

\* Instrument → device collect data.

→ Display  
→ optional (analysis)

\* Instrument → analogue

→ Digital → A/D, D/A  
→ store data

Ammeter  $\propto i$

EN50160

~~EN50160~~ ↑ standard → code

Distribution code

1 week.

95% within voltage limit.

10 min.

$$-6\% \leq \Delta V \leq 10\%$$

↓  
voltage drop.

\* Does this instrument provide True value?

true value  $\triangleq$  theoretical value based on models

\* Characteristics of measurement instruments:-

① Accuracy: How close is the reading from the true value.

Ex: measured value = 10V, voltmeter

(close to the true value) accuracy = 10%, range 0-15V, Find the true value?

sol:  $10 \pm (10\% \cdot 15) = 8.5 \text{ V} \ominus$

$= 11.5 \text{ V} \oplus$

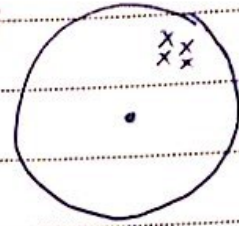
11

② precision  $\Rightarrow$  Reproducibility Ex:

$\bullet \rightarrow$  true value

$X \rightarrow$  measurement value

- high precise
- low accuracy



مقادیر قریب ہوتے ہیں مگر اصل قدر سے دور ہیں  
true value

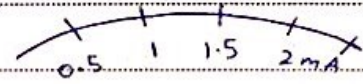
③ Sensitivity :- the ability to respond to the changes in the measured quantity (inputs)

$$S = \frac{\Delta \text{output}}{\Delta \text{input}}$$

④ threshold: minimum input that could be measured

⑤ Resolution :-

Step change  
کوئی چھوٹی تبدیلی



\* Accuracy (expressed in accuracy)

accuracy ( $\pm 0.1\%$ )

$\rightarrow$  tolerance

## \* Precision

Metric

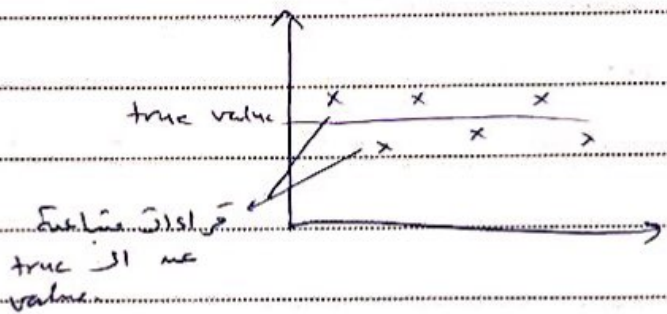
 $\sigma \triangleq$  Standard deviation

$$\sigma^2 = E[(x - \bar{x})^2]$$

↙ expectation
↘ mean

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}}$$

N = sample size

 $\bar{x} \equiv$  mean (average) $x_i \equiv$  reading
 $1 \text{ max} - \text{mean} \longrightarrow \text{Precision}$ 

**Ex** A voltmeter is used to read voltage of 5V [Dc 100  
 ((snap shot))

reading A  $\Rightarrow$  " 5.03, 4.97, 5, 5.02, 4.99, 4.89, 5.03  
 5.02, 5.01, 4.97 "

reading B  $\Rightarrow$  " 5.2, 5.2, 5.2, 5.2 "

compare accuracy, precision?

Note: \* reading 10 8 20 → mean = average

reading	10	8	20
freq	100	20	80

mean average

$$\bar{x} = E[x] = 10 * \left( \frac{100}{200} \right) + 8 * \frac{100}{200} + 20 * \frac{80}{200}$$

Sol: accuracy is

A: true value = 5V

$$\text{mean} = \frac{5.03 + 4.97 + \dots + 4.97}{10} = 5 = \text{average}$$

B: mean =  $\frac{5.2 + \dots + 5.2}{4} = 5.2 = \text{average}$

true value = 5 V

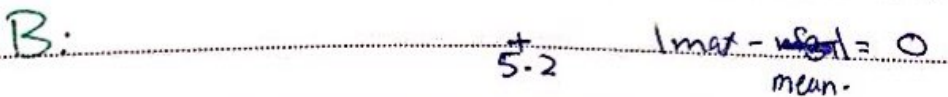
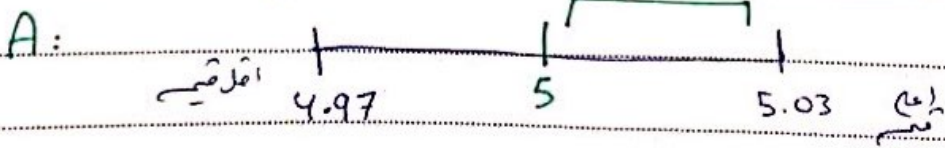
⇒ A more accurate than B

Precision

⇒ the precision in B is higher than in A

Sensitive

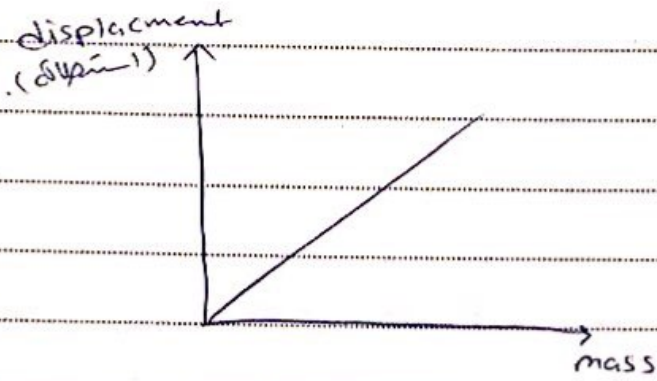
$$\text{Jump} = |\text{max} - \text{mean}| = 0.03$$



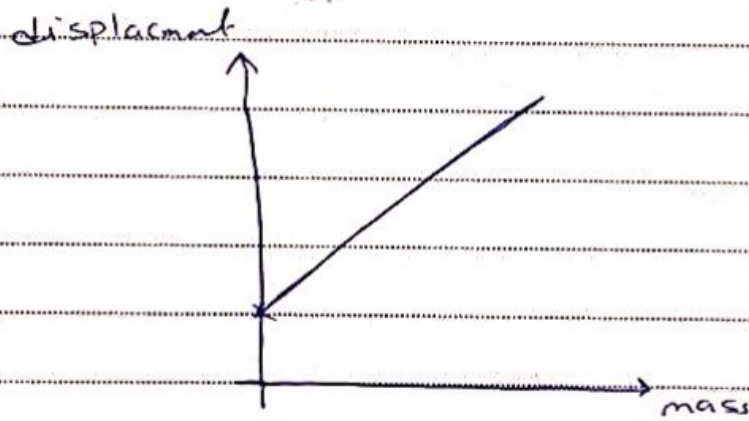


input (kg)	0	50	100
output (cm)	0	10	20

→ operating condition



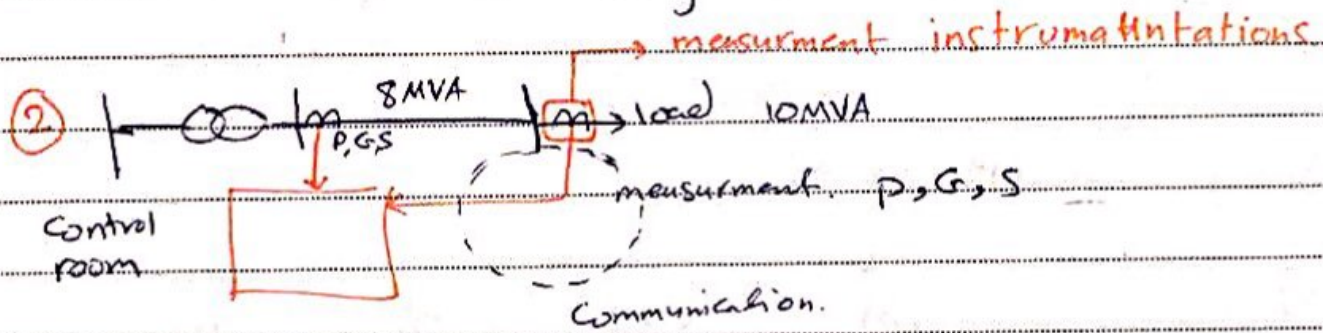
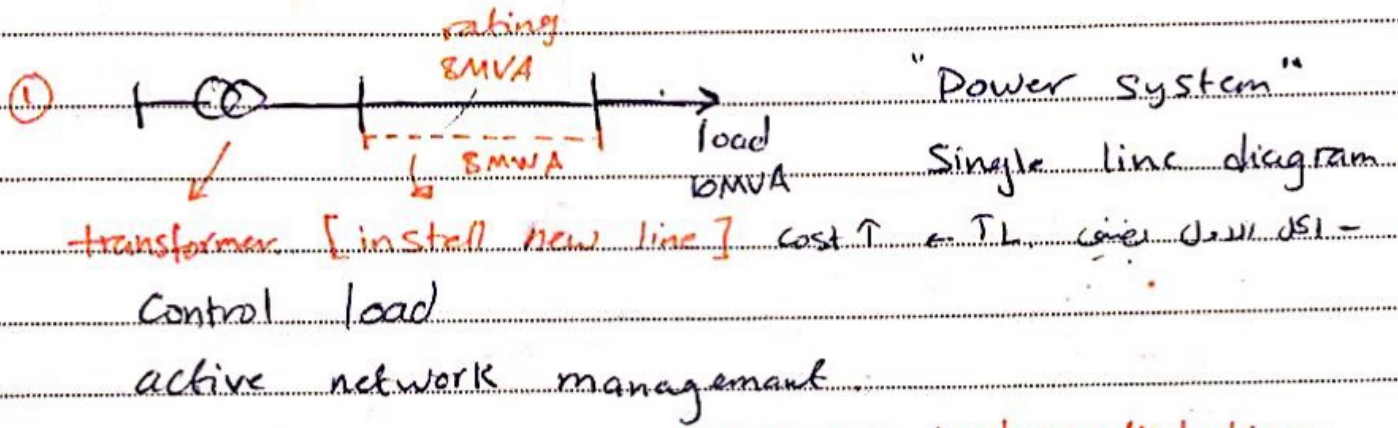
sensitivity  $\hat{=}$  slope =  $\frac{10}{50} \frac{\text{cm}}{\text{kg}} = 0.2 \text{ cm/kg}$



→ error → diff. in

Slides: error of measurement

- systematic error "سأطأ لؤ.ؤ" <sup>سأطأ</sup>
- Random error "ؤؤؤؤؤؤ" <sup>ؤؤؤؤؤؤ</sup>

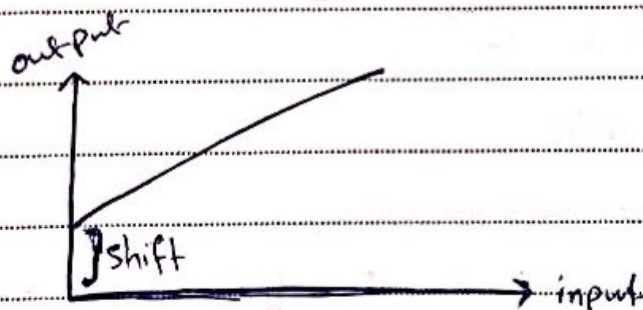


7MW → 8MW → 9MW

slide 2:

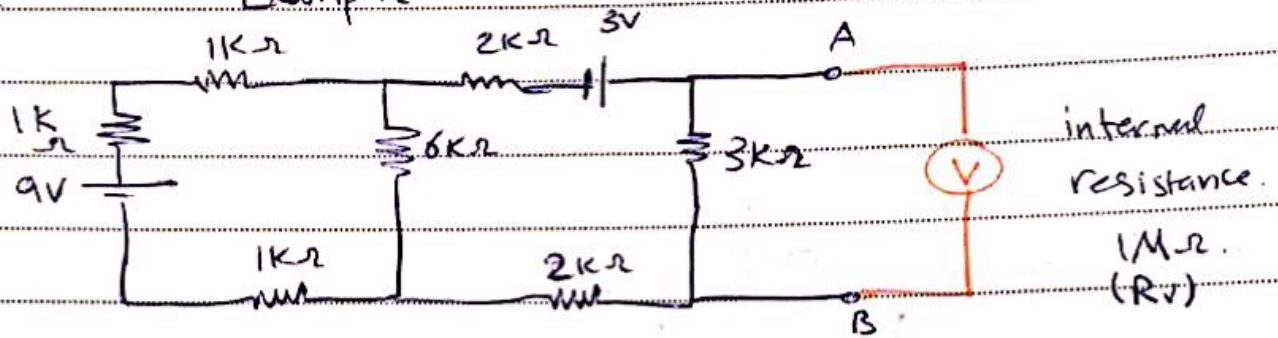
red point = mean of measurement + Gaussian noise value

slide 3:

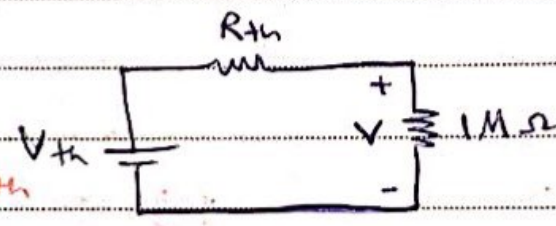
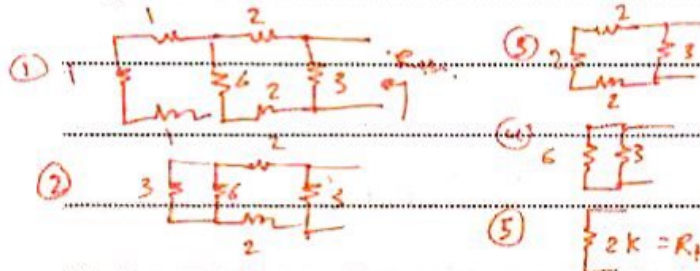


Slide 8: ~~Example~~

Slide Example



\* Error in the measurement ?!



$$V_{\text{real value}} = V_{\text{th}} (R_v \rightarrow \infty)$$

$$V_{\text{measured value}} = \frac{1\text{M}}{1\text{M} + (2\text{K})} * V_{\text{th}} = 0.998 V_{\text{th}}$$

$$\text{Error} = \frac{V_{\text{real}} - V_{\text{measured}}}{V_{\text{measured real}}} * 100\%$$

$$= \frac{V_{\text{th}} - 0.998 V_{\text{th}}}{V_{\text{th}}} * 100\%$$

$$= \frac{0.002 V_{\text{th}}}{V_{\text{th}}} * 100\% = 0.2\%$$

? -  $R_v \geq 198\text{K}\Omega$  to achieve 1% error.

$$\Rightarrow 0.01 = \frac{V_{\text{th}} - V_{\text{measured}}}{V_{\text{measured}}} \text{ less than } \textcircled{2} \frac{R}{R+2\text{K}} \quad V_{\text{th}} = 0.99 V_{\text{th}}$$

$$0.01 V_{\text{th}} = V_{\text{th}} - V_{\text{measured}}$$

$$V_{\text{measured}} = 0.99 V_{\text{th}}$$

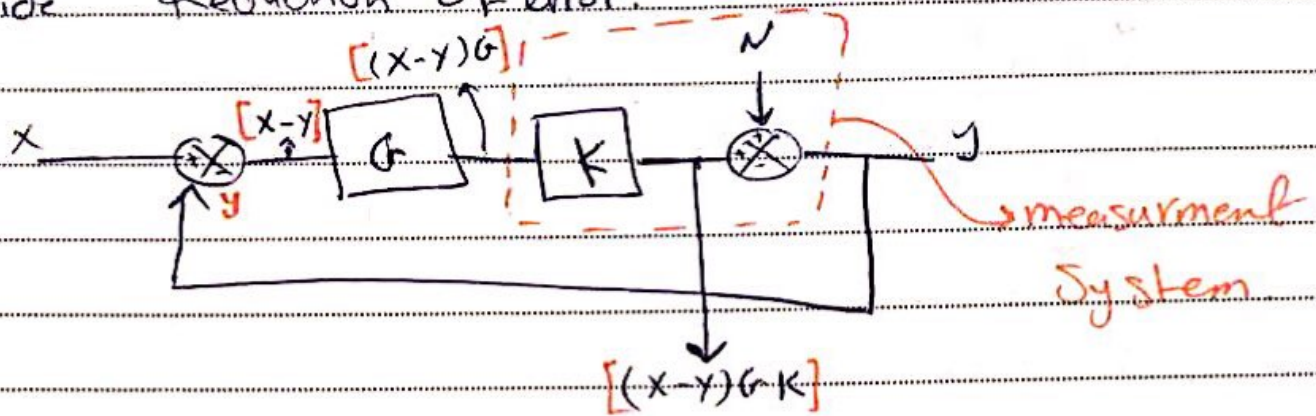
$$R = 0.99 R + 1.98\text{K}$$

$$0.01 R = 1.98\text{K}$$

$$R = 198\text{K} \quad \boxed{8}$$



slide Reduction of error.



$$y = (x-y)GK + N$$

"without- feed back

$$y = xKG + N$$

open loop"

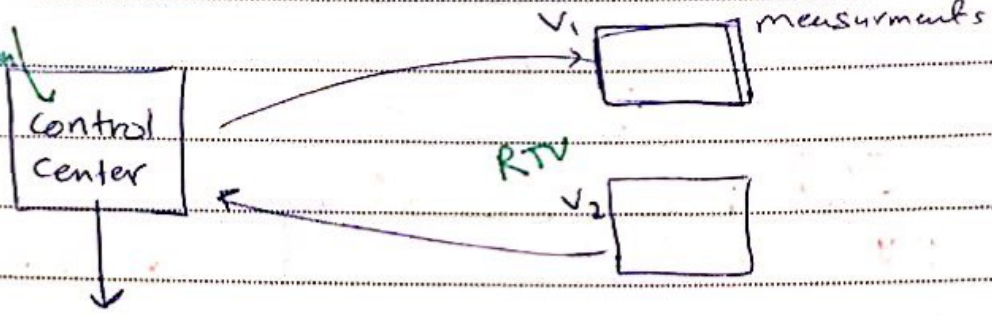
~~$$y = xGK - yGK + N$$~~

$$y = x \frac{GK}{1+GK} + \frac{N}{1+GK}$$

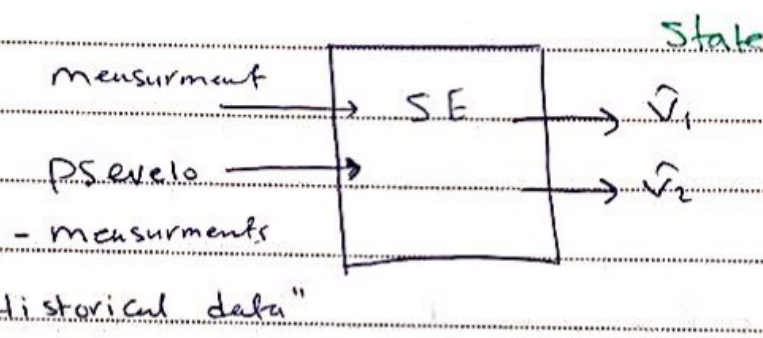
①  $G$  is very large  $\Rightarrow$  eliminate noise

②  $y \approx x$

State estimation



- 1) monitoring
- 2) decision-making algorithm



RTU = remote terminal unit.

slide: statiscal Analysis

13+14.



$$\sigma^2 = \frac{1}{n} \sum (x - \bar{x})^2$$

variance ←  $\sigma^2$       ←  $n$  sample      ←  $\bar{x}$  mean measurement

$\sigma$  = Standar variation.

~~XXXXXXXXXX~~

$n$

$n-1$  (Sample size)

$n < 30 \Rightarrow$

$n-1$  (d.f.)

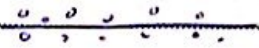
$\sigma \downarrow \rightarrow \downarrow \text{error}$

①



↑ error → ↑  $\sigma$

②



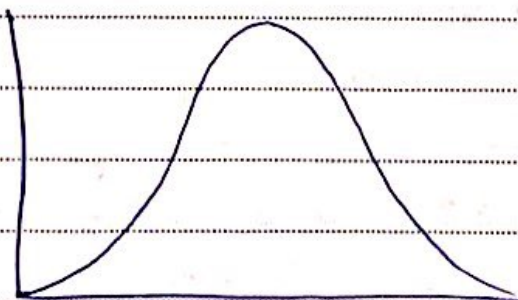
↓ error ↓  $\sigma$

Slide "Histogram"

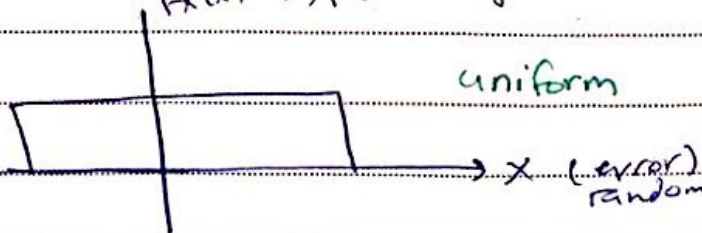
$$\text{mean} = \frac{1}{N} \sum x$$

$$\text{mean} = \sum x_i \Pr(x)$$

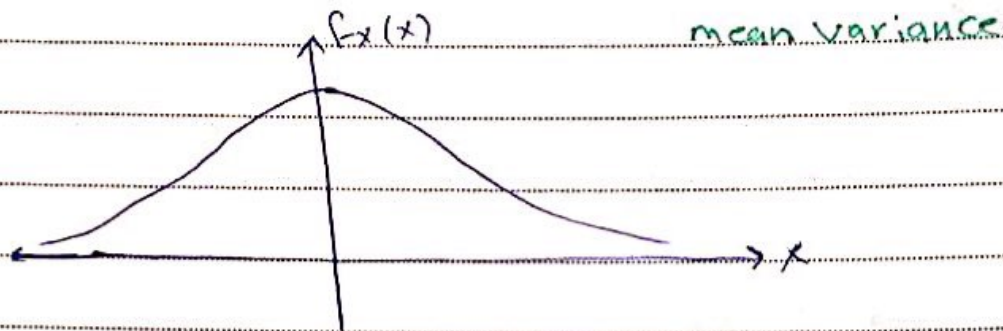
Slide Histogram  $\rightarrow$  pdf



$f_X(x) \rightarrow$  probability.

