| 0907231 Digital Logic | Mi |
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| 5 Problems, 8 Pages Solution | 7 |

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| Your Name: | Sample Solution | |
|-----------------------|-----------------------|---|
| Your Student ID: | | |
| Your Instructor Name: | | _ |
| Your Section #: | ; Your Lecture Times: | |

Read The Following Instructions Carefully:

- 1. Write your name, ID, date and sign the attached Honor Pledge. <u>Your exam</u> will NOT be graded if you do not.
- 2. This exam booklet has 6 numbered pages and 5 problems. Check that your exam includes all 6 pages. Show ALL of your work on these pages. Two blank pages are added at the end for your scratch work.
- 3. WRITE your name (in Arabic) and student number in the spaces above. Also, make sure to write your instructor's name, section # and lecture times.
- 4. You are NOT permitted to use notes, books, calculators, or mobile phones during this exam.
- 5. This exam lasts for 75 minutes. Point values are listed for each problem to assist you in best using your time.

| Problem | Max Points | Score |
|---------|------------|-------|
| 1 | 16 | |
| 2 | 10 | |
| 3 | 24 | |
| 4 | 24 | |
| 5 | 26 | |
| Total | 100 | |

Problem 1. (16 points)

A. (7 points) Perform each of the following conversions. Write your answers in the boxes at the right edge.

(i)
$$101011001_2 = 2^8 + 2^6 + 2^4 + 2^3 + 2^0 = 256 + 64 + 16 + 8 + 1 = 345_{10}$$

(ii) **218**₁₀ = 128 + 64 + 16 + 8 + 2 =
$$2^7 + 2^6 + 2^4 + 2^3 + 2^1 = 11011010_2$$

(iii)
$$11010101_2 = 011\ 010\ 101_2 = 325_8$$

(iv)
$$574_8 = 5x8^2 + 7x8^1 + 4x8^0 = 5x64 + 7x8 + 4x1 = 320 + 56 + 4 = 380_{10}$$

(v)
$$6B4_{16} = 0110\ 1011\ 0100_2 = 110101110100_2$$

(vi)
$$762_{10} = 2x256 + 15x16 + 10 = 2x16^2 + 15x16^1 + 10x16^0 = 2FA_{16}$$

(vii) $CA75_{16} = 1100\ 1010\ 0111\ 0101_2 = 001\ 100\ 101\ 001\ 110\ 101_2 = 145165_8$

B. (9 points) In the blank in front of each expression in the left hand column, write the letter (P - Z) corresponding to the equivalent expression in the right hand column. Not all answers in the right hand column will be used and some may be used more than once.

(i)
$$(A + \overline{B})(\overline{A} + C)(\overline{B} + \overline{C}) = (A\overline{A} + AC + BA + BC)(\overline{B} + C)$$

(i)
$$S: = AC\overline{B} + AC\overline{C} + \overline{B}A\overline{B} + \overline{B}A\overline{C} + \overline{B}C\overline{B} + \overline{B}C\overline{C}$$

$$= A\overline{B}C + A\overline{B} + A\overline{B}\overline{C} + \overline{B}C = A\overline{B}(C + 1 + \overline{C}) + \overline{B}C = A\overline{B} + \overline{B}C$$

(ii) R:
$$\overline{A + \overline{C}} + \overline{\overline{B} + (D + \overline{A})} = \overline{A} \cdot \overline{\overline{C}} + \overline{\overline{B}} \cdot (\overline{D + \overline{A}}) = \overline{A}C + B(\overline{D} \cdot \overline{\overline{A}}) = \overline{A}C + AB\overline{D}$$

