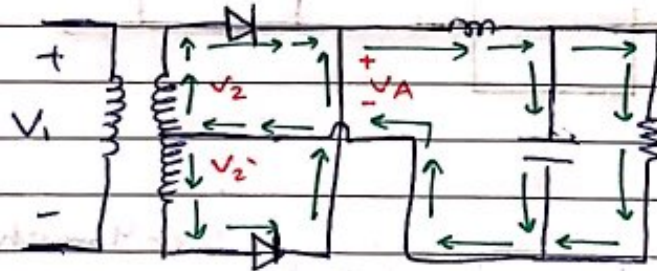


all switch are OFF \Rightarrow
IN OFF STATE :-

$$|V_2| = |V_2'|$$

$$V_2 + V_2' = 0 \quad [V_1 = 0]$$

$$\Rightarrow V_A = 0$$



$V_1 = 0 \rightarrow$ switch off

$$V_o \text{ avg} = V_A \text{ avg} = 2D \frac{N_2}{N_1} V_{in}$$

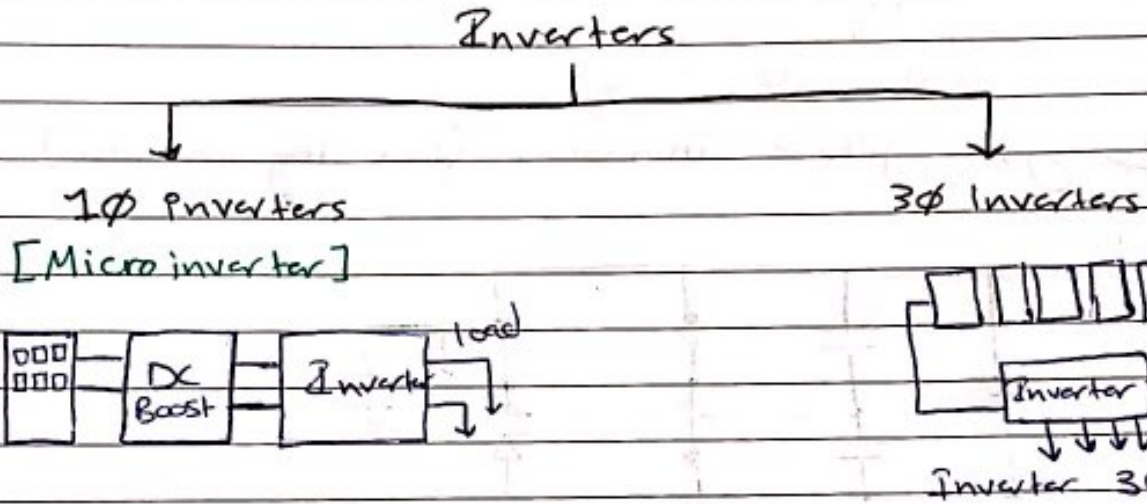
$$V_A(t) = V_i(t) + V_o(t)$$

$$V_A \text{ avg} = V_o \text{ (avg)} \quad [V_i \text{ avg} = 0]$$

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X First

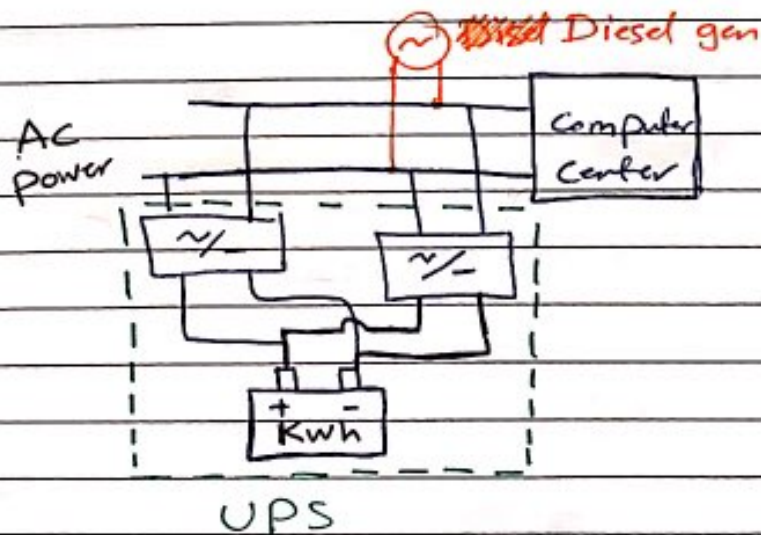
Inverters \rightarrow Inversion of DC to AC Power [PV syst II]



3 ϕ \rightarrow PWM = Pulse width modulation.
 \rightarrow SPWM = sinusoidal pulse width mod.

Applications \rightarrow

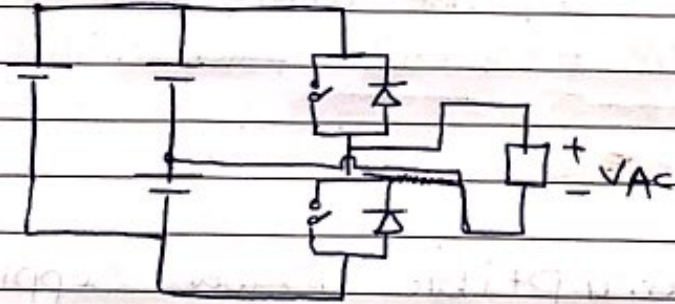
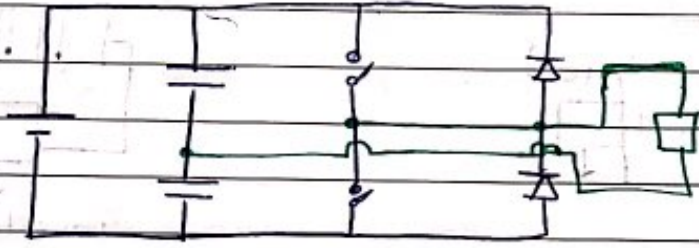
① UPS \equiv Uninterruptible Power supplies



② Renewables : PV

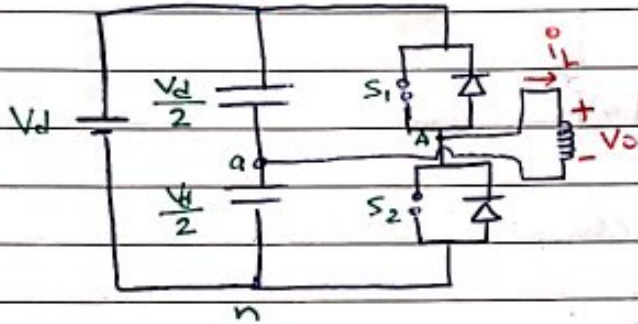
③ AC motor drive
VFD

Single Phase inversion (one leg inverter)

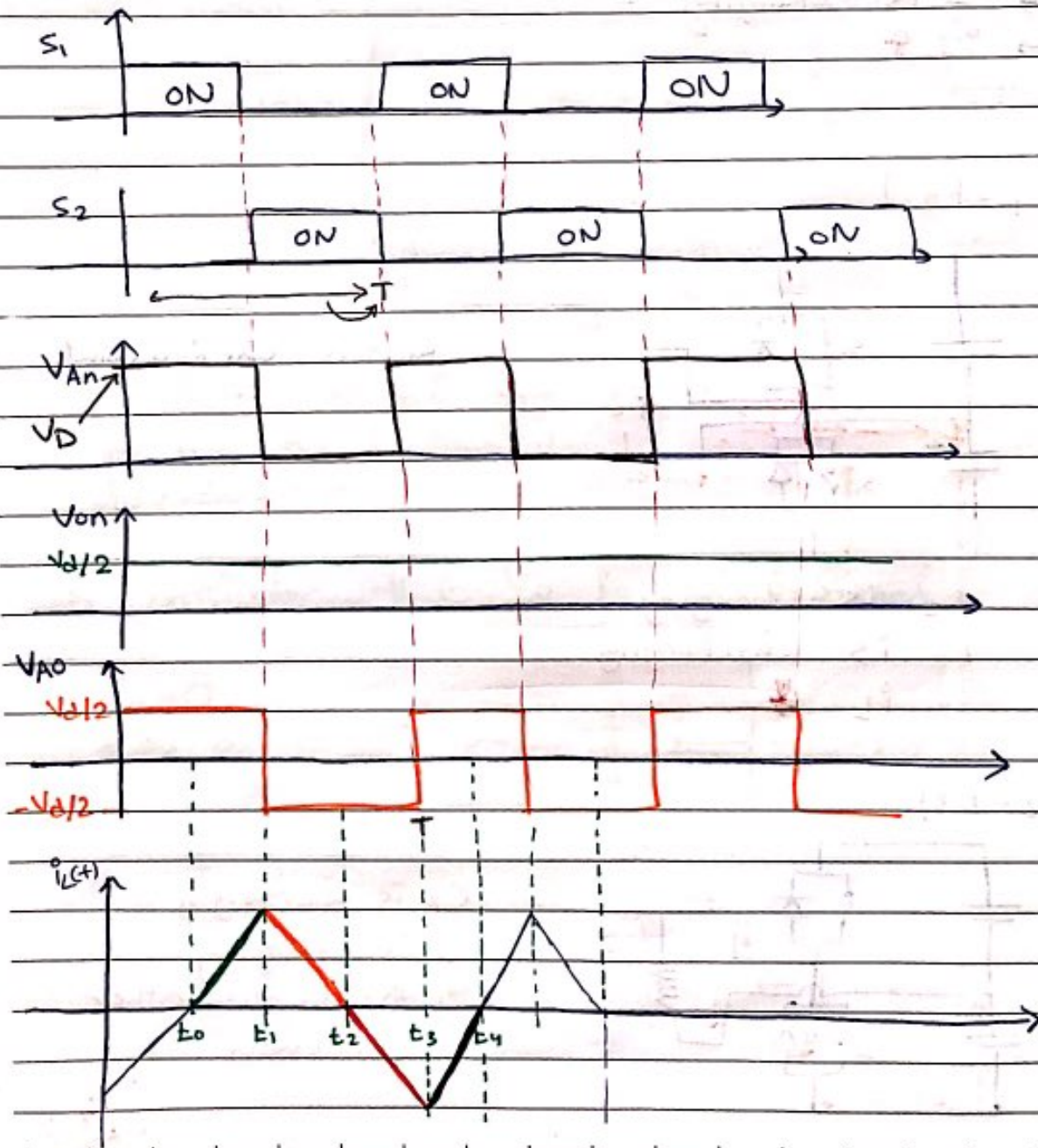


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* Single phase Inverter :-
One Leg :-

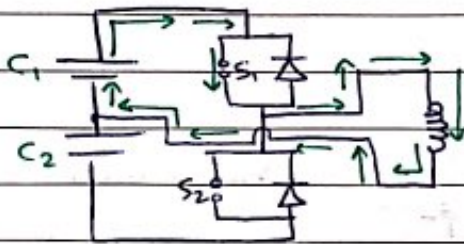


$$V_{AO} = V_{AN} - V_{ON}$$



$\Rightarrow (t_0 - t_1)$

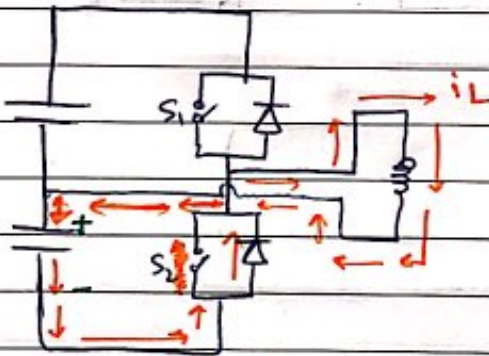
S_1 is ON, S_2 is OFF



Suppose we have a charging at C_1 :-

- $\rightarrow C_1$ is discharging
- $\rightarrow L$ is charging
- $\rightarrow i_L \uparrow$

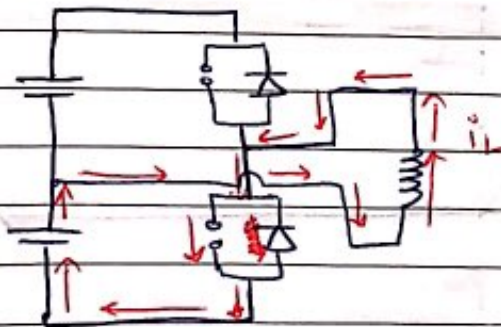
$\Rightarrow (t_1 - t_2)$



Switch uni directional.

- C_2 is charging.
- L is discharging.
- $i_L \downarrow$

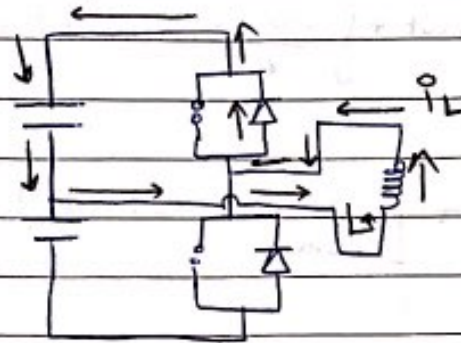
$\Rightarrow (t_2 - t_3)$



- C_2 is discharging
- L is charging
- $i_L \uparrow$ on the other direction

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$(t_3 - t_4)$



C_1 is charging
 L is discharging
 $i_L \downarrow$

* $V_{rms} = 8A$

$$V_{rms}(o) = \sqrt{\frac{1}{T} \int_0^{T/2} \left(\frac{V_d}{2}\right)^2 dt + \int_{T/2}^T \left(\frac{-V_d}{2}\right)^2 dt}$$

$$= \frac{V_d}{2} \Rightarrow \text{full of harmonic.}$$

→ We have to find the F.S of the output voltage to find the fundamental to filter the rest of the harmonic.

→ consider that V_o is odd signal :-

$$a_n = 0$$

$$a_0 = 0$$

$$b_n = \frac{2}{T} \int_0^T V_d(t) \sin n\omega t dt$$

$$= \frac{1}{\pi} \int_0^{2\pi} V_o(n\omega t) \sin n\omega t d\omega t$$



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$$= \frac{1}{\pi} \left[\int_0^{\pi} \frac{V_d}{2} \sin(n\omega t) d\omega t + \int_{\pi}^{2\pi} -\frac{V_d}{2} \sin(n\omega t) d\omega t \right]$$

$$= \frac{1}{\pi} \left[\frac{V_d}{2n} (-\cos(n\omega t)) \Big|_0^{\pi} + \left[\frac{-V_d}{2n} (-\cos n\omega t) \right]_{\pi}^{2\pi} \right]$$

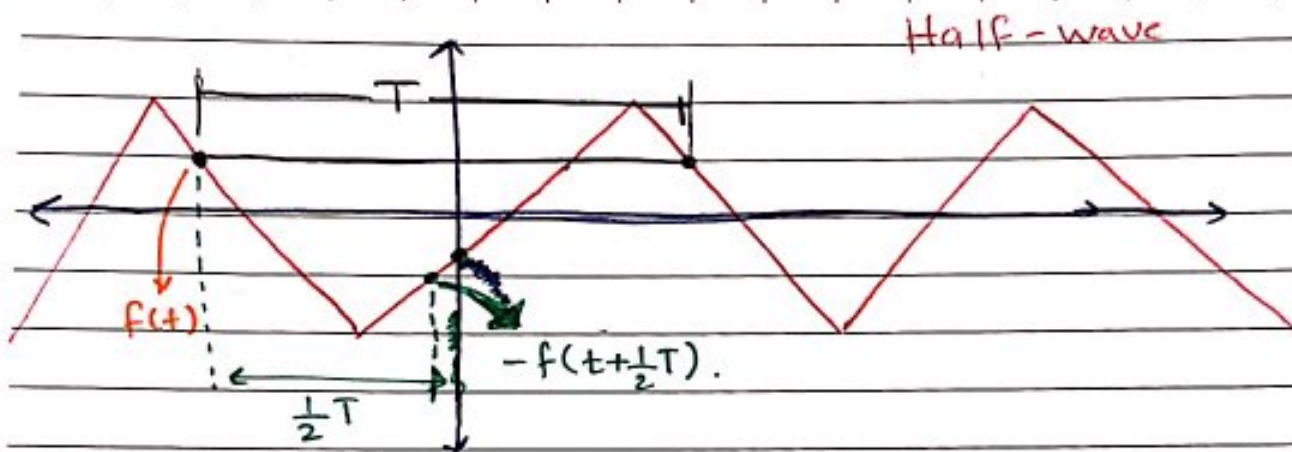
$$= \frac{2 V_d}{n\pi}$$

$$V_o(t) = \frac{V_o}{2} + \sum_{n=1,3,5}^{\infty} a_n \cos n\omega t + b_n \sin n\omega t$$

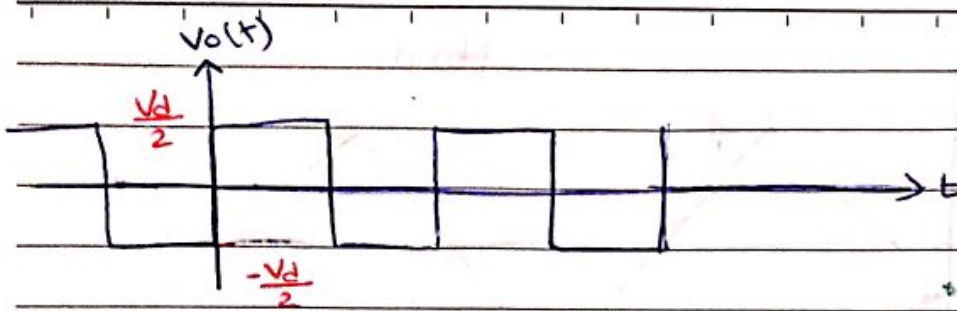
$$a_n = \frac{1}{\pi} \int_0^{2\pi} V_o(t) \cos n\omega t d\omega t$$

$$b_n = \frac{1}{\pi} \int_0^{2\pi} V_o(t) \sin n\omega t d\omega t$$

Symmetry		
Even	$f(-t) = f(t)$	$b_n = 0 \quad a_n = \frac{2}{\pi} \int_0^{\pi} f(t) \cos n\omega t dt$
odd	$f(-t) = -f(t)$	$a_n = 0 \quad b_n = \frac{2}{\pi} \int_0^{\pi} f(t) \sin n\omega t dt$
Half-wave Symmetric	$f(t) = -f(t + \frac{1}{2}T)$	$a_n = 0 = b_n (n \text{ even})$ $a_n = \frac{2}{\pi} \int_0^{\pi} f(t) \cos n\omega t d\omega t$ $b_n = \frac{2}{\pi} \int_0^{\pi} f(t) \sin n\omega t d\omega t$



Even quarter wave	Even and half wave	$b_n = 0$ $a_n = \begin{cases} \frac{4}{\pi} \int_0^{\pi/2} f(t) \cos n\omega t \, d\omega t & \text{odd} \\ 0 & \text{for } n \text{ even.} \end{cases}$
odd quarter wave	odd and half wave	$a_n = 0$ $b_n = \begin{cases} 0 & \text{for } n \text{ even} \\ \frac{4}{\pi} \int_0^{\pi/2} f(t) \sin n\omega t \, d\omega t & \text{odd} \end{cases}$



$$b_n = \frac{2V_d}{n\pi}$$

$$b_n = \frac{1}{\pi} \int_0^{\pi} \frac{V_d}{2} \sin(n\omega t) d\omega t + \int_{\pi}^{2\pi} -\frac{V_d}{2} \sin(n\omega t) d\omega t$$

Since the wave form is odd quarter wave

$$b_n = \frac{4}{\pi} \int_0^{\pi/2} \frac{V_d}{2} \sin(n\omega t) d\omega t = \frac{2V_d}{n\pi}$$

$$v_o(t) = \sum_{n=1}^{\infty} b_n \sin n\omega t$$

$$= \begin{cases} \sum_{n=1,3,5}^{\infty} \frac{2V_d}{n\pi} \sin n\omega t, & n \text{ is odd} \\ 0, & n \text{ is even} \end{cases}$$

fundamental of frequency :-

$$v_1(t) = \frac{2V_d}{\pi} \sin \omega t$$

This is the one I utilize

* RMS value of the fundamental :-

$$V_{rms} = \frac{2V_d}{\sqrt{2\pi}} = 0.45 V_d$$

For an R-L load :-

$$i_o(t) = \sum_{n=1}^{\infty} \frac{2V_d}{n\pi \sqrt{R^2 + (n\omega L)^2}} \sin(n\omega t - \Theta_n)$$

$$\Theta_n = \tan^{-1}\left(\frac{n\omega L}{R}\right)$$

$$I_{orms} = \frac{2V_d}{\sqrt{2\pi} \sqrt{R^2 + (\omega L)^2}}$$

I_{orms} = rms value of fundamental freq of output

$$P_{oi} = I_{orms}^2 R$$

$$* P_{oi} = \left[\frac{2V_d}{\sqrt{2\pi} \sqrt{R^2 + (\omega L)^2}} \right]^2 R$$

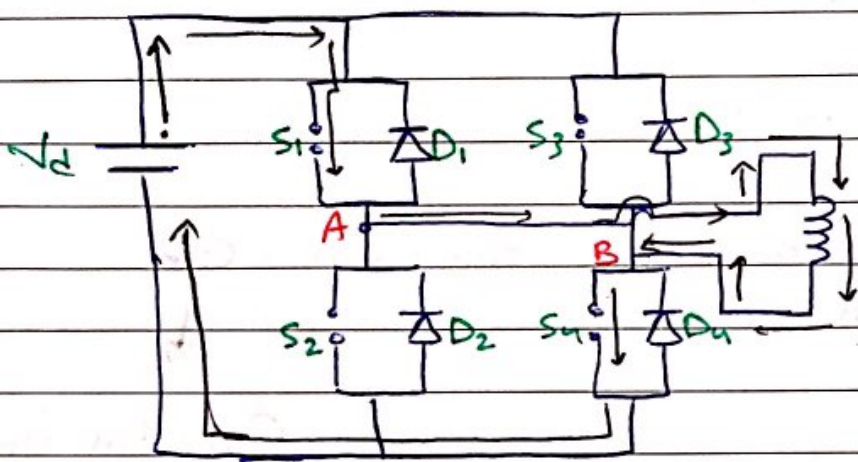
For an inductive load :-

$$\begin{aligned} i_o(t) &= \frac{1}{L} \int_0^t v(\tau) d\tau \\ &= \frac{1}{L} \int_0^{\frac{2\pi}{\omega}} \frac{2V_d}{\pi n} \sin(n\omega\tau) d\omega\tau \end{aligned}$$

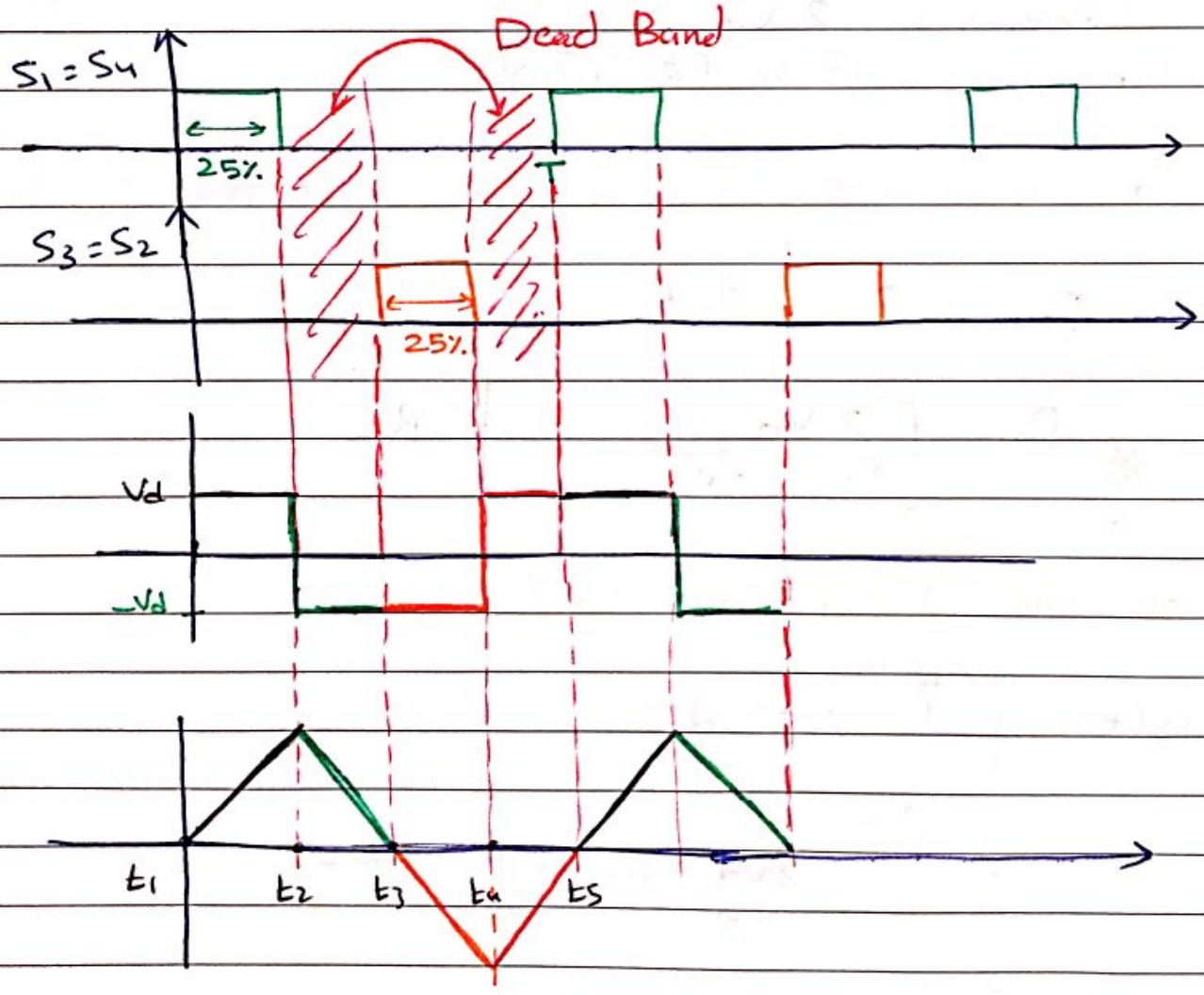
$$f = \frac{1}{T} = \frac{\omega}{2\pi}$$

Single Phase Inverters (Dead Band control)

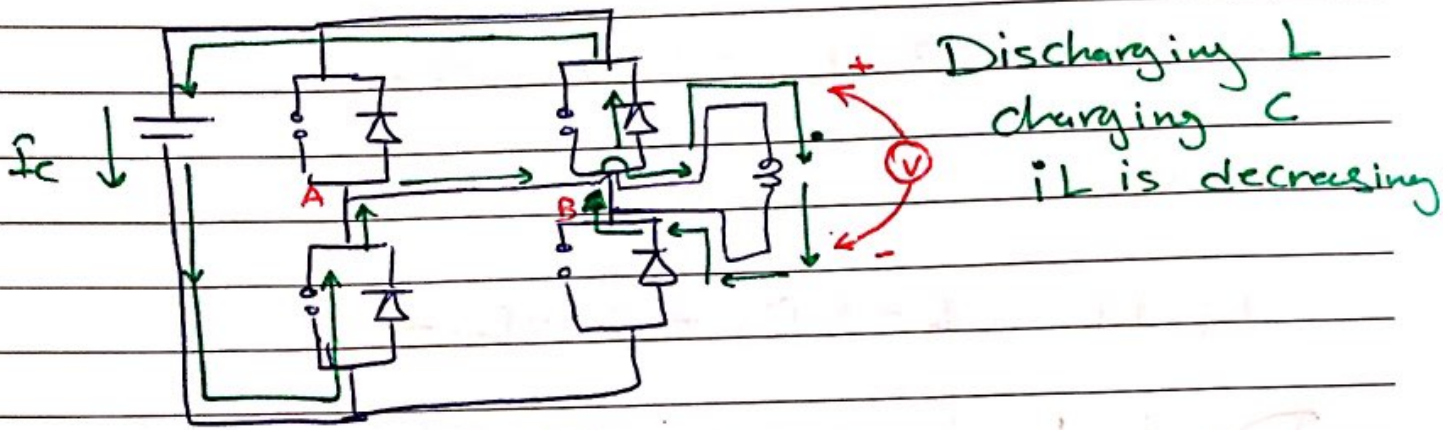
(H-Bridge)



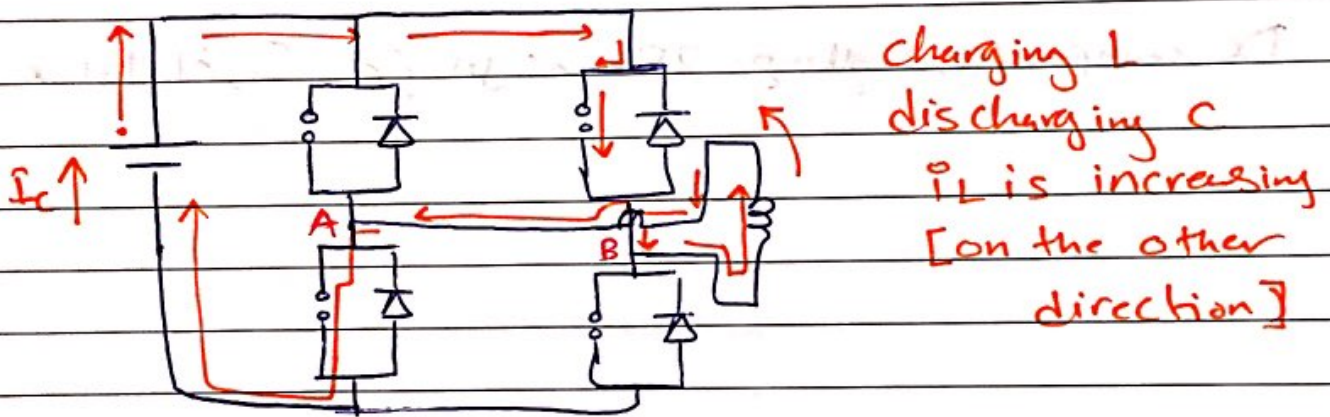
$S_1 = S_4 = 1$
 $[t_1 - t_2]$
 Discharging C
 $V_{AB} = V_d$
 Charging L
 $i_L \uparrow$



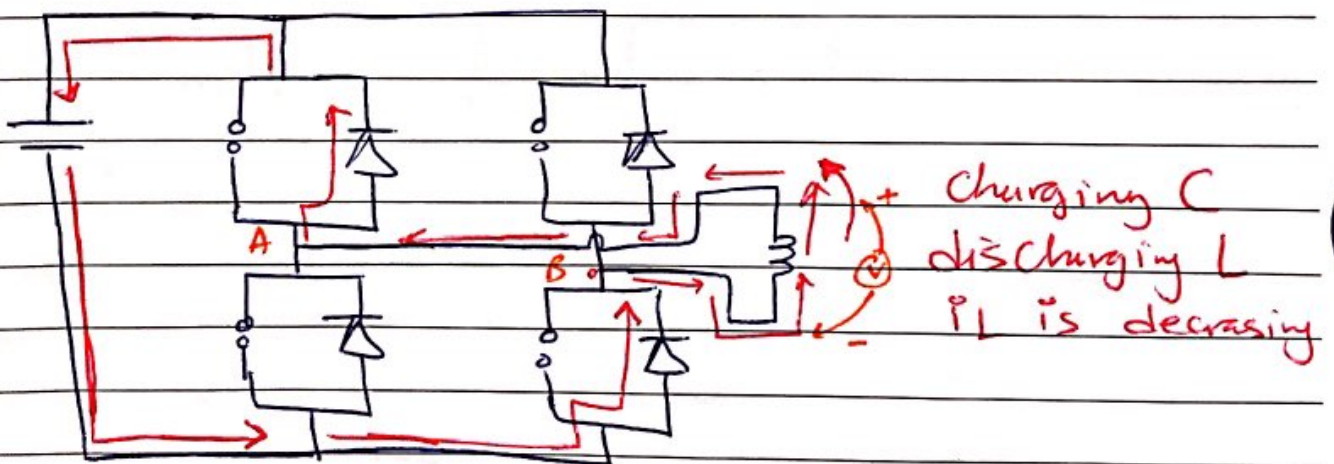
$S_x = 0 \quad (t_2 - t_3)$



$(t_3 - t_4) \quad S_2 = S_3 = 1$



$S_x = 0 \quad [t_4 - t_5]$



A connect to +ve voltage
B " " -ve "

$$t_1 - t_2 : C \rightarrow S_1 \rightarrow L \rightarrow S_4 \rightarrow C$$

$$t_2 - t_3 : L \rightarrow D_3 \rightarrow C \rightarrow D_2 \rightarrow L$$

$$t_3 - t_4 : C \rightarrow S_3 \rightarrow L \rightarrow S_2 \rightarrow C$$

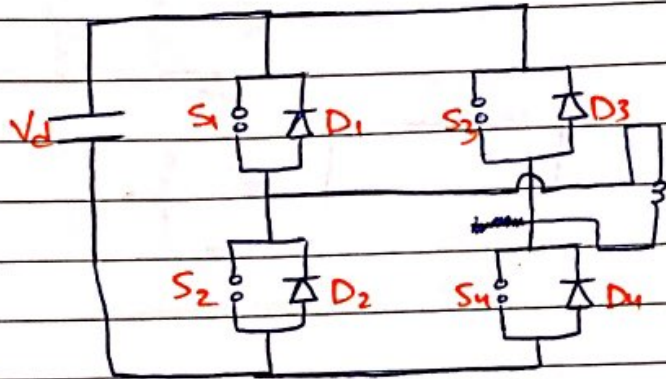
$$t_4 - t_5 : L \rightarrow D_1 \rightarrow C \rightarrow D_4 \rightarrow L$$

Dead band control ckt is studied to introduce phase shift control.

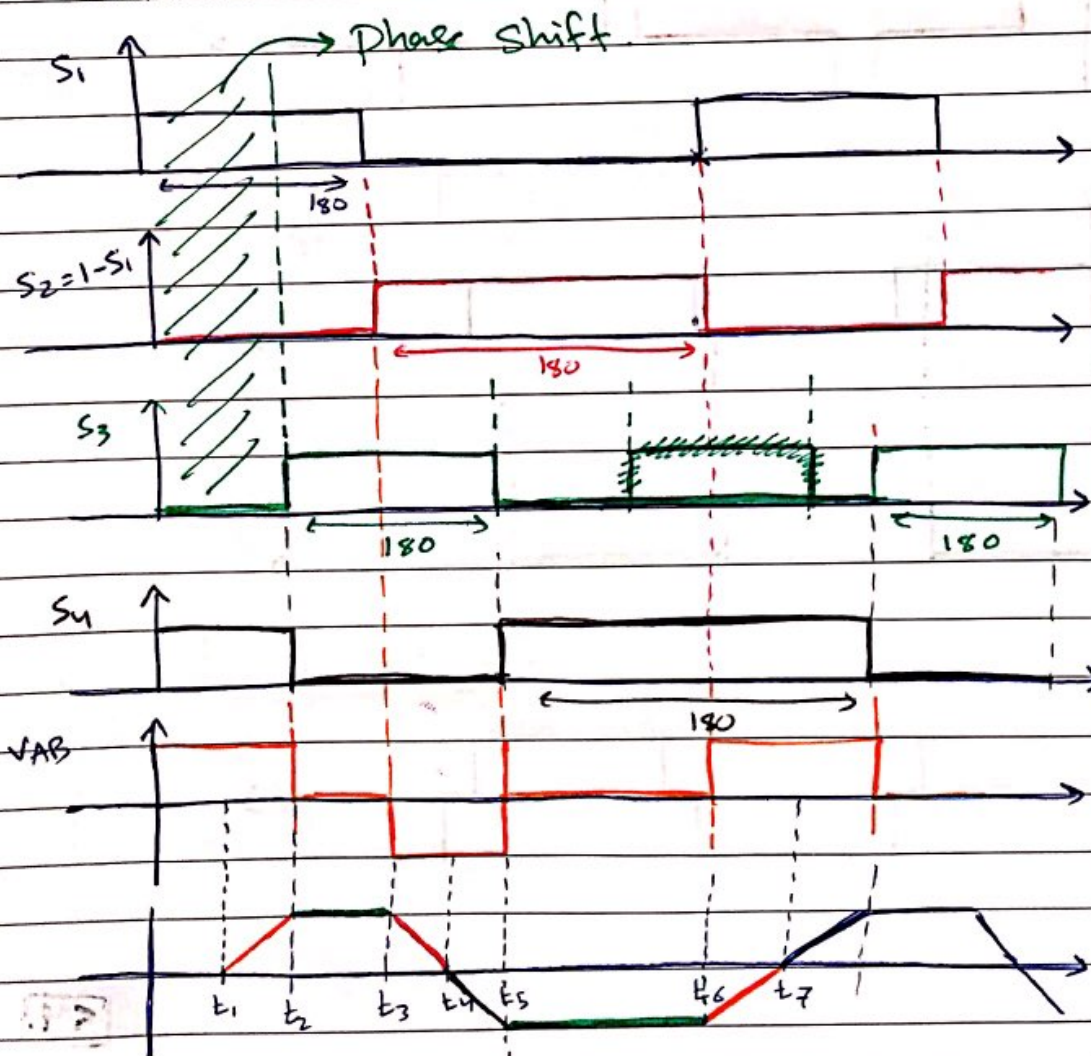
* إذا اُضرت فترة أقل من 25% من دورة الجهد، فإن DC component

Phase Shift Control:-

→ different switching technique.



→ the Dead band control technique is not fully Controllable.

