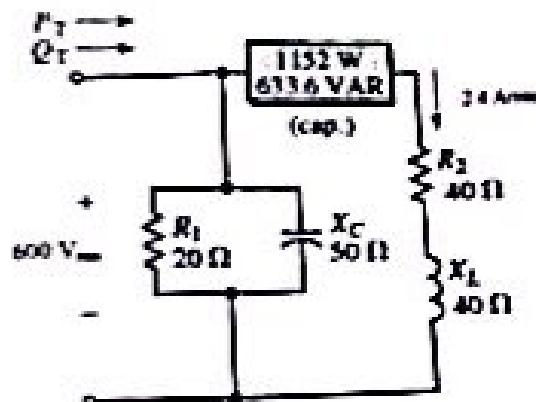


Question 4 (14 Points)

For the circuit shown below, Find:

- the total real power supplied by the source  $P_T$ .
- the total reactive power supplied by the source  $Q_T$ .
- the apparent power supplied by the source  $|S_T|$ .
- the complex power supplied by the source  $S_T$ .
- the source power factor.
- the total current supplied by the source.



$$P_T = 1152 + (2.4)^2 \times 40 + \frac{(600)}{20}$$

$$= 19.38 \text{ kW}$$

$$\textcircled{b} \quad Q_T = -633.6 + (2.4)^2 \times 40 - \frac{(600)}{50}$$

$$= -7.6 \text{ kVAR}$$

$$|S_T| = \sqrt{(19.38)^2 + (-7.6)^2}$$

$$= 20.81 \text{ kVA}$$

$$\textcircled{d} \quad S_T = 19.38 - j7.6$$

$$= 20.81 \angle -21^\circ$$

$$\textcircled{e} \quad \text{PF}_{\text{source}} = \cos(-21)$$

$$= 0.933$$

$$\textcircled{f} \quad I^T = \frac{S}{\sqrt{3}}$$

$$= \frac{19.38 \times 10^3 - j7.6 \times 10^3}{600 \angle 0^\circ}$$

$$= 35.36 \angle -21^\circ$$

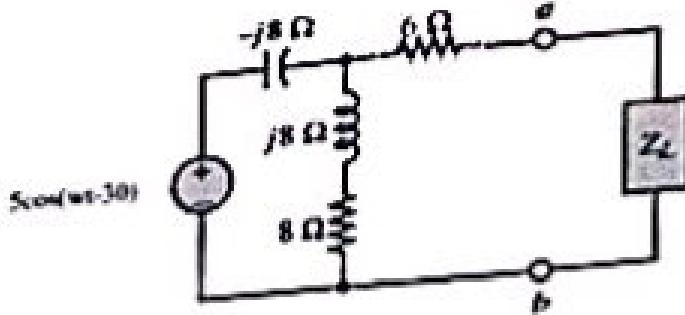
$$I = 35.36 \angle +21^\circ$$

$P_T$	$Q_T$	$ S_T $	$S_T$	$\text{PF}_{\text{source}}$	$I_{\text{max}}$
19.38 kW	-7.6 kVAR	20.81 kVA	$20.81 \angle -21^\circ$ kVA	0.933	$35.36 \angle +21^\circ$

### Question 1 (7 points)

For the circuit shown below:

- Find, draw and label the Thevenin equivalent circuit as seen by the load  $Z_L$ .
- What is the value of  $Z_L$  that maximizes the power transferred to the load.
- What is the value of this maximum power,  $P_{max}$ .
- What is value of the reactive power supplied by the source.
- If  $Z_L$  is replaced by a purely resistive load, what is the value of  $R_L$  that maximize the power transfer.
- and what is the value of this power in case (e).



Thevenin equivalent circuit

$$Z_{th} = 6 + \frac{(-j8)(8+j8)}{8}$$

$$= 16.12 \angle -29.1^\circ$$

$$\Rightarrow [14-j8] \sim$$

$$R_{th} = 5 \angle 0^\circ + \frac{8+j8}{8}$$

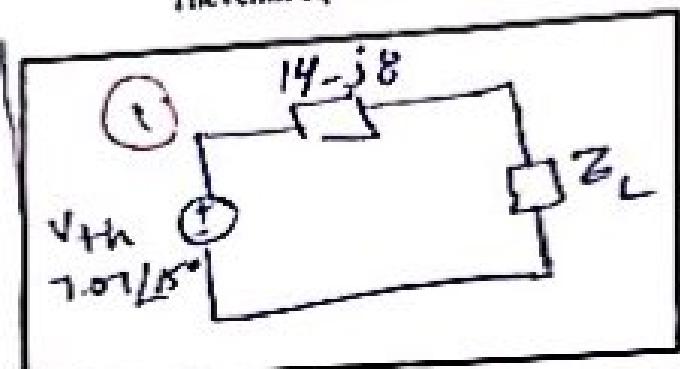
$$= [7.07 \angle 15^\circ] \sim$$

$$V_{th} = \frac{|V_{th}|^2}{8R_{th}} = \frac{(1.07)^2}{8 \times 14}$$

$$= 0.446 \text{ V}$$

source:  $\Im V \neq 0$  are in  
phase ( $\sin \theta = 0$ )

$$\theta = 0$$



$$\textcircled{3} \quad R_L = \sqrt{(R_{th})^2 + (X_{th})^2}$$

$$\Rightarrow \sqrt{14^2 + (8)^2}$$

$$= 16.12 \sim$$

$$\textcircled{4} \quad I_m = \frac{1.07 \angle 15^\circ}{14-j8+16.12}$$

$$= 0.227 \angle 29.87^\circ$$

$$P_{max} = \frac{1}{2} (0.227)^2 \times 16.12$$

$$= 0.415$$

$Z_L$	$P_{max}$	$\theta_{max}$	$R_L$	$P_{max}$
$14+j8 \Omega$	$0.446 \text{ W}$	$0$	$16.12 \Omega$	$0.415 \text{ W}$