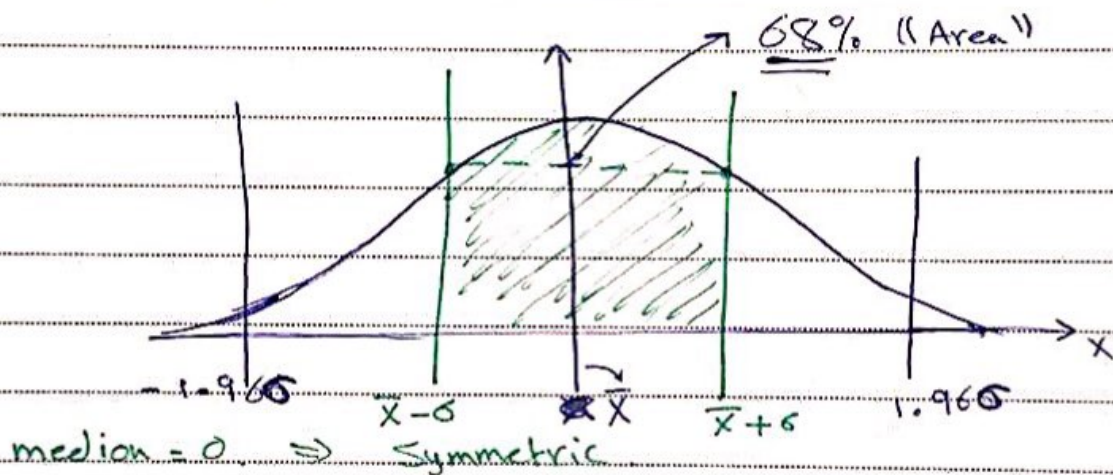


||



Wein Ball "Wind"

slide Gaussian Curve.



$$f_x(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\bar{x})^2}{2\sigma^2}}$$

$\sigma^2$  variance

$\bar{x} \equiv$  mean

at  $1.96\sigma \rightarrow$  Area = 95%

$$\Pr(-1.96\sigma \leq X \leq 1.96\sigma) = 95\%$$

$$\Pr(\bar{x} - \sigma \leq X \leq \bar{x} + \sigma) = 68\%$$

$$\Pr(\bar{x} - 1.96\sigma \leq X \leq \bar{x} + 1.96\sigma) = 95\%$$

pdf "prob. density function"

$f_X(x)$

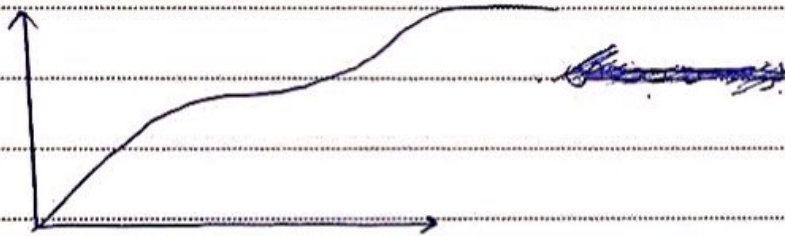
$$\Pr(x_1 \leq X \leq x_2) = \int_{x_1}^{x_2} f_X(x) dx$$

slide (CDF)

CDF  $\Rightarrow$

$$F_X(x_0) = \Pr(X \leq x_0)$$

non-decreasing




$$F_X(x_0) = \int_{-\infty}^{x_0} f_X(x) dx$$

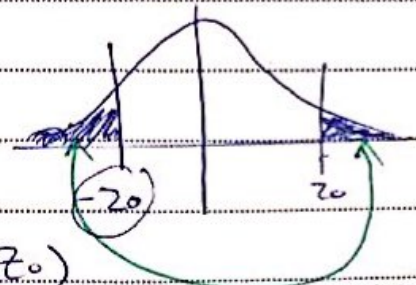
slide Standard Gaussian ...

$$F_X(x) = \Pr(X \leq x_0)$$

$$z_0 = x_0 - \text{mean}$$

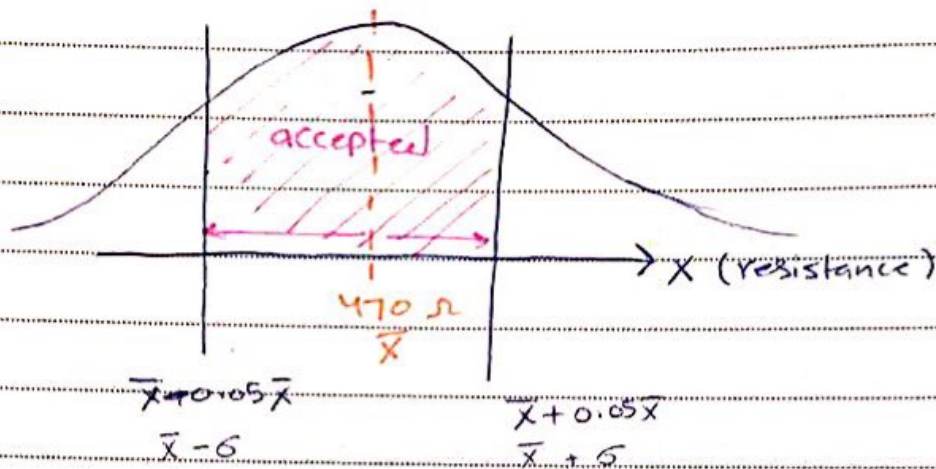
$\sigma$   
 table

$$F(-z_0) = 1 - F(z_0)$$



نفس المساحة

Slide 21

 Gaussian Curve - Example


①

$$\sigma = 23.5 \Omega, \quad \bar{x} = 470 \Omega$$

$$\Pr(\bar{x} - 0.05\bar{x} \leq X \leq \bar{x} + 0.05\bar{x})$$

$$= \Pr(X \leq \bar{x} + 0.05\bar{x}) - \Pr(X \leq \bar{x} - 0.05\bar{x})$$

$$= F_X(\bar{x} + 0.05\bar{x}) - F_X(\bar{x} - 0.05\bar{x})$$

$$F(z) = \Pr(Z \leq z)$$

$$\rightarrow \text{table } z = \frac{x - \text{mean}}{\sigma}$$

$$F_2\left(\frac{\bar{x} + 0.05\bar{x} - \bar{x}}{\sigma = 0.05\bar{x}}\right) - F_2\left(\frac{\bar{x} - 0.05\bar{x} - \bar{x}}{\sigma}\right)$$

$$= F_2(1) - F_2(-1)$$

$$= 68\%$$

$$\Pr(\text{rejection}) = 32\%$$

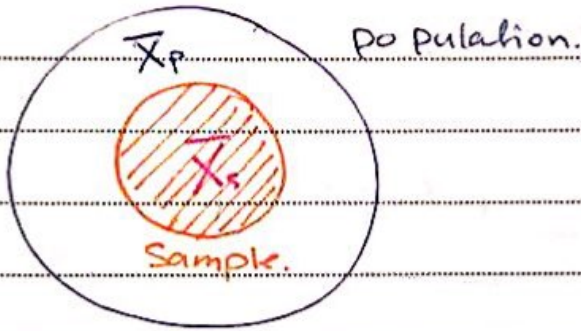
$$32\% * 10,000 = 3174 \text{ will be rejected.}$$

"random error"

$$\sigma^2 = \frac{1}{N} \sum (x - \bar{x})^2$$

↓
↓  
+5
+5

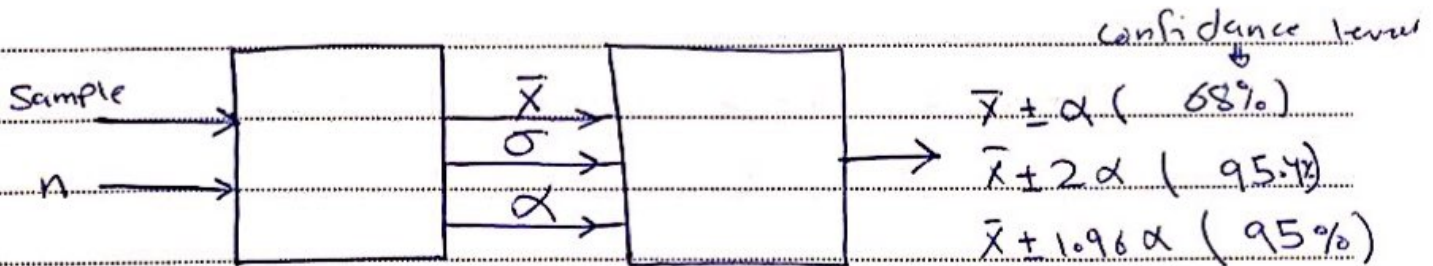
Slid 22 Standard Error of the Mean.



Confidence level.

$\alpha$  (Standard error of the mean)

$$\alpha = \frac{\sigma}{\sqrt{n}}$$



- Confidence level  $\leftrightarrow$   $\mu$  data  $\mu$   $\sigma$ ; LAS

slide 26 Example:

A voltmeter was ...

$$\begin{aligned} \text{(sample)} \quad \bar{X} &= \frac{36.1 + 36.3 + \dots + 35.8}{10} \\ &= 35.93 \text{ V} \end{aligned}$$

$$\begin{aligned} \sigma_{n-1} &= \sqrt{\frac{1}{N-1} \left[ \sum_{i=1}^N (X_i - \bar{X})^2 \right]} \\ &= 0.365 \end{aligned}$$

$$30 < \leftarrow N-1 \leftarrow \bar{X}$$

$$\alpha = \frac{\sigma}{\sqrt{n}} = 0.115$$

Confidence ~~limit~~ level  $\approx 95.4\%$

$$\bar{X} \pm 2\alpha$$

- mean true value

$$35.93 \pm 2(0.115)$$

slide 27 aggregation of error.

max

$$u = V + W$$

tolerance  $\leftarrow \bar{V} \quad \bar{W} \rightarrow$  tolerance  $\pm n\%$

$\pm m\%$

$$W = 5 \text{ volt} \pm 10\%$$

$$V = 10 \text{ V} \pm 10\%$$

16



$$U = 15V \quad (\text{No error}).$$

$$U_{\max} = (10 \times 1.1) + (5 \times 1.1)$$

$$= 11 + 5.5$$

$$= 16.5 V$$

$$(1 + 0.1)$$

$$1 + \frac{10}{100}$$

$$U_{\min} = (10 \times 0.9) + (5 \times 0.9)$$

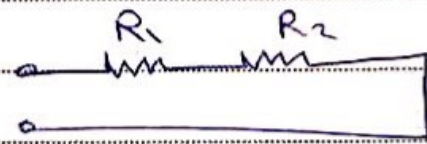
$$= 13.5 V$$

$$(1 - 0.1)$$

\*

$$R_{\text{eq}} = R_1 + R_2$$

5% ← | → 10%



Slide 32 Example.

when a steel rod - ...

$$F = \frac{E \cdot A \cdot d}{L}$$

constant

$$\Delta F = \Delta A \frac{\partial F}{\partial A} + \Delta d \frac{\partial F}{\partial d} + \Delta L \frac{\partial F}{\partial L}$$

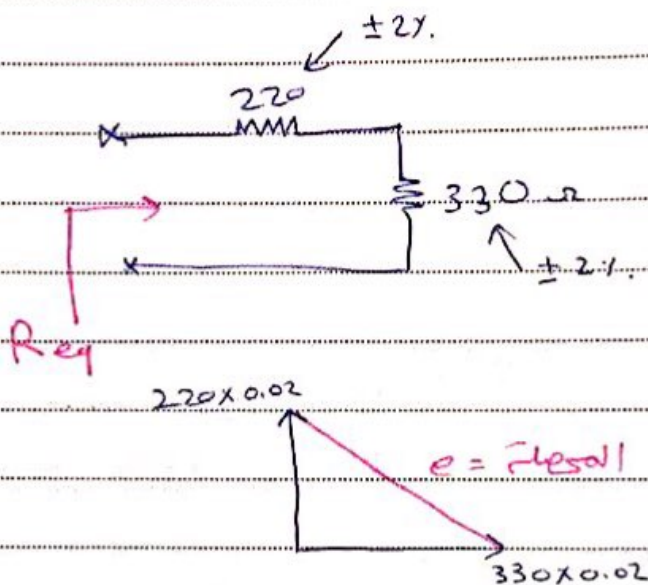
$$\left| \frac{\Delta F}{F} \right|_{\min} = \frac{\Delta A}{A} + \frac{\Delta d}{d} + \frac{\Delta L}{L}$$

$$\left| \frac{\Delta F}{F} \right|_{\max} = -\frac{\Delta A}{A} - \frac{\Delta d}{d} - \frac{\Delta L}{L}$$

slide: Probable Value - ~~Multiplication~~ Multiplication

$$e = \sqrt{(m)^2 + (n)^2}$$

slide: 37 aggregation of error:



(( probable error ))

$$e = \sqrt{(220 \times 0.02)^2 + (330 \times 0.02)^2}$$

$$e = 7.93 \Omega$$

$$R_{series} = 220 + 330 = 550 \Omega$$

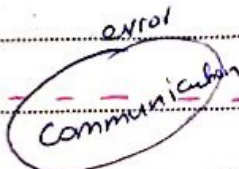
$$\frac{7.93}{550} = 1.44\%$$

× نسبة error كبير ولا صغيرة  
نسبة على نسبة الاصلية

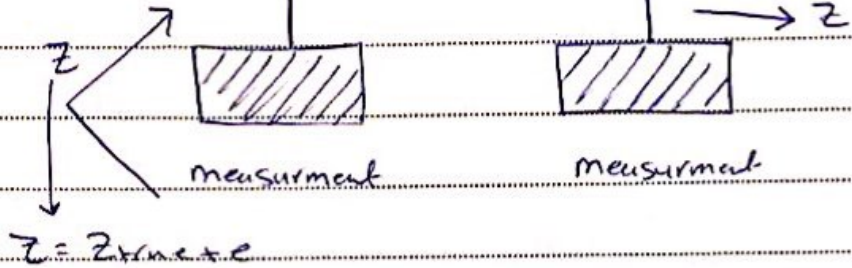
$$R = 550 \pm (1.44\% \times 550)$$

$$\frac{e}{R} = \frac{\text{true} - \text{meas}}{\text{true}}$$

\* State estimation 8A



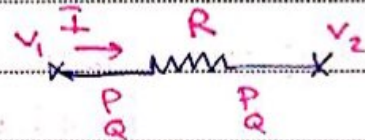
decision-making algorithm



$$z = z_{true} + e$$

e = error  
 ↳ Systematic  
 ↳ random

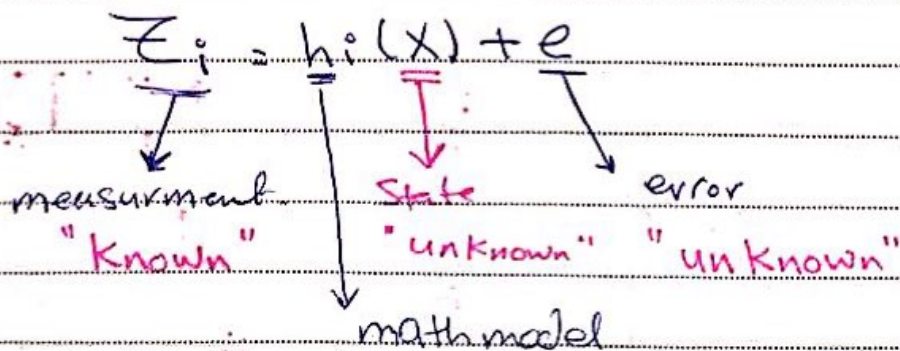
→ Know value of state (voltages and angles at each node)



1 error in measurement

in measurement / communication / SCADA

2 Not enough real measurements





\* Random error: assumptions

- Gaussian
- measurements are independent

↑ measurement → "state estimation"

\* Weighted least square error (WLS)

$$\text{Min} \sum_{i=1}^m \frac{(Z_i - h(x))^2}{\sigma_i^2}$$

minimization for error.

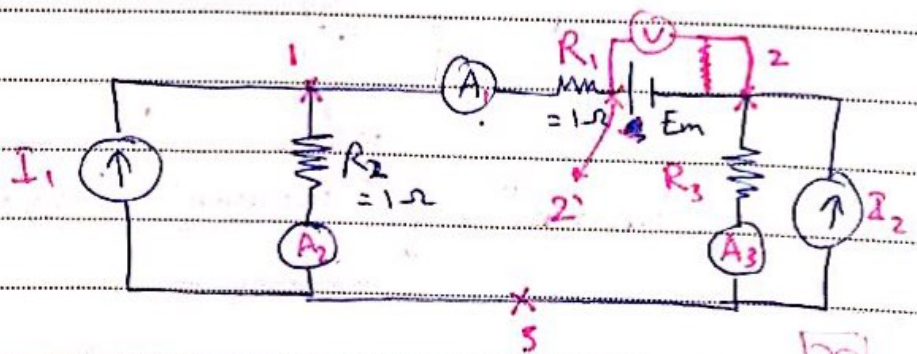
$\sigma_i \equiv$  emphasis, trust measurement  
emphasis ↓

- Pseudo measurement:

↳ historical data

\* linear least square estimation

[Ex]



$\hat{V}_1, \hat{V}_2, e$  are all unknown

$$R_1 = R_2 = R_3 = 1 \Omega$$

measurement:

$$A_1: i_{12} = 1A$$

$$A_2: i_{31} = 3.2A$$

$$A_3: i_{23} = 0.8A$$

$$V: E_m = 1.1V$$

State

$$\begin{bmatrix} V_1 \\ V_2 \\ e \\ !? \end{bmatrix}$$

$$Z? = h(x)$$

$$i_{12} = \frac{V_1 - V_2'}{R_1}$$

$$V_2' = E_m e + V_2$$

$$i_{12} = \frac{V_1 - E_m - V_2}{R_1} = V_1 - E_m - V_2$$

$$i_{12} = 1(V_1) - 1(E_m) - 1(V_2) = 1A \quad \dots \textcircled{1}$$

$$i_{31} = \frac{V_3 - V_1}{R} \Rightarrow -3.2 = \frac{0 - V_1}{1}$$

$$\boxed{-V_1 = -3.2} \quad \dots \textcircled{2}$$

$$i_{23} = \frac{V_2 - V_3}{1} = \frac{V_2 - 0}{1} = 0.8$$

$$V_2 = 0.8 \quad \dots \textcircled{3}$$

$\Rightarrow$  coefficient  $E_m, V_1 = 0$

$\boxed{21}$

$$e = 1.1 \quad v \quad \dots \quad (4)$$

$$\begin{bmatrix} 1 & -1 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ e_m \end{bmatrix} = \begin{bmatrix} 1 \\ -3.2 \\ 0.8 \\ 1.1 \end{bmatrix}$$

A

X

= Z

!?

$$A_1 = 1A + e$$

$$e = 1A - \frac{F(x)}{\text{model}}$$

Unique Solution

Unique Solution

$$Z - Ax = \text{error}$$

Minimize (WLSE)

"over determined"

- pseudo measurement  
(distorted data)

$$Ax = b = z$$

b → real measurement  
A →

↳ best estimate

Minimize error between measurement that value resulting from the model.

$$\begin{bmatrix} 1 \\ -3.2 \\ 0.8 \\ 1.1 \end{bmatrix} \text{ (Error)} = \begin{bmatrix} 1 & -1 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ e \end{bmatrix} = \begin{bmatrix} 1 - v_1 - v_2 + e_m \\ -3.2 + v_1 \\ 0.8 - v_2 \\ 1.1 - e_m \end{bmatrix}$$

WLSE

Z

A

X

$$\text{Min} \Rightarrow (1 - V_1 - V_2 + e_m)^2 + (-3.2 + V_1)^2 + (0.8 - V_2)^2 + (1.17 - e_m)^2$$

$$X = G^{-1} A^T b \quad b = Z$$

$\downarrow$   
Gain matrix

$$G = A^T A$$

$$X = \begin{bmatrix} 3.125 \\ 0.875 \\ 1.175 \end{bmatrix} \begin{matrix} V_1 \\ V_2 \\ e_m \end{matrix}$$

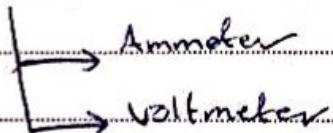
residual

$$r = b - AX = \begin{bmatrix} 1 \\ -3.2 \\ 0.8 \\ 1.1 \end{bmatrix} - \begin{bmatrix} 1 & -1 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 3.125 \\ 0.875 \\ 1.175 \end{bmatrix} = \begin{bmatrix} -0.075 \\ -0.075 \\ -0.075 \end{bmatrix}$$

Slide Meters :-

DC meters - Analogue

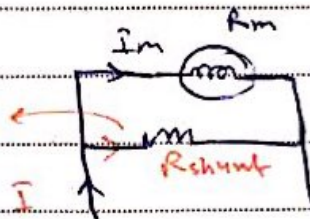
PMMC



Slide 43 Basic DC ammeter.

$\downarrow R_{shunt} \rightarrow I \uparrow$

$I - I_m$



$$I_m R_m = R_{sh} (I - I_m)$$

$$R_{sh} = \frac{I_m R_m}{I - I_m} = \frac{R_m}{\left(\frac{I}{I_m}\right) - 1}$$

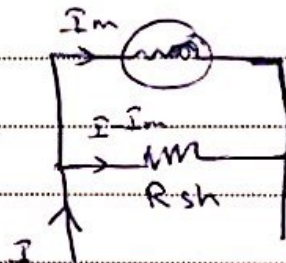
$$R_{sh} = \frac{R_m}{n - 1}$$

$$\frac{I}{I_m} = n$$

Slide 45 Basic DC Ammeter:

Ex 1

$I_m = 1 \text{ mA}$ ,  $I = (0 - 10 \text{ mA})$   
 $R_m = 100 \ \Omega$



Sol:

$$R_{sh} = \frac{100}{\left(\frac{10 \text{ mA}}{1 \text{ mA}}\right) - 1} = 11.11 \ \Omega$$

Ex 2

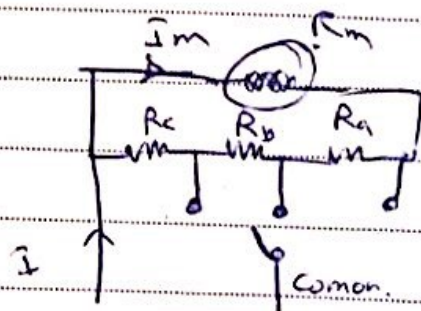
↑ range → ↓ Rsh  $\left[ R_{sh} = \frac{800}{\left(\frac{100 \text{ mA}}{100 \ \mu\text{A}}\right) - 1} = 0.8 \ \Omega \right]$

Slide 46 Multiple Range Ammeter.

