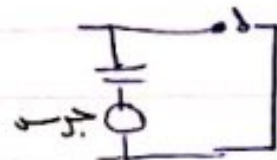


MDF: protection \rightarrow if the voltage rise \Rightarrow short ckt

E1 = 2Mbps \rightarrow 30 channel
 \rightarrow 2 control



- \rightarrow frequency reuse.
- \rightarrow Shared resources.

$$A = \frac{Q_a \lambda}{60} E_r$$

from label

active users \rightarrow no

N	1%	2%
10	4.08 122.4	4.54 136.2
20	10.97 329.1	11.77 353.1

* 30

traffic

$$A = \frac{Q_a \lambda}{60}$$

$$\lambda = 2 \text{ min}$$

$Q_a \equiv (a) \Rightarrow$ active.
 \rightarrow عدد النشيطين في الشبكة

$$A = \frac{Q_a \cdot 2}{60} = \frac{Q_a}{30}$$

$$Q_a = 30A$$

$$Q_a = \% Q \Rightarrow$$

$Q \equiv$ total users customer

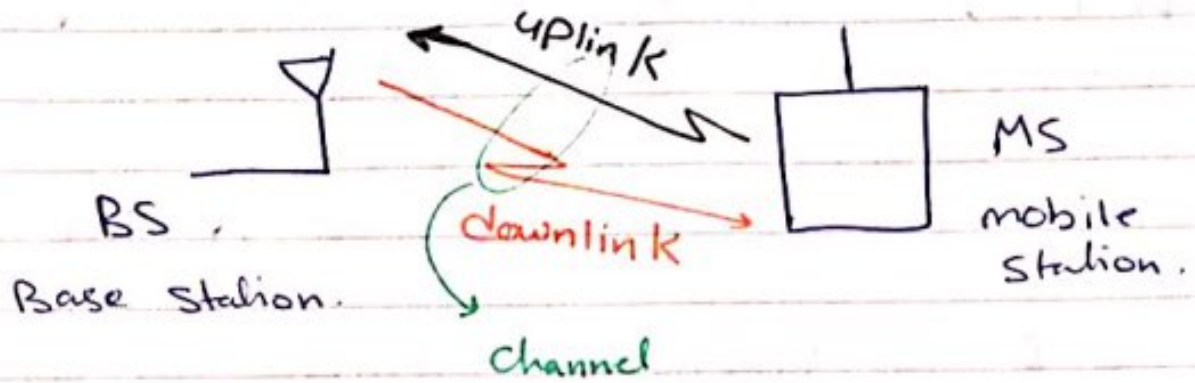
$$Q = \frac{30A}{\%}$$

- * \uparrow resources in the same place
- \uparrow channel \rightarrow \uparrow capacity

" capacity \equiv customer's no supported "

* Capacity \rightarrow economical performance system

* of channel the most critical number in cellular system.



data compression \rightarrow capacity \rightarrow ∞

ARPU: average return per user

ARPU \equiv \$

* of channel relation not linear with customer. \Rightarrow its exponential relation.

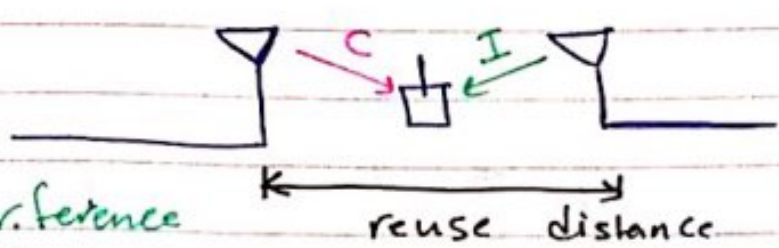
Q.O.S \equiv Quality of service.

┌ Blocking probability BP
├ BER C/I
└ Failurs

* Basic cellular design:-

frequency reuse
" in different area, 2 area independent " [3]

* بقرب كتي صير عندي (I)
 اكبر ص (I min)
 * زمان اول بخدم
 لا بد



* Same freq channel.
 * different area.

$I \equiv$ Interference
 $C \equiv$ carrier

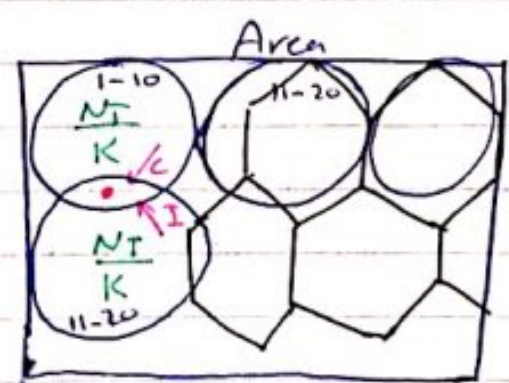
C/I

How to receive the signal

C/I → type of modulation
 → coding

↑ Interference → ↓ distance " صاف اقرب "

N_T ≡ Number of channel

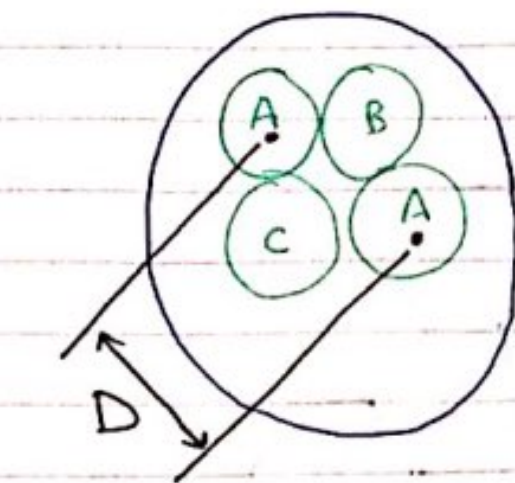


different channel → No interference.

* الـطلب اني اعني الـتلف الـجيد في الـتلف الـجيد
 like cells

$K \rightarrow$ reuse factor , $C/I > \min$
 → fill all the space with K different type
 such that $C/I > \min$ in the worst case.

$K \rightarrow \min$ to solve this problem
 لـحل الـمشكلة



N^2 means two dimension.

group of integer

K types...

reuse distance

$$\frac{N_T}{K} = N_{\text{cell}}$$

Same type \rightarrow Co. channel cell \Rightarrow
Co. channel interference.

$$i^2 + j^2 + ij = K$$

$i, j \equiv \text{integer}$

$i, j \in \mathbb{N}$

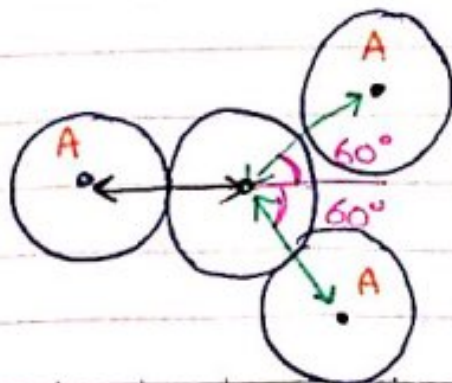
$$i=1, j=1 \rightarrow K=3$$

$$i=1, j=2 \rightarrow K=7$$

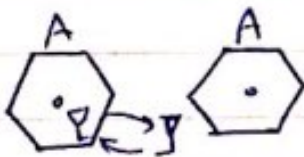
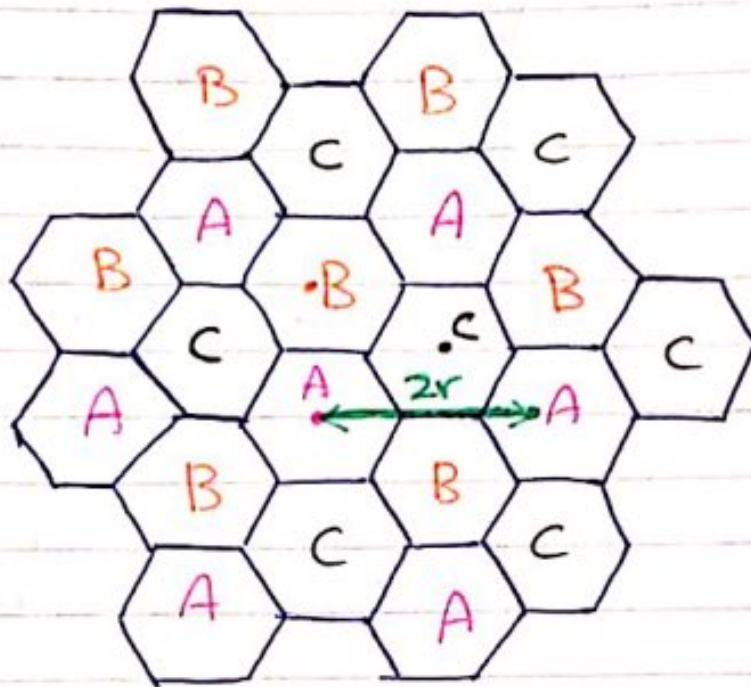
$$i=2, j=2 \rightarrow K=12$$

$$i=1, j=3 \rightarrow K=13$$

$K=4$ acceptable \Rightarrow not include the equation.



5



- Interference in base station (uplink)
- Interference down link ↓

$P_r \equiv$ power received

$$P_r = P_0 e^{-\gamma}$$

$$2 \leq \gamma \leq 4$$

$$\gamma = 3 \text{ (approx) } \rightarrow \text{best to 1st}$$

open area $\rightarrow \gamma \uparrow$

$$P_r = \underset{\substack{\uparrow \\ \text{Carrier}}}{C} + \sigma \underset{\substack{\rightarrow \\ \text{Interference}}}{I}$$

$$\frac{C}{I} \equiv CIR$$

6


smile

$$CIR = \frac{C}{\delta I} = \frac{1}{\delta} \frac{C}{I}$$

$$CIR = \frac{1}{\delta} \frac{P_o r_c^{-\delta}}{P_o r_i^{-\delta}} = \frac{1}{\delta} \left(\frac{r_c}{r_i} \right)^{-\delta}$$

$$= \frac{1}{\delta} \left(\frac{r_i}{r_c} \right)^{\delta}$$

$$\approx \frac{1}{\delta} \left(\frac{D}{R} \right)^{\delta}$$

R = cell radius 

$$\frac{D}{R} = q$$

$$q = \sqrt{3K}$$

$$CIR = \frac{1}{\delta} q^{\delta}$$

Ex

A total Area of 200 km^2 is to be covered by cellular comp system with min CIR = 4 dB if the available number of channel is 90 ?!

$$Q_a = 40 K, 1\% \text{ BP}, \Delta = 2 \text{ min}$$

$$\delta = 3$$

7

$$\text{Sol: CIR} = 4 \text{ dB} = 10^{0.4} = 2.5$$

$$\text{CIR} = \frac{1}{6} q^3$$

$$2.5 = \frac{1}{6} q^3 \Rightarrow \boxed{q = 2.5}$$

$$q = \sqrt{3K} \Rightarrow K = \frac{(q)^2}{3} = \frac{2.5^2}{3} = 2.1$$

$$\boxed{K = 3}$$

$$\text{actual CIR} = \frac{1}{6} (q)^3 = \frac{1}{6} (3)^3 = \frac{27}{6} = 4.5$$

$$\boxed{\text{CIR} = 6.5 \text{ dB}}$$

$$\text{dB} = 10 \log(4.5) = 6.53 \text{ dB}$$

$$\Rightarrow N_c = \frac{N_T}{K} = \frac{90}{3} = 30$$

$$\Rightarrow A_c = 18.59 \quad (\text{from table traffic per cell})$$

$$\Rightarrow A_T = \frac{Q \lambda}{60} = \frac{40K * 2}{60} = 1333.4$$

$$\frac{A_T}{A_c} = \text{Number of cell}$$

$$\frac{1333.4}{18.59} = 71.27 \Rightarrow \boxed{\# \text{ Cell} = 72}$$

* IF CIR = 7.5 dB \rightarrow K = 4

$$N_c = \frac{90}{4} = 22$$

$$A_c = 12.45$$

$$\begin{aligned} \text{Number of cell} &= 107.1 \\ &= 108 \end{aligned}$$

* IF $N_T = 120$

$$N_c = \frac{120}{3} = 40$$

$$A_c = 26.58$$

$$\text{Number of cell} = 51$$

Basic design :-

- ① flat earth
- ② uniform user distribution
- ③ Omni directional cells.

↳ antenna موجوده بالنسبه وبسبب هذا الاختلاف

$$(C/I)_{\min} = \frac{q^\delta}{\delta}$$

$$q = \sqrt[3]{3K} \quad K \in \{3, 4, 7, 12, 13, \dots\}$$

N_T (total)

$$N_{\text{cell}} = \frac{N_T}{K}$$

* K يعني K اجهزة في الخلية
← non linear traffic لان

Ex

$$\text{Area} = 300 \text{ km}^2$$

1 M customer → 15% active at busy hour

$$Q_a = 1M * 15\% = 150 \text{ k user (active)}$$

$$\lambda = 2 \text{ min}, \text{ BP} = 1\%, \text{ min } C/I = 8.5 \text{ dB}$$

$$N_T = 180, \delta = 3 \text{ ?!}$$

Sol:

$$q = \sqrt[3]{\delta * 10^{0.85}}$$

$$q = 3.48$$

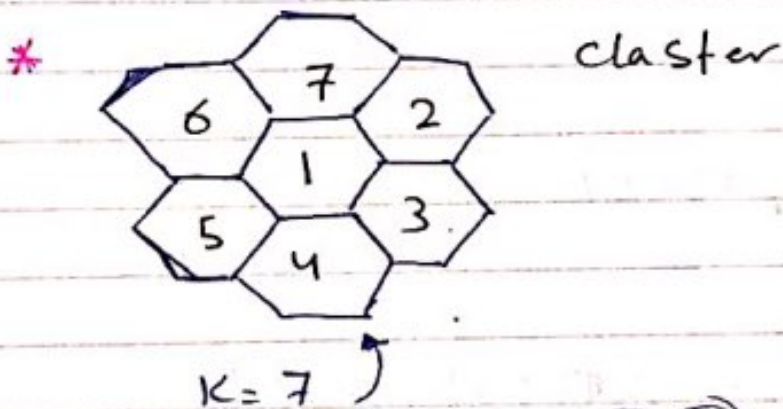
10

$$\Rightarrow K = \frac{q^2}{3} = 4.05$$

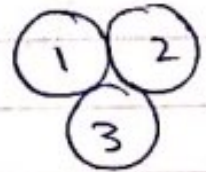
$$K = 7$$

$$q = \sqrt{3 \times 7} = 4.58$$

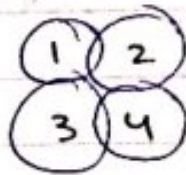
$$\Rightarrow \frac{C}{I} = \frac{(4.58)^2}{3} = 16.03 \Rightarrow 12 \text{ dB}$$



$$K = 3$$



$$K = 4 \Rightarrow$$



$$\Rightarrow N_c = \frac{180}{7} = 25.7$$

$$25 \times 7 = 175$$

7 cell system 175 cells (5 channel system)

$$\underline{2} \times 25 \text{ channel}$$

$$\underline{5} \times 26 \text{ channel}$$

} 7 cell



	cluster
25 ch \Rightarrow at 1% $\Rightarrow A_c = 14.72 E_r$	29.42
26 ch \Rightarrow at 1% $\rightarrow A_c = 15.49 E_r$	77.45
	106.87

$$29.42 \rightarrow 14.72 * 2$$

$$77.45 \rightarrow 15.49 * 5$$

$$\Rightarrow A_T = \frac{150 K * 2}{60} = 5 K E_r$$

$$\bar{A}_c = \frac{106.87}{7} = 15.27$$

$$\# \text{ of cell} = \frac{5K}{15.27} = 327.5$$

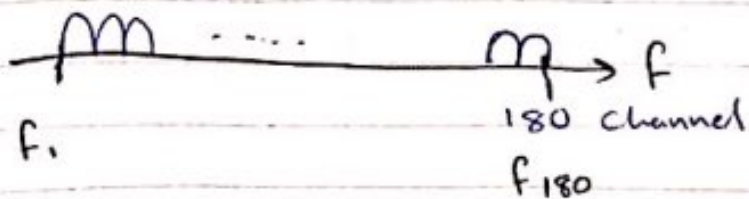
$$\text{cell} = 328$$

* if $K = 3$

$$N_c = 60$$

$$A_c = 43.2$$

$$\text{cell} = \frac{5K}{43.2} = 116 \text{ cell}$$



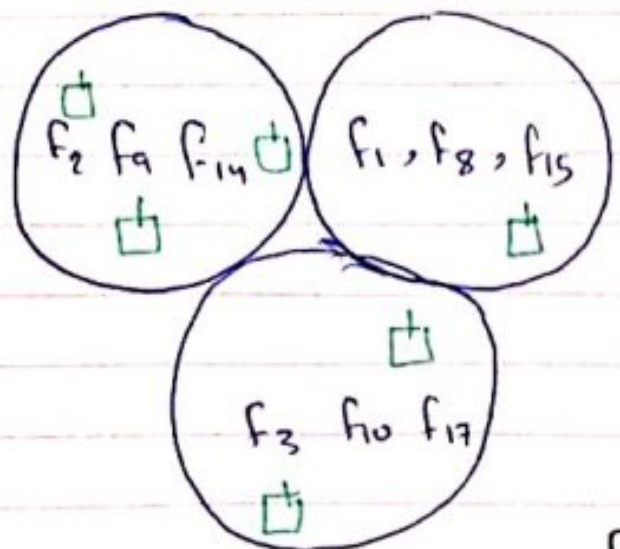
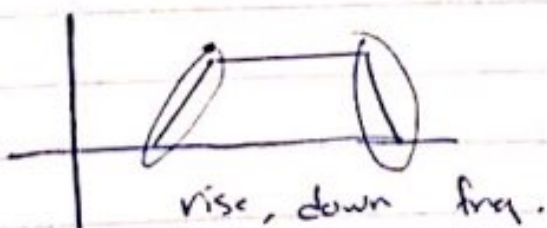
* Noises:-

$f_1 \rightarrow f_{25}$

- 1- Co. channel interference.
- 2- whit Noise
- 3- Adjacent channel interference.
 ↳ بين الـ chan و الـ جيرانها
- 4- Man made noise.

* Frequency Plan:-

1	2	3	4	...	K
f_1	f_2	f_3	f_4		f_K
f_{K+1}	f_{K+2}	...			
					f_{K+180}



frequency plan average the adjacent freq inter. and reduce its effect

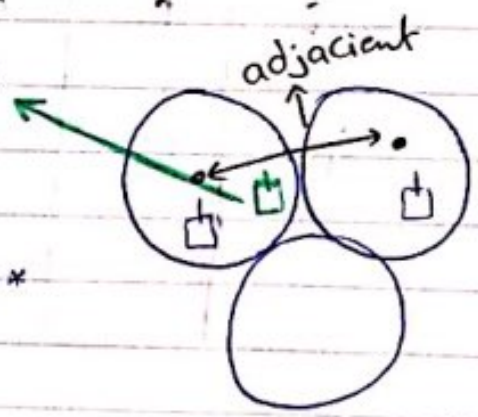
لأنه ما يرفع الخلفه الشائيه بين واقف

$$\frac{C}{\sum I} = \frac{C}{\sum I_{co} + \sum I_{adj} + \sigma n^2}$$

* اذا كانت اعطاني قيسه C/I ← اعطاني ص CD ← ازا اح به زله كبير
 وقته ~~C/I~~ C/I ≠ ∞

Near end far end → worst case.

- station ← far end
- station ← near end



Inter ↓ ← power ← BS (base station)

RSSI = received signal strength indicator

CDR complete data record
 XDR

$$\frac{C}{I} = \frac{C}{\sum I's}$$

6 co-channel. level

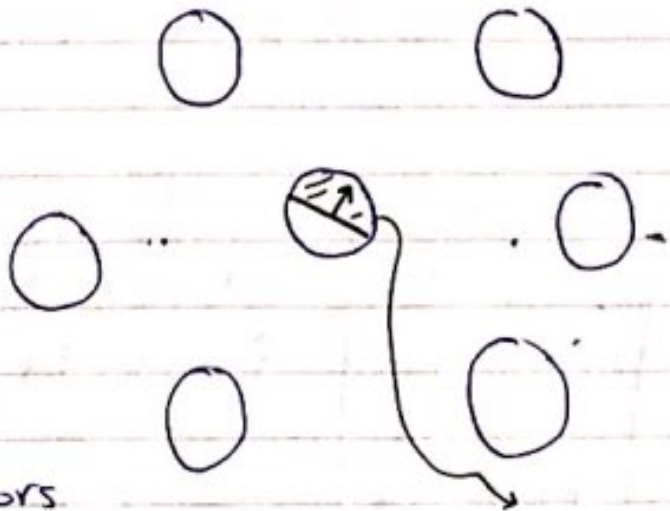
~~Study~~

* Sectionization :-

$$\frac{C}{I} = \frac{C}{\frac{6}{n} I} = \frac{q^{\delta} \cdot n}{6}$$

n = number of sectors

$$6 \geq n \geq 1$$



هذا النوع يكون 3 I's

Ex

for n=2 for same example.

$$\text{sol} \Rightarrow = 10^{0.85} = (\sqrt{3K})^3 * \frac{2}{6} = 9.5 \text{ dB}$$

$$K = 2.25 \rightarrow \boxed{K=3}$$

$$N_c = \frac{180}{3} = 60 \begin{cases} \rightarrow 30/\text{sector} \\ \rightarrow 30 \end{cases}$$

$$30 \text{ ch at } 1\% \rightarrow A_{\text{sect}} = 18.59$$

$$A_{\text{cell}} = 37.18 \text{ Er}$$

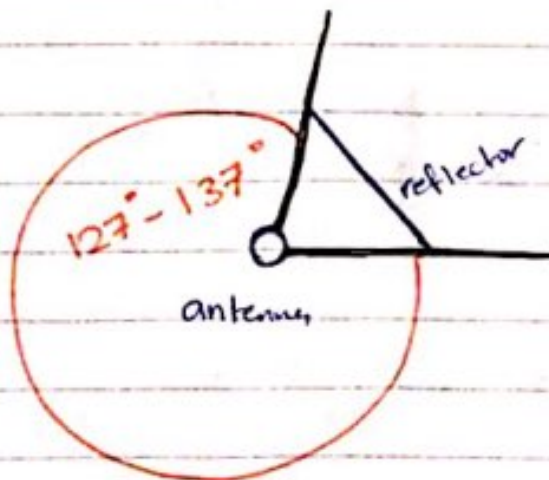
$$\text{Total no of cells} = \frac{5K}{37.18} = 134.48$$

cell = 135 cell

K →	A		B		C	
	1	2	1	2	1	2
	f ₁	f ₂	f ₃	f ₄	f ₅	f ₆
	f ₇	f ₈	..			

