

Answers should be written in ink.

Exam Duration: 50 min

Question 1

Consider the circuit shown in Fig. 1, with a current source of value I_I and V_I is voltage drop across it.

- a) Indicate the directions of I_I and the other transistors currents.
b) Add additional components and signal(s) to the circuit for it to act as a high current amplifier.

$$A_i \approx \beta_1 \beta_2$$

c) Perform the following dc analysis.

i) Express I_R in terms of β and I_{B1} .

$$I_{Rc} = I_{C2} + I_{C1}$$

$$I_{C2} = \beta_2 I_{B2} = \beta_2 I_{E1} = \beta_2 (1 + \beta_1) I_{B1}$$

$$I_{C1} = \beta_1 I_{B1}$$

$$\therefore I_R = (1 + \beta_1) \beta_2 I_{B1} + \beta_1 I_{B1}$$

$$= (\beta_2 + 2\beta_1) I_{B1}$$

ii) Write two equations involving V_I .

$$eq_1: 0 + 520 I_{B1} + 0.7 + 0.7 + V_I = 9 = 0$$

$$eq_2: -9 + 100 I_R + V_{CE2} + V_I - 9 = 0$$

iii) Solve for I_{B1} given that $V_{CE2} = 8V$.

$$V_{CE2} = 8V \quad , \quad I_R = (1 + \beta_1) \beta_2 I_{B1} + \beta_1 I_{B1} \quad \text{--- (*)}$$

$$\text{From the 2 eqs in (ii): } V_I = 9 - 1.4 - 520 I_{B1} = 7.6 - 520 I_{B1}$$

$$\text{Sub (1) in (2): } -9 + 100 I_R + 8 + (7.6 - 520 I_{B1}) - 9 = 0$$

$$\text{IR eq: } -9 + 100 (101 \times 100 I_{B1} + 100 I_{B1}) + 8 + 7.6 - 520 I_{B1} - 9 = 0$$

$$\therefore \text{Absorb } I_{B1} - 2.4 = 0$$

$$I_{B1} = \frac{2.4}{100 \times 100 + 100} = 2.47 \times 10^{-7} \text{ Ampere}$$

iv) Calculate V_{CE1} .

$$V_{C2} = 9 - 100 I_R = 8.975$$

$$-8.975 + V_{CE1} +$$

d) Calculate r_{π} and g_m for the Q_2 transistor.

$$r_{\pi 1} = \frac{V_T}{I_{B2}} = \frac{26 \text{ mV}}{2.47 \times 10^{-7}} = 10.52 \times 10^3 \Omega$$

$$I_{B2} = I_{E1} = I_B (1 + \beta_1)$$

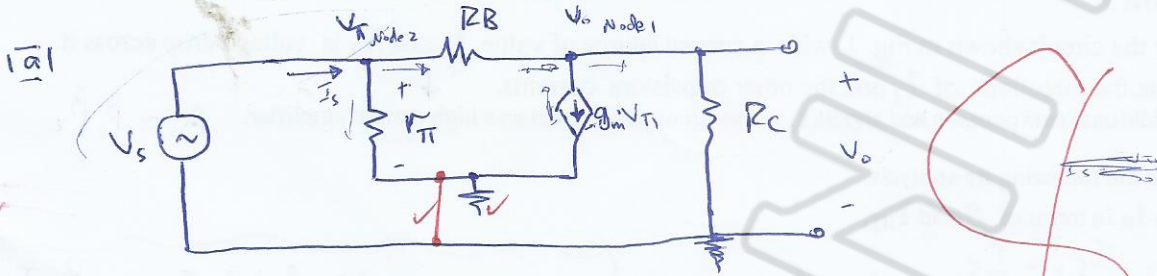
$$\frac{26 \text{ mV}}{(101) \times 2.47 \times 10^{-7}} = 1042.2 \Omega$$

$$g_{m2} = \frac{I_{C2}}{V_T} = \frac{2.49 \times 10^{-3}}{26 \text{ mV}} = 9.595 \times 10^{-2} \text{ Volt}$$

Question 2

Consider the circuit shown in Fig. 2

- Draw the small signal low frequency equivalent circuit when $r_o = \infty \Omega$.
- Use the equivalent circuit together with KCL (or otherwise) to determine the voltage gain A_v in terms of R_C , R_B and g_m . What is A_v when R_B approaches $\infty \Omega$.



Node 1:
$$\frac{V_o - V_\pi}{R_B} + \frac{V_o}{R_C} + g_m V_\pi = 0$$

Node 2:
$$\frac{V_\pi - V_o}{R_B} + \frac{V_\pi}{r_\pi} = 0$$

$$V_s = V_\pi \quad (*) \quad 5$$

$$\therefore \frac{V_o - V_s}{R_B} + \frac{V_o}{R_C} + g_m V_s = 0$$

$$V_s \left(-\frac{1}{R_B} + g_m \right) + \frac{V_o}{R_B} + \frac{V_o}{R_C} = 0$$

$$\therefore \frac{V_o}{V_i} = \frac{-\left(\frac{R_C + R_B}{R_C R_B} \right)}{\left(g_m - \frac{1}{R_B} \right)} = A_v$$

- Suppose r_o is now finite, can you easily write A_v in this case based on A_v already obtained in part b)? If NO, why not? If YES, what is A_v now, (Warning: Don not calculate from first principles).*

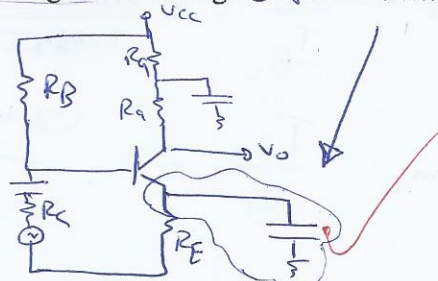
Yes, because we put it Parallel with R_C

$$A_v = \frac{-\left(\frac{R_C \parallel r_o + R_B}{R_C \parallel r_o + R_B} \right)}{\left(g_m - \frac{1}{R_B} \right)}$$

Question 3

Consider the circuit shown in Fig. 3

- Write down the most simple expression for $A_v \dots = \frac{-\beta R_a}{r_\pi + (1+\beta)R_E} \cdot \frac{R_B \parallel R_{i0}}{R_B \parallel R_{i0} + R_s} \approx \frac{-\beta R_a}{R_{i0}} \cdot \frac{R_i}{R_i + R_s}$
- Write down the input resistance $R_i \dots = R_B \parallel R_{i0} = R_B \parallel (r_\pi + (1+\beta)R_E)$
- Write down the configuration of the amplifier, and the output resistance $R_o \dots = R_a \parallel R_{C1} \parallel C_E$
- Add a passive component to increase A_v without affecting the dc biasing.. Capacitor... with R_E



2