



Electrical Circuits II (EE212)
Sec. Exam. 1st Term, 2015-2016
Dec. 3, 2015. 12:25 – 13:55



Sec.1 (S, T, T, 8-9)
Ziad Al-Khatib

Sec.1 (S, T, T, 10-11)
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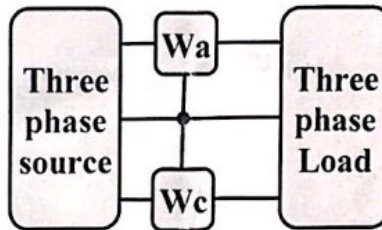
Sec.4 (M, w, 11-12:30)
Moh. Hajahmed

- ☛ Switch off your mobile. No advanced calculators, Tablets or mobile phones are allowed.
- ☛ Hand over your exam sheets with your scratch paper.
- ☛ Show work and write the final answer & units inside the box, to get credit on problems.
- ☛ Answer all problems directly on the exam sheet only.
- ☛ Feel free to use the blank space on the exam sheets for scratch work.
- ☛ Please keep 😊, 👍 & 🙌. Don't 😞, 🤔, ❓, 🙄 & 😡. Take your 🕒 & enjoy yourself.

Q1-(16Pts) Solve each part separately.

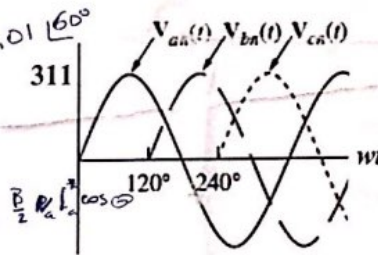
(ABET outcome (a) Assessment)

- The readings of the shown wattmeters are:
- $W_a = 1500 \text{ W}$.
- $W_c = 2200 \text{ W}$. - Determine the:
 - Total active power.
 - Total reactive power.
 - Power Factor.
 - Type of the load, Resistive, Inductive or Capacitive.



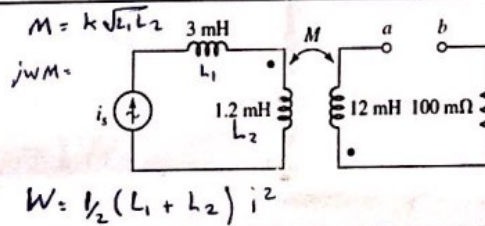
$P_T = 3700 \text{ W}$
 $Q_T = \text{ZERO}$
 $P.F = 1 \text{ unity}$
 $\text{Type} = \text{Resistive load}$

- The shown signals for a three-phase system Y-Y connection.
- $i_a(t) = 7.071 \sin(314t - 60^\circ) \text{ A}$.
- a- Write time-varying $v_{an}(t)$.
- b- Write time-varying $v_{ab}(t)$.
- Then Determine the:
 - c- Total instantaneous power $p(t)$.
 - d- Total average power P .
 - e- Total pulsating (time varying) power $P_{puls}(t)$.



$v_{an}(t) = 311 \sin(314t) \text{ V}$
 $v_{ab}(t) = 519 \sin(314t + 30^\circ) \text{ V}$
 $p(t) = 3298.6255 + 3298.6255 \cos(628t + 60^\circ)$
 $P = 3298.6255 \text{ W}$
 $P_{puls}(t) = \text{ZERO}$

- In the circuit, $k=0.75$, if $i_s(t) = 10 \cos(200t) \text{ A}$.
- Determine the:
 - a- Mutual Inductance M .
 - b- V_{ab} voltage $v_{ab}(t)$.
 - c- Max. stored energy W .



$M = j0.0623 \mu\text{H}$
 $v_{ab}(t) = \text{ZERO}$
 $W = 0.21 \text{ J}$

- In the circuit, $V_s = 220 \text{ Vrms}$.
- Find the:
 - Input impedance seen by the source Z_{in} , I_1 , V_1 , I_2 , V_2 , V_{ab} , and the total dissipated power P_T .