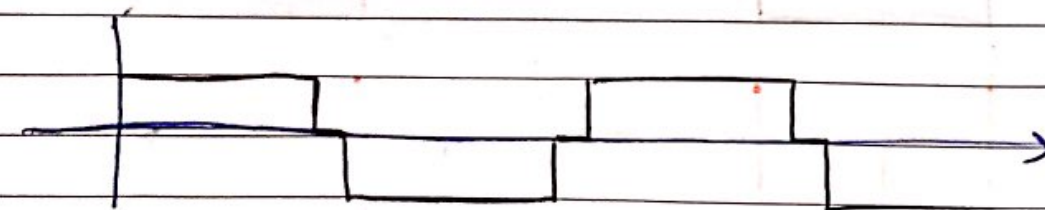
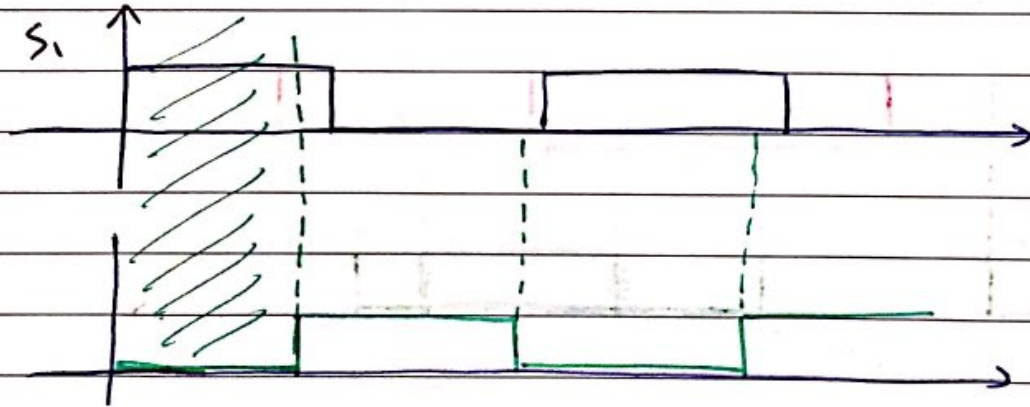
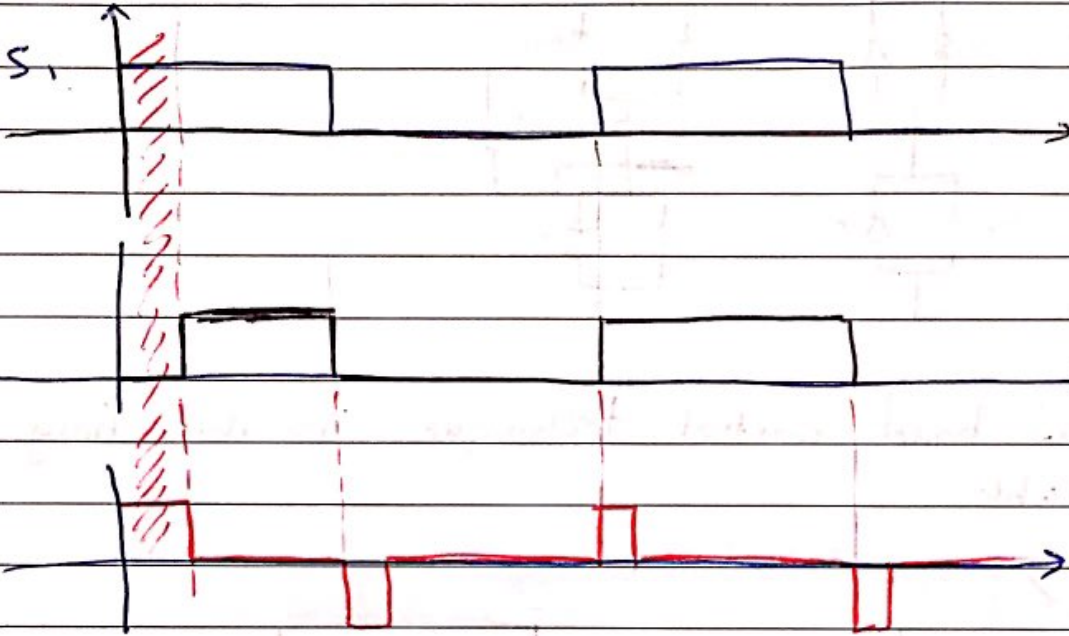


$$V_{AN} = S_1 V_d$$

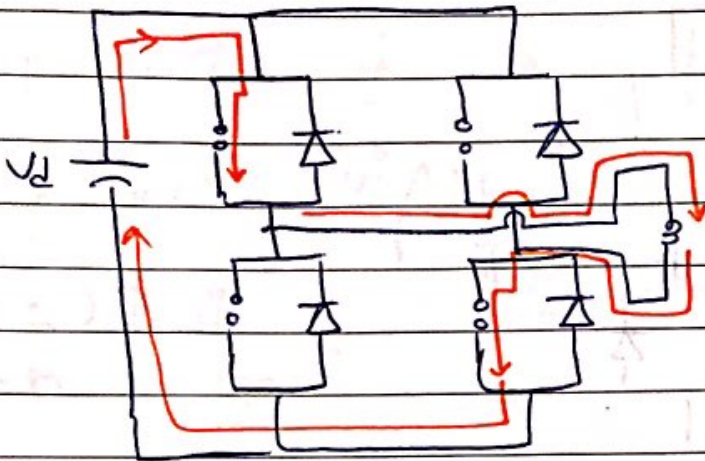
$$V_{BN} = S_3 V_d$$

$$V_{AB} = V_{AN} - V_{BN}$$

$$= V_d (S_1 - S_3)$$

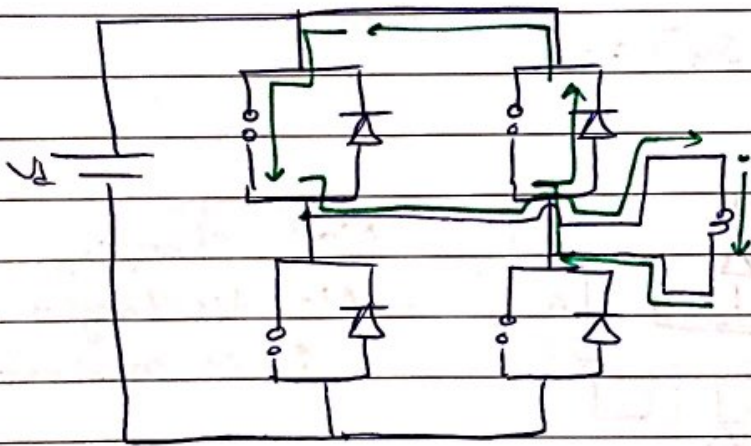


$[t_1 - t_2] [S_1 = 1 = S_4]$



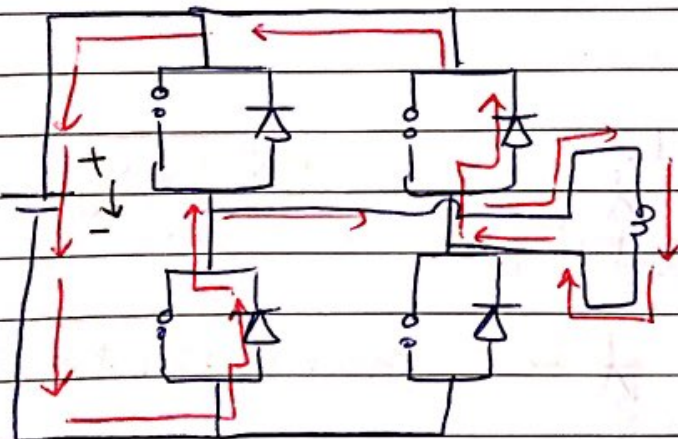
Discharge C
charging L
 $i_L \uparrow$
Path: $L \rightarrow S_4 \rightarrow C \rightarrow S_1$
 $\rightarrow L$

$(t_2 - t_3) [S_1 = 1 = S_3]$



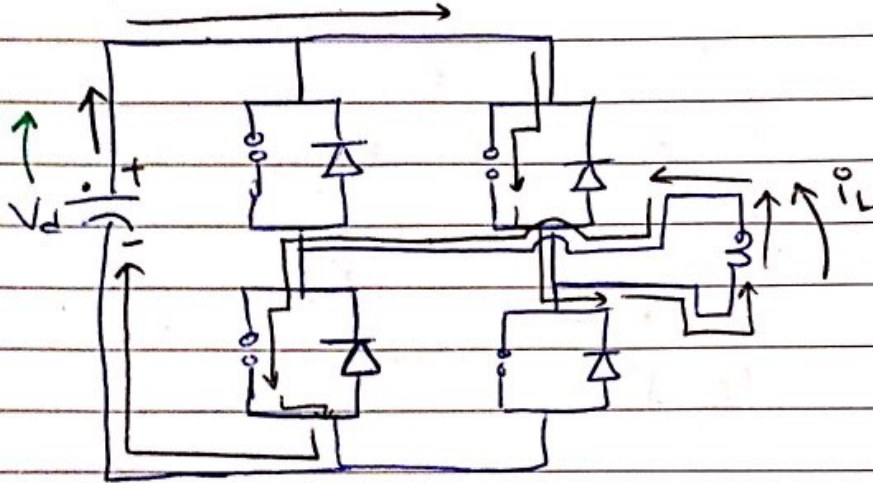
Not changing
Nor discharging
 i_L is constant.
Path: $L \rightarrow D_3 \rightarrow S_1 \rightarrow L$

$(t_3 - t_4) [S_2 = 1 = S_3]$



Discharging L
charging C
 $i_L \downarrow$
Path: $L \rightarrow D_3 \rightarrow C \rightarrow$
 $D_2 \rightarrow L$

* ($t_4 - t_5$) ($S_2 = 1 = S_3$)



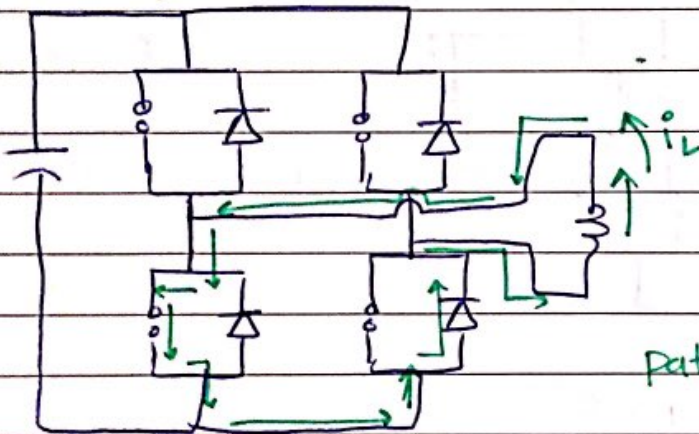
Discharging C

Charging L

$i_L \uparrow$ (with opposite direction)

path : $C \rightarrow S_3 \rightarrow L \rightarrow S_2 \rightarrow C$

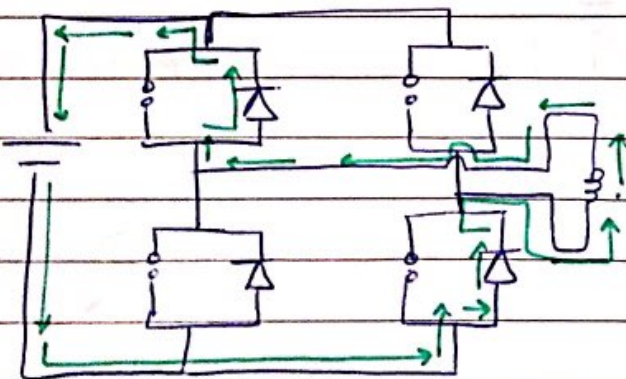
* ($t_5 - t_6$) [$S_2 = 1 = S_4$] :-



Not charging
Nor discharging
 i_L is constant

path: $L \rightarrow S_2 \rightarrow D_4 \rightarrow L$

* $t_6 - t_7$ ($S_1 = 1 = S_4$)

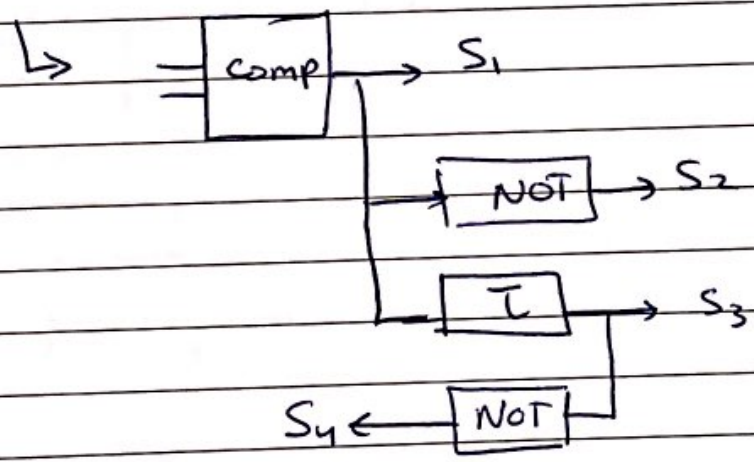
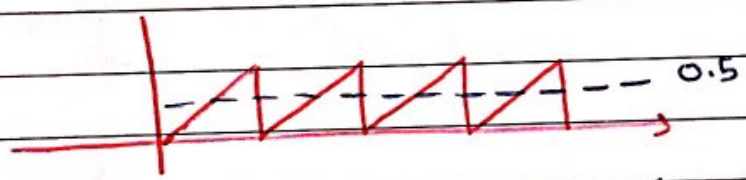
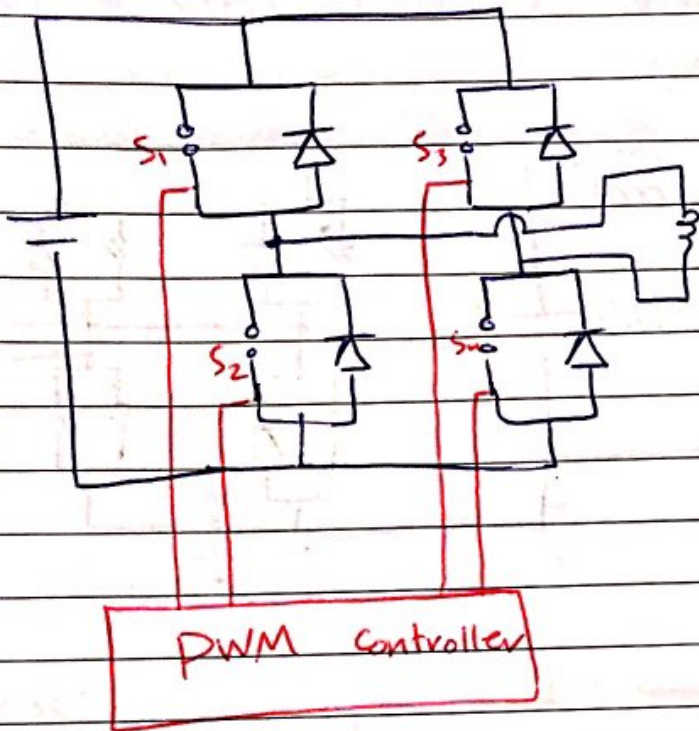


Discharging L

Charging C

$i_L \downarrow$

path: $L \rightarrow D_1 \rightarrow C \rightarrow D_4 \rightarrow L$



*** Homework 2:**

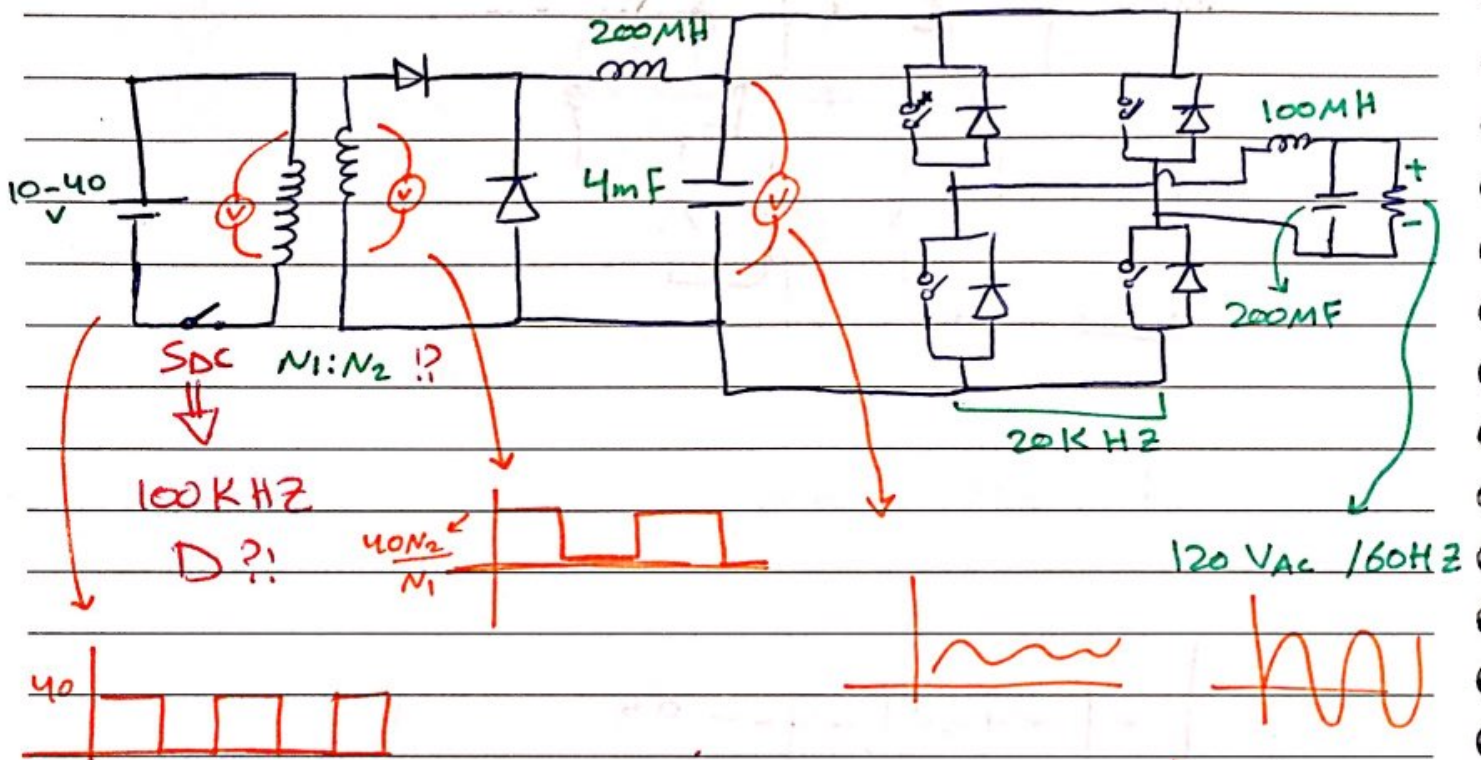
Microinverter are used in PV system to invert DC energy to single phase AC energy.

→ output voltage = 120V, 60 Hz

$V_{in} = [10 - 40VDC]$

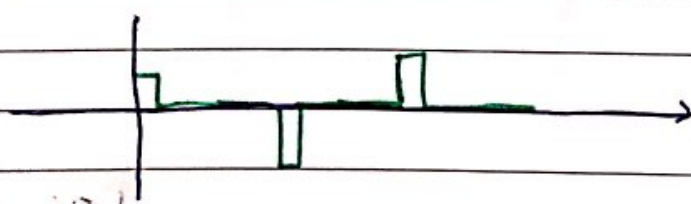
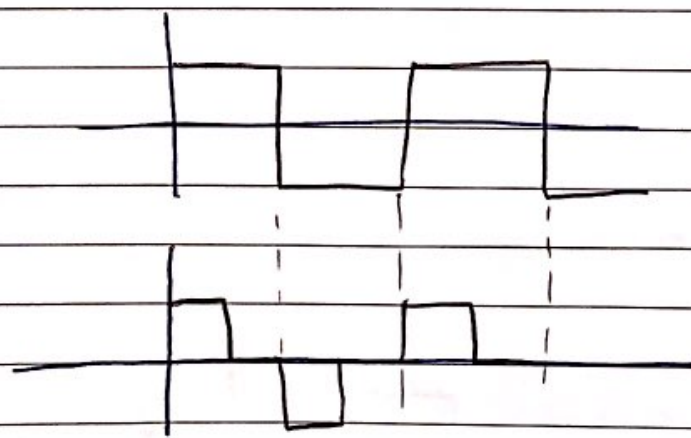
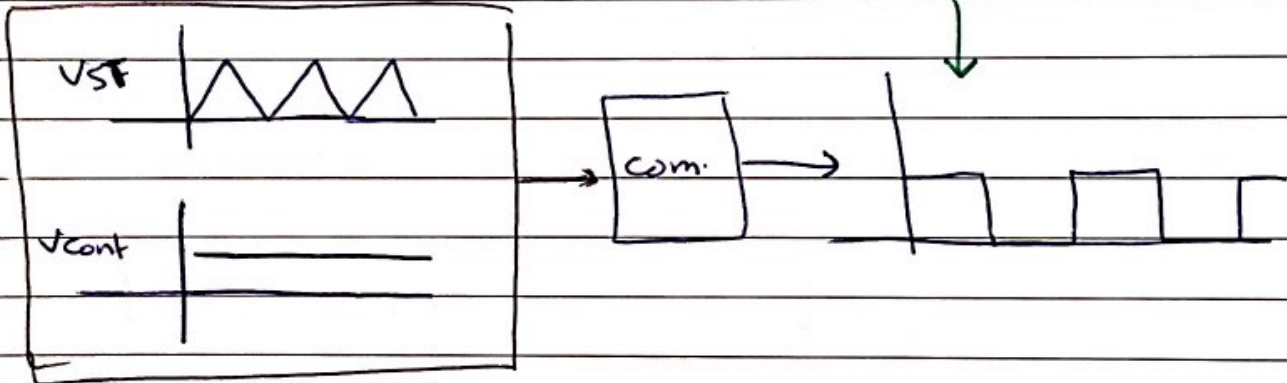
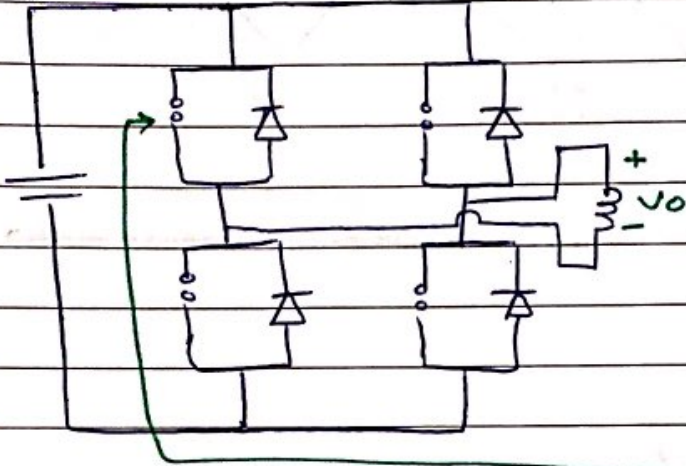
Do your own design of a PWM single phase

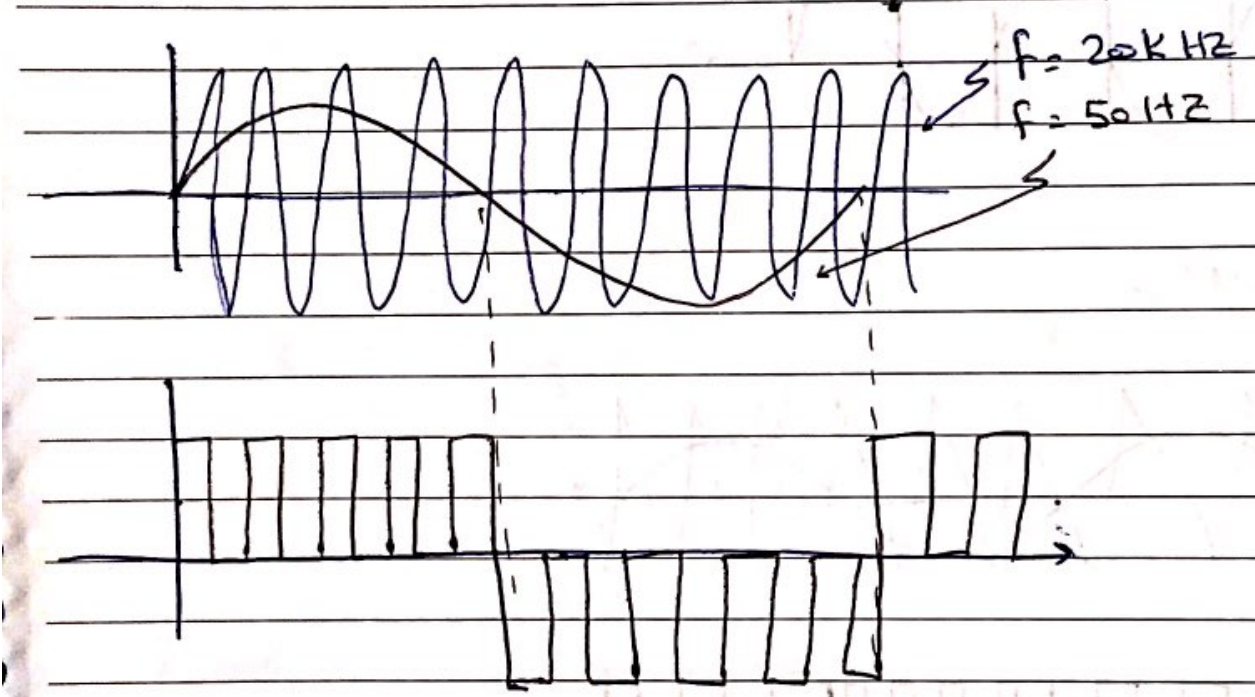
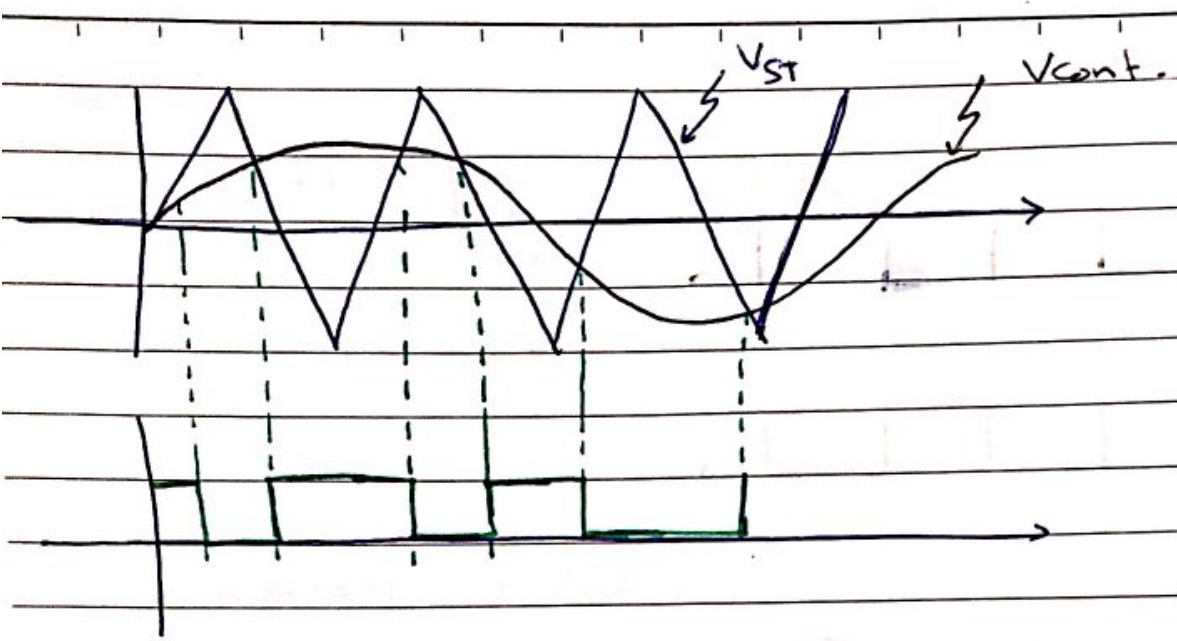
inverter and forward DC/DC Converter to have this output voltage.



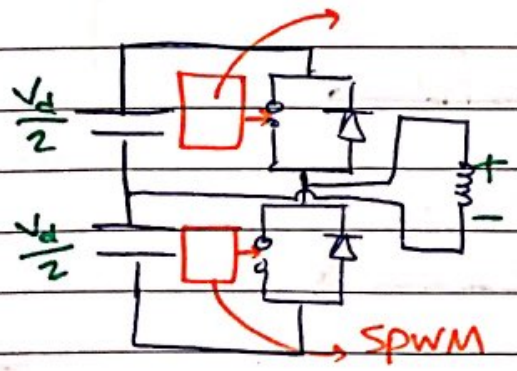
Sinusoidal PWM :-

Comparison between a sinusoidal pulse instead of a constant pulse width with V_{st}





Ex a single leg using SPWM

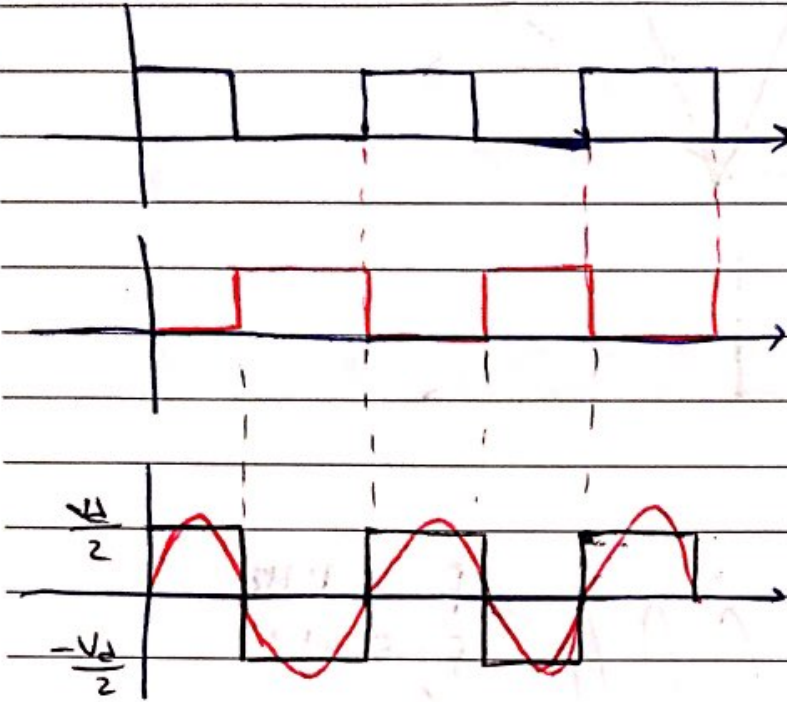


$$V_{AN} = V_d \times S_i$$

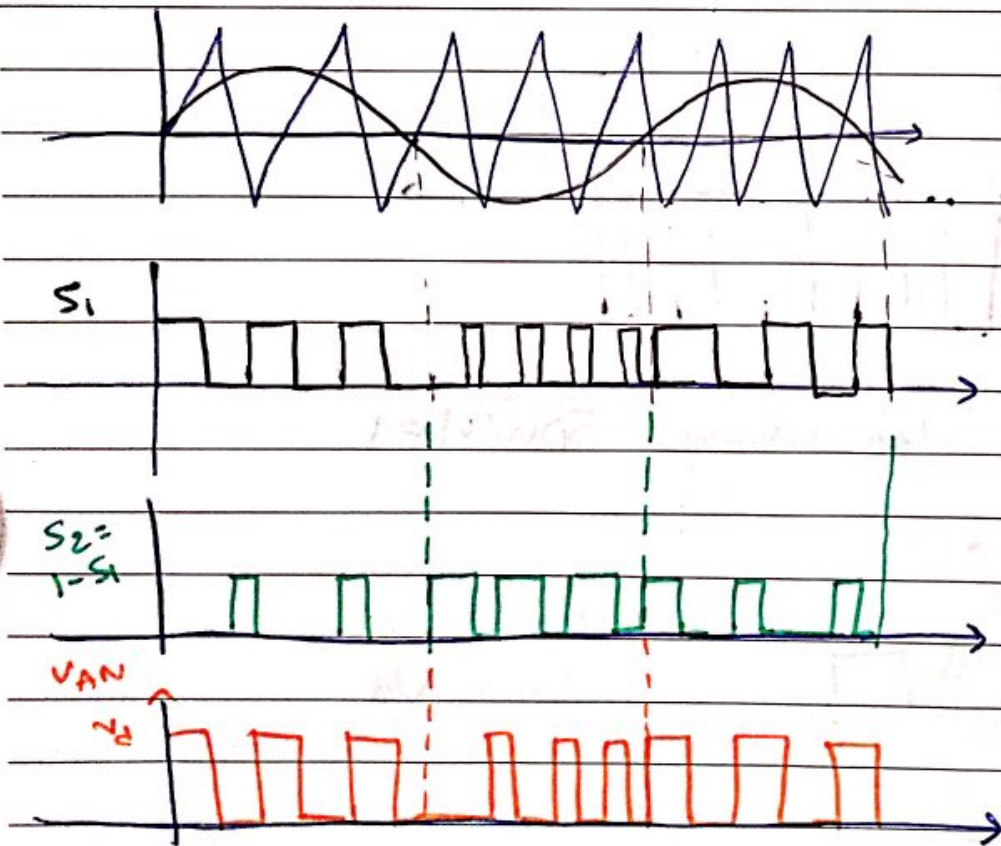
$$V_{ON} = \frac{V_d}{2}$$

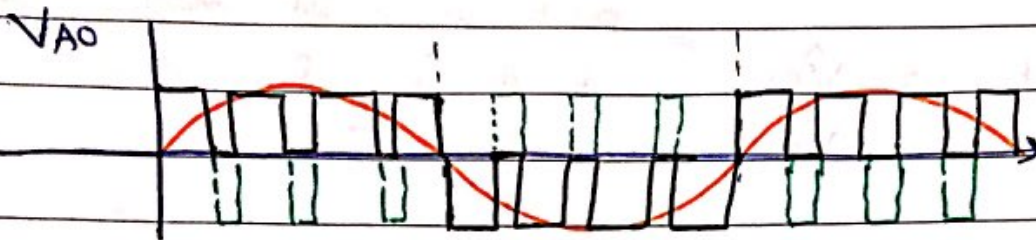
$$V_{AO} = V_{AN} - V_{ON}$$

PWM



SPWM:-





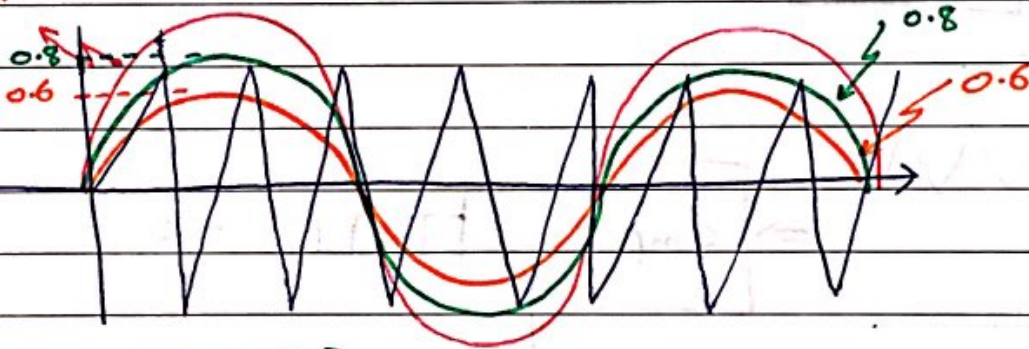
SPWM:-

* modulation index %

$$m_a = \frac{V_{cont}}{V_{tr}} = 0 \leq m_a \leq 1$$

$V_{cont} \equiv V_{control}$
 $V_{tr} \equiv V_{triangle}$

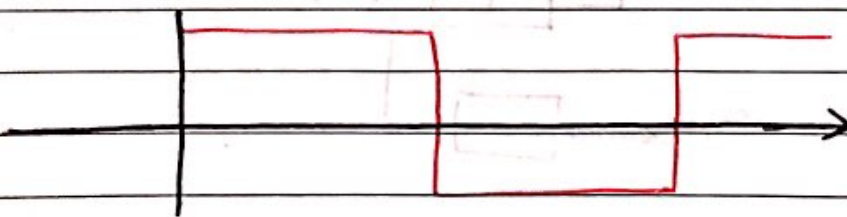
$m_a > 1$



$m_a = 0.8$

$m_a = 0.6$

Don't not over modulation :-



frequency Modulation :-

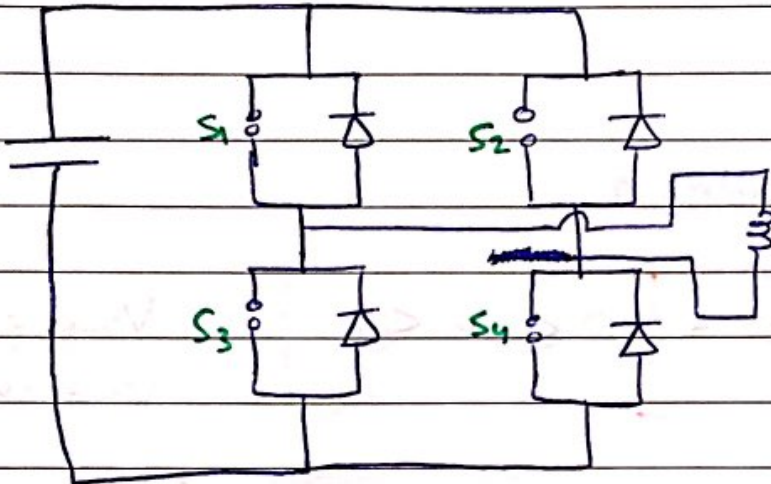
$m_f = \frac{f_s}{f_m}$ → frequency of $V_{triangular}$.

f_m → frequency of $V_{sinusoidal (control)}$

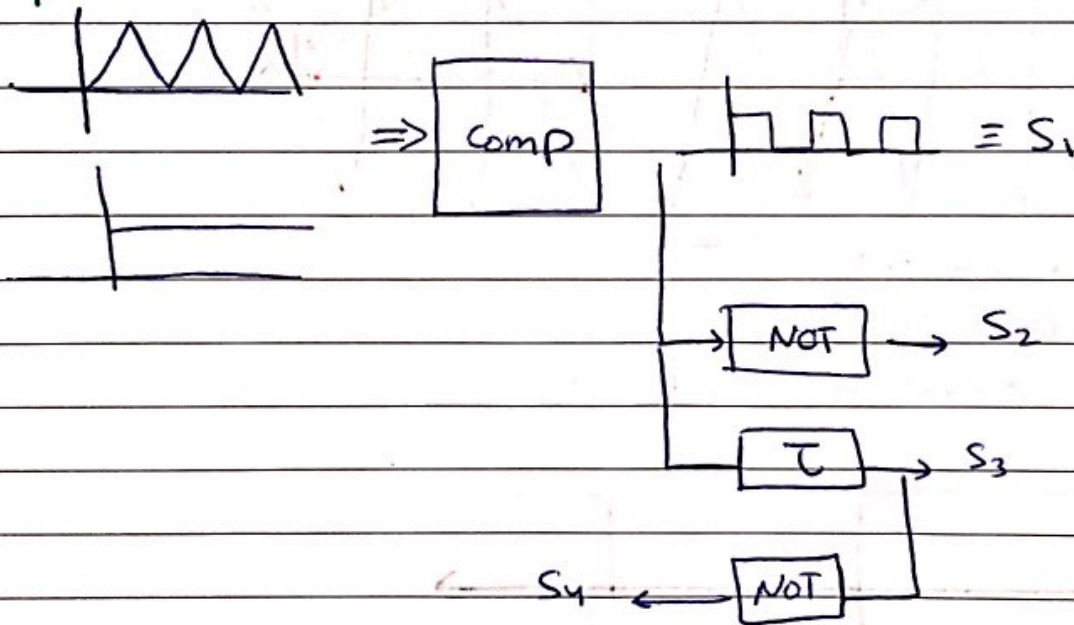
$m_f \gg 1$

$$m_a = \frac{V_{cont}}{V_{tr}} = \frac{\hat{V}_{o1}}{V_{dc}}$$

peak value of ~~output~~ the fundamental freq of the output signal.

