

Q(1): Three loads are connected in parallel across 250V (rms) as shown in Fig. 1. Load 1 absorbs 16kW and 28 kVA. Load 2 absorbs 10kVA at 0.6 leading PF. Load 3 absorbs 8KW unity PF.

- 1- Find the Impedance that is equivalent to the three parallel loads.
- 2- Find the power factor of the total load.
- 3- If the source operates at 50 Hz, find the value of the capacitor to be connected in order to improve the power factor to 0.96.

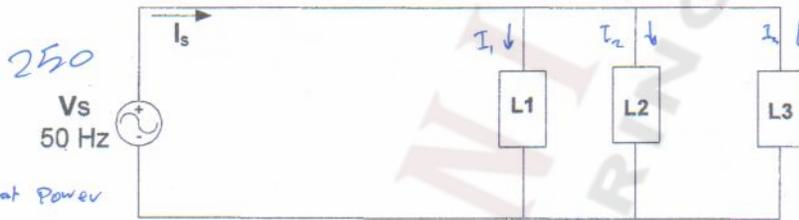


Fig. 1

(i) $V I_1 = \text{apparent power}$

$$\frac{28 \text{ kVA}}{250 \text{ V}} = I_1 = 112 \text{ Arms}$$

$$\text{P.F.} = \frac{P}{S} = \frac{16 \text{ kW}}{28 \text{ kVA}} = 0.57 = \cos(\theta - \phi_1) = \cos(-\phi_1)$$

$$\phi_1 = \cos^{-1}(0.57)$$

$$\phi = -55.15$$

Lagging

$$I_1 = 112 \angle -55.15 \text{ Arms}$$

$$Z_1 = \frac{V}{I_1} = \frac{250 \angle 0^\circ}{112 \angle -55.15} \Rightarrow Z_1 = 1.275 + j1.83 \ \Omega$$

(ii) $V I_2 = 10 \text{ kVA} \rightarrow I_2 = \frac{10 \text{ kVA}}{250} = 40 \text{ Arms}$

$$\text{P.F.} = \cos(\theta - \phi) = 0.6$$

$$\phi = \cos^{-1}(0.6)$$

$$\phi = 53.13$$

$$I_2 = 40 \angle 53.13 \text{ Arms}$$

$$Z_2 = \frac{V}{I_2} = \frac{250 \angle 0^\circ}{40 \angle 53.13} \Rightarrow Z_2 = 3.75 - j5 \ \Omega$$

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(iii) $I_3 V \cos(0) = 8 \text{ kW}$

$$I_3 = 32 \angle 0^\circ \text{ Arms}$$

$$Z_3 = \frac{250 \angle 0^\circ}{32 \angle 0^\circ} = 7.8125 \ \Omega$$

$$Z_{eq} = \left(\frac{1}{Z_1} + \frac{1}{Z_2} + \frac{1}{Z_3} \right)^{-1} = \left(\frac{1}{1.275 + j1.83} + \frac{1}{3.75 - j5} + \frac{1}{7.8125} \right)^{-1}$$

