

Q # 1 (8)	Q # 2 (14)	*Q # 3 (34) c	Q # 4 (12)	Q # 5 (22)	GRADE
3	14	33	12	22	84 / 90

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Question # 1 (8 points) Show Your Calculations

A 132/11 kV, 10 MVA Δ-Y 3-phase transformer is protected by restricted earth fault protection scheme at the Y-side. The percentage of LV winding protected against phase to ground fault is 85%. The relay setting is such that it trips for 20% out of balance. Calculate:

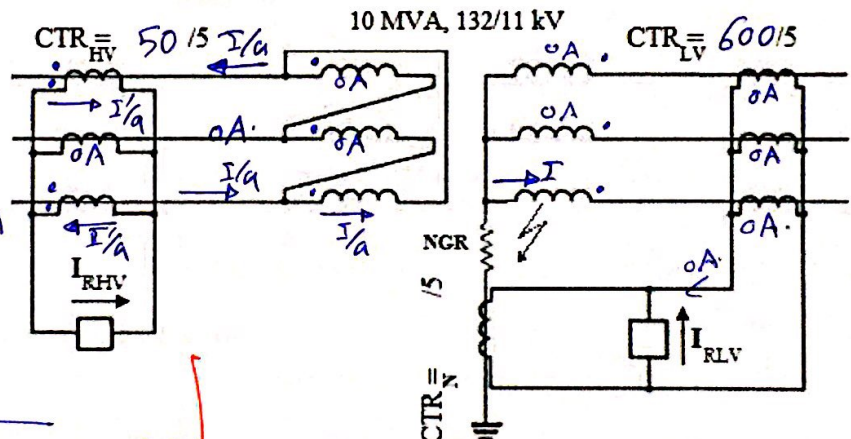
a.	the appropriate CTR_{HV} , CTR_{LV} and CTR_N .	$CTR_{HV} =$	50/5 ✓
		$CTR_{LV} =$	600/5 ✓
		$CTR_N =$	600/5 ✓
b.	the relay pick up current I_{pickup} (primary and secondary levels).	$I_{pickup-primary} =$	18.25 A ✓
		$I_{pickup-secondary} =$	446.131 A ✓
c.	the corresponding relay currents I_{RLV} and I_{RHV} .	$I_{RLV} =$	3.72 A ✓
		$I_{RHV} =$	1.825 A ✓
d.	the neutral grounding resistance (NGR) to be added in the neutral to ground connection.	$NGR =$	12.1 Ω ✓

$x = 0.85$

$$I_{HV} = \frac{10 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 43.74 \text{ A}$$

$$I_{LV} = \frac{10 \times 10^6}{\sqrt{3} \times 11 \times 10^3} = 524.86 \text{ A}$$

$CTR_{HV} = 50/5$
 $CTR_{LV} = 600/5$



CTR_N should read for 524.86 A.
 So also choose $CTR_N = 600/5$

$$I_{pickup-primary} = \frac{I}{a} \Rightarrow a = \frac{132}{11/\sqrt{3}} = 20.78$$

So $I_{pickup-primary} = (0.85) \times \frac{1}{20.78} \times 446.131$
 $= 18.25 \text{ A}$

$I = (0.85) I_{LV}$
 $= 0.85 \times 524.86$
 $I = 446.131 \text{ A}$
 pickup on the secondary.

$I_{RLV} = \frac{446.131}{600} \Rightarrow I_{RLV} = 3.72 \text{ A}$
 $I_{RHV} = \frac{18.25}{50} \Rightarrow I_{RHV} = 1.825 \text{ A}$

* for NGR:
 $NGR \Rightarrow I = \frac{x V_{sec}}{NGR}$
 $NGR = \frac{(0.85) \times 11000/\sqrt{3}}{446.131}$
 $\Rightarrow NGR = 12.1 \Omega$