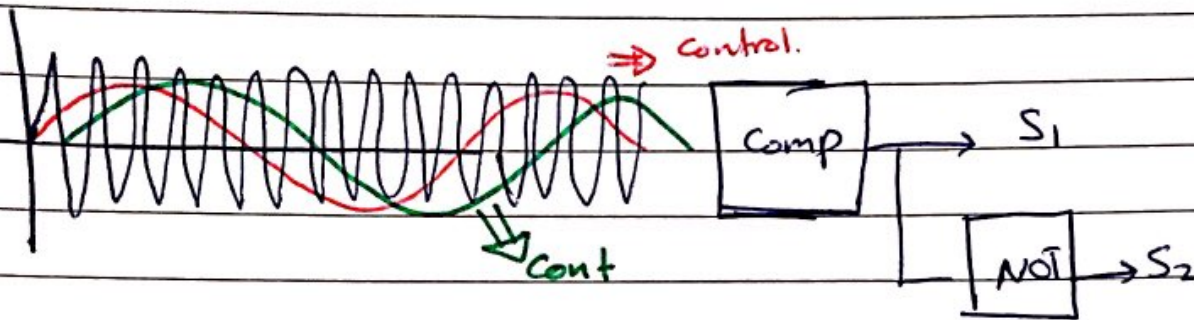


DWM:-

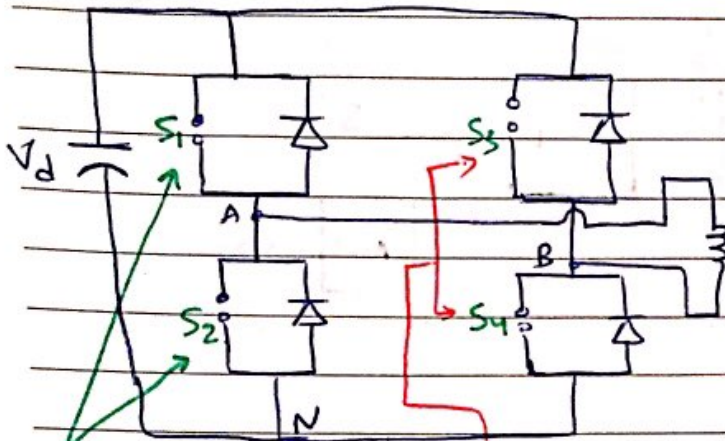


SPWM:-

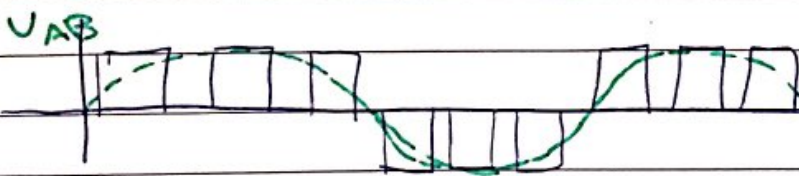
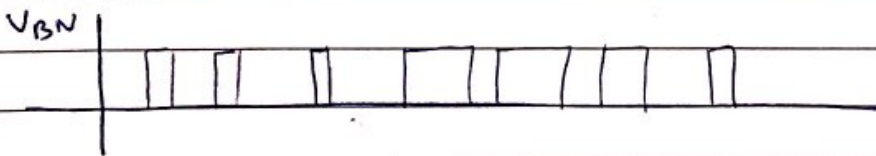
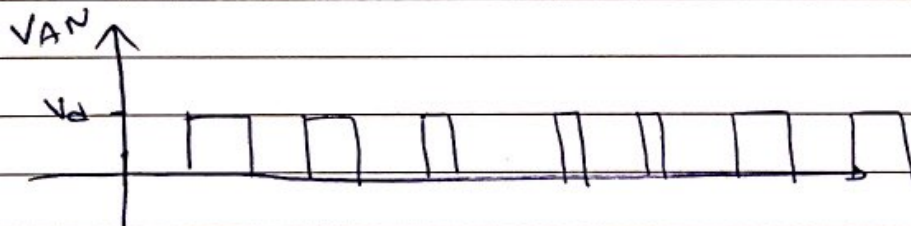
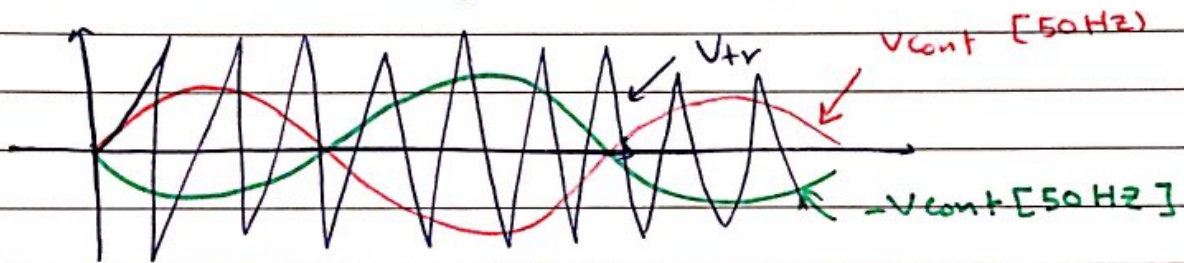
control signal



* Unipolar SPWM for Single phase Inverter Δ



V_{cont} and V_{tr} \rightarrow ($-V_{cont}$ and V_{tr})

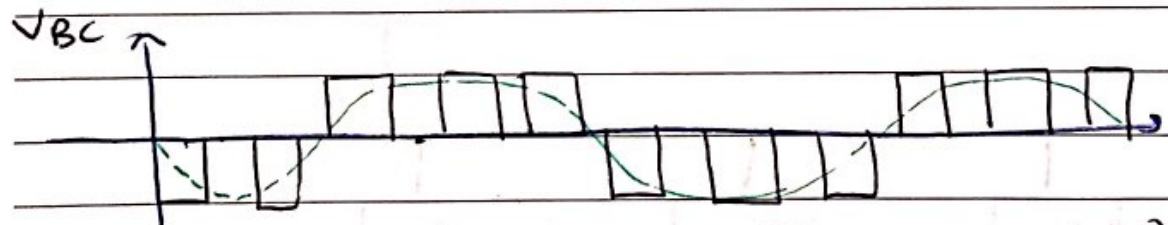
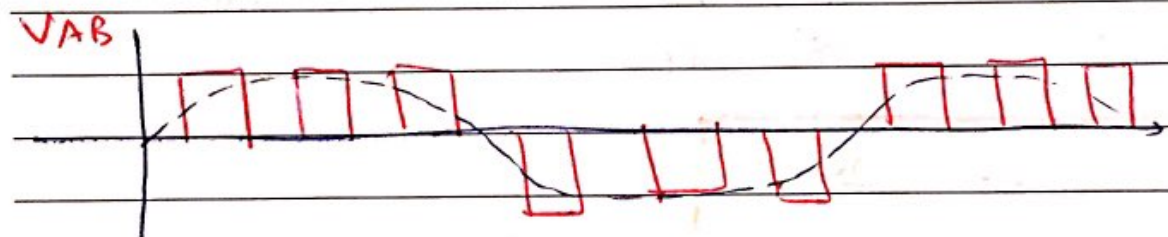
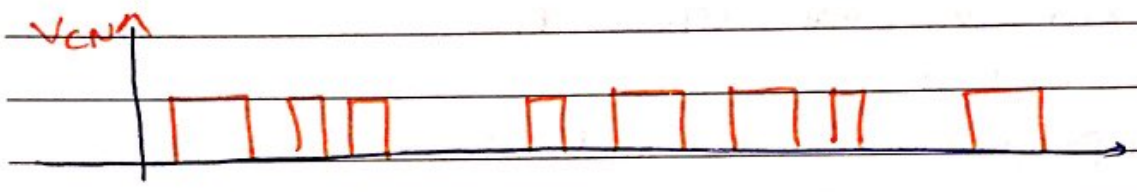
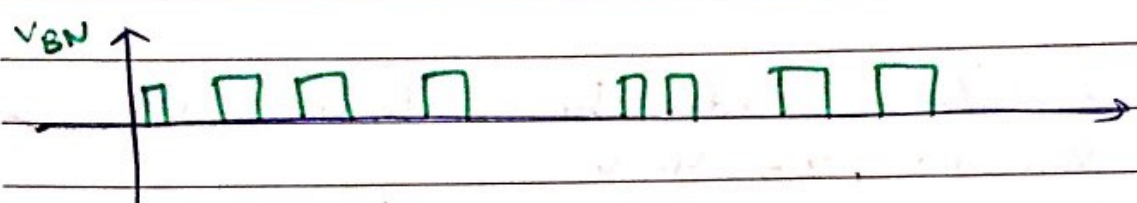
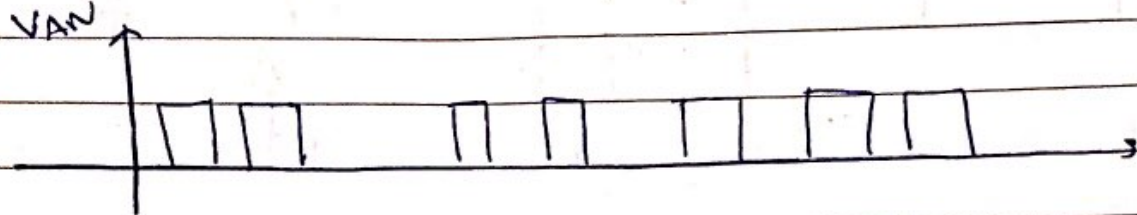
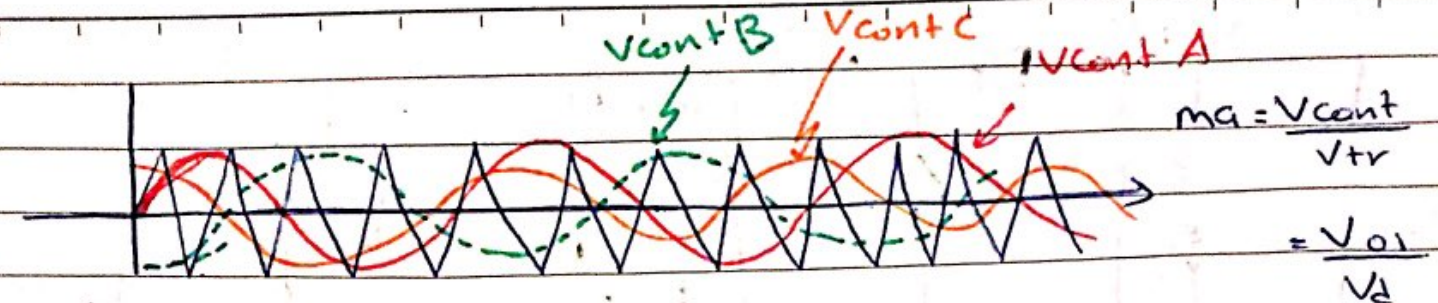


$V_{cont} > V_{tr}$: S_1 is ON $V_{AN} = V_d$

$V_{cont} < V_{tr}$: S_2 is ON $V_{AN} = 0$

$(-V_{cont}) > V_{tr}$: S_3 is ON $V_{BN} = V_d$

$(-V_{cont}) < V_{tr}$: S_4 is ON $V_{BN} = 0$



must connect either Δ Tr. or Δ load
 Y load will not get AC power.

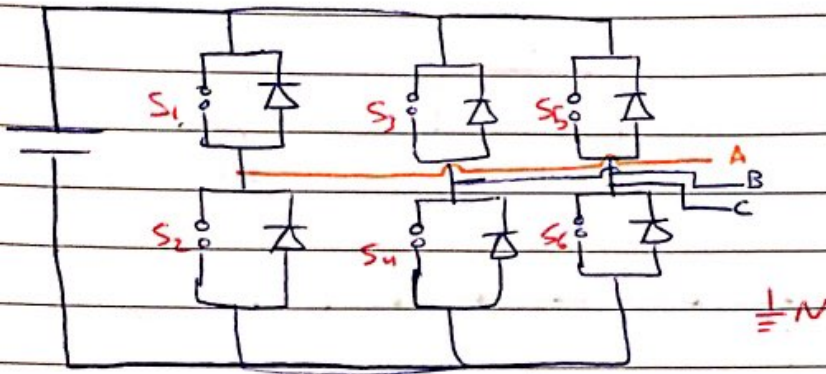
$$\left. \begin{aligned} V_{AN} &= S_1 V_d \quad (S_2 = 1 - S_1) \\ V_{BN} &= S_3 V_d \quad (S_4 = 1 - S_3) \\ V_{CN} &= S_5 V_d \quad (S_6 = 1 - S_5) \end{aligned} \right\} \begin{array}{l} 3 \text{ independent switches} \\ 3 \text{ complementary " } \end{array}$$

fundamental

$V_{LL1} = 0.612 m_a V_d$
 $V_{LL1 \text{ max}} = 0.612 V_d$

$m_a = 1$ [RMS]

3 ϕ inverters : Six step inversion :-



$$V_{an} = S_1 V_d \quad S_2 = 1 - S_1$$

$$V_{bn} = S_3 V_d \quad S_4 = 1 - S_3$$

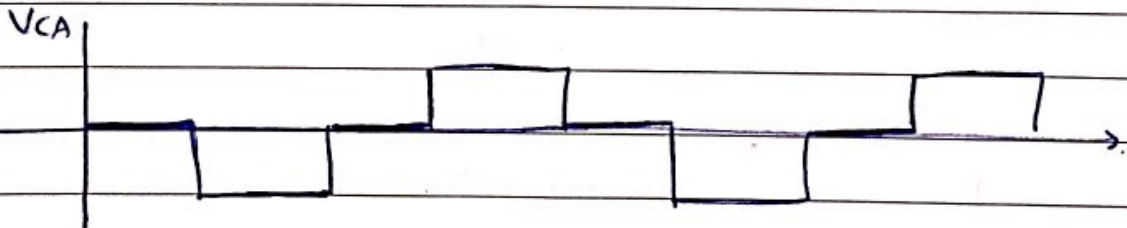
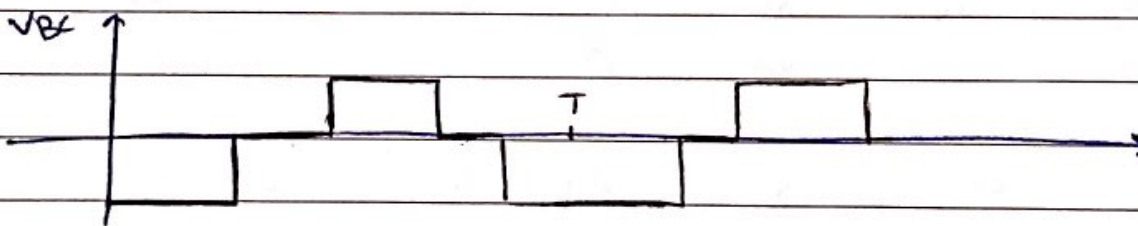
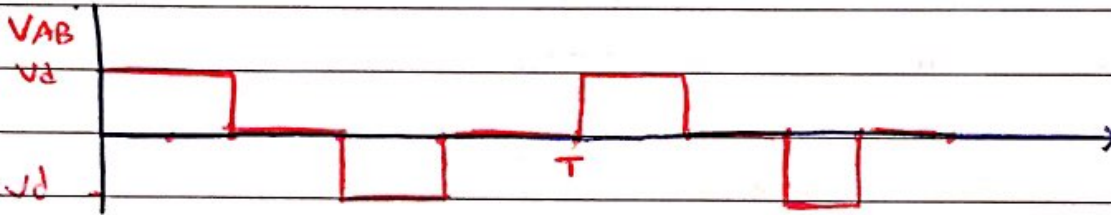
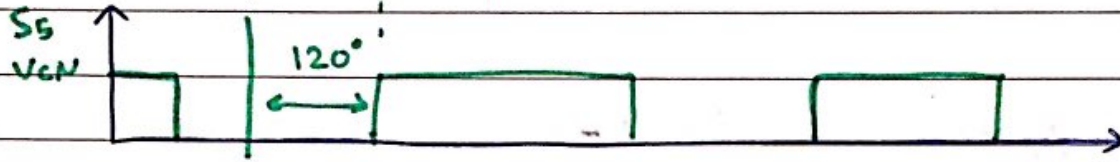
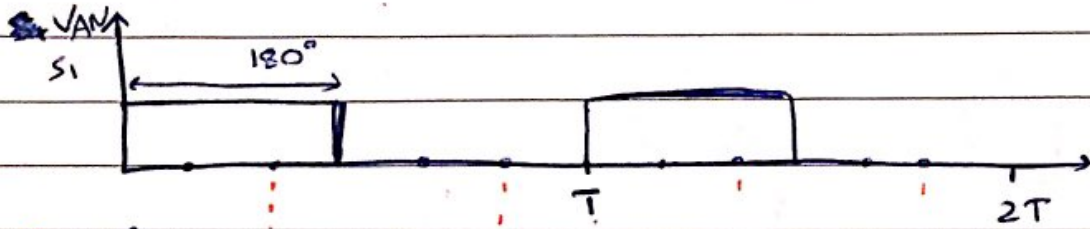
$$V_{cn} = S_5 V_d \quad S_6 = 1 - S_5$$

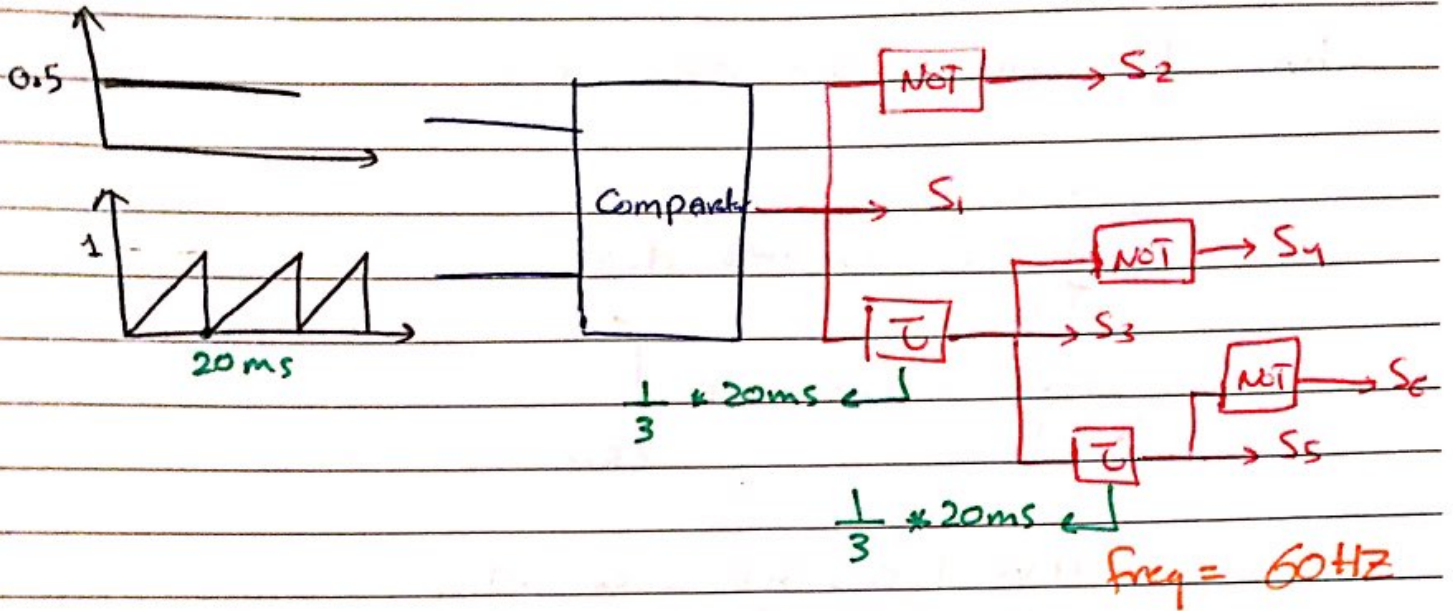
\Rightarrow 8 switching states [2^3]

	S_1	S_3	S_5	V_{AN}	V_{BN}	V_{CN}	V_{AB}	V_{BC}	V_{CA}
①	1	0	0	V_d	0	0	V_d	0	$-V_d$
②	1	1	0	V_d	V_d	0	0	V_d	$-V_d$
③	0	1	0	0	V_d	0	$-V_d$	V_d	0
④	0	1	1	0	V_d	V_d	0	0	V_d
⑤	0	0	1	0	0	V_d	V_d	$-V_d$	V_d
⑥	1	0	1	V_d	0	V_d	0	$-V_d$	0
⑦	0	0	0	0	0	0	0	0	0
⑧	1	1	1	V_d	V_d	V_d	0	0	0

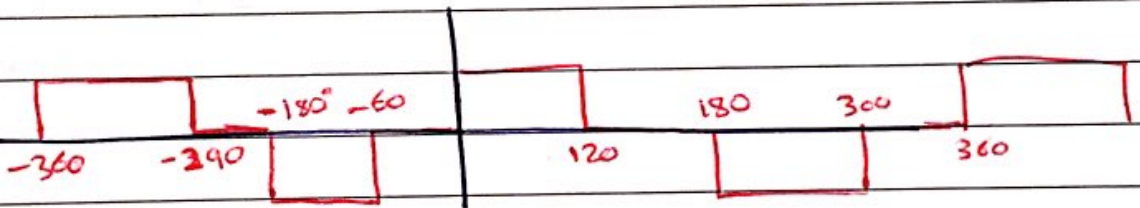
① \rightarrow ⑥ Active , ⑦ \rightarrow ⑧ \rightarrow Non active

$$V_{AN} = V_d S_1$$





$$V_{ab} = \frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos n\omega t + b_n \sin n\omega t$$



\rightarrow odd quarter wave symmetric.

$$a_n = 0 = a_0$$

$$b_n = 0 \text{ for } n \text{ even.}$$

100

$$b_n = \frac{4}{\pi} \int_0^{\pi/2} V_{AB}(t) \sin n\omega t \, d\omega t$$

$$= \frac{4}{\pi} \int_{\pi/6}^{\pi/2} V_d \sin n\omega t \, d\omega t$$

$$= \frac{4V_d}{n\pi} \left[-\cos n\omega t \right]_{\pi/6}^{\pi/2}$$

$$= \frac{4V_d}{n\pi} \left[\cos \frac{n\pi}{6} - \cos \frac{n\pi}{3} \right]$$

$$= \frac{4V_d}{n\pi} \sin\left(\frac{n\pi}{2}\right) \sin\left(\frac{n\pi}{3}\right)$$

= 0 for n = 3, 6, 9
triples

$$b_n = \begin{cases} 0 & n \text{ even.} \\ 0 & n = 3, 6, 9, 12, 15 \\ \frac{4V_d}{n\pi} \left(\frac{\sqrt{3}}{2}\right) & \text{elsewhere } [1, 5, 7, 11, 13, 17, 19] \end{cases}$$

$$V_{ab} = \sum_{n=1,5,7}^{\infty} \frac{4V_d}{n\pi} \left(\frac{\sqrt{3}}{2}\right) \sin \left[n(\omega t + \frac{\pi}{6}) \right]$$

$$V_{bc} = \sum_{n=1,5,7}^{\infty} \frac{4V_d}{n\pi} \left(\frac{\sqrt{3}}{2}\right) \sin \left[n(\omega t - \frac{\pi}{2}) \right]$$

101

$$V_{ca} = \sum_{n=1,3,5}^{\infty} \frac{4V_d}{n\pi} \left(\frac{\sqrt{3}}{2}\right) \sin\left[n(\omega t - \frac{7\pi}{6})\right]$$

$$V_{ab(1)} = \frac{4V_d}{\pi} \left(\frac{\sqrt{3}}{2}\right) \sin\left(\omega t + \frac{\pi}{6}\right)$$

The RMS value of the fundamental Δ

$$V_{ab(1)}_{rms} = \frac{4V_d}{\pi\sqrt{2}} \left(\frac{\sqrt{3}}{2}\right) = 0.7796 V_d$$



the highest value
from DC-3 ϕ AC
inversion.

The RMS value of the output signal [VAB]



$$V_{rms} = \sqrt{\frac{1}{2\pi} \left[\int_0^{2\pi/3} (V_d)^2 d\omega t + \int_{\pi/3}^{5\pi/3} (-V_d)^2 d\omega t \right]}$$

$$= \sqrt{\frac{2}{2\pi} \int_0^{2\pi/3} (V_d)^2 d\omega t}$$

$$= 0.8165 V_d$$

* Comparison between 6-step & SPWM

- Six step has no zero states while SPWM has.
- Switching frequency :-

SPWM → $f_s \gg f_{\text{fundamental}}$.

6-Step → $f_s = f_{\text{fundamental}}$.

- 6 step has lower order.

- 6 step has less lower order harmonics in its output voltage.

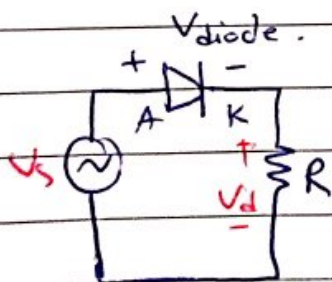
$$\text{6-step} \Rightarrow V_{LL}(n) = \frac{0.78 V_d}{n} \quad n = 1, 5, 7, 11$$

$$\text{SPWM} \Rightarrow V_{LL}(n) = \frac{0.61 V_d}{n} \quad n = 1, 3, 5, 7, 9$$

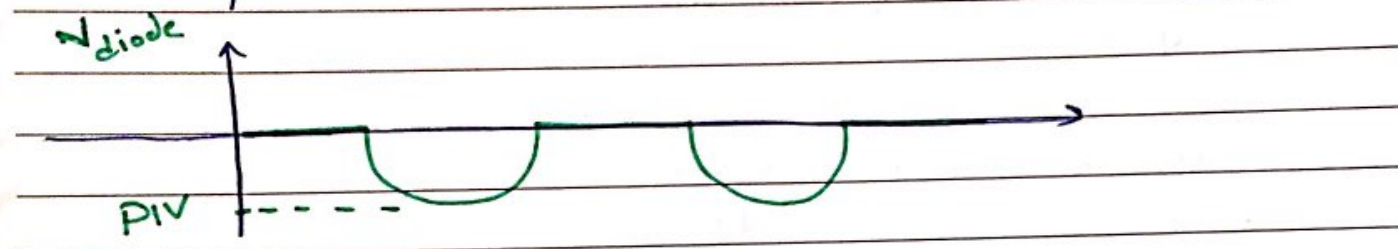
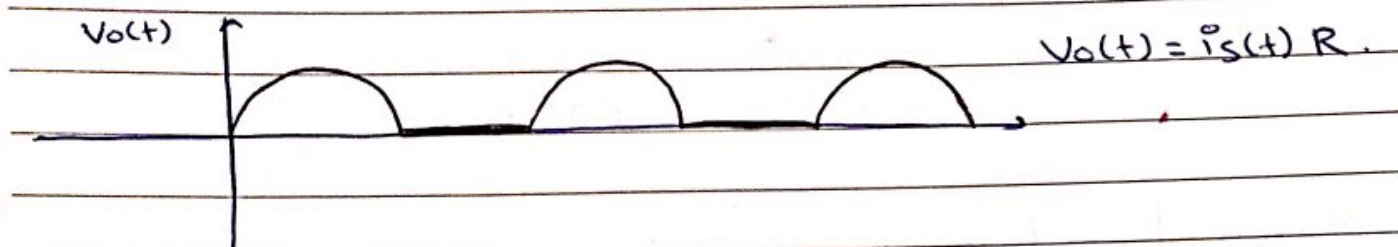
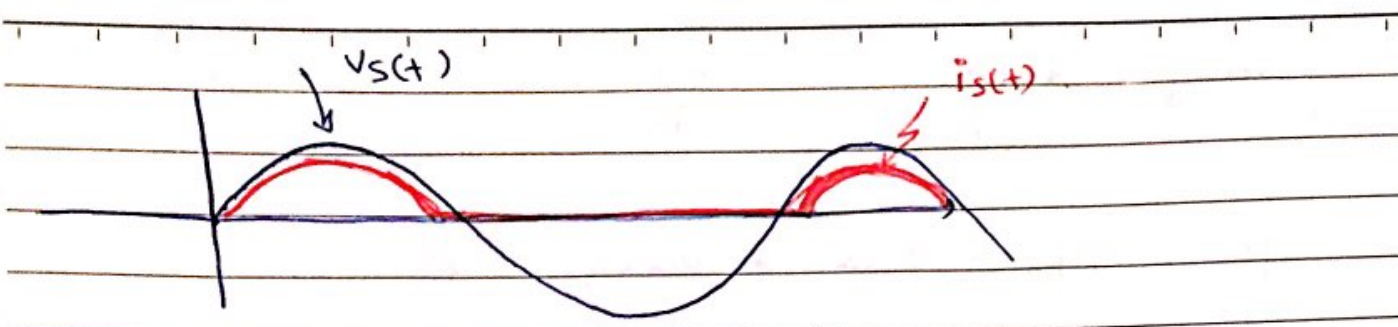
* AC to DC Conversion [Rectification]

- DC power supplies
- Utility to DC microgrids
- Electronics and home application.
- HVDC

Basic Rectifier Circuit :-



→ It works when it is FB
 $[V_A > V_K]$ and it prevents
 the current flow when
 $[V_K > V_A]$



PIV \equiv Peak Inverse voltage.

$$v_s(t) = \sqrt{2} V_{rms} \sin \omega t$$

$$= V_m \sin \omega t$$

$$i(t) = \begin{cases} \frac{\sqrt{2} V_{rms} \sin \omega t}{R} & 0 < \omega t < \pi \\ 0 & \text{else} \end{cases}$$

$$I_{oavg} = \frac{1}{2\pi} \int_0^{\pi} \frac{\sqrt{2} V_{rms} \sin(\omega t)}{R} d\omega t = \frac{\sqrt{2} V_{rms}}{2\pi R} \left[-\cos \omega t \right]_0^{\pi}$$

$$I_{oavg} = \frac{\sqrt{2} V_{rms}}{R\pi} = \frac{V_m}{R\pi}$$

$$V_{oavg} = \frac{1}{2\pi} \int_0^{\pi} \sqrt{2} V_{rms} \sin \omega t d\omega t$$

$$V_{oavg} = \frac{\sqrt{2} V_{rms}}{\pi} = \frac{V_m}{\pi}$$

$$P_{oavg} = P_{DC} = I_{oavg} * V_{oavg}$$

$$P_{oavg} = \frac{2V_m^2}{R\pi^2} = \frac{V_m^2}{R\pi^2}$$

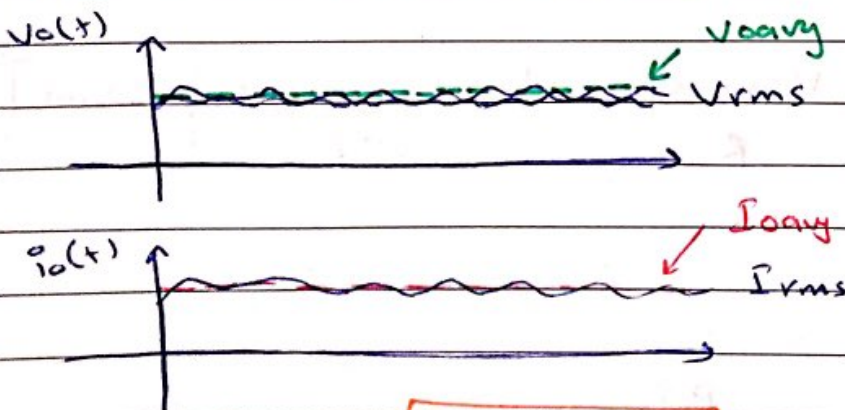
$$V_{o,rms} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} V_m^2 \sin^2 \omega t \, d\omega t}$$

$$V_{o,rms} = \frac{V_m}{2} = \frac{V_{rms}}{\sqrt{2}}$$

$$\Rightarrow I_{o,rms} = \frac{V_{o,rms}}{R} = \frac{V_m}{2R} = \frac{V_{rms}}{\sqrt{2}R}$$

$$P_{AC} = V_{rms} I_{rms}$$

$$\Rightarrow P_{AC} = \frac{V_m^2}{4R} = \frac{V_{rms}^2}{2R}$$



$$P_{DC} = V_{oavg} * I_{oavg}$$

$$P_{AC} = V_{rms} * I_{rms}$$

$$\eta = \frac{P_{DC}}{P_{AC}}$$

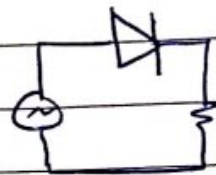
η = Conversion efficiency

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Ex Find the performance parameter for a single phase half wave rectifier.

1) η ?!

$$\eta = \frac{P_{DC}}{P_{AC}} = \frac{V_m^2 / R \pi^2}{V_m^2 / 4R} = 40.53\%$$



2) Find the form factor:-

$$FF = \frac{V_{rms}}{V_{dc}} \quad [\text{need to be } 1]$$

$$FF = \frac{V_m/2}{V_m/\pi} = \pi/2 = 1.57$$

$$FF = 1 \rightarrow V_{rms} = V_{dc} \quad (\text{good conversion})$$

3) Find the ripple factor ?!

$$RF = \sqrt{\frac{(V_{rms})^2}{V_{dc}^2} - 1} = \sqrt{(FF)^2 - 1} = \sqrt{(1.57)^2 - 1}$$

$$RF = 1.211$$

4) PIV of Diode ?!

$$PIV = V_m = \sqrt{2} V_{rms}$$

5) Find the power factor of the ckt.

$$PF \triangleq \frac{\text{Real power}}{\text{apparent power}} = \frac{P}{S}$$

RMS value of output

$$PF = \frac{V_{rms} \cdot I_{rms}}{V_{sin} \cdot I_{sin}} = \frac{V_{rms}/\sqrt{2} \times V_{rms}/R\sqrt{2}}{V_{rms} \times V_{rms}/\sqrt{2}R} = \frac{1}{\sqrt{2}}$$

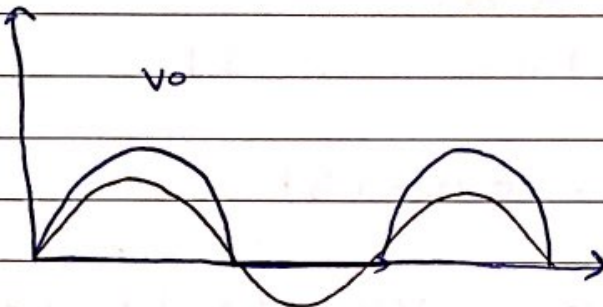
RMS value of the input

$$PF = 0.707$$

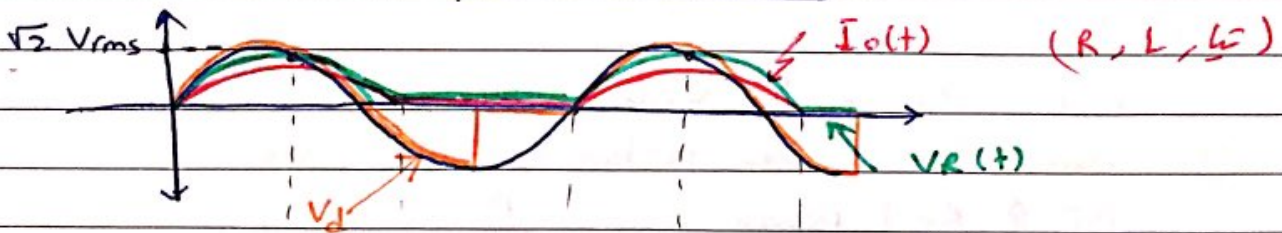
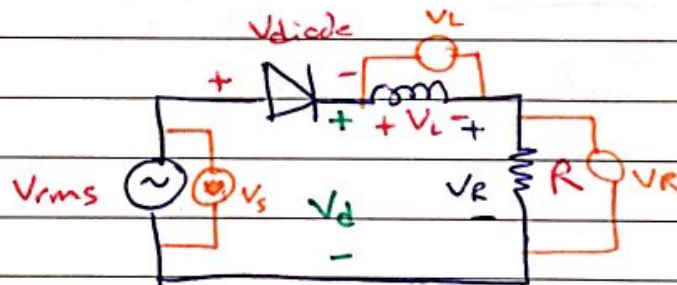
* we only use RMS value in Real life.

$$* THD_c = \sqrt{\frac{I_o^2 - I_{o1}^2}{I_{s1}^2}} = \frac{\sqrt{\sum_{n=2}^{\infty} I_n^2}}{|I_{n1}|}$$

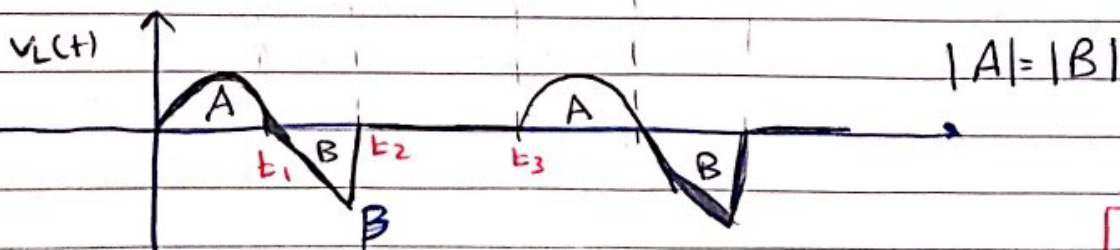
$$* THD_v = \sqrt{\frac{V_o^2 - V_{o1}^2}{V_{s1}^2}} = \frac{\sqrt{\sum_{n=2}^{\infty} V_n^2}}{|V_{n1}|}$$

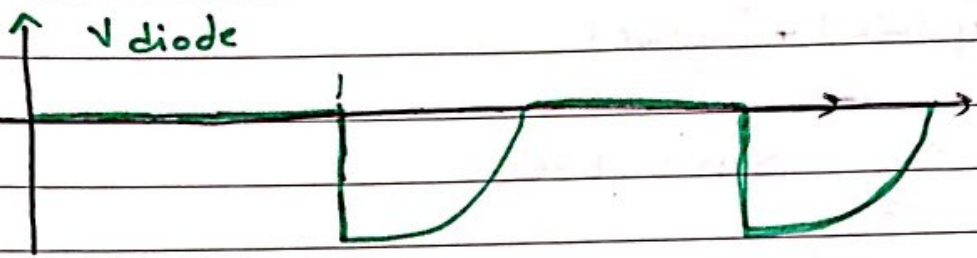
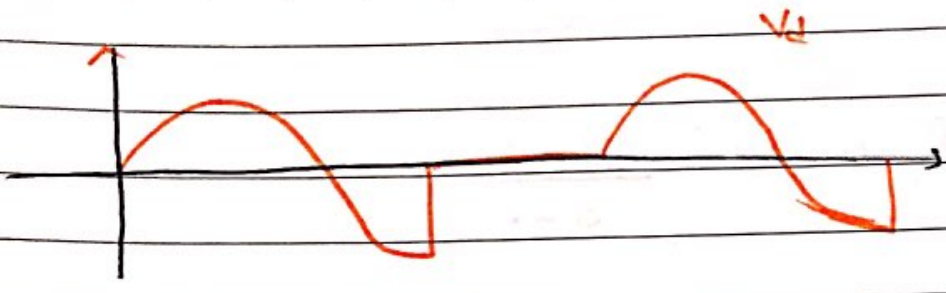


* HWR with R-L Load



$V_L = V_s - V_R$
 ... voltage across Inductor





* Inductor will not change its current abruptly
 It will change its polarity instantaneously when
 the diode is ON & Δ

$$V_L(t) = V_S(t) + V_R(t)$$

$$V_L(t) = L \frac{di_L(t)}{dt}$$

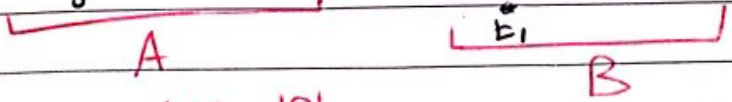
"0 mean initial condition not zero."
 condition

$$i_L(t) = \frac{1}{L} \int_0^t V_L(\tau) d\tau$$

* $\int_0^t \sin \omega t = -\cos \omega t \Big|_0^t = \cos \omega t - 1$?!

$$i_L(t) = \frac{1}{L} \int_0^{t_3} V_L(\tau) d\tau$$

$$= \frac{1}{L} \int_0^{t_1} V_L(\tau) d\tau + \frac{1}{L} \int_{t_1}^{t_2} V_L(\tau) d\tau$$



$$|A| = |B|$$

$$V_m = \sqrt{2} V_{rms}$$

$$V_m \sin(\omega t) = R i(\omega t) + L \frac{di(\omega t)}{d\omega t}$$

$$i(\omega t) = i_f(\omega t) + i_n(\omega t)$$

$$\Rightarrow i_f(\omega t) = \frac{V_m}{Z} \sin(\omega t - \theta)$$

$$\Rightarrow i_n(\omega t) = A e^{-\frac{\omega t}{\tau}}$$

$$Z = \sqrt{R^2 + (\omega L)^2}$$

$$\theta = \tan^{-1}\left(\frac{\omega L}{R}\right)$$

$$\tau = \frac{L}{R}$$

$$i(0) = 0 = \frac{V_m}{Z} \sin(-\theta) + A$$

$$A = \frac{V_m}{Z} \sin \theta$$

$$i(\omega t) = \frac{V_m}{Z} \left[\sin(\omega t - \theta) + \sin(\theta) e^{-\frac{\omega t}{\tau}} \right]$$

$$i(\beta) = 0 = \frac{V_m}{Z} \left[\sin(\beta - \theta) + \sin(\theta) e^{-\beta/\omega\tau} \right]$$

$$\sin(\beta - \theta) + \sin(\theta) e^{-\beta/\omega\tau} = 0$$

$$\theta = \pi/3, \omega = 2\pi f, \tau = 10^{-3}$$

$$\text{Solve } \left[\sin\left(X - \frac{\pi}{3}\right) + \sin\left(\frac{\pi}{3}\right) e^{-X/2\pi f \times 10^{-3}} \right] \Rightarrow X = \beta = 225^\circ$$

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$$i(\omega t) = \begin{cases} \frac{V_m}{Z} \sin(\omega t - \theta) + \sin \theta e^{-\frac{\omega t}{\tau}}, & 0 \leq \omega t \leq \beta \\ 0, & \beta < \omega t < 2\pi \end{cases}$$

$$V_{d \text{ avg}} = \frac{1}{2\pi} \int_0^{\beta} V_m \sin(\omega t) \cdot d\omega t = \frac{V_m}{2\pi} [1 - \cos(\beta)]$$

$$I_{o \text{ avg}} = \frac{V_{o \text{ avg}}}{\sqrt{R^2 + (\omega L)^2}} = \frac{V_m [1 - \cos \beta]}{2\pi \sqrt{R^2 + (\omega L)^2}}$$

$$= \frac{1}{2\pi} \int_0^{\beta} i(\omega t) d\omega t.$$

$$V_{\text{rms}} = \sqrt{\frac{1}{2\pi} \int_0^{\beta} V_m^2 \sin^2(\omega t) d\omega t}$$

$$= \sqrt{\frac{1}{2\pi} \int_0^{\beta} V_m^2 \left(\frac{1}{2} - \frac{1}{2} \cos(2\omega t) \right) d\omega t}$$

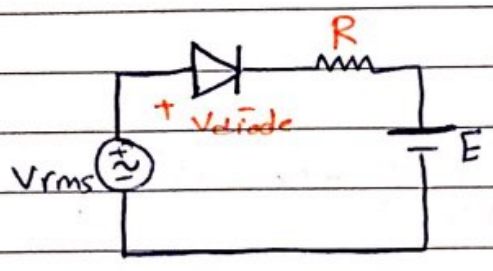
$$= \sqrt{\frac{V_m^2}{2\pi} \left[\frac{1}{2} \beta - \frac{1}{4} \sin 2\beta \right]}$$

$$= \frac{V_m}{2\sqrt{\pi}} \sqrt{\beta - \frac{1}{2} \sin(2\beta)}$$

Radian

* HWR with E & R

↳ Battery



$$-V_m \sin \omega t + V_{diode} + E = 0$$

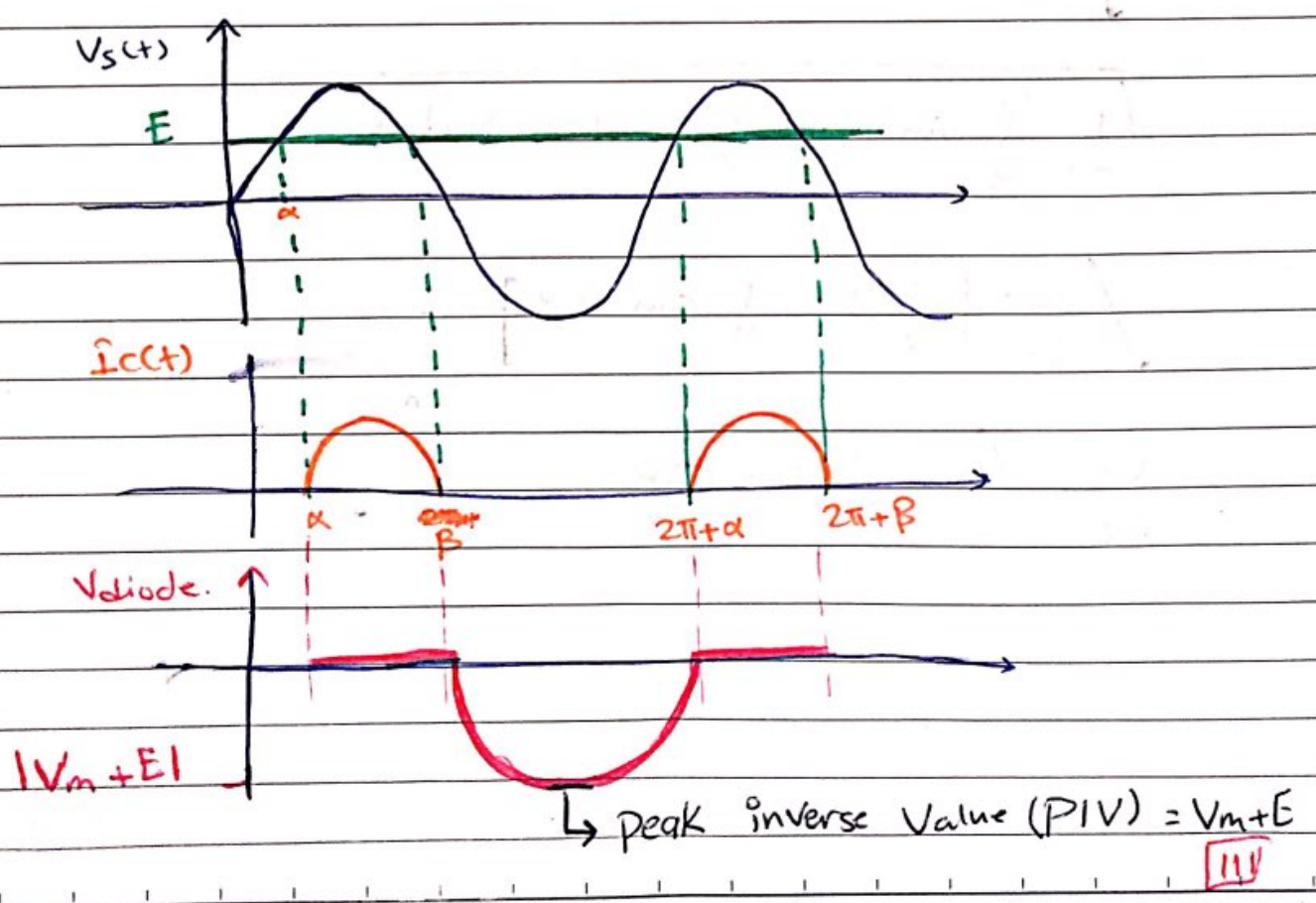
$$V_{diode} = V_m \sin \omega t - E$$

Charging a battery from AC source.