$$Z_{eq} = 1.666 + j0.832 \ \Omega$$

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~~P.F. = cos φ~~

$Z_{eq} = 1.86 \angle 26.53^\circ$

$P.F. = \cos(26.53^\circ) = 0.8946$ lagging

+ ~~(L)~~

$PF = 0.8946$ lagging



~~$P = I^2 R \cos \phi$~~

~~$I = \frac{250}{Z_{eq}} = 134.2 \angle -26.53^\circ$~~

~~$P = 250 * 134.2 * 0.8946$
 $P = 30.013 \text{ kW}$~~

$P = P_{L1} + P_{L2} + P_{L3}$

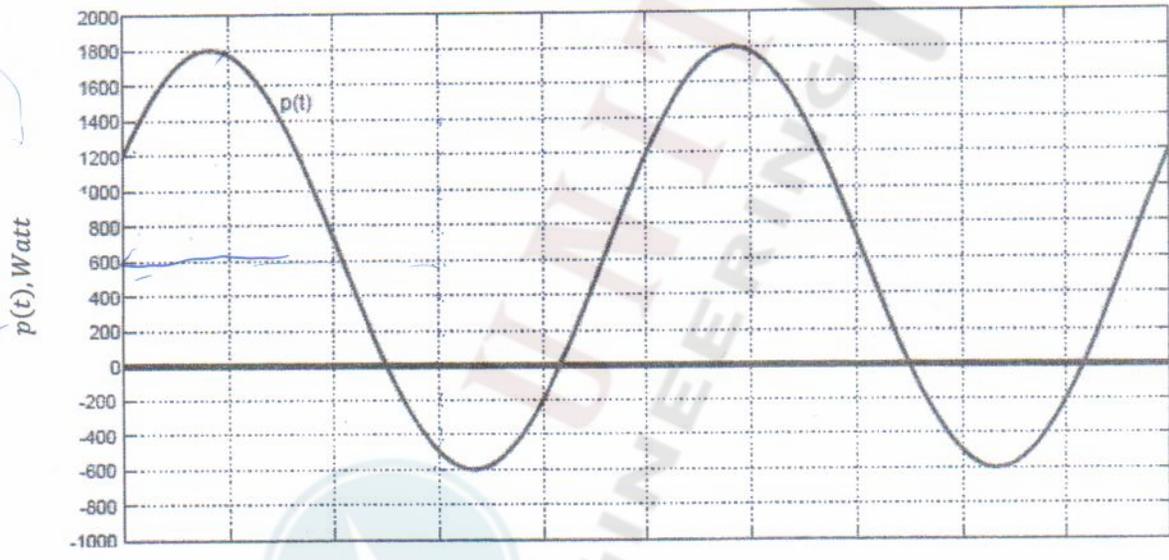
$= 16 \text{ kW} + 10 \text{ kVA} * 0.8 + 21 \text{ kW}$
 $= 30 \text{ kW}$

$C = \frac{P (\tan \phi_1 + \tan \phi_2)}{\omega V_{rms}^2} = 1.2 \text{ mF}$

$C = 1.2 \text{ mF}$

Q(2): Fig.2 shows the instantaneous power $p(t)$ consumed by the load terminals, where terminal voltage is given by $v(t) = V_m \cos(\omega t)$, then find the followings:

- 1- PF.
- 2- The reactive power Q .
- 3- The Complex power S .



$P = 600 \text{ watt}$

Fig. 2

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Apperant power = $\frac{1800 - (-600)}{2} = 1.2 \text{ KVA}$

P.F = $\frac{P}{A.P} = \frac{600}{1.2k} = 0.5$

$\cos(\theta - \phi) = 0.5$
 $\theta - \phi = \cos^{-1}(0.5)$
 $0 - \phi = 60$ $\phi = -60$

PF = 0.5 Lagging

$Q = \text{Apperant power} \sin(\theta - \phi)$
 $= 1.2 \text{ KVA} \sin(0 - (-60))$
 $= 1.039 \text{ KVAR}$

$Q = 1.039 \text{ KVAR}$

$S = 600 + j1039$
 $S = P + jQ$
 $= 600 + j1039$

$S = 600 + j1039$

marks) Q(3): In the system shown in Fig.3, given $Z_Y = 20 + j8 \Omega$, and (+) phase sequence is assumed. If $I_{aA} = 20 \angle -46^\circ$ A rms, and the source is operating with $PF = 0.94$ lagging, find the following:

- 1- R_w
- 2- The total complex power supplied by the source
- 3- V_{an} .
- 4- V_{AB} .