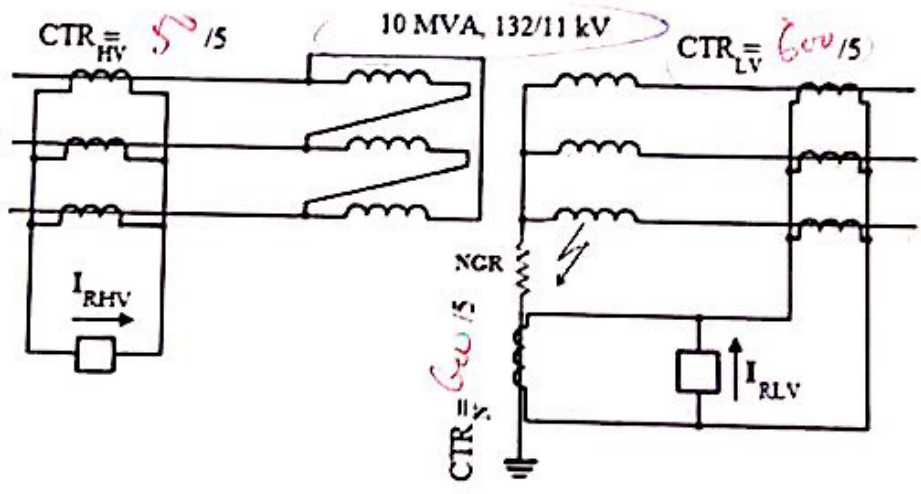
Q#1(8)	Q#2(14)	Q#3(34)	Q#4(12)	Q#5(12)	GRADE
					90/90

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Question # 1 (8 points) Show Your Calculations

A 132/11 kV, 10 MVA Δ-Y 3-phase transformer is protected by restricted earth fault protection scheme at the Y-side. The percentage of LV winding protected against phase to ground fault is 85%. The relay setting is such that it trips for 20% out of balance. Calculate:

a.	the appropriate CTR_{HV} , CTR_{LV} and CTR_N .	$CTR_{HV} = 50/5$	
		$CTR_{LV} = 600/5$	
		$CTR_N = 600/5$	
b.	the relay pick up current I_{pickup} (primary and secondary levels).	$I_{pickup-primary} = 104.9$	A
		$I_{pickup-secondary} = 0.874$	A
c.	the corresponding relay currents I_{RLV} and I_{RHV} .	$I_{RLV} = 0.874$	A
		$I_{RHV} = 0.0$	A
d.	the neutral grounding resistance (NGR) to be added in the neutral to ground connection.	$NGR = 9.08$	Ω



Solution:

$$I_{HV} = \frac{10 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 43.7 \text{ A}, \quad I_{LV} = \frac{10 \times 10^6}{\sqrt{3} \times 11 \times 10^3} = 524.4 \text{ A}$$

$$CTR_{HV} = 50/5 \quad CTR_{LV} = 600/5 \quad CTR_N = 600/5$$

$$I_{pickup-primary} = 0.2 \times 524.4 \Rightarrow I_{pickup} = 104.9 \text{ A} \quad I_{pickup-secondary} = \frac{104.9}{600/5} = 0.874 \text{ A}$$

$$I_{RLV} = \frac{104.9}{600/5} = 0.874 \text{ A} \quad I_{RHV} = 0.0 \text{ A}$$

$$x = \frac{R \times I_p}{V_{ph}} \Rightarrow 1 - 0.85 = \frac{R \times 104.9}{11000/\sqrt{3}} \Rightarrow R = \frac{0.15 \times 6350.9}{104.9} \Rightarrow R = 9.08 \Omega$$

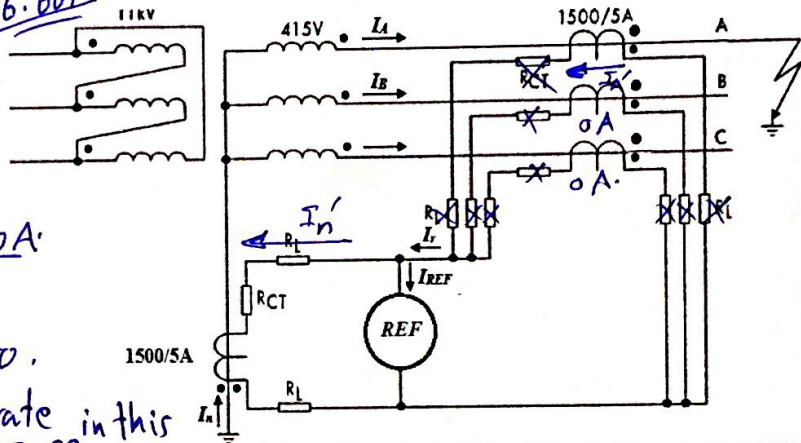
Question # 2 (14 points) Show Your Calculations