* sec I can control

and keep seq from about any freq.



$$n=3 \Rightarrow N_c = \frac{180}{3} = 60 \begin{cases} \rightarrow 20 \text{ /sector} \\ \rightarrow 20 \\ \rightarrow 20 \end{cases}$$

$$\frac{C}{I} = 11.3 \text{ dB} \left[(\sqrt{3K})^3 + \frac{3}{6} \right]$$

$$A_{\text{cell}} = 32.91 \text{ Er}$$

$$20 \text{ ch at } 17. \text{ BP} \rightarrow A_{\text{sect}} = 10.97$$

$$\text{total no of cell} = \frac{5K}{32.91} = 151.9$$

$$\# \text{ of cell} = 152 \text{ cell}$$

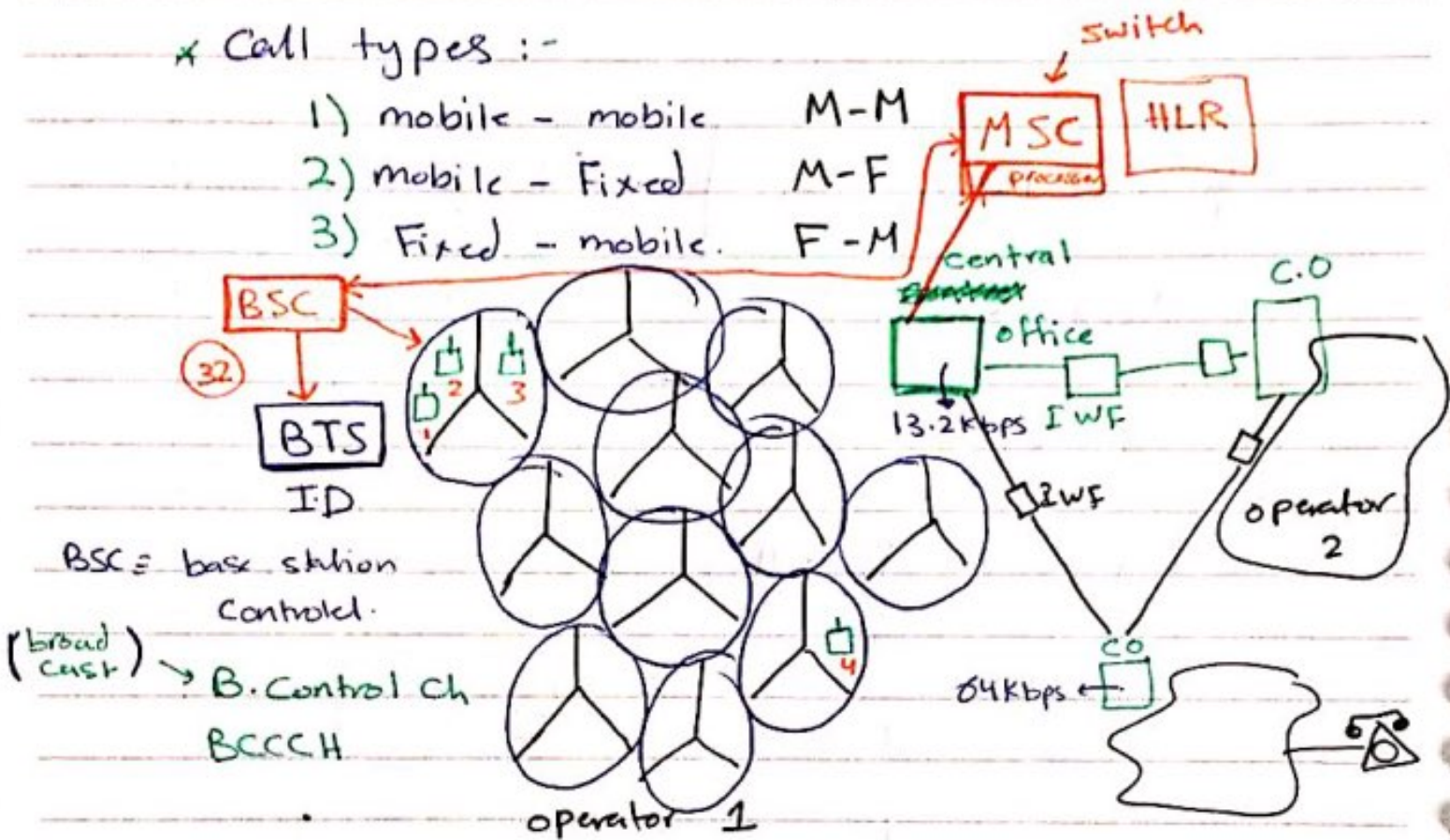
K →	A			B			C		
	1	2	3	1	2	3	1	2	3
	f_1	f_2	f_3	f_4	f_5	f_6	f_7	f_8	f_9
	f_{10}	f_{11}					

Cell configuration $K \times n$ $(3 \times 3) \Rightarrow$
best solution for any cellular sys.

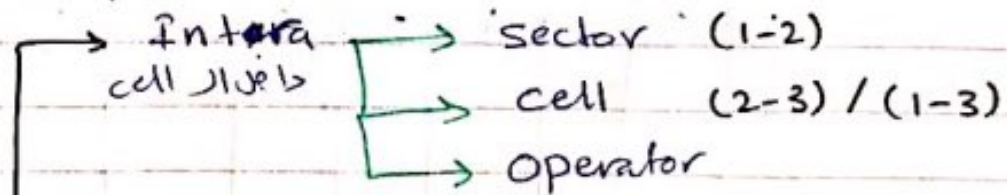
* Call setup 84

* Call types :-

- 1) mobile - mobile M-M
- 2) mobile - Fixed M-F
- 3) Fixed - mobile F-M



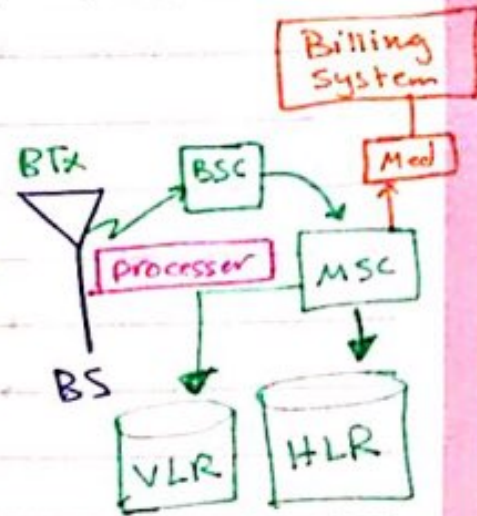
M-M



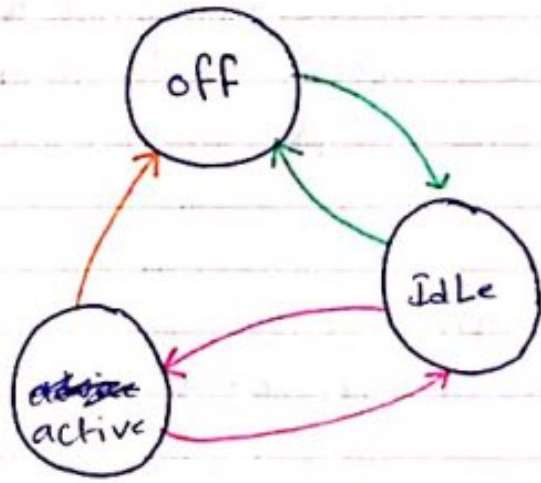
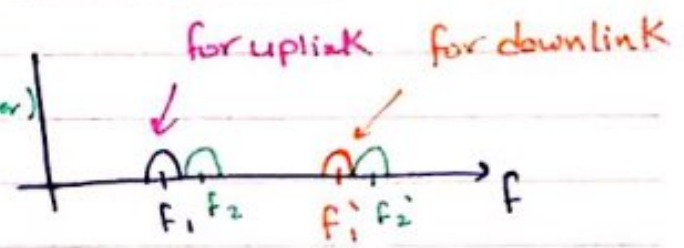
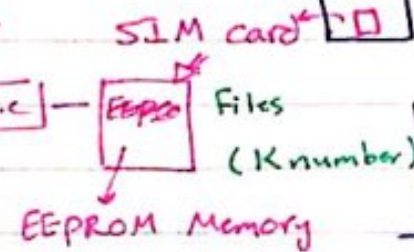
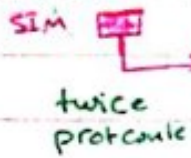
IWF : ~~Inter~~ working frame.
Inter

* Call setup 84

~~XXXXXXXXXXXX~~
FDD and TDD



M.C ≡ Micro Controller



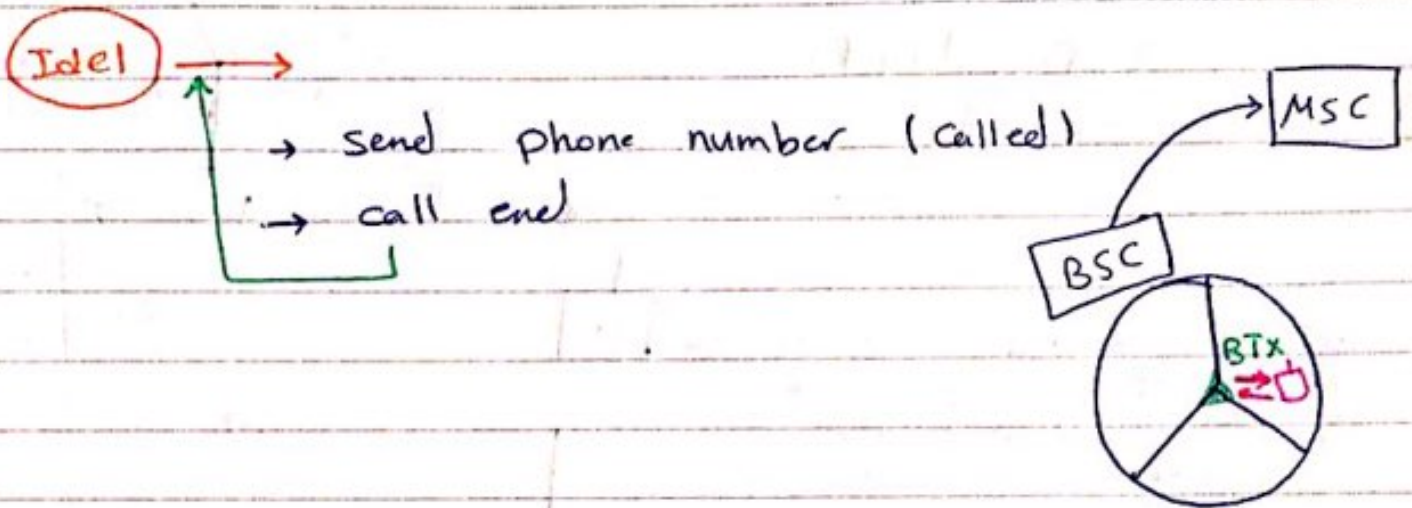
M.S State

- power ON
- Network search (Random access)
- Authentication

~~XXXXXXXXXXXX~~ "Noise → best password."
M-Seq

19

use gold code to create a password.
 ↳ 2 m-sec.



* Control data are transmitted through voice channel when active mode. ((on call))

Control channel (كناية) Voice channel (كناية صوتية) *
 channel (قناة) channel (قناة)

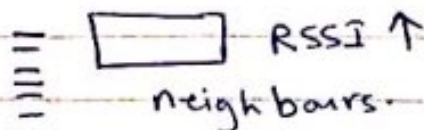
* Idle =>

location update.

measurement report ✓

→ RSSI

for 7 nearest BTS then order them



→ (H.O request) " X ... " *
 H.O = Hand over

RSS \equiv Recive signal strangth.

min power recived ≥ -110 dBm

min P_r (GSM) ≥ -100 dBm

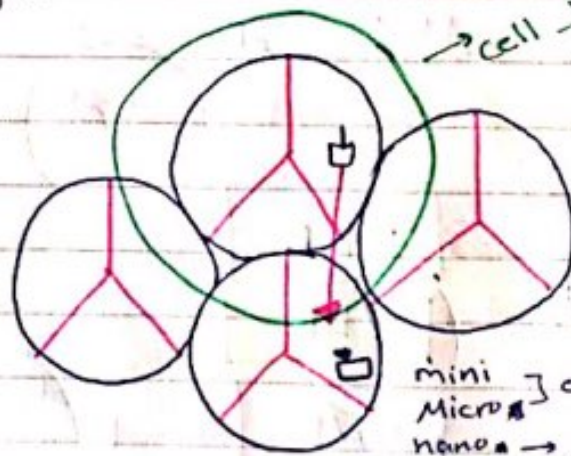
* -83 dBm = $10^{-8.3}$ mw = 5pw

H.C "Home? cell"

$N_1 \rightarrow$ Neighbor.

N_2

N_6



كبر ال cell \rightarrow

(delayed) H.O
cell breathing

mini } out doors
Micro }

nano \rightarrow flat (طاقه)
pico (طاقه)

"H.O" Hand over Failiur 8

- NO Idte channel in next cell (congestion)

\rightarrow delayed H.O

"كالتنقل، ما تلاقى ch فاقية"

- stability of H.W "Hard wave"

\rightarrow design

\rightarrow base station

- c/I or P_r levels

→ ~~#~~ Hard H.O \equiv hard hand over

"لا تغير الـ frequency"

↳ $(f_1 \rightarrow f_2)$

→ Soft H.O "التبديل"

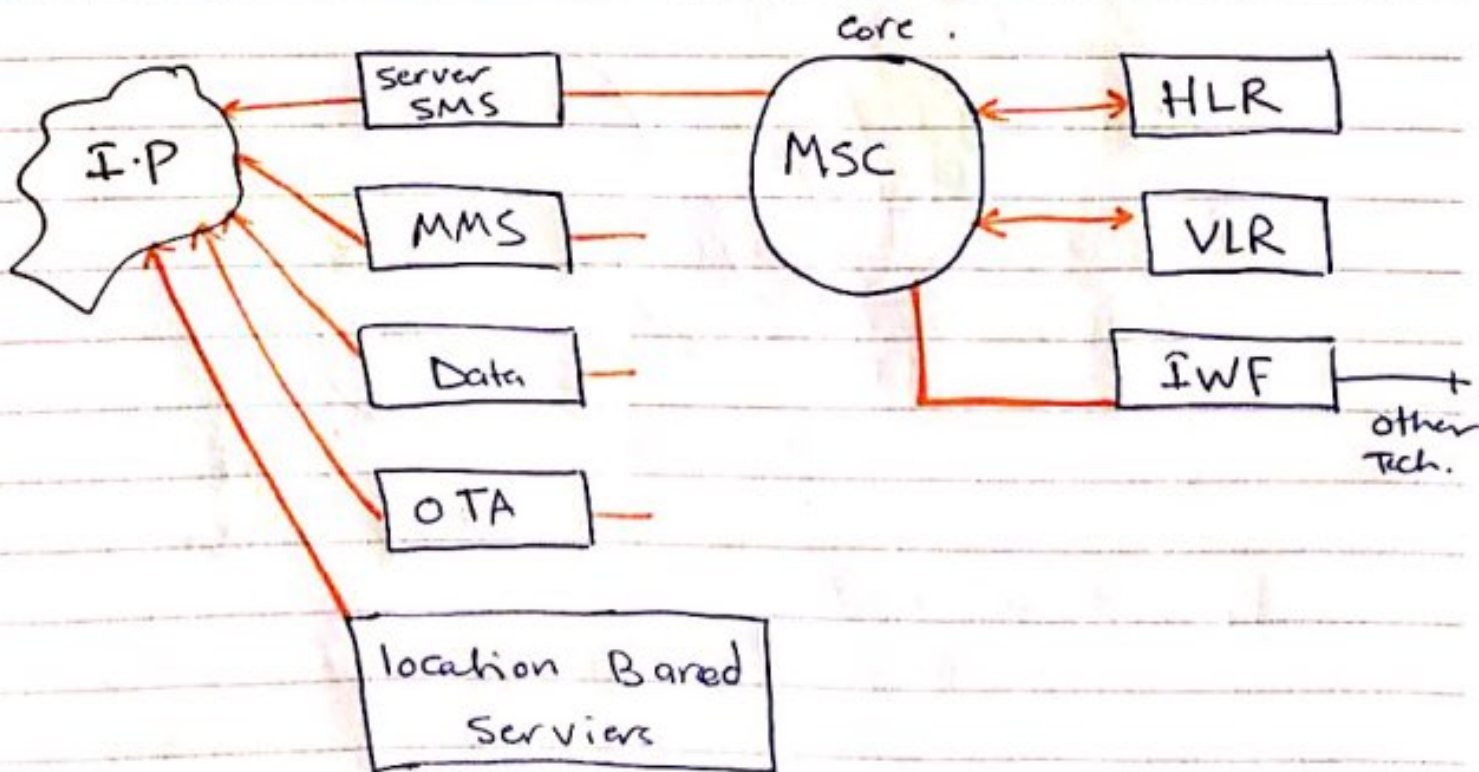
* Channel Assignment:

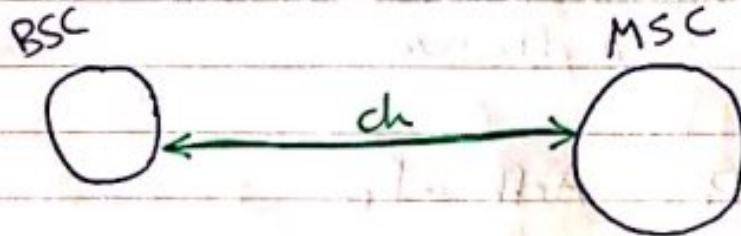
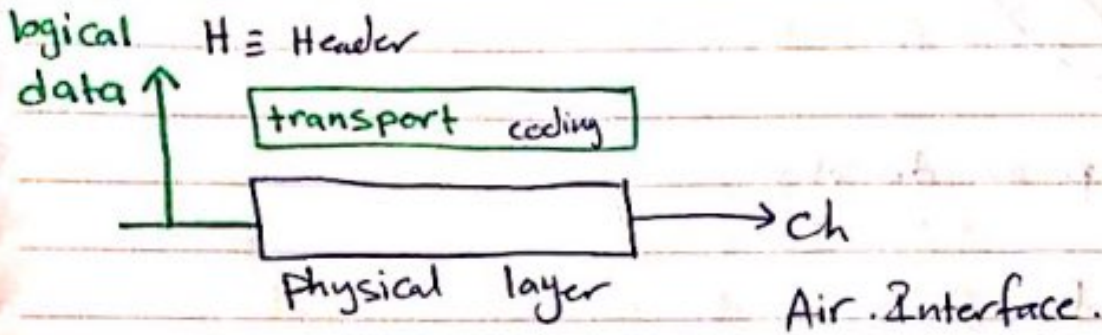
- Fixed
- Dynamic

"cluster: different type of cell"

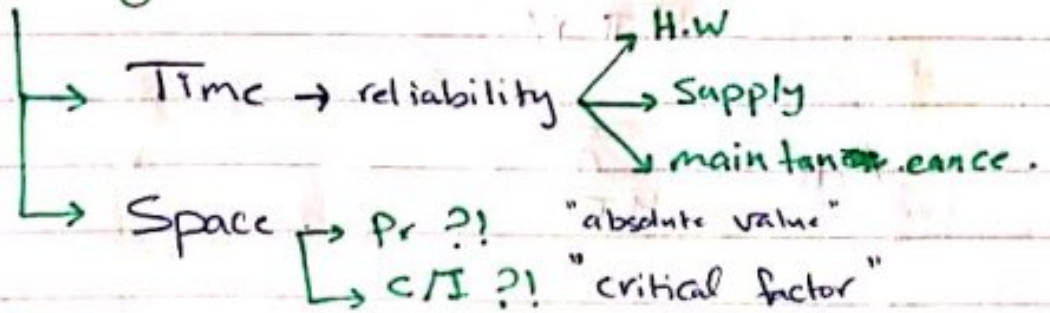
- Hybrid $\left\{ \begin{array}{l} \rightarrow \text{Fixed } \checkmark \text{ group} \\ \rightarrow \text{Dynamic } \textcircled{?} \end{array} \right.$

VAS \equiv value added cells.



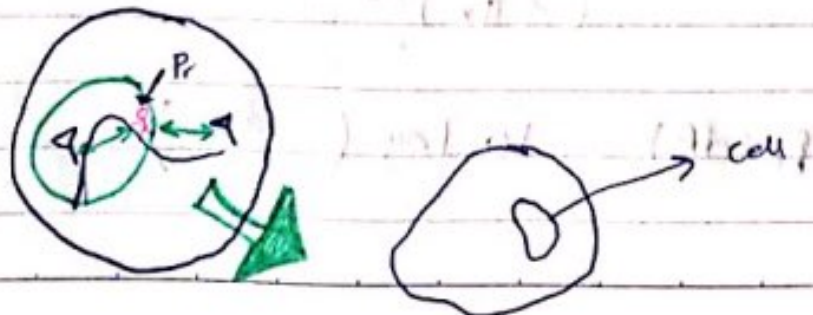


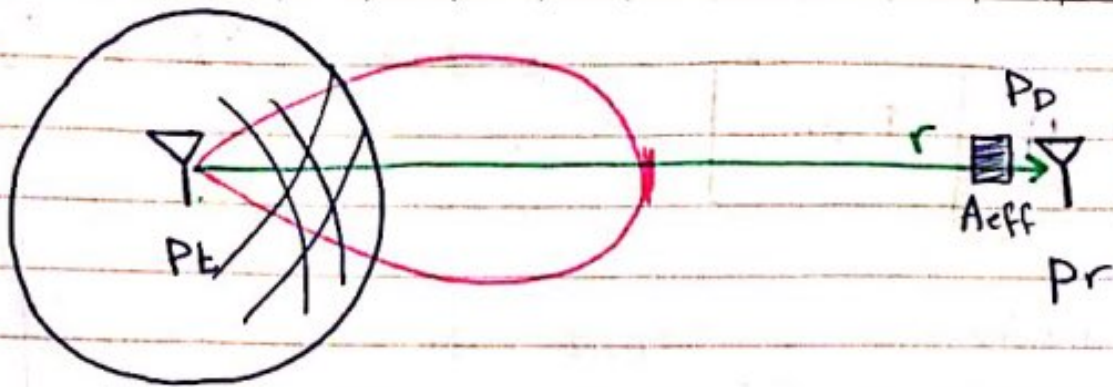
* Coverage



percentage of time you make a successful call in any location in the network.

ATOLL





$P_D \equiv$ power density

$$P_D = \frac{P_t}{4\pi r^2}$$

$A_{eff} \equiv$ A effective

$$P_r = A_{eff} \cdot P_D$$

$$P_r = \frac{P_t A_{eff}}{4\pi r^2}$$

$$A_{eff} = \frac{G_r \lambda^2}{4\pi}$$

① free space model :-

$$P_r = \frac{P_t \cdot G_r \lambda^2 \cdot G_t}{(4\pi r)^2}$$

$$P_r(\text{dB}) = 10 \log (\quad)$$

$$P_r(\text{dB}) = \underbrace{P_t + G_t + G_r}_{\text{EIRP}} - 20 \log \left(\frac{4\pi r}{\lambda} \right)$$

$$* \lambda = \frac{c}{f}$$

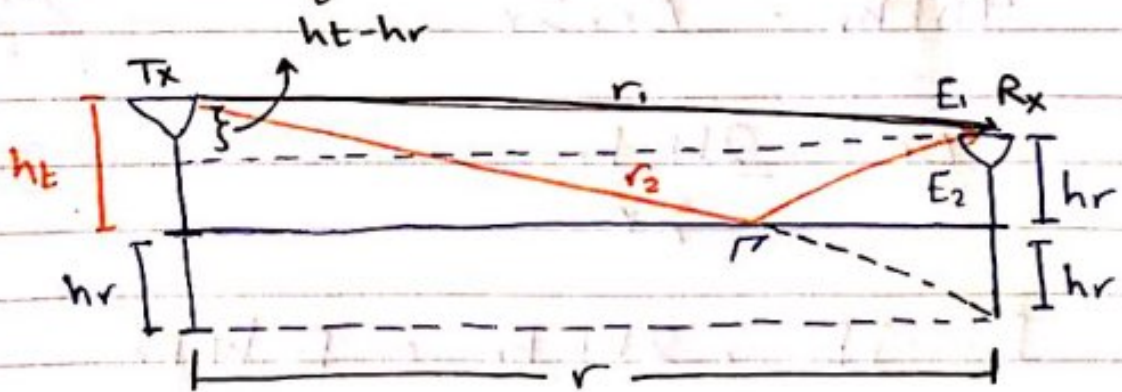
$$P_r(\text{dB}) = P_t + G_t + G_r - \underbrace{20 \log \left(\frac{4\pi fr}{c} \right)}_{\text{free space loss}}$$

free space loss.