$Z_R = \frac{Z_L}{n^2}$

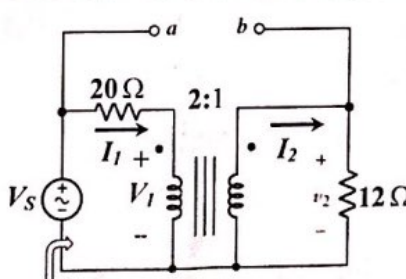
$Z_{in} = Z_L + Z_R$

$I_1 = n I_2$

$V_2 = n V_1$

$I_1 = \frac{Z_{in}}{V_s} = \frac{Z_{in}}{220}$

$P = I_1^2 Z_{in}$



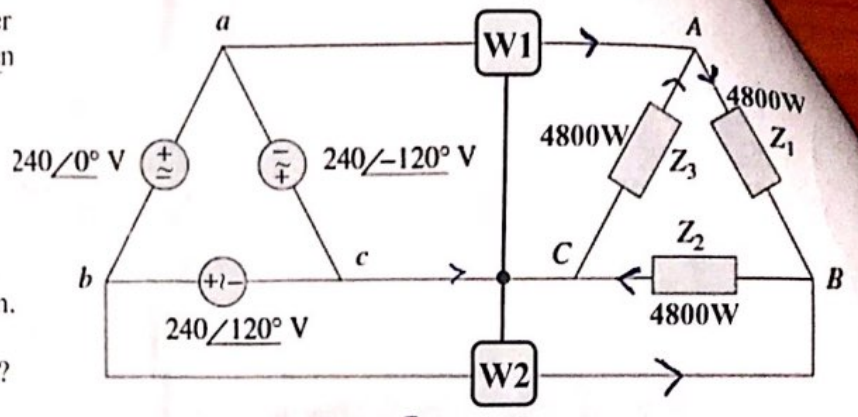
$Z_{in} = 68 \Omega$
 $I_1 = 3.235 \text{ A (rms)}$
 $V_1 = 220 \text{ Vrms}$
 $I_2 = 6.47 \text{ A (rms)}$
 $V_2 = 110 \text{ Vrms}$
 $V_{ab} = \text{ZERO}$
 $P_T = 711.633 \text{ W}$

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Q2-(SP1) I- In the circuit shown, consider a balanced 3-phase system, given voltage in rms, $Z_1=Z_2=Z_3=R$.

Determine the:

- a- R.
- b- I_{AB} , I_{BC} , and I_{CA} .
- c- I_{aA} , I_{bB} , I_{cC} .
- d- Wattmeter reading of: W1, W2.
- e- Type of element for PF correction.
- f- Is the reading of (W1 + W2) equals to the total power? Why?