An 11kV/415V, 1MVA 3-phase transformer is protected by a restricted earth fault (REF) relay which is connected as shown in the diagram below. Assume that the CT resistances R_{CT} and the connecting lead resistances, R_L , can be neglected. Answer the following parts to this question:

a.	i. For a LG fault from terminal A to earth of 2000 A fault current, find the CTs secondary phasor currents , residual current, neutral current, and the resultant current in the REF relay I_{REF} .	$I'_A =$	6.667	A
		$I'_B =$	0	A
		$I'_C =$	0	A
		$I_r =$	6.667	A
		$I_n =$	6.667	A
		$I_{REF} =$	0	A
ii. State if the relay should operate or not.		Yes	<input checked="" type="radio"/> No	

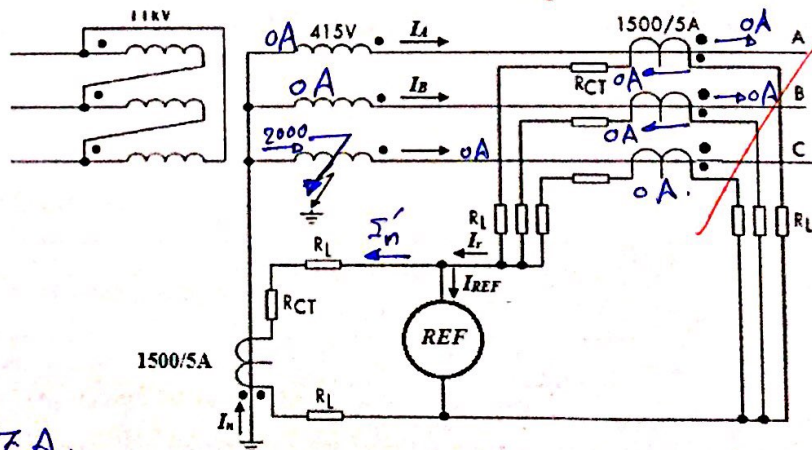
$I_A = 2000 \text{ A} \Rightarrow I'_A = \frac{2000}{\frac{1500}{5}} = 6.667 \text{ A}$
 $I_B = 0 \Rightarrow I'_B = 0$
 $I_C = 0 \Rightarrow I'_C = 0$

$I_r = I'_A = 6.667 \text{ A}$
 $I_n = 6.667 \times \frac{1500}{5} = 2000 \text{ A}$
 $I'_n = 6.667 \text{ A}$
 $I_{REF} = I_r - I'_n = \text{Zero}$
 it won't operate in this case.



b.	i. Assume a fault of 2000 A fault current develops from the middle parts of the phase winding C of the transformer to the transformer core which is connected to earth, find the CTs secondary phasor currents , residual current, neutral current, and the resultant current in the REF relay I_{REF} .	$I'_A =$	0	A
		$I'_B =$	0	A
		$I'_C =$	0	A
		$I_r =$	0	A
		$I_n =$	6.667	A
		$I_{REF} =$	-6.667	A
ii. State if the relay should operate or not.		<input checked="" type="radio"/> Yes	No	