(iii) U:
$$=\overline{AB} + \overline{A} \cdot \overline{C} + \overline{A} \cdot \overline{D} + \overline{C} \cdot D \cdot B + \overline{C} \cdot D \cdot \overline{C} + \overline{C} \cdot D \cdot \overline{D}$$
$$=\overline{A} \cdot B + \overline{A} \cdot \overline{C} + \overline{A} \cdot \overline{D} + \overline{C} \cdot D \cdot B + \overline{C} \cdot D \cdot \overline{C} + \overline{C} \cdot D \cdot \overline{D}$$
$$=\overline{A} \cdot B + \overline{A} \cdot \overline{C} + \overline{A} \cdot \overline{D} + \overline{C} \cdot D \cdot (B+1) = \overline{A} \cdot B + \overline{A} \cdot \overline{C} + \overline{A} \cdot \overline{D} + \overline{C} \cdot D$$

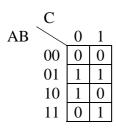
Problem 2. (10 points)

A. (4 points) Given $F(A, B, C) = \Sigma m (1, 3, 4, 5, 7)$, express the function in <u>algebraic</u> sum-of-minterm and product-of-maxterm form.

$$F(A, B, C) = \underline{\overline{A} \cdot \overline{B} \cdot C + \overline{A} \cdot B \cdot C + A \cdot \overline{B} \cdot \overline{C} + A \cdot \overline{B} \cdot C + A \cdot B \cdot C}$$
(sum-of-minterms)

$$F(A, B, C) = \frac{(A + B + C)(A + \overline{B} + C)(\overline{A} + \overline{B} + C)}{(\text{product-of-maxterms})}$$

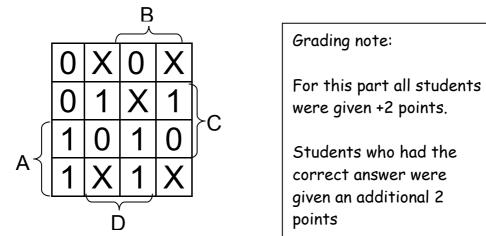
B. (4 points) Given the function **G**(**A**, **B**, **C**) defined by the Karnaugh map below, complete the truth table and the short-hand SOP and POS expressions for this function.



| А | В | С | G |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

C. (2 points) Complete the Karnaugh map for

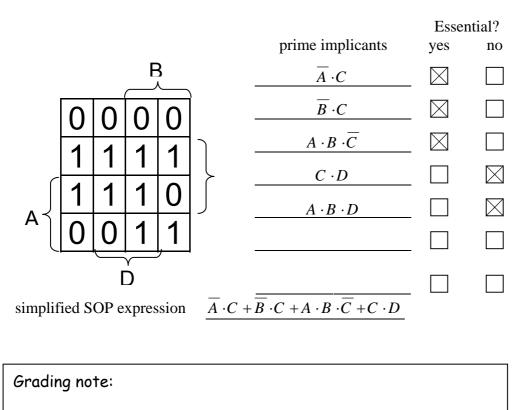
 $H(A, B, C, D) = \Pi M (0, 2, 5, 11, 14) + d(1, 4, 7, 9, 12)$



Problem 3 (24 points)

For the follow expression, derive a simplified *sum of products* expression using a Karnaugh Map. List the prime implicants, indicating which are essential.

$$F(A,B,C,D) = \overline{A} \cdot C \cdot D + A \cdot B \cdot D + \overline{B} \cdot C + \overline{A} \cdot C \cdot \overline{D} + A \cdot B \cdot \overline{C} \cdot \overline{D}$$



