

15  
20

2	2/10
3	6/10
4	22/24
Sum	45/60

EE 090371 Electrical Machines (1)

First Exam.  
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Q1) In a 4-poles machine, the poles, rotor and yoke are made of the same magnetic material with the following data for magnetization curve:

B (Tesla)	0.6	0.9	1.1	1.5	2	2.5
H (kA/m)	0.1	0.2	1.05	1.15	1.2	2.0

For a closed loop between two adjacent poles, the lengths of flux path in this loop for the various components in METER are as follows:

Pole=0.2, air gap=0.005, rotor=0.1 and yoke=0.4

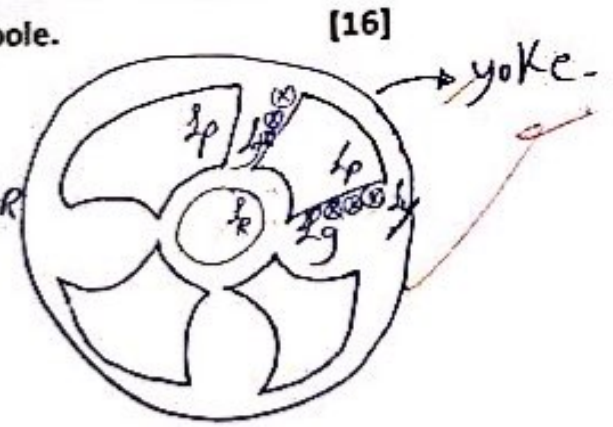
It is required to have the following flux densities at the various Components:

Component	Pole	Air gap	Rotor	Yoke
B (Tesla)	1.5	0.86	0.9	1.1

By SKETCHING the magnetic structure and WRITING the relevant expression EVALUATE the required mmf per pole.

15  
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2



$$mmf = Ni = H_p l_p + H_g l_g + \frac{1}{2} H_y l_y + \frac{1}{2} H_r l_r$$

⇒ mmf ⇒

$$H_p = 1.15 \text{ kA/m}$$

$$H_y = 1.05 \text{ kA/m}$$

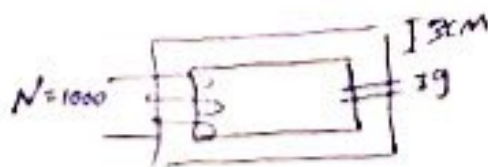
$$H_r = 0.2 \text{ kA/m}$$

$$H_g = \frac{B}{\mu_0} = \frac{0.86}{4\pi \times 10^{-7}} = 684.366 \text{ kA/m}$$

$$mmf = (1.15 \text{ k})(0.2) + (684.366 \text{ k})(0.005) + \frac{1}{2} (0.2 \text{ k})(0.1) + \frac{1}{2} (1.05 \text{ k})(0.4)$$

$$mmf = 3871.83 \text{ A.t.}$$





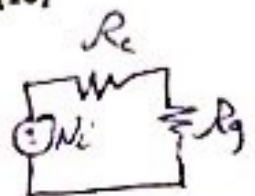
$$g = 0.12 \text{ cm}$$

$$l_c = 30 \text{ cm}$$

Q2) A rectangular laminated core contains an air gap with length of 0.12 cm and has one coil wound on it. The core has a thickness of 3 cm and width of 2.5 cm. The mean length of flux path is 30 cm, stacking factor is 0.93 and  $\mu_r = \infty$ . By using the given data and taking fringing field into account, evaluate the self inductance of the coil if it has 1000 turns.

$$A_{\text{Total}} = (3 \text{ cm}) \times (2.5 \text{ cm}) = 7.5 \times 10^{-4} \text{ m}^2 \quad [10]$$

$$\Rightarrow A_c = A_T \times \text{S.F.} = 6.975 \times 10^{-4} \text{ m}^2$$



$$Ni = \phi (R_c + R_g)$$

$$L = \frac{N^2}{R} = \frac{N^2 \mu A}{l} \quad e = \frac{L \text{ di}}{\text{dt}} \quad R = R_c + R_g$$

$$L = \frac{(1000)^2 \times 4\pi \times 10^{-7} \times \infty \times 6.975 \times 10^{-4}}{30 \times 10^{-2}} = \infty$$

\* the value of self inductance of a coil depend on  $\mu$  so it is also depend on  $\mu_r$  by the relation  $L = \frac{N^2 \mu_0 \mu_r A}{l} \Rightarrow$  so when  $\mu_r \rightarrow \infty$   $L$  is also  $\rightarrow \infty$

Q3) If the applied voltage to the primary of a transformer at no-load and its frequency are doubled, show by using mathematical derivation what will happen to its Eddy and Hysteresis losses. [10]

we know that:

voltage & f are doubled.