- The Diode works when $V_m \sin \alpha = E$

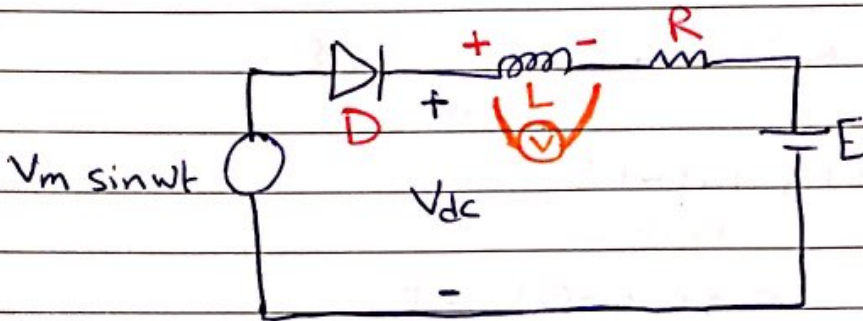
$$\alpha = \sin^{-1}\left(\frac{E}{V_m}\right)$$

and turns off on $\beta = \pi - \alpha$



$$I_{0, \text{peak}} = \frac{V_m - E}{R}$$

* HWR with E and RL load



* التفريغ لن يكون
الاعتماد على inductor

* Two driving forces
E / Vm

$$-V_m \sin \omega t + V_{\text{diode}} + E = 0$$

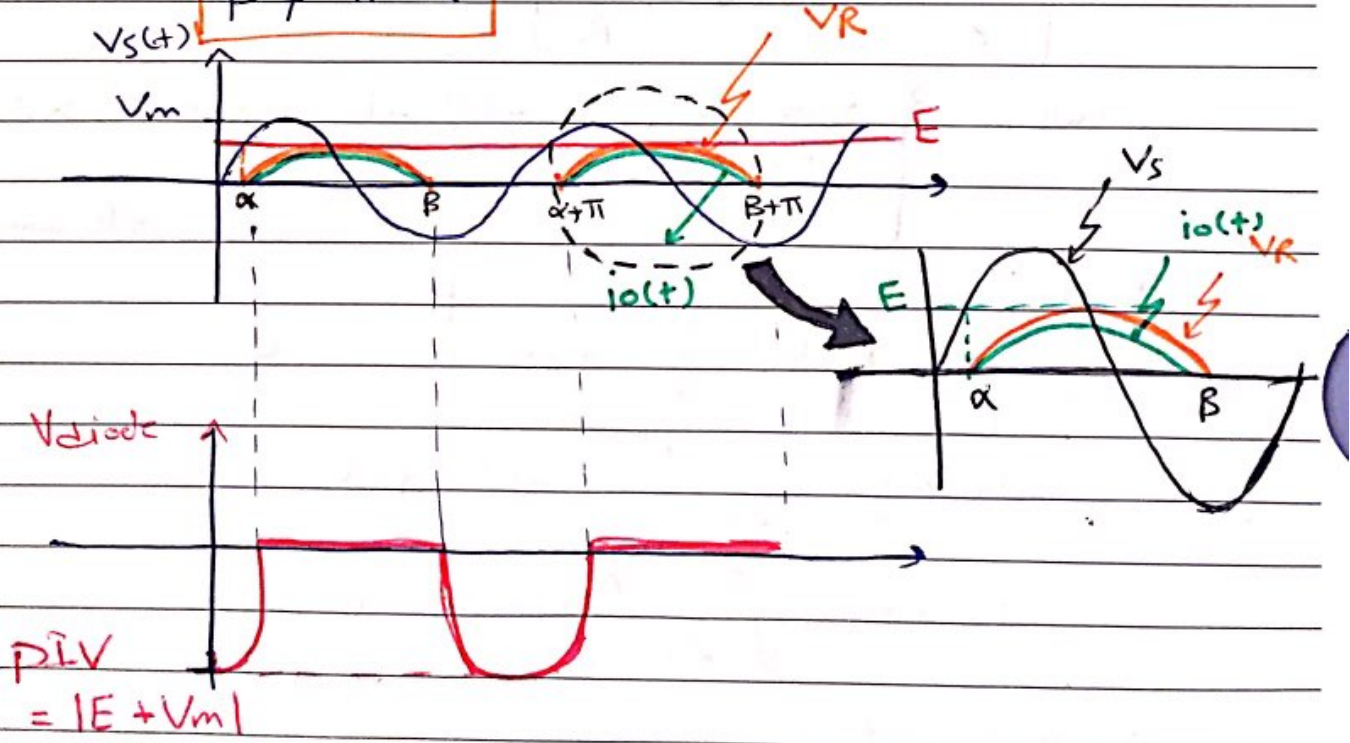
$$V_{\text{diode}} = V_m \sin \omega t - E$$

(VR, L = 0) voltage drop across L is zero

$$\alpha = \sin^{-1} \left(\frac{E}{V_m} \right)$$

$$i(\beta) = 0$$

$$\beta \neq \pi - \alpha$$



$$\text{PIV} = |E + V_m|$$

$$V_{diode} = \begin{cases} 0 & \alpha \leq \omega t \leq \beta \\ V_m \sin \omega t - E & \text{elsewhere.} \end{cases}$$

* Applying KVL

$$V_m \sin(\omega t) = R i(\omega t) + L \frac{di(\omega t)}{d\omega t} + E$$

$$i(\omega t) = i_f(\omega t) + i_n(\omega t)$$

↳ Forced ↳ natural.

$$i_f(\omega t) = \frac{V_m}{Z} \sin(\omega t - \theta) - \frac{E}{R}$$

$$i_n(\omega t) = A e^{-\frac{\omega t}{\tau}}$$

$$Z = \sqrt{R^2 + (\omega L)^2}$$

$$\theta = \tan^{-1}\left(\frac{\omega L}{R}\right)$$

$$\tau = \frac{L}{R}$$

Applying initial condition :- $I_c [i(\alpha) = 0]$

$$A = \left[\frac{V_m}{Z} \sin(\alpha + \theta) + \frac{E}{R} \right] e^{\alpha/\tau}$$

$$i(\omega t) = \begin{cases} \frac{V_m}{Z} \sin(\omega t - \theta) - \frac{E}{R} + A e^{-\frac{\omega t}{\tau}}, & \alpha \leq \omega t \leq \beta \\ 0 & \text{elsewhere} \end{cases}$$

$$\beta \triangleq i(\beta) = 0$$

$$\frac{V_m}{Z} \sin(\beta - \theta) - \frac{E}{R} + A e^{-\frac{\beta}{\tau}} = 0$$

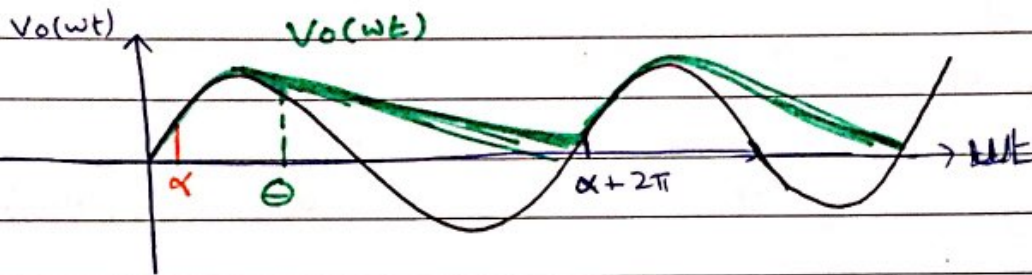
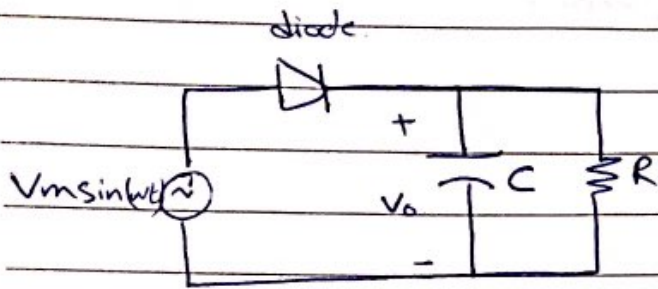
$$I_{o, \text{avg}} = \frac{1}{2\pi} \int_{\alpha}^{\beta} i(\omega t) d\omega t$$

$$I_{o, \text{rms}} = \sqrt{\frac{1}{2\pi} \int_{\alpha}^{\beta} i^2(\omega t) d\omega t}$$

$$\begin{cases} V_{o, \text{avg}} = E \\ V_{o, \text{rms}} = E \end{cases}$$

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* HWR with RC Load:-



voltage across capacitor does not change abruptly (due to C)

$\alpha \rightarrow$ 2 curve. Δ ω $\cos \theta$

$\theta \rightarrow$ 2 curve. Δ ω $\sin \theta$

$$V_o(\omega t) = \begin{cases} V_m \sin(\omega t) & D \text{ is ON} \\ V_\theta e^{-(\omega t - \theta)/\omega RC} & D \text{ is OFF} \end{cases}$$

$$V_\theta = V(\theta) = V_m \sin(\theta)$$

\hookrightarrow at $\omega t = \theta$

$$\frac{d}{d\omega t} V_m \sin \omega t = \frac{d}{d\omega t} V_\theta e^{-(\omega t - \theta)/\omega RC}$$

$$V_m \cos \omega t = V_m \sin \theta \left(\frac{-1}{\omega RC} \right) e^{-(\omega t - \theta)/\omega RC}$$

$$V_m \cos \theta = V_m \sin \theta \left(\frac{-1}{\omega RC} \right) e^{-(\theta - \theta)/\omega RC}$$

$$\frac{1}{\tan \theta} = \frac{-1}{\omega RC}$$

$$\theta = \tan^{-1}(-\omega RC)$$

$$\ominus = -\tan^{-1}(\omega RC)$$

$\theta > 90^\circ$

((الزاوية على قطع الب يحوط π))

at $\omega t = 2\pi + \alpha$

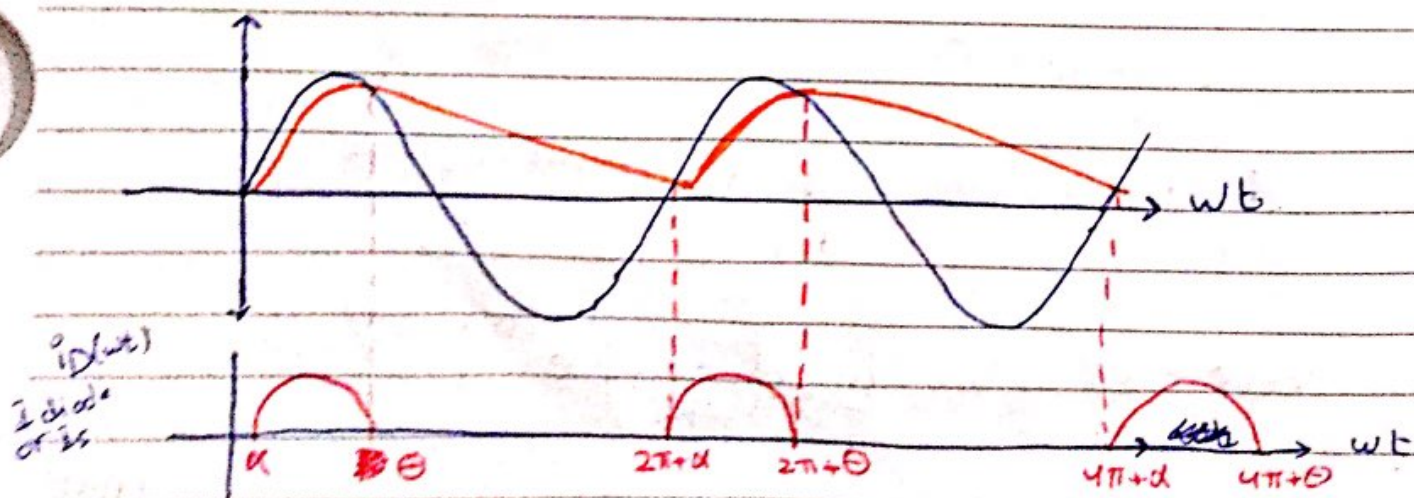
$$V_m \sin(2\pi + \alpha) = (V_m \sin \theta) e^{-(2\pi + \alpha)/\omega RC}$$

$$\sin \alpha = \sin \theta e^{-\underbrace{(2\pi + \alpha - \theta)}_{\text{radian}}/\omega RC} = 0$$

rad \rightarrow راديان \leftarrow radian/degree

In exponential the θ in radian.

$V_o > V_{in} \rightarrow$ diode R.B



$$i_c(\omega t) = C \frac{dV_c(t)}{dt} = \omega C \frac{dV_c(\omega t)}{d\omega t}$$

$$i_c(\omega t) = \begin{cases} \omega C V_m \cos(\omega t) & \text{Dis ON } \alpha < \omega t \leq \theta \\ \frac{-V_m \sin \theta}{R} e^{-(\omega t - \theta)/\omega RC} & \text{Dis OFF otherwise} \end{cases}$$

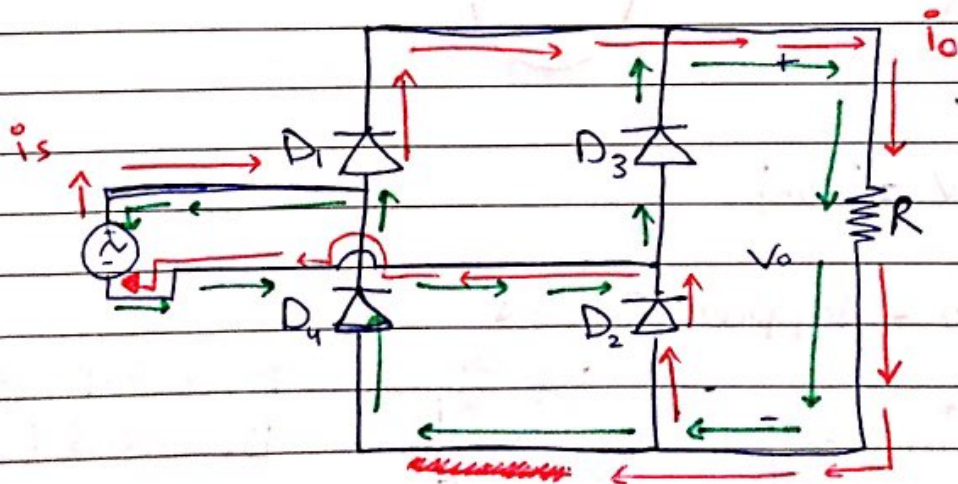
$$i_s(\omega t) = i_D(\omega t) - i_c(\omega t) + i_R(\omega t)$$

$$I_{s \text{ avg}} = I_D \text{ avg} = I_R \text{ avg}$$

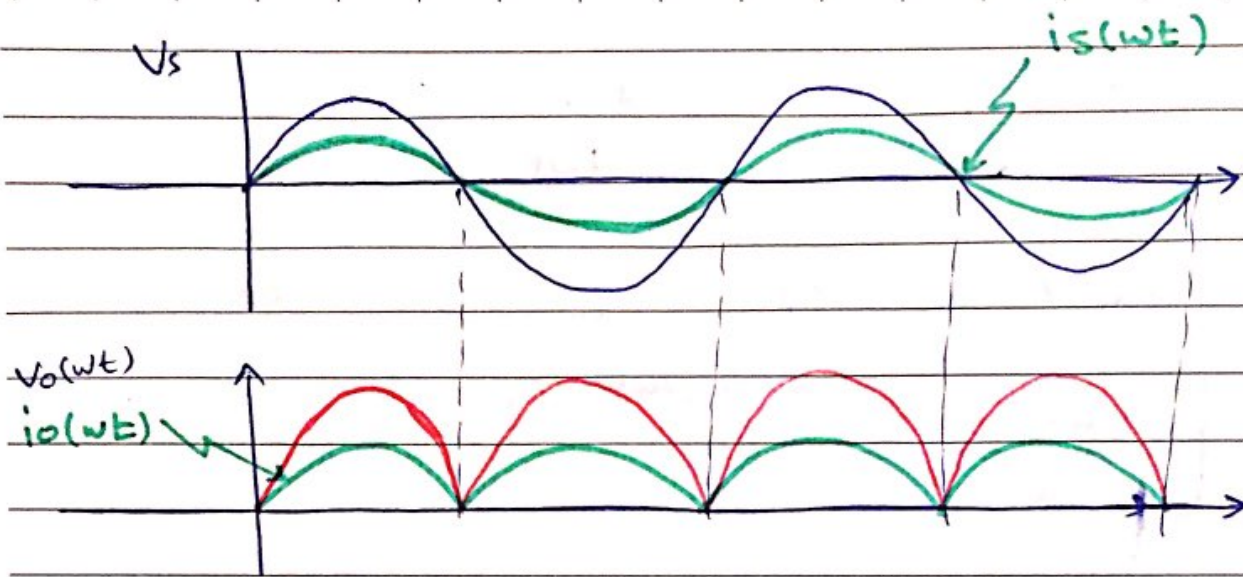
$$* V_o \text{ avg} = \int_{\alpha}^{\theta} \dots + \int_{\theta}^{2\pi + \alpha} \dots$$

$$* I_o \text{ avg} = \frac{V_o \text{ avg}}{R}$$

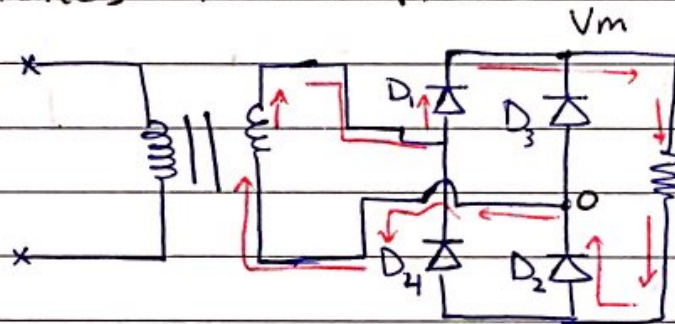
* FWR with R-Load θ



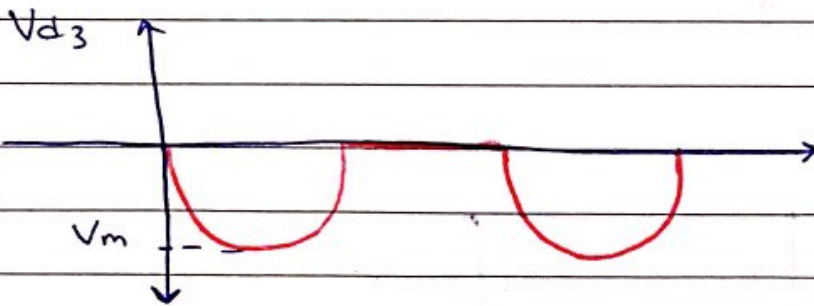
+ +ve cycle
- -ve cycle



2] approaches For FWR 8A

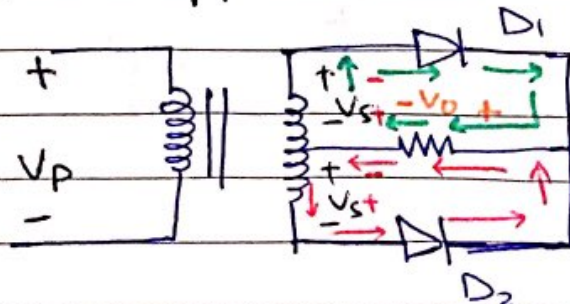


FW bridge Rectifier.



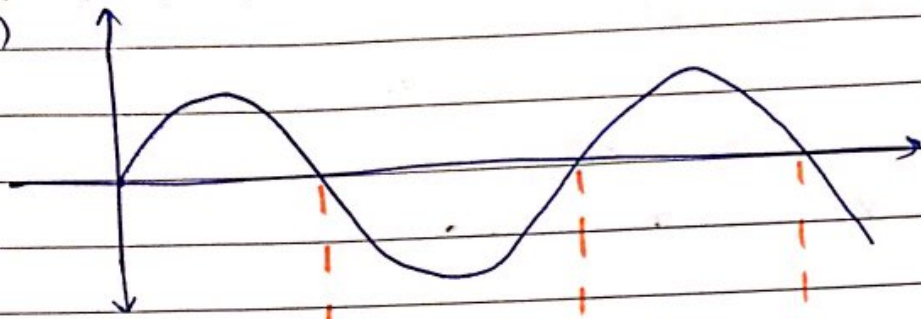
$PIV = |V_m|$

* Center-tapped TR 8A



$D_2 \rightarrow R.B (+ve \text{ cycle})$
 $D_1 \rightarrow R.B (-ve \text{ half cycle})$

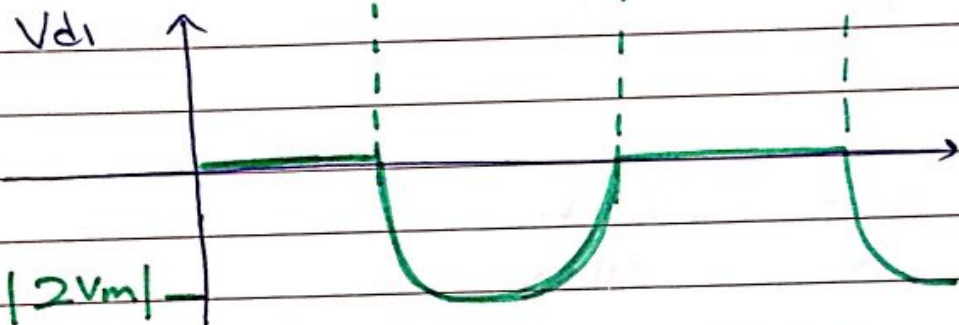
$V_s(\omega t)$



$V_o(\omega t)$



V_d



$|2V_m|$

$$V_o + V_s + V_d = 0$$

$$V_d = V_o - V_s$$

$$V_d = -2V_o = |2V_o|$$

* Study the Performance Parameter:-

$$\boxed{1} \quad \eta = \frac{P_{DC}(\omega)}{P_{AC}(\omega)}$$

$$\eta = \frac{V_{o\text{avg}} \cdot I_{o\text{avg}}}{V_{\text{rms}} I_{\text{rms}}} = \frac{\frac{2V_m}{\pi} \times \frac{2V_m}{\pi R}}{\frac{V_m}{\sqrt{2}} \times \frac{V_m}{R\sqrt{2}}} = \frac{8}{\pi^2} = 81.2\%$$

$$\boxed{2} \quad FF = \frac{V_{\text{rms}}(\omega)}{V_{o\text{avg}}}$$

$$= \frac{V_m/\sqrt{2}}{2V_m/\pi} = 1.11$$

$$\boxed{3} \quad RF = \sqrt{FF^2 - 1} = 0.483$$

$$\boxed{4} \quad PF = \frac{V_{\text{rms}o} \times I_{\text{rms}o}}{V_{\text{rms}in} \times I_{\text{rms}in}} = 1$$

Ex Finding FOS of output voltage for FWR ?!

$$V_o(t) = V_{dc} + \sum_{n=1}^{\infty} a_n \cos n\omega t + b_n \sin n\omega t.$$

$$V_{dc} = V_{o\text{avg}} = \frac{2V_m}{\pi} = \frac{1}{\pi} \int_0^{\pi} V_m \sin \omega t \, d\omega t.$$

$$a_n = \frac{1}{\pi} \int_0^{2\pi} V_o \cos n\omega t \, d\omega t$$

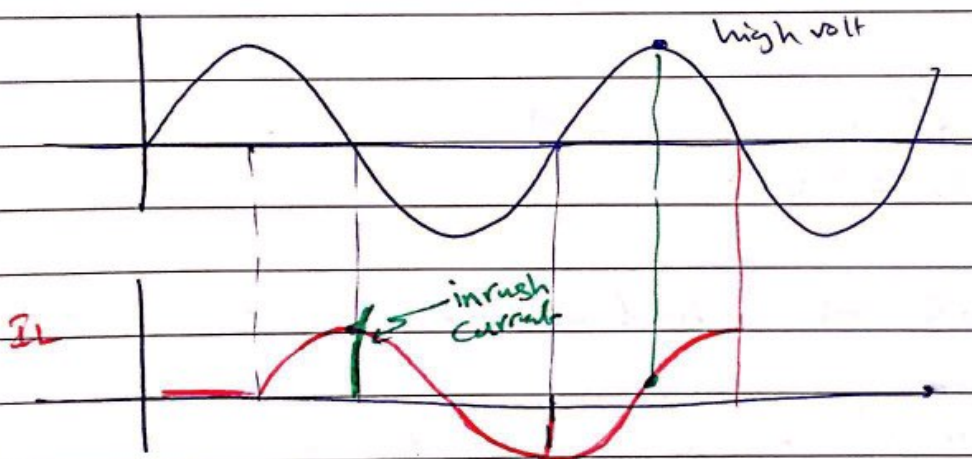
$$= \frac{2}{\pi} \int_0^{\pi} V_m \sin \omega t \cos n\omega t \, d\omega t$$

$$\Rightarrow a_n = \begin{cases} \frac{4V_m}{\pi} \sum_{n=2,4,6}^{\infty} \frac{-1}{(n-1)(n+1)} & , n = 2, 4, 6, \dots \\ 0 & , n = 1, 3, 5 \end{cases}$$

$$\Rightarrow b_n = \frac{1}{\pi} \int_0^{2\pi} V_0 \sin n\omega t \, d\omega t.$$

$$\frac{2}{\pi} \int_0^{\pi} V_m \sin n\omega t \sin \omega t \, d\omega t = 0$$

$$V_0(t) = \frac{2V_m}{\pi} - \frac{4V_m}{3\pi} \cos 2\omega t - \frac{4V_m}{15\pi} \cos 4\omega t + \dots$$

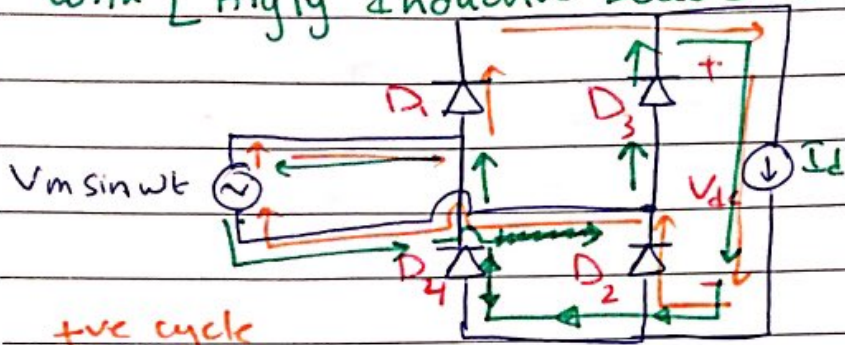


* Inrush current = AC + DC.

at point \rightarrow high volt and low current there's no inrush current.

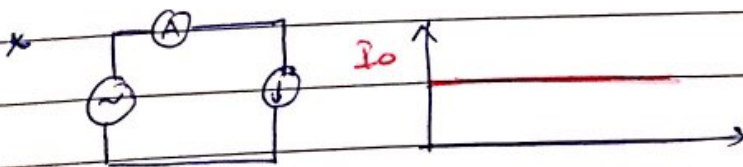
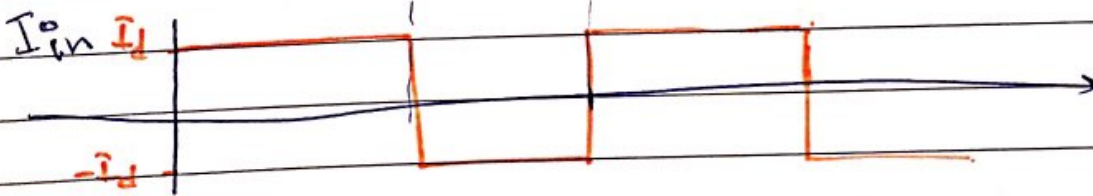
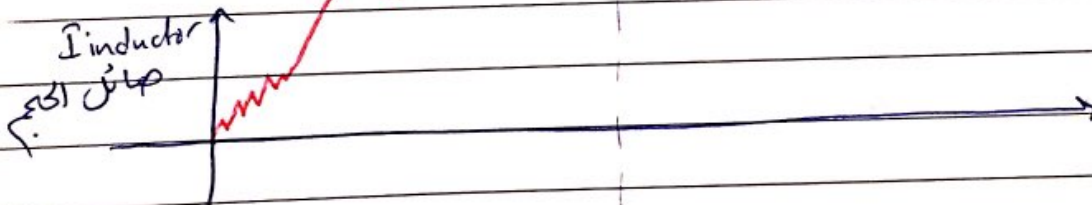
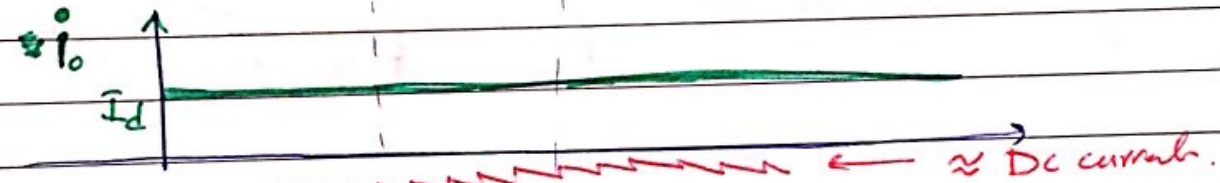
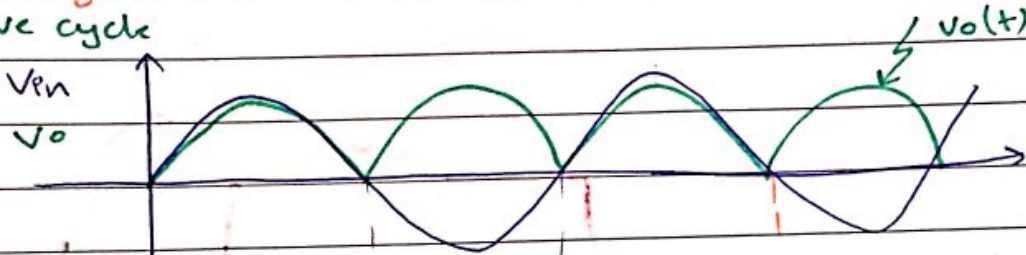
\rightarrow Inrush current have second harmonic.

FWR with constant current load Δ
 with [Highly Inductive Load] \equiv constant current.



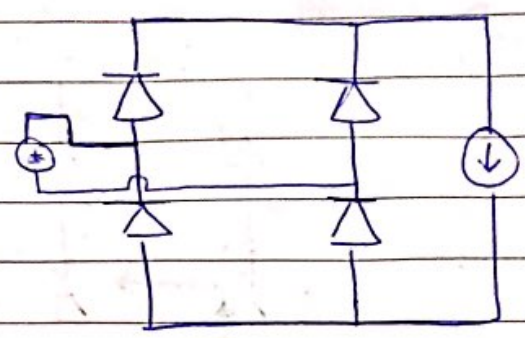
Load is highly inductive $\therefore I_L \approx$

+ve cycle
 -ve cycle



(Load I_L)

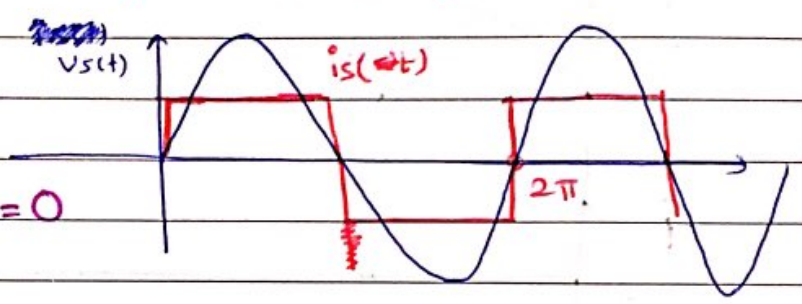
In practice, the source current can not be 100% constant (rect) and the source will supply the sum of fourier series of current.



$$i_s(t) = I_{dc} + \sum_{n=1}^{\infty} a_n \cos(n\omega t) + b_n \sin(n\omega t)$$

$$\frac{a_0}{2} = I_d$$

$$= \frac{1}{2\pi} \int_0^{2\pi} i_s(\omega t) d\omega t = 0$$



$a_n = 0$ \rightarrow odd function

$$b_n = \frac{2}{\pi} \int_0^{\pi} I_d \sin(n\omega t) d\omega t$$

$$b_n = \frac{4 I_d}{n\pi} \text{ for } n=1, 3, 5, \dots$$

$$i_s(t) = \frac{4 I_d}{\pi} \left(\sin(\omega t) + \frac{\sin(3\omega t)}{3} + \frac{\sin(5\omega t)}{5} + \dots \right)$$

$$I_{s1} = \frac{4 I_d}{\pi} \sin \omega t$$

source PF = 0.4

$$P = \frac{P}{S} = \frac{V_s I_{s1} \cos \theta}{V_s I_s}$$

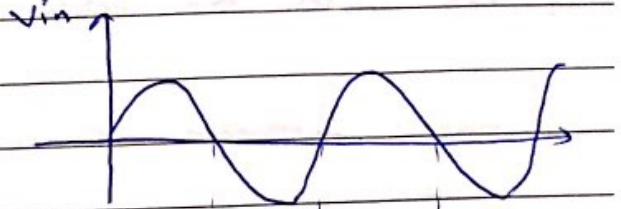
θ between V_s and I_{s1}

$$= \frac{I_{s1}}{I_s} \cos \theta$$

conventional PF (Displacement PF)

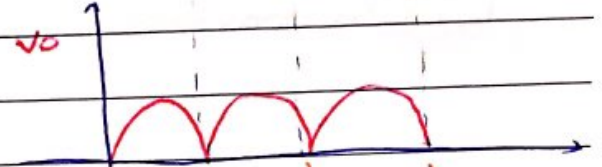
$$P = \frac{\hat{I}_s}{\hat{I}_s} \cdot \text{DPF}$$

إذا كان عندى harmonic
بقدم هذا القانون



$$\hat{I}_{s,rms} = \frac{4 \hat{I}_d}{\pi \sqrt{2}} = 0.9 \hat{I}_d$$

$$V_{o,avg} = \frac{2V_m}{\pi}$$

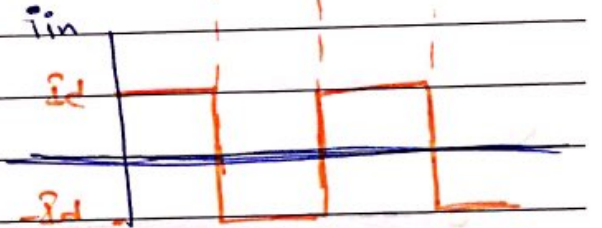


$$V_{rms} = \frac{V_m}{\sqrt{2}}$$



$$I_{o,rms} = I_{o,avg} = \hat{I}_d$$

$$P_{o,avg} = \frac{2V_m}{\pi} \times \hat{I}_d$$



$$P_{in,avg} = \frac{V_m}{\sqrt{2}} \times \frac{4 \hat{I}_d}{\sqrt{2} \pi}$$

$$= \frac{2V_m}{\pi} \hat{I}_d = P_{o,avg} \quad [P_{in} = P_{o,avg}] \text{ No phase shift}$$

$$PF = \frac{I_{s,rms}}{I_{s,rms}} \cdot \text{DPF}$$

$$= \frac{4 \hat{I}_d / \sqrt{2} \pi}{\hat{I}_d} \cdot 1$$

$$= 0.9$$

rms value $\rightarrow P \rightarrow PF \text{ of LP} *$

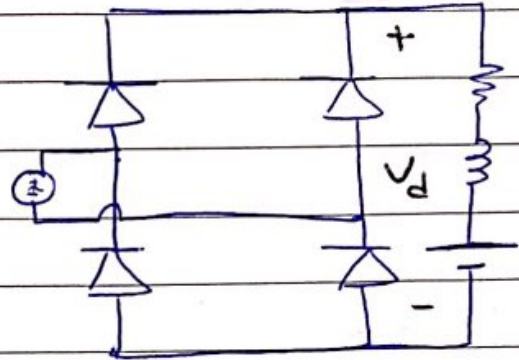
rect \rightarrow full ind \rightarrow *
DPF = 1 \rightarrow لا

FWR with RL load with E & Δ

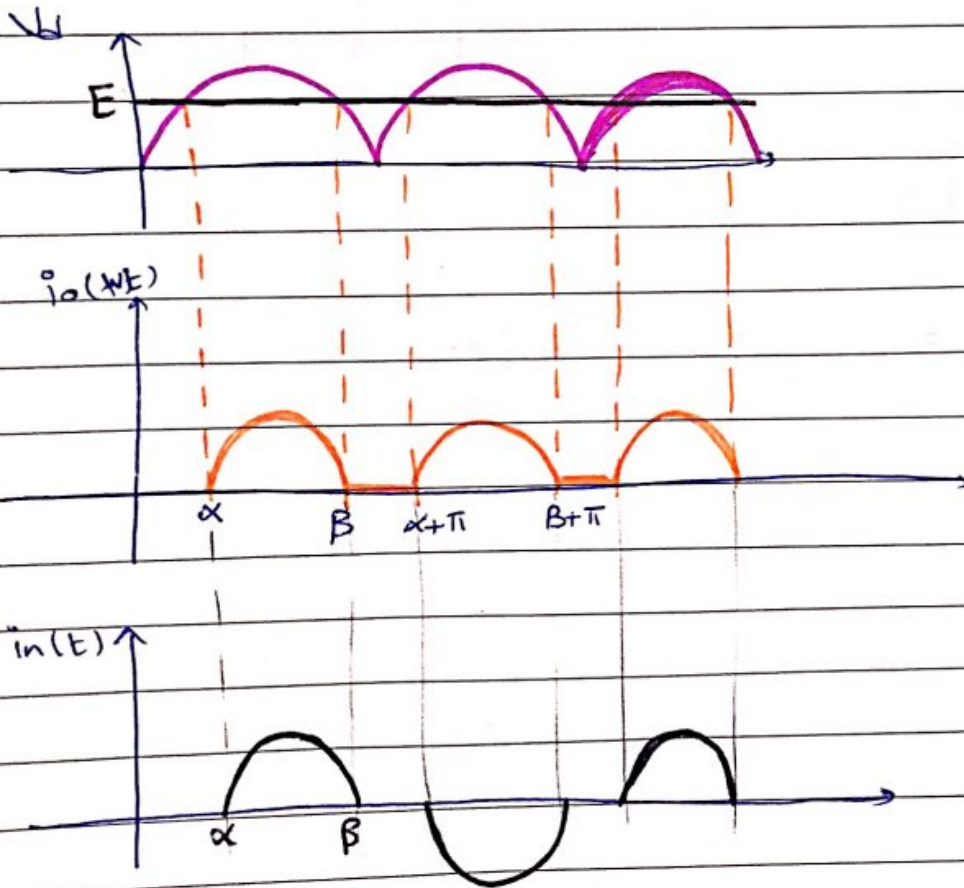
I have 2 modes of operations

1] Continuous

2] Discontinuous.

