

1 For the circuit shown in Fig. (2) Answer the following questions:

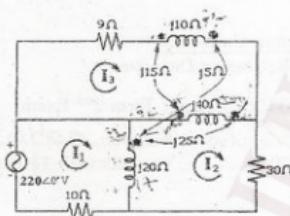
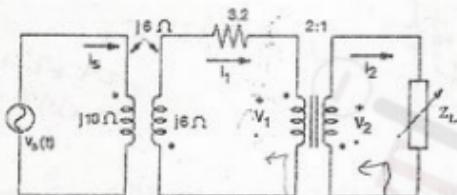


Fig.(2)

$$\begin{aligned}
 & -220 + j20(I_1 - I_2) + 10I_1 + j25(I_2 - I_3) + j5I_3 = 0 \\
 & j20I_1 - j20I_2 + 10I_1 + j25I_2 - j25I_3 = 220 \\
 & (10 + j20)I_1 + j25I_2 - j25I_3 = 220
 \end{aligned}$$

- The 1<sup>st</sup> mesh equation:
  - a)  $j20(I_2 - I_1) - j25(I_2 - I_3) - j5I_3 + 10I_1 = 220\angle 0^\circ$
  - b)  $j20(I_1 - I_2) - j25(I_2 + I_3) - j5I_3 + 10I_1 = 220\angle 0^\circ$
  - c)  $(10 + j20)I_1 + j45I_2 + j20I_3 = 220\angle 0^\circ$
  - d)  $(10 + j20)I_1 - j45I_2 + j20I_3 = 220\angle 0^\circ$**
- The 2<sup>nd</sup> mesh equation:
  - a)  $30I_2 + j20(I_1 - I_2) + j25(I_2 - I_3) + j5I_3 + j40(I_2 - I_3) - j25(I_1 - I_2) + j15I_3 = 0$
  - b)  $30I_2 + j20(I_2 - I_1) + j25(I_2 - I_3) + j5I_3 + j40(I_2 - I_3) - j25(I_1 - I_2) + j15I_3 = 0$
  - c)  $j45I_1 \pm (30 + j110)I_2 - j45I_3 = 0$**
  - d)  $j45I_1 + (30 + j110)I_2 - j45I_3 = 0$
- Assume that the currents  $I_1 = 16.4447\angle -5.1^\circ A$ ,  $I_2 = 4.1813\angle 1.6807^\circ A$  and  $I_3 = 6.4526\angle -165.42 A$ , the voltage across  $|V_{j40\Omega}|$  is:
  - a) 4825 V
  - b) 248.5 V**
  - c) 2486 V
  - d) 2856 V

**2** For the circuit shown in Fig.(3) all resistances and reactances are given in  $\Omega$ . Answer the following questions:



$$3.2 + \underline{36}$$

Fig. 4

4. The load impedance  $Z_L$  is adjusted to absorb the average maximum power, so  $\bar{Z}_L$  is equal to:  
 a)  $1\angle -36.87^0\Omega$       b)  $4\angle -36.87^0\Omega$       c)  $2\angle 36.87^0\Omega$       d)  $0.8 + j0.6\Omega$

5. The impedance looking by source terminals, when the load impedance  $Z_L$  is adjusted to absorb the average maximum power is:  
 a)  $8.52\angle -60^0\Omega$       b)  $7.82\angle 60^0\Omega$       c)  $5.82\angle -60.4^0\Omega$       d)  $8.72\angle 60^0\Omega$

**3** For Fig.(4)  $V_s = 102\angle -36.87^0\text{V}_{rms}$ .

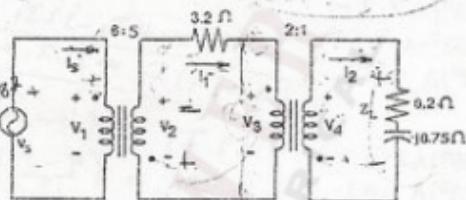


Fig. 4

6. The current source  $I_1$  is  
 a)  $14.167\text{A}$       b)  $-17\angle 36.87^0\text{A}$       c)  $-17\angle 0^0\text{A}$       d)  $-14.67\text{A}$
7. The load current  $|I_2|$  is  
 a)  $34\text{ A}$       b)  $13.33\text{ A}$       c)  $17\text{ A}$       d)  $-3.4\text{ A}$
8. The voltage  $|V_3|$  is  $\approx$   
 a)  $122\angle -36.87^0\text{V}$       b)  $-26\angle 36.87^0\text{V}$       c)  $53\angle 105^0\text{V}$       d) no answer
9. The reactive power delivered by the source  $Q_s$  is  $\approx$   
 a)  $0\text{ VAr}$       b)  $870\text{ VAr}$       c)  $-433.5\text{ VAr}$       d)  $-867\text{ Var}$