Ex

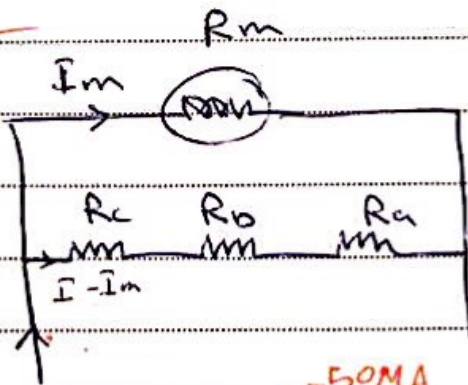
$I_m = 50 \ \mu\text{A}$   
 $R_m = 2400 \ \Omega$

- 3 ranges →
- 5 mA
  - 50 mA
  - 500 mA





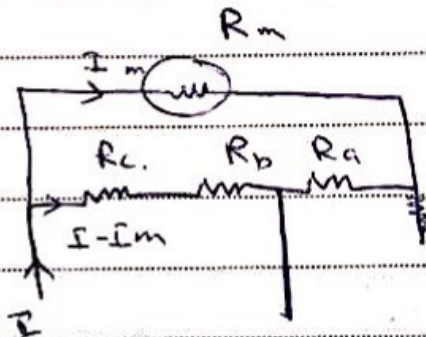
5mA :-



$$R_c + R_b + R_a = \frac{I_m R_m}{I - I_m} \dots (1)$$

$\xrightarrow{50\text{mA}}$   $\xrightarrow{2400}$   
 $\xleftarrow{5\text{mA}}$   $\xleftarrow{50\text{mA}}$

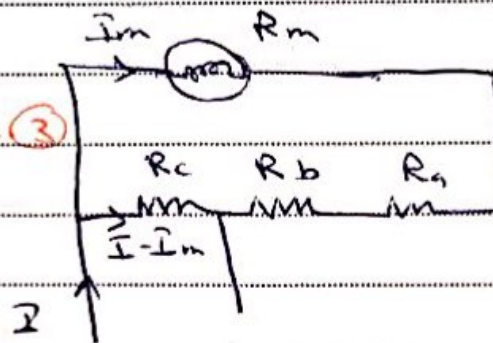
50mA :-



$$\frac{I_m (R_m + R_a)}{I - I_m} = R_c + R_b \dots (2)$$

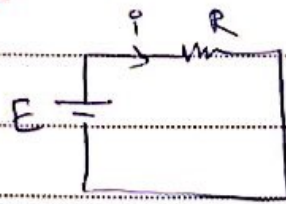
500mA :-

$$\frac{I_m (R_a + R_b + R_m)}{I - I_m} = R_c \dots (3)$$

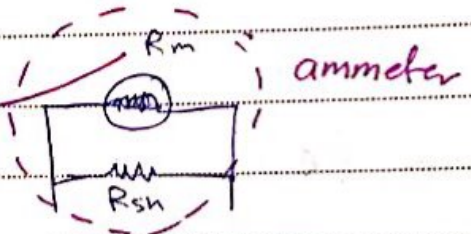
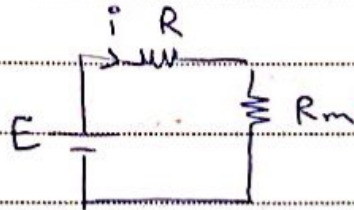


- $R_c = 2.18 \Omega$
- $R_b = 9 \Omega$
- $R_a = 21.81 \Omega$

**Slide 49** Ammeter loading effects



$$i_{\text{applied}} = \frac{E}{R}$$

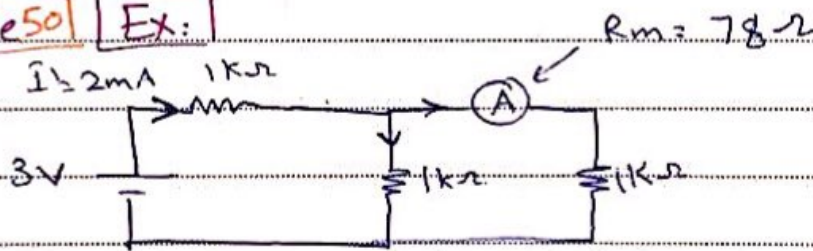


$$i_{\text{measured}} = \frac{E}{R + R_m}$$

↓ ammeter resistance.

$$\text{Insursion error} = \frac{i_{\text{exp}} - i_m}{i_{\text{exp}}}$$

**Slide 50** Ex:



$$i'_{\text{expected}} = \frac{3}{1.5k} = 2\text{mA}$$

$$i_{\text{expected}} = \frac{3}{3k} = 1\text{mA}$$



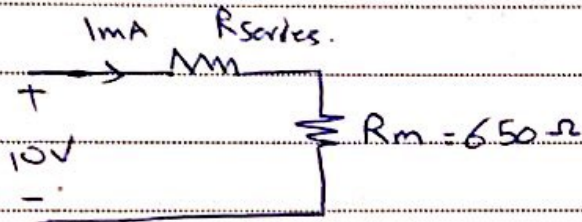
$$i' = \frac{3}{1k + (1k + 78) \parallel 1k} = 1.97\text{mA}$$

$$I_{\text{measured}} = I' \cdot \frac{1K}{1K + 1K + 78} = 0.95 \text{ mA}$$

$$\text{error} = \frac{1 - 0.95}{1} \times 100 = 5\%$$

**Slide 51 Basic DC Voltmeter.**

**Ex** A ~~param~~ Perament:



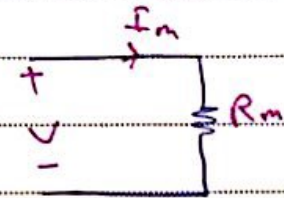
$$-10 + 1\text{mA}(R_s + R_m) = 0$$

$$R_{\text{series}} = 9.35 \text{ K}\Omega$$



$$R_1 \rightarrow V_1$$

$$R_1 + R_2 \rightarrow V_2$$



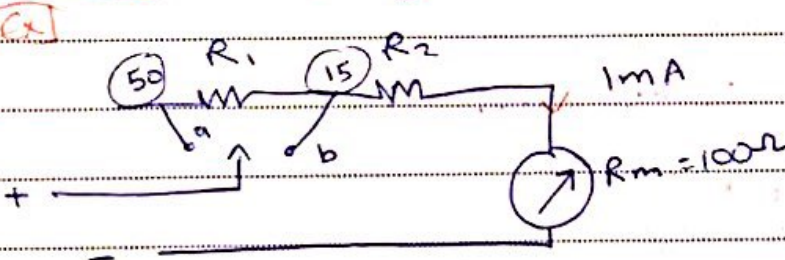
full scale deflection (as 20V scale)

$$V_{\text{Full scale deflection}} = I_m R_m$$

Full scale.



**Slide 52 Multi Range Voltmeter**



range: 0-15V, (0-50)V

Design ( $R_1, R_2$ )

$\uparrow R \rightarrow \uparrow$  scale

b  $I_m$  is 15V is ohms

$$b \Rightarrow 15 = I_m (R_2 + R_m) \dots \textcircled{1}$$

$$a \Rightarrow 50 = I_m (R_1 + R_2 + R_m) \dots \textcircled{2}$$

$$R_2 = 14.9 \text{ K}\Omega$$

$$R_1 = 35 \text{ K}\Omega$$

slide Sensitivity

$$\text{Sensitivity} = \frac{1}{I \text{ full scale deflection}} \Omega$$

$$S = \frac{1}{I_m} \dots 50 \text{ MA}, 500 \text{ MA}$$

50 MA more sensitive

slide Multi range  $\Rightarrow$  S  $\frac{V}{\Omega}$

$$S = \frac{1}{1 \text{ mA}} = 1000 \Omega/V$$

total series resistance =	$15 \times 10^3 \Omega = 15000 \Omega$	15V
" " "	$50 \times 10^3 \Omega = 50K \Omega$	50V

$$15K = R_2 + R_m$$

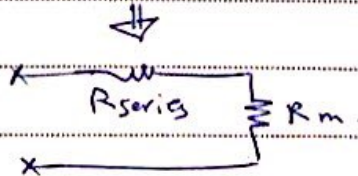
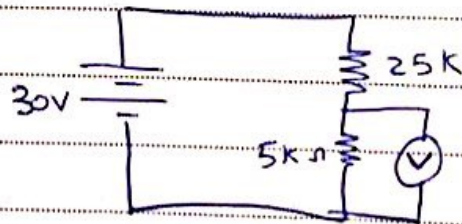
$$50K = R_1 + R_2 + R_m$$

slide Voltmeter loading effect:-

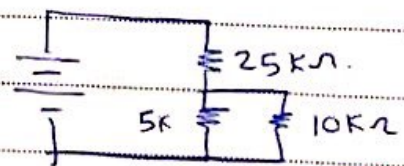
meter A  $\Rightarrow$

$$R_{\text{voltmeter}} = \frac{V \times S}{V}$$

$$= 10 \text{ K}\Omega$$

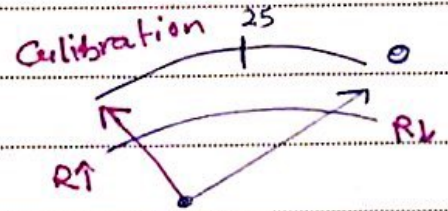


meter B  $\Rightarrow$   $R_V = 10 \times 20 \text{ K}\Omega = 200 \text{ K}\Omega$

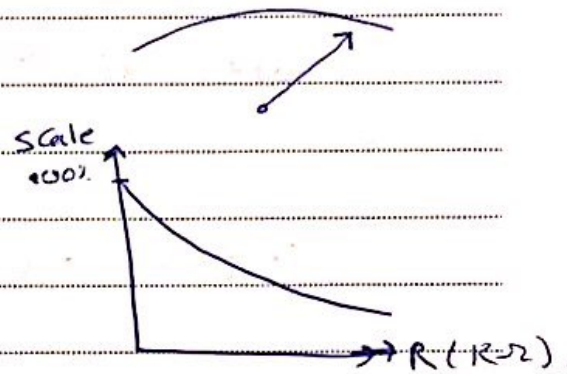
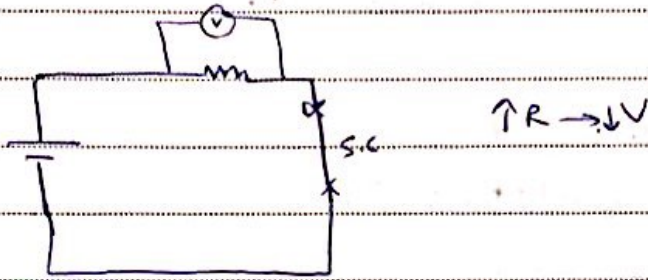


Slide ohmmeter

Reverse  
Nonlinear



50% deflection non-linear  $\rightarrow$  50% deflection  $\rightarrow$  2V is linear

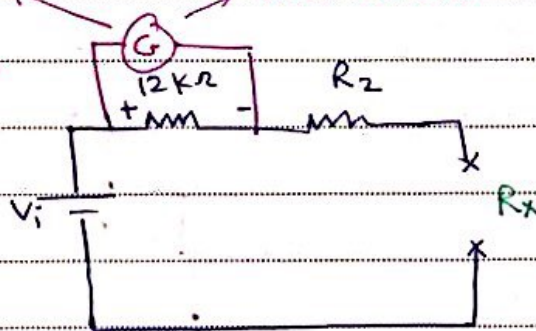


Slide 62:

50mA Full scale deflection

$R_{in} = 2400 \Omega$

Ex:



- Reverse  
- Not linear.

$V_i, R_2 ?!$

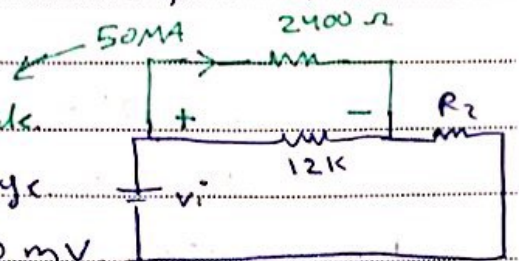
$\rightarrow$  full scale deflection,  $R_x = 0 ?!$

$\rightarrow$  20% full scale deflection  $R_x = 200k \Omega$

Soln

Full scale deflection voltage

$$50mA \times 2400 = 120 mV$$

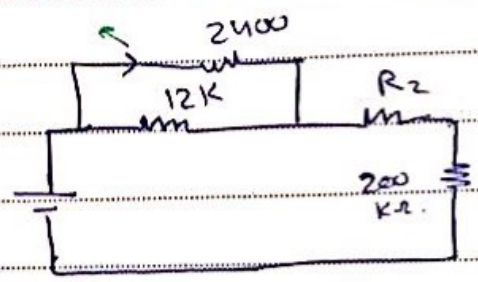


$$120 mV = V_i \times \frac{12k / 2400}{(12k / 2400) + R_2}$$

$$240 + 0.12 R_2 = 2000 V_i \quad \dots \textcircled{1}$$

20% full scale deflection.

$$\textcircled{2} \quad 20\% (2400 \times 50\text{MA}) = 0.024 \text{ V.}$$



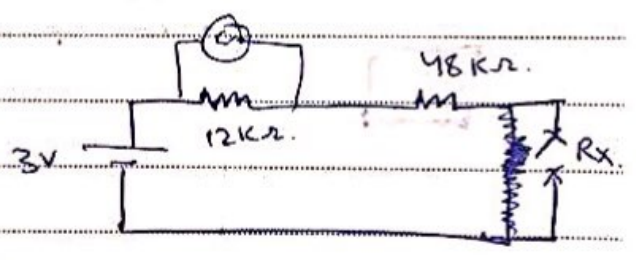
$$0.024 = V_i \left( \frac{12K // 2400}{(12K // 2400) + R_2 + 200K} \right)$$

$$4848 + 0.024 R_2 = 2000 V_i \quad \dots \textcircled{2}$$

$$R_2 = 48K\Omega$$

$$V_i = 3V$$

③



% d \* 120mV = 3 \* (2400 // 12K)

!?

$$\frac{(2400 // 12K)}{(2400 // 12K) + 48K + 450K}$$

75K  
50K

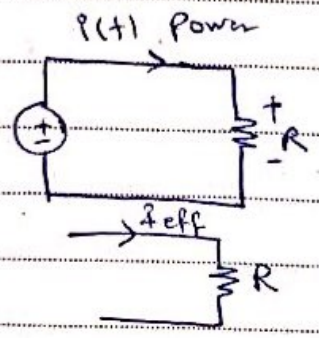
Rx = 450KΩ

Rx ↓

(full scale deflection)

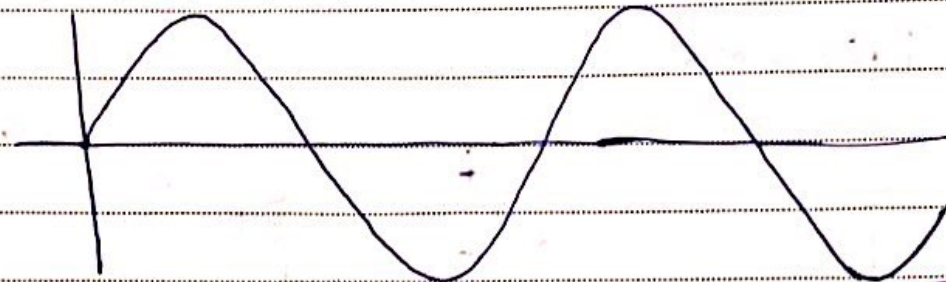
- 450K → 10%
- 75K → 40%
- 50K → 50%

slide AC volt.



rms

30



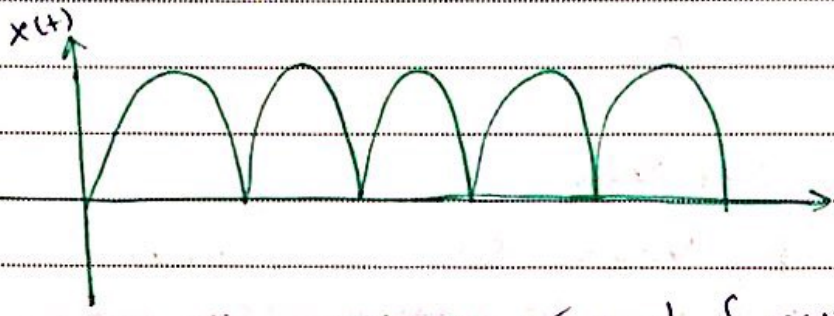
⇒ Rectifier.

average = 0.

$$I_{rms} = \sqrt{\frac{1}{T} \int i(t)^2 dt}$$

$$V_{rms} = \frac{V_m}{\sqrt{2}}$$

$$\therefore V_{rms} = 0.707 V_m$$



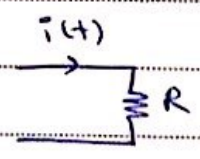
(FWR)

$$\text{average } V = \frac{1}{T} \int x(t) dt$$

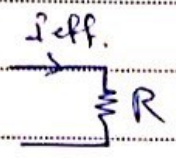
= 0.636 V<sub>m</sub> ⇒ error size 0.707 ~ 0.636

Safe Factor. ← scaling v. error 1.15

$$P_{av} = \frac{1}{T} \int i^2(t) dt = \frac{1}{2} i_{max}^2 R$$



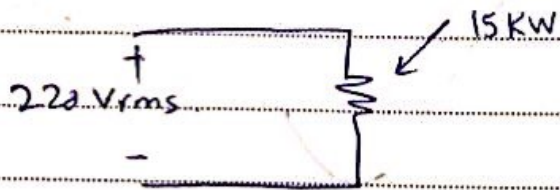
$$P_{av} = \frac{i_{rms}^2 \times R}{i_{eff}^2 \times R}$$



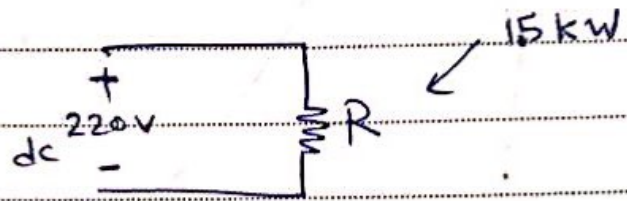
$$\frac{1}{2} i_{max}^2 R = \frac{i_{rms}^2 \times R}{i_{eff} \times R}$$

$$i_{rms} = \frac{i_m}{\sqrt{2}}$$

# Slide 66 True RMS



AC rms



dc

~~FWR~~

## AC signals

$$V_{rms} = 0.707 V_m$$

$$HWR \Rightarrow V_{av} = 0.5 V_m \quad \text{"Half wave rectifier"}$$

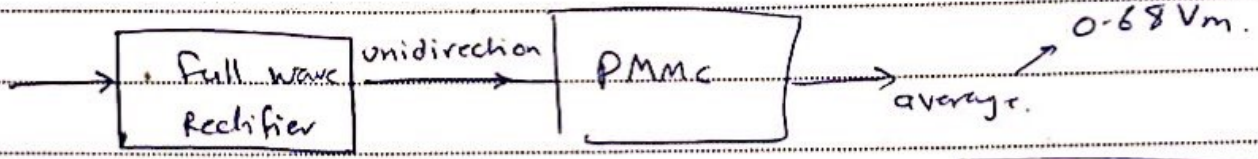
$$FWR \Rightarrow V_{av} = 0.636 V_m \quad \text{"Full wave"}$$

$$V_{av} = \frac{1}{T} \int_0^T x(t) dt$$

$$SF = \frac{V_{rms}}{V_{avg}} = \frac{0.707 V_m}{0.636 V_m} = 1.1$$



slide 71 AC voltmeter



True rms  
0.707 Vm

slide 72

\* correction factor

$$CF = \frac{SF \text{ waveform}}{SF \text{ sinusoidal}}$$

(ohmmeter)  $\Rightarrow$  Accuracy = 3% full scale. (~~Accuracy = 3% of reading~~)

if Full scale = 10V  $\Rightarrow$  Accuracy = 3%  $\times$  10 = 0.3V

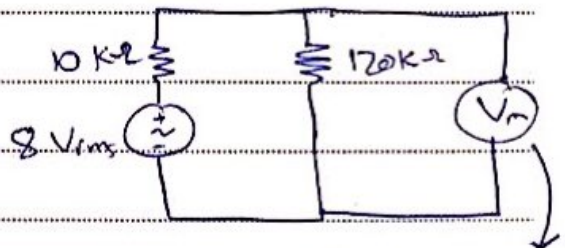
reading = 9V  $\Rightarrow$  9  $\pm$  0.3V  
 reading = 1V  $\Rightarrow$  1  $\pm$  0.3V  
 [analogue meter]

slide 73 Ex: A PMMC ...