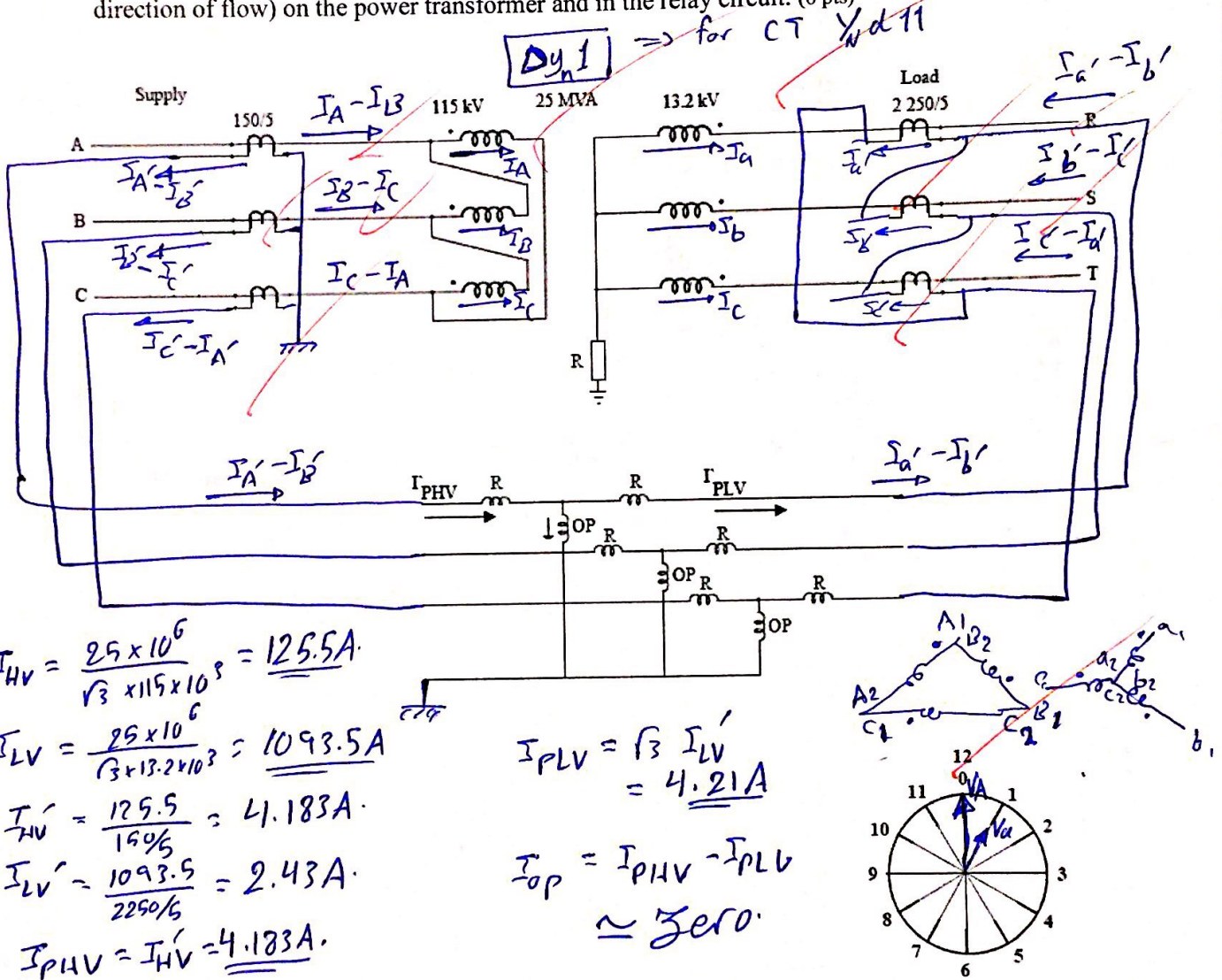
$I'_A = I'_B = I'_C = 0$
 $I_r = I'_A + I'_B + I'_C = 0$
 $I'_n = -I_{REF}$
 $I_n = 2000 \text{ A}$
 so $I'_n = \frac{2000}{\frac{1500}{5}} = 6.667 \text{ A}$
 $I_{REF} = -6.667 \text{ A}$



Question # 3 (34 points) ABET outcome "c" Assessment Show Your Calculations

In the figure below, an incomplete schematic diagram of a protection arrangement for a 25 MVA, 115/13.2 kV Δ-Y connected power transformer is shown. Current transformers (CT) ratio is 150/5 on the 115 kV side and 2250/5 on the 13.2 kV side.

