

Circuits 2

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POWER UNIT

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Electrical Circuits II

①

* Summary *

* CHAPTER (10):

* for the capacitor:

$$i_c(t) = C \frac{dV_c(t)}{dt}$$

$$V_c(t) = \frac{1}{C} \int i_c(t') dt' + V_c(0)$$

* the current leads the voltage.

* for the inductor:

$$V_L(t) = L \frac{di_L(t)}{dt}$$

$$i_L(t) = \frac{1}{L} \int V_L(t') dt' + i_L(0^-)$$

* the voltage leads the current.

* Converting from phasor to time domain:

⊗ the amplitude must be positive and peak value.

* Converting from time domain to phasor:

① Amplitude must be (+ve).

② it must be a cosine function.

* CHAPTER (11):

* instantaneous power:

$$P(t) = v(t) \cdot i(t)$$

$$P(t) = \frac{V_m I_m}{2} [\cos(2\omega t + \theta_V + \theta_I) + \cos(\theta_V - \theta_I)]$$

* Average Power:

$$P = \frac{1}{T} \int_0^T P(t) dt$$

* just the resistance has an average power.

$$P_{avg} = \frac{V_m I_m}{2} \text{ (in R)}$$

$$P_{avg} = \text{Zero (in L \& C)}$$

$$P_{avg} = \frac{V_m I_m}{2} \cos(\theta_V - \theta_I) \text{ (in any element)}$$

$$P_{avg} \text{ (in R)} = \frac{1}{2} V_m I_m = \frac{V_m^2}{2R} = \frac{1}{2} I_m^2 R$$

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*Maximum Power Transfer:

happens when:

$$Z_{th} = Z_L^*$$

if power is maximized:

$$P_{avg}|_{load} = \frac{V_{th}^2}{8R}$$

* for multiple signals & multiple frequencies:

$$i(t) = I_{m1} \sin \omega_1 t + I_{m2} \cos \omega_2 t + I_{m3} \sin \omega_3 t + \dots$$



$$P_{avg} = \frac{1}{2} I_{m1}^2 R + \frac{1}{2} I_{m2}^2 R + \frac{1}{2} I_{m3}^2 R + \dots$$
$$P_{avg} = \frac{V_{m1}^2}{2R} + \frac{V_{m2}^2}{2R} + \frac{V_{m3}^2}{2R} + \dots$$

* RMS:

$$V_{eff} = V_{rms} = \sqrt{\frac{1}{T} \int_0^T V^2(t) dt} \Rightarrow \text{in general.}$$



$$I_{rms} = \frac{I_m}{\sqrt{3}} \Rightarrow \text{for ST waveform.}$$

$$I_{rms} = \frac{I_m}{\sqrt{2}} \Rightarrow \text{for a sinusoidal signal.}$$

⇒ for a resistor:

$$P_{avg} = V_{rms} I_{rms} = V_{rms}^2 / R = I_{rms}^2 R$$

if there is multiple frequencies:

$$P_{avg} = (I_{rms1}^2 + I_{rms2}^2 + I_{rms3}^2 + \dots) R$$

* Power factor:

$$PF = \cos(\theta_v - \theta_i)$$

Leading if $\theta_v - \theta_i \Rightarrow (-ve)$.
Lagging if $\theta_v - \theta_i \Rightarrow (+ve)$.

equal 1
for resistance.

equal zero
for pure inductance or capacitance.

* Complex Power: (Assume RMS values)

$S = V I^* = \frac{V^2}{Z^*} = I^2 Z$	\Rightarrow Complex Power (VA)
$ S = V I $	\Rightarrow Apparent Power (VA)
$P = V I \cos(\theta_V - \theta_I)$	\Rightarrow Real/Average Power (W)
$Q = V I \sin(\theta_V - \theta_I)$	\Rightarrow Reactive Power (VAR)

* Adding capacitor to a ckt to give us new Pf:

we find P from the old Pf since it will be always constant then find Q_1 Then Q_2 from $Q_2 = P * \tan(\cos^{-1}(Pf_{new}))$

$\Rightarrow Q_c = Q_2 - Q_1$

$\Rightarrow C = \frac{|Q_c|}{|V_{rms}|^2 \omega}$

* RMS value for multiple signals:

$V_{rms} = \sqrt{(V_{rms1})^2 + (V_{rms2})^2 + \dots}$

✳ CHAPTER (12):

* in Balanced systems:

if the load is Δ -connected:

$V_{LL} = V_{phase}$
 $I_L = \sqrt{3} I_p \angle -30^\circ$ --- (1)

if the load is Y-connected:

$V_{LL} = \sqrt{3} V_{LN} \angle +30^\circ$ --- (2)
 $I_L = I_p$

$Z_\Delta = 3 Z_Y$ --- (3)

* Always in Balanced-systems: convert to Y-Y and use the single phase ckt \Rightarrow will be the easiest way to solve.