V<sub>true</sub> voltage (ideal)

$$= 8 * \frac{120}{120K + 10K}$$

$$= 7.38V$$

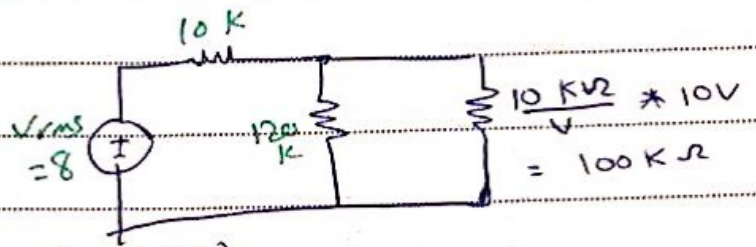


Analogue  
(0-10V)  
Sensitivity = 10K/V

measured value

V<sub>m</sub>  $\equiv$  calibrated to read  
V<sub>rms</sub> for sinusoidal [33]

measured value:



$$V_{\text{measured}} = 8 * \frac{(120K / 100K)}{(120K // 100K) + 10K}$$

$$= 6.76 \text{ V}$$

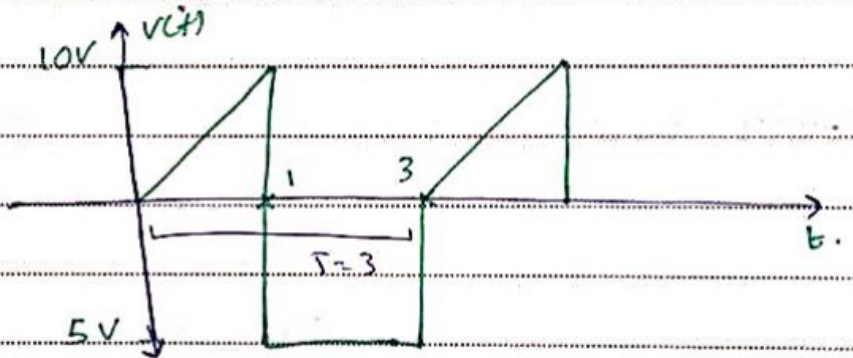
$$\% \text{ error} = \frac{6.76 - 7.38}{7.38} * 100\%$$

$$= -8.4\%$$

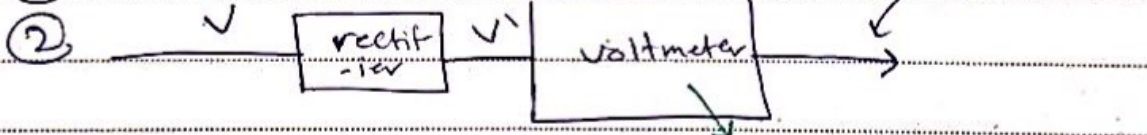
error =  $\frac{V_{\text{meas}} - V_{\text{desired}}}{V_{\text{desired}}}$

slide 73

EX2



①  $V_{\text{rms}}$



calibrated to read measure sinusoidal signal.

③ error in the rms reading?

Sol:

$$① V_{\text{rms}} = \sqrt{\frac{1}{3} \left[ \int_0^1 (10t)^2 dt + \int_1^3 (-5)^2 dt \right]} = 5.27 \text{ V}$$



$V_{avg}(\text{rectified signal}) = 25V$

$28.87 = 25V * 1.1 * \text{Correction Factor}$

$V_{rms} = \text{average} * \text{calibrated} * CF$

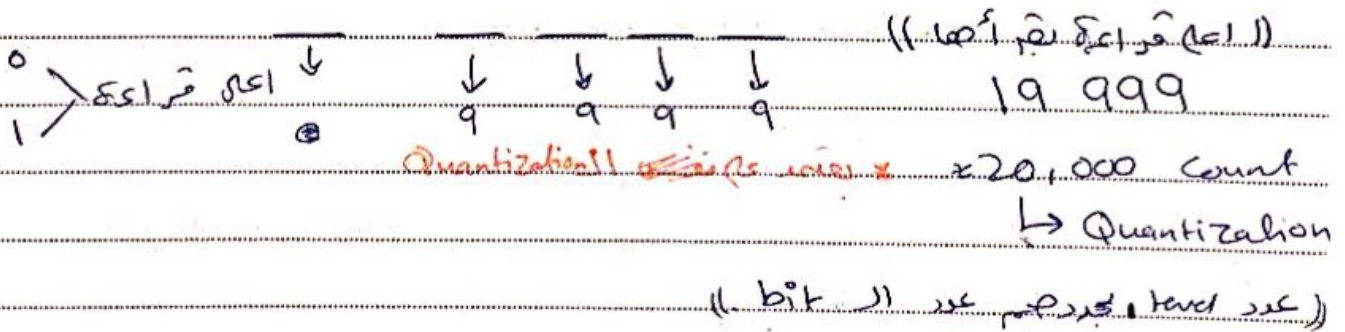
$CF = 1.04$

$((1.1) \rightarrow \text{calibrated} * CF)$

OR  $CF = \frac{SF_{\text{waveform}}}{SF_{\text{sinusoidal}}} \Rightarrow (rms/average = SF)$

Digital multimeter.

Ex 1 IF  $\Rightarrow$  4 1/2 digit multimeter

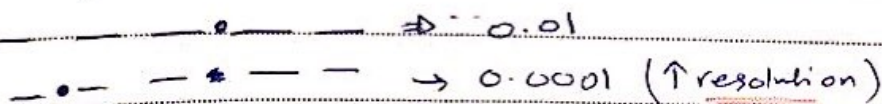


accuracy  $\Rightarrow$  percentage from reading

Accuracy =  $\pm 0.1\% \pm 1$

$\Rightarrow$  least significant digit (LSD)

$\uparrow$  Range  $\rightarrow$   $\downarrow$  resolution



\* max voltage  $< 2 \Rightarrow \underline{1.9999}$  (max display)  
 resolution  $\Rightarrow 0.0001 \Rightarrow 100 \text{ mV}$

to display 2V

0 2 . 0 0 0  
 resolution  $\rightarrow 0.001 \Rightarrow 1 \text{ mV}$

slide 81 | Example:-

4 1/2 digit.

reading 1.8000  
 accuracy ( $\pm 0.05\% \pm 1$ )

$$1.8000 * \frac{1.05}{100} = \underline{1.8009 \text{ V}}$$

$$1.8000 * \frac{0.95}{100} = \underline{1.7991 \text{ V}}$$

1  $\Rightarrow$  1 digit  $\Rightarrow$  LSD

1.8000  $\rightarrow$  0.0001

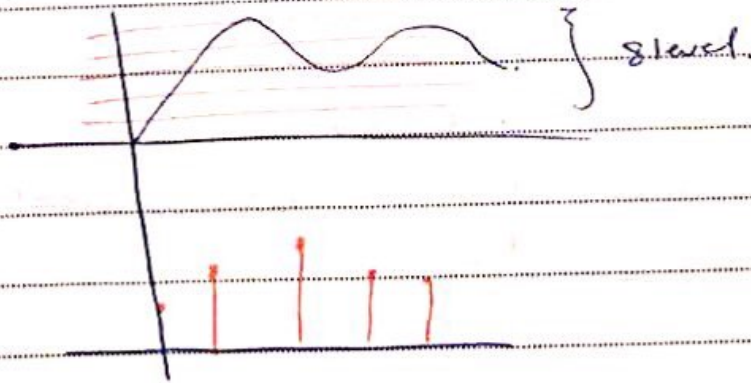
$$1.8009 \text{ V} \rightarrow 1.8009 + 0.0001 = 1.8010$$

$$1.7991 \text{ V} \rightarrow 1.7991 - 0.0001 = 1.7990$$

4 digit  $\Rightarrow$  (9  $\leftarrow$  0) no digit  $\rightarrow$  1) input



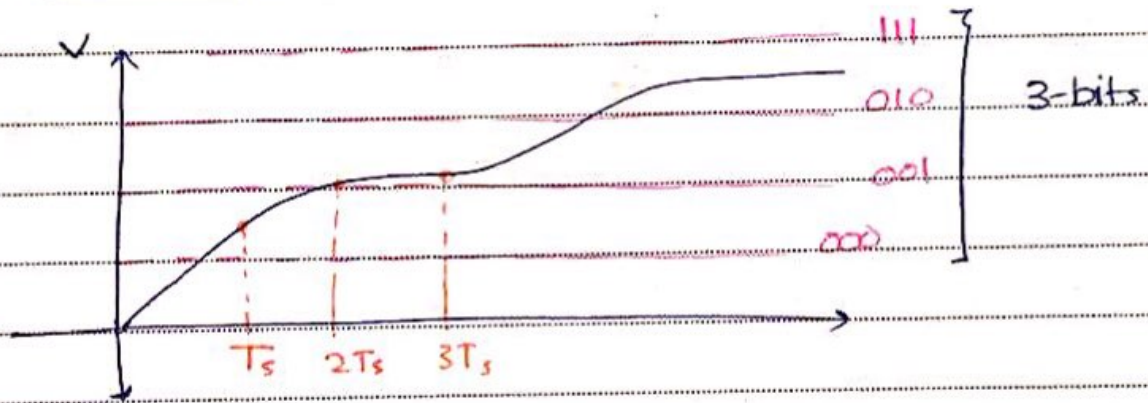
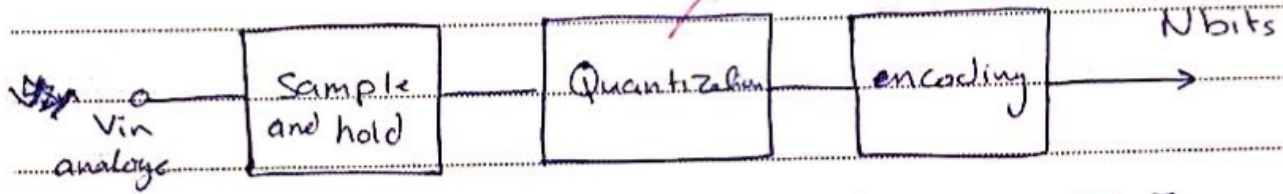
Subject



000 → L<sub>1</sub>  
 001  
 010  
 100  
 101  
 110  
 111 → L<sub>8</sub>

Slide Analogue to Digital Converter (ADC)

→ defined # of level



$T_s \triangleq$  Sampling time

$f_s \triangleq$  Sampling frequency  $\Rightarrow f_s = \frac{1}{T_s}$  Hz

# of levels =  $2^N$

Step size =  $\frac{V_{max} - V_{min}}{2^N}$

Quantization error =  $\frac{\Delta}{2}$

\* ADC 8 ~~bits~~



0V

Vref = 5V

3 bits  $\Rightarrow$  8 level

Vin = ?

Vref III

$$\Delta = \text{Step size} = \frac{V_{ref}}{2^N}$$

Resolution

3Δ 010

2Δ 001

$$V_{in} = \frac{V_{ref}}{2^N} \times (R)$$

Digital Code

Δ 000  
Step size

Digital Code

Slide : Digital Multimeter :-

[EX] Signal from ...

$$\text{max Quantization} = \frac{\Delta}{2}$$

$$\text{Quantization error \%} = \frac{\Delta/2}{V_{Full\ scale}} \times 100\%$$

$$= \frac{(V_{Full\ scale} / 2^N) / 2}{V_{Full\ scale}} \times 100\%$$

$$\text{Quantization error} = \frac{1}{2^{N+1}} \times 100\%$$

40



Sol Ex :-

800 mV  $\longrightarrow$  1500 mV

ADC

Code  $\Rightarrow$  80

150

 $\Delta \equiv$  Step size ?! or Fine resolution ?!

$$800 \text{ mV} = \Delta 80$$

$$\Delta = 10 \text{ mV}$$

Slide: Accuracy

$\uparrow$  accuracy  $\uparrow$  #obits (level)

\* Sampling rate  $\Rightarrow$  different between the 2 figure

slide: Ramp-Type Digital Voltmeter

"Voltage to time conversion"

$$V(t) = V_0 - mt$$

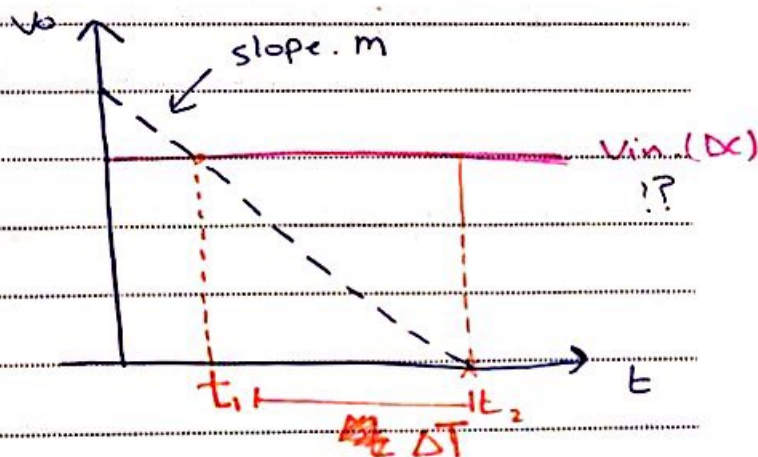
at  $t_1 \Rightarrow$ 

$$V_{in} = V_0 - mt_1 \quad \dots (1)$$

at  $t_2 \Rightarrow$ 

$$V_{in} = V_0 - mt_2$$

$$0 = V_0 - mt_2 \quad \dots (2)$$

time  $\leftarrow$  Volt  $\rightarrow$   $\times$ 

$$V_{in} = m(t_2 - t_1)$$

41

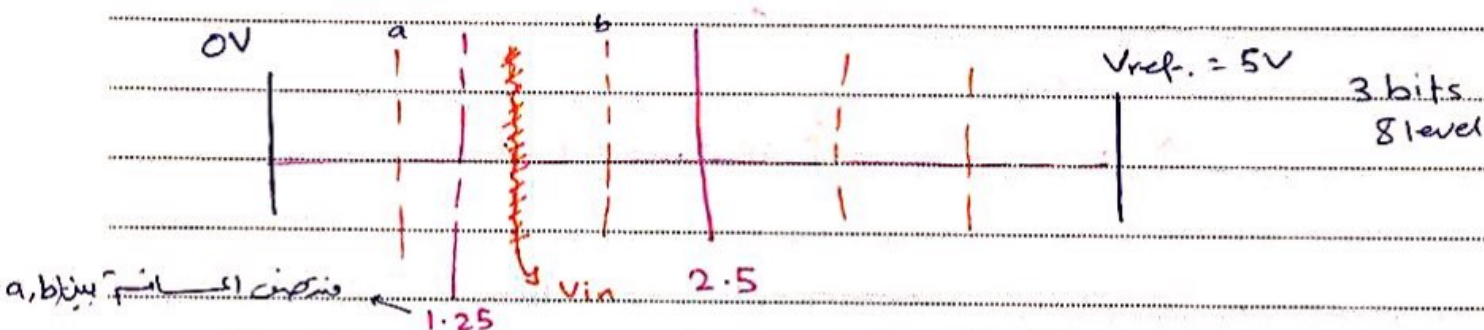
$$\Delta T = \frac{V_{in}}{m}$$

error إذا كان  $V_{in}$  في اليمين يتقلص  $V_{in}$  في اليمين يتقلص  $V_{in}$  في اليمين يتقلص  
 disadvantages  
 ramp slope

$$\Delta T = n T_s$$

$$V_{in} = m n T_s$$

Slide: Successive Approximation



Suppose  $V_{in}$  between 0 and 2.5

\* Compare with 2.5V  $\Rightarrow$  0 bit

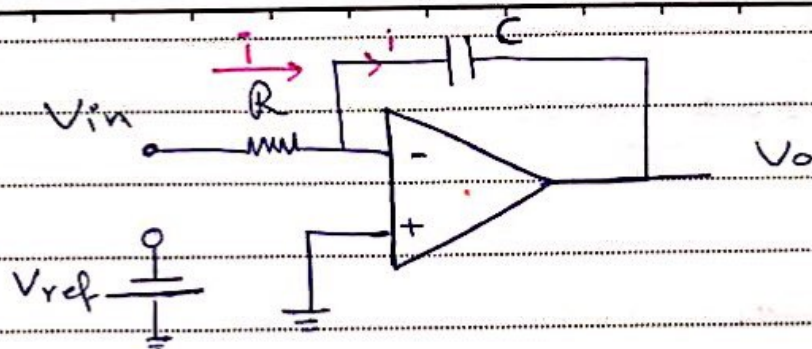
\* Compare with 1.25V  $\Rightarrow$  1 bit

" 1.25  $V_{in}$  "

\* Compare with  $\Rightarrow$  0 bit

MSD  $\Rightarrow$  010

Slide: Dual-slope digital voltmeter



charging  $\rightarrow$  voltage output  $\uparrow$

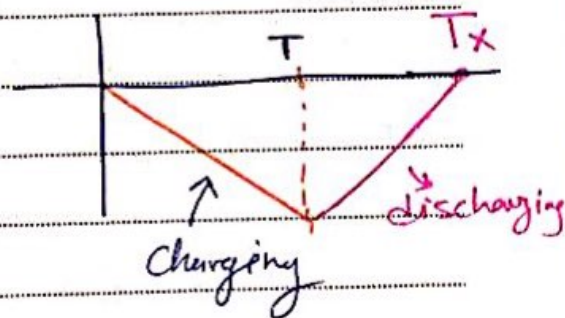
$$i_c = C \frac{dv}{dt}, \quad v = \frac{1}{C} \int C i_c dt = \frac{1}{C} \int \frac{V_{in}}{R} dt$$

$$V_c = \frac{1}{R_c} \int V_{in} dt$$

$$V_c + V_o = 0$$

$$V_o = -\frac{1}{R_c} \int V_{in} dt$$

$T \rightarrow$  "defined"



$$V_o = -\frac{1}{R_c} \int -V_{ref} dt + V_{initial} = 0$$

$$0 = \frac{V_{ref}}{R_c} T_x - \frac{V_{in}}{R_c} * T$$

*loop*

$$T_x = \frac{V_{in} T}{V_{ref}}$$

$$V_{in} = \frac{T_x * V_{ref}}{T}$$

Slide: Dual-Slope ...

[Ex] A digital slope ...

$$V_{ref} = 10V, T = 10ms$$

$$T_{conversion} = T + T_x$$

$$T_x = \frac{V_{in} T}{V_{ref}} = \frac{6.8 * 10ms}{10} = 6.8ms$$

$$T_{conversion} = 10ms + 6.8ms = 16.8ms$$

[Ex] A dual slope ---

$$V_{in} = ?$$

$$V_{in} = \frac{T_x * V_{ref}}{T}$$

Slide Meter Types:-

- \* Residential Energy kWh.
- \* power  $\Rightarrow$  Industrial, Capacitive charge P
- \* penalty PF  $\Rightarrow$  PF = 0.88 "Industrial" 44

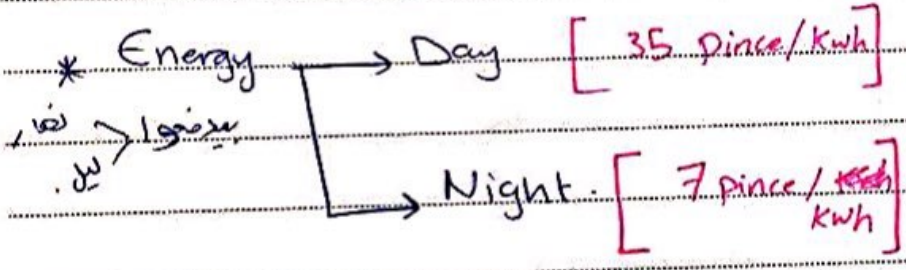
Generat

18/7  
8PM

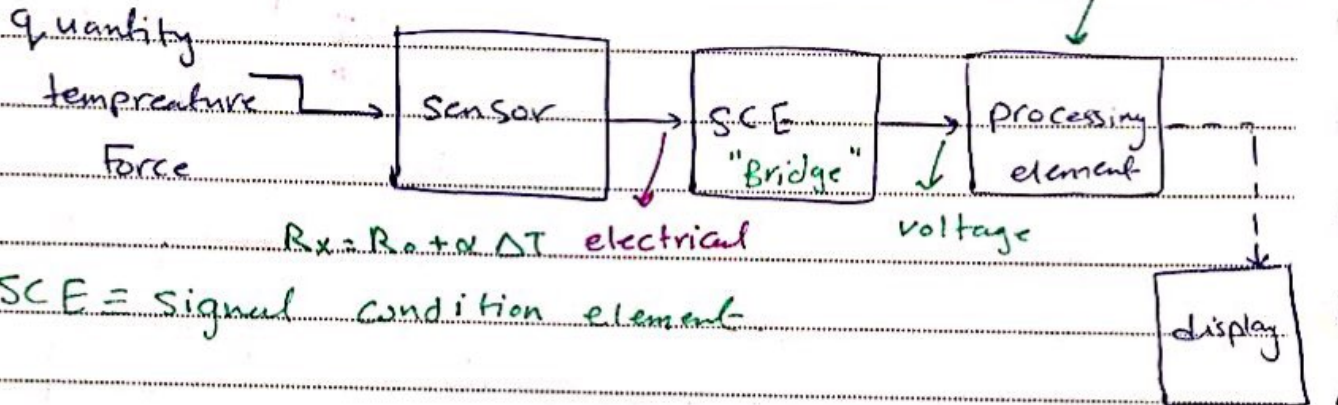
transmit

distributed

industrial



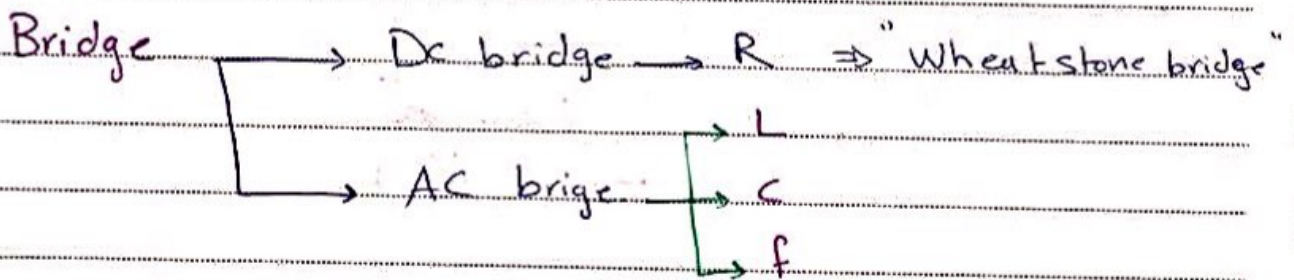
Bridge:-



SCE = Signal condition element

$R_x = R_0 + \alpha \Delta T$  electrical

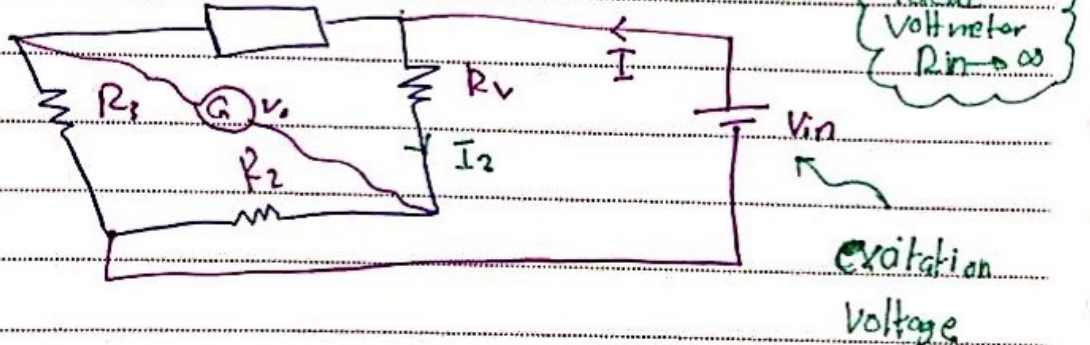
- Reactance
- Inductive
- Capacitor
- Frequency
- phase.