$$4800 = \frac{V^2}{R}$$

$$R = \frac{V^2}{P} = \frac{(240)^2}{4800} = 12 \Omega$$

Since it's Δ -connection Phase & line voltage are Equal

$$I_{AB} = \frac{V_L}{Z_1} = \frac{240 \angle 0^\circ}{12} = 20 A$$

$$I_{BC} = \frac{240 \angle 120^\circ}{12} = 20 \angle 120^\circ$$

$$I_{CA} = \frac{240 \angle -120^\circ}{12} = 20 \angle -120^\circ$$

$$I_{aA} = I_{AB} + I_{bB}$$

$$I_{aA} = I_{AB} - I_{CA}$$

$$I_{bB} = I_{BC} - I_{AB}$$

$$I_{cC} = I_{CA} - I_{BC}$$

$$W_1 = V_{ac} * I_{aA}$$

$$W_2 = V_{bc} * I_{bB}$$

$$R = 12 \Omega$$

$$I_{AB} = 20 \angle 0^\circ A$$

$$I_{BC} = 20 \angle 120^\circ A$$

$$I_{CA} = 20 \angle -120^\circ A$$

$$I_{aA} = 34.64 \angle 30^\circ A$$

$$I_{bB} = 34.64 \angle 150^\circ A$$

$$I_{cC} = 34.64 \angle -90^\circ A$$

$$W_1 = 8313.6 \text{ W}$$

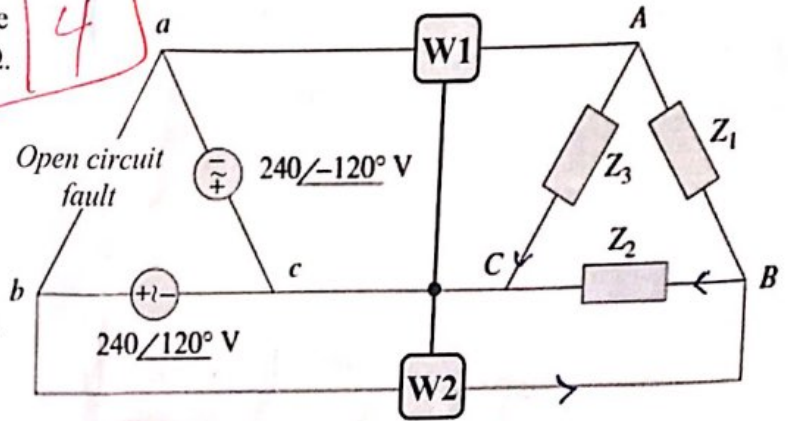
$$W_2 = 8313.6 \text{ W}$$

Type: No NEED

f- Yes, because it's a Balanced System

Q2-(8Pts) II- In the circuit shown, the voltage in rms, assume $Z_1=Z_2=Z_3=R=12\Omega$. Consider an open circuit fault at source ab (V_{ab} opened).

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Determine the:

- I_{AB} , I_{BC} , and I_{CA} .
- I_{aA} , I_{bB} , and I_{cC} .
- Wattmeter reading of: W1, W2.
- System is balanced or Unbalanced.
- What is the advantage of the DELTA connection source?

$$\bar{I}_{CA} = \frac{240 \angle 120^\circ}{12}$$

$$\bar{I}_{BC} = \frac{240 \angle 120^\circ}{12} = 20 \angle 120^\circ$$

⊥

$$I_{aA} = I_{AC}$$

$$I_{bB} = I_{BC}$$

$$I_{cC} = I_{BC} + I_{CA}$$

$$W_1 = V_{ac} * I_{cC}$$

$$W_2 = V_{bc} * I_{bB}$$

$$I_{AB} = \text{ZERO}$$

$$I_{BC} = 20 \angle 120^\circ \text{ A}$$

$$I_{CA} = 20 \angle 120^\circ \text{ A}$$

$$I_{aA} = 20 \angle 60^\circ$$

$$I_{bB} = 20 \angle 120^\circ$$

$$I_{cC} = 20 \angle 180^\circ$$

$$W_1 = 4800$$

$$W_2 = 4800$$

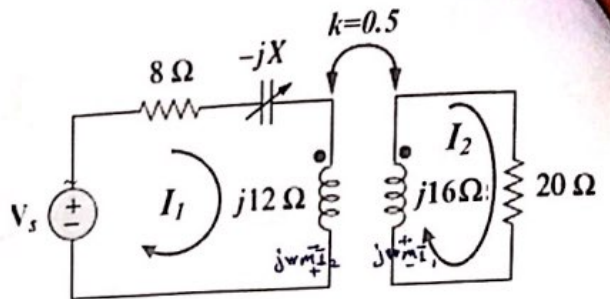
d- Unbalanced

e-

the total Power remains the Same even if there is a Voltage Source turned off

Q3-(12Pts) In the shown circuit, $V_s = 100$ Vrms.

- Find the mutual impedance ($j\omega M$).
- Write the mesh current equations in **matrix** form.
- Draw and label the T equivalent circuit **only** for the coupled coils.
- Find the value of X that will give maximum power transfer to the 20Ω load.
- Find I_1 and I_2 .



a- ~~$M = k \sqrt{L_1 L_2}$~~
 $M = k \sqrt{L_1 L_2}$
 $= 0.5 \sqrt{j12 \times j16} =$