EIRP \equiv effective isotropic received power.

$$P_r = P_t + G_t + G_r - \text{loss}$$

[2] two ray model :-



* دو صحت ال signal بقا موشن *

$$\vec{E} = \vec{E}_1 + \vec{E}_2$$

$$\Delta\theta = \frac{\Delta r}{\lambda} \cdot 2\pi$$

$$E_1 = E_0 \angle \theta$$

$$E_2 = \Gamma E_0 \angle \Delta\theta$$

$$\boxed{\Gamma = -1}$$

$$E = E_1 + E_2 = E_0 (1 - e^{j\Delta\theta})$$

$\rightarrow \cos \Delta\theta + j \sin \Delta\theta$

$$\therefore = E_0 - j E_0 \Delta\theta = -j E_0 \Delta\theta$$

$$r_2^2 = r^2 + (ht + hr)^2$$

$$r_1^2 = r^2 + (ht - hr)^2$$

$$(r_2^2 - r_1^2) = (r_2 - r_1)(r_2 + r_1)$$

$$4ht hr = \Delta r \cdot 2r$$

$$\therefore \Delta r = \frac{2ht hr}{\lambda r}$$

$$E = -j E_0 \cdot \frac{2ht hr}{r} = \frac{E_0 ht hr}{r^2}$$

$$E_0 = \frac{E_t}{r}$$

$$\boxed{P_r = \frac{P_0 ht^2 hr^2}{\lambda^2 r^4} \rightarrow \delta}$$

* free space :-

$$P_r = \underbrace{P_t + G_t + G_r}_{\text{EIRP}} - \text{loss}$$

$$\rightarrow \left(20 \log \left(\frac{4\pi r}{\lambda} \right) \right)$$

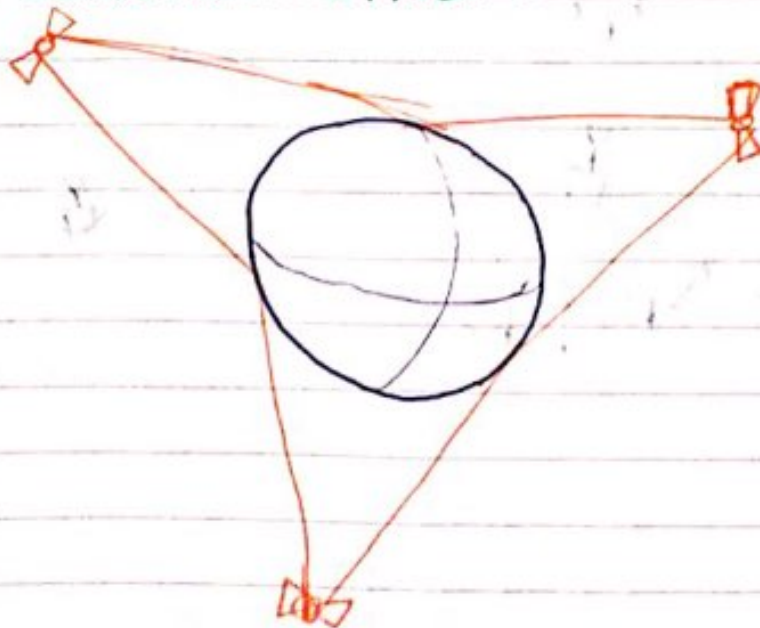
free space loss

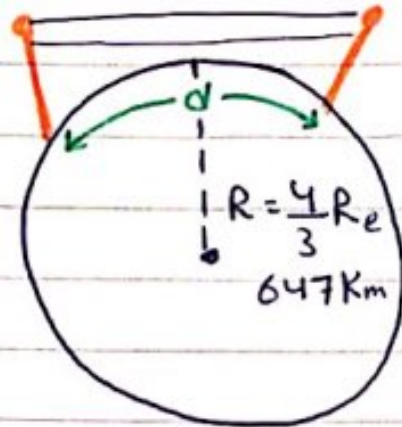
* two ray Model :-

$$P_r = P_o \frac{h_t^2 h_r^2}{\lambda^2 r^4}$$

$$P_r = P_o + 20 \log(h_t) + 20 \log(h_r) + 20 \log(f) - 20 \log(c) - 40 \log(r)$$

* Earth curvature effect :-

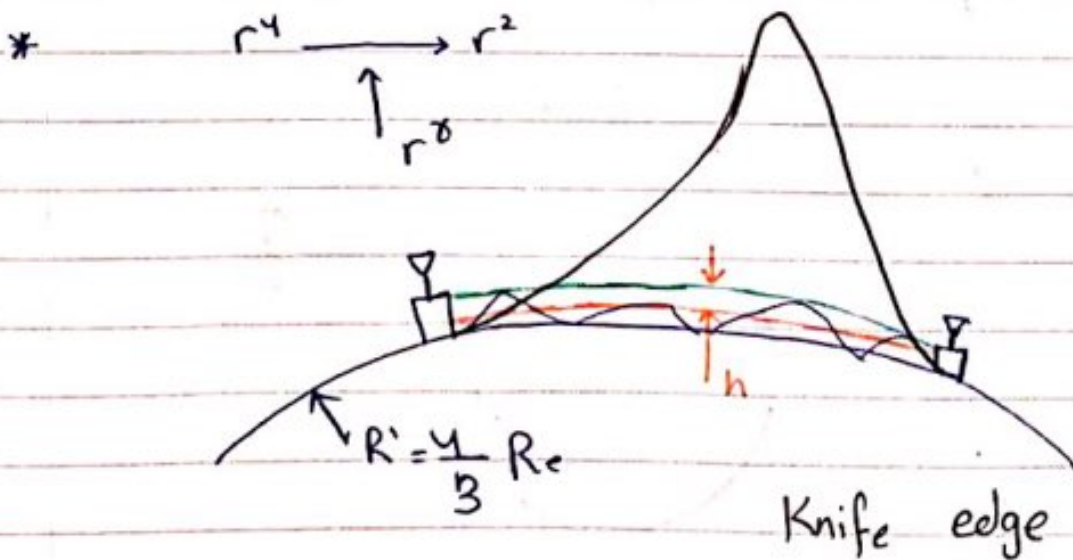


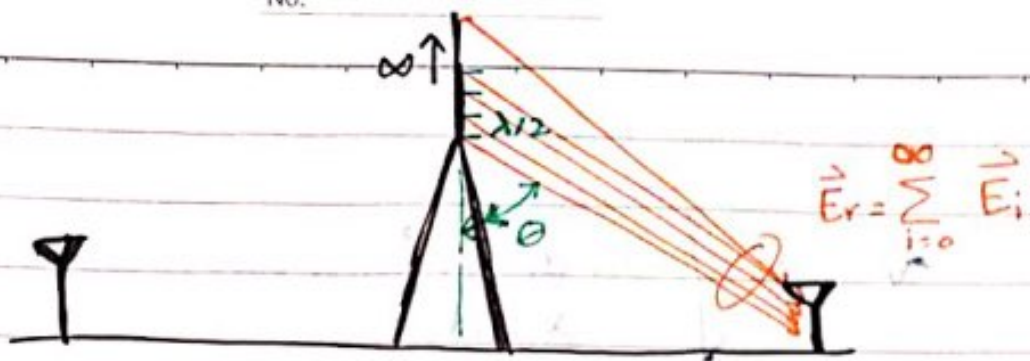


$$d_{\max} = \sqrt{17 h_r} + \sqrt{17 h_t} \quad \text{Km}$$

h_t, h_r in m.

$R_e \equiv$ radius earth.





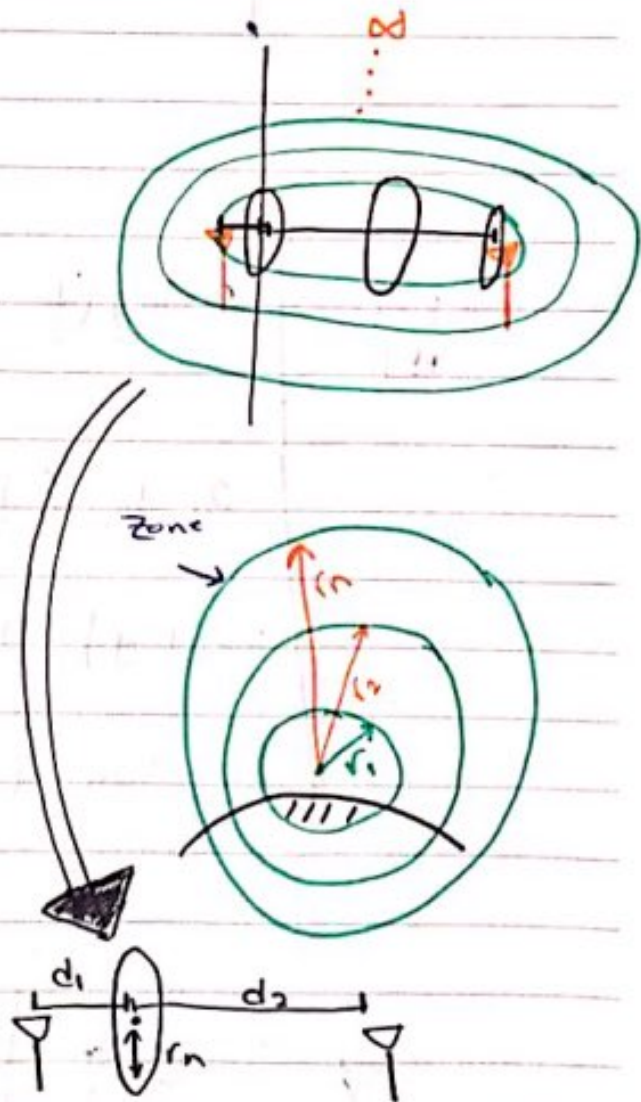
$$\Delta d = \frac{\lambda}{2} \cos \theta$$

$$\Delta \phi = \Delta d \frac{2\pi}{\lambda}$$

$$\Delta \phi = \frac{\pi \lambda \cos \theta}{\lambda}$$

$$r_n = \sqrt{\frac{n \lambda d_1 d_2}{d_1 + d_2}}$$

$n \equiv$ number of fringed zone.

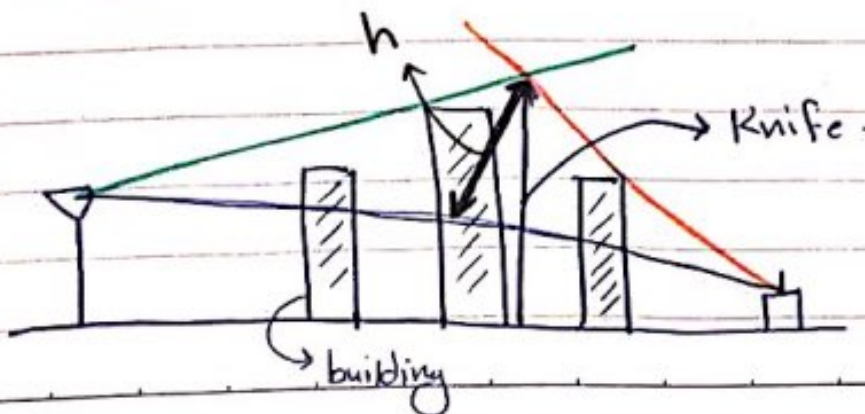


Knife edge loss:-

$$v = h \sqrt{\frac{2(d_1 + d_2)^2}{\lambda d_1 d_2}}$$

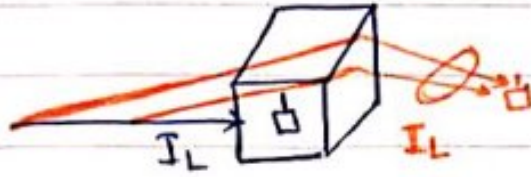


$$\text{loss} = L_{\text{knife}} = \begin{cases} 20 \log \left(\frac{1}{2} - 0.62v \right) & -1 \leq v < 0 \\ 20 \log \left(\frac{1}{2} e^{-0.95v} \right) & 0 \leq v < 1 \\ 20 \log \left[0.4 - \sqrt{0.1184 - (0.38 - 0.10)^2} \right] & 1 \leq v < 2.4 \\ 20 \log \left(\frac{0.225}{v} \right) & v \geq 2.4 \end{cases}$$



30

cm:le

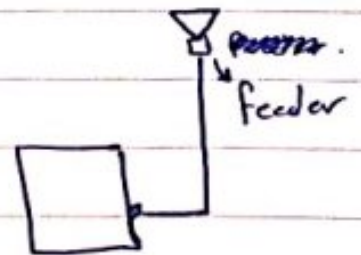


$f_L =$ ~~insertion~~ loss
Insertion

* General ~~model~~ path loss Model :-

$$P_r = P_t + G_t + G_r - \text{LOSS}$$

$$\text{LOSS} = \text{Loss}_{\text{free space}} + 10 \log(r) + L_{\text{knife if exist}} + L_{\text{feeder}} + L_{\text{weather}} + L_{\text{others}}$$



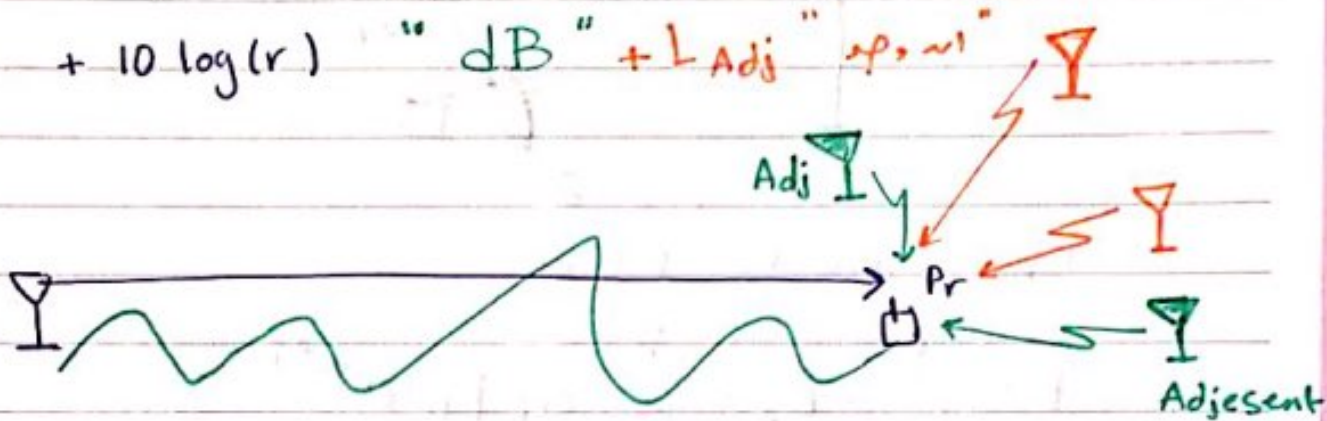
$$P_r = P_t + G_t + G_r - \text{loss}$$

path losses:-

dBW
dBm

$$\text{Loss} = L_{\text{free}} + L_{\text{knife}} + L_{\text{feeder}} + L_{\text{weather}} + L_{\text{others}}$$

$$+ 10 \log(r) \quad \text{" dB " } + L_{\text{Adj}} \text{ "sp. int"}$$



$$P_r = C \quad \text{from Home}$$

$$P_r = \bar{I} \text{ co.ch} \quad \text{from Co. channel interference calls}$$

$$P_r = \bar{I} \text{ Adj}$$

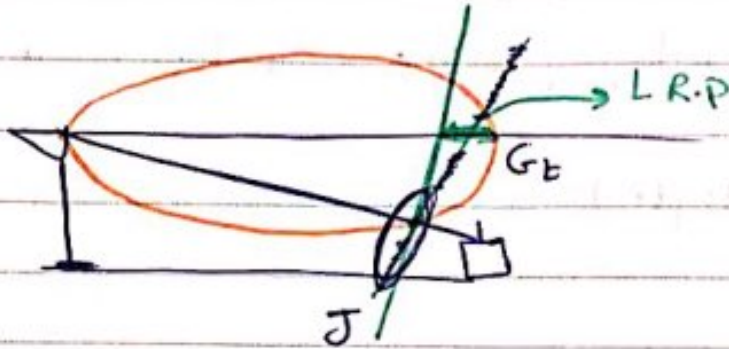
$$\text{Loss adj} = 40 \text{ dB}$$

~~Actual CI~~

$$\text{Actual CI} \bar{I} = \frac{C}{\sum I_s + \sigma_n^2}$$

adj ch. → co.ch → adj ch. → co.ch → adj ch. → co.ch → adj ch. → co.ch → adj ch.

$$\text{Loss} = L_{\text{free}} + L_{\text{knife}} + L_{\text{feeder}} + L_{\text{weather}} + L_{\text{other}} + L_{\text{adj}} + 10 \gamma \log(r) - a(ht) - b(hr) + L_{\text{R.P}}$$



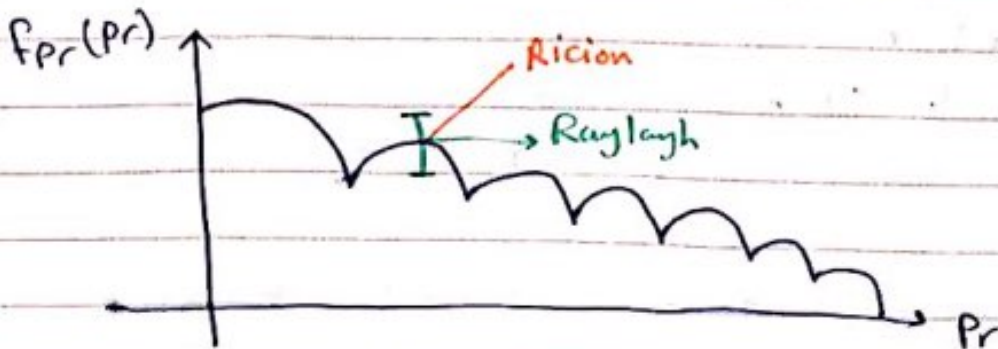
L.R.P = Radiation Pattern

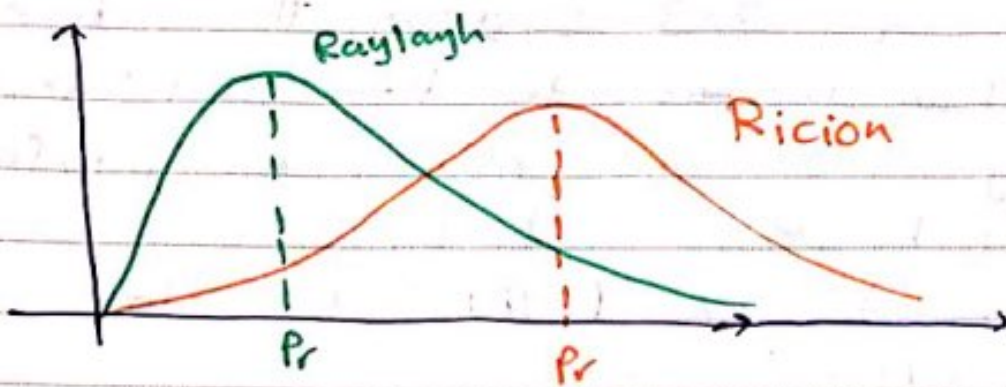
$$\vec{E} = \sum_{j=1}^J E_j = \sum_{i=1}^J \alpha_i E_t e^{j\delta_i}$$

$$P_r = \frac{|E|^2}{\eta_0} \begin{matrix} \rightarrow \text{Rician LOS} \\ \rightarrow \text{Rayleigh LOS} \end{matrix}$$

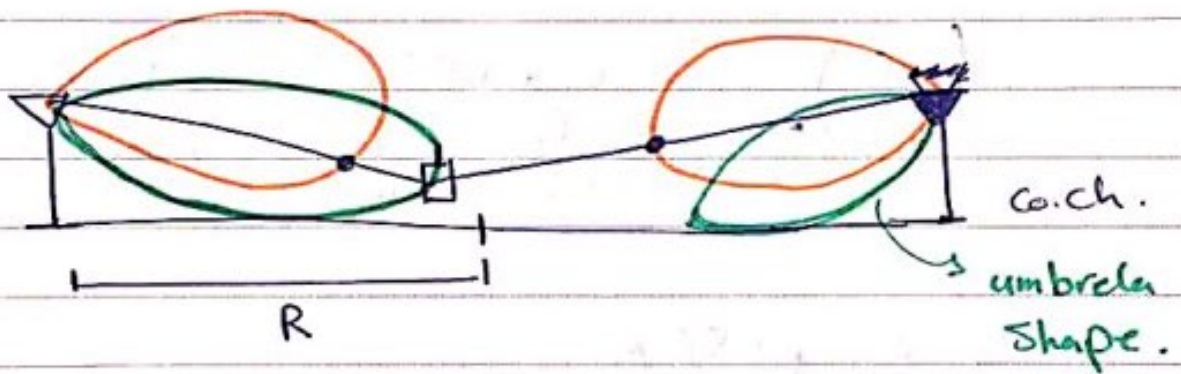
Long ~~term~~ term is log normal R.V

Line of sight (dominant component)





$$P_r > P_r$$



Down teltting :-

$$\frac{C \uparrow}{I \downarrow}_{new} = \left(\frac{C}{I} \right)_{old} + \uparrow C + \downarrow I$$

"Hata's Model"

$$P_r = P_x - 10\gamma \log(r)$$

$$P_r = P_0 / r^\gamma$$

at certain constant.