" voltage ...  $R_x$  "

"Wheatstone bridge" → balanced  
 → unbalanced.

Wheat Stone bridge  $R_x$  sensor  $R_x??$



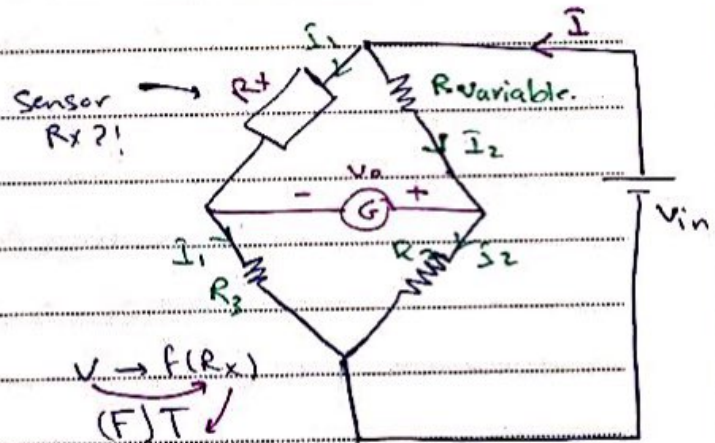


Null method (balanced)

Deflection method (unbalanced)

$$V_o = V_{in} \left( \frac{R_x}{R_x + R_3} \right) - V_{in} \left( \frac{R_v}{R_v + R_2} \right)$$

$$V_o = V_{in} \left( \frac{R_x}{R_x + R_3} - \frac{R_v}{R_v + R_2} \right)$$



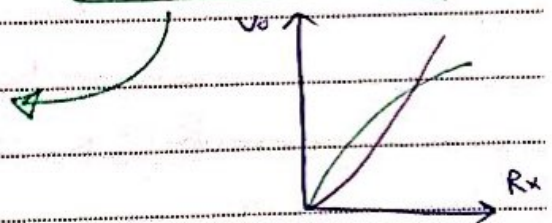
Null method: ( $R_v \rightarrow \Rightarrow V_o = 0$ ) "balanced"

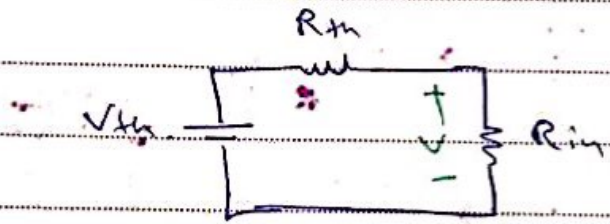
$$V_o = 0 \rightarrow V_{in} \left( \frac{R_x}{R_x + R_3} - \frac{R_v}{R_v + R_2} \right) = 0$$

$$\frac{R_x}{R_x + R_3} - \frac{R_v}{R_v + R_2} \Rightarrow R_x R_v + R_x R_2 = R_v R_x + R_v R_3$$

$$R_x R_2 = R_v R_3$$

$$R_x = \frac{R_v R_3}{R_2}$$





\* Deflection method :-

resistance control جي قيمت جي Voltage جي قياس

$R_v$  replaced  $R_1$  (Nominal  $R_x$ )

$$V_o = V_{in} \left( \frac{R_x}{R_x + R_3} - \frac{R_1}{R_1 + R_2} \right)$$

$C$   
 $C = f(R)$   
 $R_x (RT)$

Case 1  $R_2 = R_3$

$R_x = R_1$  (Nominal)  $\Rightarrow V_o = 0$

$\rightarrow R_x = R_1 + \Delta R_x$   $\begin{cases} V_o (+ve) \\ V_o (-ve) \end{cases}$

((nominal) ke value ke nominal ke value ke  $R_x$  ke value ke)

**Ex**

pressure sensor measure pressure (0-10 bar)

$R_x = 120 + \frac{338 \cdot m\Omega}{bar}$   $\rightarrow R_v = \infty$   
voltage meter

nominal.

maximum current sensor  $\leq 30 \text{ mA}$   
( $R_x$ )

Find  $V_o$  when pressure is 10 bar and max  $V_{in}$  is used?

- Deflection method.

$R_1 = R_2 = R_3 = 120 \Omega$



$$I_1 \leq 300 \text{ mA}$$

$$\frac{V_{in}}{R_x + R_3} \leq 300 \text{ mA}$$

$$\frac{V_{in}}{120 + 120} \leq 300 \text{ mA}$$

$$V_{in} \leq 7.2 \text{ V}$$

10 bar

$$R_x = 120 + 0.338 \times 10$$

$$= 120 + 3.38 = 123.38 \Omega$$

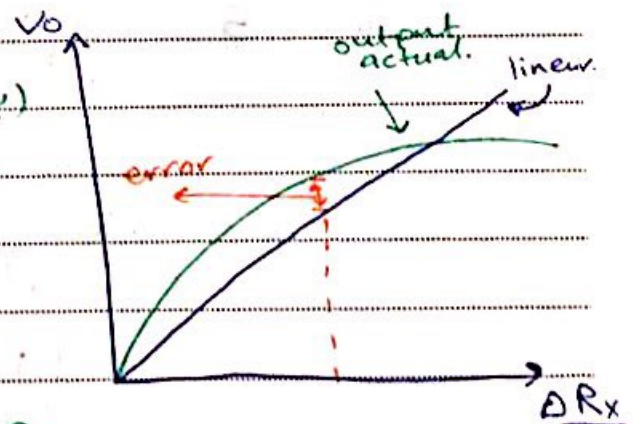
$$V_o = V_{in} \left( \frac{R_x}{R_x + R_3} - \frac{R_1}{R_1 + R_2} \right)$$

$$V_o = 50 \text{ mV}$$

at 0 bar  $\rightarrow V_o = 0 \text{ V}$

\* output actual ( $\Delta R_x$  vs  $V_o$  vs bar)

Case 8  $\Delta R_x$  is small compared  
nominal



$$V_o = V_{in} \left( \frac{R_x}{R_x + R_3} - \frac{R_1}{R_1 + R_2} \right) \dots (1)$$

nominal  $\Delta R_x$  is small

$$V_o' = V_{in} \left( \frac{R_x + \Delta R_x}{R_x + \Delta R_x + R_3} - \frac{R_1}{R_1 + R_2} \right) \dots (2)$$

$$\delta V_o = f(\delta R_x)$$

$$R_x + \underbrace{\delta R_x}_{\text{small}} \approx R_x$$

$$\delta V_o = V_o' - V_o'' \quad (1) - (2)$$

$$\delta V_o = \frac{\delta R_x}{R_x + R_3} V_{in}$$

من العلاقة يتبين بان التغيرات في المقاومة قليلة

$$\frac{\delta V_o}{\delta R_x} = \frac{V_{in}}{R_x + R_3} \Rightarrow \text{sensitivity bridge.}$$

Ex

A resistance thermometer ( $0^\circ \rightarrow 50^\circ \text{C}$ )

$R_{\text{nominal}} = 500 \Omega$  at  $0^\circ \text{C}$

$$\Delta R = \frac{4 \Omega}{1^\circ \text{C}}$$

$$R_1 = R_2 = R_3 = 500 \Omega, V_{in} = 10 \text{V}$$

$$R_x = 500 + 4T$$

↳ temperature.

$$V_o = V_{in} \left( \frac{R_x}{R_x + R_3} - \frac{R_1}{R_1 + R_2} \right)$$

$$V_o = 10 \left( \frac{125 + T}{250 + T} - 0.5 \right) \quad (V_o \propto T \text{ non linear})$$

$$\text{at } T = 0 \rightarrow V_o = 0$$

$$\text{at } T = 25^\circ \text{C} \rightarrow V_o = 0.455 \text{V}$$

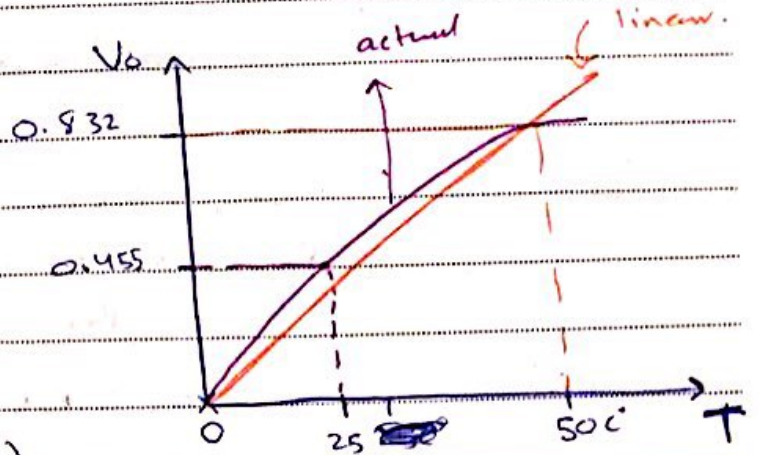
$$\text{at } T = 50^\circ \text{C} \rightarrow V_o = 0.833 \text{V}$$

50

Subject

$$V_o = 0.016T$$

$$V_o = 10 \left( \frac{125+T}{250+T} - 0.5 \right)$$



بي اطلع ال max  $\rightarrow$  تف دباري 0.5

# DC Bridge

measurement error

Balanced  $R_2 R_3 = R_x R_1$

$$R_x = \frac{R_2 R_3}{R_1}$$

tolerance  $R_2 = R_2 \pm \Delta R_2$

$$R_3 = R_3 \pm \Delta R_3$$

$$R_1 = R_1 \pm \Delta R_1$$

\* limiting error :-

$$R_x = \frac{(R_2 \pm \Delta R_2)(R_3 \pm \Delta R_3)}{(R_1 \pm \Delta R_1)}$$

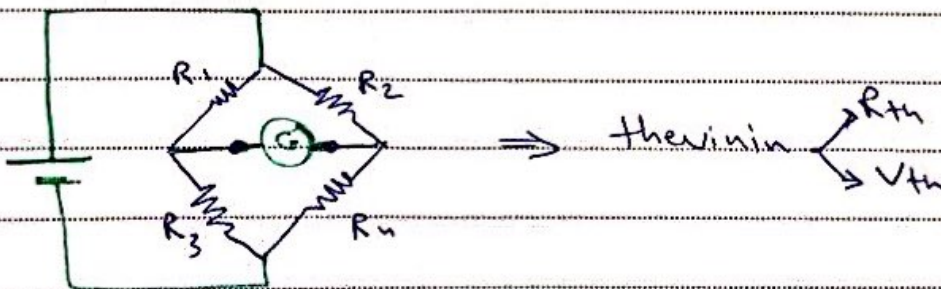
approximation ( $\Delta R_2 \times \Delta R_3 \approx 0$ )

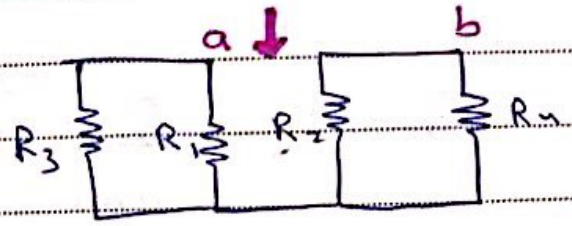
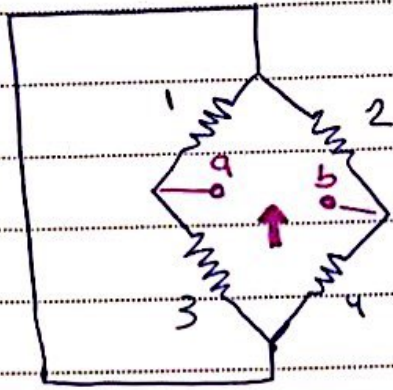
$$R_x = \frac{R_3 R_2}{R_1} \left( 1 \pm \frac{\Delta R_1}{R_1} \pm \frac{\Delta R_2}{R_2} \pm \frac{\Delta R_3}{R_3} \right)$$

for that it's  $\left[ \begin{array}{l} (+ve) \\ (-ve) \end{array} \right]$   $R_{x \max}$   $R_{x \min}$   
 called limiting error

Example : study !!

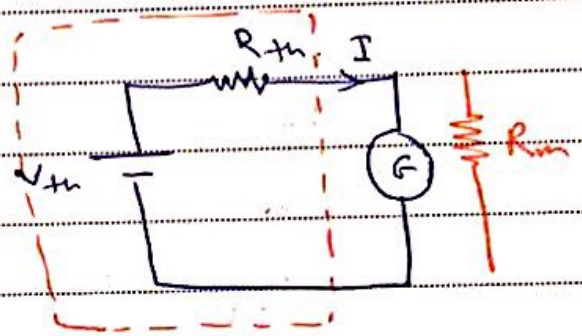
\* Sensitivity for Galvanometer :-



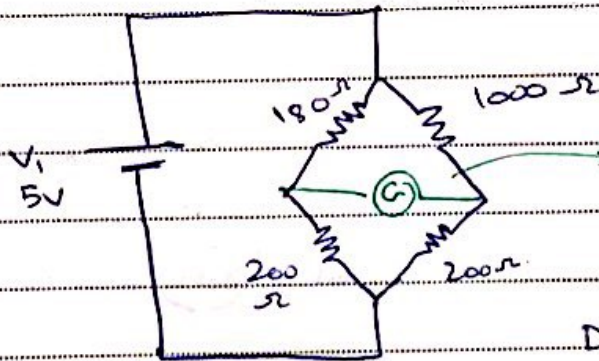


$$R_{th} = (R_1 // R_3) + (R_2 // R_4)$$

$$V_{th} = V_s \left( \frac{R_1}{R_1 + R_3} - \frac{R_2}{R_2 + R_4} \right)$$



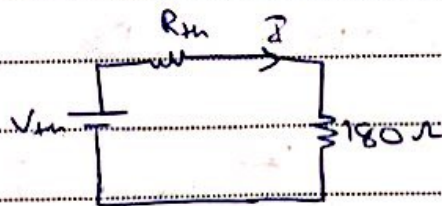
Example 1:-



Sensitivity  $\frac{10 \text{ MM}}{1 \text{ MA}}$

Deflection by the Galvano meter ?

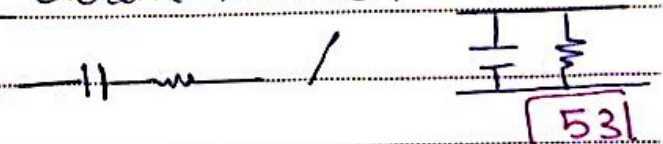
Example 2:-



Capacitor:

(AC bridge)

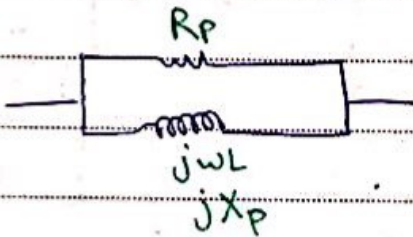
$\epsilon, \sigma$  dielectric material.



# \* Quality factor $Q$

Quality =  $\frac{\text{energy stored}}{\text{average energy dissipated}}$

dissipation factor =  $\frac{\text{energy lost}}{\text{energy stored}} = \frac{1}{Q}$



$Z_{eq} = R_p \parallel jX_p$

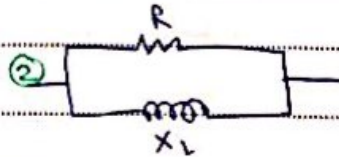
$Z_{eq} = \frac{R_p X_p^2 + j X_p R_p}{R_p^2 + X_p^2} = R_s + j X_s$



Quality factor:  $\textcircled{1} \frac{R}{\omega L}$

$\textcircled{1} \therefore Q = \frac{|\hat{I}|^2 \cdot X_L}{|\hat{I}|^2 \cdot R} = \frac{\omega L}{R}$

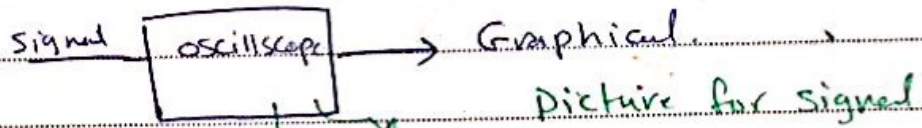
$\textcircled{2} Q = \frac{V^2 / X_L}{V^2 / R}$



$Q = R / X_L$

Balanced  $Z_1 Z_4 = Z_2 Z_3$    
 } magnitude   
 } phase

\* Slide oscilloscope :



ADC voltage

\* CRO Analogue oscill.

10:1

down scale for signal.

(voltage division)  $\Rightarrow$  down 1 below 10 times \*

volt. scale  $\Rightarrow$   $\frac{1}{10}$  of the original

$\downarrow$  f.c  $\rightarrow$  a (V division)

"Attenuation for prob"

$\uparrow$  input impedance  $\downarrow$  error

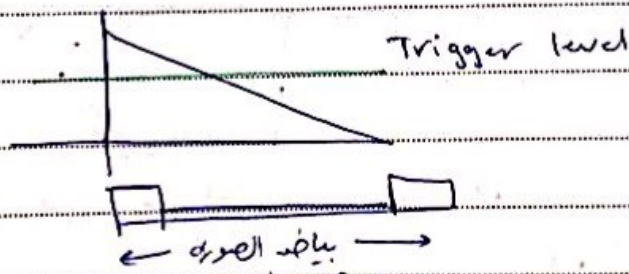
scale  $\rightarrow$  V division

\* 1 cycle  $\rightarrow$  Time division

up/down  $\rightarrow$  volt division

\* 8 vertical division  $\Rightarrow$  Max peak to peak = 8

\* trigger :

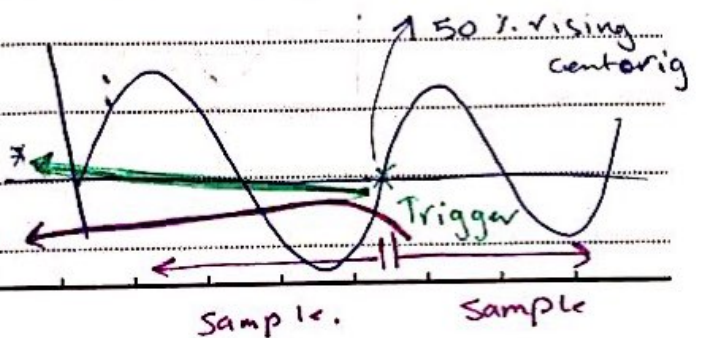


(Trigger  $\rightarrow$  Peak to Peak)

Trig = Rising and 50%

centering (5 Trigger level)

centering (5 Trigger level)



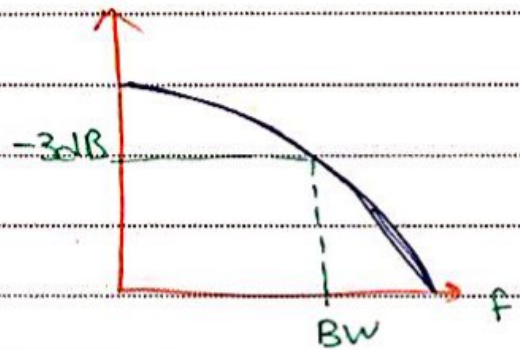




$\vec{u}_{ep} \vec{u}_{\omega} \vec{u}_{N\omega} \vec{u}_{\omega} \leftarrow \text{distortion } \vec{u}_{ic} \vec{u}_{\omega} \leftarrow \text{(2) } \vec{u}_{L} \vec{u}_{\omega} *$   
 Signal  $\omega$

for figure (2)  $\Rightarrow x(t) = A \cos(\omega_1 t) + A_2 \cos(\omega_2 t)$

(1)  $\Rightarrow x(t) = A \cos(\omega_1 t)$   
 $A_2 \cos(\omega_2 t) \ll A$

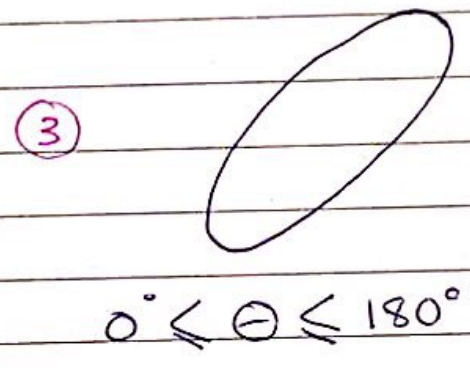
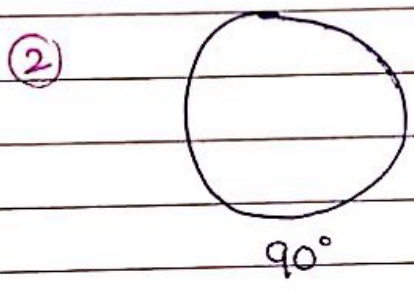
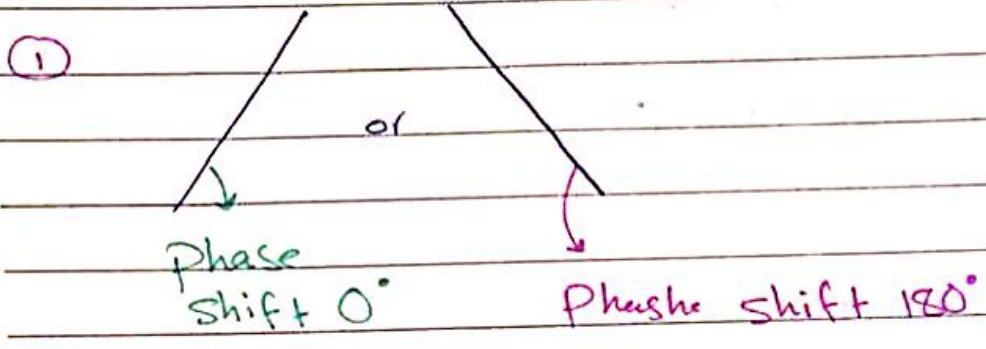