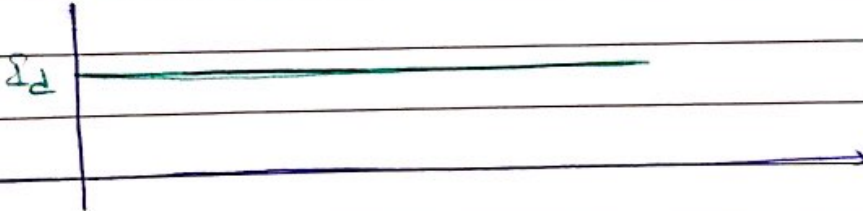
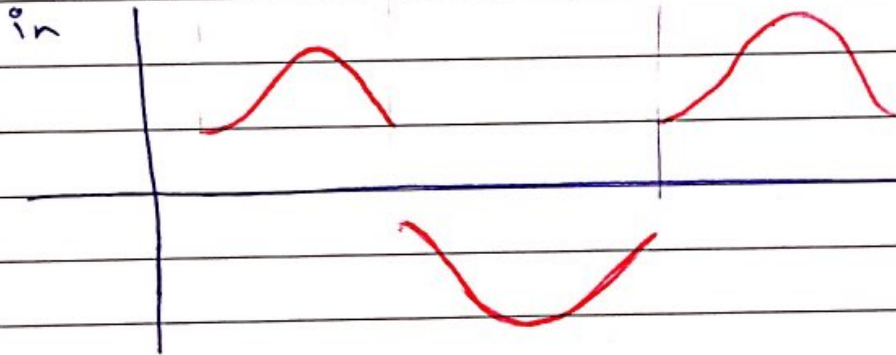
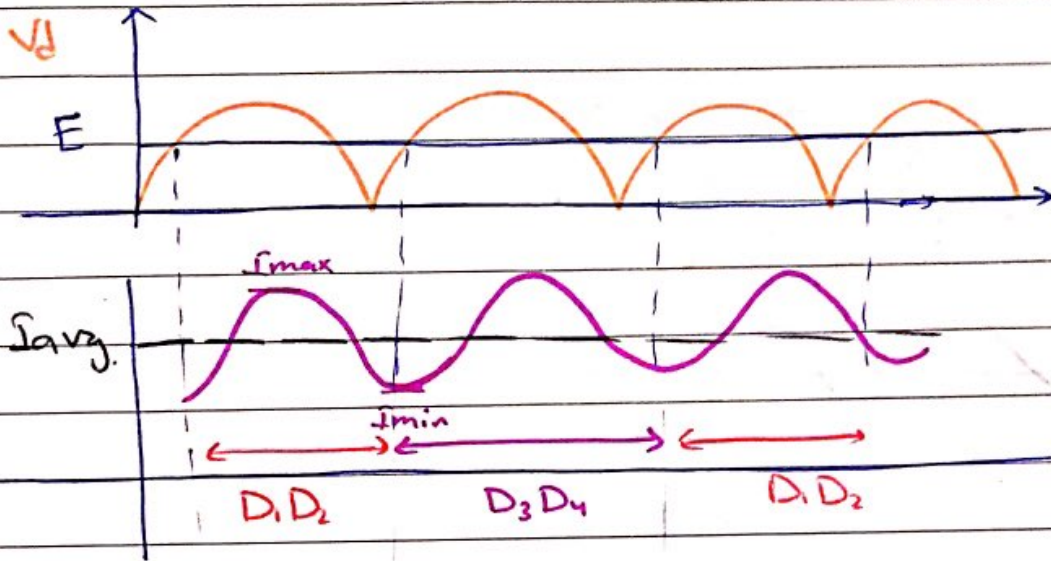


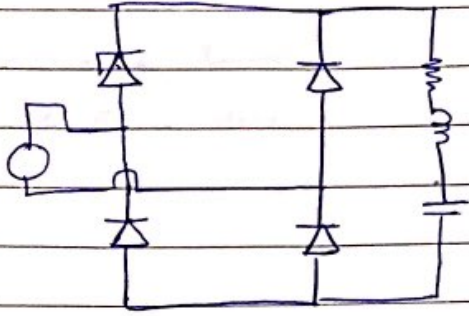
Discontinuous :-



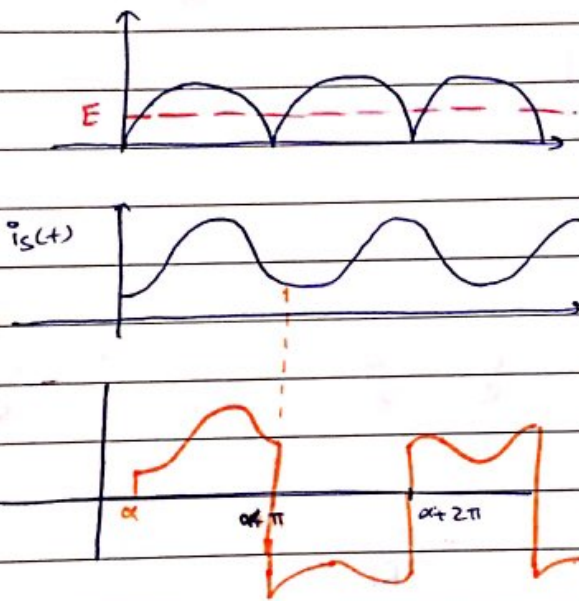
$\beta \Rightarrow$ $\frac{\pi}{2} < \beta < \pi$
0 = $\frac{\pi}{2}$ $\leq \beta < \pi$

* CONTINUOUS





next cycle
 Contin. FWR → i_o $\neq 0$ \rightarrow $\alpha < \pi$
 discontin. \rightarrow $i_o = 0$ \rightarrow $\alpha > \pi$



Continuous Mode.

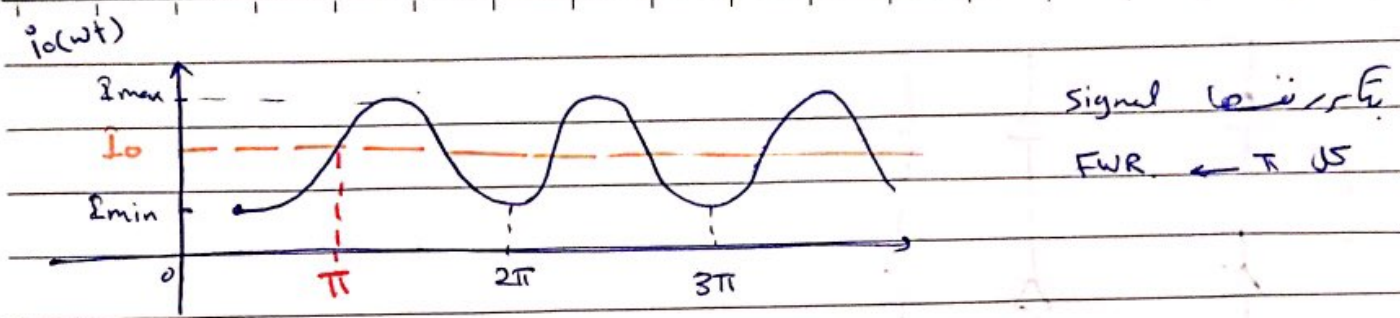
$$L \frac{di_o(\omega t)}{d\omega t} + R i_o(\omega t) + E = |V_m \sin \omega t|$$

$$i_o(\omega t) = \left| \frac{V_m}{Z} \sin(\omega t - \theta) \right| + A_1 e^{-\frac{\omega t}{\tau}} - \frac{E}{R}$$

$$Z = \sqrt{R^2 + (\omega L)^2}$$

$$\theta = \tan^{-1} \left(\frac{\omega L}{R} \right)$$

$$\tau = \frac{L}{R}$$



at $\omega t = \pi \rightarrow i_o(\omega t) = \hat{i}_o$

$$i_o(\pi) = \hat{i}_o = \left| \frac{V_m}{Z} \sin(\pi - \theta) \right| + A_1 e^{-\pi/\omega\tau} - \frac{E}{R}$$

$$A_1 = \left[\hat{i}_o + \frac{E}{R} - \frac{V_m}{Z} \sin \theta \right]$$

$$i_o(2\pi) = \hat{i}_o$$

$$i_o(0) = \hat{i}_o$$

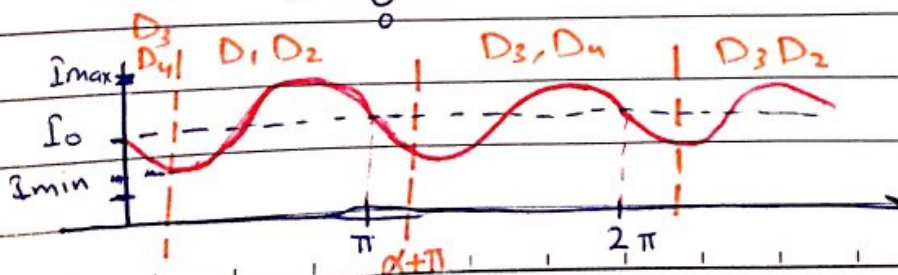
$$= \left| \frac{V_m}{Z} \sin(-\theta) \right| + \left[\hat{i}_o + \frac{E}{R} - \frac{V_m}{Z} \sin \theta \right] e^{-\pi/\omega\tau} - \frac{E}{R}$$

$$\hat{i}_o = \frac{V_m}{Z} \sin \theta \frac{1 + e^{-\pi/\omega\tau}}{1 - e^{-\pi/\omega\tau}} - \frac{E}{R}$$

$$i_o(\omega t) = \frac{V_m}{Z} \left[\sin(\omega t - \theta) + \frac{2 \sin \theta e^{-\omega t/\omega\tau}}{1 - e^{-\pi/\omega\tau}} \right] - \frac{E}{R}$$

for $0 \leq \omega t - \theta \leq \pi$

$$I_{o \text{ avg}} = \frac{1}{\pi} \int_0^{\pi} i_o(\omega t) d\omega t$$

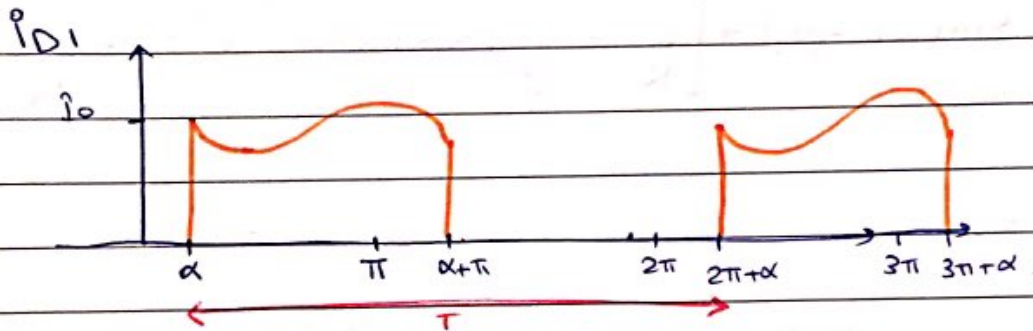


$$P_o(\omega t) = 5 \sin(\omega t) + 3 e^{-\frac{\omega t}{0.005}} - 5$$

↳ $I_{o \text{ avg}} \neq 5$

$$I_{o \text{ avg}} = \frac{1}{\pi} \int_0^{\pi} 5 \sin \dots$$

$$\Rightarrow \bar{I}_D \text{ avg} = \frac{1}{2\pi} \int_0^{\pi} P_o(\omega t) \cdot d\omega t.$$



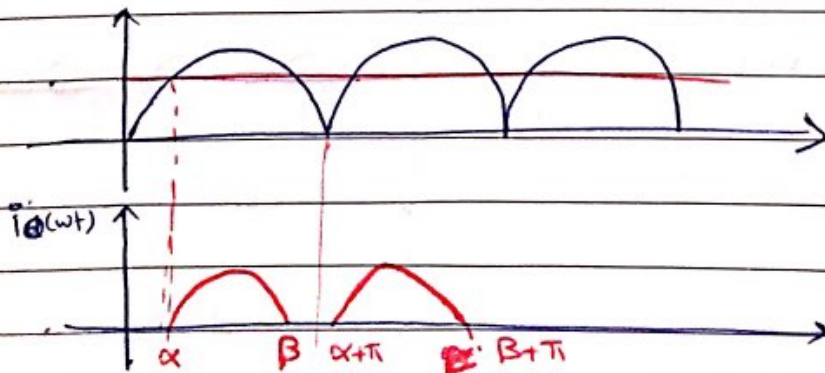
average = area

$$\Rightarrow \bar{I}_D \text{ rms} = \sqrt{\frac{1}{2\pi} \int_0^{\pi} P_D^2(\omega t) \cdot d\omega t.}$$

↓
1 2 3 4

$$\Rightarrow I_{o \text{ rms}} = \sqrt{I_{D1 \text{ rms}}^2 + I_{D3 \text{ rms}}^2} = \sqrt{2} \bar{I}_D \text{ rms}$$

Discontinuous MODE 84



$$i_0(\omega t = \alpha) = 0$$

$$0 = \frac{V_m}{Z} \sin(\alpha - \theta) + A e^{\frac{-\alpha}{\omega\tau}} - \frac{E}{R}$$

$$A = \left[\frac{E}{R} - \frac{V_m}{Z} \sin(\alpha - \theta) \right] e^{\frac{\alpha}{\omega\tau}}$$

$$i_0(\omega t) = \frac{V_m}{Z} \sin(\omega t - \theta) + \left[\frac{E}{R} - \frac{V_m}{Z} \sin(\alpha - \theta) \right] e^{\frac{\alpha}{\omega\tau}} - \frac{E}{R}$$

$$i_0(\omega t = \beta) = 0$$

$$\frac{V_m}{Z} \sin(\beta - \theta) + \left[\frac{E}{R} - \frac{V_m}{Z} \sin(\alpha - \theta) \right] e^{\frac{\alpha - \beta}{\omega\tau}} - \frac{E}{R} = 0$$

β is defined as

$$\sin(\beta - \theta) + \left[\frac{E}{R V_m \cos \theta} - \sin(\alpha - \theta) \right] e^{\frac{\alpha - \beta}{\omega\tau}} - \frac{E}{V_m \cos \theta} = 0$$

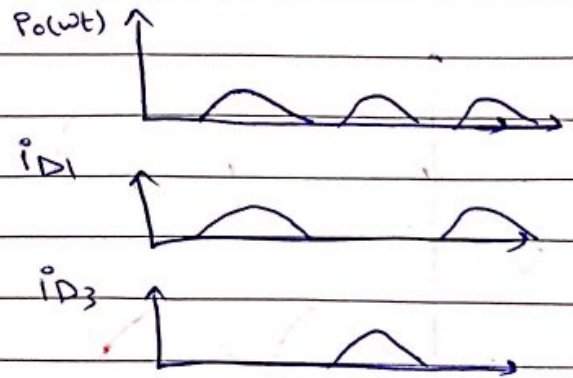
$$\cos \theta = \frac{R}{Z}$$

$$* \quad \bar{I}_D \text{ avg} = \frac{1}{2\pi} \int_{\alpha}^{\beta} i_0(\omega t) d\omega t$$

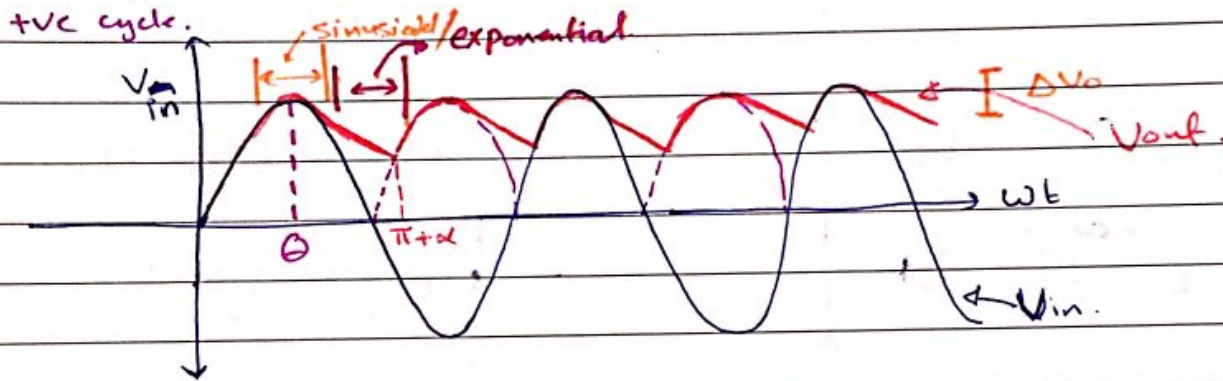
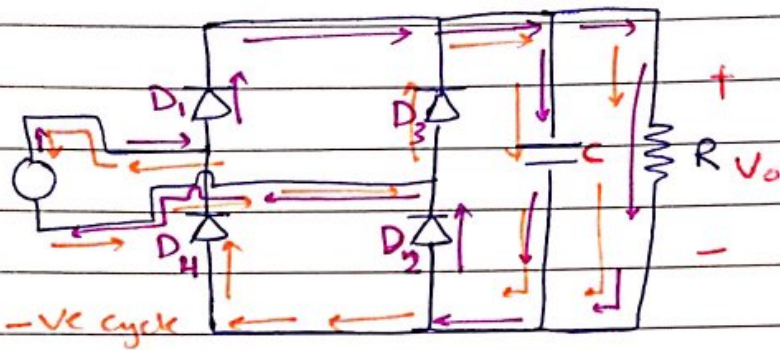
$$* \quad \bar{I}_o \text{ avg} = 2 * \bar{I}_D \text{ avg}$$

$$* \quad \bar{I}_D \text{ rms} = \sqrt{\frac{1}{2\pi} \int_{\alpha}^{\beta} i_0^2(\omega t) d\omega t}$$

$$* \quad \bar{I}_o \text{ rms} = \sqrt{2} \bar{I}_D \text{ rms}$$



* FWR with an output capacitor Δ



$$\Delta V_o = V_m - |V_m \sin(\pi + \alpha)|$$

$$= V_m (1 - \sin \alpha)$$

$$V_o(\omega t) = \begin{cases} |V_m \sin \omega t| & \pi + \alpha \leq \omega t \leq \pi + \theta \\ V_m \sin \theta e^{-\frac{(\omega t - \theta)}{wRC}} & \theta \leq \omega t \leq \pi + \alpha \end{cases}$$

$$\theta = \tan^{-1}(-wRC)$$

$$= \pi - \tan^{-1}(wRC) \quad [\text{by equalizing the derivatives}]$$

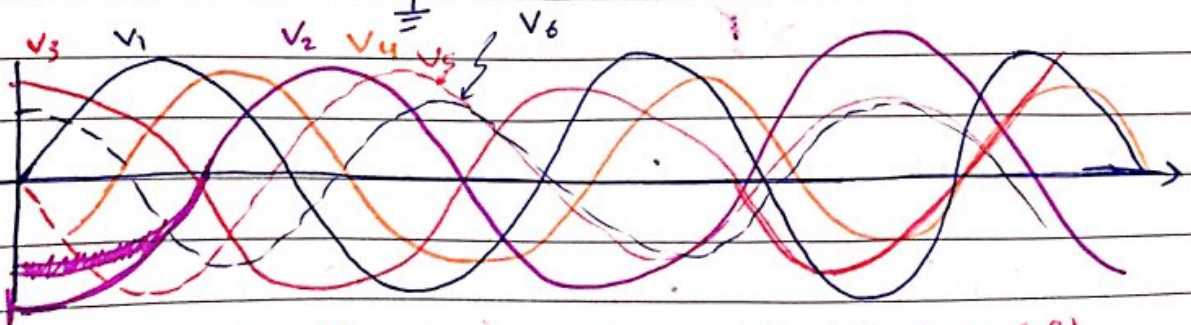
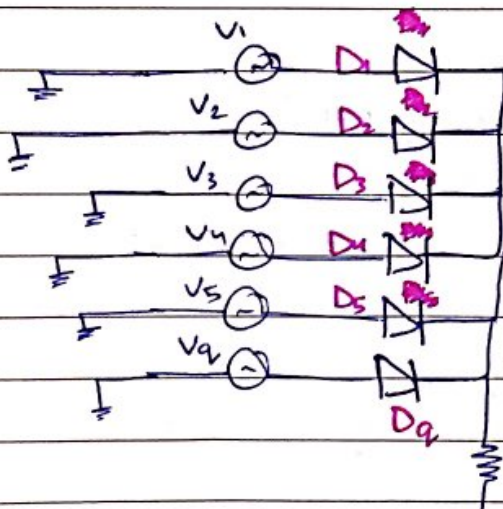
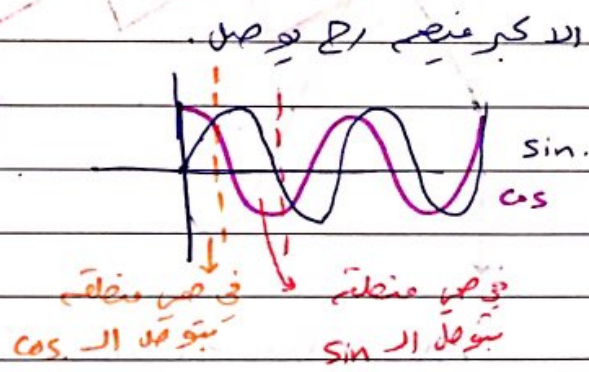
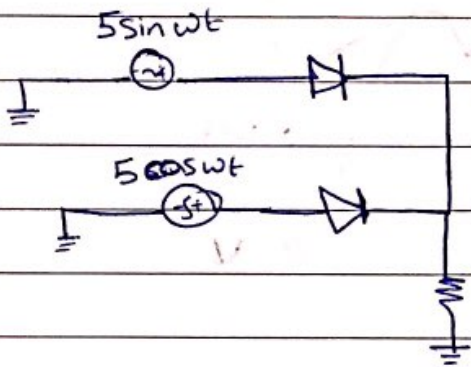
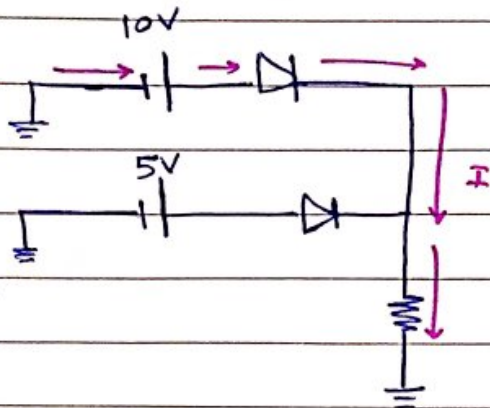
* How to find α ?

$$|V_m \sin(\alpha + \pi)| = V_m \sin \theta e^{-\frac{-(\pi + \alpha - \theta)}{wRC}}$$

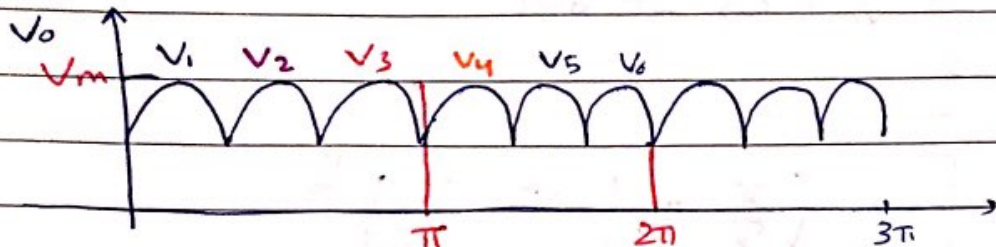
$$\sin \theta e^{-\frac{-(\pi + \alpha - \theta)}{wRC}} - \sin \alpha = 0$$

initial value of $\alpha = 200^\circ$

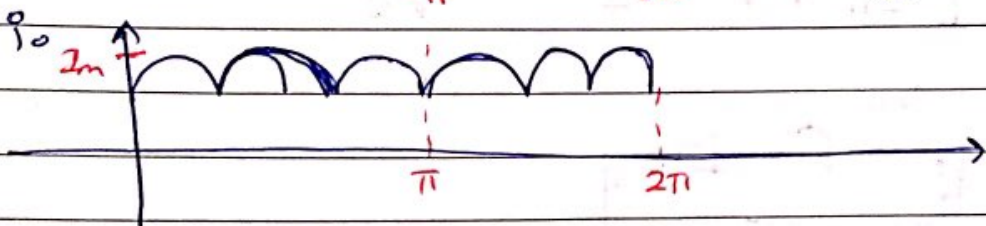
* Multi-phase Diode Rectification 84



6 signal Phase between them 60° ($V_1, V_2 \rightarrow 60^\circ$)

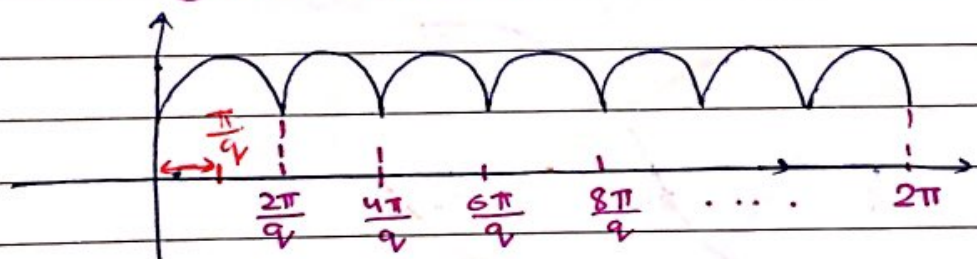


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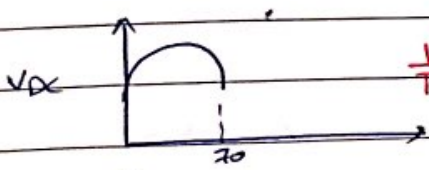


$$I_m = \frac{V_m}{R}$$

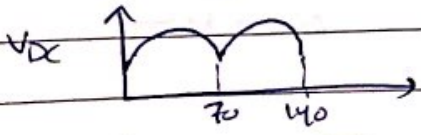
IN GENERALSA



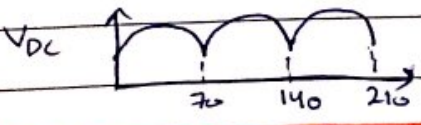
$$V_{DC} = \frac{1}{\pi/q} \int_0^{\pi/q} V_m \cos \omega t = V_m \frac{q}{\pi} \sin \frac{\pi}{q}$$



$\frac{1}{T} \int_0^{T_0} v(\omega t) d\omega t$ V_{DC} value the same.



$$\frac{1}{2T} \left[\int_0^{T_0} v(\omega t) d\omega t + \int_{T_0}^{2T_0} v(\omega t) d\omega t \right]$$



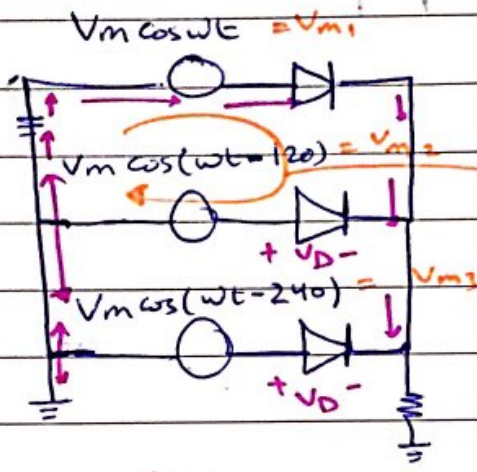
$$\frac{1}{3T} \dots$$

OUR assumption $V_1 = V_m \cos \omega t$

$$V_{rms} = \sqrt{\frac{q}{\pi} \int_0^{\pi/q} V_m^2 \cos^2 \omega t \, d\omega t}$$

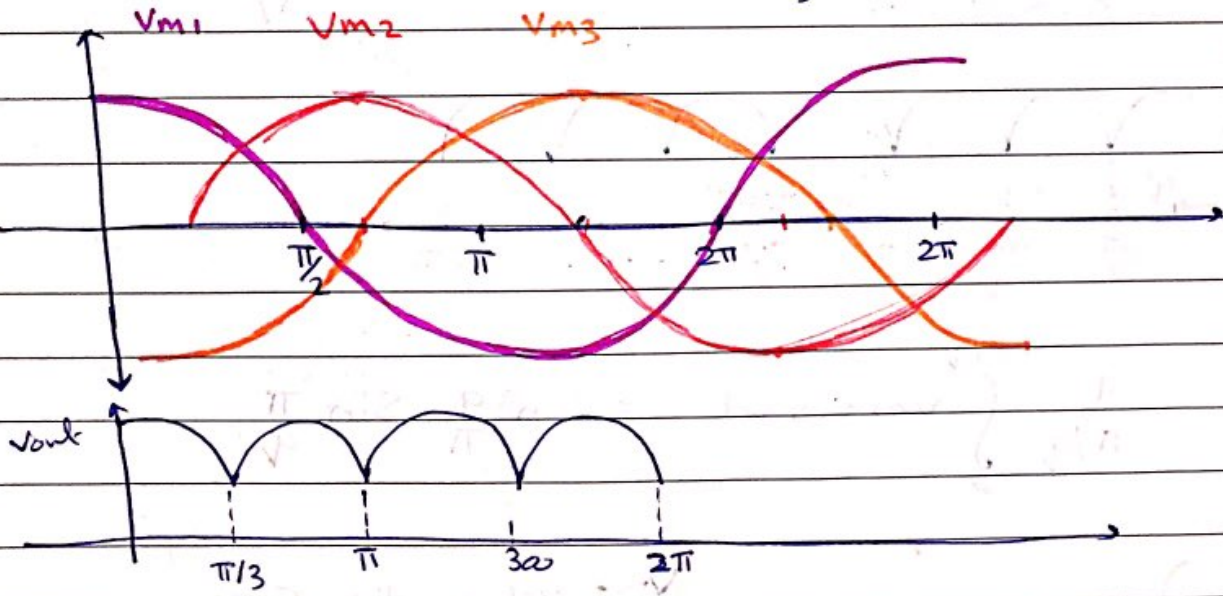
$$V_{rms} = V_m \left[\frac{q}{2\pi} \left(\frac{\pi}{q} + \frac{1}{2} \sin \frac{2\pi}{q} \right) \right]^{1/2}$$

$$\Rightarrow q = 3$$



$$V_D + V_{an} - V_{bn} = 0$$

$$V_D = |V_{ab}|$$



$$V_{DC} = \frac{1}{\pi/3} \int_{\pi/3}^{\pi/3 + \pi/3} V_m \cos \omega t \, d\omega t$$

$$= \frac{1}{2\pi/3} \int_{\pi/3}^{\pi/3 + \pi/3} V_m \cos(\omega t - 120^\circ) \, d\omega t$$

V_{m1}, V_{m2}
تبدیل 60°

$$V_{DC} = \frac{3 V_m \sin \frac{\pi}{3}}{\pi} = 0.827 V_m$$

$$I_{DC} = \frac{0.827 V_m}{R}$$

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$$V_{rms} = \sqrt{\frac{1}{\pi/3} \int_0^{\pi/3} V_m^2 \cos^2(\omega t) d\omega t}$$

$$= 0.84068 V_m.$$

$$I_{rms} = \frac{V_{rms}}{R}$$

$$V_{rms} = V_m \left[\frac{q}{2\pi} \left(\frac{\pi}{q} + \frac{1}{2} \sin \frac{2\pi}{q} \right) \right]^{\frac{1}{2}}$$

⇒ DV System "download"

$$I_{rms} = 0.84068 \frac{V_m}{R}$$

$$P_{Dc} = V_{oc} I_{Dc} = ~~0.84068 \frac{V_m^2}{R}~~$$

$$P_{Dc} = (0.827)^2 \frac{V_m^2}{R}$$

$$P_{Ac} = V_{rms} \cdot I_{rms}$$

$$P_{Ac} = (0.84068)^2 \frac{V_m^2}{R}$$

$$\eta = \frac{P_{Dc}}{P_{Ac}} = 96.77\%$$

$$\Rightarrow FF = \frac{V_{rms}}{V_{DC}} = \frac{0.84068}{0.827} = 1.0165$$

$$\Rightarrow RF = \sqrt{FF^2 - 1}$$

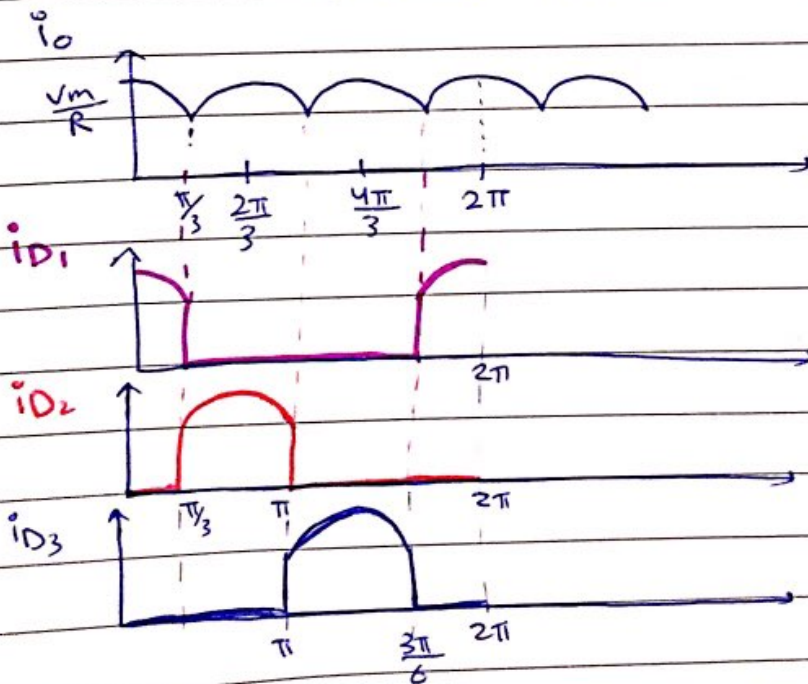
$$= 18.24\%$$

PIV of diode is $\sqrt{2} V_{LC}$ (Peak value)

$\sqrt{2} \sqrt{3} V_{an} \rightarrow$ RMS value for single phase.

$$PF = \frac{V_{rms(o)} * I_{rms(o)}}{3 V_{rms(i)} I_{rms(i)}}$$

$$= \frac{(0.84068) (0.84068) V_m^2 / R}{3 * V_m / \sqrt{3}}$$



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$$I_{rms}(D) = \sqrt{\frac{1}{2\pi R} \int_{\pi/3}^{\pi} V_m^2 \cos^2(\omega t - 120^\circ)}$$

$$= \frac{1}{\sqrt{3}} I_o(rms)$$

$$I_{rms} = 0.84068 \frac{V_m}{R}$$

$$I_{diode} = I_{source}$$

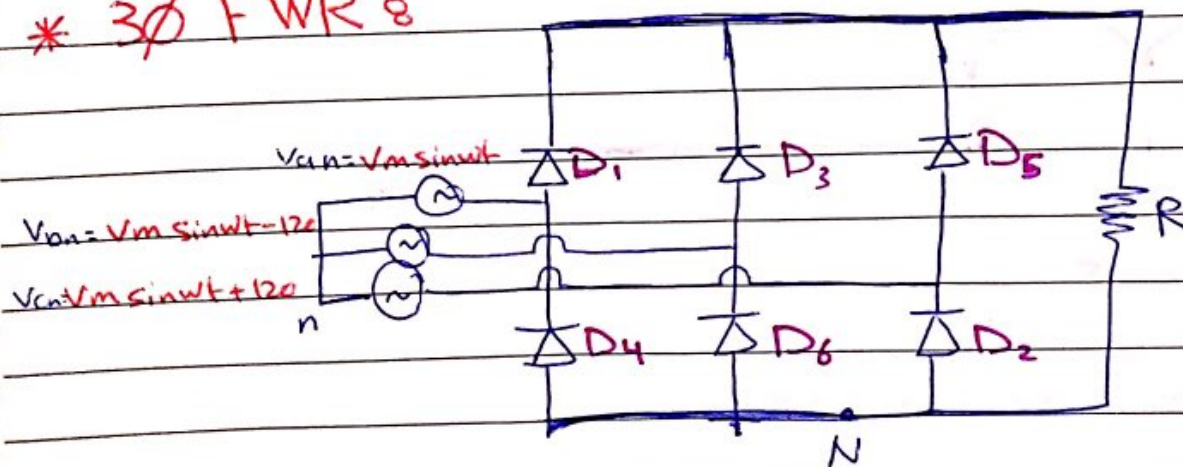
$$= 0.84068 \frac{V_m}{\sqrt{3} R}$$

$$= 0.4854 \frac{V_m}{R}$$

$$PF = \frac{(0.84068)(0.84068) V_m^2 / R}{3 \times \frac{V_m}{\sqrt{2}} \times 0.4854 \frac{V_m}{R}}$$

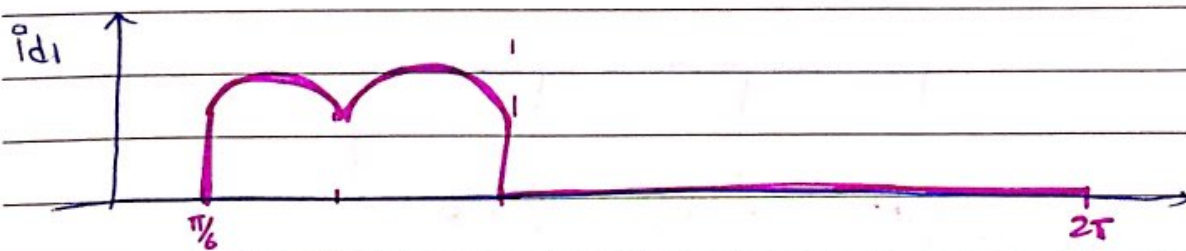
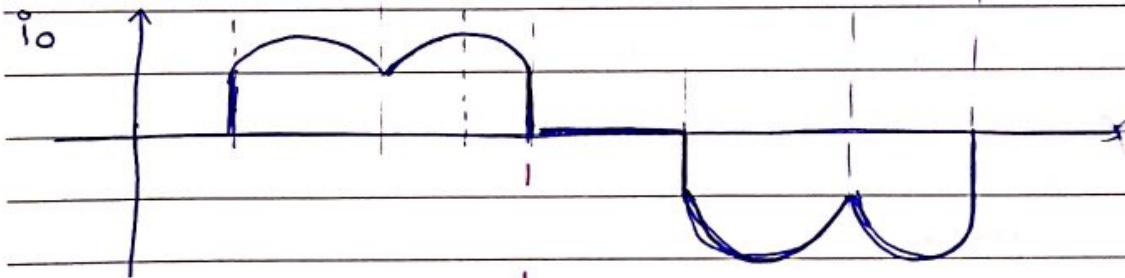
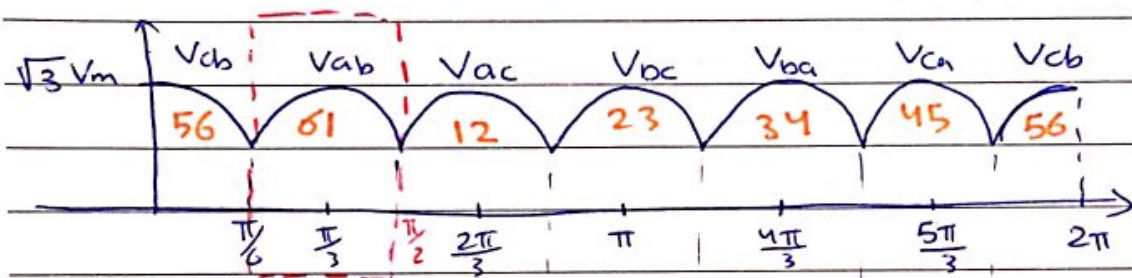
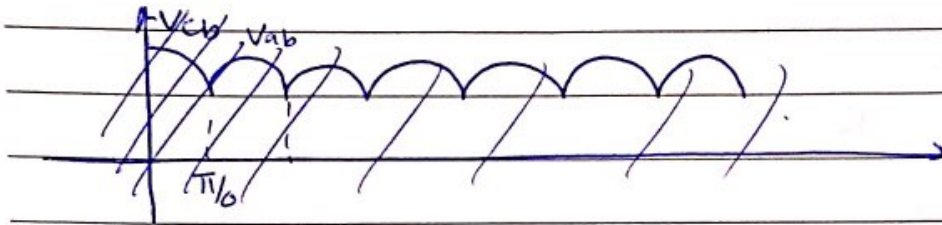
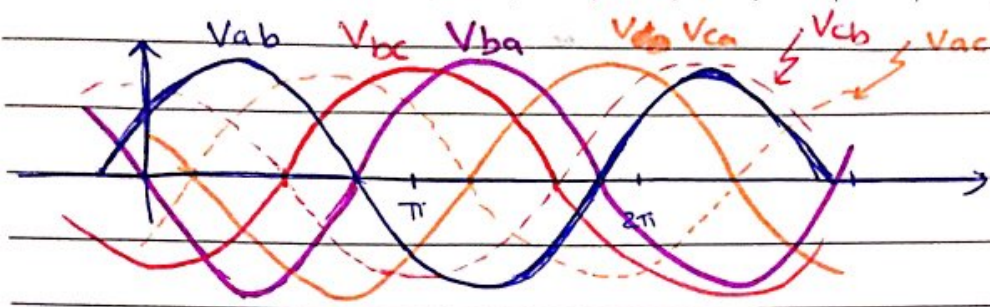
$$PF = 0.6844$$

* 3Ø FWR 8



each pair of diodes will conduct when the instantaneous L-L voltage is highest.

