

Amplifiers

NoteBook

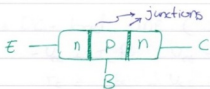
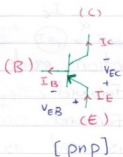
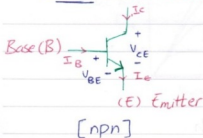
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* Transistor: BJT & FET

• BJT: (C) collector



* Mode of operation for BJT:-

1. Forward-active mode (or active region)

BE: Forward-biased

BC: Reverse-biased

→ BJT is used as Amplifier.

• $V_{BE} = V_{BE(ON)} = 0.7V$

• $V_{CE} > V_{CE(sat)}$ where $V_{CE(sat)} \approx 0.2V$ or $0.3V$

• $I_C = \beta I_B$, β : Gain [unitless] → at a certain temperature, characteristic of the transistor

- $50 < \beta < 300$
- $I_C = (1 + \beta) I_B$
- $I_C = \frac{1}{\alpha} I_E$

2. Saturation mode ::

BE: Forward

BC: Forward

BJT is used as a switch.

- $V_{BE} = 0.7V$
- $V_{CE} = V_{CE(sat)}$
- $I_C < \beta I_B$

3. Inverse-active mode:

BE: reversed - biased

BC: forward - biased

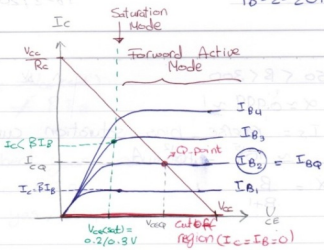
4. Cutoff mode:

BE: reverse

BC: reverse

$$I_C = I_B = I_E = 0$$

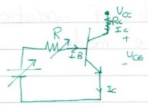
18-2-2014 / Tue



* DC-load line ($I_C \propto V_{CC}$)

$$-V_{CC} + I_C R_C + V_{CE} = 0$$

$$I_C = \frac{V_{CC}}{R_C} - \frac{V_{CE}}{R_C}$$



* V_T : Thermal voltage ($V_T = 0.026$) at room temperature 300k

- $50 < \beta < 300$
- $\alpha \approx 0.999 \approx 1$
- $I_s =$ reverse-bias saturation current
 $\approx 10^{-15} - 10^{-12} \text{ A}$
- $\alpha = \frac{\beta}{\beta + 1}$

* DC analysis of BJT :-

- Finding the mode of operation.
- DC load line.
- Finding the relation between v_o & v_i .
- DC analysis of multi-stage circuit.

• Steps for finding the mode of operation:

① Assume Forward-active mode

$$\rightarrow V_{BE} = 0.7$$

$$\rightarrow I_C = \beta I_B$$

② check your assumption

$$\rightarrow I_B > 0 \text{ and } V_{CE} > V_{CE}(\text{sat}), \text{ if yes stop}$$

③ otherwise assume saturation mode

$$\rightarrow V_{BE} = 0.7$$

$$\rightarrow V_{CE} = V_{CE(\text{sat})}$$

$$I_C \neq \beta I_B$$

④ check your assumption

$$I_C < \beta I_B$$

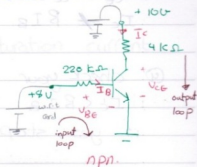
if yes, stop

⑤ otherwise, cut off mode.

Ex.: consider the following ckt:-

Given: $\beta = 100$, $V_{BE(on)} = 0.7V$

$V_{CE(sat)} = 0.2V$



1. Find the mode of operation

• assume F.A.M. \rightarrow I_C خروجي
 I_B و

$V_{BE} = 0.7$ I_C و I_B و

$I_C = \beta I_B$

\rightarrow input loop:

$-8 + 220 I_B + 0.7 = 0$

$I_B = \frac{8 - 0.7}{220} = 33.2 \mu A > 0 \checkmark$

$I_C = \beta I_B = 100 * 33.2 \mu A = 3.32 \text{ mA}$

\rightarrow output loop:

$-10 + 4 * 3.32 + V_{CE} = 0$

$V_{CE} = 10 - 4 * 3.32 = -3.28V > V_{CE(sat)}$

No, incorrect assumption.