- Identify the vector group of the Δ-Y connected transformer. (4pts)
- Complete the three-phase wiring connection from current transformers to the differential relay. (9 pts)
- Indicate on your completed schematic diagram the current distribution (both magnitude and direction of flow) on the power transformer and in the relay circuit. (6 pts)



- Calculate for full-load condition (7 pts)

Item	115 kV Δ-Side	13.2 kV Y-Side
i. the transformer HV and LV line currents (I_{HV} and I_{LV}) at both sides.	$I_{HV} = 125.5$ A	$I_{LV} = 1093.5$ A
ii. the CT secondary phase currents I'_{HV} and I'_{LV} .	$I'_{HV} = 4.183$ A	$I'_{LV} = 2.43$ A
iii. the pilot wire currents I_{PHV} and I_{PLV} on both left- and right-hand sides of the relay.	$I'_{PHV} = 4.183$ A	$I'_{PLV} = 4.21$ A
iv. the operating current I'_{OP}	$I'_{OP} = 0$	A

e. A single-phase to earth fault at the middle of the LV winding, as indicated in the figure shown below, has resulted in a fault current of 548.7 A. The differential relay is set to operate at 5% of the CT rating. Calculate (8 pts)

i.	the relay secondary pickup current, $I_{pickup-sec}$	$I_{pickup-sec} =$	<u>0.6</u>	A
ii.	the relay operating current, I_{Rop}	$I_{Rop} =$	<u>0.6</u>	A
iii.	state whether this earth fault could cause the relay to operate.		<u>Yes</u>	No

$$a = \frac{115}{13.2/\sqrt{3}} = 15.09$$

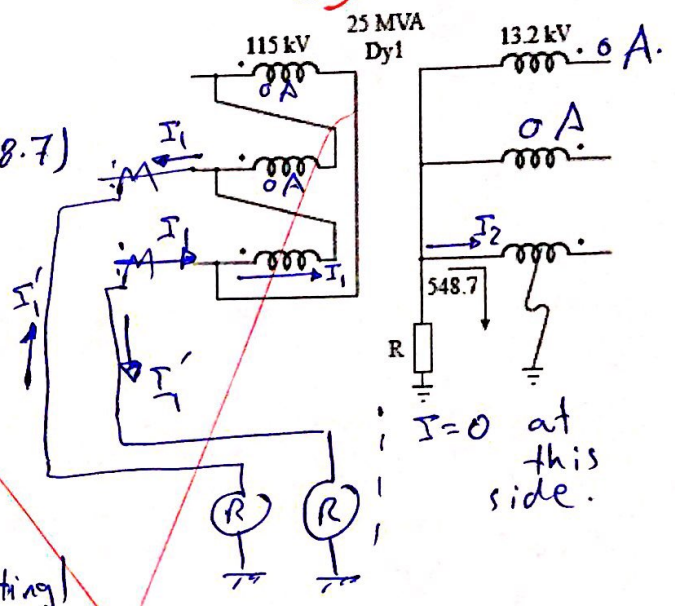
$$I_1 = \frac{I_2}{a} \times \frac{1}{2} = \frac{0.066}{2} \times (548.7) = 18.2 A$$

$$I_1' = \frac{18.2}{\frac{150}{5}} = 0.6 A$$

$$I_{Rop} = I_1' = 0.6 A$$

it will operate @ 5% (CT rating)
 $= (0.05)(5) = 0.25 A$

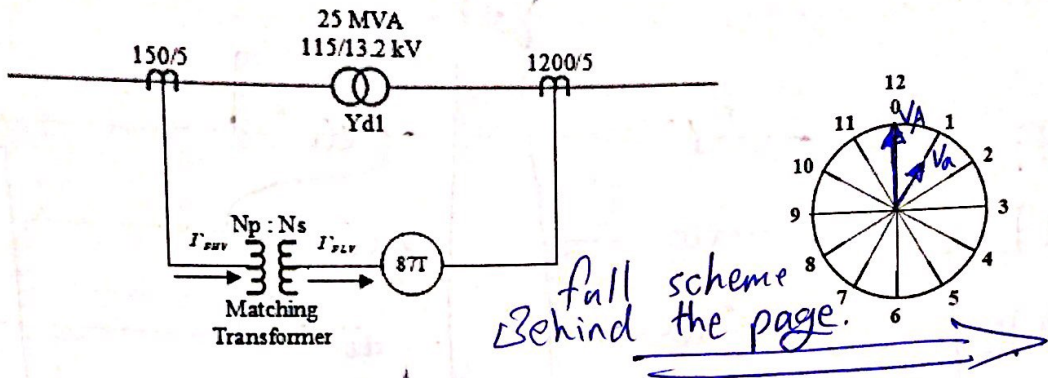
$0.6 > 0.25 \Rightarrow$ yes it will trip.