* In UnBalanced systems: DON'T use the relations in Box (1) & (2) & (3)

* Always the unbalanced system: \Rightarrow unbalanced in the load
 (source is always balanced)
 $\hookrightarrow V_{ab} = \sqrt{3} V_{an} \angle +30^\circ$ (we it always)

* in Balanced system:

if there is a line (with or without impedance) \Rightarrow connected with n & N
 \Rightarrow we don't care to it, it has NO effect.

$I_a + I_b + I_c = 0$ \Rightarrow always in balanced-system.

* in Unbalanced system: (Three Cases)

① if just only a line (without impedance) connected to n & N

$\Rightarrow I_a + I_b + I_c = I_{Nn}$ & $V_n = V_N = 0$

② if it is line (with impedance) \Rightarrow

$I_a + I_b + I_c = I_{Nn}$
 $V_n = 0, V_N \neq 0$
 $\Rightarrow V_N = \frac{Z}{Z_{line}} * I_{Nn}$

③ if No line between n & N $\Rightarrow V_N \neq 0, I_a + I_b + I_c = 0$

* Power in 3phase system:

$P_\Delta = P_Y = 3 V_p I_p \cos(\theta_v - \theta_i)$	$S_\Delta = S_Y = 3 V_p I_p^*$
$Q_\Delta = Q_Y = 3 V_p I_p \sin(\theta_v - \theta_i)$	$ S_\Delta = S_Y = \sqrt{3} V_L I_L $

* Losses in the 3phase system:

$S_{losses} = S_{source} - S_{load}$
 $S_{losses} = 3 |I_L|^2 Z_{T.L}$

* Wattmeter mesurments:

\Rightarrow Determine the voltage (V) & the current (I) that measured by this wattmeter then:

$P = |V| |I| \cos(\theta_v - \theta_i)$

* if 3-wattmeters used: $P_{Total} = P_1 + P_2 + P_3$

* In Two-Wattmeters method:

$P_T = P_1 + P_2$ $Q_T = \sqrt{3}(P_2 - P_1)$ $S_T = P_T + jQ_T$

$Pf = \cos \theta$ $\theta = \tan^{-1} \left(\frac{\sqrt{3}(P_2 - P_1)}{P_1 + P_2} \right)$

✳ CHAPTER (13):

✳ Linear Transformer:

⇒ Virtual source: we put it between the dot & the coil

* Choosing the polarities:

if the current enter the dot ⇒ take it (+ve) for the other dot.
if " " leaves " " ⇒ take it (-ve) " " " " " "

* Energy stored:

$W = \frac{1}{2} L_1 I_1^2 + \frac{1}{2} L_2 I_2^2 (\pm) M I_1 I_2$

(-) if one current leaves & the other enters. (+) if both currents leaving or entering the dots.

* Coupling Coefficient: $K = \frac{M}{\sqrt{L_1 L_2}}$

* For Linear transformer with current entering in primary & leaving in secondary:

$Z_{11} = R_1 + j\omega L_1$ + any other impedances in primary.

$Z_{22} = R_2 + j\omega L_2 + Z_L$ + any other impedances in secondary.