Ex

For a 3x3 system the down
telling increase the Home cell signal
by 2 dB and reduces the interference
 I_1 by 1 dB I_2 by 2.5 dB
Find the new (C/I) if the old
 $C/I = 7 \text{ dB} ?!$

$$\text{sol:- } \left(\frac{C}{I}\right) = \frac{C}{I_1 + I_2} = \frac{C}{2I} \quad "I_1 = I_2"$$

$$\left(\frac{C}{I}\right)_{\text{new}} = \frac{C * 1.58}{\frac{I_1}{1.25} + \frac{I_2}{1.77}}$$

$$\begin{aligned} &"C \text{ increase } (*) 10^{0.2} \\ &I \text{ decrease } \left(\frac{\circ}{\circ}\right) \frac{I_1}{10^{0.1}} + \frac{I_2}{10^{0.25}} \end{aligned}$$

$$= \frac{C * 1.58 * 2}{2I \left(\frac{1}{1.25} + \frac{1}{1.77}\right)}$$

$$= \left(\frac{C}{I}\right)_{\text{old}} * 2.31$$

$$\Delta(C/I) = 3.6 \text{ dB} \quad "10 \log(2.31)"$$

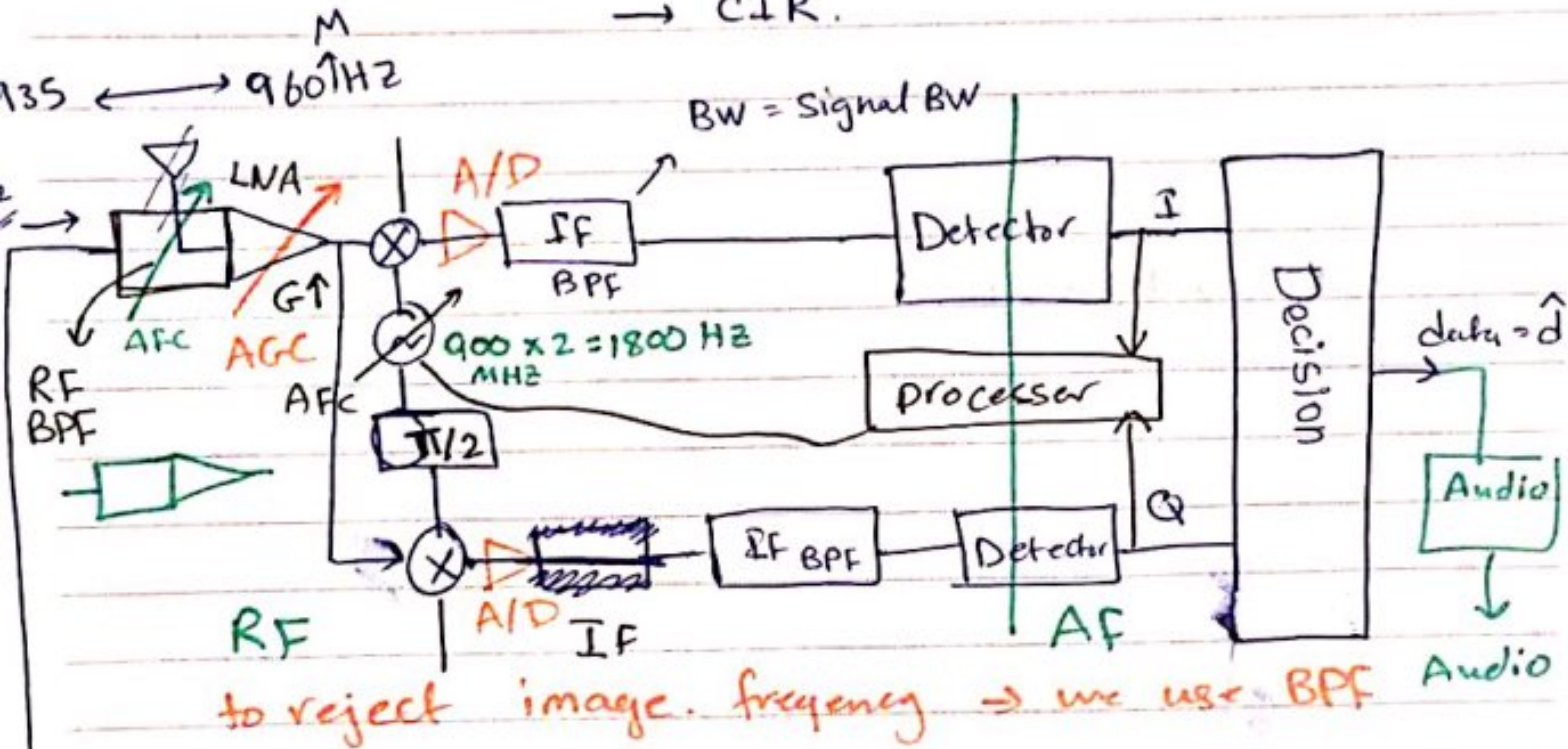
$$(C/I)_{\text{new}} = 10.6 \text{ dB} \quad "3.6 + 7 = 10.6 \text{ dB}"$$

* Coverage :-

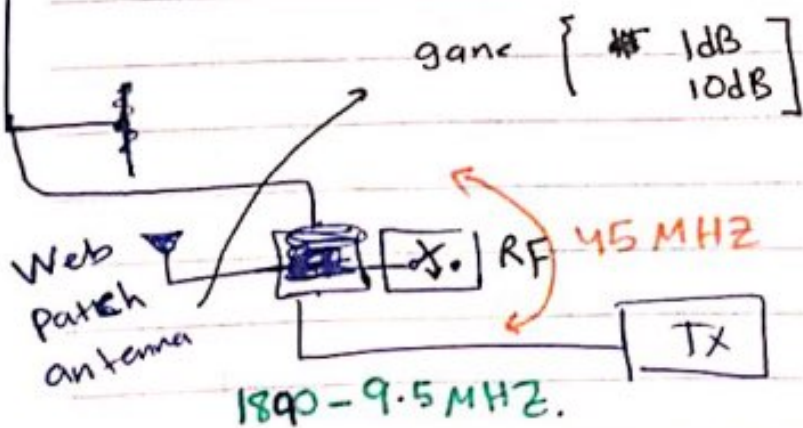
time → ~~reliability~~ reliability of equipment.

Space → propagation loss

- Pr
- CIR.



to reject image frequency → we use BPF



120 = (20dBm) ← (80-120)mw level
 100 pw. jā → PR
 (-70dBm)

Rx Sensitivity (P_r) = min P_r .

$P_r \rightarrow$ antane. λ ω

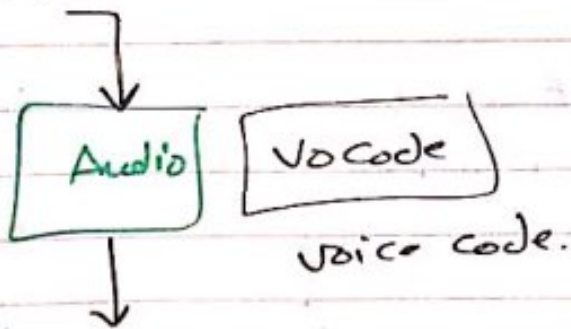
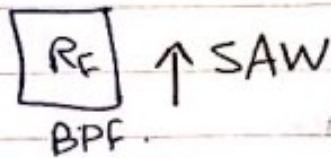
$P_D \rightarrow$ ant \leftarrow ω

$$G = \frac{A_{eff} \times \lambda^2}{4\pi r^2}$$

$P_D =$ power density.

$$P_r = P_D \cdot A_{eff}$$

[AG-PS Rx $P_{min} = -170$ dBm.]



Audio processor.

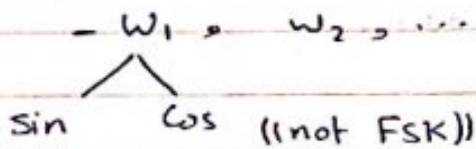
1. Network cell info like freq.
2. Cell Towers.

for ASK, PSK, QAM,

↳ $BW = \frac{rb}{m} (1 + \alpha)$ Hz for 1 and 2 dimension

for. FSK, Multi carrier, N-D modulation.

↳ wide band modulation.



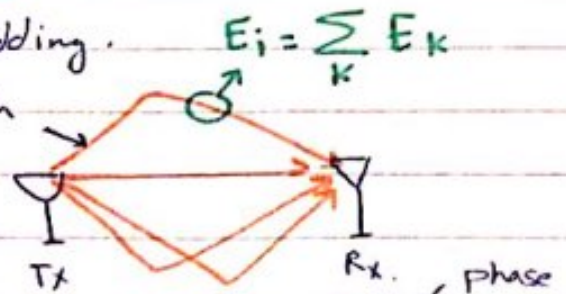
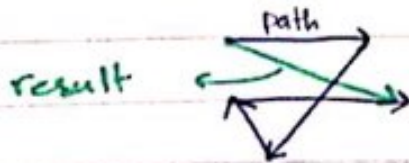
→ SS (spread spectrum)

$FSK BW = M \frac{rb}{m} (1 + \alpha)$

"BW just"

↳ using for fading. Multi path

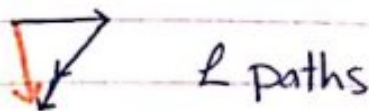
* Fading :-



$$E_k = E_0 e^{j\delta k} e^{-\alpha k}$$

$\alpha \equiv R.V$
 $\delta \equiv R.V$

worst case two ray model



$$E_i = \alpha_i E_o$$

fading →

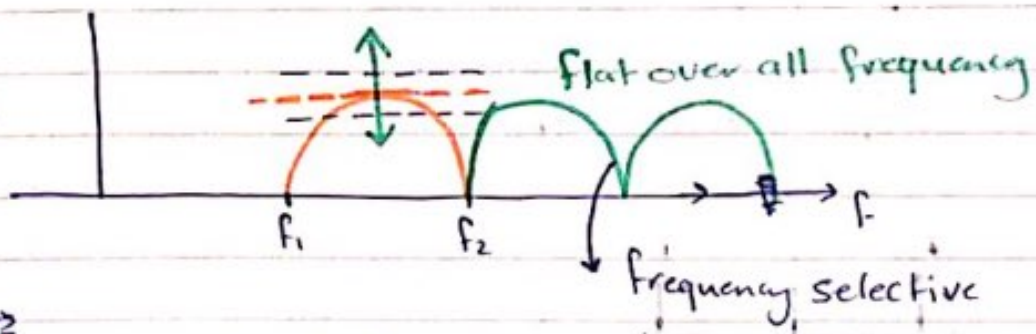
تغير في نسبة الإشارة في القناة

slow
fast.

Slow fading → slow (flat fading)
quasi slow (quasi static) channel equalizer. (كل شيء ثابت)

fast fading

channel in frequency domain:-

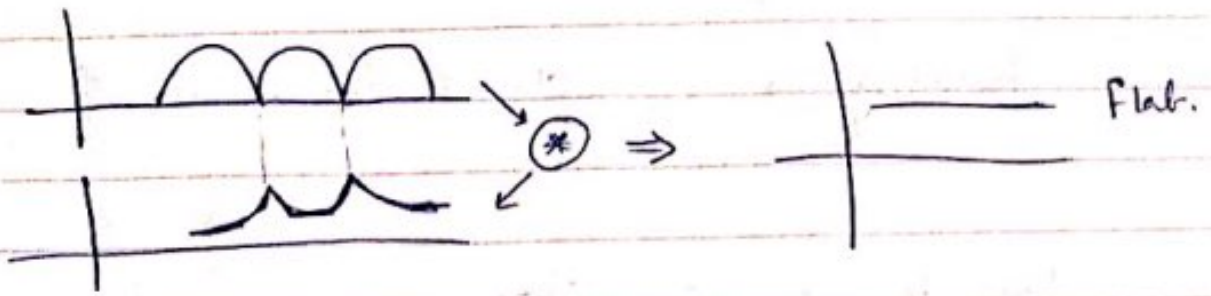


$$\Delta \theta = \frac{2\pi}{\lambda} \Delta d$$

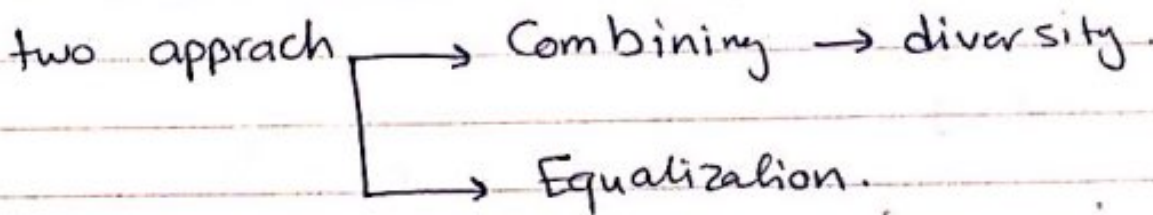
frequency band ↑ → λ ↓
[worst case. ← frequency selective ~LS ISI]

selective → band.

x. equalizer.



~~two approach~~

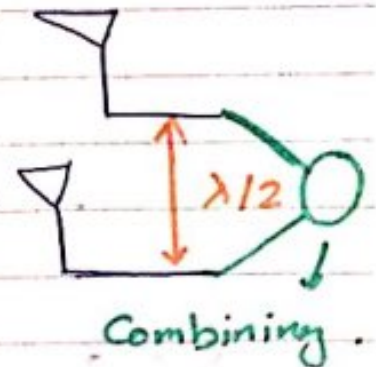


need 2 independent antenna.

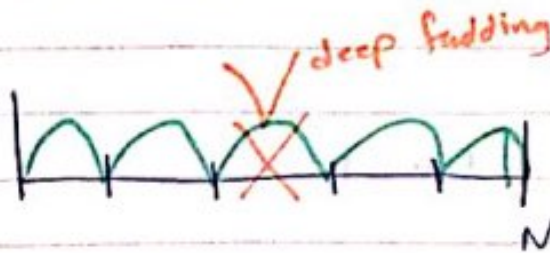
combining -> 2 signal zap
phase shift = 180°



Tx with 2 Rx with modem
fading $\propto 1/r^2$

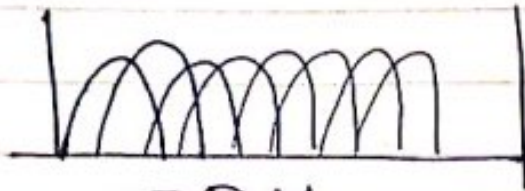


data $\rightarrow E_c$
Sub channel
Sub carrier.



selective $\propto 1/r^2$
non selective $\propto 1/r^4$

40



OFDM \Rightarrow FSK positive
 \hookrightarrow orthogonal

2G - GSM \rightarrow اوريبي

- IS 54
- IS 36
- IS 95

\rightarrow NCDMA $N \equiv$ ~~Narrow~~ Narrow

WCDMA $W \equiv$ wide band.

3G - CDMA (Power control) \rightarrow UMTS

\hookrightarrow Power Control. SIPIS

2.5 EDGE
GPRS

3.5G OFDM (Y-Max) } for IP

4G OFDM

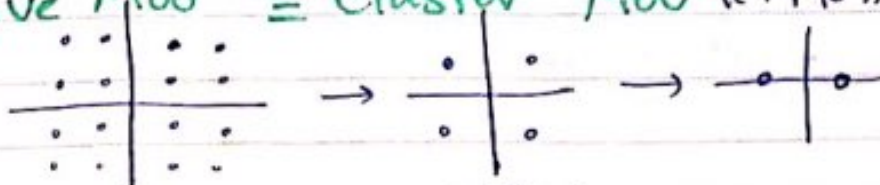
* each sub carrier:

((2004))

Adaptive Mod

\equiv Cluster Mod

((1996))



16 QAM

4QAM

... , Y max في ...

41

Quiz 1:

given the path loss equation as:

$$L = 65 + (1.3ht + 31) \log(r)$$

find the C/I from a user 500 m from his own base station. and coverage. 2.5 km from each cells.

the cell configuration is 3x3

$$ht = 20 \text{ km.}$$

find γ ?

$$\gamma = \text{~~3.1~~ } = 3.1$$

$$\frac{C}{I} = (EIRP - L_c) - (\bar{I}) - (L_i + 3) - L_c$$

~~3.1~~

$$\bar{I} = EIRP - (L_i + 3)$$

$$\frac{C}{I} = 68 + (26 + 31) \log(r) - 65 - 57(\log(r))$$

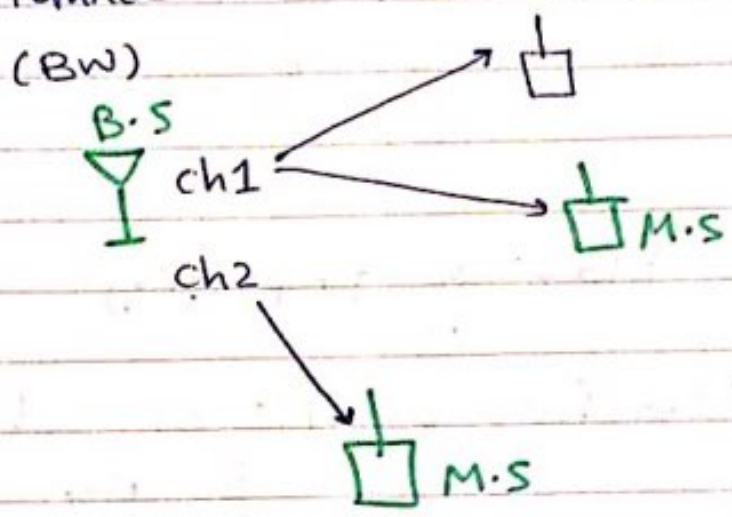
$$= 3 + 57 \log\left(\frac{2500}{3}\right) - 57(\log_3(500))$$

$$= 42.8 \text{ dB}$$

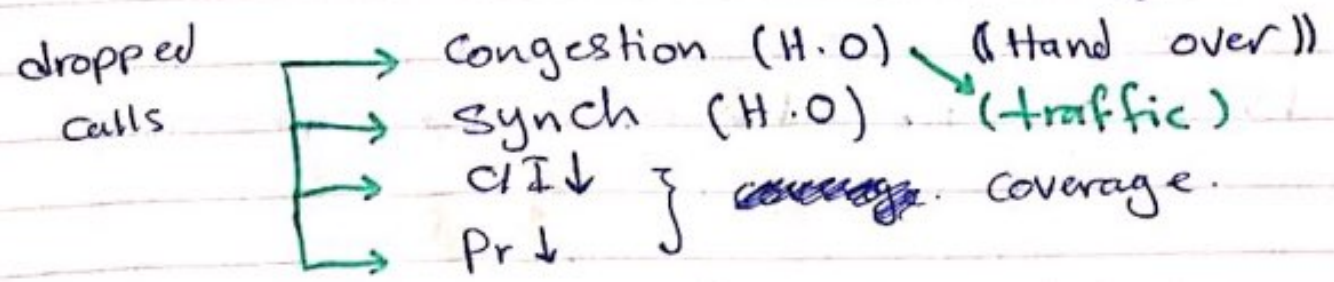
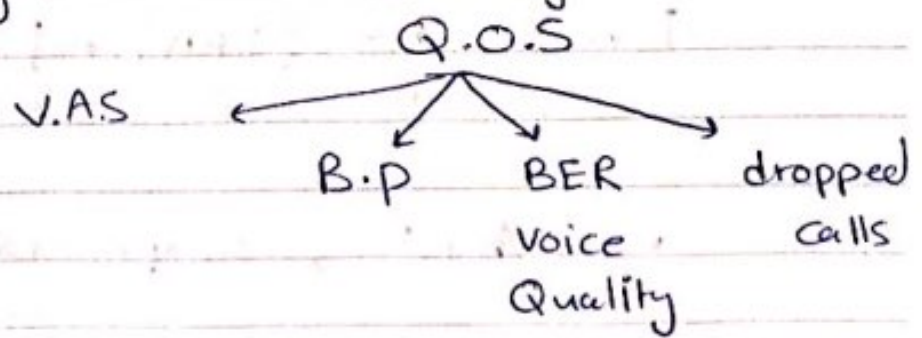
42

Channel:

- fading
- Interference



⇒ max capacity . → under Quality of Service



Voice Quality

- source code (Data compression).
 (related to Modulation)
- Channel code E.CC

B.p \equiv blocking probability

↳ Traffic \rightarrow No of channel.

↳ BW
↳ spectral efficiency
7% \Rightarrow
dimension of modulation.

$$BW_{ch} = \frac{r_b}{m} (1+\alpha) \cdot BW_{expansion\ factor} \left(\frac{n}{k}\right)$$

$$r_b = r_b^* \cdot \text{Compression ratio.}$$

$$BW_{ch} = \frac{r_b}{m} (1+\alpha) \cdot BW_{expansion\ factor} \cdot \text{compression ratio.}$$

↓ ↓ BER ↑ ↓

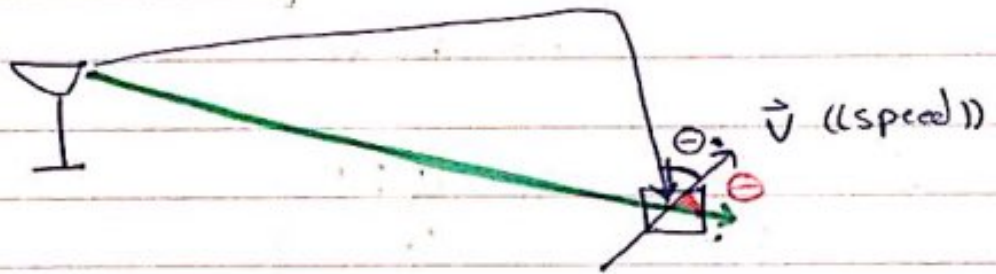
BER \uparrow \rightarrow BW_{ex} \uparrow

((60) BER 5-61)) [49]

$$\text{BER}_{\text{Coded}} \cong (\text{BER}_{\text{ch}})^{E+1}$$

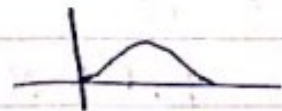
$$\uparrow E \rightarrow \uparrow \frac{n}{k}$$

Doppler effect :-
related to fading



$$\Delta f = \frac{v \cos \theta}{c}$$

$\Delta f \cong R \cdot V$ (Random variable)

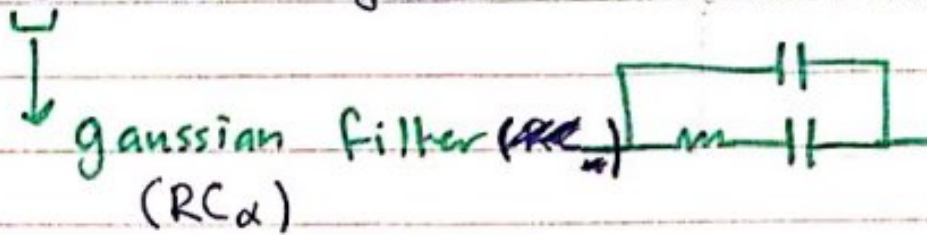


Multiple Access :

- TDMA "Time"
- FDMA
- Hybrid (TDD, FDD)
- CDMA (soft H.O)

⇒ GSM → binary.

GMSK gaussian minimum shift keying.



$\pm \pi/2$ "0", "1"

$$r_b^c = 13.2 \text{ Kbps}$$

⇒ IS ⇒ use different type of modulation
"non binary", more efficient.

IS 36 } π QDPSK
54 } (m=2)

$$r_b^c = 16 \text{ Kbps}$$

⇒ IS95
NCDMA

$$\Phi = \sum_{i=1}^N v_i(t) c_i(t)$$

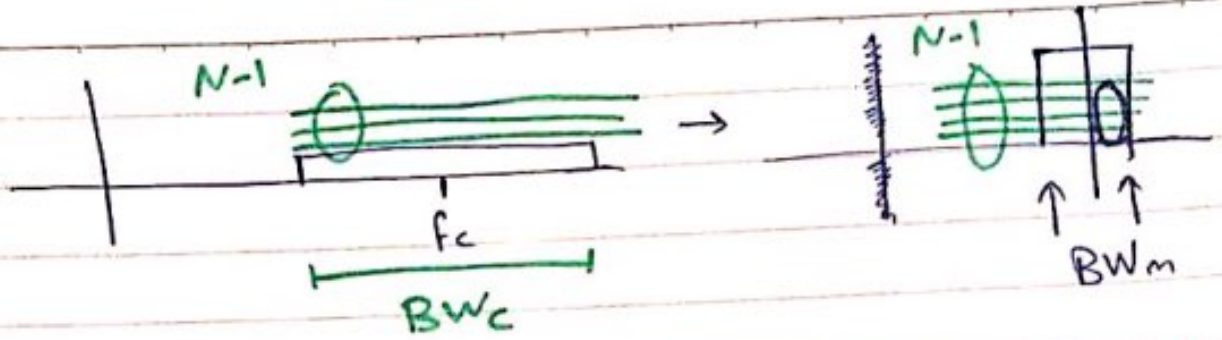
$$\hat{v}_k = \langle c_k, \Phi \rangle = v_k + \underbrace{\sum_{k \neq i} v_i(t) c_i(t) \cdot c_k(t)}_{\text{MAI}}$$

MAI ≡ multiple access interference.