Question # 4 (12 points)

Show Your Calculations

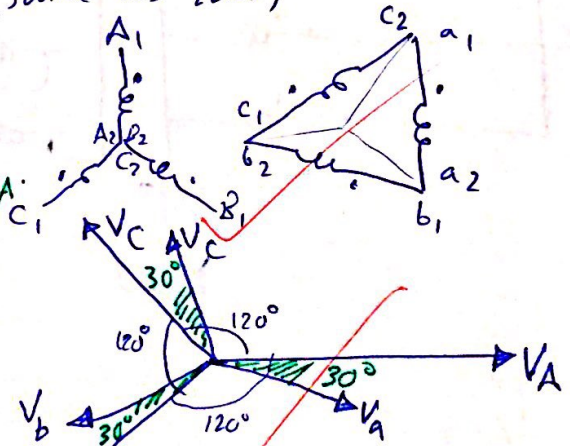
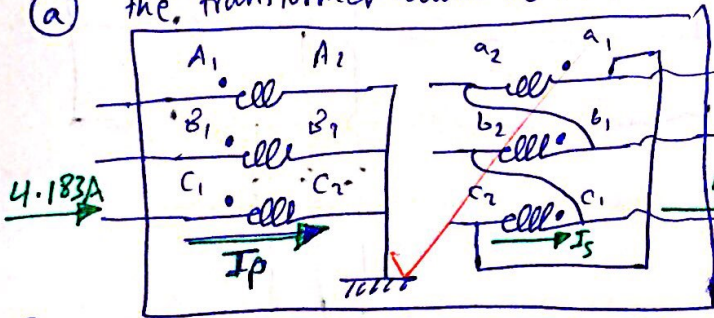
For the 25 MVA, 115/13.2 kV Yd1 transformer shown below, it is required to set the (87T) differential relay with matching transformer. If the CTs on both sides of the transformer are Y-connected,



- Identify the vector group of the matching transformer and draw its schematic diagram. Verify the vector group and transformer connections using phasor diagrams.
- Calculate for full-load conditions:

i.	the pilot wire currents I'_{PHV} and I'_{PLV} on both left- and right-hand sides of the relay.	$I'_{PHV} = 4.183$ A	$I'_{PLV} = 4.556$ A
ii.	the appropriate turns ratio N_p/N_s of the matching transformer which can be installed in the primary circuit of 115 kV CT side to compensate the magnitude and phase difference.	$\frac{N_{p-match}}{N_{s-match}} = 0.6287$	

(a) the matching transformer would be as follows: (same as Yd1)



(b)

$$I_{HV} = \frac{25 \times 10^6}{\sqrt{3} \times 115 \times 10^3} = 125.5 \text{ A}$$

$$I_{LV} = \frac{25 \times 10^6}{\sqrt{3} \times 13.2 \times 10^3} = 1093.5 \text{ A}$$