For each correct prime implicant: +1

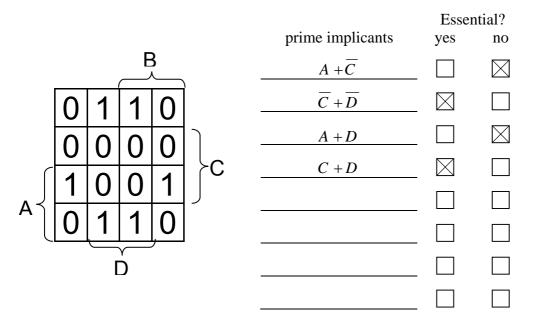
For each correct yes/no: +1

For each incorrect prime implicant: -1

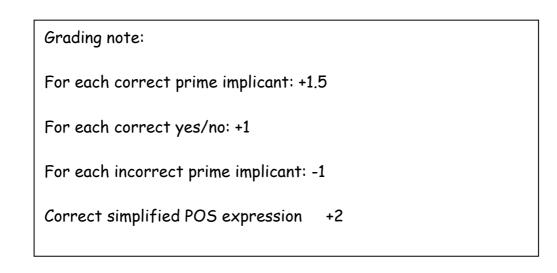
Correct simplified SOP expression +2

B. (12 points) For the follow expression, derive a simplified *product of sums* expression using a Karnaugh Map. List the prime implicants, indicating which are essential.

$$F(A,B,C,D) = (\overline{A} + \overline{B} + C + D) \cdot (\overline{A} + \overline{C} + \overline{D}) \cdot (A + C + D) \cdot (A + \overline{C}) \cdot (B + C + D)$$

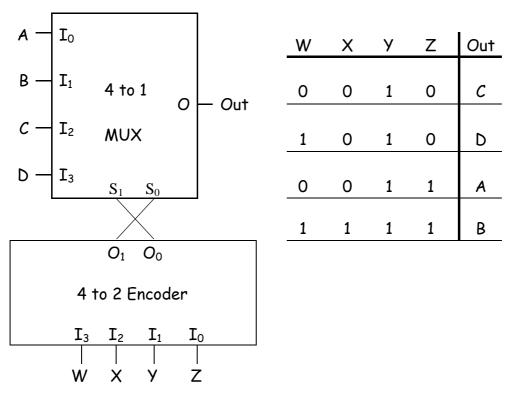


simplified POS expression: $(C+D) \cdot (\overline{C}+\overline{D})(A+\overline{C})$ or $(C+D) \cdot (\overline{C}+\overline{D}) \cdot (A+D)$

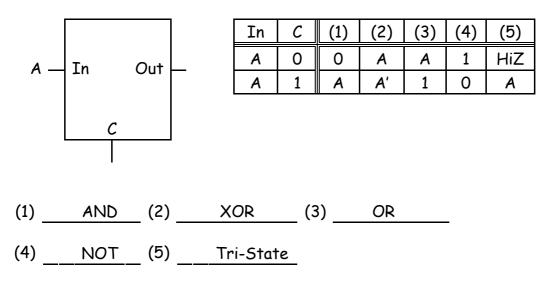


Problem 4 (24 points)

A. (14 points) Consider the following circuit below. Assume the encoder has the following input priority: $I_2 > I_0 > I_3 > I_1$. Determine Out for the following Input patterns.



B. (10 points) Consider five possible definitions for the block below left. One block input is the symbolic value A. The other input, C is a control value. The output behavior for each of the five definitions is given. Give the *logical (gate) name* for each definition. Note that A' means **not** A.



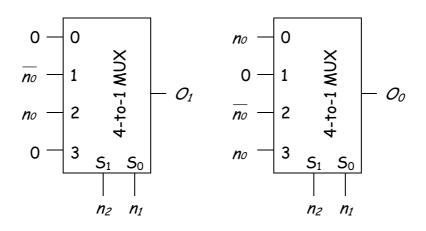
Problem 5 (26 points)

Design a combinational circuit that takes a 3-bit binary number $n = (n_2 n_1 n_0)$ and computes its "modulo 3", i.e., the remainder from n/3 operation. Assume that complemented inputs are available.

A. (6 points) Build the truth table.

| n 2 | <i>n</i> 1 | n _o | \mathcal{O}_1 | \mathcal{O}_{O} |
|------------|------------|----------------|-----------------|-------------------|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 |

B. (10 points) Design the circuit using the minimum number of 4-to-1 multiplexers



C. (10 points) Design the circuit using the minimum number of 2-to-4 decoders with enable and gates.