MAI

46

smile...



$$MAI = \frac{P}{\left(\frac{BW_c}{BW_m}\right)} = \frac{P}{C.G}$$

$$C.G = \frac{BW_c}{BW_m}$$

$$\frac{C}{I} = \frac{C.G}{(N-1) \cdot \frac{3}{8}}$$

$$\Rightarrow \frac{C}{I} = \frac{C.G \cdot 8}{(N-1) \cdot 3}$$

C.G = coding gain.

N = Capacity.

(↑ C.G → ↑ N)

Power spectral density power * base station

Power spectral density Control.

power control (fast)

↳ Speed = 15K

* (3/8 of time have interference.)

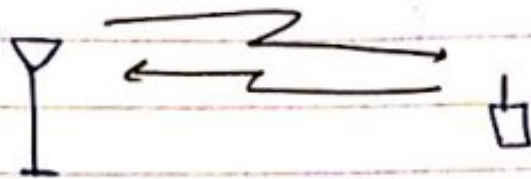
$$\Rightarrow \gamma = \frac{3}{8}$$

$$\frac{C}{I} = \frac{C.G}{(N-1) \cdot \gamma + \sigma_n^2}$$

PN

47

* Multiple Access



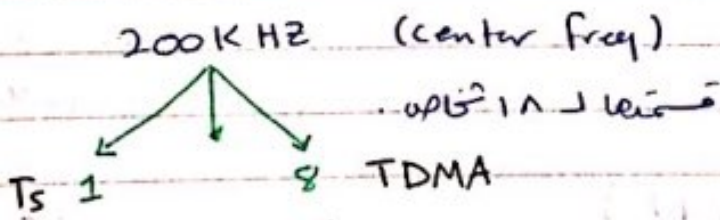
total BW
 r_b limit
 the
 Capacity

- 1- TDMA
- 2- FDMA
- 3- TDMA / FDMA (GSM)

$r_b = 13.2 \text{ Kbps}$

* Analog (AMPS)

$\frac{25 \text{ MHz}}{0.2} \text{ (total BW)} = 125 \text{ ch for analog}$



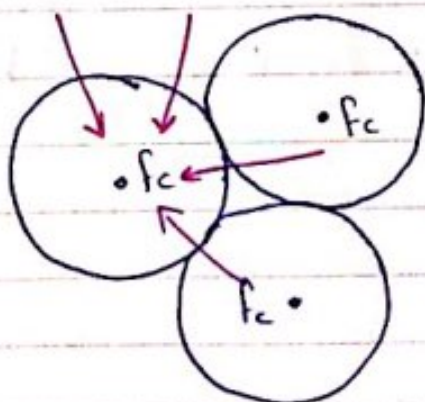
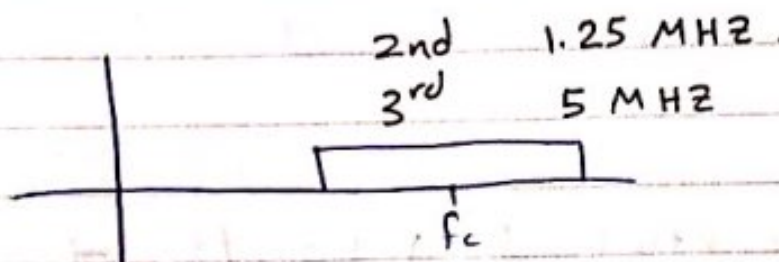
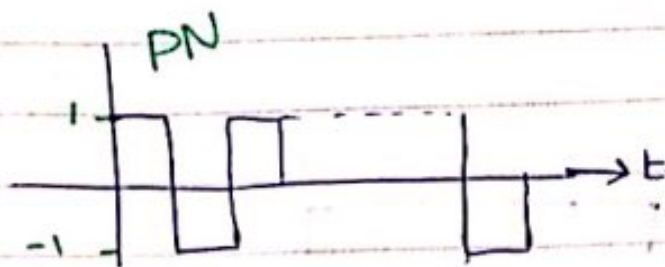
4- CDMA \Rightarrow C/I limit the capacity.

$$\frac{C}{I} = \frac{C \cdot G}{(N-1)I + \sigma_n^2}$$

SS = Spread spectrum

$$C \cdot G = \frac{\text{BW (channel) S.S}}{\text{BW user}} = \frac{r_c}{r_b}$$

$$V_i = C_i * d_i \rightarrow \phi = \sum_{i=1}^N V_i$$



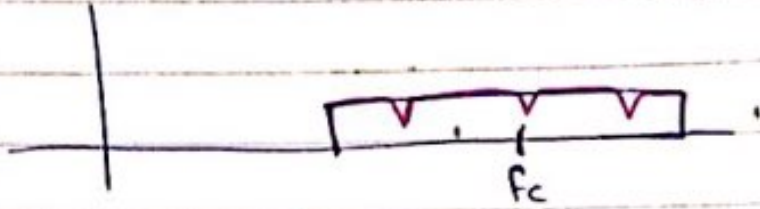
انقدرت نفس
BW

codes \rightarrow Channelization code
 \rightarrow Scrambling code. (sc)

$$V_i = C_i^{ch} \cdot C_k^{sc} \cdot d_i$$

Same freq $k=1 \rightarrow$ "SC maj"

$$\frac{C}{I} = \frac{CG}{(N-1)I + \sigma_n^2 + I_{\text{other cells}}}$$



→ frequency selective fading channel.

Matched filter Rx. for SS \equiv RAKE
 power control 15 K times/S → fast

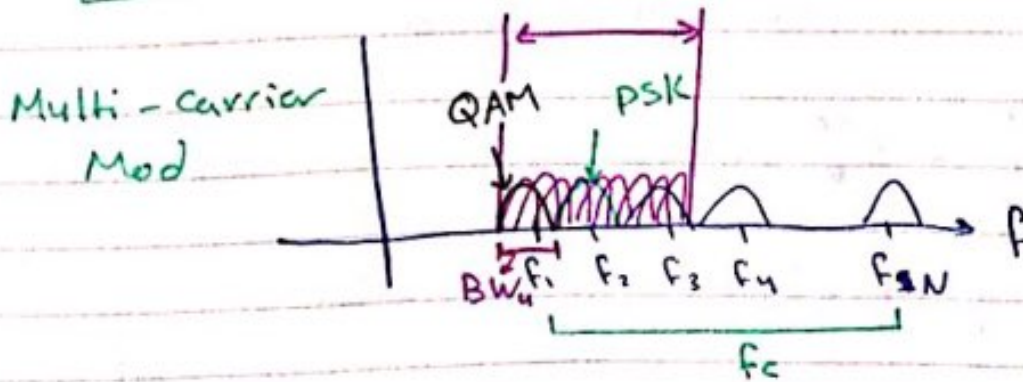
F.H \equiv frequency hopping



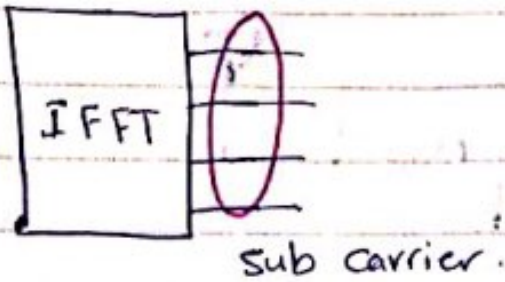
FH in busy hour.

F.H \Rightarrow to average interference $\sim (C/I)$ equal.

5- OFDMA :-



$$BW = N \cdot BW_u$$

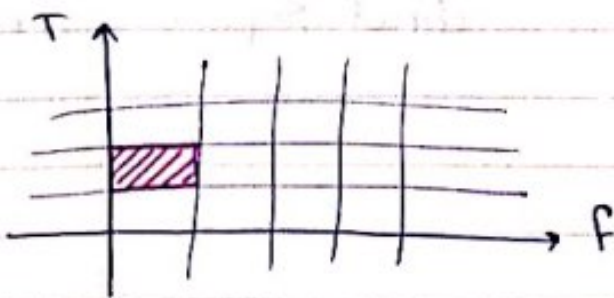


Orthogonal \rightarrow No I.C.I

I.C.I \equiv Inter carrier Interference.

Sub carrier \leftarrow also freq \leftarrow fading \leftarrow LL

Sub carrier \rightarrow Modulation (2D) QAM
 time slot.
 R.B \equiv resource block.

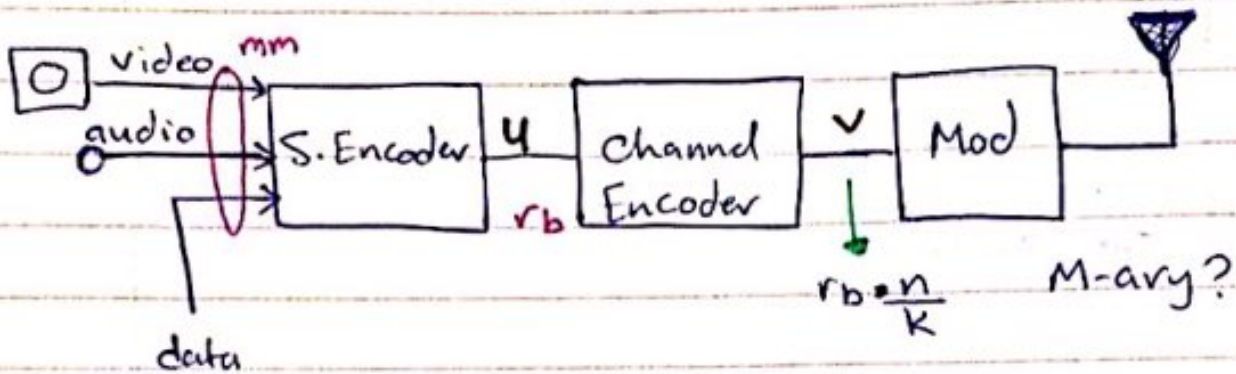


RB $15 \times$
 into Modulation

PAPR \equiv peak average power ratio.
 \rightarrow (water filling algorithm)

GSM → GPRS

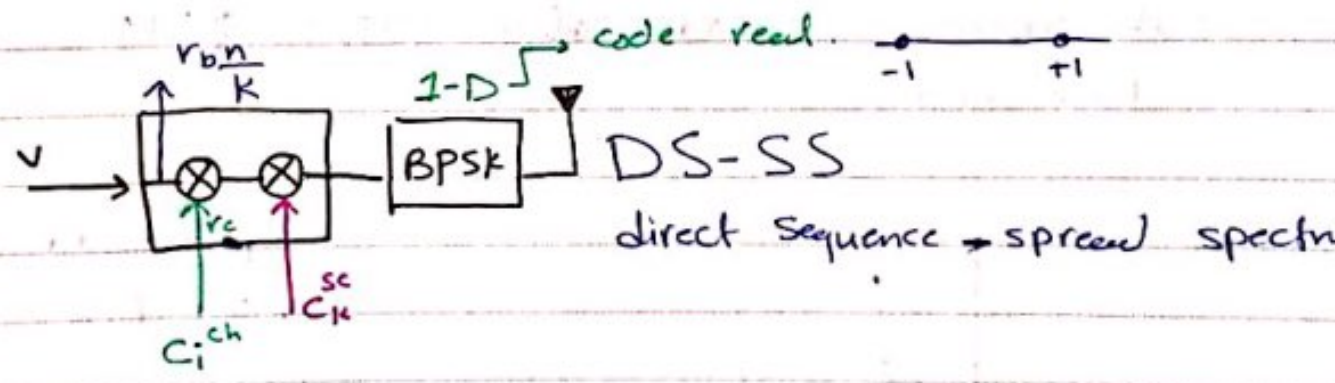
GMSK $\pi/4$ -QDPSK



$$BW_{ch} = \frac{r_b \cdot \frac{n}{K}}{m} (1 + \alpha)$$

{ FDMA
TDMA

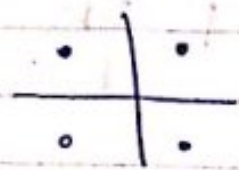
$$BW_{user} = BW_{ch} / N_{user}$$



spread $c_k = \text{spread } c_i$

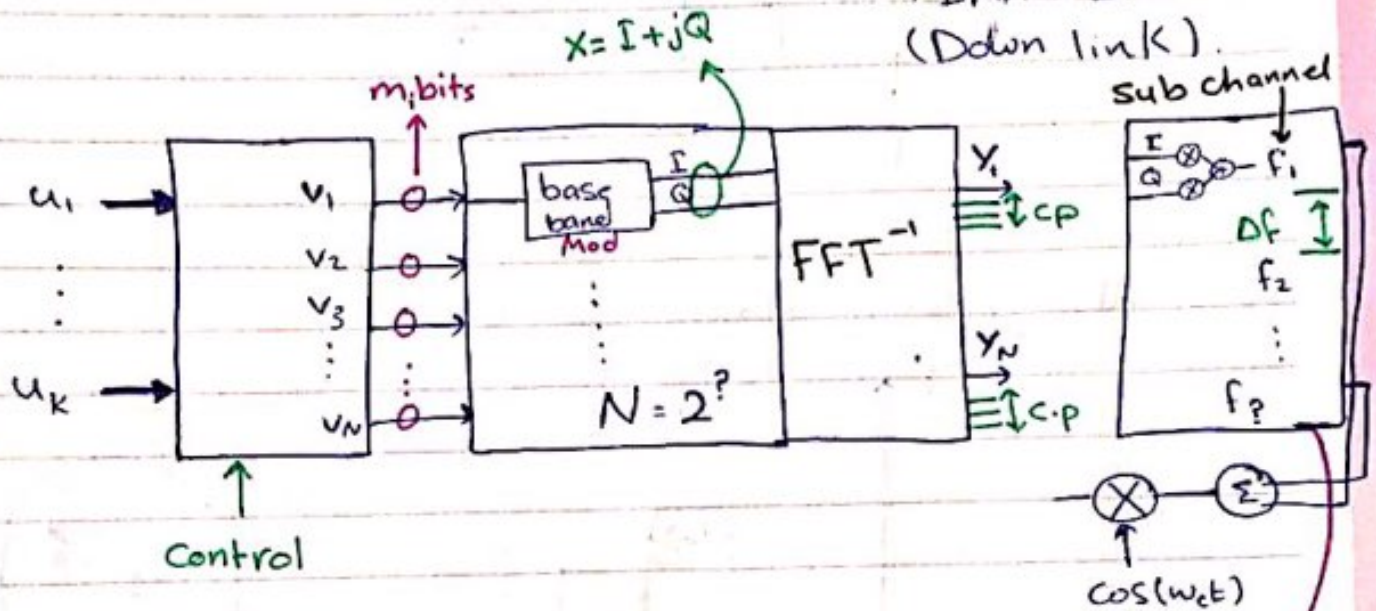
BPSK ≡ Binary phase shift Keying

if 2-D ⇒ $c_i = c_i^{real} + j \cdot c_j^{im}$



Multi-Carrier Modulation :-

OFDM = UL (uplink)
 OFDMA = DL (Down link)



FFT^{-1} = Fast Fourier transformer inverse.

$(N + c.p) \Delta f = BW_{total}$

$$\vec{y} = A \vec{x}$$

$$A = \left[e^{j \frac{nm\pi}{N}} \right]$$

$$A^{-1} = A^H = A^{*T}$$

→ CP = cyclic prefix. (12% from total signal).

* OFDMA :-

total data rate = $\sum_{i=1}^N m_i \rightarrow BW_{ch} = (N + CP) \Delta f$

53

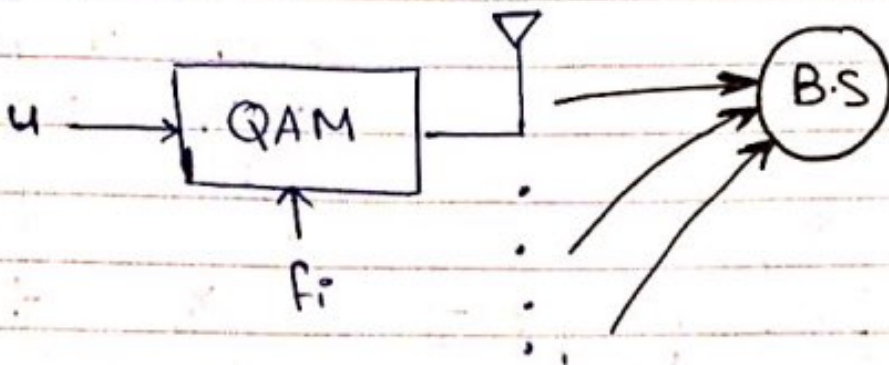
$\Delta f = 10 \text{ KHZ}$

←

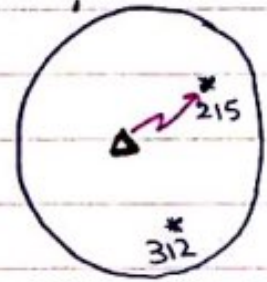
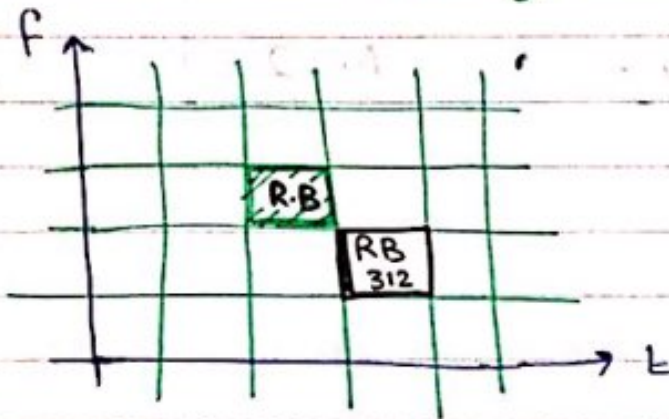
$\Delta f = \frac{f_s}{N}$

$f_s = f \text{ sampling}$

UL: UP link



RB \equiv resource block. (capacity).



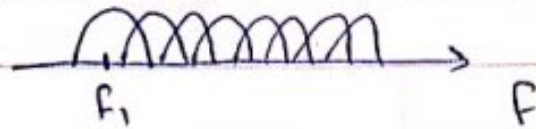
data \rightarrow loss less compression.

Video \rightarrow lossy compression.
audio \rightarrow lossy compression.

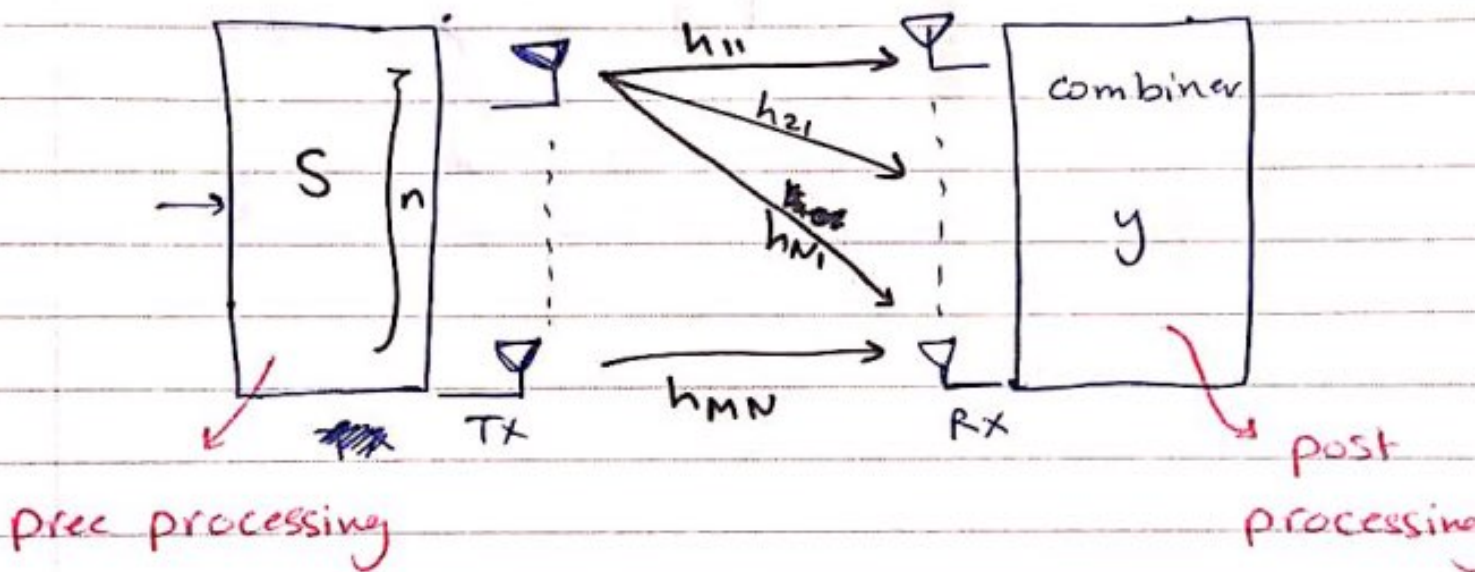
data \Rightarrow real use GSM.

"Mid \Rightarrow 20/11/2017 Monday"

- coding gain
- Diversity gain



OFDMA \rightarrow flat fading

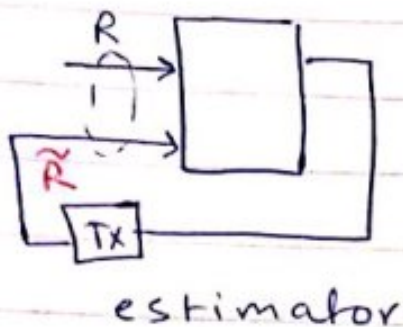


MIMO System.

$$H = \begin{bmatrix} h_{11} & h_{21} & \dots & h_{n1} \\ h_{12} & h_{22} & \dots & \vdots \\ \dots & \dots & \dots & h_{mN} \end{bmatrix} \quad y = HS$$

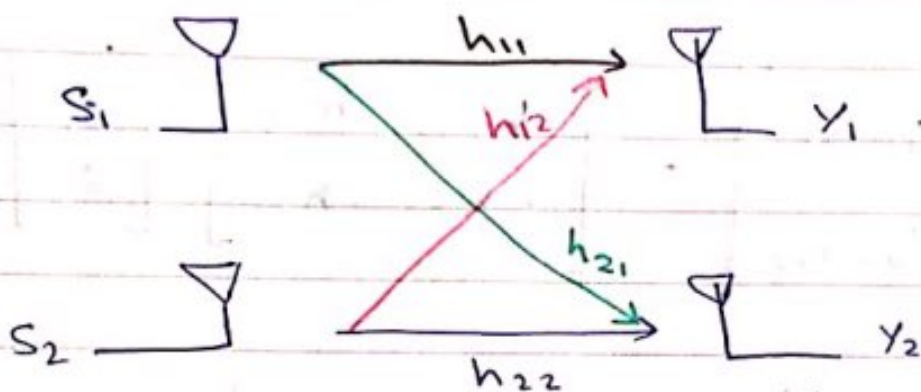
$$S = H^{-1} y$$

$$H^{-1} = \{ H H^T \}^{-1}$$



* Maximal combiner ratio
 $CN = \frac{\lambda_{\max}}{\lambda_{\min}}$ $\lambda \equiv$ eigenvalue

* Condition number measuring stability.