$$I'_{HV} = \frac{125.5}{150/5} = 4.183 \text{ A} \equiv I'_{PHV}$$

$$I'_{LV} = \frac{1093.5}{1200/5} = 4.556 \text{ A} \equiv I'_{PLV}$$

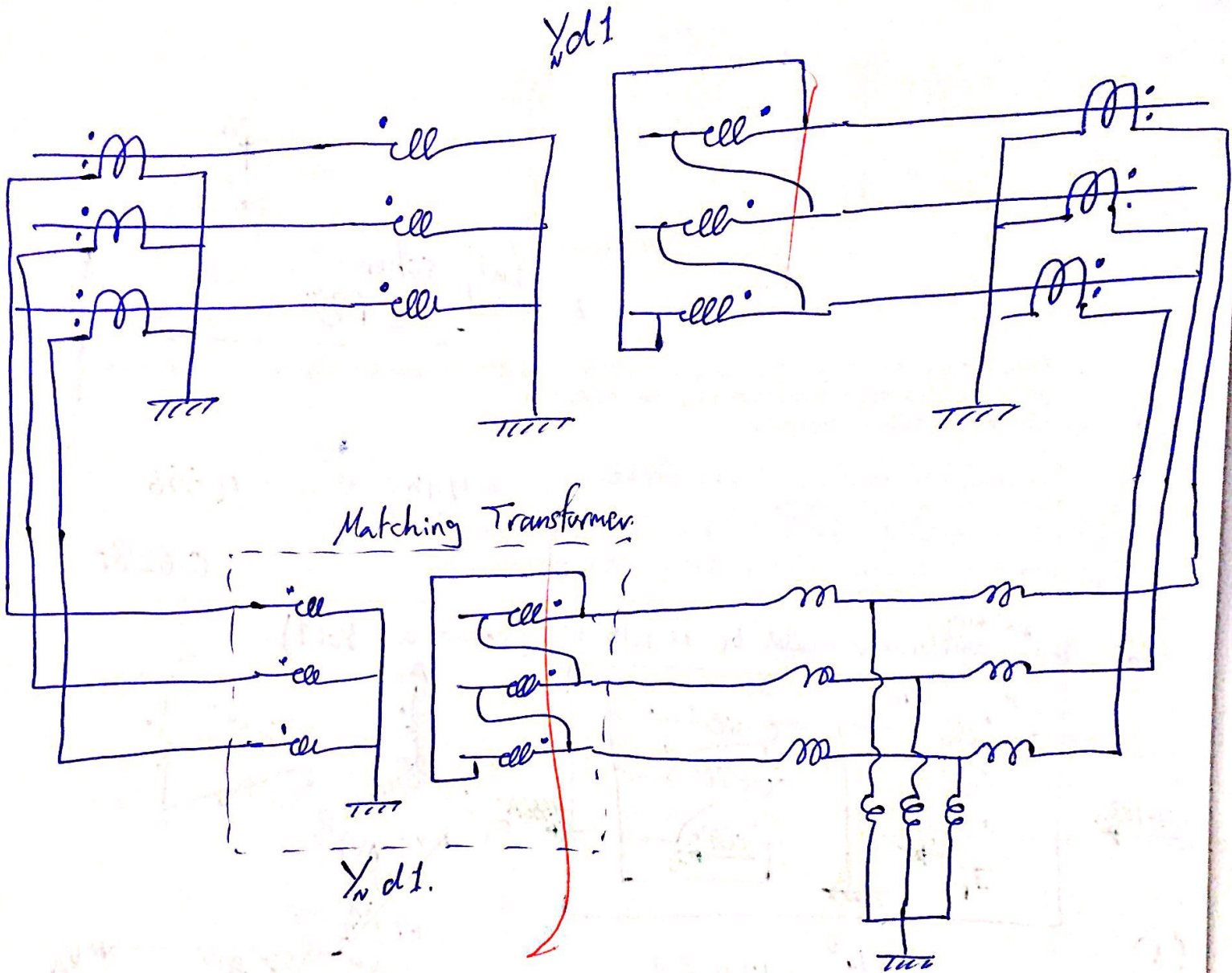
since CTs Both Y connected

$$I_p = 4.183 \text{ A}$$

$$\Rightarrow \frac{N_p}{N_s} = \frac{I_s}{I_p} = \frac{263}{4.183} = 0.6287$$

$$I_s = \frac{4.556}{\sqrt{3}} = 2.63 \text{ A}$$

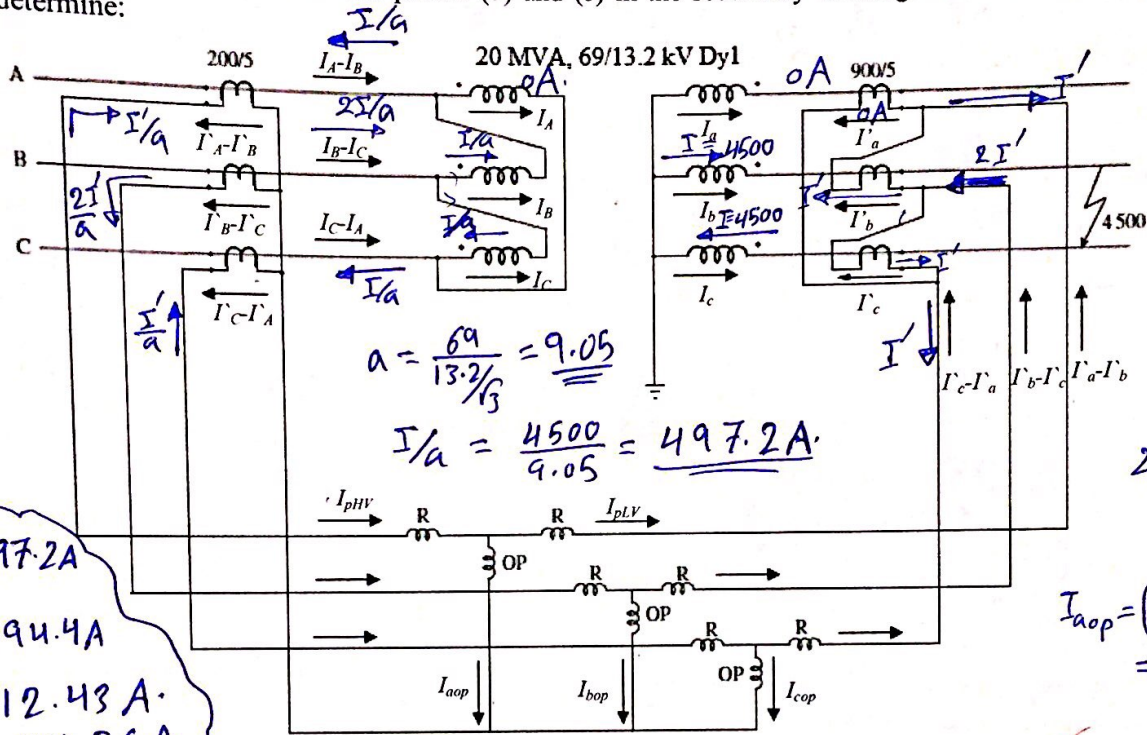
Q4



Question # 5 (22 points)

Show Your Calculations

Consider the 20-MVA, 69/13.2-kV, Dyl transformer whose connections are shown below. The CTs on the 69-kV side of the transformer have a ratio of 200/5, and those on the 13.2-kV side a ratio of 900/5. The differential relays operate for a current equal to 20% of nominal current. If a line-line fault of 4500 A occurs between phases (b) and (c) in the secondary windings of the transformer, determine:



$\frac{I}{a} = 497.2 A$
 $2\frac{I}{a} = 994.4 A$
 $\frac{I'}{a} = 12.43 A$
 $2\frac{I'}{a} = 24.86 A$

$a = \frac{69}{13.2/\sqrt{3}} = 9.05$
 $\frac{I}{a} = \frac{4500}{9.05} = 497.2 A$

$I' = \frac{4500}{\frac{900}{5}} = 25 A$
 $2I' = 50 A$

$I_{aop} = (-\frac{I'}{a}) + I' = 25 - 12.43 = 12.57 A$