XYZ of oscilloscope  $z$ : intensity (  $\frac{\delta^2}{\text{cell}}$  )

CATHODE  $\Rightarrow \vec{u}_{ic}$  2 deflection  $\left[ \begin{array}{l} \rightarrow \text{vertical} \\ \rightarrow \text{Horizontal} \end{array} \right.$

# Oscilloscope (X-Y mode) :-

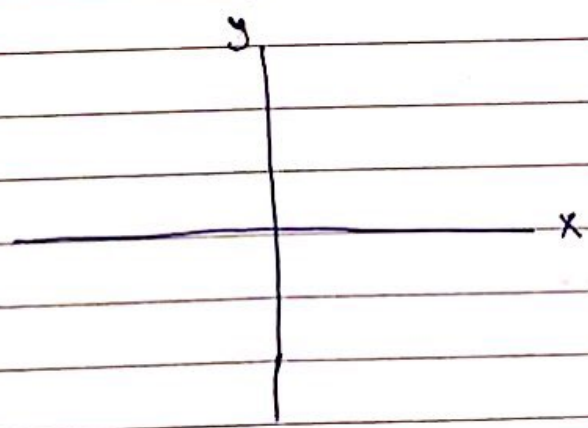
if we insert a sinusoidal signal. 3 possible cases in the X-Y mode are



[Ex]

$$x = \sin \omega t$$

$$y = \cos \omega t$$



→ Zero crossing (x=0) :-

$$x = \sin \omega t = 0 \quad \omega t = 0, \pi$$

$$y(\omega t = 0) = 1 \Rightarrow (0, 1)$$

$$y(\omega t = \pi) = -1 \Rightarrow (0, -1)$$

\* ~~Max~~  $(y=0)$   $\Delta$

$$\cos wt = 0 \rightarrow wt = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$X(wt = \frac{\pi}{2}) = 1 \Rightarrow (1, 0)$$

$$X(wt = \frac{3\pi}{2}) = -1 \Rightarrow (-1, 0)$$

Max y :

$$\max \cos(wt) \Rightarrow wt = 0$$

$$X(0) = 0 \Rightarrow (0, 1)$$

$$Y(0) = 1$$

Max X :

$$\max \sin wt \Rightarrow wt = \frac{\pi}{2}$$

$$X(\frac{\pi}{2}) = 1$$

$$\Rightarrow (1, 0)$$

$$Y(\frac{\pi}{2}) = 0$$

Min X :-

$$\min \sin wt \Rightarrow wt = \frac{3\pi}{2}$$

$$Y(\frac{3\pi}{2}) = 0$$

$$\Rightarrow (-1, 0)$$

$$X(\frac{3\pi}{2}) = -1$$

Min y :-

$$\min \cos wt \Rightarrow wt = \pi$$

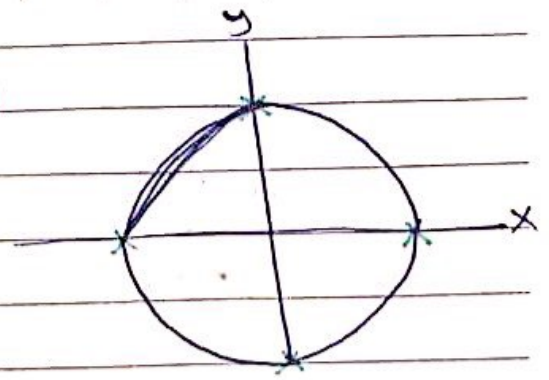
$$X(\pi) = 0$$

$$Y(\pi) = -1 \Rightarrow (0, -1)$$

[60]

So we have :

$$(0, 1), (1, 0), (0, -1), (-1, 0)$$



**Ex**

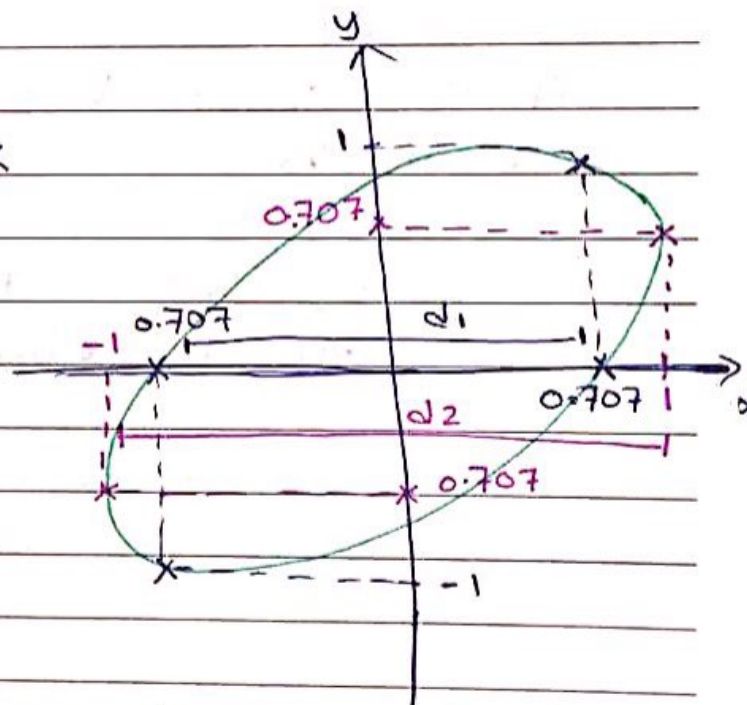
$$x = \cos(\omega t)$$
$$y = \cos(\omega t - 45^\circ)$$

Do the same steps as the previous example.

$$d_1 = \text{zero crossing}$$
$$d_2 = \text{peak to peak}$$

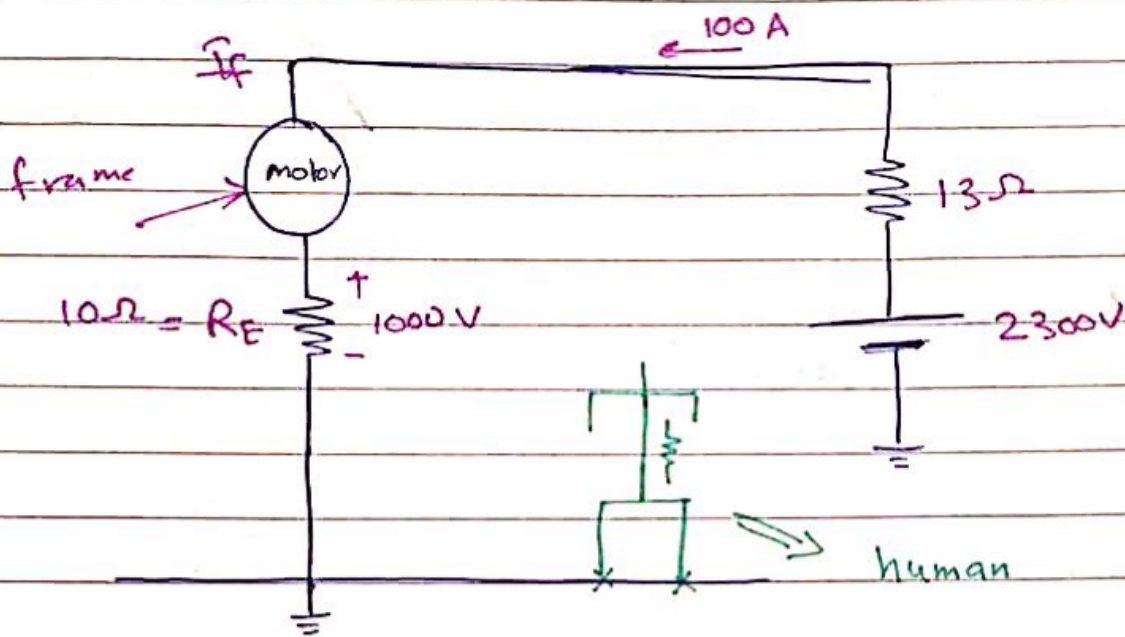
from  $d_1$  and  $d_2$  we evaluate the phase shift.

$$\theta = \sin^{-1}\left(\frac{d_1}{d_2}\right)$$



Note: also we could use the y-axis to find the phase shift with the same way.

## \* Earthing :



if the human touch the motor after a fault happend we protect him:

- ① by wearing a safty shoes.
- ② by using Tire to clear fault.
- ③ by reducing  $R_E$ .

\* The conductor between motor and the earth.  
⇒ must be able to carry the fault current.

0 → 10 mA (No Impact)

150 mA → 200 mA (dead).

## \* Electrical shock:-

difference in the voltage and will create a path of current.

The worst path for current passing through the human, that between human hands

(since it will pass through the heart).

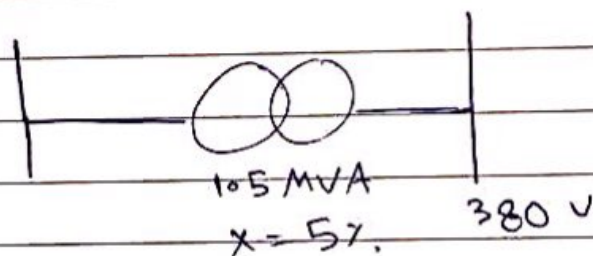
current relation that related to human to has No impact from the current:-

$$I = \frac{116 \text{ mA}}{\sqrt{t}}$$

time to clear fault

max safe current

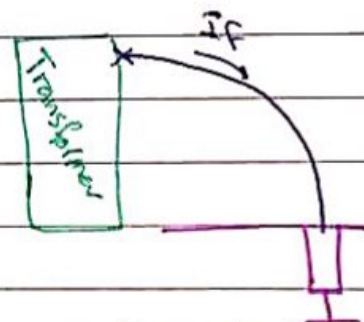
Ex



3-phases transformer

Find  $I_f$  ?!

Find cross section ?!



Sol:-

$$I_f = \frac{1}{X\%} \times \text{full load current}$$

with stand =  
fault current :  
cross section.

$$\text{full load current} = \frac{1.5 \text{ M}}{\sqrt{3} \times 380}$$

$$I_f = 20 \times \frac{1.5 \text{ M}}{\sqrt{3} \times 380}$$

$$I_f \approx 45 \text{ KA}$$

63

$$\text{Cross section (mm}^2\text{)} = 9 * \sqrt{E} * I_f$$

$t =$  time to clear fault

assume  $t = 0.5$  sec.

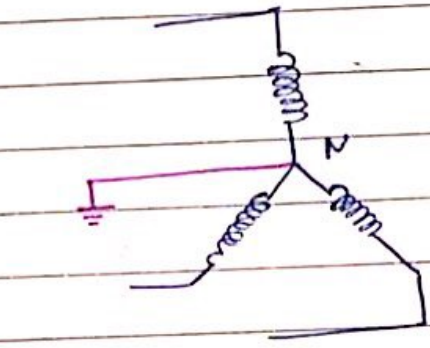
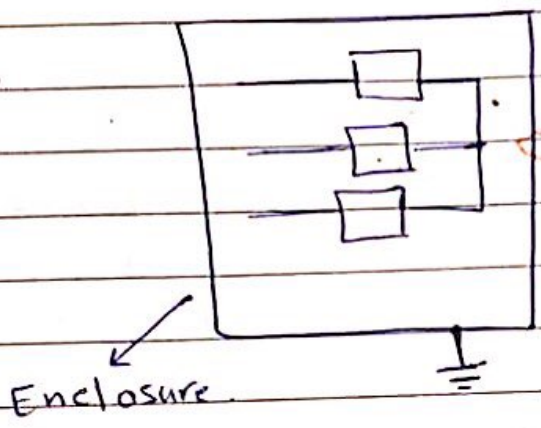
$$\text{Cross section (mm}^2\text{)} = 9 * \sqrt{0.5} * 45k.$$

$$\text{Cross Section} = 286 \text{ mm}^2$$

84

# Grounding :-

Connecting anet work point to the ground through as impedance.

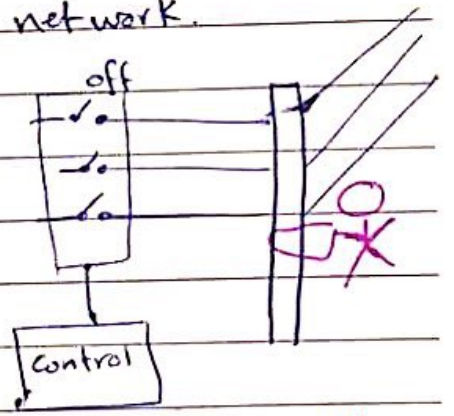


\* توہر سار آتے اور fault current

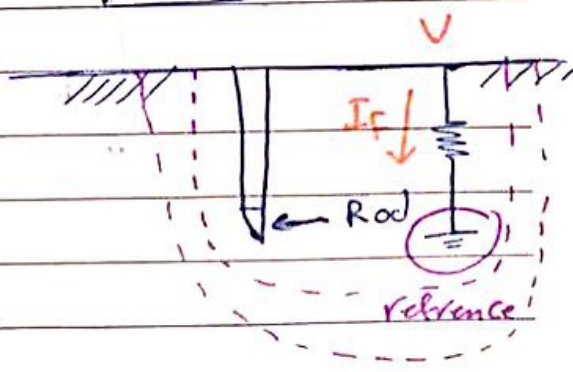
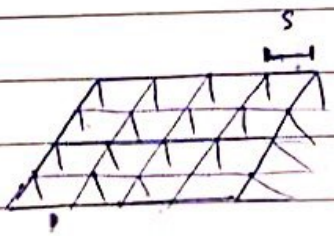
## Grounding

- Safety unenergized element.
- performance of the network.

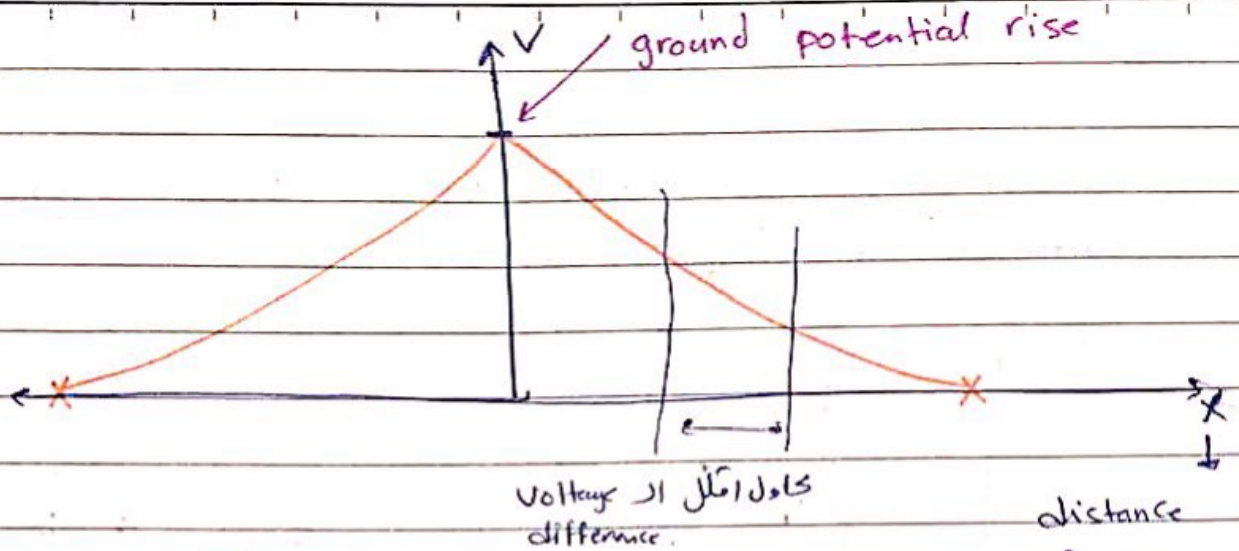
فولٹ سے بچانے کے لیے ← fault  
 وولٹیج کی فرق ← voltage difference  
 "اگر کسی جگہ پر" ← "اگر کسی جگہ پر"



## \* Safety :-



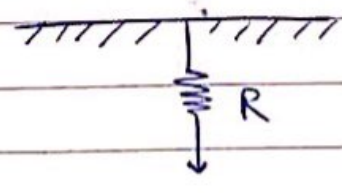
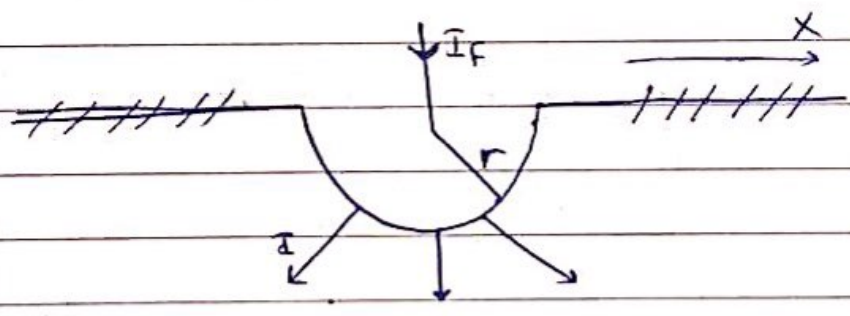




Safety means:

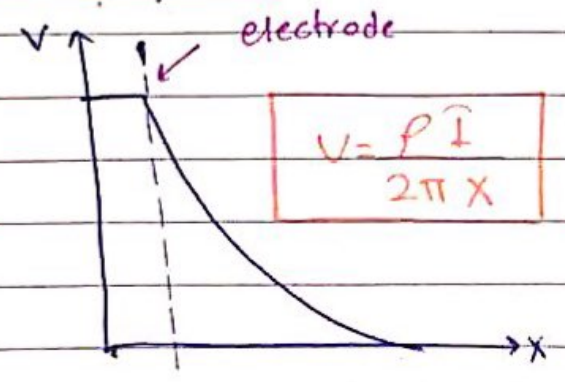
- Insulation (Gloves, boots)
- Grounding  $\Rightarrow$  reduce GPR "ground potential rise"
- equipotential rise  $\Rightarrow$  reduce voltage difference in the site.