	TS1	TS2
out 1	S_1	S_2
out 2	S_1	$-S_1$

	TS1	TS2
y_1	$S_1 h_{11} + S_2 h_{12}$	$S_2 h_{11} - S_1 h_{12}$
y_2	$S_1 h_{21} + S_2 h_{22}$	$S_2 h_{21} - S_1 h_{22}$

$$y_1 = \begin{bmatrix} y_1 \text{ TS1} \\ y_2 \text{ TS2} \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{12} & h_{11} \end{bmatrix} \begin{bmatrix} S_1 \\ S_2 \end{bmatrix}$$

$$\Delta = |h_{11}|^2 + |h_{12}|^2$$

determine of receiving matrix
is positive $\begin{matrix} \swarrow & \searrow \\ \text{ } & \text{ } \end{matrix}$ $\begin{matrix} \swarrow & \searrow \\ \text{ } & \text{ } \end{matrix}$ *

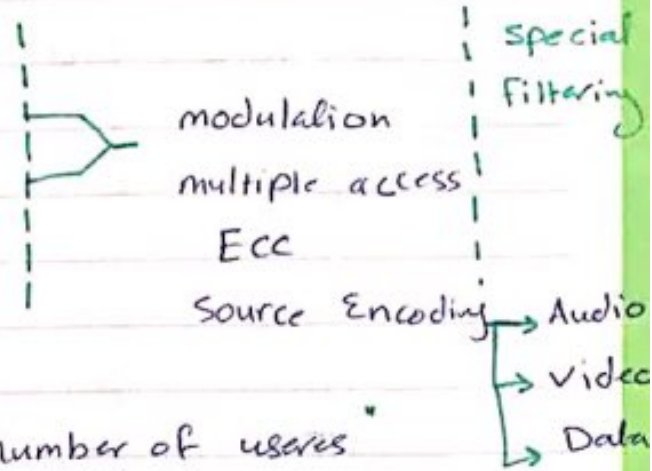
inverse في $\sim \Delta$ \leftarrow det في $\sim \Delta$ \leftarrow $\begin{matrix} \swarrow & \searrow \\ \text{ } & \text{ } \end{matrix}$ $\begin{matrix} \swarrow & \searrow \\ \text{ } & \text{ } \end{matrix}$ *

$$y_2 = \begin{bmatrix} y_2 T_{s1} \\ y_2 T_{s2} \end{bmatrix} = \begin{bmatrix} h_{21} & h_{22} \\ -h_{22} & h_{21} \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix}$$

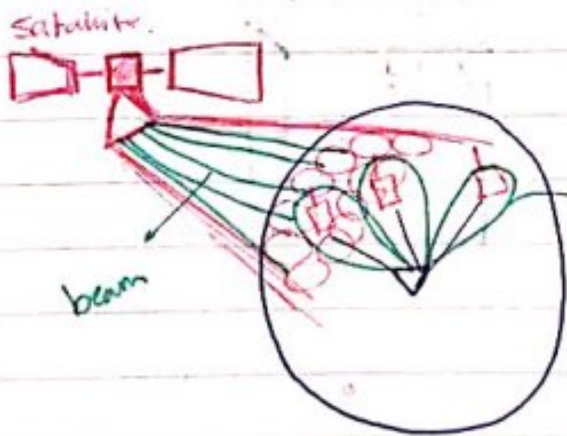
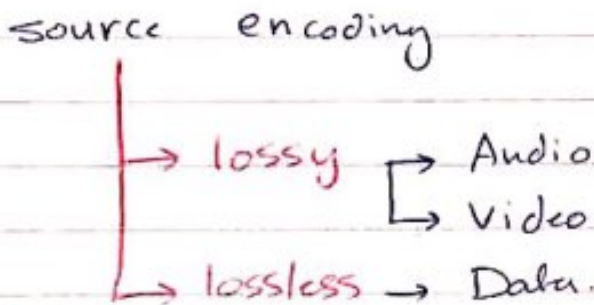
Time and space diversity.

Basic design:-

- Traffic (capacity)
- No of channel
- C/I \bar{I}
 - sectorization
 - down teltting
 - F.H.



" capacity \equiv data rate not number of users "



3 beam \rightarrow
beam "independent for each other"

- Iridium "66 sat"
- Global star "44 sat"
- Odessy "!"
- Al Thuraya "✓"

$\nabla \equiv$ base station
" K=1 "

* Spatial Filtering by using
Antenna - arrays

* Space time codes. $\left\{ \begin{array}{l} \rightarrow \text{STBC} \\ \rightarrow \text{STTC} \end{array} \right\} \rightarrow \text{Smart diversity}$
STC \rightarrow ~~conventional code~~

STBC \equiv Space time block code.

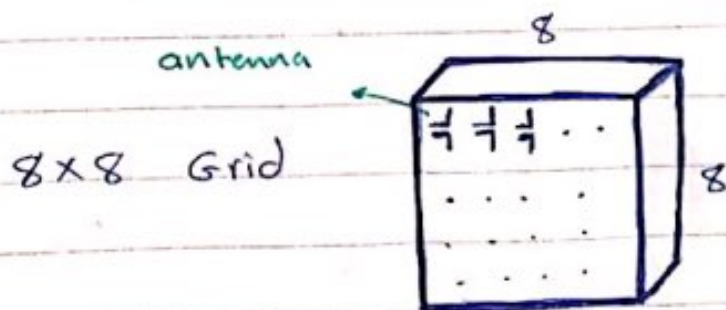
STTC \equiv Space time ~~conventional~~ code
Trilles

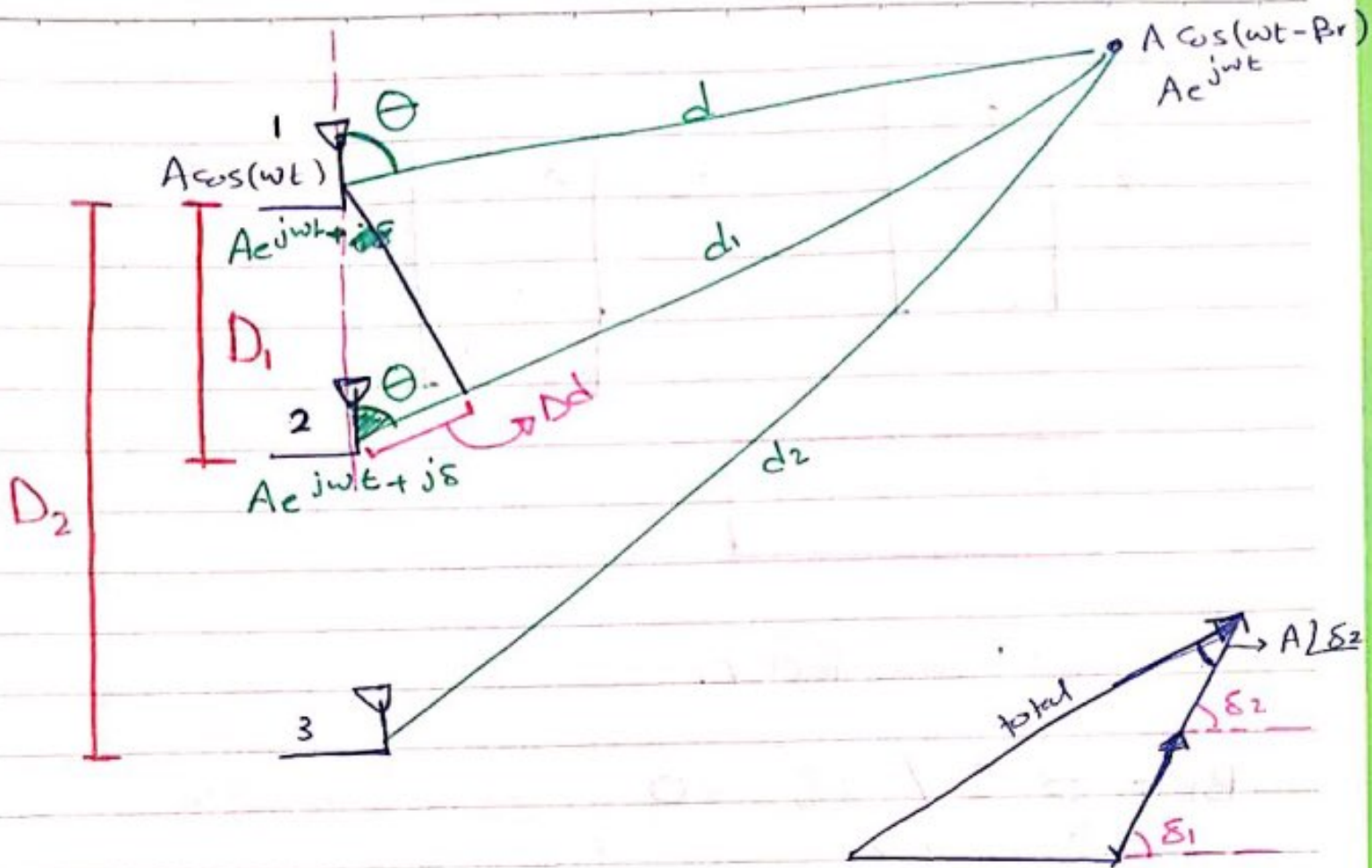
* Smart Antenna.

"Can provide beam"

\rightarrow Beam forming

\rightarrow ~~Adaptive~~ Adaptive beam antenna.





$$\Delta d_{12} = D_1 \cos \theta$$

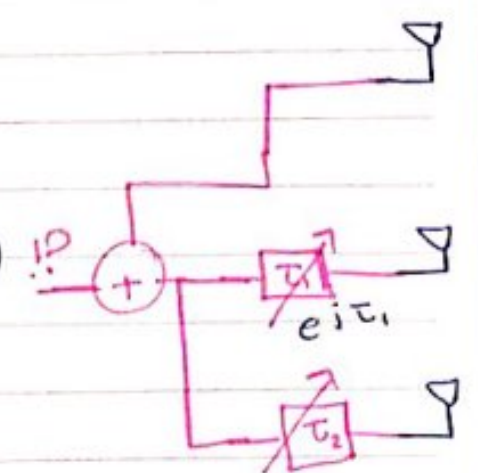
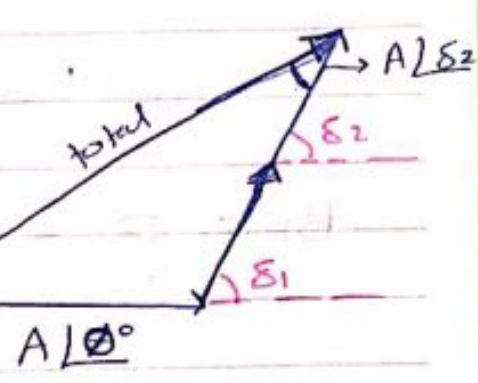
$$\Delta d_{13} = D_2 \cos \theta$$

$$\delta_1 = \frac{2\pi D_2 \cos \theta}{\lambda}$$

$$V = \sum_{i=1}^L A e^{j \left(\frac{2\pi D_i \cos \theta}{\lambda} - \tau_i \right)}$$

for each θ find τ_i 's

$$V = \sum e^{j \frac{2\pi D_i}{\lambda} \cdot a_i} \cdot e^{j \cos \theta \cdot a_i} \cdot e^{-j \tau_i}$$



∞

$$\Theta = \begin{bmatrix} e^{j\theta} \\ e^{j\theta} \\ \vdots \\ e^{j\theta} \end{bmatrix} \quad \Leftrightarrow \quad \tau = \begin{bmatrix} e^{-j\tau_1} \\ e^{-j\tau_2} \\ \vdots \\ e^{-j\tau_L} \end{bmatrix}$$

$$\text{BF} = \Theta^T \tau$$

BF \equiv Beam Factor.

$$\text{BF} = \Theta \tau / w \tau = 0$$

\hookrightarrow Θ matrix

General equation.

$w \equiv$ weigh vector.

$$\vec{D} = \begin{bmatrix} e^{j\theta} \\ e^{j\theta} \\ \vdots \\ e^{j\theta} \end{bmatrix}$$

$$\vec{C} = \begin{bmatrix} e^{-j\tau_1} \\ e^{-j\tau_2} \\ \vdots \\ e^{-j\tau_L} \end{bmatrix}$$

$$\text{BF} = \vec{\Theta}^T \vec{\tau}$$

BF \equiv Beam Factor.

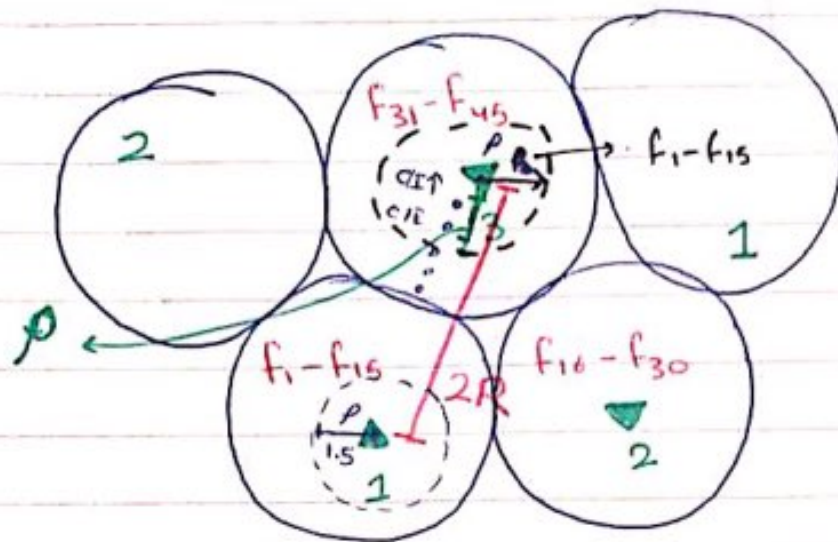
$$\text{BF} = \vec{\Theta} \vec{\tau} / w \tau = 0$$

$\hookrightarrow \Theta$ matrix

General equation.

$w \equiv$ weigh vector.

* Micro cells :-



Find P that satisfy $(C/I)_{\min}$

$$C = d^{-\gamma} = P^{-\gamma}$$

$$I_1 = 3(2R - P)^{-\gamma} \quad \text{on average.} \Rightarrow I = (2R)^{-\gamma}$$

$$\frac{C}{I} = \frac{\left(\frac{2R}{P}\right)^{\gamma}}{3}$$

Ex $\gamma = 3$, $R = 2 \text{ Km}$ $\left(\frac{C}{I}\right)_{\min} = 8 \text{ dB}$

Find P ?!

$$(C/I)_{\min} = 10^{0.8} = 6.3$$

$$\frac{2R}{P} = \sqrt[3]{3 * 6.3}$$

$$P = \frac{2 * 2 \text{ Km}}{\sqrt[3]{18.9}} = 1.5 \text{ Km}$$

62

Quiz 2

for a 3×3 cell configuration each sector uses 15 channel in a certain cell we implement a M-cell by using 2 channel from each surrounding sector find the M-cell radius if the min C/I is 9dB ?!

12 channel

I at $2R$

(I = 1)

$$\frac{C}{I} = \frac{P^{-\delta}}{2R^{-\delta}}$$

$$\frac{C}{I} = \left(\frac{2R}{P} \right)^{\delta}$$

$$\sqrt[3]{10^{0.4}} = \frac{2R}{P}$$

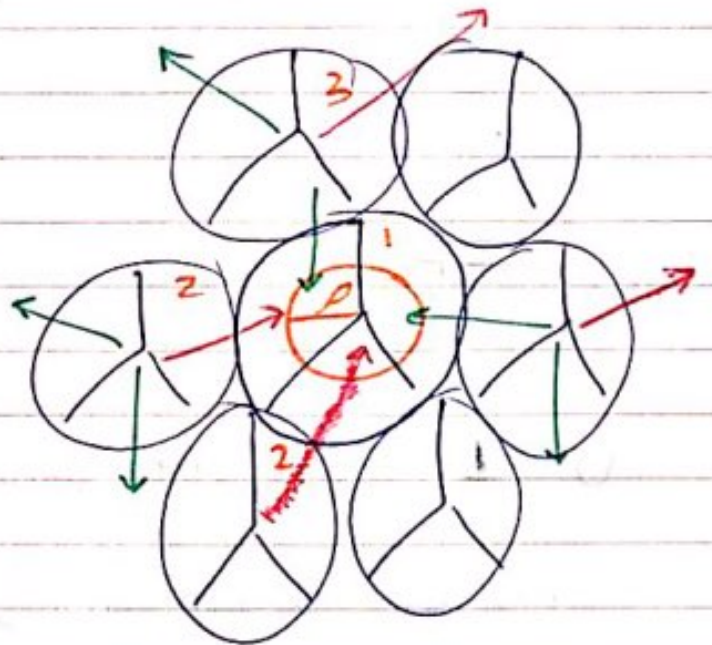
$$R = P$$

at 15 dB

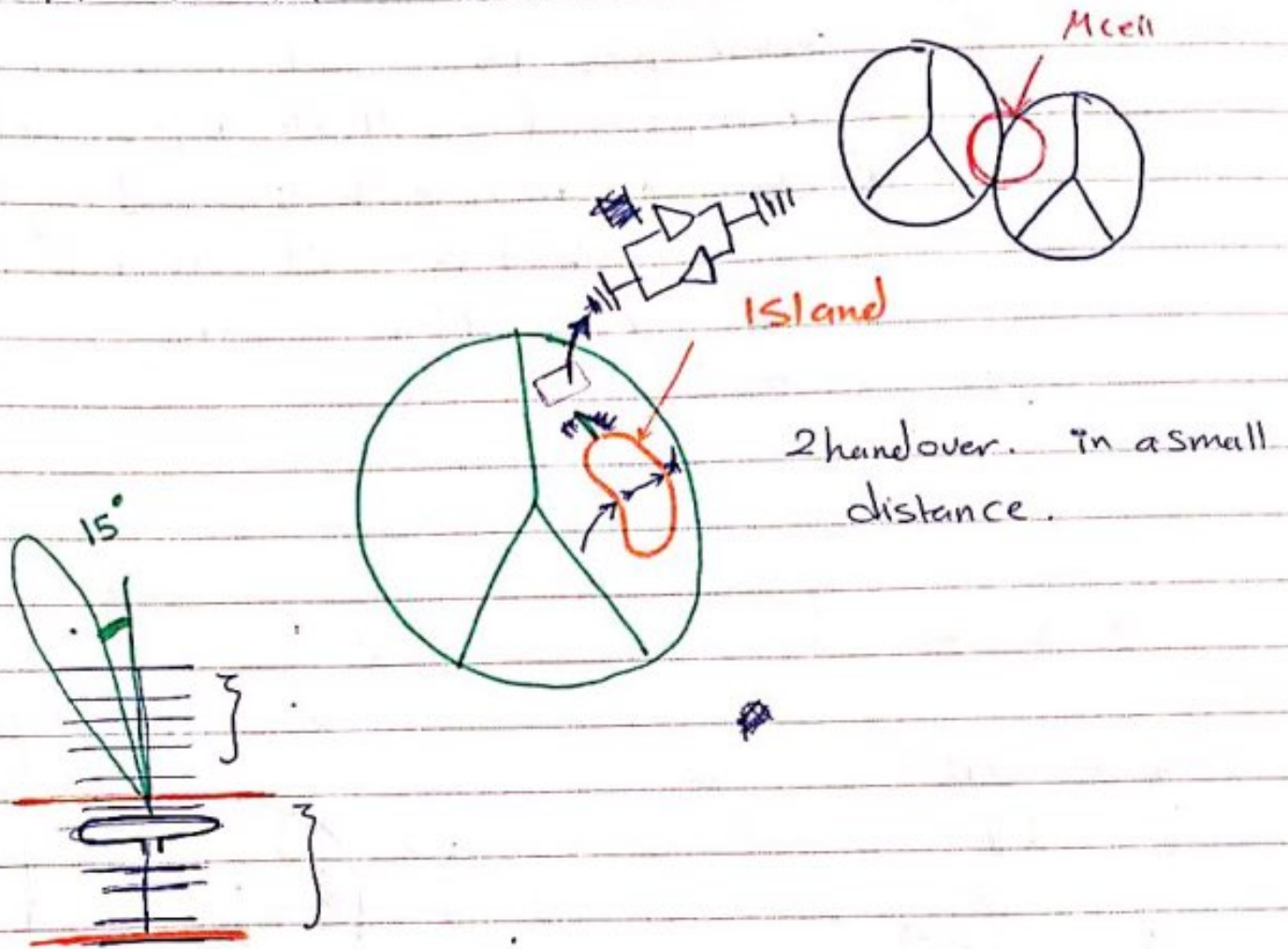
$$\frac{2R}{P} = \sqrt[3]{31.6}$$

$$P = 0.63R$$

63



if M cell between 2 cell



UAGI ANTENNA Passive Receiver

between 2 antenna → 2 amplifier.

Quiz 3

For 3x3 cellular system operates at ~~8~~

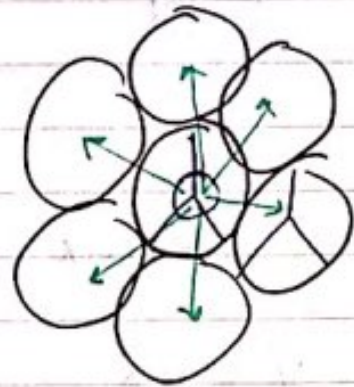
$\frac{C}{I} = 8.5$ dB if micro cell is inserted inside of

cell with radius $r = 0.4R$ and $P_{EM} = \frac{1}{10} P_t$

⇒ find the new C/I in the surrounding Macro cell?!

$$\frac{C}{I} = \frac{R^{-\alpha}}{2D^{-\alpha} + \alpha(2R-r)^{-\alpha}}$$

$$\alpha = \frac{P_{EM}}{P_t}$$



$$\frac{C}{I} = \frac{R^{-\alpha}}{2D^{-\alpha} + \frac{1}{10}(1.6R)^{-\alpha}}$$

$$= \frac{1}{2\left(\frac{D}{R}\right)^{-\alpha} + \frac{1}{10}(1.6)^{-\alpha}}$$

$$\frac{C}{I} = \frac{(D/R)^{\alpha}}{2} = 7.08$$

$$\frac{D}{R} = 2.41$$

$$\left(\frac{C}{I}\right)_{\text{new}} = \frac{1}{2(2.41)^3 + \frac{1}{10}(1.6)^{-3}} = 5.97$$

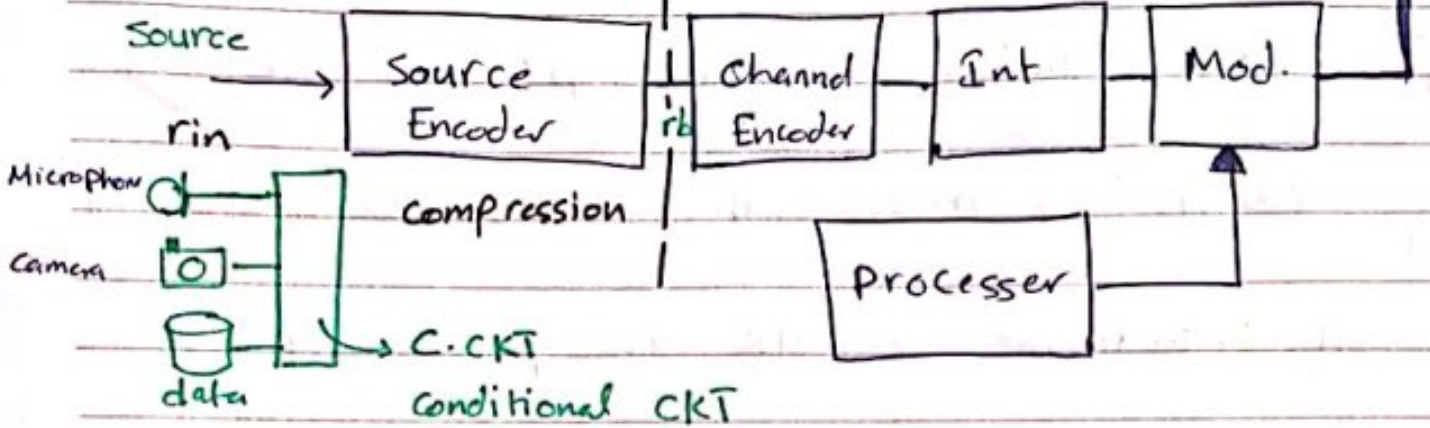
7.76 dB

65

smile...

mean square error \equiv mse

A/D \rightarrow mse = $\frac{\Delta^2}{12}$ (step size)



Inside Frame \rightarrow pilot data.