$Z_{in} = Z_{11} + \frac{(\omega M)^2}{Z_{22}}$

Reflected Impedance = $\frac{(\omega M)^2}{Z_{22}}$

⇒ you can find I_1 & I_2 easily from:

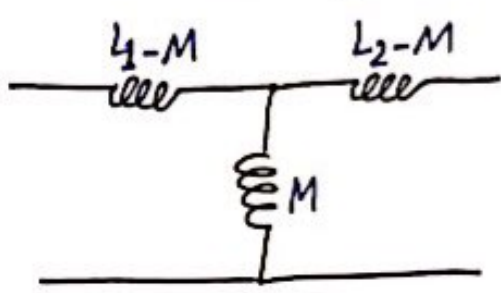
$I_1 = V_s / Z_{in}$

for I_2 : ⇒

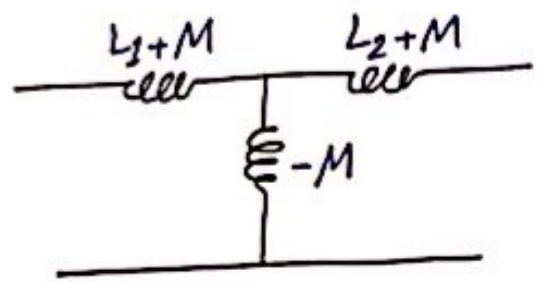
$I_2 = \frac{j\omega M}{Z_{22}} I_1$

if both currents entering the dot here you have to multiply I_2 by (-1) if you use this way.

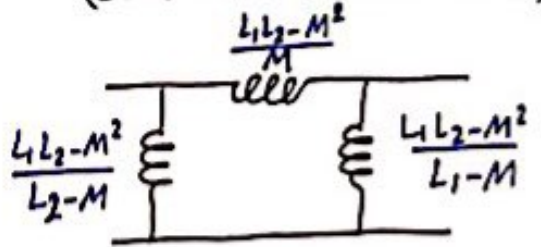
* T-equivalent ckt:
(Both currents entering) or leaving



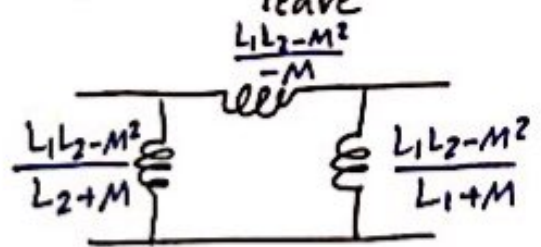
(one current enter and the other leave.)



* π-equivalent ckt:
(Both currents enter or leave)



(one current enter & other leave)



* We use T & π just if there is a connection between the primary & the secondary

* Ideal Transformer:

$a \text{ or } n = \frac{N_2}{N_1} = \frac{V_2}{V_1} = \frac{I_1}{I_2}$

for currents:
if the currents entering or leaving the dots together (-ve) n
otherwise (+ve) n

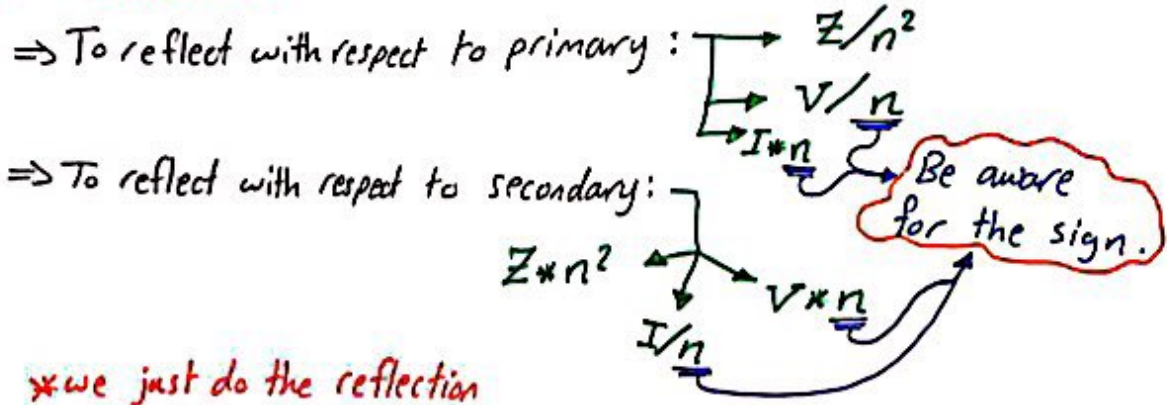
always n (+ve)
for $\frac{N_2}{N_1}$

for voltages:
if V_1, V_2 both (+ve) or both (-ve) ⇒ (+ve) n
otherwise (-ve) n .

* Complex Power:

$$S_{\text{primary}} = S_{\text{secondary}} = V_1 I_1^* = V_2 I_2^*$$

* Reflection:



* we just do the reflection if there is NO connection between primary & secondary. Otherwise, use mesh & nodal.

