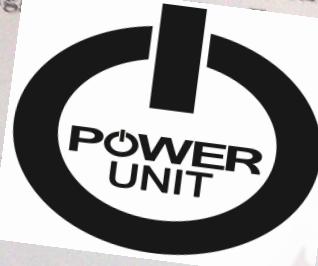


Name(in Arabic)

Student No.  
Section

2 (12-1pm)

Programmable calculators are not allowed.  
Derive any formula you use.

1. A voltage of  $v(t) = \frac{100 \cos(\omega t - 90^\circ)}{100 \sin(100\pi t)}$  V, is applied to a certain non-linear load. The flowing current is given by:  
 $i(t) = 2 + 9 \sin(100\pi t) - 12 \cos(100\pi t) + 5 \sin(300\pi t)$  A  
 Find:

(i) The rms value of the current

4marks

$$\underline{2 + 9 \cos(100\pi t - 90^\circ)} - 12 \cos(100\pi t) + 5 \cos(300\pi t - 90^\circ)$$

$$\underline{2 + 15} \angle -143.13^\circ + \underline{5} \angle -90^\circ$$

$$= \sqrt{129} \quad ?$$

(ii) The power factor

$$F = \frac{P}{V_{rms} \cdot I_{rms}} = \frac{\cancel{(15\sqrt{2})} \cdot \cancel{(15/\sqrt{2})} \cdot \cancel{\cos(-90^\circ)}}{\cancel{(100/\sqrt{2})} \cdot \sqrt{129}} \quad I_{rms} = 15/\sqrt{2} \quad V_{rms} = 100/\sqrt{2}$$

$$\frac{(15/\sqrt{2})}{\sqrt{129}} \cdot \cos(-90^\circ - (-143.13)) = 0.560 \quad \checkmark$$

(iii) The distortion volt ampere

$$= S^2 - P^2 - Q^2 \quad \checkmark$$

$$\frac{I_{rms}}{I_{rms}} = \frac{(15/\sqrt{2})}{(\sqrt{129})} = 0.933 \quad ?$$

3

(iv) The total harmonic distortion

2. A single phase half wave rectifier with an RL load and a freewheeling diode.  
 $V_m = 200V$ ,  $R = 10 \Omega$ ,  $L = 0.05H$ ,  $f = 50Hz$ .  
 Find

(i) The output average current

$$I_{rms} = \frac{200}{\sqrt{2}} = 141.42$$

4marks

$$\phi = \tan^{-1} \left( \frac{VL}{IR} \right)$$

$$I_{dc} = \frac{V_m}{\pi R} = 6.369$$

(ii) The rms value of the output current

$$\frac{V_m}{\pi} + \frac{V_m}{2} \sin(\omega_0 t) - \sum \frac{2V_m}{n^2 - 1} \cos(2n\omega_0 t)$$

$n$	$U_n$	$Z$	$X$	$I_n$	$I_{rms}$
0	63.7	10	0	6.37	6.37
1	100	12.6	15.7	5.37	3.798
2	84.3	32.95	31.4	1.28	0.904
4	8.49	63.6	68.8	+133	0.094

4

$$I_{rms} = \sqrt{(6.37)^2 + (3.798)^2}$$

$$= 7.416$$

$$u = t$$

$$x = \frac{1}{2} \pi f L$$

$$u = \pi$$

(iii) The output power

$$P = I_{rms}^2 R$$

$$= (7.416)^2 \times 10 = 550.01$$

(iv) The supply power factor

$$PF = \frac{(550)}{(200)(7.416)} = 0.524$$

3. A single phase half wave rectifier with a resistive load and a smoothing capacitor. Find the following

a. Value of the angle  $\theta$  in degrees (When the diode stops)

$$\pi - \theta = (\omega t + \phi) \\ \pi - 82^\circ = \omega t + \phi$$

$$203.8^\circ$$

$$\frac{\pi}{180} \times 203.8 = 50$$

$$\omega R C = 31.4$$

b. Value of the angle  $\alpha$  in degrees (When the diode starts)

$$\pi - \alpha = \omega t + \phi \\ \pi - 55^\circ = \omega t + \phi$$

$$55^\circ$$

c. The output voltage ripple.