1

2

3

4

5

Question 2 (4 points)

For the circuit shown,  $Z_1 = 10 + j12$  and  $Z_2 = 5 + j8$ . Find the following:

- the source PF.
- the total current supplied by the source (magnitude and phase).
- the value of a capacitor to be added in parallel with the loads to make the source PF = 0.95.
- the total source current after the capacitor is connected to the circuit (magnitude and phase).

a & b

$$Z_{eq} = \frac{(10 + j12)(5 + j8)}{10 + j20}$$

$$= 5.89 \angle 55^\circ$$

$$I_{rms} = \frac{V_{rms}}{Z} = \frac{120\angle 0^\circ}{5.89 \angle 55^\circ}$$

$$= 20.3 \angle -55^\circ$$

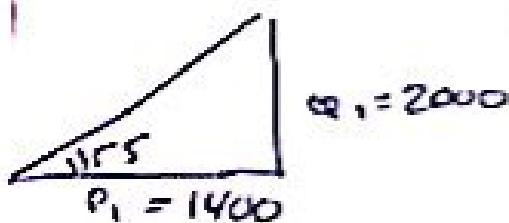
$$PF = \cos(0^\circ - 55^\circ)$$

$$= 0.513$$

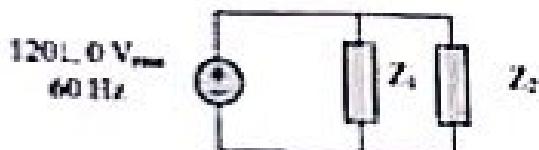
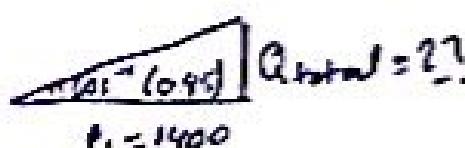
$$\textcircled{1} \quad S = P + jQ = 120\angle 0^\circ \times 20.3 \angle -55^\circ$$

$$= 1400 + j200$$

Before



After



$$Q_{total} = Q_C + Q_R$$

$$Q_{total} = I_s \times \tan(18.18^\circ) \times 0.95$$

$$= 460 \text{ VAR}$$

$$Q_C = 460 - 2000$$

$$= -1540 \text{ VAR}$$

$$C = \frac{Q_C}{\omega \sqrt{I_{rms}^2}} = \frac{1540}{2\pi(60)(20.3)}$$

$$= 2.831 \times 10^{-4} \text{ F}$$

$$\textcircled{2} \quad S = \sqrt{I^*}$$

$$1400 + j460 = 120\angle 0^\circ \times I^*$$

$$I^* = 2.23 \angle 18.18^\circ$$

$$I = 12.23 \angle -18.18^\circ$$

PF <sub>source</sub>	I <sub>source</sub>	C	I <sub>source</sub> after
0.513	20.35 ∠ -55°	2.831 × 10 <sup>-4</sup>	12.23 ∠ -18.18°

Name: KEY

Matric:

ID#

Serial #:

Question 1 (20 marks)

The voltage across a  $4\text{-j}5\Omega$  impedance is shown below. Find:

- the frequency of the signal,  $f$ .
- the voltage effective value (rms)  $V_{rms}$ .
- the average real power delivered to the load,  $P_{avg}$ .

(a)



$$T = 0.3 \text{ sec}$$

$$f = \frac{1}{T} = \frac{1}{0.3} = 3.33 \text{ Hz}$$

$$= \sqrt{\frac{2}{0.3} \times 400 \frac{(\cdot)^2}{J}} = 0$$

$$= \frac{1}{3} V_{rms}$$

(b)  $V_{rms} = \sqrt{\frac{1}{T} \int_0^T v(t) dt}$

where

$$v(t) = \begin{cases} -2t & 0 \leq t < 0.05 \\ 20t - 3 & 0.15 \leq t < 0.2 \\ 0 & \text{elsewhere} \end{cases}$$

(c)



$$I_{rms} = \frac{1}{\sqrt{4 + j5}}$$

$$= 0.052 \angle -51.3^\circ$$

$$\Rightarrow P_{avg} = |I_{rms}|^2 R$$

$$\Rightarrow (0.052)^2 \times 4$$

$$= 0.011 \text{ W}$$

$f$	$V_{rms}$	$P_{avg}$
3.33 Hz	$\frac{1}{3} V_{rms}$	0.011 W

✓ ✓ ✓ ✓ ✓