17. If the pole zeros plot of  $Z_{in}(\sigma)$  is shown in Fig.5, then transfer function of  $Z_{in}(\sigma)$  is.

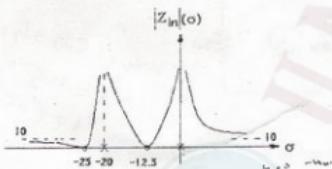


Fig. 5

- a)  $10 \frac{\sigma^2 + 37.5\sigma + 312.5}{\sigma^2 + 20\sigma}$   
 b)  $100 \frac{\sigma^2 + 37.5\sigma + 312.5}{\sigma^2 + 20\sigma + 200}$   
 c)  $10 \frac{\sigma^2 - 37.5\sigma + 312.5}{\sigma^2 + 20\sigma + 200}$   
 d) none of them

18. The poles and zeros configuration of  $|Z_{in}(\sigma)|$  shown in Fig.6(a) represents the input impedance of the circuit shown in Fig. 6(b). The poles  $p_1, p_2$  are:

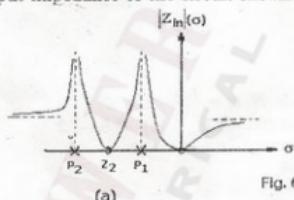
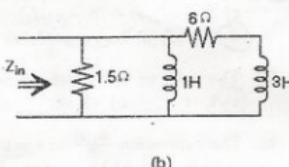


Fig. 6



$$6+3s/1/s$$

$$\frac{6s+3s^2/1/s}{6+4s} \frac{1/s}{6+4s}$$

$$9+4.5s^2$$

$$\frac{6s+3s^2+1.5}{(6+4s)/6}$$

19. The zeros of  $|Z_{in}(j\omega)|$  shown in Fig.7 are:

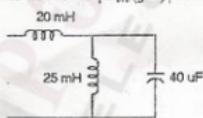


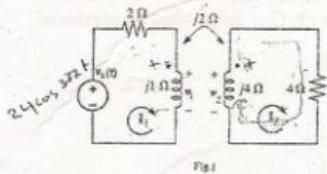
Fig. (7)

- a) -750, 750 rad/s b) -500, 500 rad/s c) -1000, 1000 rad/s d) 1500, -1500 rad/s

20. The poles of  $|Z_{in}(j\omega)|$  shown in Fig.7 are:

- a) -750, 750 rad/s b) -1500, 0, 1500 rad/s c) -500, 500 rad/s d) 1000, -1000 rad/s

- 4 For the circuit shown in Fig.1, if the voltage source  $v_s(t) = 24 \cos 377t$  V. Answer the following questions:



$$\begin{aligned} & j1I_1 - j2I_2 \\ & -24 + 2I_1 + j1I_1 - j2I_2 = 24 \\ & (2 + j1)I_1 - j2I_2 = 24 \end{aligned}$$

Fig.1

10. One of the following equations that describe the 1<sup>st</sup> loop is wrong, that is:

- a)  $V_1 = j1I_1 - j2I_2$
- b)  $24\angle 0^\circ = (2 + j1)I_1 - j2I_2$
- c)  $24\angle 0^\circ = 2I_1 + V_1$
- d)  $24\angle 0^\circ = (2 + j1)I_1 + j2I_2$

$$j4I_2 - j2I_1$$

11. One of the following equations that describe the 2<sup>nd</sup> loop is wrong, that is:

- a)  $V_2 = -j4I_2 + 4I_2 - j2I_1$
- b)  $0 = (-4 - j4)I_2 + j2I_1 - V_2$
- c)  $0 = 4I_2 - V_2$
- d)  $V_2 = j2(I_1 - 2I_2)$

$$\begin{aligned} & -24\angle 0^\circ + 2I_1 + j1I_1 - j2I_2 = 0 \\ & (2 + j1)I_1 - j2I_2 = 24 \quad \rightarrow ① \end{aligned}$$

12. The current  $i_1(t) =$

- a)  $i_1(t) = 2.17 \sin(377t - 21.2^\circ)$  A  $-0.71$
- b)  $i_1(t) = 4.91 \cos(377t + 22.5^\circ)$  A  $4.47$
- c)  $i_1(t) = 9.41 \cos(377t - 11.31^\circ)$  A  $9.23$
- d)  $i_1(t) = 6.47 \cos(377t + 51.2^\circ)$  A  $3.28$

$$\begin{aligned} & -j4I_2 + 4I_2 - j2I_1 = 0 \\ & (4 - j4)I_2 - j2I_1 = 0 \quad \rightarrow ② \end{aligned}$$

13. The current  $i_2(t) =$

- a)  $i_2(t) = 3.33 \cos(377t + 33.69^\circ)$  A  $2.7$
- b)  $i_2(t) = 2.19 \cos(377t - 30.13^\circ)$  A  $1.93$
- c)  $i_2(t) = 9.13 \cos(377t - 13.69^\circ)$  A  $8.9$
- d)  $i_2(t) = 1.31 \cos(377t + 63.19^\circ)$  A  $0.65$

$$\begin{aligned} & j2I_1 = (4 - j4)I_2 \\ & I_1 = \frac{(4 - j4)}{j2} I_2 \\ & I_1 = (j2 - 2)I_2 \end{aligned}$$