eddy losses represented by:  $P_e = V f^2 B_m^2 \tau^2 K_e$

Hysteresis losses represented by:  $P_h = A_h \cdot f \cdot V = K_h B_m^n f V$

\* Now the change happen on the voltage @ No load & the frequency. but from  $P_e$  &  $P_h$  we Notice that they does not depend on the voltage, on the other hand they depend on the frequency.

so  $f_{\text{new}} = 2 f_{\text{old}}$

so  $P_{e_{\text{new}}} = M_1 \times 4 f^2$  &  $P_{h_{\text{new}}} = M_2 \times 2 f$

$\Rightarrow P_e = M_1 f^2$

from that:  $P_{e_{\text{new}}} = 4 P_{e_{\text{old}}}$  &  $P_{h_{\text{new}}} = 2 P_{h_{\text{old}}}$

$P_h = M_2 f$

where  $M_1$  &  $M_2$  are constants.

Notice that Hysteresis losses is doubled.

& the Eddy losses become 4-times its old value.



Q4) Conventional O/C and S/C tests were performed on (40/2.4) kV transformer with the following readings

O/C:  $I=9.1$  A  $P=1925$  W

S/C:  $I=12.5$  A  $P=4075$  W



a- Find the parameters of the transformer which can be evaluated from the O/C test and referred to HV side. [12]

we can find from o/c test  $R_c$  &  $X_m$ .

\* By conventional: o/c test applied @ LV side  
so 2.4 kV should be the rated voltage.

$$\Rightarrow \begin{aligned} P_{oc} &= 1925 \text{ W} \\ I_{oc} &= 9.1 \text{ A} \\ V_{oc} &= 2.4 \text{ kV} \end{aligned}$$

$R_c$  can be evaluated from  $R_c = \frac{V_{oc}^2}{P_{oc}} \Rightarrow R_c = 2992.2 \Omega$

$$|Y| = \frac{I_{oc}}{V_{oc}} = 3.79 \times 10^{-3} = \frac{1}{R_c^2} + \frac{1}{X_m^2}$$

\* But these values in LV so in HV side: (reflect to a-side)

so  $X_m$  can be evaluated:

Solving  $\Rightarrow X_m = 264.77 \Omega$

$$\begin{aligned} R_c &= a^2 (2992.2) \Rightarrow R_c = 831.5 \text{ k}\Omega \\ X_m &= a^2 (264.77) \Rightarrow X_m = 73.58 \text{ k}\Omega \end{aligned}$$

b- Find the values of parameters which can be evaluated from the S/C test in PU by using the transformer ratings as base values. [12]

\* By Conventional S/C test applied @ HV side

we have:

$$\begin{aligned} P_{sc} &= 4075 \text{ W} \\ I_{sc} &= 12.5 \text{ A} \\ V_{sc} &= 40 \text{ kV} \end{aligned}$$

we can find from s/c test  $R_{eq}$  &  $X_{eq}$

so  $R_{eq} = \frac{P_{sc}}{I_{sc}^2} \Rightarrow R_{eq} = 26.08 \Omega$

where  $|Z| = \frac{V_{sc}}{I_{sc}} = 3200 = \sqrt{R_{eq}^2 + X_{eq}^2}$

to find  $X_{eq}$ : solving:  $X_{eq} = 3199.89 \Omega$

\* Now  $R_{eq}$ ,  $X_{eq}$  which had been evaluated in HV side, so we find the base

@ HV:  $|S| = |I_{sc}| \times |V_{sc}| = (12.5)(40 \text{ kV}) \Rightarrow S = 500 \text{ kVA}$

take  $S_b = 500 \text{ kVA}$  &  $V_b = 40 \text{ kV}$   $\Rightarrow Z_b = \frac{V_b^2}{S_b} = \frac{(40 \times 10^3)^2}{500 \times 10^3} \Rightarrow Z_b = 3200 \Omega$

Continue  $\rightarrow$

⇒ Continue  $Q_4$  (part b):

we have  $R_{eq} = 26.08 \Omega$ ,  $X_{eq} = 3199.89 \Omega$

∴  $Z_b = 3200 \Omega$

So PU values will be as follows:

$$R_{eq}(pu) = \frac{R_{eq}}{Z_b} = \frac{26.08}{3200}$$

$$X_{eq}(pu) = \frac{X_{eq}}{Z_b} = \frac{3199.89}{3200}$$

$R_{eq}(pu) = 0.326$	PU
$X_{eq}(pu) = 39.999$	PU

the values are (in PU):

$$R_{eq}(pu) = 0.00815 \text{ PU}$$

$$X_{eq}(pu) = 0.99997 \text{ PU}$$