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$$V_{an} = V_m \sin \omega t$$

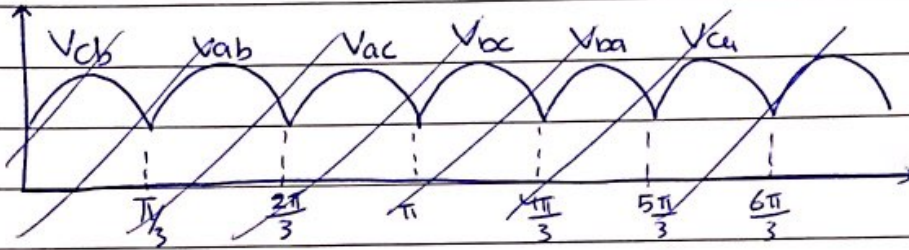
$$V_{ab} = \sqrt{3} V_m \sin(\omega t + 30^\circ)$$

$$V_{DC(0)} = \frac{1}{\pi/3} \int_{\pi/6}^{\pi/2} \sqrt{3} V_m \sin(\omega t + 30^\circ) d\omega t$$

$$V_{bc} = \sqrt{3} V_m \sin(\omega t - 90^\circ)$$

$$V_{cb} = \sqrt{3} V_m \sin(\omega t + 90^\circ)$$
$$= \sqrt{3} V_m \cos(\omega t)$$

$$V_{DC}(\omega) = \frac{1}{\pi/6} \int_0^{\pi/6} \sqrt{3} V_m \cos \omega t \, d\omega t.$$



$$V_{DC} = \frac{6}{\pi} \int_0^{\pi/6} \sqrt{3} V_m \cos \omega t \, d\omega t$$

$$= \frac{3\sqrt{3}}{\pi} V_m$$

$$V_{DC} = 1.654 V_m$$

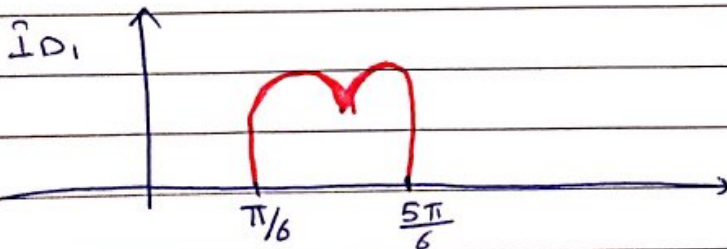
$$I_{DC} = \frac{V_{DC}}{R}$$

$$V_{rms} = \sqrt{\frac{6}{\pi} \int_0^{\pi/6} (\sqrt{3} V_m)^2 \cos^2 \omega t \, d\omega t}$$

$$= \left(\frac{3}{2} + \frac{9\sqrt{3}}{4\pi} \right)^{1/2} V_m$$

$$V_{rms} = 1.6554 V_m$$

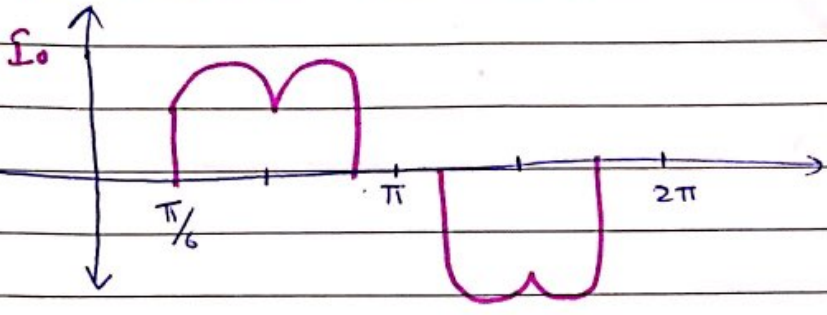
$$I_{rms} = \frac{V_{rms}}{R}$$



$$I_{Drms} = \sqrt{\frac{1}{2\pi} * 2 \int_{\pi/6}^{\pi/2} (\sqrt{3} V_m)^2 \sin^2(\omega t - 30) \, d\omega t}$$

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$$I_{Drms} = 0.5518 I_m \quad \frac{\sqrt{3} V_m}{R}$$

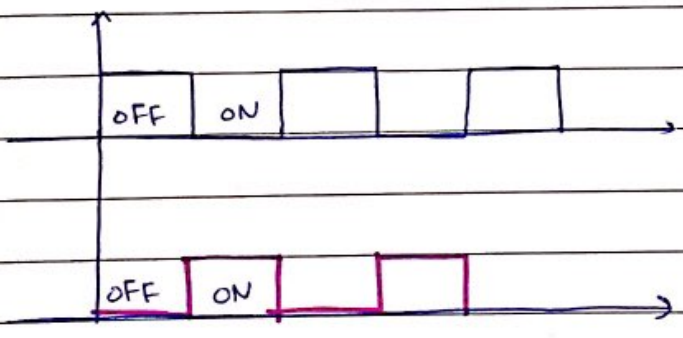
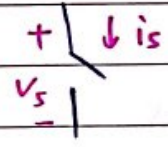


$$I_{Drms} = \sqrt{\frac{8}{2\pi} \int_0^{\pi/6} I_m^2 \cos^2 \omega t \, d\omega t}$$

$$I_{Drms} = 0.7804 I_m$$

Switching Devices 84

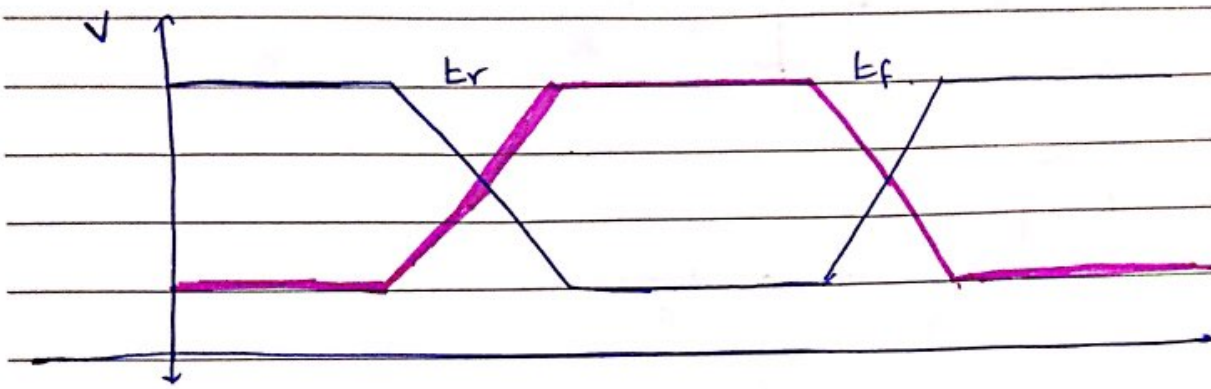
A Ideal switch
Power losses = 0



B Real switches

When S is ON: $V_s \neq 0$ → can not be neglected → Conduction loss

S is off: $I_s \neq 0$ → leakage loss
↳ can be ignored



$t_r \equiv$ reverse time

$t_f \equiv$ forward time

$$W_{on} = \frac{1}{2} V_s t_r$$

$$W_{off} = \frac{1}{2} V_s t_f$$

$$P_{loss} = \frac{W_{on}}{T_s} = W_{on} f_s$$

IGBT 1200V at 300A

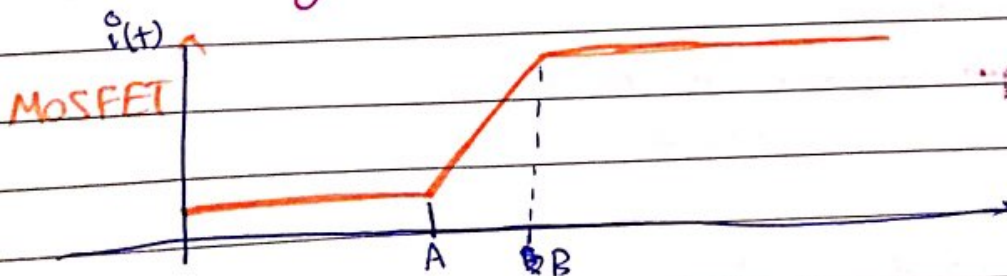
$$V_s = 2V$$

$$t_r = 1-2 \mu s$$

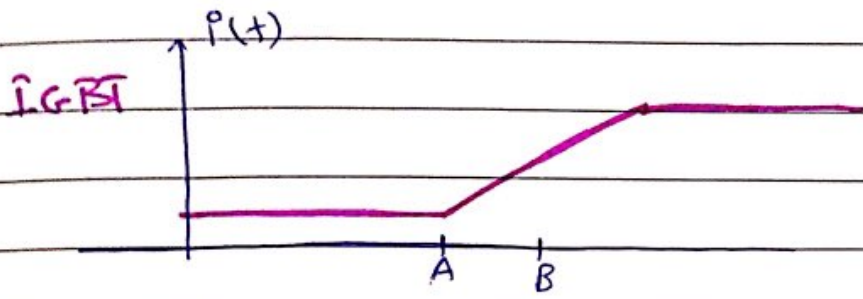
MOSFET 100ns

100 ns

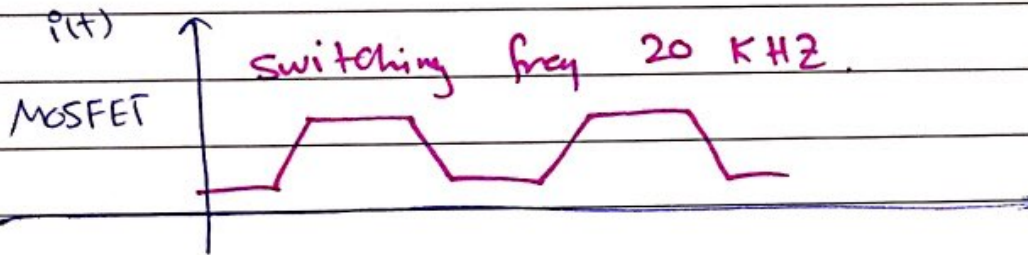
Switching Speed Vs Switching Frequency Δ



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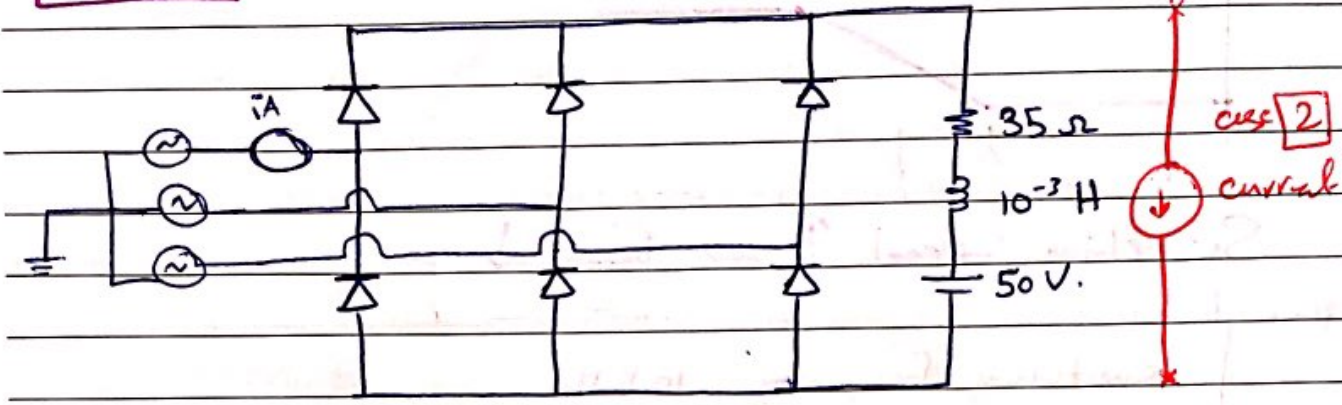


Switching speed $\uparrow \rightarrow$ losses \downarrow



switching freq $\uparrow \rightarrow$ losses \downarrow

HW 38



$V_{LL} = 208$

1 plot $V_d, I_o, i_{diode}, i_a, \text{PF}, \text{THD}, \text{Harmonic}$

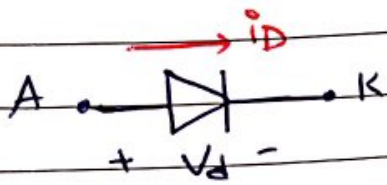
2 repeat above for 10A current source.

cover	problem	model	V_d	I_o
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/> 1 <input type="checkbox"/> 2	<input type="checkbox"/>
i_{diode}	i_a	PF THD	Case 1	Case 2
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

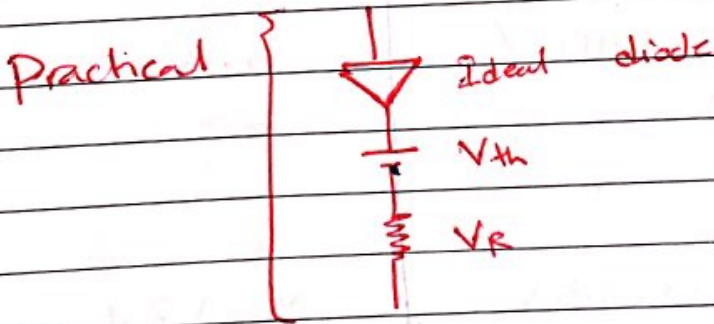
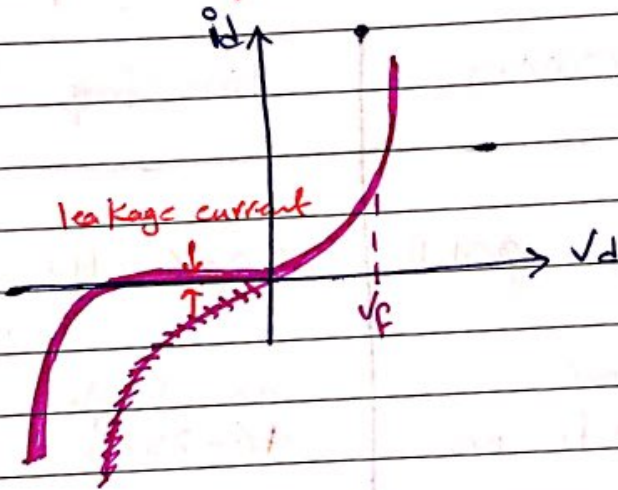
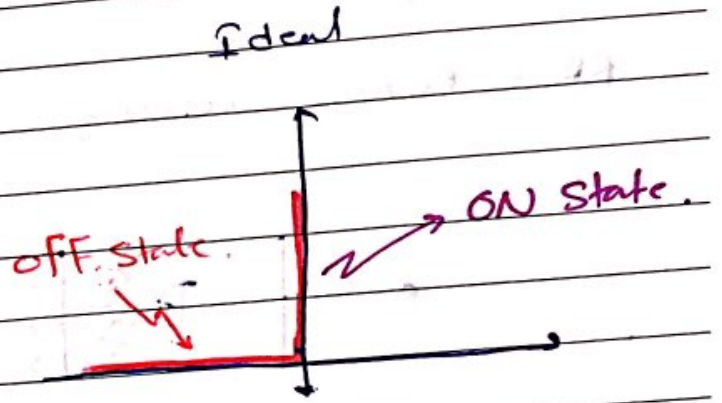
10 pages report

29/4 ← HW $\overline{\text{red}}$

* Power Diode Δ

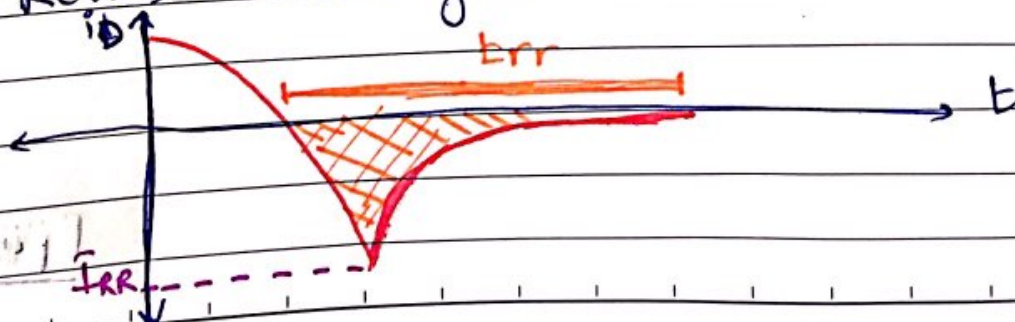


- ↳ Unidirectional
- ↳ uncontrolable



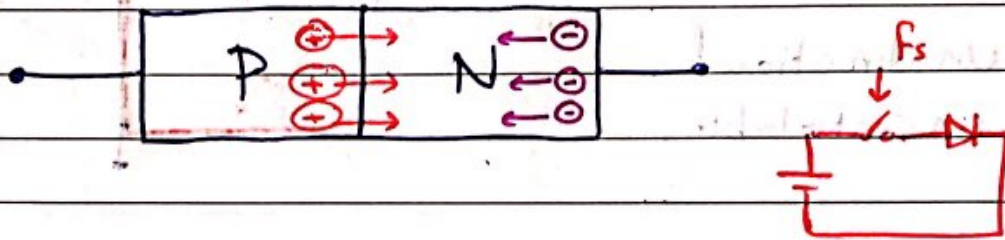
$V_{th} \downarrow \rightarrow T \uparrow$
 $R_s \uparrow \rightarrow T \uparrow$

* Reverse Recovery Δ



$$\rightarrow P_{RR} = \frac{1}{2} I_{RR} \times t_{rr}$$

RR \equiv Reverse recovery.



Schottky	Fast recovery	line freq
switching freq $f_s = \text{very high}$	$f_s = \text{high up to } 20\text{KHz}$	50-60 Hz
$t_{rr} \rightarrow$ extremely low (nano second)	t_{rr} low 0.1 μs \rightarrow few nano	t_{rr} high 16-25 μs
power rating 100V, 300A	6000V, 1100A 204 μs sep, 0.15 μs	6000V, 3500A
V_f at 30KHz $V_f = 0.6\text{V}$	$V_f = 0.8-1.5\text{V}$	$V_f = 1-2\text{V}$

* Thyristors \Rightarrow SCR \equiv Silicon controlled Rectifier

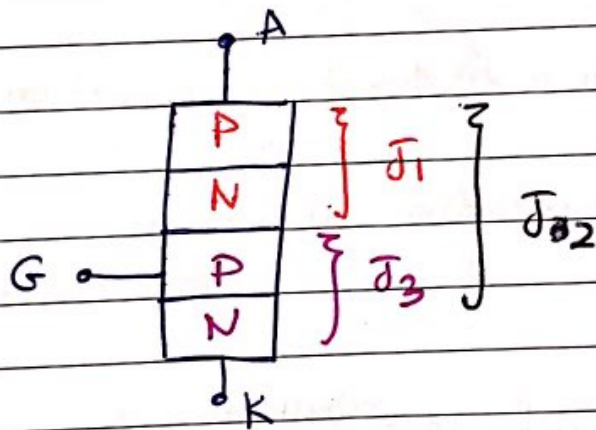
\rightarrow Uni directional

\rightarrow controlled ON only

Switching OFF for reverse bias *

\rightarrow Low ON-state.

\rightarrow multi Kilo Hz Switching



$J =$ junction.

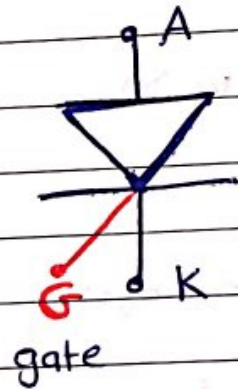
IF $V_A > V_K$

J_1 and J_3 are F.B

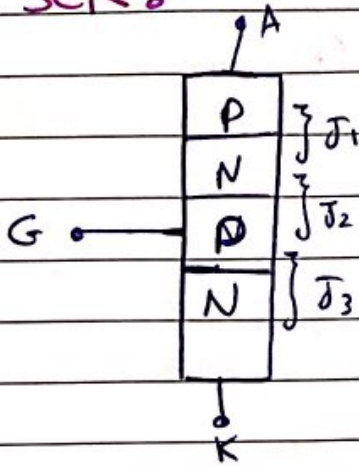
J_2 is R.D

only small leakage current flows from anode to cathode [leakage current]

\rightarrow This will make the device in forward blocking condition.

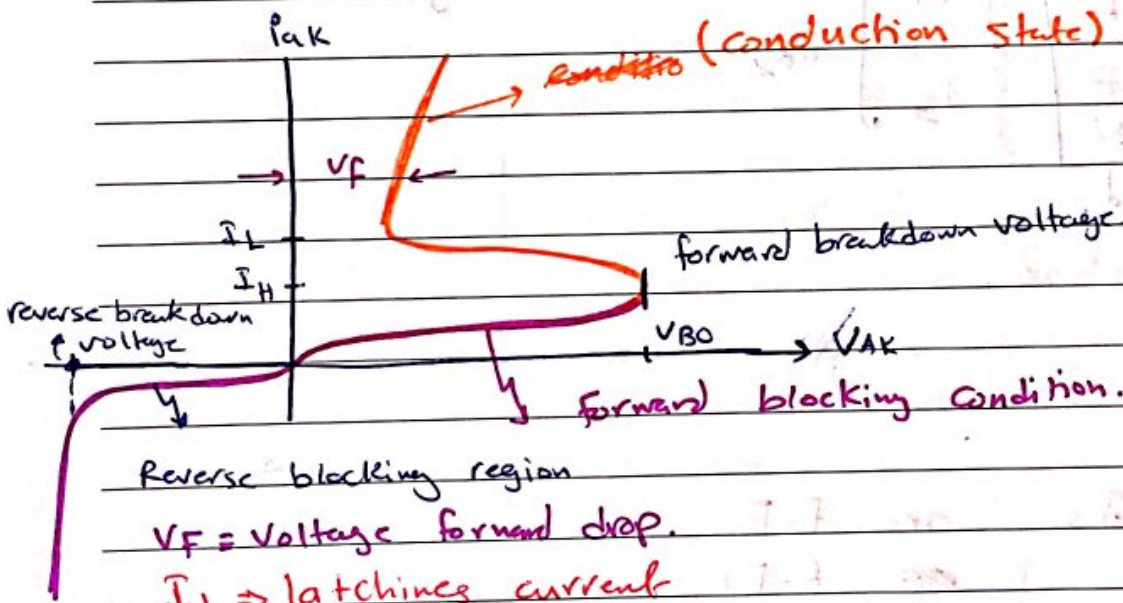


* SCR *



If $V_A > V_K$ J_1 and J_3 F.B
 J_2 R.B

→ leakages cutoff ≈ 0 [Forward blocking condition]



Reverse blocking region

V_F = Voltage forward drop.

I_L \Rightarrow latches current

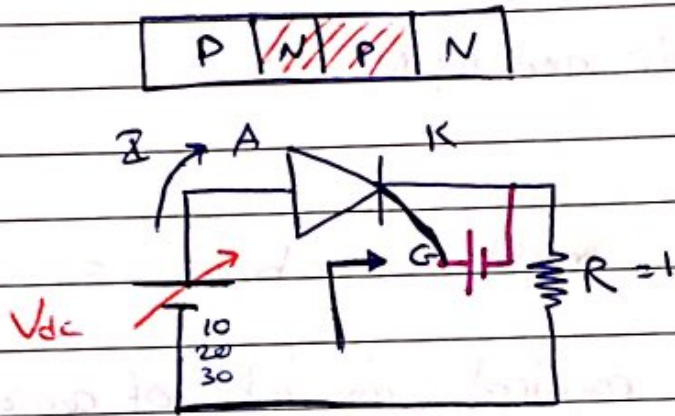
I_H \Rightarrow Holding current.

If V_{AK} is increased to a sufficiently large value J_2 breaks \Rightarrow avalanche breakdown

\Rightarrow large forward anode current. [conduction state]
 typically $V_F = 1V$

⇒ **SCR** can be turned ON by increasing the forward voltage (V_{AK}) beyond V_{BO} . But this will be destructive.

⇒ In practice, Forward voltage is maintained below V_{BO} , the voltage is applied between the gate and the Cathode.



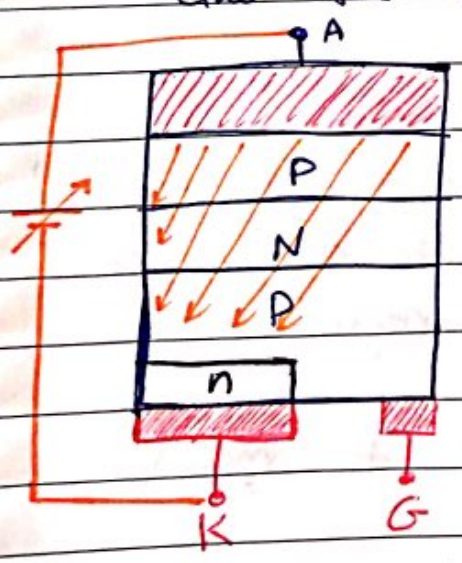
$$I = \frac{100}{R}$$

For turning on the SCR

↳ F.B

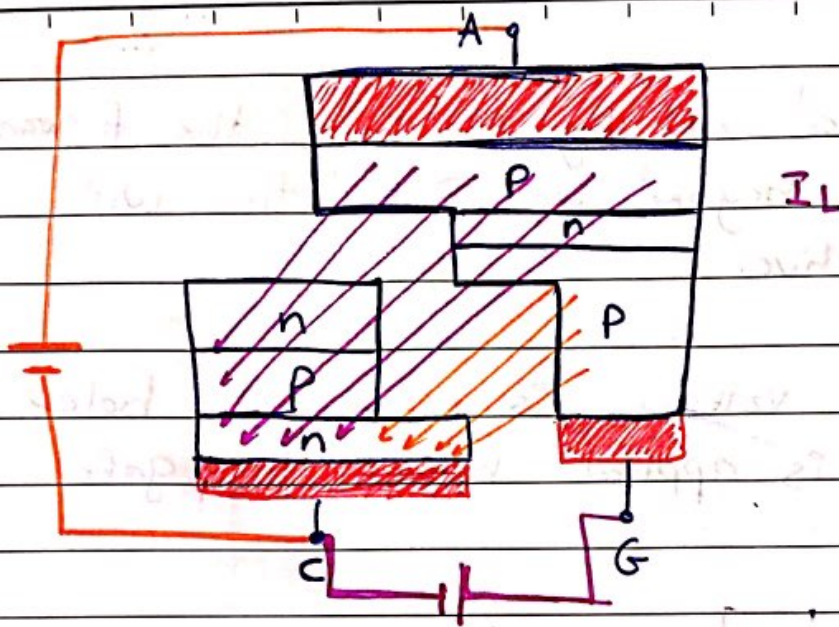
↳ apply I_{gate} (tvc voltage between the gate and the Cathode).

↳ the starting current $> I_L$



I_L 2 layer approach

PNPN structure



Sections of pnp and npn

⇒ The anode current must be above some certain value (I_L) to maintain the required amount of carrier flow across the junction or the device will ~~revert~~ revert to blocking condition.

I_L is the minimum current required to maintain the SCR in the on-state ~~revert~~ immediately after the SCR is turned ON the gate and has been removed.

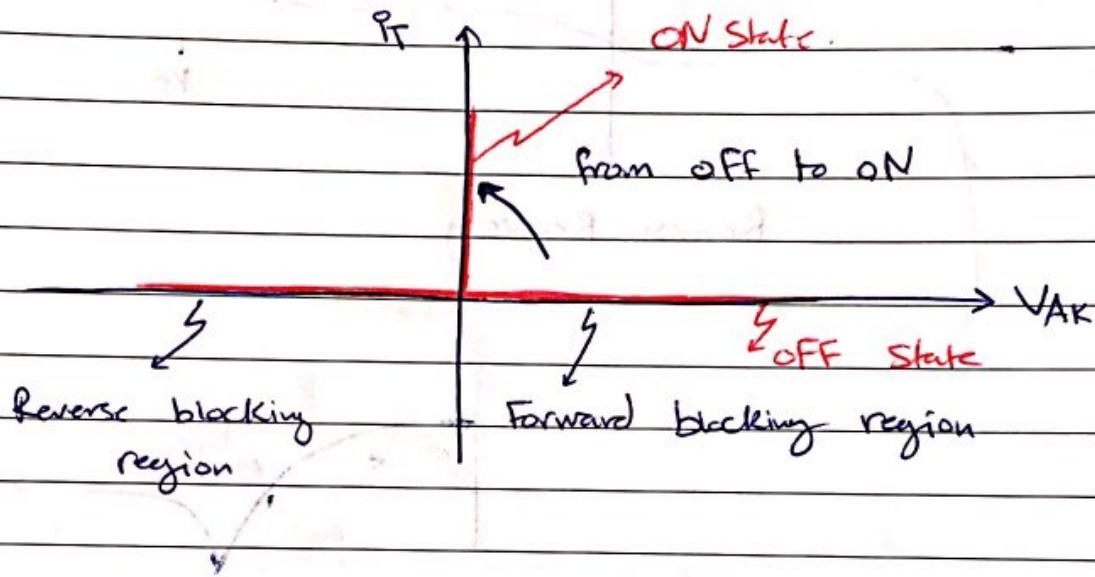
* During conduction, if the anode current is reduced below (I_H) there will be a depletion region across J_2 and the SCR is in blocking region.

I_H ~~is~~ is the minimum current to maintain the SCR in the ON-state

$$I_H < I_L$$

* SCR has a bidirectional blocking capability.
voltage

* Ideal SCR Char 84

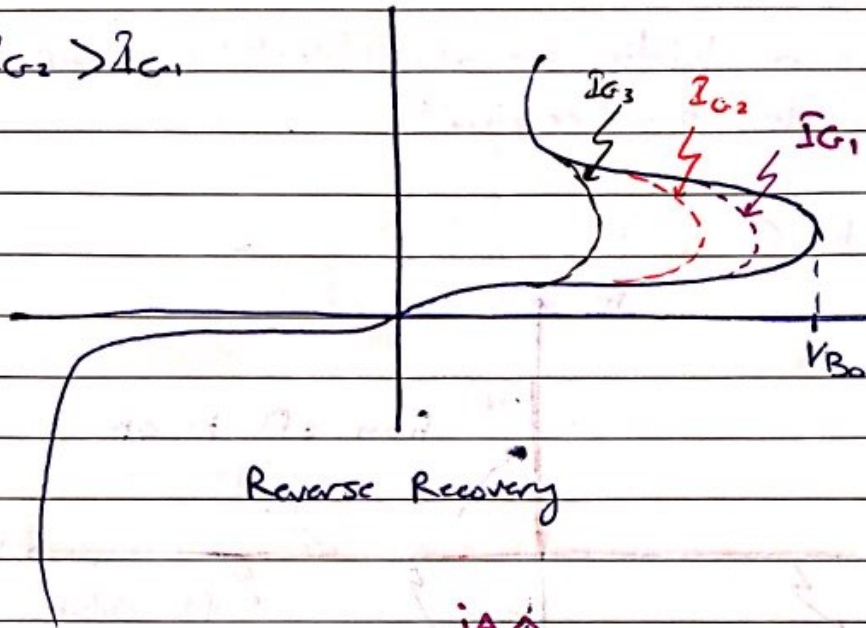


* Usually Forward blocking voltage = reverse blocking voltage.

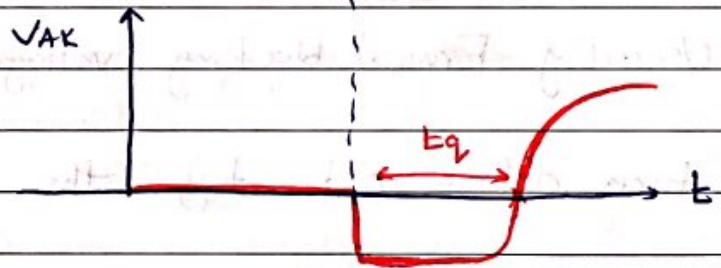
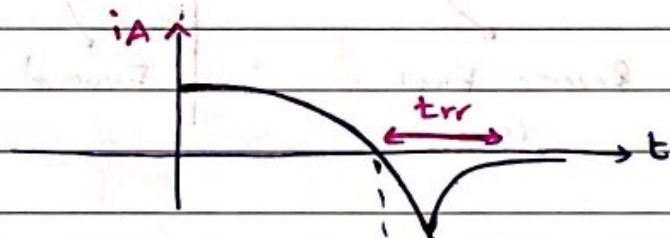
* turn off is not by the gate

↳ uncontrolled off.

$I_{G3} > I_{G2} > I_{G1}$

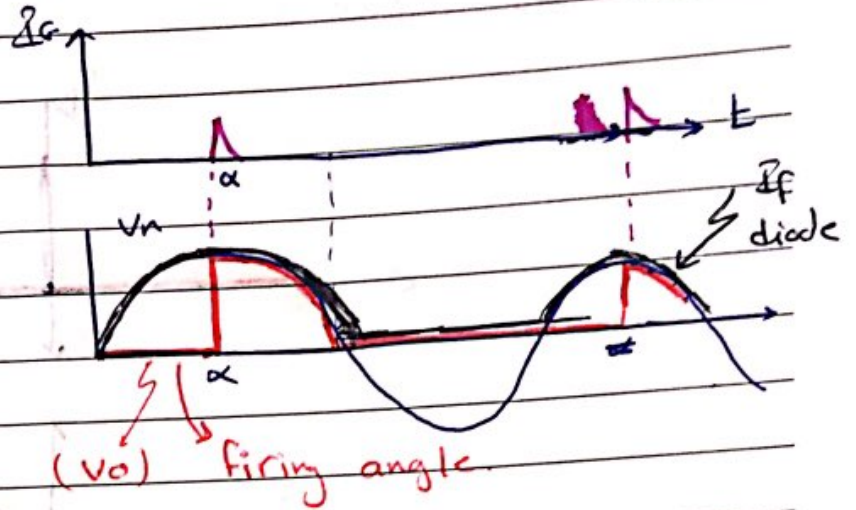
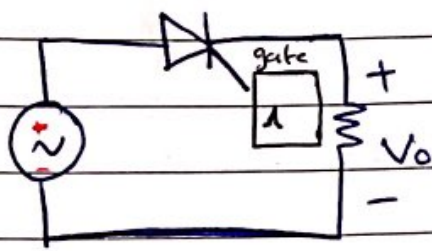


Reverse Recovery

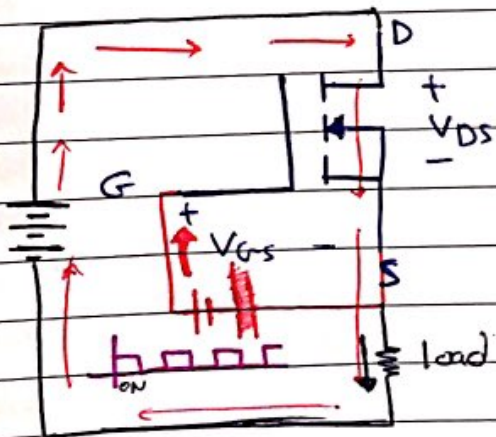
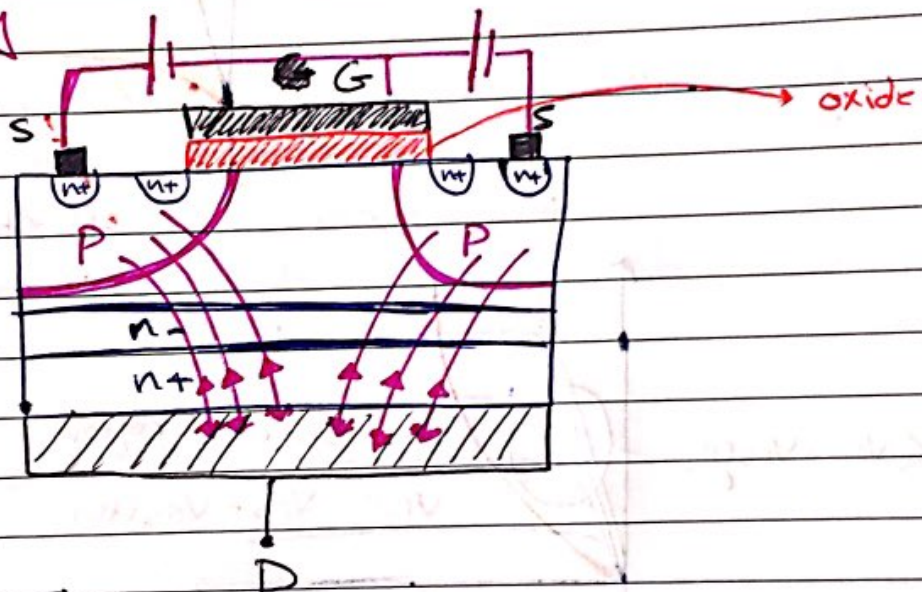


↳ $t_q \equiv$ from zero cross over of current to zero cross over of voltage.

↳ During $t_q \Rightarrow$ a reverse voltage must be maintained across the device capable of blocking a forward voltage without going into its on state.