✱ CHAPTER (14):

* Common Relations for series & Parallel Resonance:

$$\beta = \frac{\omega_0}{Q_0}$$

$$\omega_0 = \frac{1}{\sqrt{LC}} \quad f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$\omega_0 = \sqrt{\omega_1 \omega_2}$$

$$\omega_{1,2} = \omega_0 \left[\sqrt{1 + \left(\frac{1}{2Q_0}\right)^2} \mp \frac{1}{2Q_0} \right]$$

* Approximate:

$$\omega_{1,2} = \omega_0 \mp \frac{1}{2}\beta$$

$$\omega_0 = \frac{1}{2}(\omega_1 + \omega_2)$$

$$N = \frac{\omega - \omega_0}{\frac{1}{2}\beta}$$

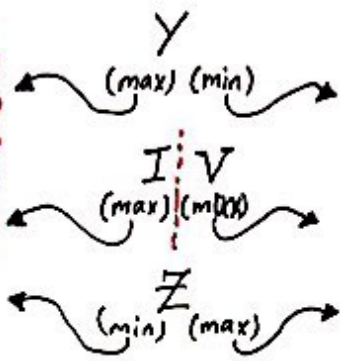
* Series Resonance:

$$Q_0 = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 RC}$$

$$|V_L(\omega_0)| = |V_C(\omega_0)| = V Q_0$$

$$Z = R + j\omega L + \frac{1}{j\omega C}$$

$$Z_{\text{app}} = R(1 + jN)$$



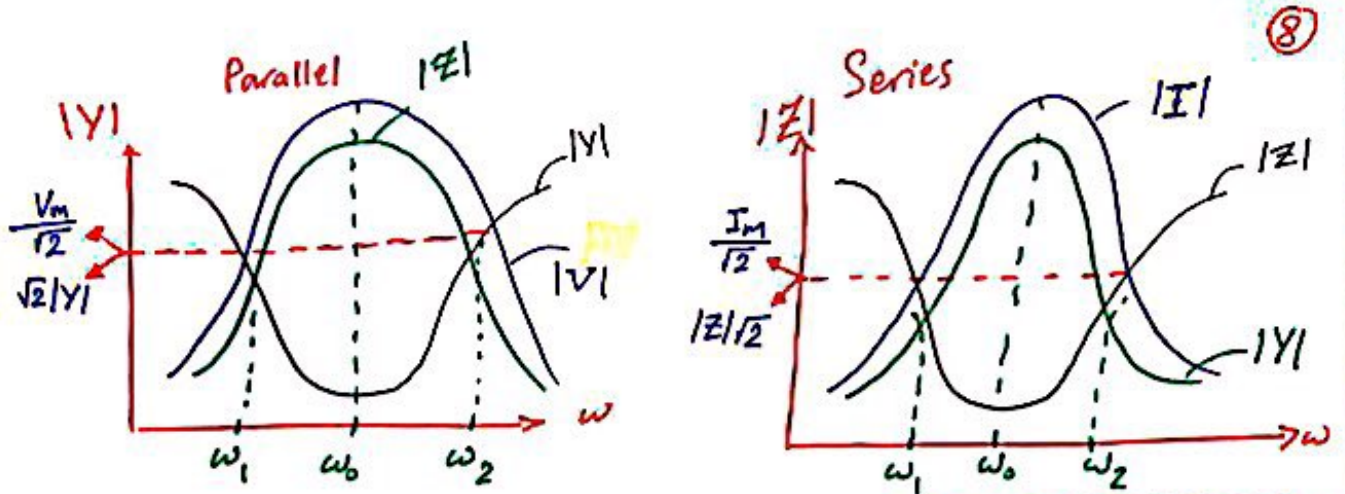
* Parallel Resonance:

$$Q_0 = \omega_0 RC = \frac{R}{\omega_0 L}$$

$$|I_L(\omega_0)| = |I_C(\omega_0)| = I Q_0$$

$$Y = \frac{1}{R} + j\omega C + \frac{1}{j\omega L}$$

$$Y_{\text{app}} = \frac{1}{R}(1 + jN)$$



***if you find $P(\omega_0)$ then $P(\omega_1) = P(\omega_2) = \frac{1}{2} P(\omega_0)$

***Other Resonance Forms:**

KEY: To find ω_0 just choose what is easy to deal with Z or Y then find the equivalent & put the imaginary part = 0

*** Transfer function:** $\frac{\text{output}}{\text{input}}$

*** Filters:**

*** Low pass filter:** RC ckt \Rightarrow output on C.
 RL ckt \Rightarrow output on R.
 other ckt \Rightarrow make $|H_V(\omega_c)| = \frac{1}{\sqrt{2}}$
 Then find $\underline{\omega_c}$.