14. The current  $i_1(t = 5ms) =$
- a) 1.2A
  - b) 2.1A
  - c) -1.1A
  - d) -2.2A

$$\begin{aligned} & (2 + j1)(j2 - 2)I_2 - j2I_2 = 0 \\ & (-j4 - 4 + 2 - j2)I_2 - j2I_2 = 24 \\ & (-2 - j6)I_2 - j2I_2 = 24 \end{aligned}$$

15. The current  $i_2(t = 5ms) =$
- a) -3.2A
  - b) -2.61A
  - c) 3.2A
  - d) 32A

$$\begin{aligned} & (-2 - j8)I_2 = 24 \\ & I_2 = \frac{24}{-2 - j8} \\ & I_2 = \frac{24}{-2 - j8} \times \frac{-2 + j8}{-2 + j8} \\ & I_2 = \frac{24(-2 + j8)}{(-2)^2 + 8^2} \end{aligned}$$

16. The energy stored in the perfectly coupled circuit at  $w(t = 5ms)$  is:
- a) 100 mJ
  - b) 10 mJ
  - c) 22.5 mJ
  - d) -10 mJ

$$= \frac{24}{8.23} \text{ J} < 76$$

$$\begin{aligned} & (2 + j1)I_1 - j2I_2 = 24 \\ & I_1 = \frac{24 + j6}{2 + j1} \times \frac{2 - j1}{2 - j1} \\ & I_1 = \frac{48 - j24 + j12 + 6}{5} \\ & = \frac{54 - j12}{5} \approx 10.8 - j2.4 \\ & = 11.06 \angle -12.53^\circ \end{aligned}$$

$$\begin{aligned} & (2 + j1)I_1 - j2(1.9 + j1.1) = 24 \\ & 2I_1 + j1I_1 - j2(1.9) - j2(j1.1) = 24 \\ & 2I_1 + j1I_1 - j3.8 - j2.2 = 24 \end{aligned}$$

$$\begin{aligned} & I_2 = 2.19 \angle 30.13^\circ \\ & I_2 = 1.9 + j1.1 \end{aligned}$$

- 5 For the circuit shown in Fig. 8., the forced source is  $V_s(t) = 10e^{-2t}$  V and  $i_1(0) = i_2(0) = 10$  A. Answer the following questions:

$$A + B = 10 \quad \text{--- } \textcircled{1}$$

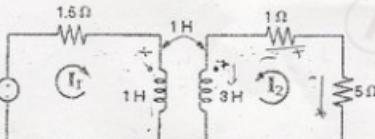


Fig. (8)

$$\begin{aligned} -Vs + 1.5\dot{I}_1 + 3\dot{I}_2 &= 0 \\ \sqrt{s} &= 1.5 \\ \sqrt{s} &= (1.5 + s)\dot{I}_1 + 3s\dot{I}_2 \end{aligned}$$

21. The 1<sup>st</sup> mesh equation in s-domain may be expressed as

- a)  $V_s = (1.5 + s)I_1(s) - sI_2(s)$
- b)  $V_s = (1.5 + s)I_1(s) + sI_2(s)$
- c)  $V_s = (1.5 + s)I_1(s) + 3sI_2(s)$
- d) none of them

22. The 2<sup>nd</sup> mesh equation in s-domain may be expressed as

- a)  $0 = -sI_1(s) + (6 + 3s)I_2(s)$
- b)  $0 = sI_1(s) - (6 + 3s)I_2(s)$
- c)  $0 = sI_1(s) + (6 - 3s)I_2(s)$
- d)  $0 = sI_1(s) + (6 + 3s)I_2(s)$

$$\begin{aligned} 3s\dot{I}_2 + 5\dot{I}_2 + \dot{I}_2 &= 0 \\ 3s\dot{I}_2 + 6\dot{I}_2 + s\dot{I}_1 &= 0 \\ (6 + 3s)\dot{I}_2 + s\dot{I}_1 &= 0 \end{aligned}$$

23. The poles of the transfer function  $H(s) = \frac{I_2(s)}{V_s}$  are:

- a) 4, -1
- b) -2, -5
- c) -1.08, -4.17
- d) -0.5, -1.2

24. The expression  $\frac{di_2(t)}{dt}$  at  $t = 0^+$  is:

- a) 22.5
- b) 32
- c) -12
- d)  $-\frac{33}{2}$

25. Assume that  $i_2(t) = Ae^{-5t} + Be^{-6t} + 80e^{-2t}$  and  $\frac{di_2(0)}{dt} = 32$ , then constants A and B are:

- a) 0, 40
- b) -228, 158
- c) 96, -128
- d) -158, 0

$$i_2(0) = A + B + 80 = 10$$

$$\frac{di_2(0)}{dt} = -5Ae^{-5t} + 6Be^{-6t} - 2(80)e^{-2t} = 32$$

$$A + B = -70 \quad \text{--- } \textcircled{1} \quad 6$$

$$-5A - 6B = 192 \quad \text{--- } \textcircled{2}$$