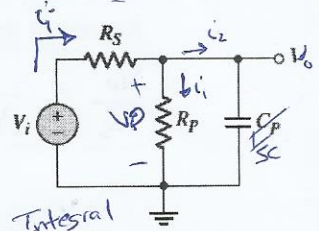


5

**Question 1** Consider the circuit shown.

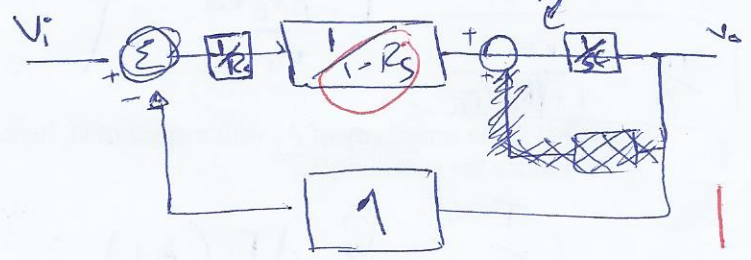
Obtain a **detailed block diagram** representation of the circuit with  $V_o$  as output and  $V_i$  as set value. Clearly indicate on it where to measure  $V_o$ ,  $I_s$ ,  $I_p$ ,  $I_c$ .



$i_s = i_p + i_c(t) \dots (1)$   
 By current division  $\Rightarrow i_c(t) = \frac{R_p i_s(t)}{(R_p + C_p)} \times$   
 $V_i(t) = i_s R_s + i_p R_p \dots \times V_o(t) = \dots \int i_c(t) dt$

Laplace Transformation:

$I_s(s) = I_p(s) + I_c(s)$   
 $I_c(s) = \frac{R_p I_s(s)}{(R_p + \frac{1}{sC})}$



Use **block diagram reduction techniques** to determine  $V_o(s)/V_i(s)$ .

$V_i(s) = I_s(s) R_s + V_o(s)$   
 $V_i(s) = I_s(s) R_s + \frac{1}{sC} I_c(s)$   
 ~~$V_i(s) = I_p(s) R_p + V_o(s)$~~

$V_i(s) = I_p(s) + \frac{V_o(s)}{R \frac{1}{sC}} + V_o(s)$  *not like this*  
 $V_i(s) = \frac{I_p(s)}{s} + V_o(s) (\frac{1}{sC} + 1)$   
 $V_i(s) = \frac{V_i(s) - V_o(s)}{R_s} + V_o(s) (\frac{1}{sC} + 1)$

\* By voltage division:  
 $V_o(s) = \frac{V_i(s) R_p}{R_s + R_p}$   
 $\therefore \frac{V_o(s)}{V_i(s)} = \frac{R_p}{R_s + R_p}$   
 $I_p(s) = \frac{V_i - V_o}{R_s}$

Evaluate  $V_o(t)$  when  $V_i = 10V$ ,  $R_s = R_p = 8K\Omega$ ,  $C_p = 5\mu F$ .

$V_o(t) = \frac{V_i(t) * R_p}{R_s + R_p}$  *Voltage division*

$V_o(t) = \frac{10 * 8}{8 + 8} = \frac{80}{16} = 5 \text{ volt}$

$V_i(s) (1 - \frac{1}{R_s}) = V_o (R \frac{1}{sC} + \frac{1}{R_s} + 1)$   
 $\frac{V_i(s)}{V_o(s)} = \frac{(R \frac{1}{sC} + \frac{1}{R_s} + 1)}{(1 - \frac{1}{R_s})}$   
 $\frac{10}{16} = \frac{5}{80}$



**Question 2** a) state appreciable parameter variations and external disturbances encountered by a

i) a bullet (رصاصة مسدس)	open loop	
ii) a rocket.	open loop	

b) The absolute value of the gain  $A_v$  of a particular common emitter amplifier is given by  $A_v = \frac{V_o}{V_s} = \frac{\beta R_c}{r_\pi + \beta R_E}$

Represent this gain relationship as a negative feedback system. What are  $G$  and  $H$  for that system.

$$\frac{V_o}{V_s} = \frac{G}{1 + GH}$$

$$\frac{V_o}{V_s} = \frac{\beta R_c}{1 + \frac{\beta R_c R_E}{r_\pi}}$$

$$\frac{V_o}{V_s} = \frac{R_E}{1 + R_E/r_\pi}$$

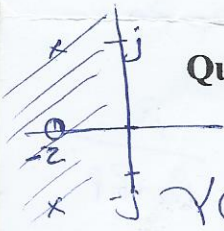
$\therefore G = R_E$  and  $H = R_E/r_\pi$

What is the sensitivity of  $A_v$  with respect of  $G$ , hence what are the conditions on the components of  $G$  in order to reduce the sensitivity?

$$\frac{T}{G} = \frac{G}{T} \frac{dT}{dG} (A_v) = \frac{G}{T} \frac{dT}{dG} \left( \frac{\beta R_c}{r_\pi + \beta R_E} \right)$$

$$\frac{T}{G} = \frac{1}{1 + \frac{R_E^2}{r_\pi}} = \frac{1}{1 + GH}$$

**Question 3** a) Given  $Y(s) = \frac{58}{s(s^2 + 4s + 29)}$ . Calculate  $y(t)$  using any method you know.



$$Y(s) = \frac{58}{s(s^2 + 4s + 29)}$$

$$\lim_{t \rightarrow \infty} y(t) = \lim_{s \rightarrow 0} s F(s) = \frac{58}{29} = 2$$

$$\frac{58}{s(s^2 + 4s + 29)} = \frac{A}{s} + \frac{Bs + C}{s^2 + 4s + 29}$$

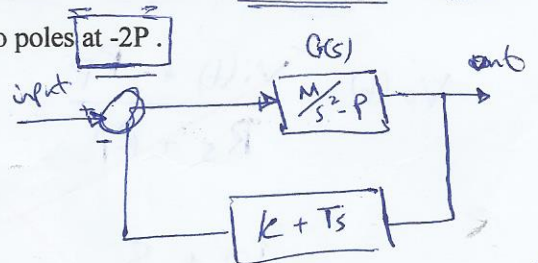
$$A(s^2 + 4s + 29) \Big|_{s=0} = 58$$

$$A \times 29 = 58$$

$$A = 2 \quad B = -8 \quad C = 2$$

b) A simplified transfer function of a bicycle is  $G(s) = \frac{M}{s^2 - P}$  where  $M$  and  $P$  are positive numbers. Introduce whatever is needed in order to have a closed loop system with two poles at  $-2P$ .

$$G(s) = \frac{M}{s^2 - P} \Rightarrow \frac{M}{(s - \sqrt{P})(s + \sqrt{P})}$$



Zero  $\omega_n = \sqrt{b}$   
 Zero  $\zeta = \frac{a}{2\sqrt{b}}$   
 Zero  $\omega_d = \omega_n \sqrt{1 - \zeta^2}$

$$Q3: Y(s) = \frac{2}{s} + \frac{-8s + 2}{s^2 + 4s + 29}$$

$$y(t) = 2u(t) + -8te^{-4t} + 2te^{-4t}$$

0  
0  
1  
2