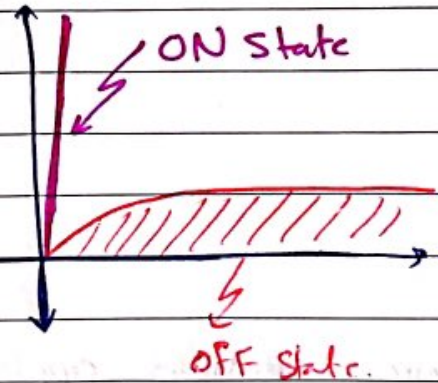
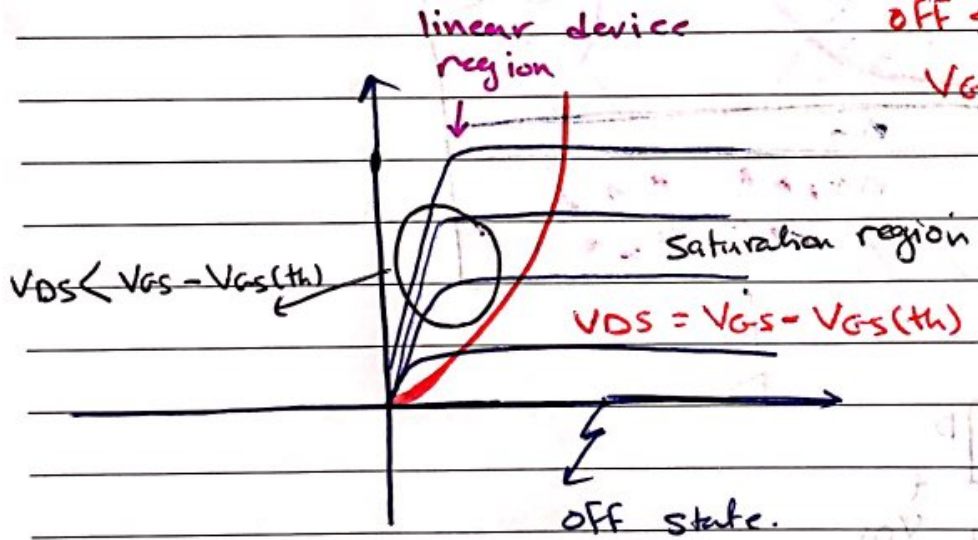
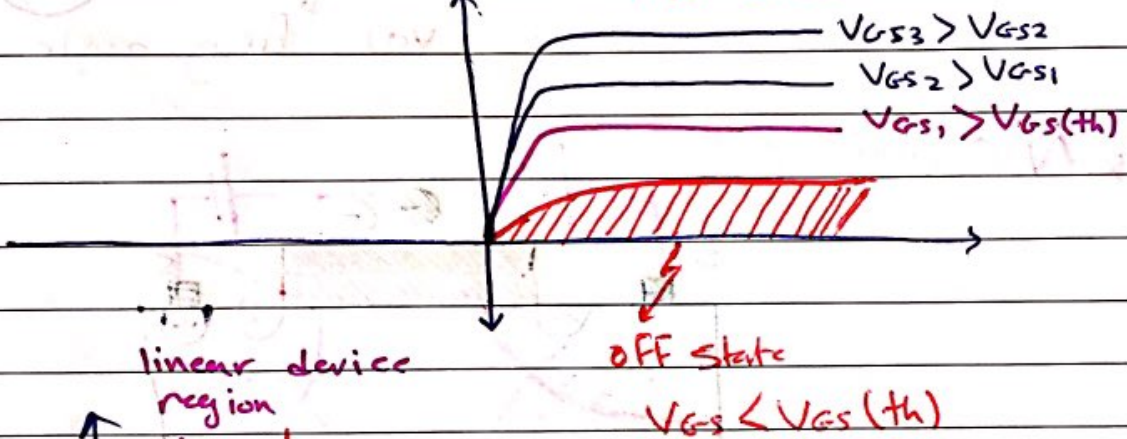
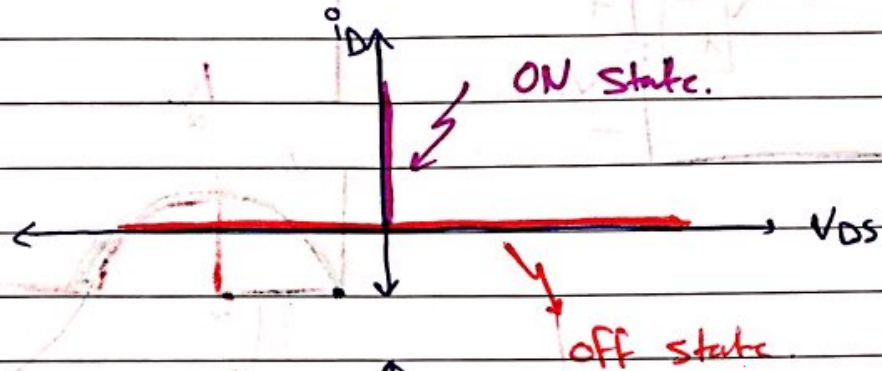


* MOSFET 84



↳ This device will require continuous application of voltage between gate and source to stay in the ON-state.

Ideal Char :-



Comment:

- * voltage controlled device.
- * No reverse voltage blocking capability [Forward only]
- * Unidirectional device.
- * In the ohmic region

$$V_{DS} = R_{DS_ON} * I_{DS}$$

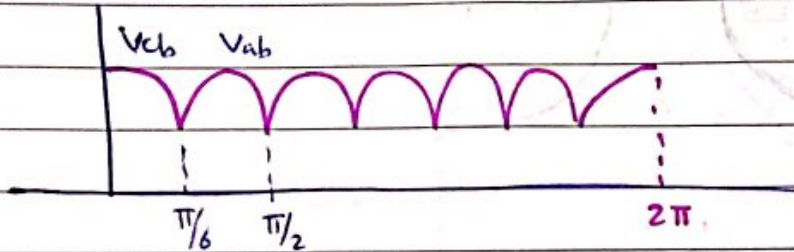
$20\text{m}\Omega$

- * In the ON state the device can be model as ~~diode~~ resistor
- * Switching time is in the range of few hundreds of nano seconds.
- * typical rating 1000V and 100A
- * $V_{GS} = \pm 5\text{V}$

$$V_{an} = V_m \sin \omega t$$

$$V_{ab} = \sqrt{3} V_m \sin(\omega t + 30)$$

$$V_{cb} = \sqrt{3} V_m \cos(\omega t)$$

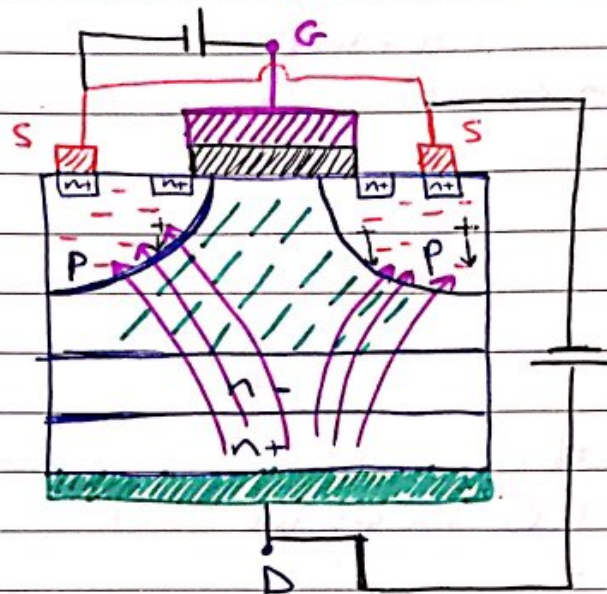


$$\begin{aligned} v_{out} &= \frac{12}{2\pi} \int_0^{\pi/6} \sqrt{3} V_m \cos \omega t \, d\omega t \\ &= \frac{6\sqrt{3} V_m}{\pi} \left[\frac{1}{2} \right] = \frac{3\sqrt{3} V_m}{\pi} \end{aligned}$$

$$\begin{aligned} v_{out} &= \frac{6}{2\pi} \int_{\pi/6}^{\pi/2} \sqrt{3} V_m \sin(\omega t + 30) \, d\omega t \\ &= \frac{3\sqrt{3} V_m}{\pi} \left[-\cos(\omega t - \pi/6) \right]_{\pi/6}^{\pi/2} \\ &= \frac{3\sqrt{3} V_m}{\pi} [0.5 + 0.5] \\ &= \frac{3\sqrt{3} V_m}{\pi} \end{aligned}$$

MOSFET 84

Vertical channel



$$V_{ds} = R_{d-on} * I_D$$

↑ thickness → ↑ power.

" power MOSFET "

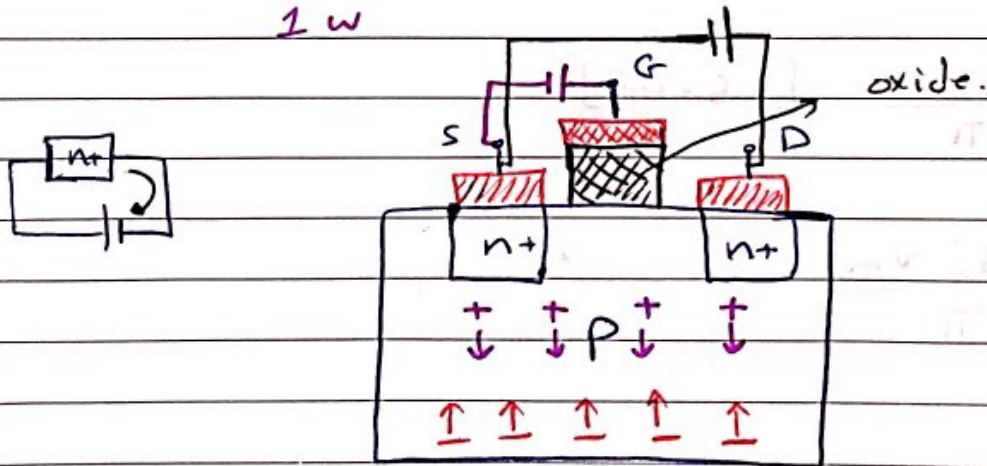
V or U

MOSFET U MOSFET

2 enhancement MOSFET

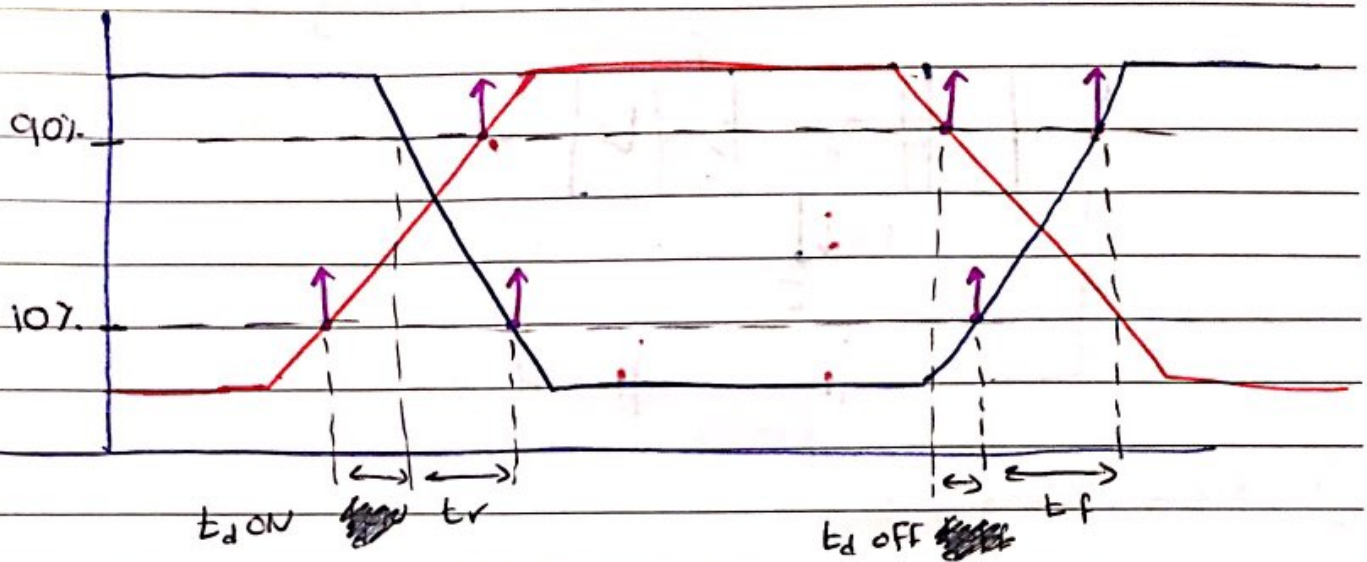
n-type

1 w



* No reverse blocking capability → only forward blocking.

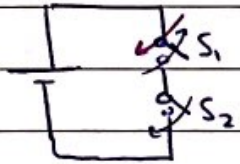
MOSFET Switching waveforms



$$t_{d ON} + t_r < t_{d OFF} + t_f$$

turning the switch ON is faster than turning it OFF

$$S_2 = 1 - S_1$$

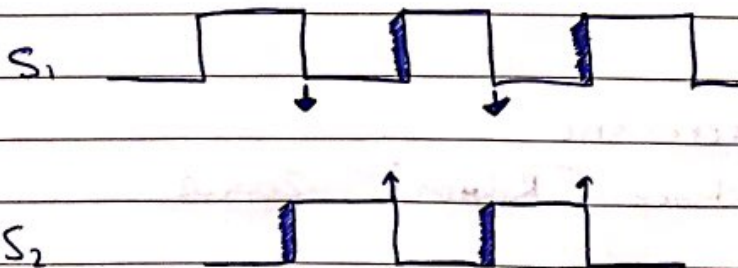


Problem:-

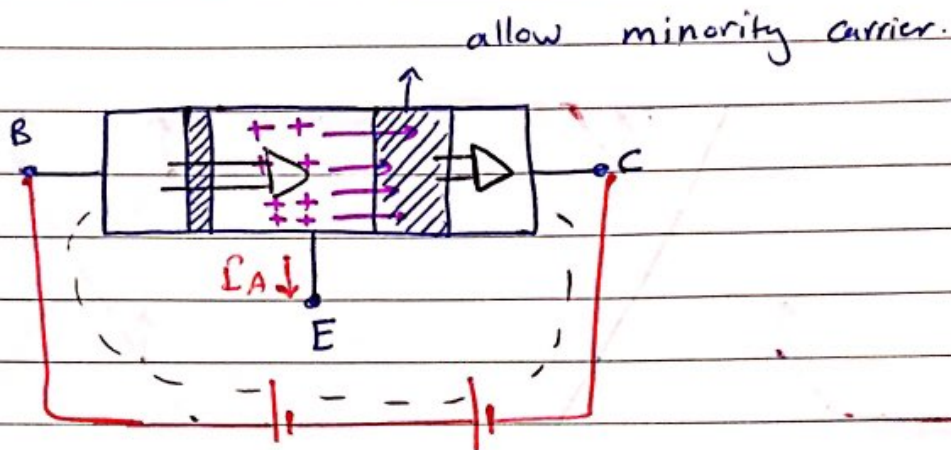
MosFET in series will short ckt the source.

solution:-

use of dead band



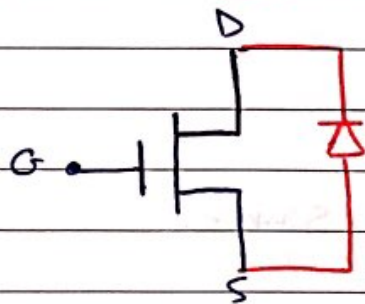
BJT 3A



Disadvantages:-

- ↳ current - controlled
- ↳ low input impedance [we need large energy to run]
- ↳ Bad in charge handling
- ↳ Low switching speed.

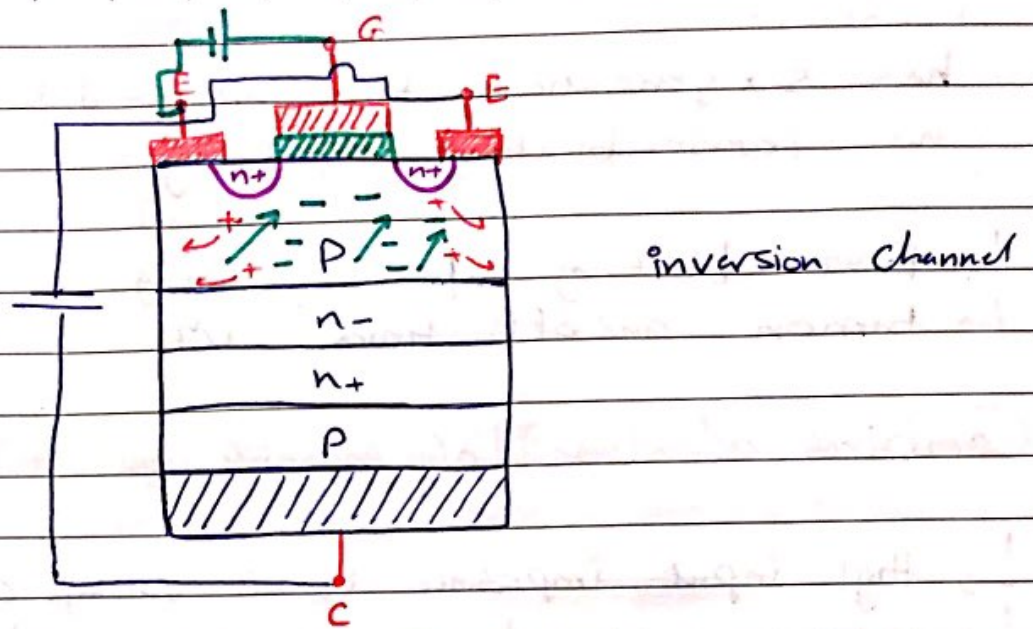
MOSFET 3A



Disadvantage:-

- ↳ Body Diode
- ↳ Bad conduction characteristic
- ↳ high-ON-state resistance [$R_{ds(on)}$] $20m\Omega$

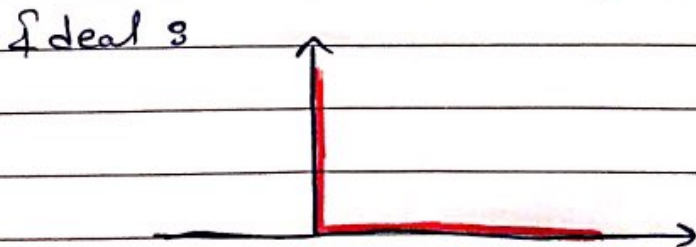
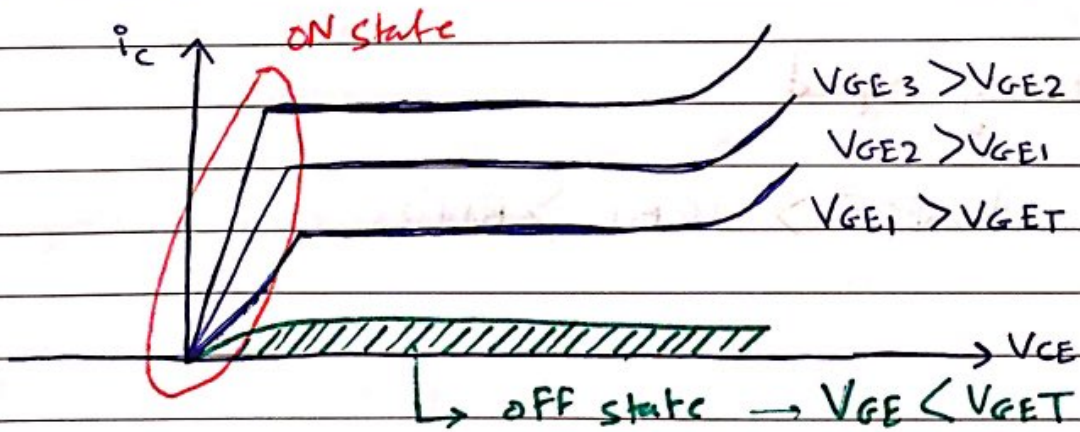
IGBT



↳ Voltage controlled device (apply V_{GE} the device will conduct).

↳ It requires continuous application of V_{GE} in order to stay in the ON-state mode.

↳ Unidirectional device.



IGBT:-

has six generations, the up-to-date version has no reverse blocking capability.

- ↳ Forward blocking capability only
- ↳ turnon and off times $1\mu s$

Combines advantage of MOSFET and BJT:-

- ↳ High input impedance (small voltage cause large energy)
- ↳ voltage controlled device (power and control CKT are completely independent)
- ↳ V_f is small like BJT.

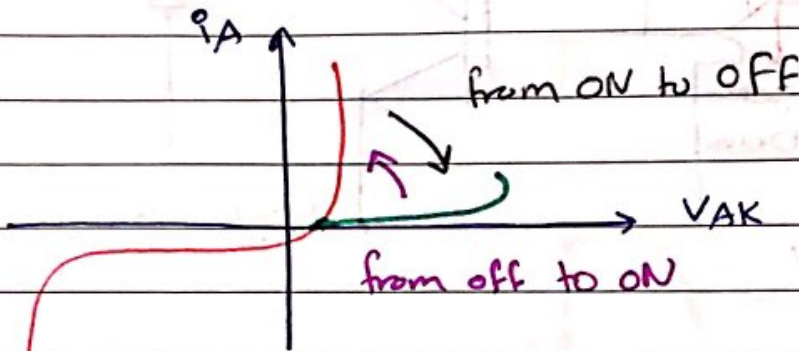
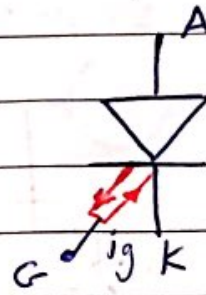
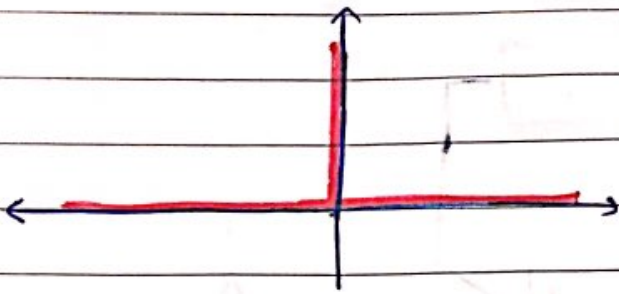
Current rating Δ

$BJT > IGBT > MOSFET$

Switching Speed

$MOSFET > IGBT > BJT$.

GTO: Gate turn-off Thyristor.



↳ $V_f = (2-3) V$

↳ Switching Speed few $\mu s - 25 \mu s$

↳ V & Rating [4.5 KV - few KA]

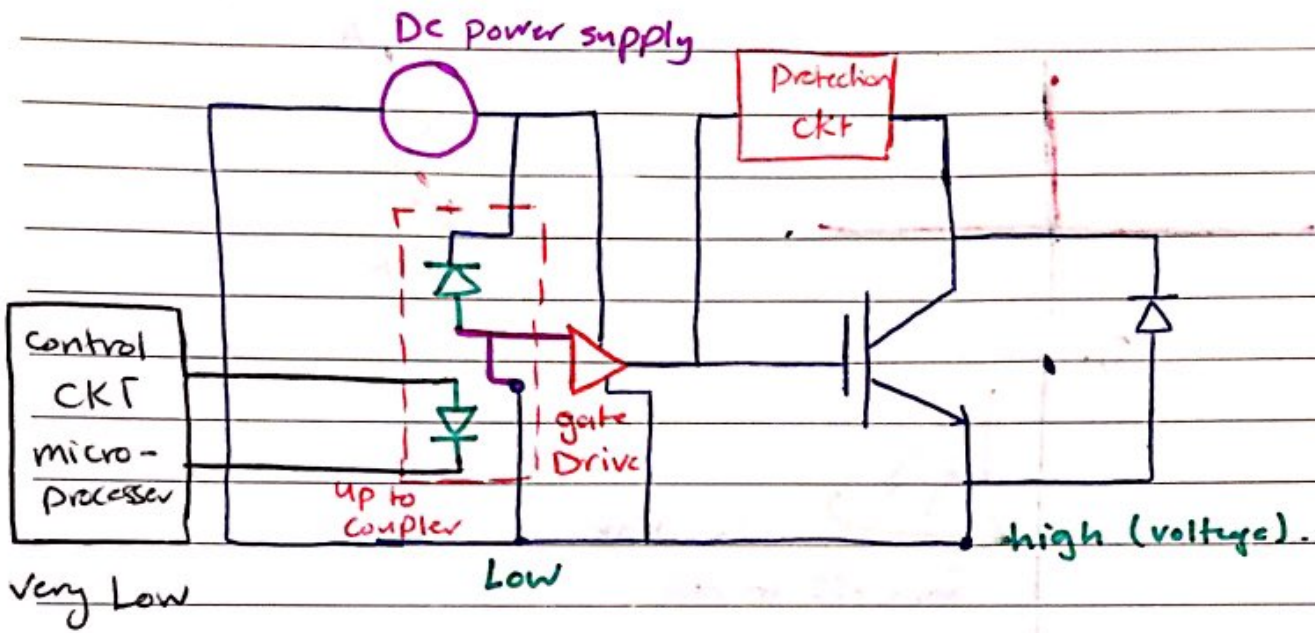
↳ Voltage → current

↳ Gate current turn ON, only in the beginning (small value)

↳ Gate can be turned off by applying very large negative gate current $[\frac{1}{3} i_A]$ by applying -ve V_{GC}

↳ this large current needs to flow for few seconds

Gate Drive 8Δ



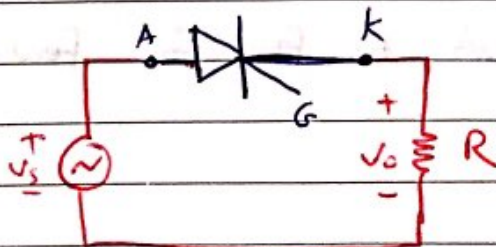
Disadvantage:-

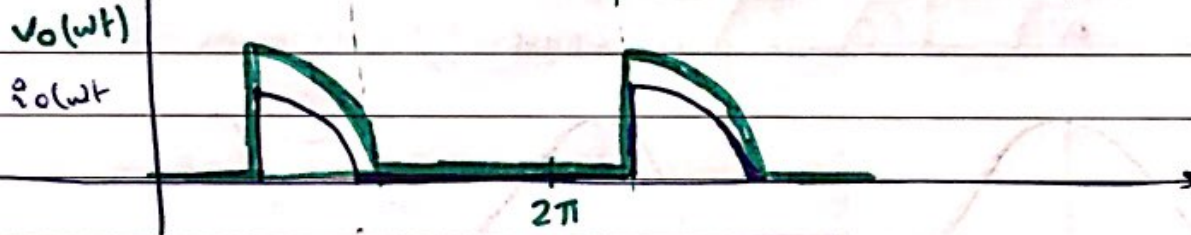
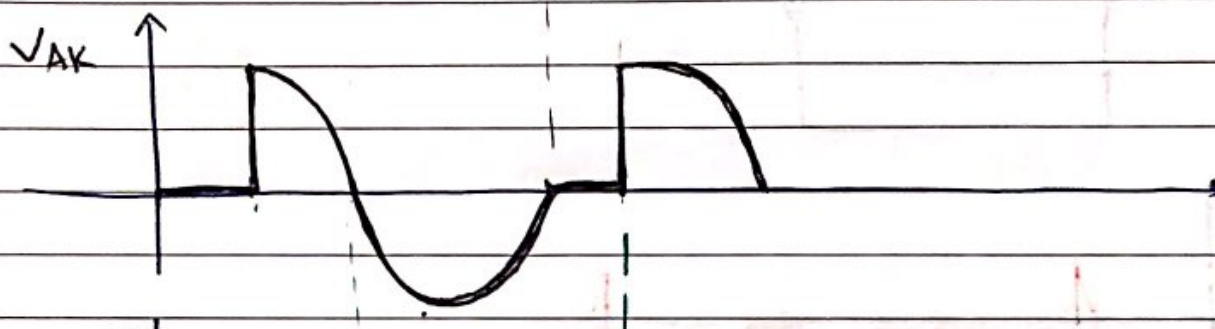
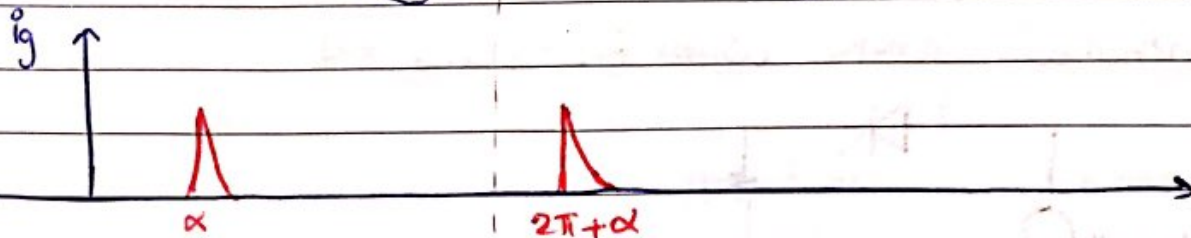
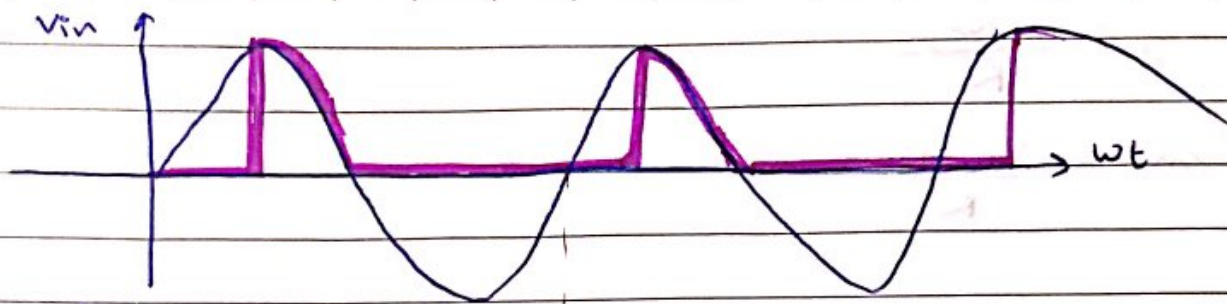
- ↳ turn ON and turn off the switch
- ↳ protect the device in cause of different type of failure
- ↳ Control the speed.

The Controlled HWR 8Δ

SCR :-

- ↳ FB
- ↳ current must be applied to the gate at ~~the~~ firing angle.





$$V_o = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin(\omega t) d\omega t$$

$$V_o = \frac{V_m}{2\pi} [1 + \cos \alpha]$$

not $\alpha = 0$ $V_o = \frac{V_m}{2\pi}$

$$V_{orms} = \sqrt{\frac{1}{2\pi} \int_{\alpha}^{\pi} V_m^2 \sin^2 \omega t d\omega t}$$

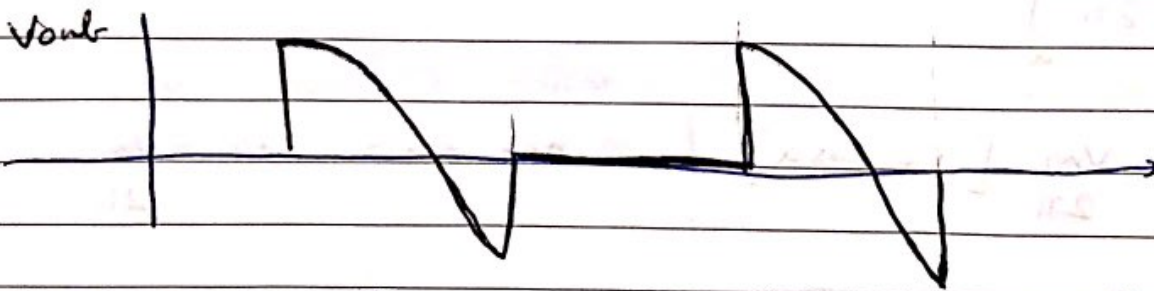
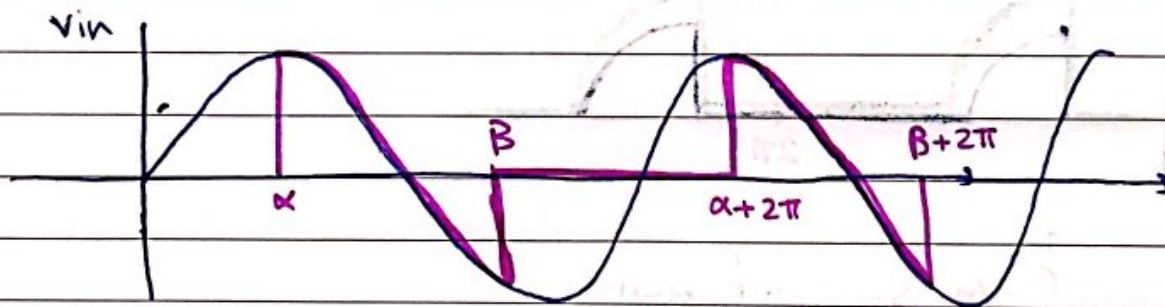
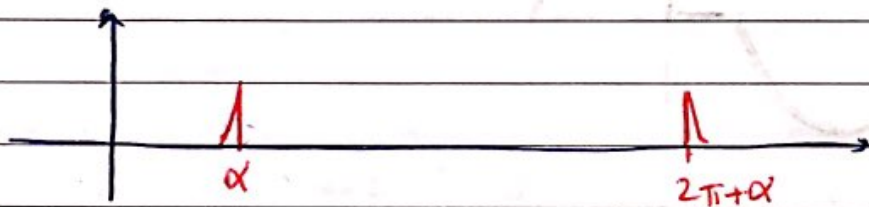
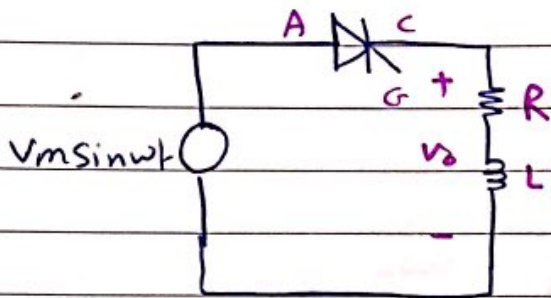
$$= \frac{V_m}{2} \sqrt{1 - \frac{\alpha}{\pi} + \frac{\sin(2\alpha)}{2\pi}}$$

radings

$$I_{o \text{ avg}} = \frac{V_{o \text{ avg}}}{R}$$

$$I_{o \text{ rms}} = \frac{V_{o \text{ rms}}}{R}$$

Controlled HWR with RL-load $\theta \Delta$



$$i_{fn} = i_o(\omega t) = \begin{cases} \frac{V_m}{Z} \sin(\omega t - \theta) - \frac{V_m}{Z} \sin(\alpha - \theta) e^{\frac{\alpha - \omega t}{\omega T}} & \alpha \leq \omega t \leq \beta \\ 0 & \text{elsewhere} \end{cases}$$

$$V_{out \text{ avg}} = \frac{1}{2\pi} \int_{\alpha}^{\beta} V_m \sin(\omega t) d\omega t = \frac{V_m}{2\pi} [\cos \alpha - \cos \beta]$$

$$V_{rms} = \sqrt{\frac{1}{2\pi} \int_{\alpha}^{\beta} v_m^2 \sin^2(\omega t) d\omega t}$$

$$I_o \text{ avg} = \frac{1}{2\pi} \int_{\alpha}^{\beta} i_o(\omega t) d\omega t$$

$$I_o \text{ rms} = \sqrt{\frac{1}{2\pi} \int_{\alpha}^{\beta} i_o^2(\omega t) d\omega t}$$

$$Z = \sqrt{R^2 + \omega L^2}$$

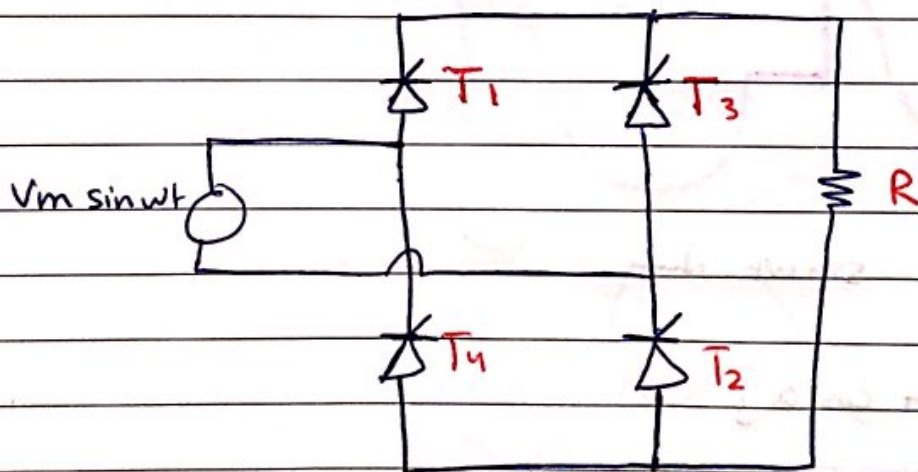
$$\theta = \tan^{-1}\left(\frac{\omega L}{R}\right)$$

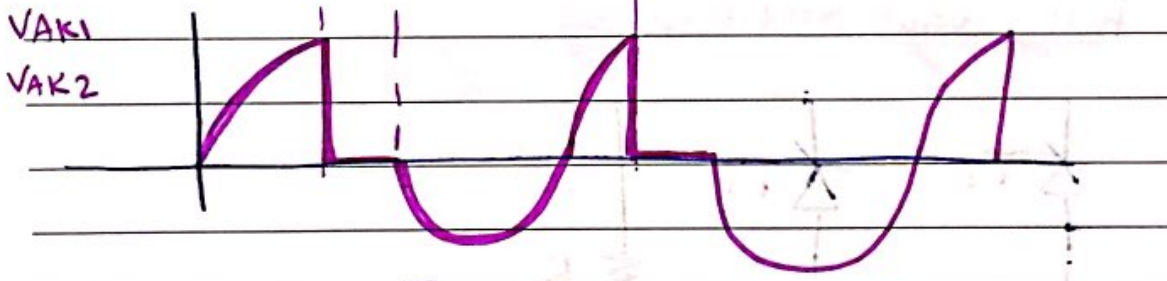
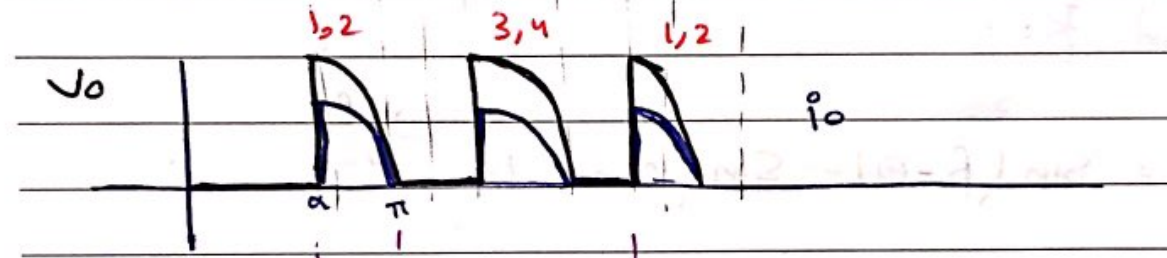
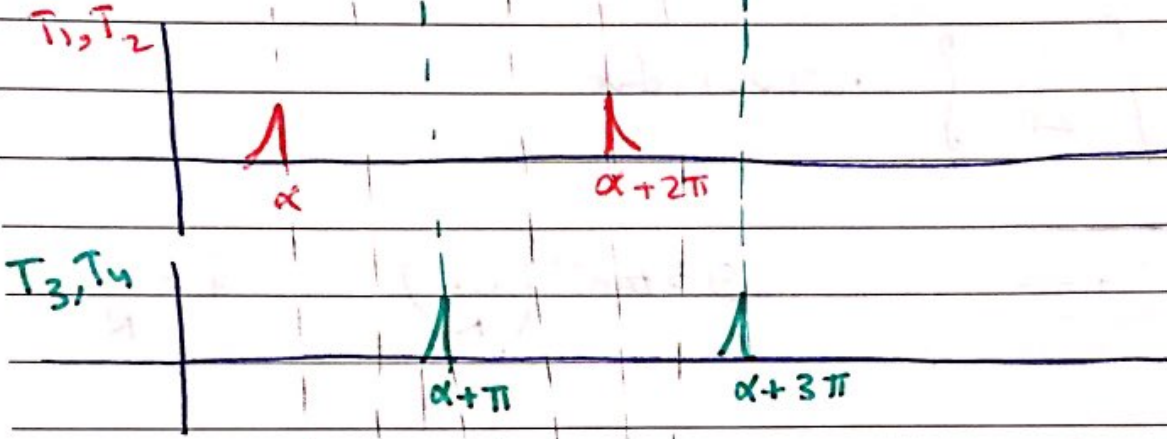
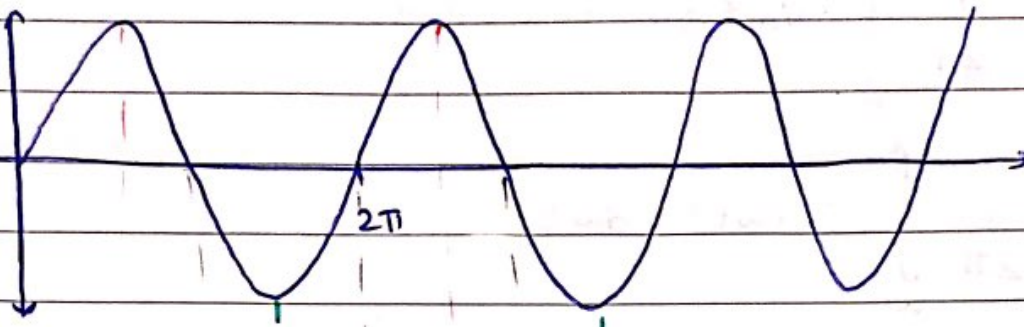
$$\phi = \frac{L}{R}$$