$\omega_c = \frac{1}{RC}$
 $\omega_c = \frac{R}{L}$

*** High pass filter:** RL ckt \Rightarrow output on L.
 RC ckt \Rightarrow output on R.
 other ckt \Rightarrow put $|H_V(\omega_c)| = \frac{1}{\sqrt{2}}$
 Then find $\underline{\omega_c}$.

$\omega_c = \frac{R}{L}$
 $\omega_c = \frac{1}{RC}$

*** Band pass filter:** RLC ckt \Rightarrow output on R. $\Rightarrow \omega_0$ & ω_1 & ω_2 as in resonance.

*** Band stop filter:** RLC ckt \Rightarrow output on (L & C) $\Rightarrow \omega_0$ & ω_1 & ω_2 as in resonance.

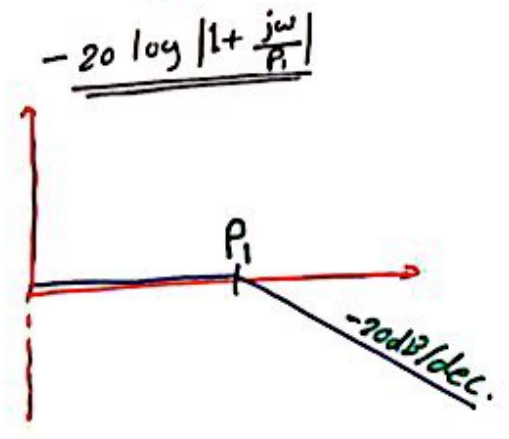
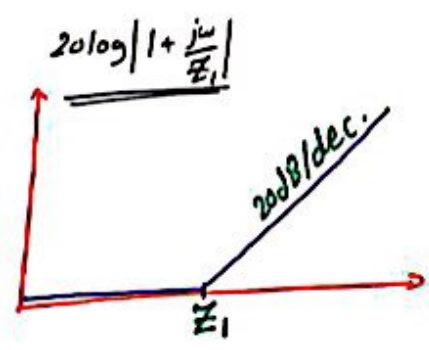
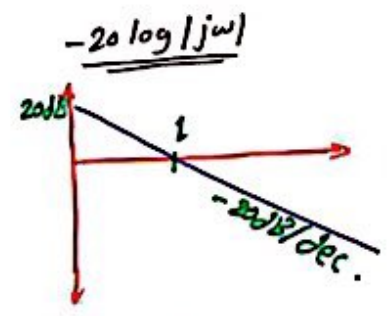
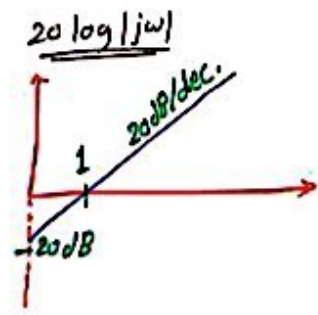
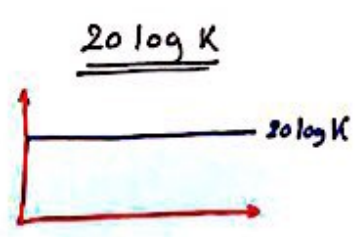
* Bode Plot: could be zero or pole.