$X \equiv$ Transmit signal (vector)
 $y \equiv$ Received signal (vector)
 $H \equiv$ Matrix

$$\vec{y} = H \vec{x}$$

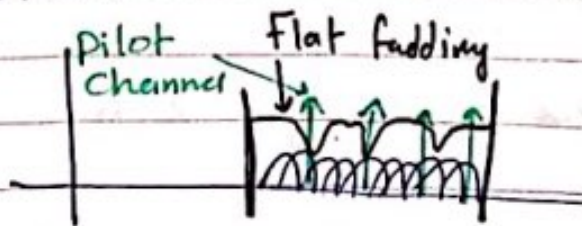
vector $n \times 1, k \times 1$

$$h = [h_0 \ h_1 \ h_2 \ \dots]$$

H for slow fading, fast fading.

In OFDM

Water filling Algorithm



equality likely \rightarrow equalization

المنهجية المتساوية
 size of attenuation
 " " "

CSF frequency selective \rightarrow flat

Pilot - channel \rightarrow synchronization
 \rightarrow amp \rightarrow amp signal, channel estimate.
 Pilot

$L_{\text{packet}} = 1\text{K bytes}$ 8K bit

total size = $1000 \times 8\text{K}$

$$\text{BER required} = \frac{1}{8\text{M}} = 1.25 \times 10^{-7}$$

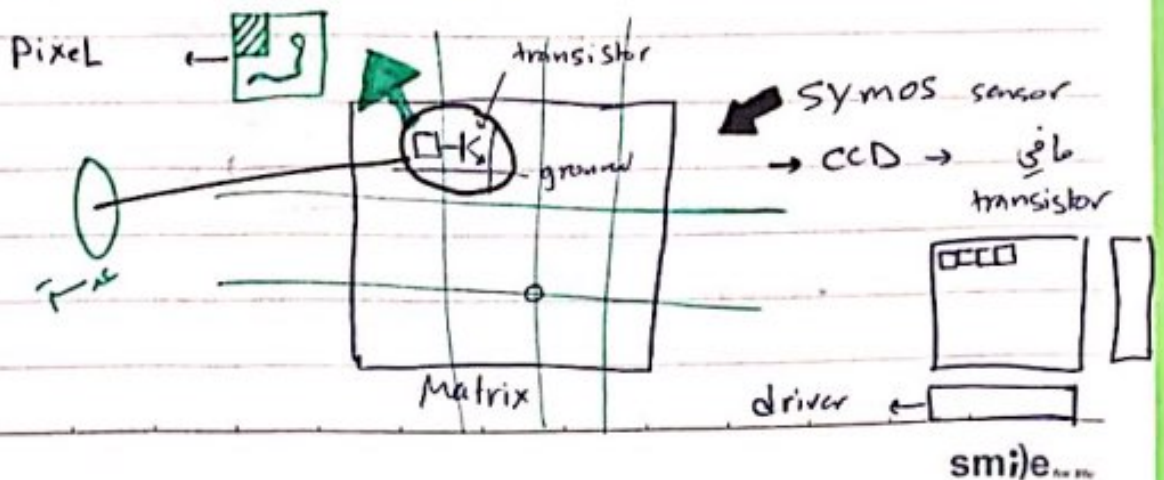
using channel coding to get BER required.

$$\boxed{\text{BW} \propto r_b} \Rightarrow \text{linear}$$

\downarrow BW \rightarrow signal loss ((compress))

Source Encoding:-

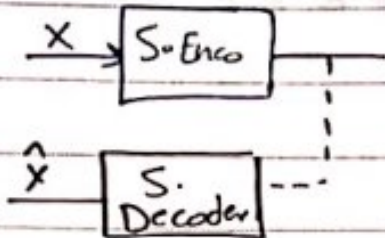
- loss less "use for control data" \Rightarrow compach
- lossy (audio (A), (V) ~~and~~ Video) \Rightarrow compression.



67

Rate \equiv bits (bits per sample)
use

* Compression ratio = 5 \rightarrow $\frac{1}{5}$ of original



$$mse = E \{ |x - \hat{x}|^2 \} = D \text{ random } \rightarrow (\text{audio})$$

$= L_2 \rightarrow$ average dist

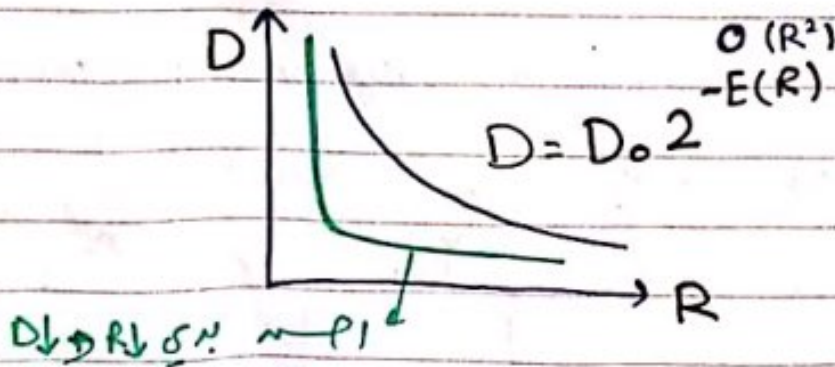
$\uparrow mse \rightarrow \uparrow$ distortion.

$$E \{ |x - \hat{x}| \} = L_\infty$$

\uparrow norm

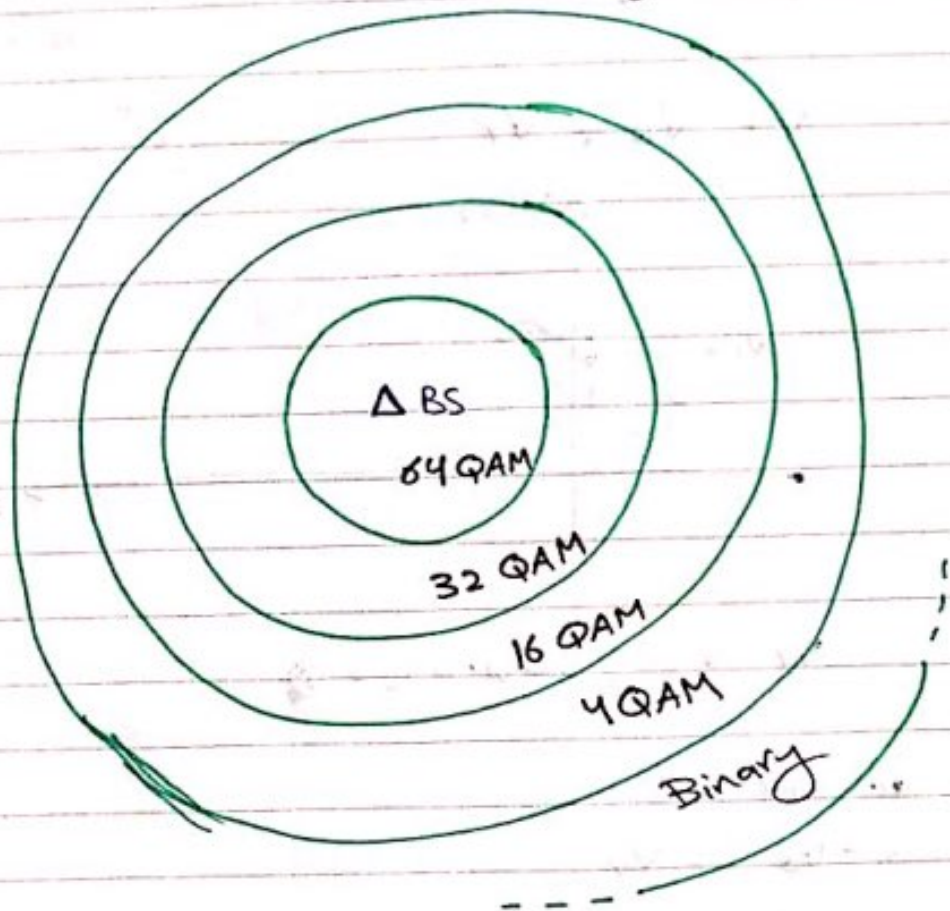
$L_2 \equiv$ second norm (used)

R-D : Rate Distortion theory for each type of source encoder.
 $\uparrow R \rightarrow D \downarrow$

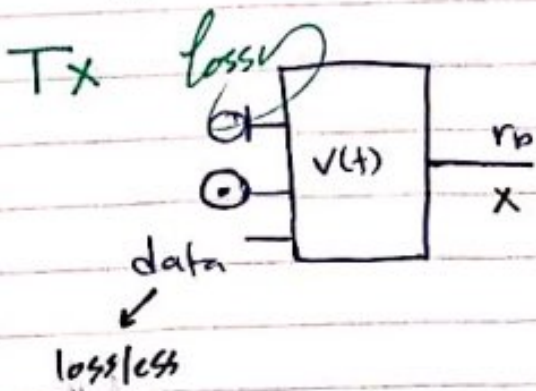


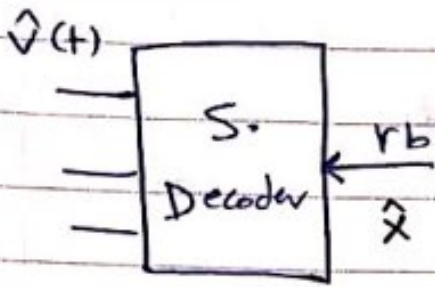
$E \equiv$ energy function of R.

$\alpha \propto$ attenuation factor at low freq.



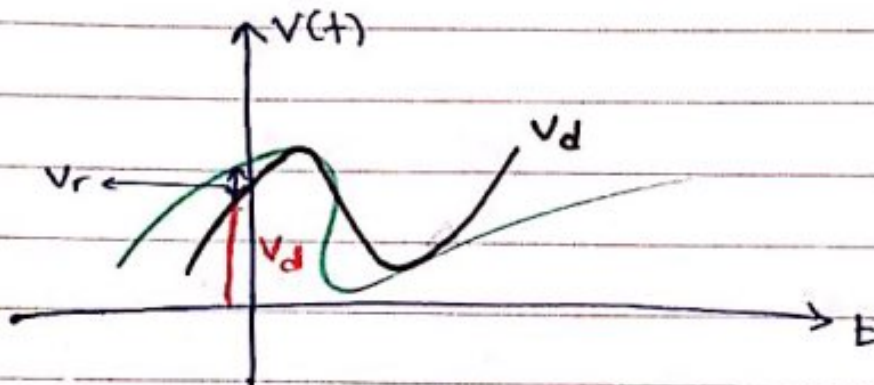
$BW_{ch} \propto r_b$





$$V = V_d + V_r \quad \text{"Voltage"}$$

$r \equiv \text{random}$
 $d \equiv \text{deterministic}$



$$V_r \rightarrow \text{noise}$$

at TX

$$V - V_d = V_r$$

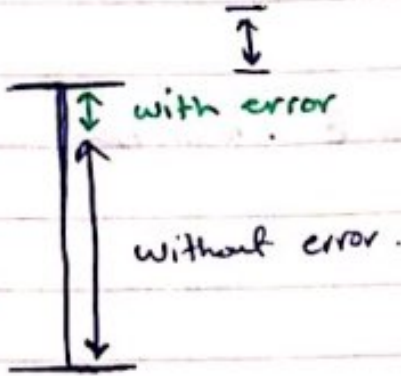
at Rx

calculate V_d

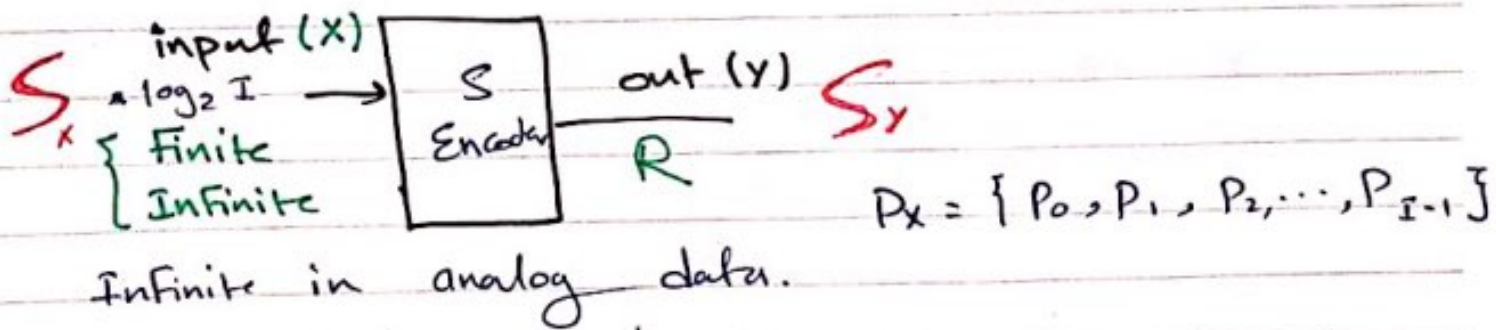
using V_r

$$V_r + V_d = V$$

$V_r \Rightarrow \text{levels small}$



* loss less \rightarrow data digital
 \rightarrow Finite elements.
~~for bounded input~~
 use for finite input levels.



In Finite, data use lossless

$$X \in \{X_{01}, X_{02}, X_{02}, \dots, X_{J-1}\}$$

\rightarrow Symbols

$$Y \in \{Y_0, Y_1, Y_2, \dots, Y_{J-1}\}$$

group

Source is consist of (letter, word, symbols) and a prob distribution function for these letters.

$$H = \sum_{i=0}^{I-1} P_i \log_2 P_i \text{ bits}$$

* Entropy of the source represents number of bits.
 * مقياس كمية المعلومات في ال source

* مقياس كمية المعلومات في ال source

We can compress any source to its entropy without loss.

$$R \geq H$$

$H \Rightarrow$ عدد ال actual number
 : $(\log_2 I)$

* $\log_2 I \rightarrow$ just for equally likely.

Example

$S_x = \{a \ b \ c \ d\}$ "4 letter \rightarrow ~~2bit~~ 2bit if equally likely"
 $P_x = \{0.1 \ 0.1 \ 0.4 \ 0.4\}$

Sol:

$$H = -2 * 0.1 (\log_2 0.1) - 2 * 0.4 \log_2 (0.4) \\ = 1.722 \text{ bits}$$

Its a non convex problem ?!

72

loss less codes :-

1- Huffman code.

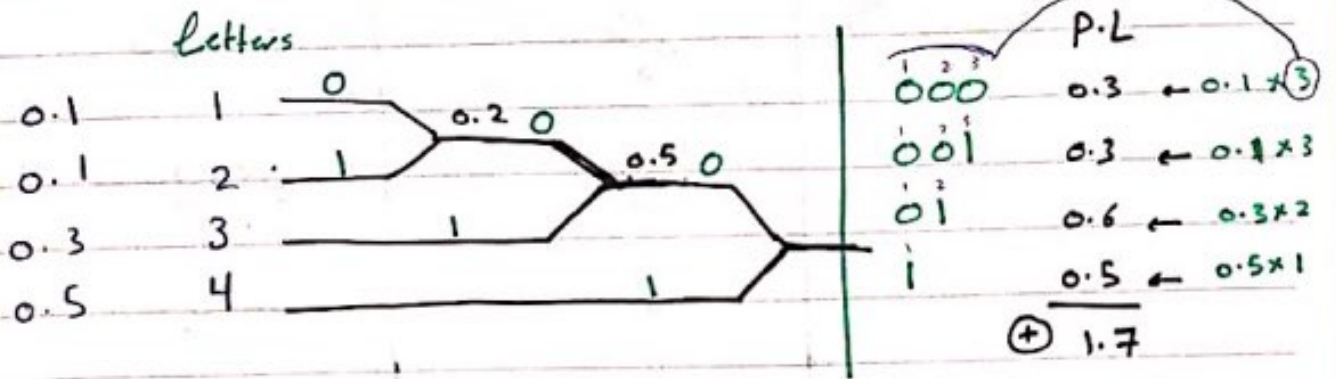
2- LZ

Source :-



$\mathcal{L} = \{1, 2, 3, 4\}$ "letters"

$P = \{0.1, 0.1, 0.3, 0.5\}$



Combine ~~last~~ lowest prop.

$$\sum P.L = R$$

data = 4 3 4 4 2 1 4 1
 d = 1 01 1 1 001 000 1 000
 4 3 4 4 2 1 4 1

73

"1 beāo nāgī Rk. ie letter 4 "1 1 1 1" *

$$R_{xx}[m] = E \{ X[n] \cdot X[n+m] \}$$

* LZ: -

Ex $d = \underline{10110011} \mid \underline{0001111} \mid \underline{01010111100110}$

	(m) i (index)	data	(m+1) code word = #of bit + 1 index
i.c	0000	0	$\frac{0000}{i} \frac{0}{d}$
	0001	1	0001
	0010	01	00001 ↑ index for 0
	0011	10	00010
	<u>0100</u>	<u>011</u>	<u>0010</u> 1
	0101	00	00000
	0110	011	<u>0100</u> 1 0111
	0111	101	00111
	1000	010	00100
	1001	11	00011
	1010	110	10010
	1011	0110	01000

74

smile

Ex d = | | | | | | | | | | | | | | | | | | | | | |

	Index (m)	data	Code word (m+1)
i.c	0000	0	00000
	0001	.1	00011
	0010	11	00111
	0011	111	00101
	0100	1111	00111
	0101	11111	01001
	0110	111111	01011
	0111	1111111	01101
	1000	11111111	01111
	1001	11...1 9 ones	10001
	1010	11...1 10 ones	10011
	1011	11...1 11 ones	10101

* Lossy :-

⇒ Audio :-

row data

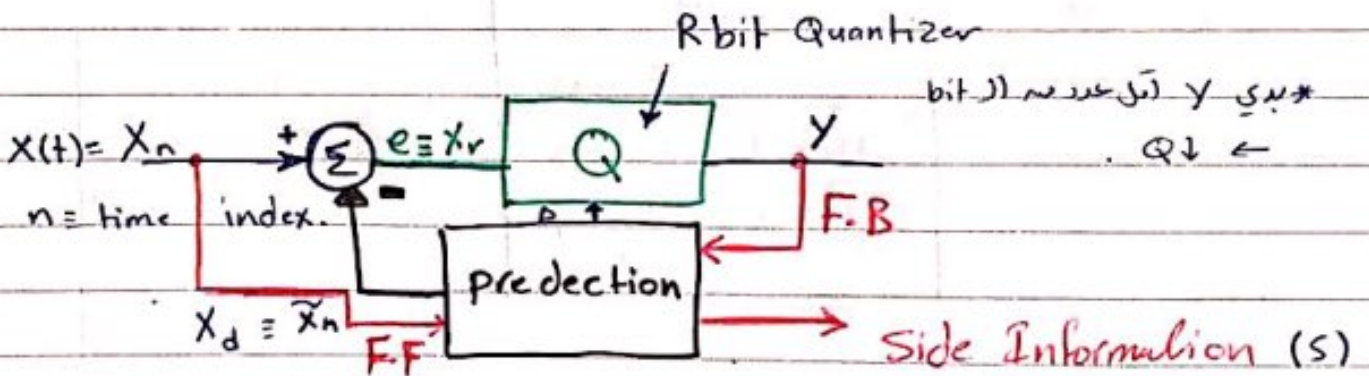
"BW μ s"

$X(t)$

random wave form



$$X(t) = X_d(t) + X_r(t)$$



bit) y \downarrow \leftarrow Q

* $Q \equiv$ Quantization "

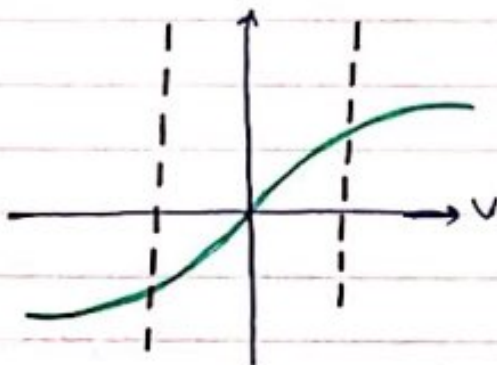
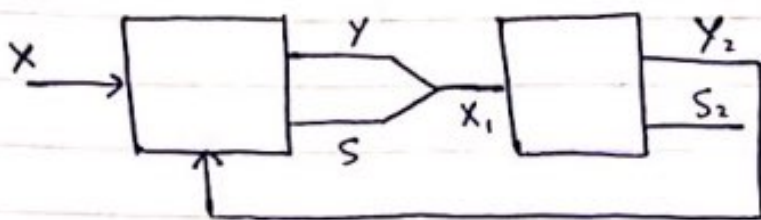
* $\Delta \equiv$ \downarrow Q and Prediction in Δ

F.F \equiv feed forward.

F.B \equiv Feed Back.

* "data = y + side inf."