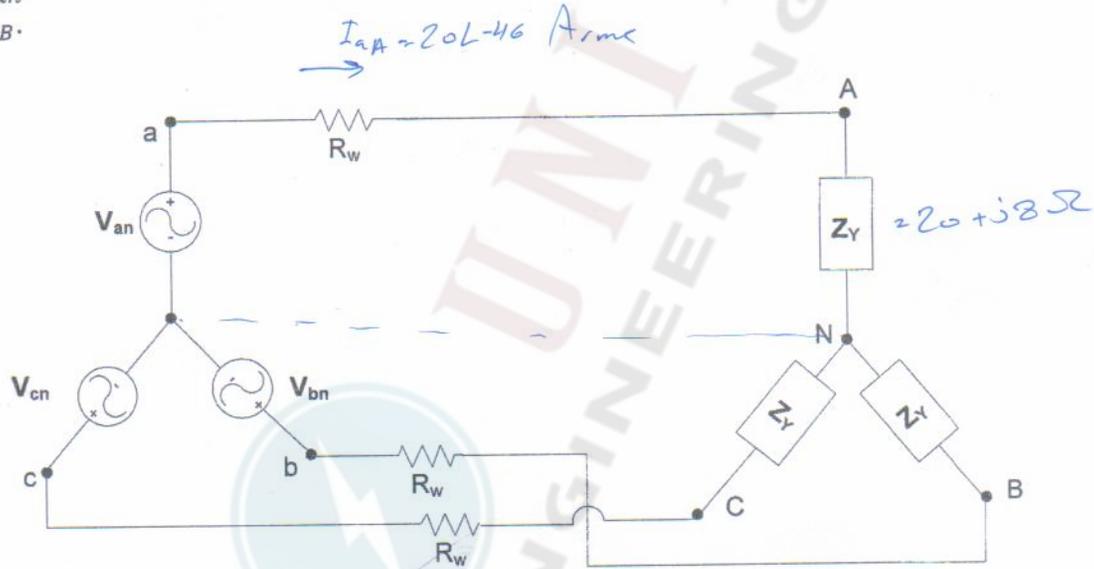
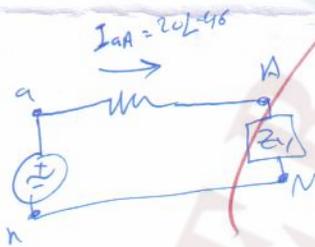


Fig. 3



$\cos^{-1}(0.94) = \theta + 46$

$\theta = -26.05$

$\theta - \phi = 19.95$

$\cos(\theta - \phi) = 0.94$

$\theta - \phi = 19.95$

$19.95 = \tan^{-1} \frac{8}{20+R}$

$\tan 19.95 = \frac{8}{20+R}$

$0.363 = \frac{8}{20+R}$

$0.363(20+R) = 8$

$7.26 + 0.363R = 8$

$R = 2.038 \Omega$

Handwritten scribbles and a large red circle.

$R_w = 2.038 \Omega$

Section: 1:00-2:00

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اسم:

$$I R = V$$

$$\vec{V} = 20 \angle -46^\circ * 22.032 + j8$$

$$V_{an} = 468.9 \angle -26.05^\circ$$

$$S = P + jQ$$

$$P = |I| |V| \cos(\theta - \phi)$$

$$= (20 * 468.9) * 0.94$$

$$P = 8815.3 \text{ W}$$

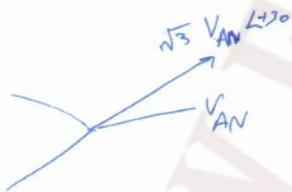
S

$$Q = (20 * 468.9) * \sin(\theta - \phi)$$

$$= 3199.7 \text{ VAR}$$

$$S = (8.815 + j3.199) \text{ kW}$$

$$V_{an} = 468.9 \angle -26.05^\circ$$



$$V_{AN} = I Z_Y$$

$$= 430.8 \angle -24.2^\circ$$

$$V_{AB} = \sqrt{3} V_{AN} \angle +30^\circ$$

$$= 746.2 \angle +5.8^\circ$$

$$V_{an} = 468.9 \angle -26.05^\circ \text{ V}$$

$$V_{AB} = 746.2 \angle +5.8^\circ \text{ V}$$

Good Luck
Thank You 6/6 ☺