⇒ standard form:

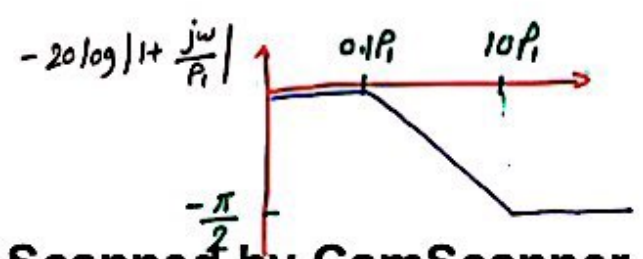
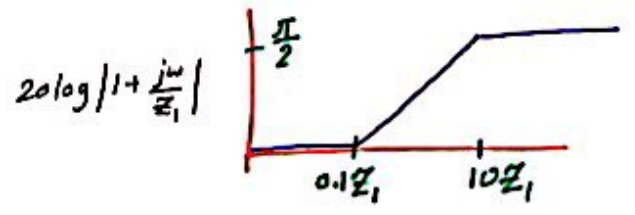
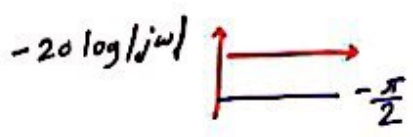
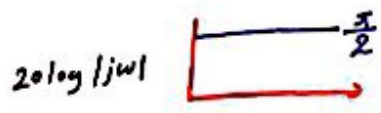
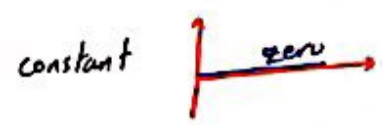
$$H(\omega) = \frac{K (j\omega)^{+1} \left[1 + \frac{j\omega}{Z_1} \right]}{\left[1 + \frac{j\omega}{P_1} \right]}$$

constant. Zero @ Z_1 Pole @ P_1

⇒ Drawing $H_V(\omega)$:



⇒ Drawing $\angle H_V(\omega)$:

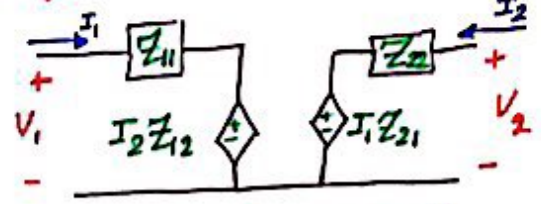


CHAPTER (19):

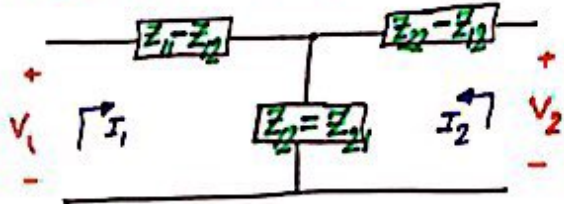
* Z-parameters:

* $I_2 = 0$:	* $I_1 = 0$:
$Z_{11} = \frac{V_1}{I_1}$	$Z_{22} = \frac{V_2}{I_2}$
$Z_{21} = \frac{V_2}{I_1}$	$Z_{12} = \frac{V_1}{I_2}$

* equivalent ckt for 2-port network:



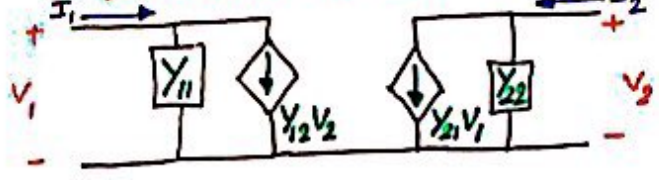
* Special case: (reciprocal)



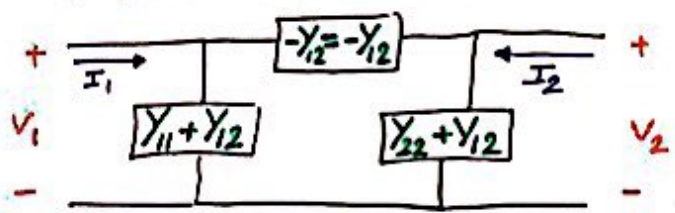
* Y-parameters:

* $V_2 = 0$:	* $V_1 = 0$:
$Y_{11} = \frac{I_1}{V_1}$	$Y_{12} = \frac{I_1}{V_2}$
$Y_{21} = \frac{I_2}{V_1}$	$Y_{22} = \frac{I_2}{V_2}$

* equivalent ckt for 2-port network:



* special case: (reciprocal)



* Z_{in} & Z_{out} :

$Z_{in} = \frac{V_1}{I_1}$

$Z_{out} = Z_{22} - \frac{Z_{12} Z_{21}}{Z_{11} + Z_g}$

GOOD

LUCK