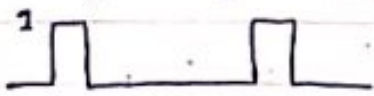
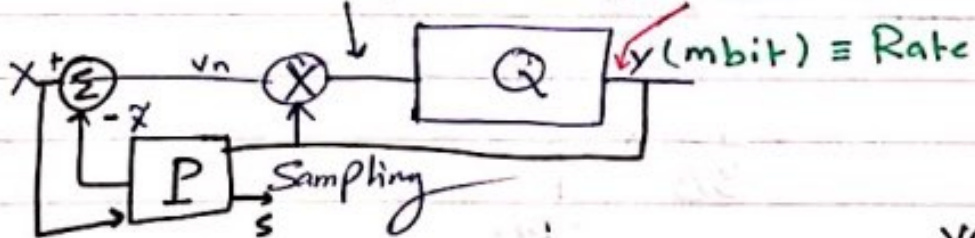
Feed F out performs the Feed Back production



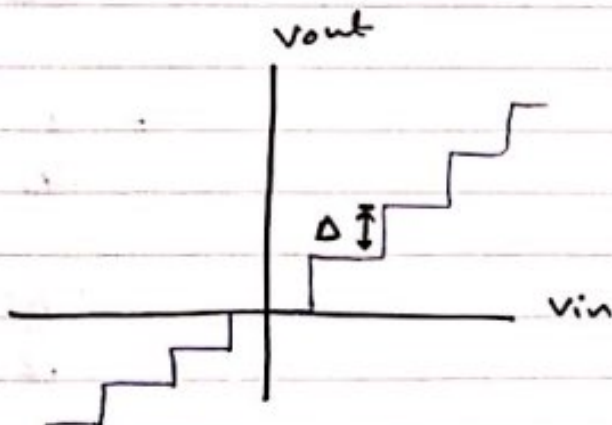
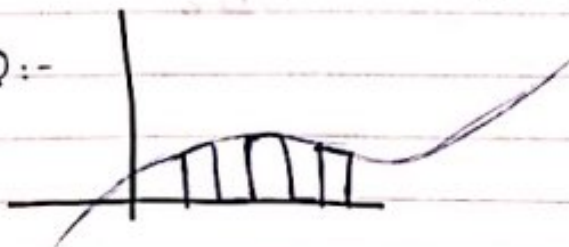
Basic :

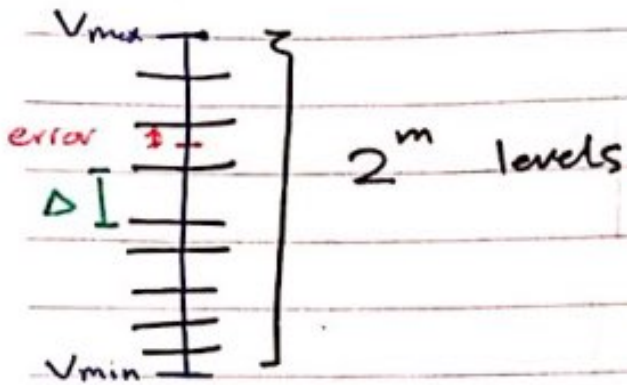
1- A/D :-

Discrete Signal after Q \Rightarrow digital Signal



after Q :-





$\Delta \equiv$ Step size

$$\Delta = \frac{V_{max} - V_{min}}{2^m}$$

uniform Quantizer
 Δ متساوية

mse = $E \{ \text{Error}^2 \}$ = $\int_{-\Delta/2}^{\Delta/2} \frac{1}{\Delta} e^2 de$

↳ mean square error

$$= \frac{1}{3\Delta} e^3 \Big|_{-\Delta/2}^{\Delta/2}$$

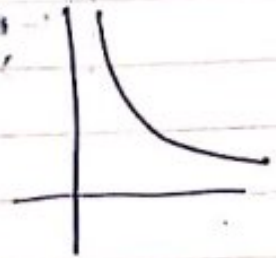
$$= \frac{2}{3\Delta} \left(\frac{\Delta}{2} \right)^3 = \frac{2\Delta^3}{3\Delta \cdot 8}$$

$$= \frac{\Delta^2}{12}$$

$D \equiv$ Distortion.

$$D = \frac{\Delta^2}{12} = \frac{(V_{\max} - V_{\min})^2}{12} \cdot 2^{-2R}$$

$$D_n = \frac{(\overbrace{V_{\max} - V_{\min}}^{\Delta V_{PP}})^2}{12 \sigma_x^2} 2^{-2R_u}$$



$$D_n = \frac{(\overbrace{e_{\max} - e_{\min}}^{\Delta e_{PP}})^2}{12 \sigma_x^2} 2^{-2R_c}$$

σ_x ← variance *
normalized ISI ~ Δe

$$\Delta V_{PP} = 3 \Delta e_{PP} \quad " 3 > 1 "$$

⊕ $\sigma_x \sim 2D \sim 15 \text{ dB}$

$R_c \equiv R$ compressed

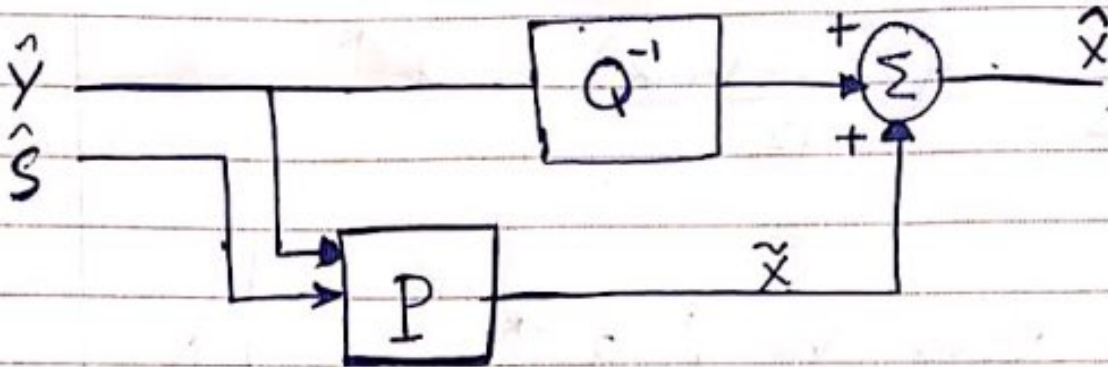
$R_u \equiv R$ uncompressed

$$R_c < R_u$$

* Lossy comes from quantization.

$\Delta \uparrow \rightarrow \text{error} \uparrow \rightarrow \text{Rate} \downarrow$

at RX:-



~~Discrete Time System~~

$S \equiv$ control signal " ~~control signal~~ " ~~لا إشارات~~

$Y \equiv$ row data ("sample")

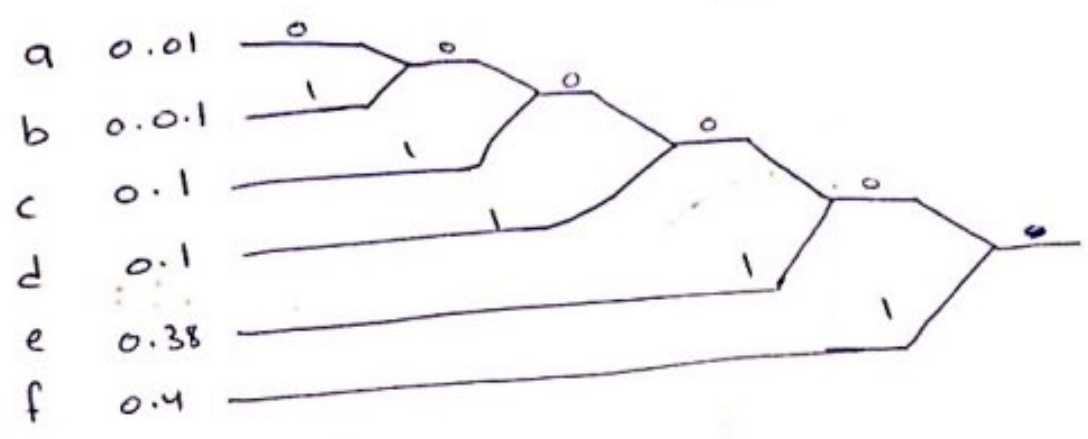
Quiz 3

MON 18/12

Given $\ell = \{a \ b \ c \ d \ e \ f\}$

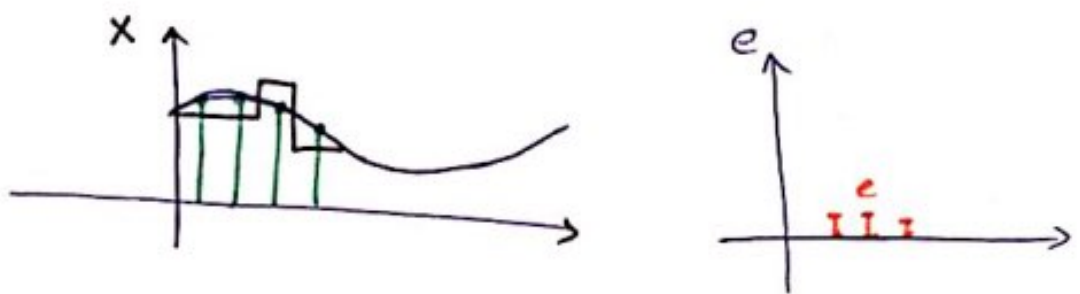
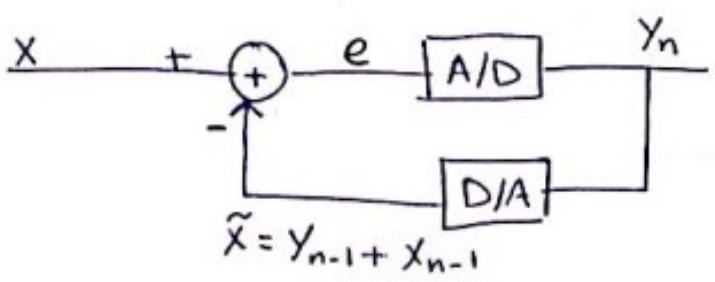
$P = \{0.01, 0.01, 0.1, 0.1, 0.4, 0.38\}$

Find the Huffman code and Rate ?!



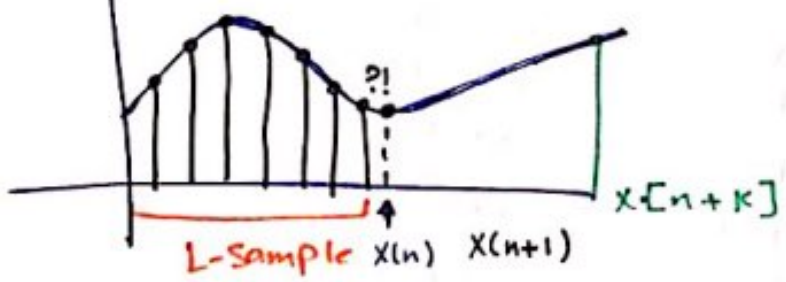
00000	a	5×0.01	$= 0.05$
00001	b	5×0.01	$= 0.05$
0001	c	0.1×4	$= 0.4$
001	d	0.1×3	$= 0.3$
01	e	0.38×2	$= 0.76$
1	f	0.4	0.4
			<hr/>
			1.96

II DPCM Δ



III RPE-LTP Δ
RPE-STP

Long Time Prediction \equiv LTP



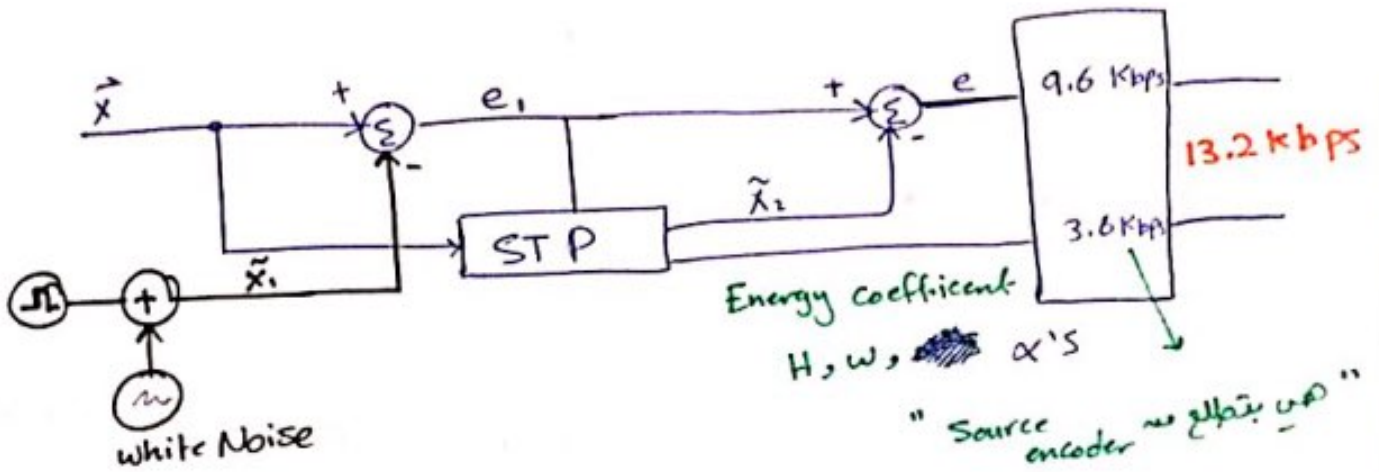
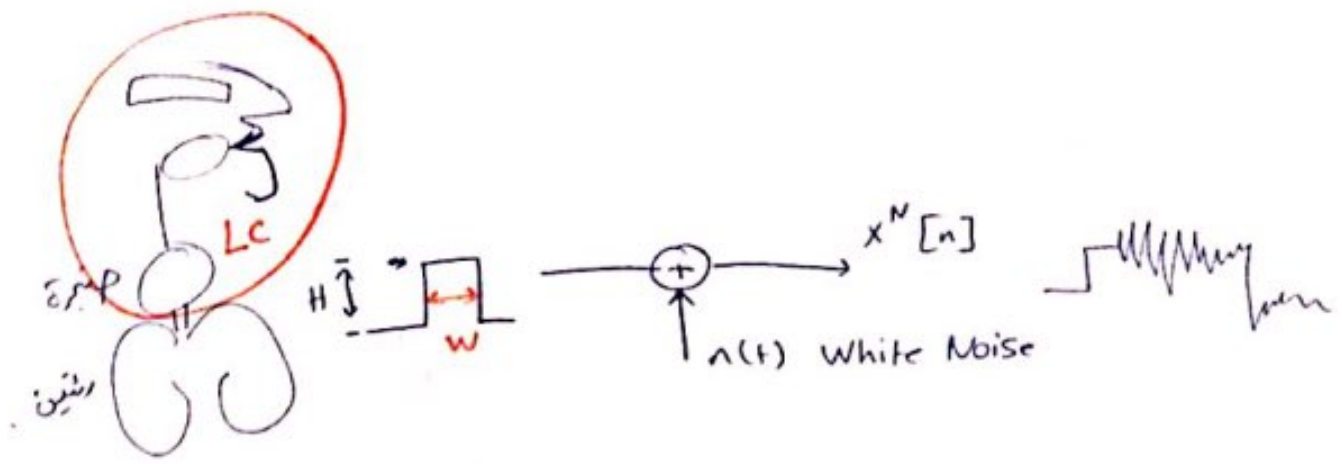
$$x[n+1] = \sum_{i=0}^{L-1} \alpha_i x[n-i] = \alpha^T X$$

$$X = \begin{bmatrix} x_n \\ x_{n-1} \\ x_{n-2} \\ \vdots \\ x_{n-L+1} \end{bmatrix}$$

$$\alpha = \begin{bmatrix} \alpha_0 \\ \alpha_1 \\ \alpha_2 \\ \vdots \\ \alpha_{L-1} \end{bmatrix}$$

$$H[z] = \sum_{i=0}^{L-1} \alpha_i z^{-i}$$

(hi)



length Phoneme
 20ms
 8 K Sample
 (160 Sample)

VO Coder
 "voice"

~~alpha~~

$$\vec{\alpha} = \text{eig}(E\{X X^T\})$$

9.6 K in 1sec \Rightarrow in 20ms = 192 bits

3.6 K in 1sec \Rightarrow in 20ms = 72 bits

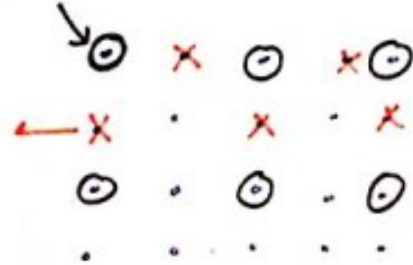
264 bits

+

MP3 84



odd frames



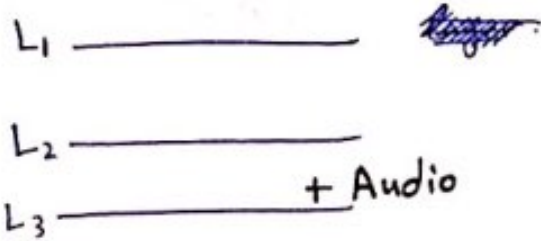
even frame

$$(1920 * 1080) * 15$$

$$31M * 3 = 100M \text{ bytes}$$

$$800 \text{ M bps} \rightarrow 27.5 \text{ Mbps}$$

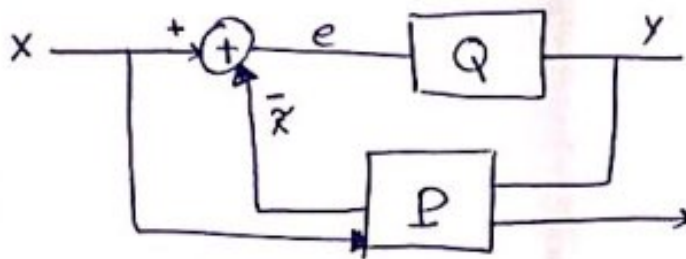
DVB \equiv Digital video broadcasting.



MP3 \equiv M player 3

Quiz 4 Draw the block diagram of general Source Encoder if the Prediction Filter can predict 90% of the input signal
Calculate the compression ratio?!

SOL:



$$(VPP)_e = \frac{10}{100} (VPP)_x$$

$$D_1 = \frac{(VPP)^2}{12 \sigma_x^2} 2^{-2R_1}$$

$$D_2 = 0.01 K 2^{-2R_2}$$

$$\frac{D_1}{D_2} = 1 = 100 \frac{2^{-2R_1}}{2^{-2R_2}}$$

$$2^{-2R_2} = 100 2^{-2R_1}$$

$$-2R_2 = \log_2(100) - 2R_1$$

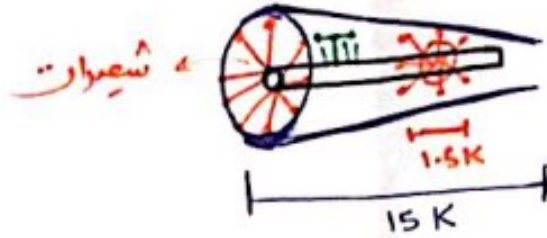
$$R_1 = \frac{1}{2} \log_2(100) + R_2$$

$$R_1 = 3.32 + R_2$$

* MP3:- Audio signal not speak signal.

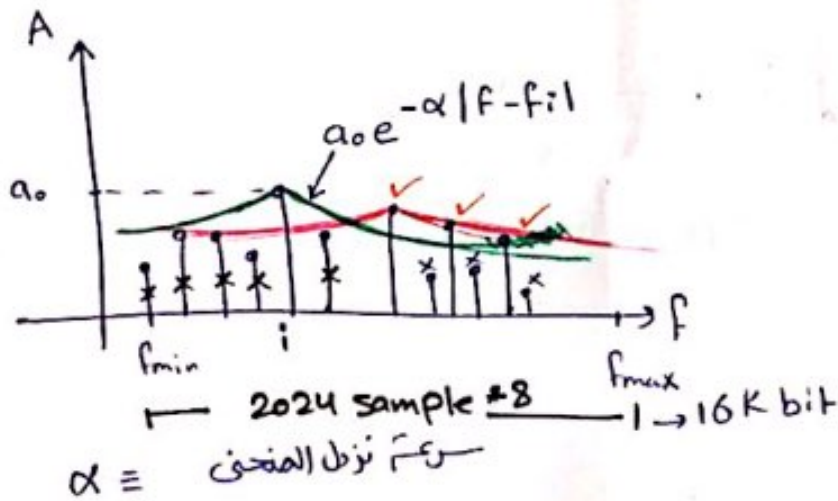
↳ layer 3

* بينج (ع)
 frequency domain
 time في u
 domain
 لنموذج كل سرعة الـ
 طول مختلف



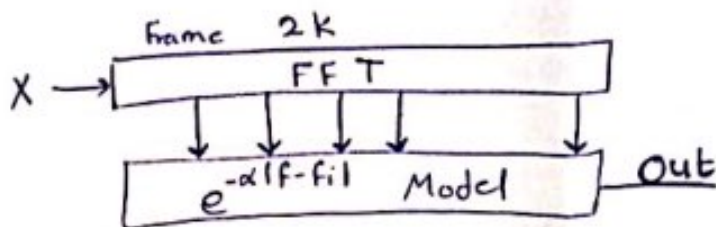
$$1.5K * 15K = 22.5M$$

Psychoacoustic Model #4



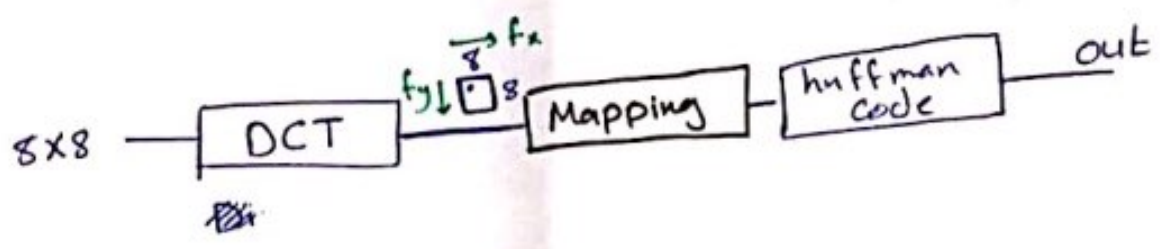
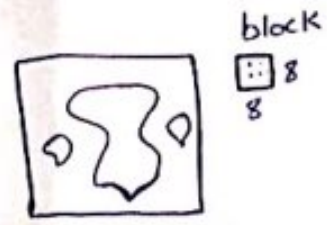
$$20 \uparrow * (11 \text{ bits} + 11) = 420$$

↳ location

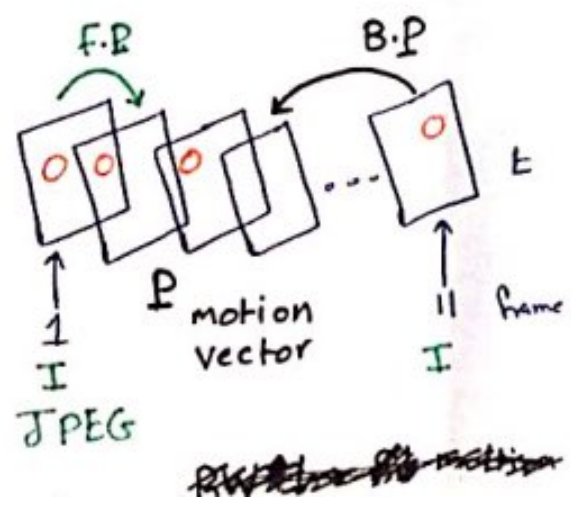
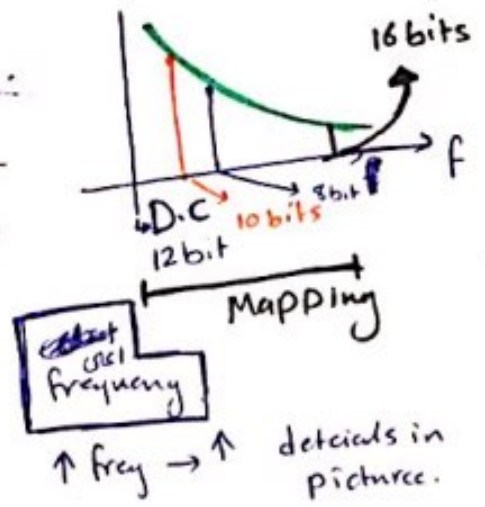
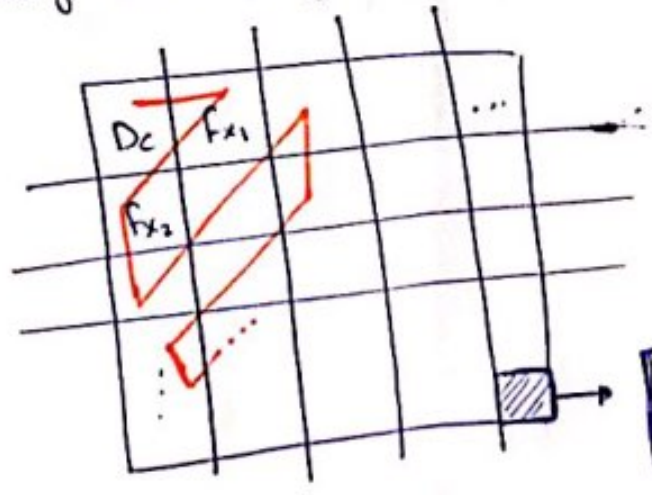


MPEG-2: video compression

JPEG



DCT \equiv Discrete cosine transform
frequency \Rightarrow changing ω



P \equiv Prediction
F \equiv Forward prediction
B.P \equiv Backward "

87

K-L transformer \Rightarrow optimal transformer
and the best transformer.

DCT \Rightarrow fast \Rightarrow FFT and take real part

" The End "