$$\text{Ripple} = V_m (1 - \sin \alpha) = 36.16$$

$$\frac{dV}{dt} = 180 \text{ V/D}$$

d. The equation of the diode current as function of time

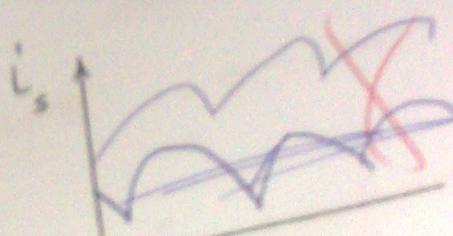
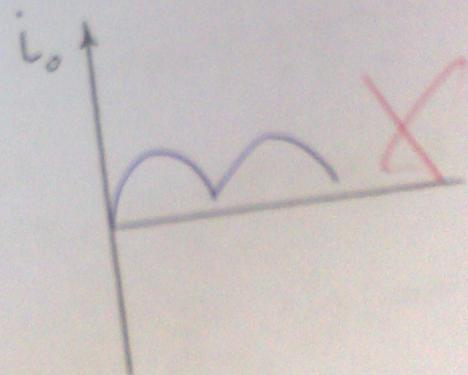
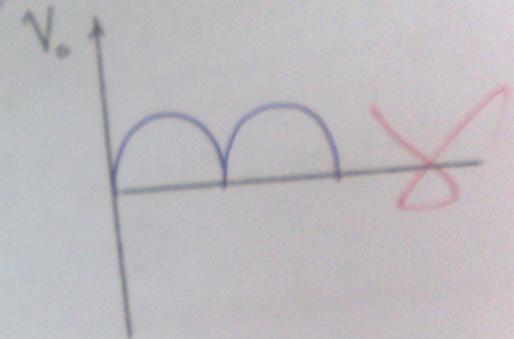
$$i_D(t) = i_{DC} + i_R$$

$$i_D(t) = \frac{V_m}{R} \sin(\omega t) + \omega C V_m \cos(\omega t - \phi)$$

4. A full wave bridge rectifier with  $V_m = 200V$ , 50Hz, a resistance of  $4\Omega$ , an inductance of  $20mH$  and a dc source of  $100V$ . 3marks

(i) Is the current continuous or discontinuous? Why?

(ii) Sketch the waveform of the output voltage, output current and the supply current showing the exact values of the angles on the waveforms



① Voltage of  $v(t) = 100 \sin(100\pi t)$  is applied to a certain non-linear load. The following current is given by:

$$i(t) = 2 + 9 \sin(100\pi t) - 12 \cos(\pi t) + 5 \sin(360\pi t) \text{ A}$$

① Find the rms value:

$$(i) I_{rms} = \sqrt{2^2 + \left(\frac{15}{2}\right)^2 + \left(\frac{5}{2}\right)^2} = 11.36 \text{ A}$$

$$(ii) P.F = \frac{I_{rms} \cdot I_{rms}}{I_{rms}} = \frac{\frac{15}{\sqrt{2}}}{11.36} = 0.933 \cos(+53) = 0.59$$

$$(iii) P = \frac{100}{\sqrt{2}} \times \frac{15}{\sqrt{2}} \cos(53) = 450$$

$$Q = \frac{100}{\sqrt{2}} \times \frac{15}{\sqrt{2}} \sin(53) = 600$$

$$VA = \frac{100}{\sqrt{2}} \times 11.36 = 803$$

$$\therefore D = \sqrt{803^2 - 600^2 - 450^2} = 286.9 \text{ VA}$$

$$(iv) THD = \sqrt{\frac{1}{D_F^2} - 1} = \sqrt{\frac{1}{0.933^2} - 1} = 0.383$$

A single & halfwave, RL load and freewheeling diode,  $V_m = 200V$

$$R = 10\Omega, L = 0.05H, f = 50Hz$$

n	$V_n$	$X_n$	$Z_n$	$I_n$	$I_{rms}$	$I_{rms} = \sqrt{6.28^2 + 3.87^2 + 0.91^2} = 7.4$
0	62.8	0	10	6.28	6.28	
1	100	15.7	18.6	5.376	3.8	
2	127.4	31.4	32.887	1.287	0.91	$7.4^2 \times 10 = 0.567W$

3. A single phase half wave rectifier with resistive load and a smoothing capacitor

$$V_m = 200, R = 1\text{ k}\Omega, C = 100 \mu\text{F}, f = 50\text{ Hz}$$

$$\theta = \pi - \tan^{-1} \omega RC$$

$$= 91.7^\circ$$

$$\alpha = 56^\circ$$

$$\Delta V = V_m (1 - \sin \alpha) = 200 (1 - \sin 56^\circ)$$

$$= 34.13 \text{ V}$$

4. Full wave bridge rectifier with  $V_m = 200 \text{ V}$ ,  $50\text{ Hz}$ ,  $R = 4$  ohms, inductance  $20\text{ mH}$ , DC source  $= 100\text{ V}$

$$(i) \sin \alpha = \frac{E}{V_m} = \frac{100}{200}$$

$$\alpha = 30^\circ$$

$$\beta = 150^\circ$$

$$\frac{wL}{R} = 1.57$$

29/3

static Induction Thyristor : slide M1  
reverse biased configuration

Light Activated Silicon : self biasing  
↳ Change of voltage  $\rightarrow$  bias