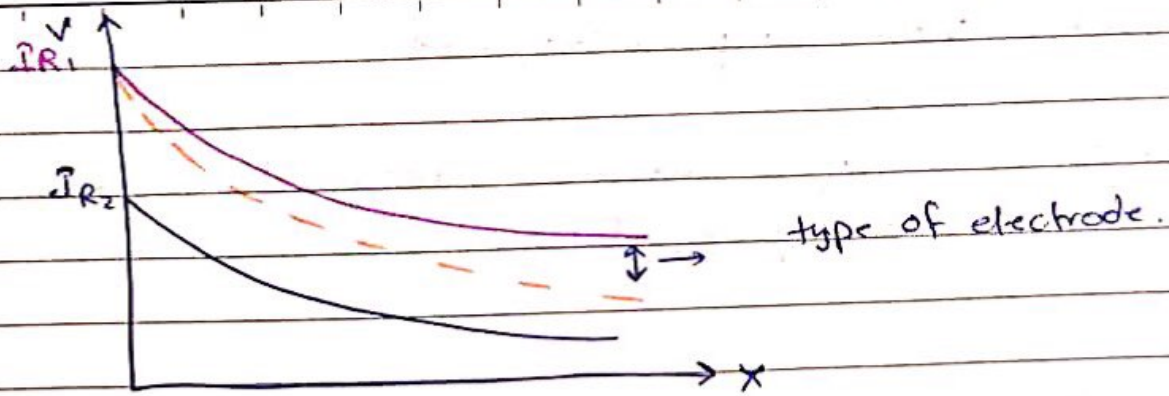
Hemispherical electrode :-



$$R = \frac{\rho}{2\pi r} \Omega$$

$\rho \equiv$  soil resistivity

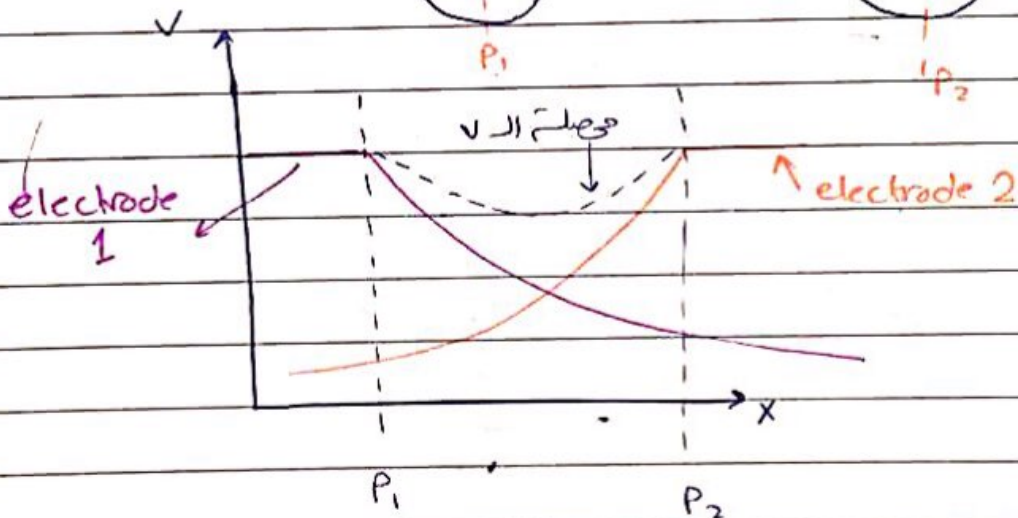
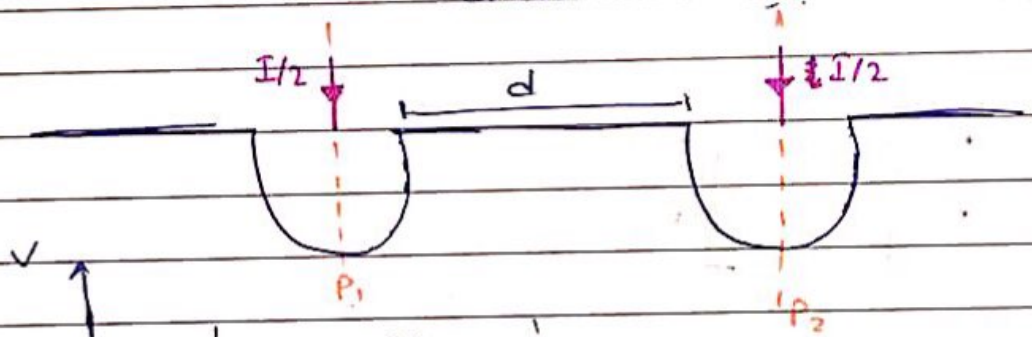




الفتر بين - - - - - المقاومة  $R$  في النوعين من Electrode

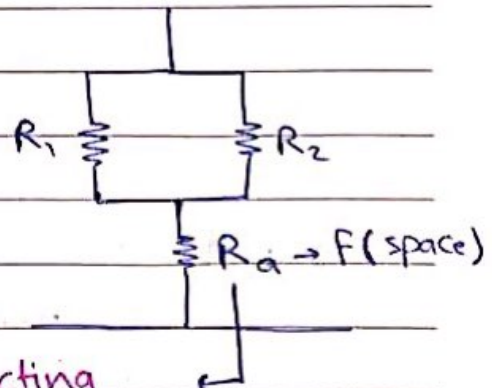
$\downarrow IR_2 \rightarrow \downarrow$  voltage difference

في أقل المقاومة  $R_{eq}$  بين Electrode



$\uparrow d \rightarrow R \downarrow$

المقاومة  $R_1, R_2$  في النوعين من Electrode  
 المقاومة  $R$  في النوعين من Electrode  
 المقاومة  $R_a$  في النوعين من Electrode



$$R_{eq} = \frac{R}{N \cdot \gamma}$$

interacting resistance

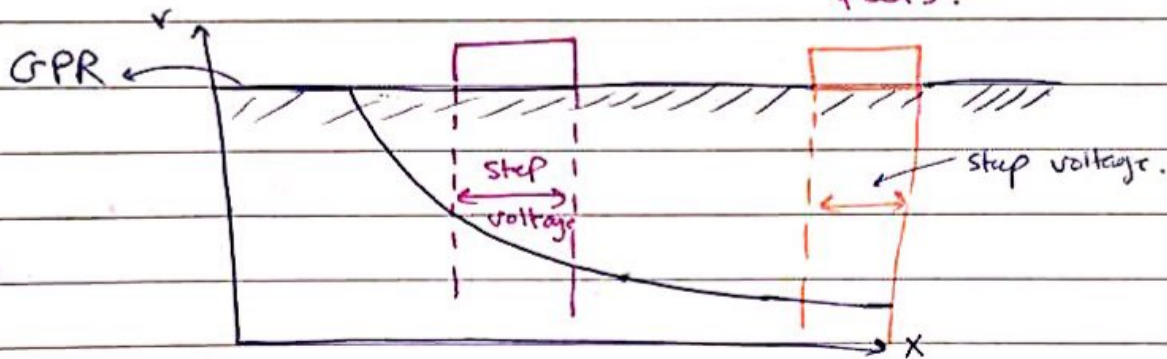
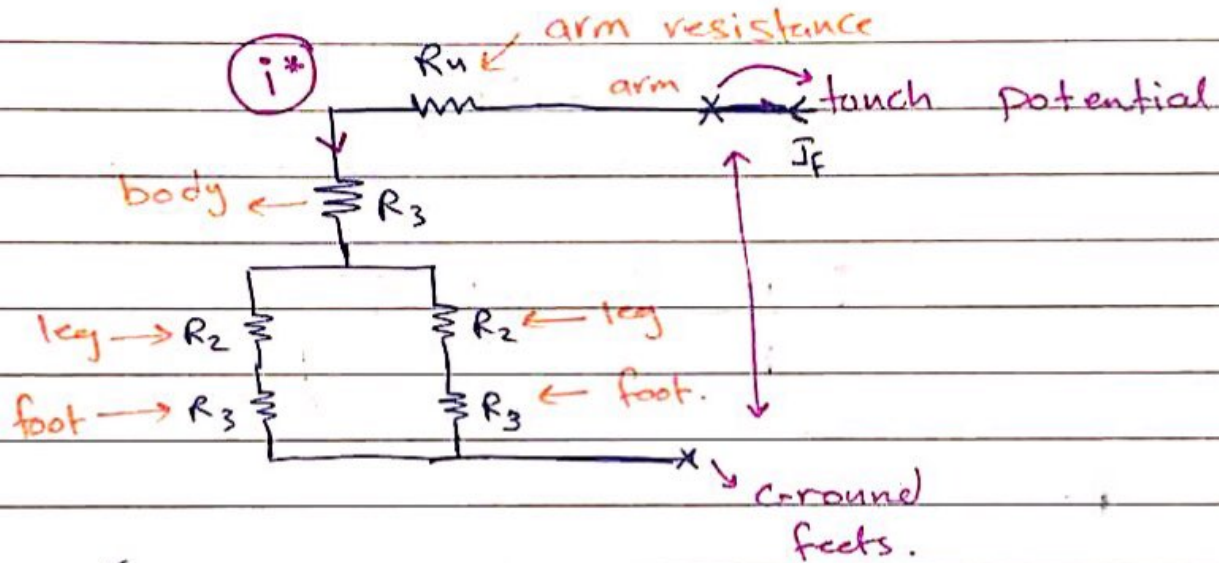
$\gamma \Rightarrow$  efficiency  $\rightarrow$  depend on space.

$\downarrow \gamma \rightarrow R_{eq} \uparrow$  ( $\downarrow \gamma \rightarrow$  space  $\downarrow$ )

## \* touch and step voltage 88

**touch** = voltage difference between your hand and your feet

**voltage** = voltage difference between your feet.



step voltage.  $\int \dots$

## \* IEEE 8

$< 1 \text{ mA} \rightarrow$  No sensation.

$1 - 8 \text{ mA} \rightarrow$  sensation of "shock"

$8 - 15 \text{ mA} \rightarrow$  painful shock.

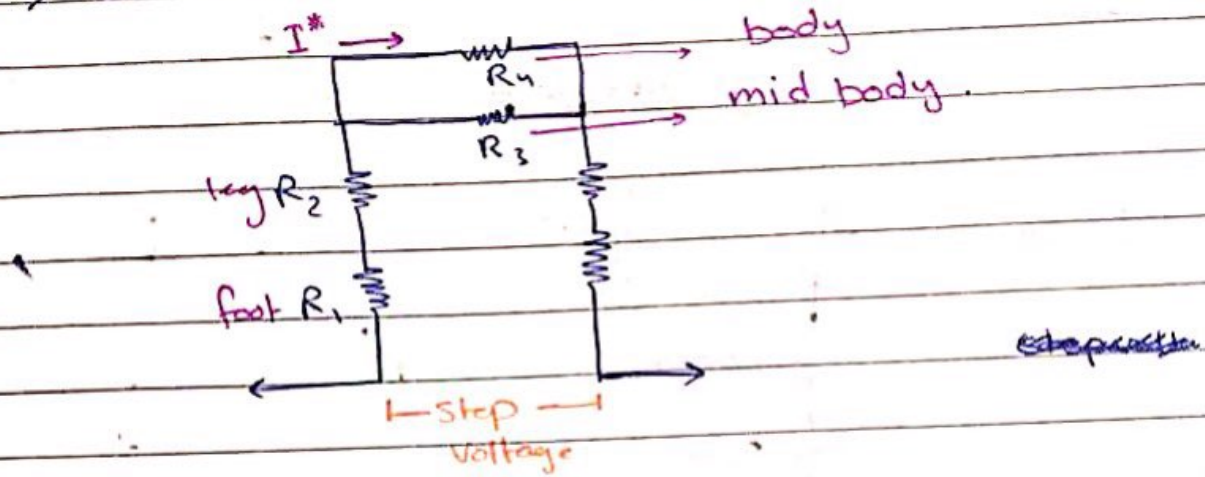
$15 - 20 \text{ mA} \rightarrow$  loss of muscle control

$20 - 50 \text{ mA} \rightarrow$  muscle failure.

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50 - 200 mA  $\rightarrow$  heart failure.

> 200 mA  $\rightarrow$  death and burns.

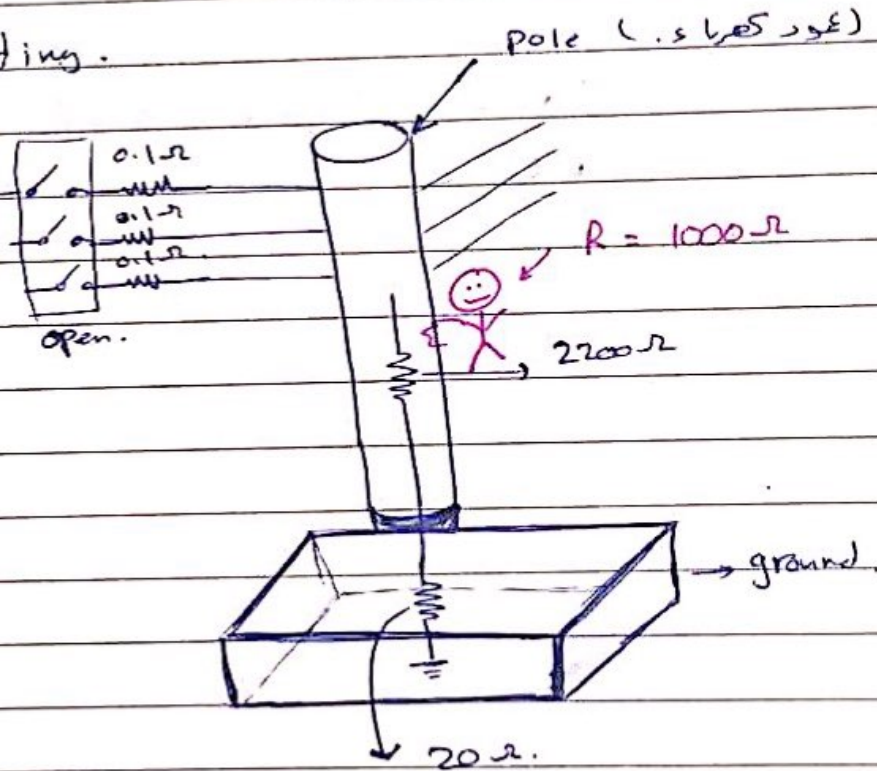


### Grounding and Bonding.

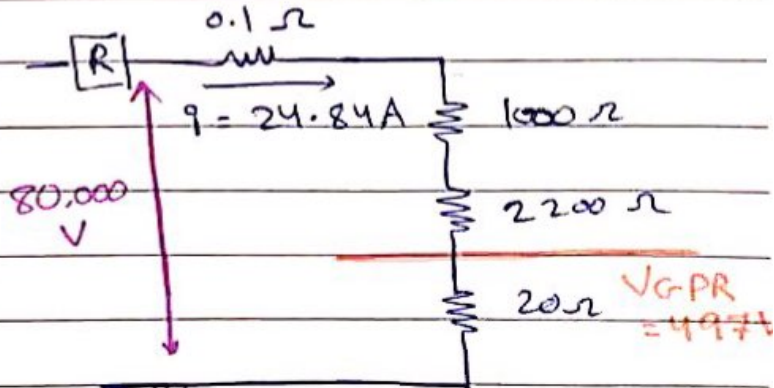
Ex:

\* code of practice.

VLG = 80KV.

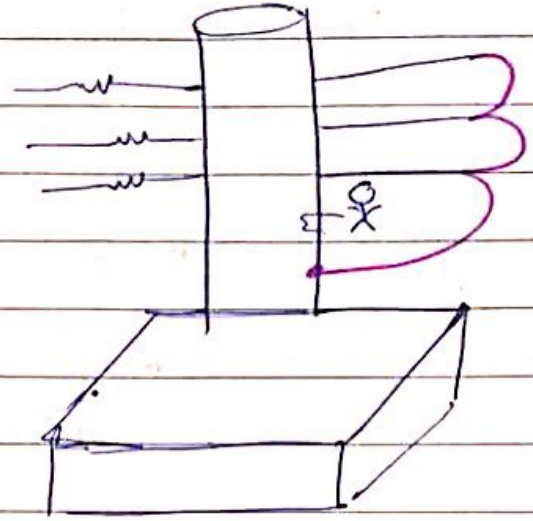
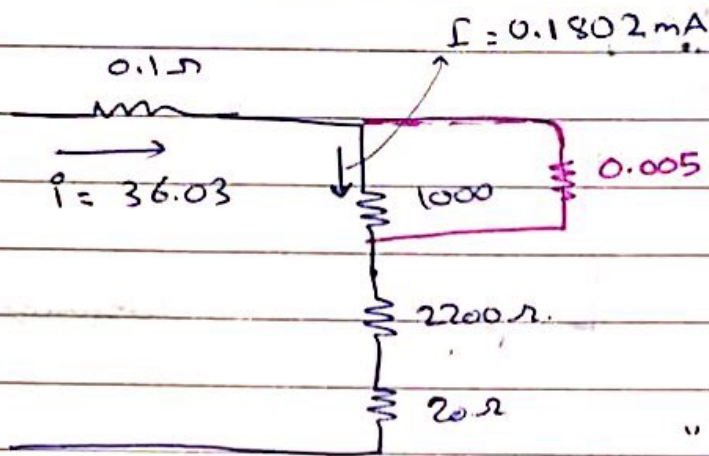


$i \Rightarrow$  small compared to the setting of the relay protection.



# Equipotential Bonding.

Solution  $\Rightarrow$

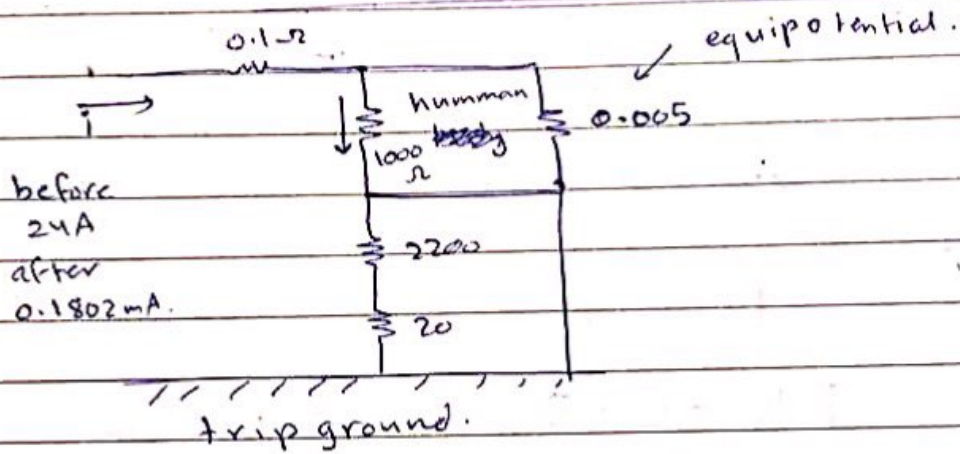
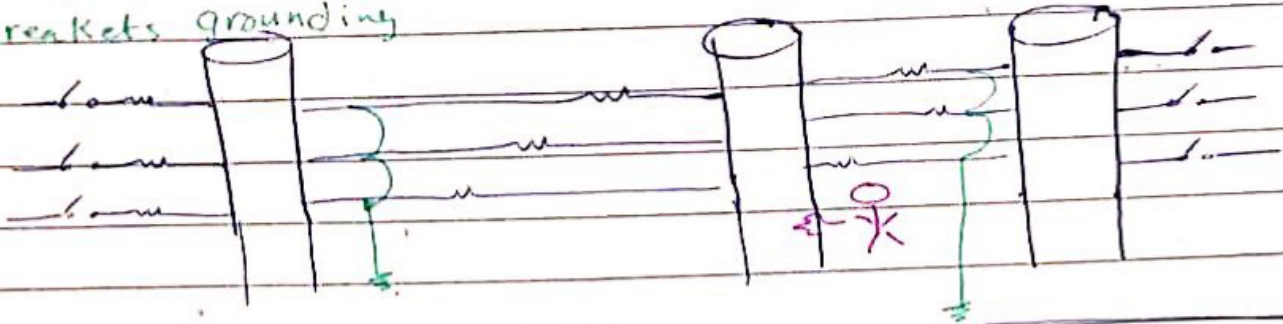


\* ربطت حوالت الـ "خص"  $\Rightarrow$  الـ

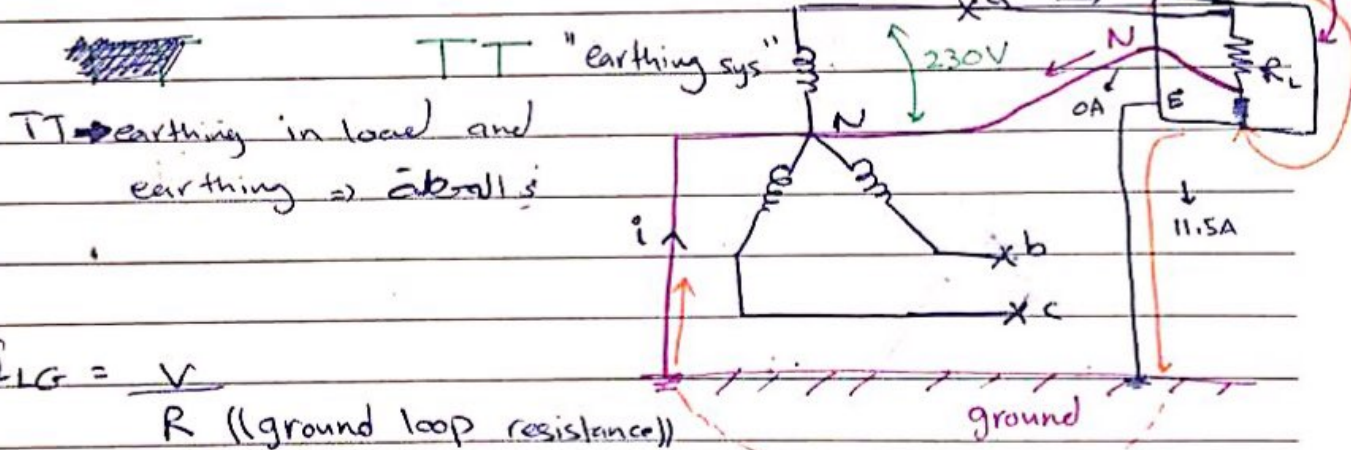
لـ نزلت الـ لا ونزلت الـ

$$I = \frac{110 \text{ mA}}{\sqrt{E}} \quad \text{"safe current"}$$

breakers grounding



types of earthing system :-

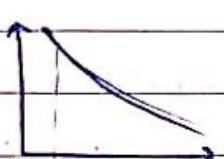


$$I_{LG} = \frac{V}{R \text{ (ground loop resistance)}}$$

$I_{LG}$  small  $\Rightarrow$  Ground loop  $\approx 20\Omega$  LG fault.