b- mesh ① $100 = 8\bar{I}_1 - jX\bar{I}_1 + j12\bar{I}_1 - j6.928\bar{I}_2$

$(8 - jX + j12)\bar{I}_1 - (j6.928)\bar{I}_2 = 100$

mesh ② $-j6.928\bar{I}_1 + (20 + j16)\bar{I}_2 = 0$

e- $\Delta = (160 + 128i) - -47.99 =$

$= 208 - 128i$
 $\Delta_1 = (2000 + 1600i)$

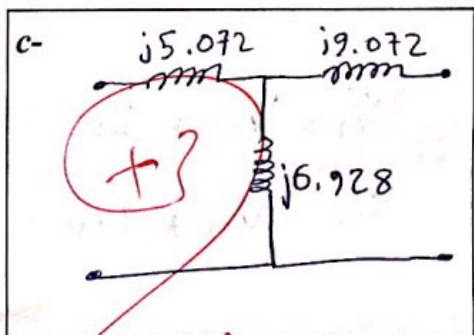
$\Delta_2 = (j692.8)$

$\bar{I}_1 = \frac{\Delta_1}{\Delta} = \frac{2000 + j1600}{208 - 128i} = 10.49$

$\bar{I}_2 = \frac{\Delta_2}{\Delta} = \frac{j692.8}{208 - 128i}$

a- $j\omega M = j6.928 \Omega$

b-
$$\begin{bmatrix} 8 - jX + j12 & -j6.928 \\ -j6.928 & 20 + j16 \end{bmatrix} \begin{bmatrix} \bar{I}_1 \\ \bar{I}_2 \end{bmatrix} = \begin{bmatrix} 100 \\ 0 \end{bmatrix}$$



d- $X = -j12$

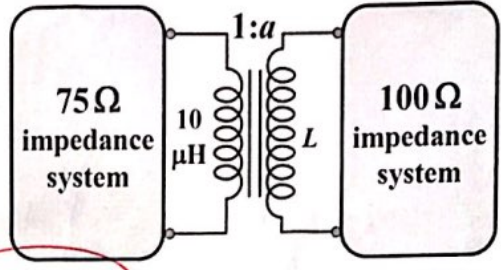
e- $\bar{I}_1 = 10.487 \angle 70.26^\circ \text{ A}$
 $\bar{I}_2 = 2.836 \angle 121.6^\circ \text{ A}$

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Q4-(6Pts) I- A transformer is used to match the different impedance systems with each others. A computer/electrical/mechatronics engineer want to couple a coaxial cable with BNC socket to UTP cable with RJ-45 socket as shown in the figure, the used transformer is an **ideal**, **determine** the:



- a- Required turns ratio (a) for maximum energy power transfer.
- b- Inductance L value in 100-ohm side.



Handwritten notes for Q4-I:

$$Z_R = \sqrt{L/n^2}$$

$$\frac{Z_2}{Z_1} = n^2$$

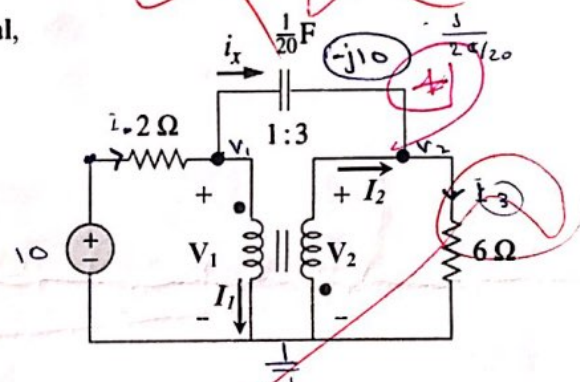
$$\frac{L_2}{L_1} = 2$$

a- $a = 1.547$

b- $L = j19.47$

Q4-(10Pts) II- In the shown circuit, the transformer is an **ideal**, $v_s(t) = 10 \cos(2t)$ V. **determine** the following:

- a- Primary voltage and current V_1, I_1 .
- b- Secondary voltage and current V_2, I_2 .
- c- Feedback current i_x .



Handwritten mesh equations for Q4-II:

$$\frac{10 - V_1}{2} = I_1 \quad \text{--- (1)}$$

$$\frac{V_1 - V_2}{-j10} = i_x \quad \text{--- (2)}$$

$$\frac{V_2}{6} = I_3 \quad \text{--- (3)}$$

Handwritten transformer relationships:

$$V_2 = 3V_1$$

$$I_1 = 3I_2$$

a- $V_1 =$
 $I_1 =$

b- $V_2 =$
 $I_2 =$

c- $i_x =$

Handwritten mesh equations with circled 'X' marks:

mesh 1: $10 = 2I_1 + V_1$

mesh 2: $+V_1 = -j10 I_x + V_2$

mesh 3: $V_2 = 6 I_2$