How to find β :-

$$i(\beta) = 0 = \sin(\beta - \theta) - \sin(\alpha - \theta) e^{\frac{(\alpha - \beta)}{\omega \tau}}$$

* Controlled Full wave Rectifier as





$$V_{o\text{avg}} = \frac{1}{\pi} \int_{\alpha}^{\pi} V_m \sin \omega t \, d\omega t$$

$$= \frac{V_m}{\pi} [1 + \cos \alpha]$$

$$V_{o\text{rms}} = \sqrt{\frac{1}{\pi} \int_{\alpha}^{\pi} V_m^2 \sin^2 \omega t \, d\omega t}$$

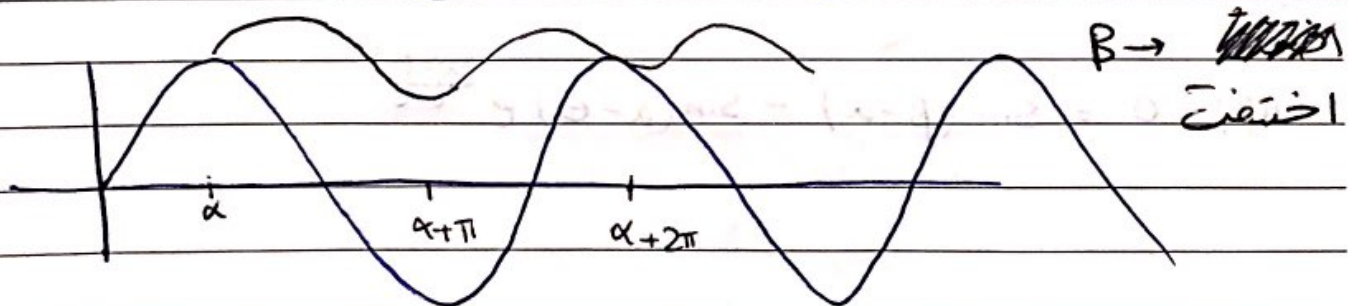
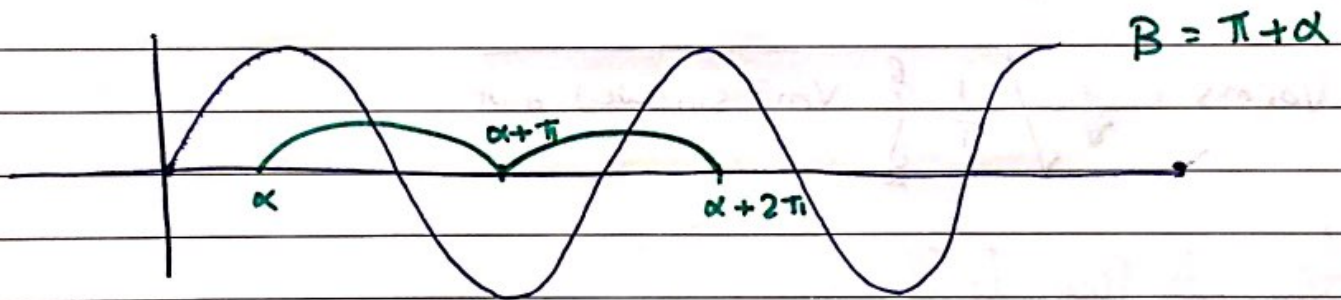
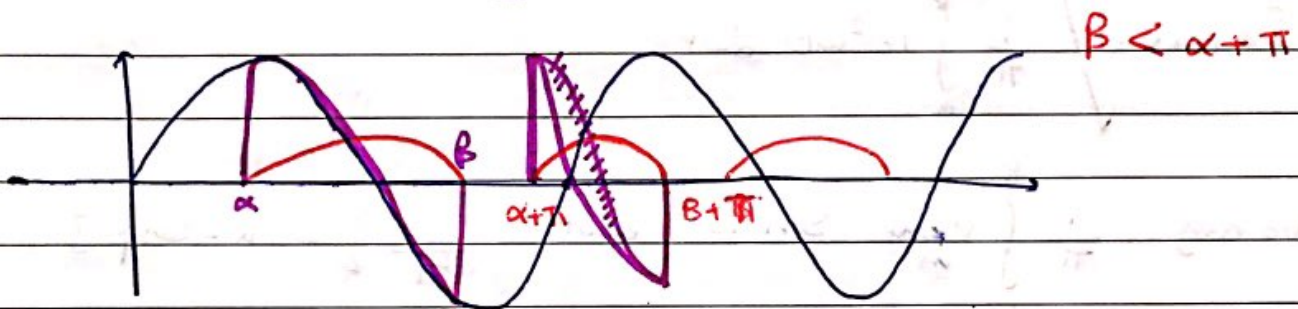
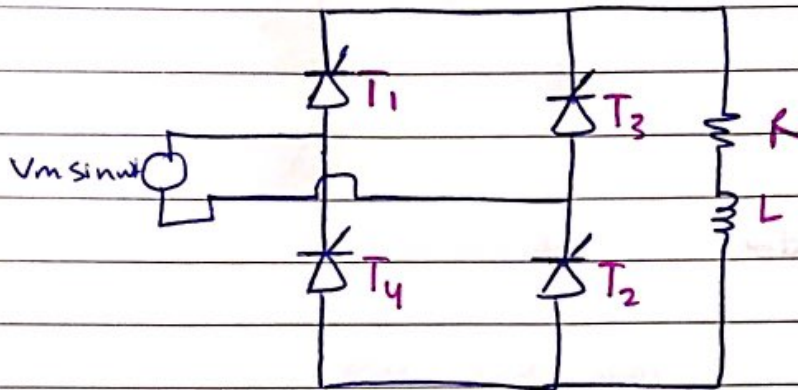
$$= V_m \sqrt{\frac{1}{2} - \frac{\alpha}{2\pi} + \frac{\sin 2\alpha}{4\pi}}$$

radian

$$I_{o\text{avg}} = \frac{V_{o\text{avg}}}{R}$$

$$I_{o\text{rms}} = \frac{V_{o\text{rms}}}{R}$$

Controlled Full wave rectifier with R-L Load :-



Discontinuous Mode Δ

$$i_o(\omega t) = \begin{cases} \frac{V_m}{Z} [\sin(\omega t - \theta) - \sin(\alpha - \theta)] e^{\frac{(\alpha - \omega t)}{\omega C}} & \alpha \leq \omega t \leq \beta \\ 0 & \text{elsewhere} \end{cases}$$

$$I_o \text{ avg} = \frac{1}{\pi} \int_{\alpha}^{\beta} i_o(\omega t) d\omega t$$

$$I_o \text{ rms} = \sqrt{\frac{1}{\pi} \int_{\alpha}^{\beta} i_o^2 \omega t d\omega t}$$

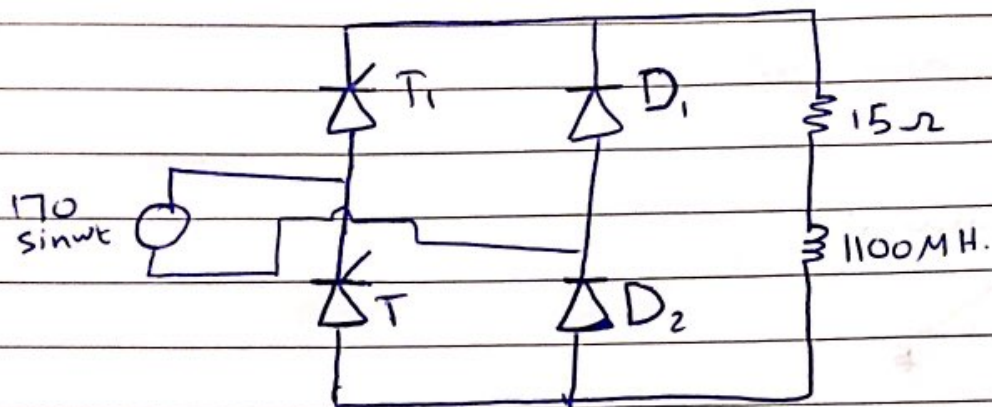
$$V_o \text{ avg} = \frac{1}{\pi} \int_{\alpha}^{\beta} V_m \sin \omega t d\omega t = \frac{V_m}{\pi} [\cos \alpha - \cos \beta]$$

$$V_o \text{ rms} = \sqrt{\frac{1}{\pi} \int_{\alpha}^{\beta} V_m^2 \sin^2(\omega t) d\omega t}$$

How to find β ?

$$i(\beta) = 0 = \sin(\beta - \alpha) - \sin(\alpha - \theta) e^{\frac{(\alpha - \beta)}{\omega C}}$$

Home work 484.



Simulate the ckt shown &

T_1 is triggered at 45°

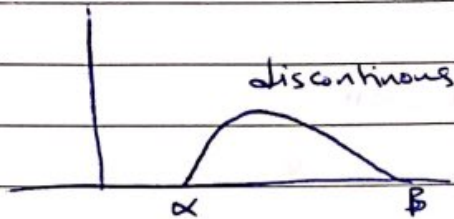
T_2 is " " " 225°

Show the result for :-

- 1] i_s and V_s [source current and voltage.]
- 2] v_{avg} and V_{rms}
- 3] repeat the above with a constant current source [10A] replaces the RL load.

Full wave controlled Rectifier with R-L load

↳ discontinuous mode $\theta > \Delta$



$$\sin(\beta - \theta) - \sin(\alpha - \theta) e^{-\frac{\alpha - \beta}{\omega\tau}} = 0$$

For continuous Mode $\theta < \Delta$

$$i_o(\omega t) > 0$$

for $\omega t = \alpha + \pi$

$$\frac{V_m}{Z} \left[\sin(\pi + \alpha - \theta) - \sin(\alpha - \theta) e^{-\frac{\alpha - \pi + \alpha}{\omega\tau}} \right] > 0$$

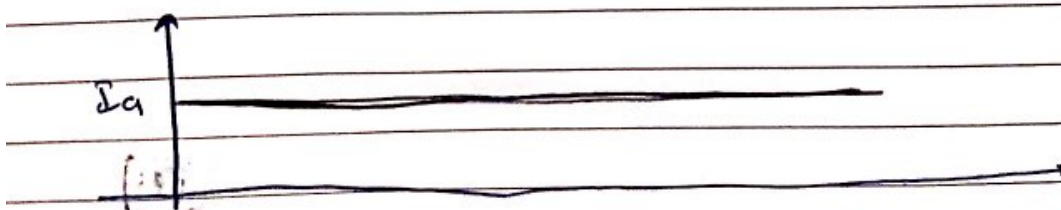
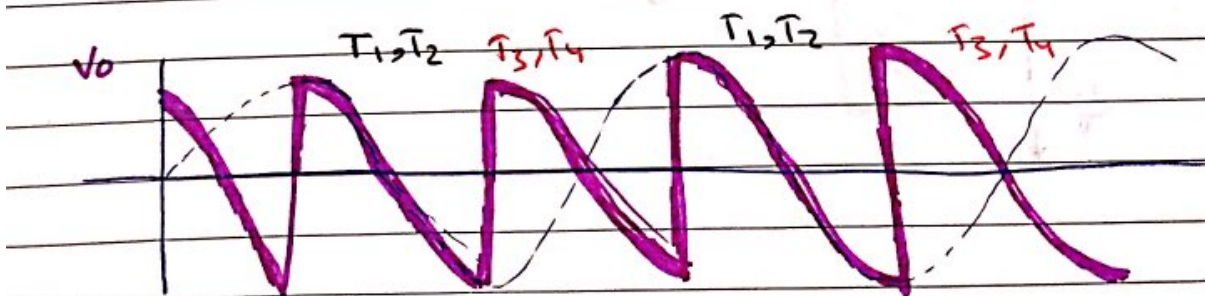
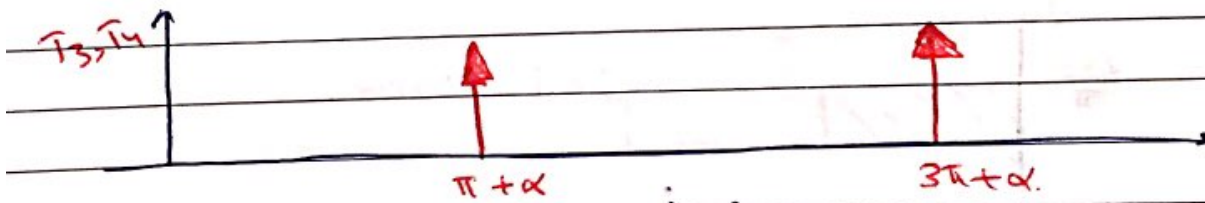
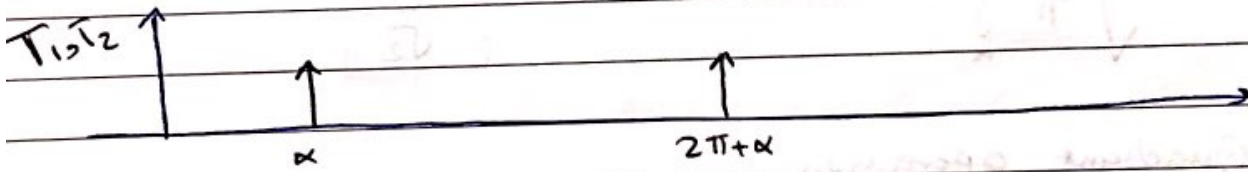
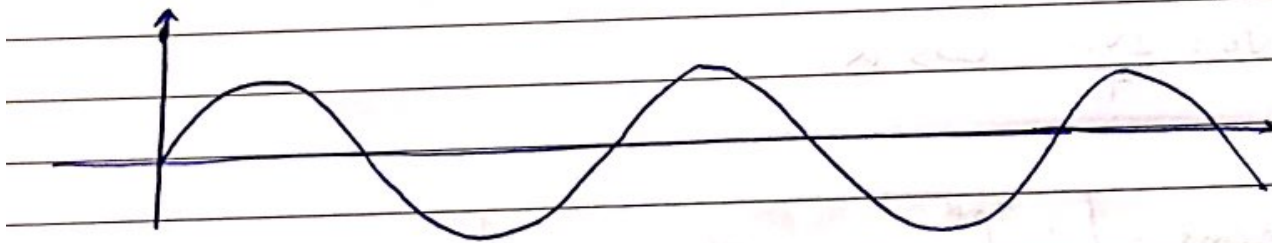
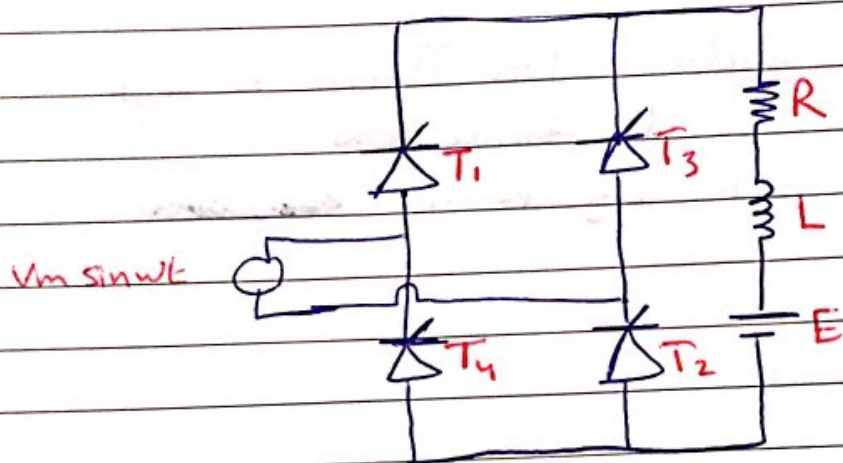
$$\sin(\theta - \alpha) \left[1 + \sin(\theta - \alpha) e^{-\frac{\pi}{\omega\tau}} \right] > 0$$

$$\sin(\theta - \alpha) > 0$$

$$\alpha < \theta$$

$$\alpha < \tan^{-1} \frac{\omega L}{R}$$

FW controlled rectifier with RL load [highly inductive] a battery



Triggering occurred at α when α is greater than $\sin^{-1}\left(\frac{E}{V_m}\right)$

T_1, T_2 Continuous to conduct after π due to high inductance, until T_3, T_4 is turned ON

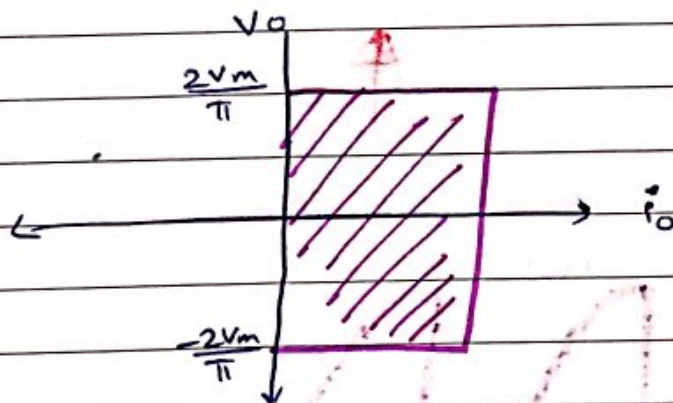
T_1, T_2 are turned off by natural commutation

$$V_o = \frac{1}{\pi} \int_{\alpha}^{\pi+\alpha} V_m \sin \omega t \, d\omega t$$

$$V_o = \frac{2V_m}{\pi} \cos \alpha$$

$$V_{o\text{rms}} = \sqrt{\frac{1}{\pi} \int_{\alpha}^{\pi+\alpha} V_m \sin(\omega t) \, d\omega t} = \frac{V_m}{\sqrt{2}}$$

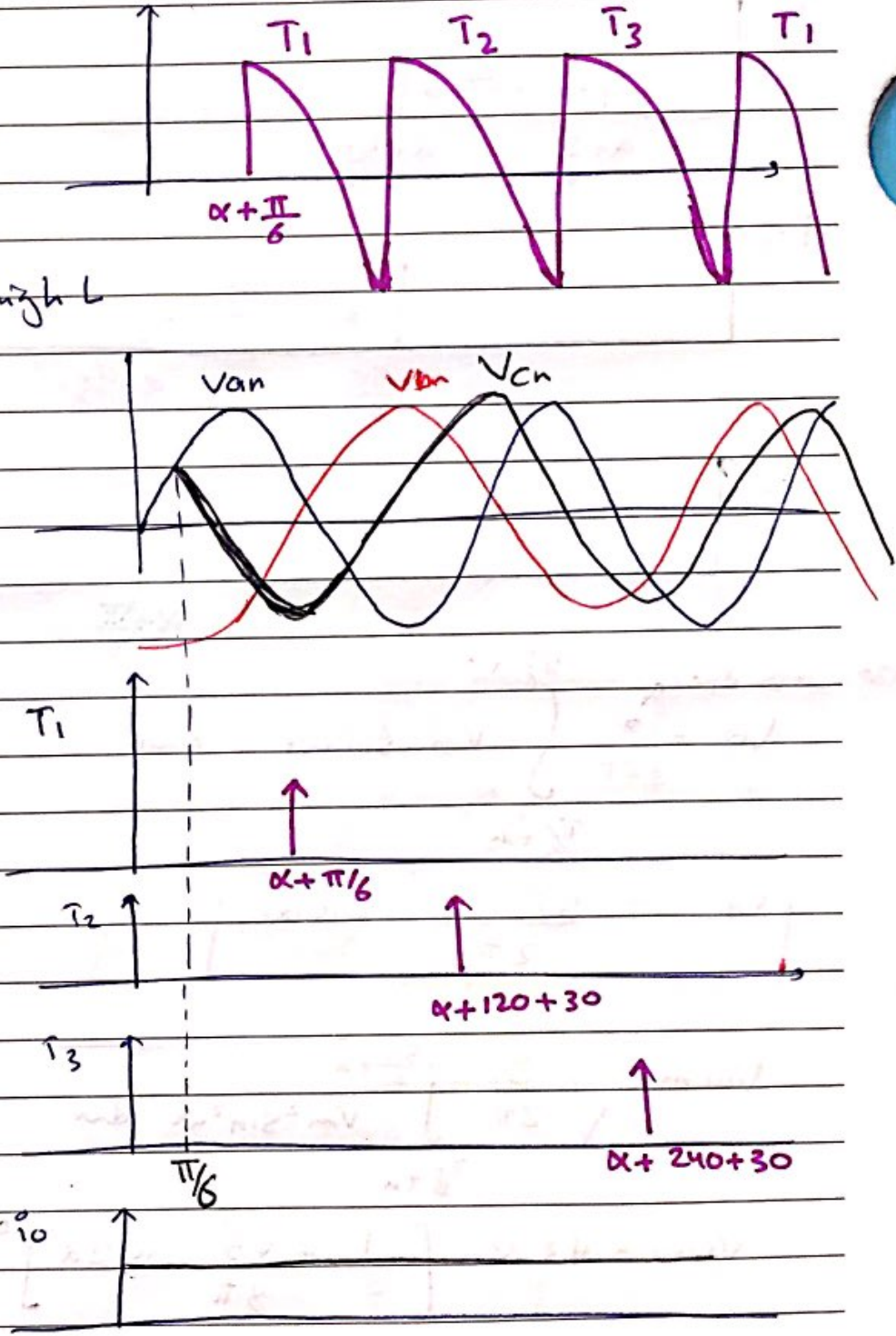
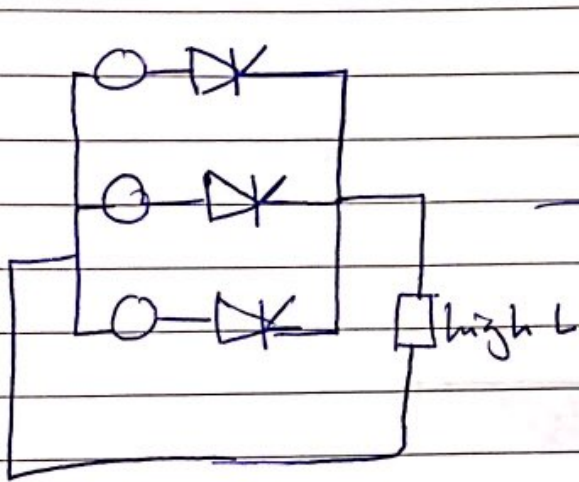
* 2 Quadrant operation.



Semi inverter.

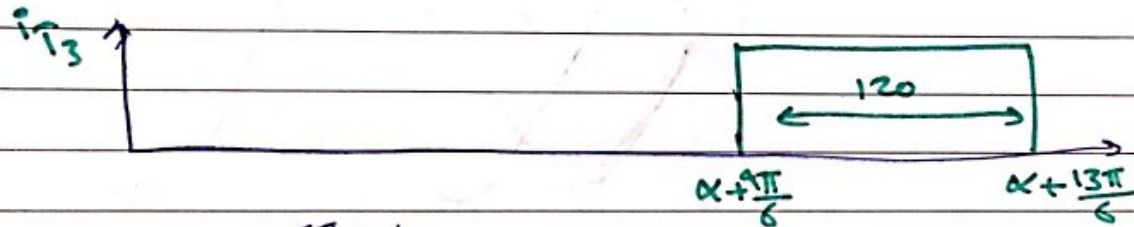
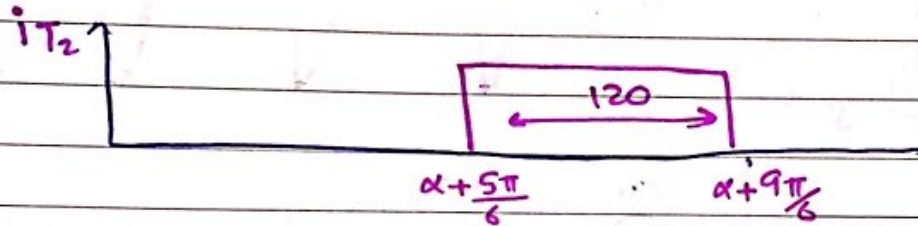
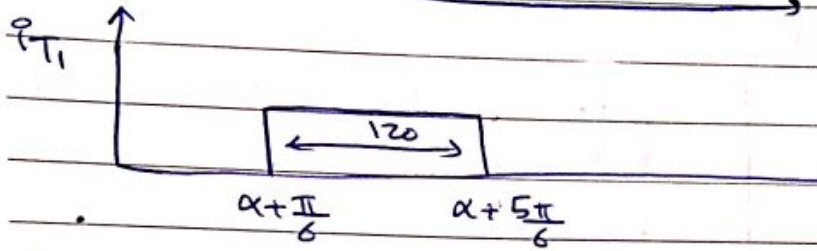
EX 10.1

3 ϕ Controlled HWR



174

174



120° 2π/3 3π/2

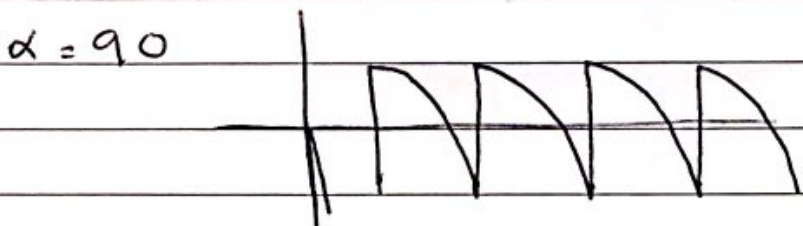
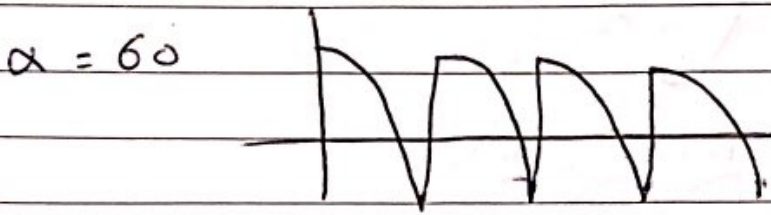
$$V_{dc} = \frac{3}{2\pi} \int_{\frac{\pi}{6} + \alpha}^{\frac{5\pi}{6} + \alpha} V_m \sin \omega t \, d\omega t$$

$$V_{dc} = \frac{3\sqrt{3} V_m \cos \alpha}{2\pi}$$

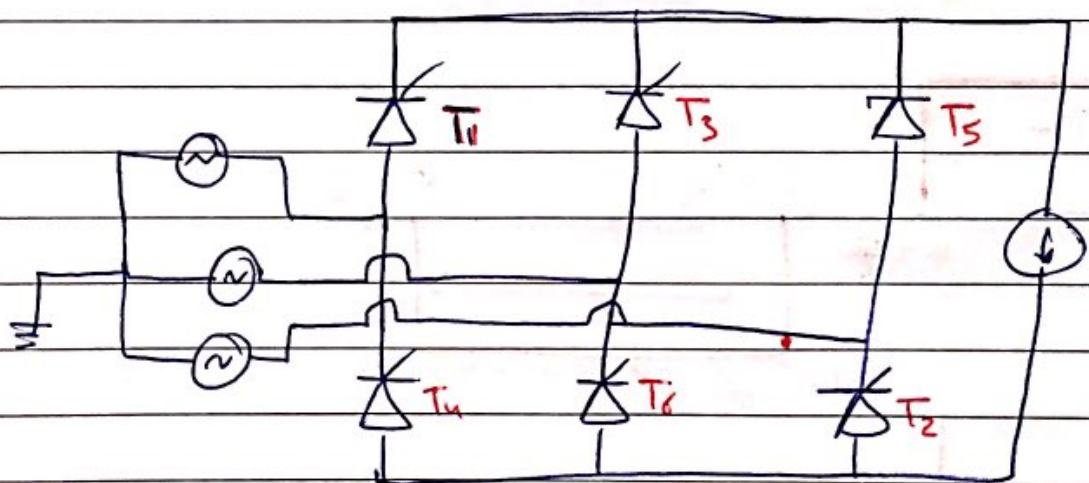
$$V_{rms} = \sqrt{\frac{3}{2\pi} \int_{\frac{\pi}{6} + \alpha}^{\frac{5\pi}{6} + \alpha} V_m^2 \sin^2 \omega t \, d\omega t}$$

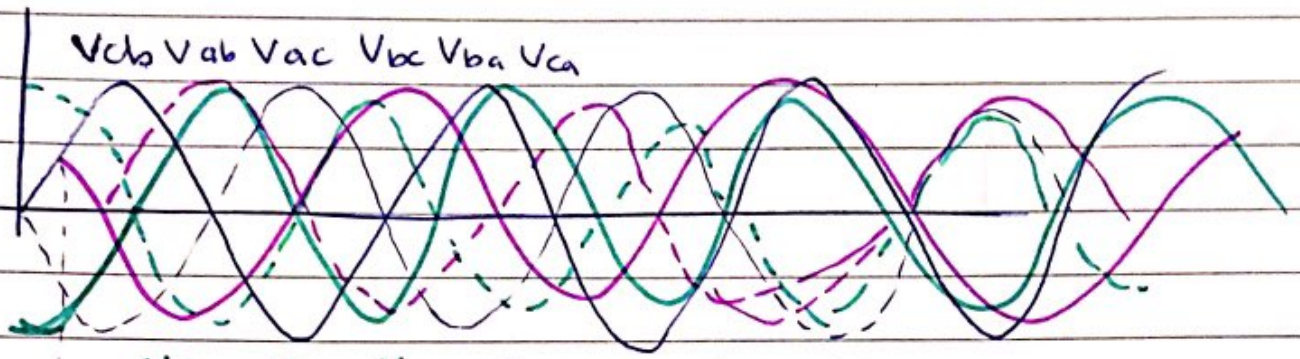
$$V_{rms} = \sqrt{3} V_m \left[\frac{1}{6} + \frac{\sqrt{3}}{8\pi} \cos 2\alpha \right]^{0.5}$$

HWR

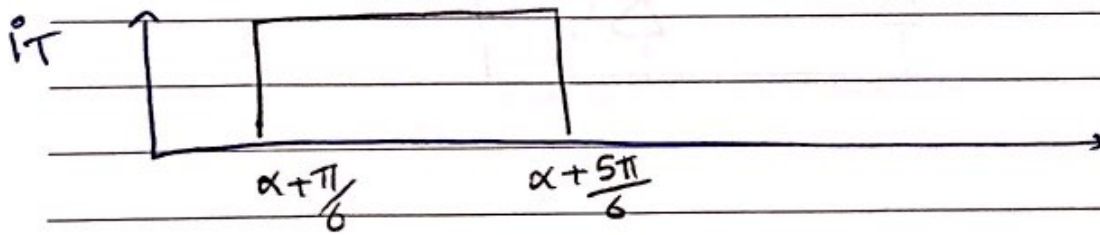
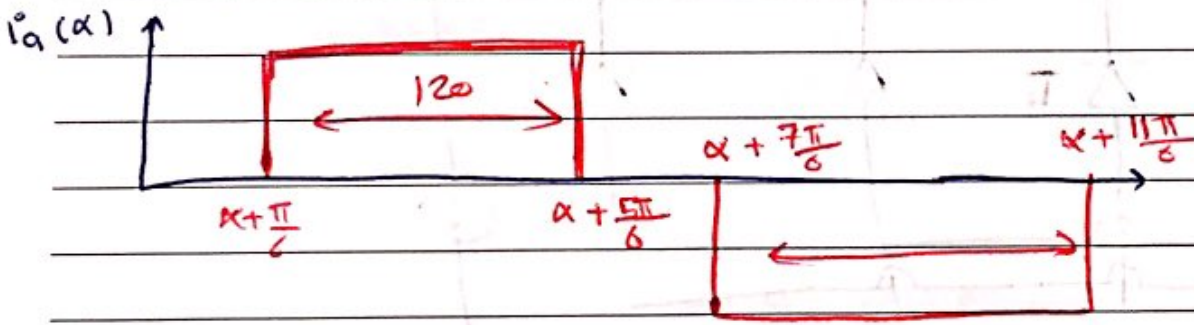
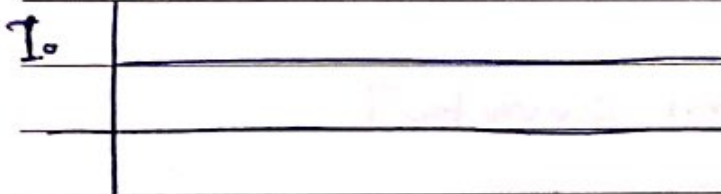
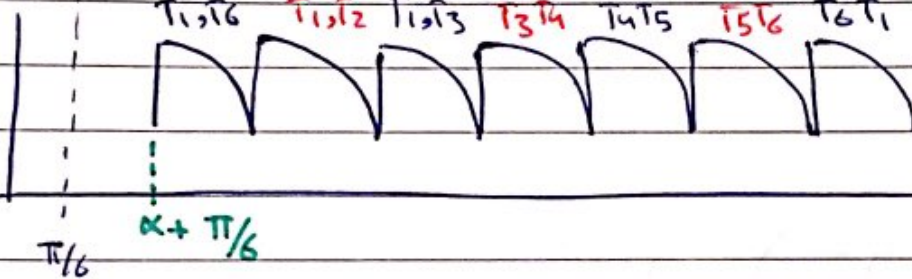


3 ϕ Controlled rectifier [semi converter]





V_{cb} V_{ab} V_{ac} V_{bc} V_{ba} V_{ca}
 $T_{1,2}$ $T_{1,2}$ $T_{1,2}$ $T_{3,4}$ $T_{4,5}$ $T_{5,6}$ $T_{6,1}$



$$\begin{aligned}
 V_{dc} = V_{o\text{avg}} &= \frac{3}{\pi} \int_{\alpha + \pi/6}^{\alpha + 5\pi/6} V_{ab} \, d\omega t \\
 &= \frac{3}{\pi} \int_{\alpha + \pi/6}^{\alpha + \pi/2} \sqrt{3} V_m \sin(\omega t + \pi/6) \, d\omega t
 \end{aligned}$$

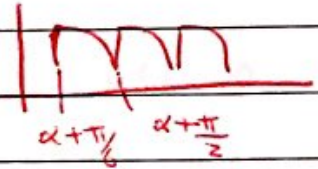
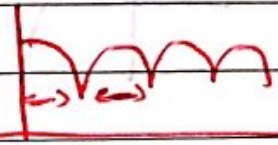


$$V_{dc} = \frac{\sqrt{3}}{\pi} 3 V_m \cos \alpha$$

$$V_{an} = V_m \sin \omega t$$

$$V_{ab} = \sqrt{3} V_m \sin(\omega t + 30)$$

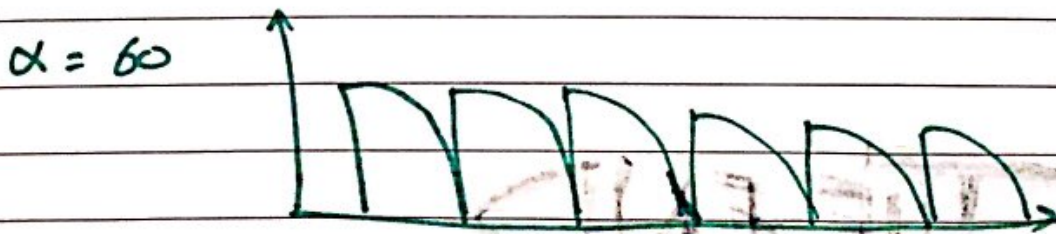
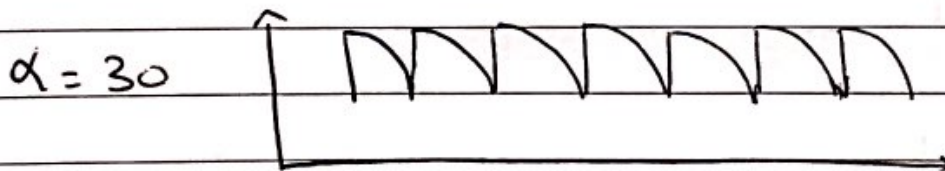
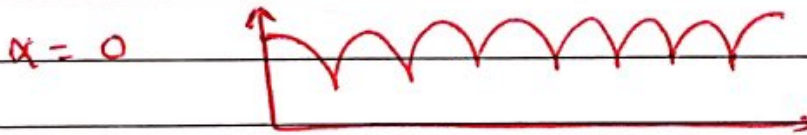
$$V_{cb} = \sqrt{3} V_m \cos(\omega t)$$

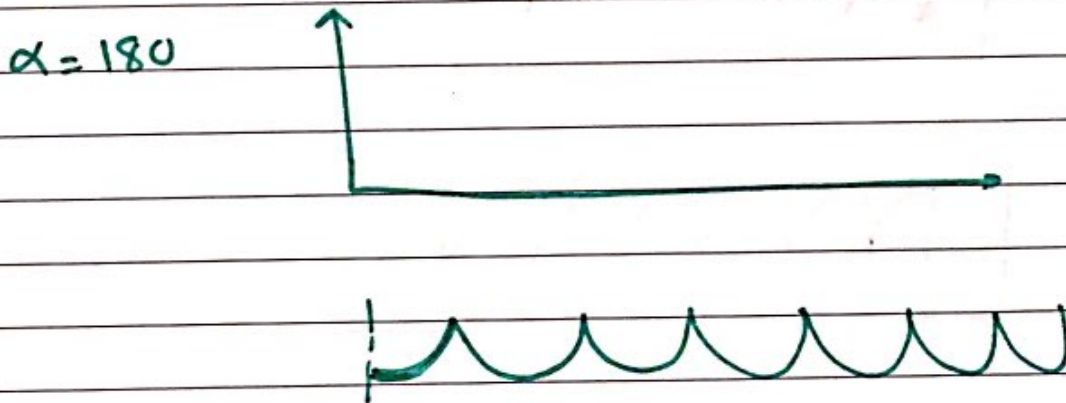
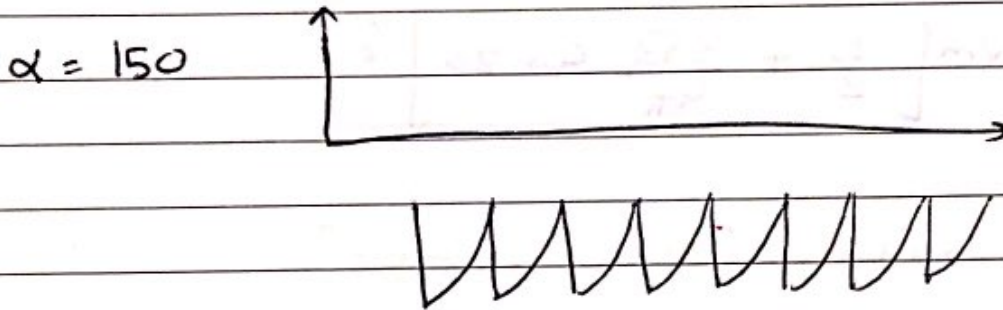
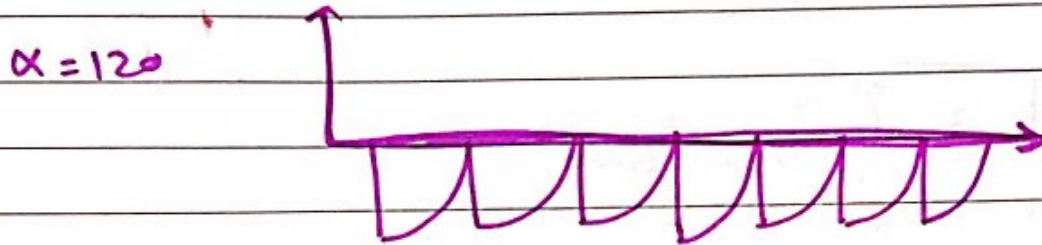


$$V_{rms} = \sqrt{\frac{3}{\pi} \int_{\alpha + \pi/6}^{\alpha + \pi/2} V_{ab}^2 d\omega t}$$

$$V_{rms} = \sqrt{3} V_m \left[\frac{1}{2} + \frac{3\sqrt{3}}{4\pi} \cos 2\alpha \right]^{1/2}$$

3 ϕ controlled rectifier [semi converter]:





THE END