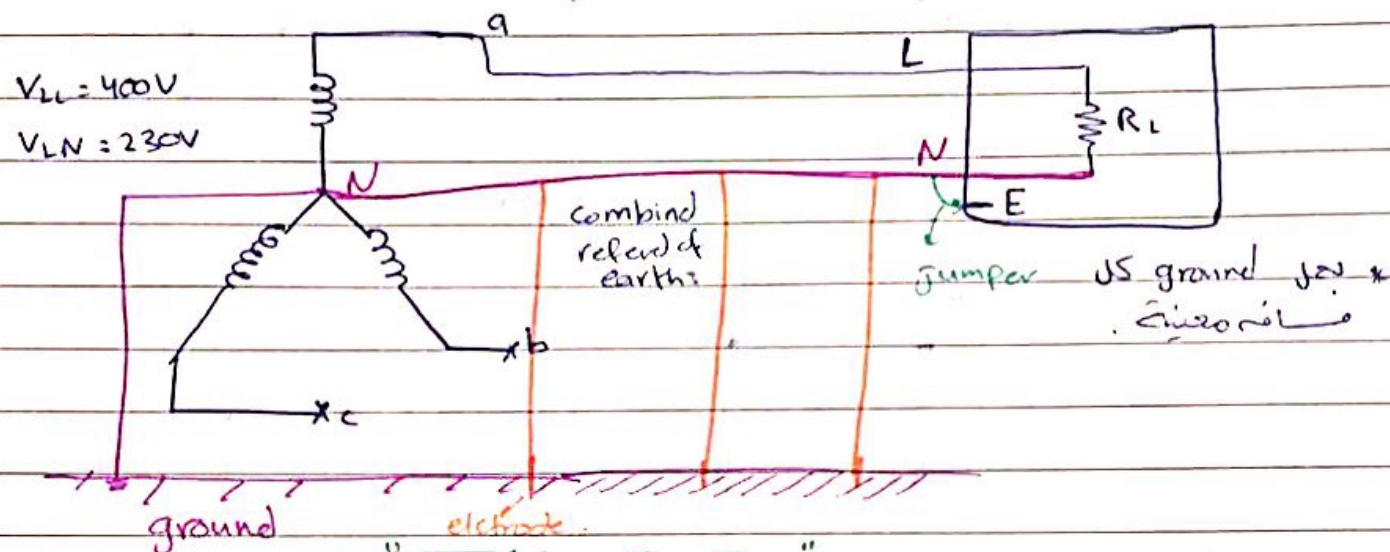
$$I_{LG} = \frac{230}{20\Omega} = 11.5 \text{ A}$$

fuses  $\Rightarrow$   $\uparrow$  current  $\rightarrow$  fuse break

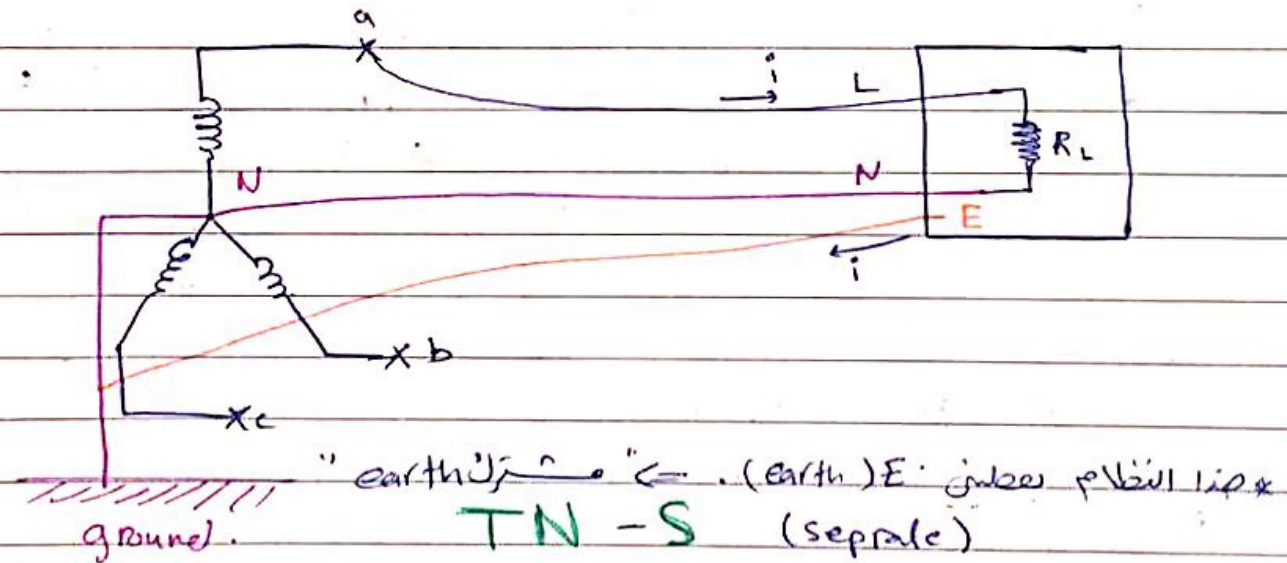


dis: TT  $\rightarrow$  current  $\rightarrow$  fuse break

\*  $I_{L1} = 11.5A \rightarrow I_N = 0 \Rightarrow$  قراءه التيار  
 اذا وجد ان الفرق كبير بين  $I_{L1}$  و  $I_N$  يعني ان هناك fault في احد الاجزاء System

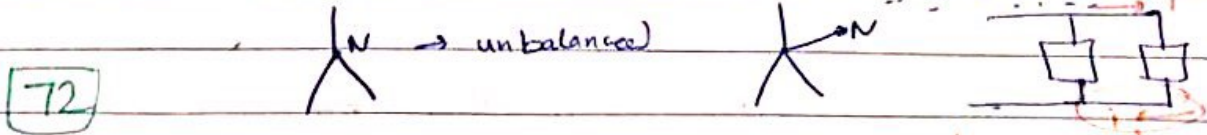


"TN-C-S" C = Combined S = Separate  
 (PME) = protective multiple earthing



disadvantage: if fault in customer 1, it affects customer 2. Voltage will rise in one customer & fall in the other.

\*  $N \rightarrow$  unbalance  $\Rightarrow$  shifted. (230V will be low or high)



Voltage difference

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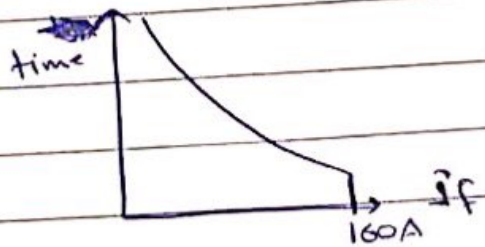
ground loop :-

TNS  $\approx 0.8 \Omega \rightarrow \hat{I}_{LG} = \frac{230}{0.8} = 287.5 A$

TN-C-S  $\approx 0.35 \Omega \rightarrow \hat{I}_{LG} = 657 A$

TT  $\rightarrow 21 \Omega \rightarrow \hat{I}_{LG} = 11 A$   
 $\rightarrow 100 \Omega \rightarrow \hat{I}_{LG} = 2.3 A$

MCB  $\rightarrow 32 A$  type B  
 $32 * 5 = 160 A$

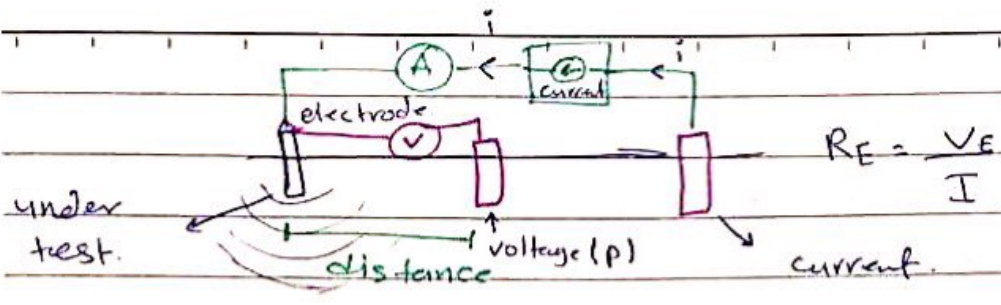


MCB 32A - type C  
 $10 * 32 A = 320 A$

"جب 320 اے"

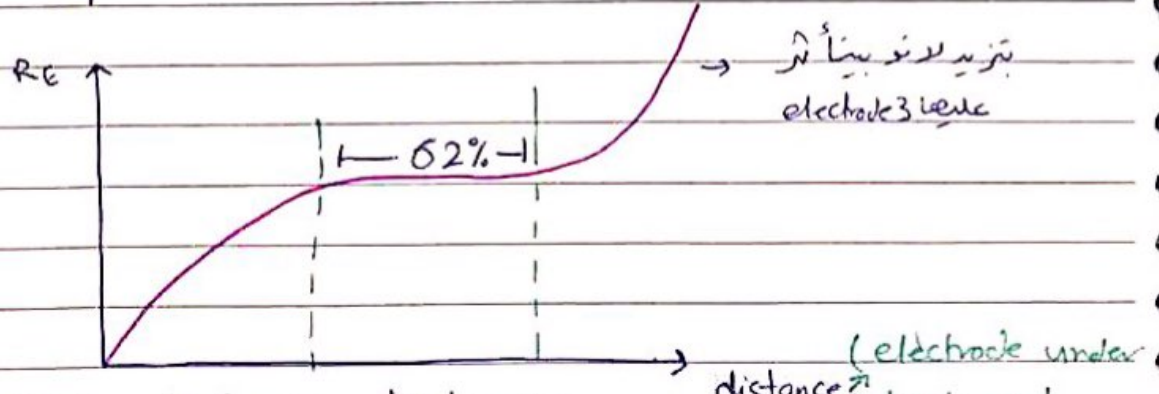
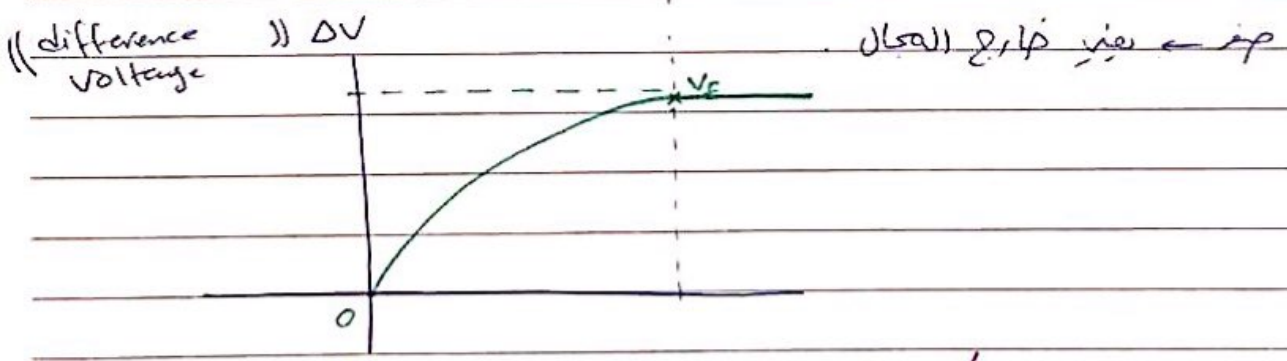
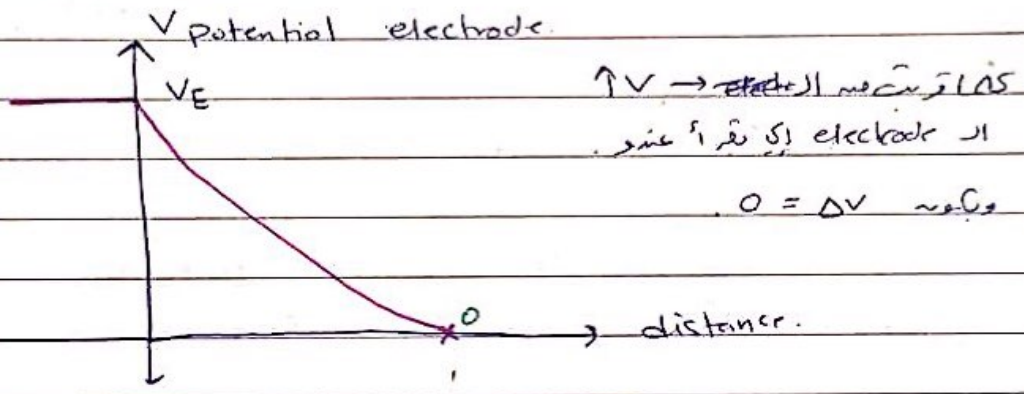
RCD ; لوپ میں بہا بہا کی ناکافی  
 RCD = residual current device.





في اشارة برقي اقيس المقاومة (2 terminal) ← first terminal (الطرف الاول)  
 second terminal ← RE = المقاومة / التيار

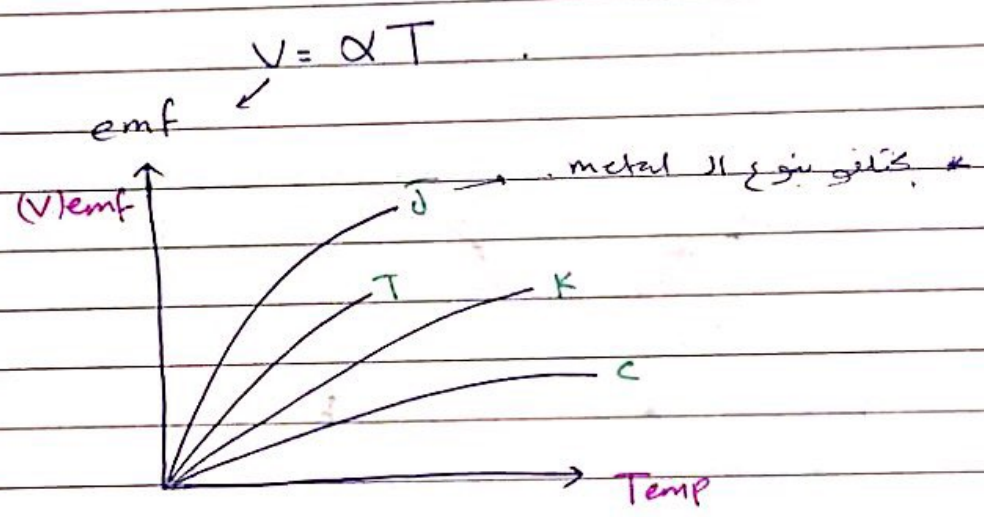
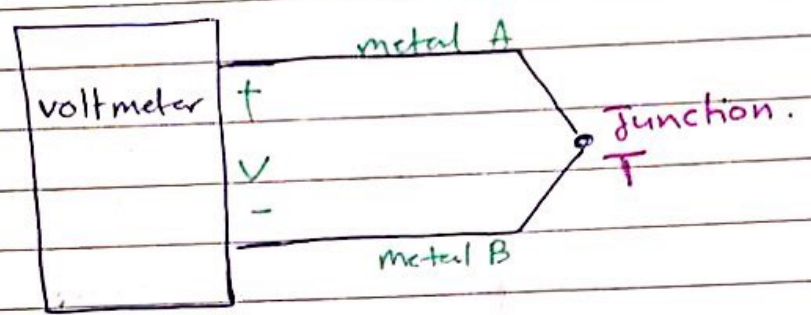
موجود في باظلام الارض (الارض)



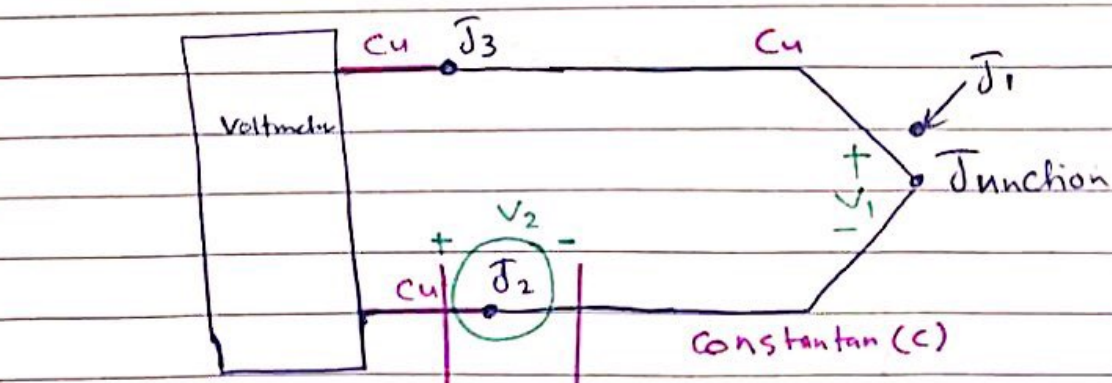
74 (( 62% distance between electrode under test and current electrode )) distance (electrode under test and potential electrode)

Parallel ← electrode ← (1) ← RE ← (2) ←

\* Thermocouples  $\Delta$  "temperature  $\rightarrow$  voltage"



Type T: (Cu, constantan)

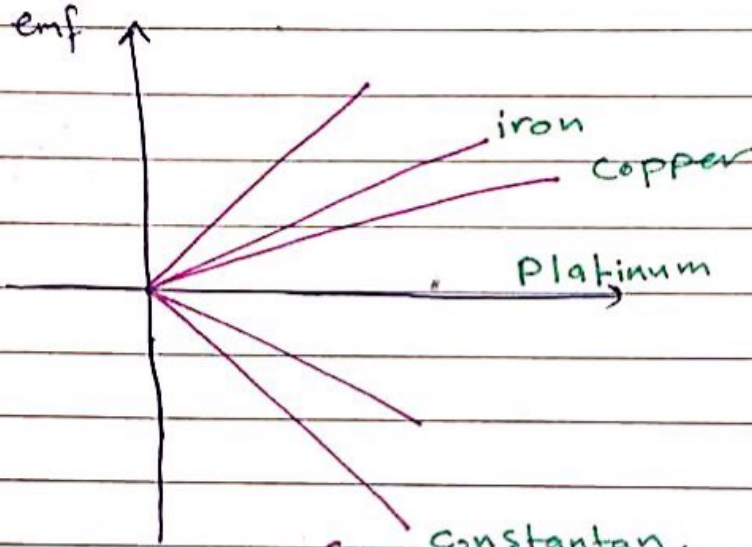


$J_2 \Rightarrow C - Cu (emf)$   
 $V = V_1 - V_2$   
 ice } ref  $\Rightarrow T = 0$   
 $V_2 = 0$

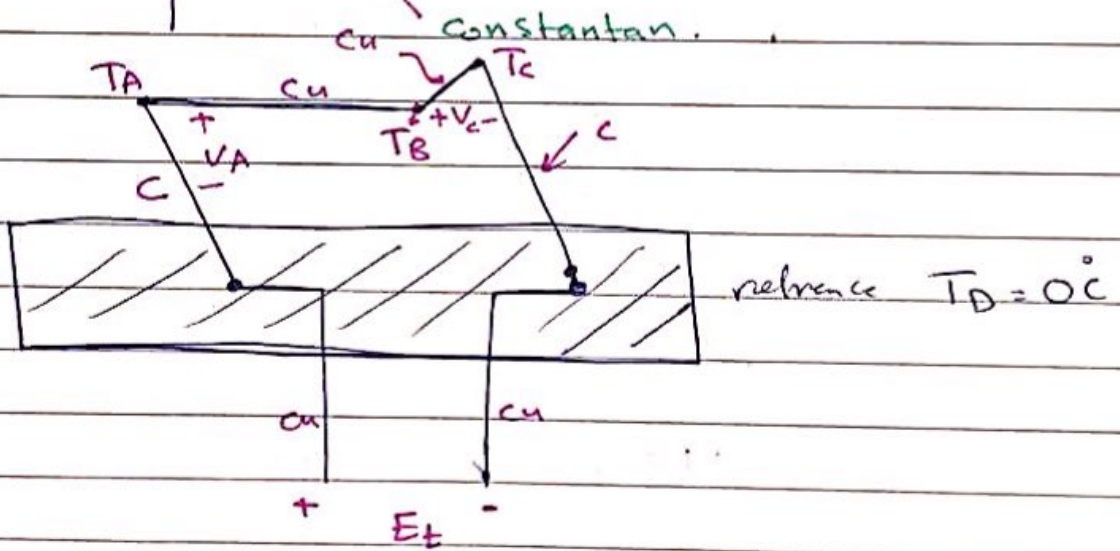
# \* Reference Function :-

$T_2 \Rightarrow$  reference (ice)  $\Rightarrow 0^\circ\text{C} \rightarrow V_2 = \alpha T$   
 $V_2 = 0.$

$$V = V_1 = \alpha T_{J_1}$$



Ex



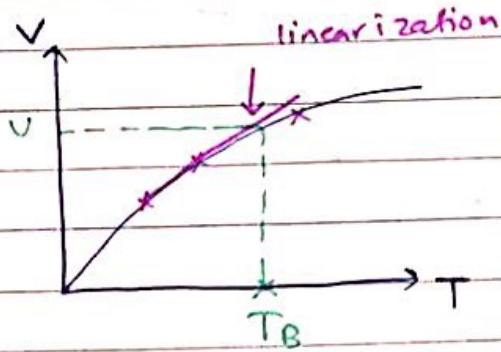
$T_B = 121.1^\circ\text{C}$  ,  $E_t = 2.05\text{ mV}$   
 $V_A = +1.517\text{ mV}$

- ① emf (B, C) ?!
- ②  $T_A, T_C$  ?!

sol: ①  $V_B = 0$  (Cu-Cu Junction)  
 $V_C = ?!$  KVL  
 $-E_t - V_A + V_C = 0$   
 $V_C = E_t + V_A$

$$V_c = 2.05 \text{ mV} + 1.517 \text{ m} = 3.567 \text{ mV}$$

②  $T_A \Rightarrow$  curve  
 curve of the cell



linearization for ~~the cell~~ - plei jilasi 1 di  
 tabel no plei c. 10.6

T			
V			

time domain  $\xrightarrow{\Downarrow}$  frequency domain  
fourier series

$$x(t) = a_0 + \sum_{n=1}^N a_n \cos n\omega_0 t + \sum_{n=1}^N b_n \sin n\omega_0 t$$

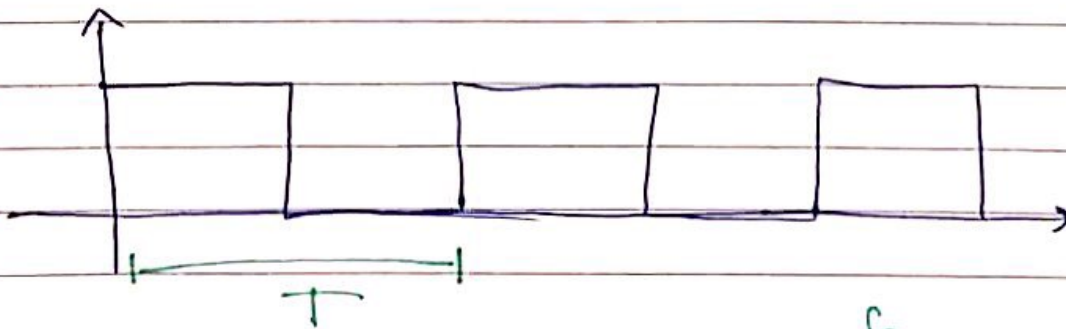
$\Rightarrow a_0 =$  dc signal.

$$= \text{average} = \frac{1}{T} \int x(t) dt$$

$$\Rightarrow a_n = \frac{2}{T} \int x(t) \cos n\omega_0 t dt$$

$$\Rightarrow b_n = \frac{2}{T} \int x(t) \sin n\omega_0 t dt$$

$\omega_0 \triangleq$  fundamental freq



$$f_0 = \frac{1}{T} \text{ Hz}$$

$f_0$   
 $1f_0$   
 $2f_0$   
 $3f_0$   
 $\vdots$

} harmonic

(78)

### \* Distortion analyzers:

وہی ہے کہ ہم نے الٹا harmonic الٹا fundamental.

\* low pass filter ← Third harmonic الٹا

Third harmonic الٹا

### \* Wave:

Frequency selective

### \* Hertzodyne:

BW الٹا carrier الٹا signal الٹا

$$dB = 20 \log \frac{V_2}{V_1}$$

$$dBm \rightarrow mw$$