a.	the magnitude and direction of the phase currents in the LV-side windings.	$I_a =$	0 A
		$I_b =$	4500 A
		$I_c =$	-4500 A
b.	the magnitude and direction of the phase currents in the CT secondary of the LV-side windings.	$I'_a =$	0 A
		$I'_b =$	25 A
		$I'_c =$	-25 A
c.	the magnitude and direction of the line currents in the CT secondary of the LV-side windings.	$I'_a - I'_b =$	-25 A
		$I'_b - I'_c =$	50 A
		$I'_c - I'_a =$	-25 A
d.	the magnitude and direction of the phase currents in the HV-side windings.	$I_A =$	0 A
		$I_B =$	497.2 A
		$I_C =$	-497.2 A
e.	the magnitude and direction of the line currents in the HV-side windings.	$I_A - I_B =$	-497.2 A
		$I_B - I_C =$	994.4 A
		$I_C - I_A =$	-497.2 A
f.	the magnitude and direction of the phase currents in the CT secondary of the HV-side windings.	$I_A - I_B =$	-12.43 A
		$I_B - I_C =$	24.86 A
		$I_C - I_A =$	-12.43 A
g.	the relay operating currents	$I_{aop} =$	12.57 A
		$I_{bop} =$	-25.14 A
		$I_{cop} =$	12.57 A
h.	the fault between phases b and c causes relay	(Operation)	No Operatio

$I_{bop} = (2\frac{I'}{a}) + (-2I')$
 $= 24.86 - 50 = -25.14 A$

$I_{cop} = (-\frac{I'}{a}) + I' = 25 - 12.43 = 12.57 A$