• assume saturation mode

$V_{BE} = 0.7V$

$V_{CE} = V_{CE(sat)} = 0.2V$

\rightarrow input loop $\rightarrow I_B = 33.2 \mu A$

→ output loop:-

$$-10 + 4 I_c + 0.2 = 0$$

$$I_c = 2.45 \text{ mA}$$

check : $I_c \stackrel{?}{<} \beta I_B$

$$2.45 < 3.32 \quad \checkmark$$

yes, saturation Mode

2. Find Q-point values:-

$$Q\text{-point values: } I_{BQ} = 3.32 \text{ mA}$$

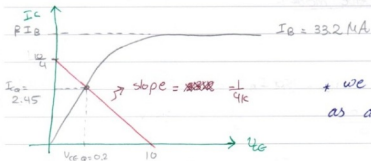
$$I_{CQ} = 2.45 \text{ mA}$$

$$V_{CEQ} = 0.2 \text{ V}$$

3. Find and draw the DC load line:-

$$-10 + 4 I_c + V_{CE} = 0$$

$$I_c = \frac{10 - V_{CE}}{4} \text{ [mA]} \rightarrow \text{DC-load line.}$$



* we cant use it as amplifier.

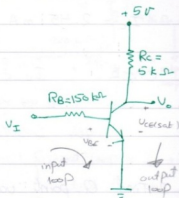
* Ex * Draw the voltage transfer curves ($V_o \times V_i$) for the following cct :-

Given:

$$V_{BE(sat)} = 0.7 \text{ V}$$

$$V_{CE(sat)} = 0.2 \text{ V}$$

$$\beta = 120$$



• cutoff :-

$$I_C = I_B = I_E = 0$$

$$\rightarrow V_o = 5 \text{ V} \quad (V_i \text{ غير موجودة})$$

• saturation :-

$$V_{CE(sat)} = 0.2$$

$$\rightarrow V_o = 0.2 \text{ V}$$

• Forward active mode :-

$$V_{BE} = 0.7$$

$$I_C = \beta I_B$$

$$\rightarrow \text{input loop: } -V_i + 150 I_B + 0.7 = 0$$

$$I_B = \frac{V_i - 0.7}{150}$$

$$\rightarrow \text{output loop: } -5 + 5 I_C + V_o = 0$$

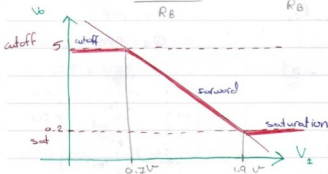
$$I_c = \frac{5 - V_o}{5}$$

$$\Rightarrow I_c = \beta I_B$$

$$\frac{5 - V_o}{5} = 120 \left(\frac{V_i - 0.7}{150} \right)$$

$$V_o = 5 - 120 \frac{R_c}{R_B} V_i + \frac{120 R_c + 0.7}{R_B}$$

$$V_o = 5 + \frac{120 R_c + 0.7}{R_B} - 120 \frac{R_c}{R_B} V_i \quad \text{"negative slope"}$$



cutoff and sat
slope. βI_B is

1

• Example :- *input loop then output loop*
use thevenin circ. to find V_{BE}

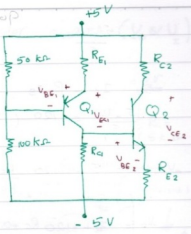
Given:-

$\beta = 100$ for both Q_1 & Q_2

$I_{C1} = I_{C2} = 0.8 \text{ mA}$

$V_{EB1} = V_{BE2} = 0.7 \text{ V}$

$V_{EC1} = 3.5 \text{ V}$, $V_{EE2} = 4 \text{ V} \rightarrow Q_1 \text{ \& \& } Q_2$
are in F.A.M



• Find R_{E1} , R_{C1} , R_{E2} , R_{C2}

Q_1 : pnp

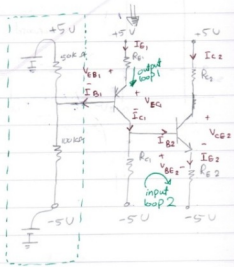
Q_2 : npn

$\Rightarrow I_{B1} = I_{B2} = \frac{I_{C1}}{\beta} = \frac{0.8}{100}$

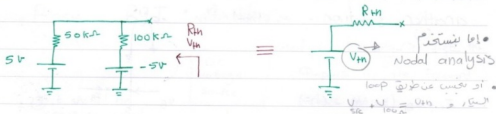
$I_{B1,2} = 8 \text{ \mu A}$

$\Rightarrow I_{E1} = I_{E2} = (1 + \beta) I_{B1}$

$I_{E1,2} = 0.808 \text{ mA}$



2



$$R_{th} = 50 // 100 = \frac{5000}{150} = 33.3 \text{ k}\Omega$$

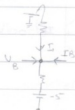
$$-5 + 50I + 100I + -5 = 0$$

$$I = \frac{10}{150} \text{ mA}$$

$$\rightarrow -V_{th} + I(100) - 5 = 0$$

$$V_{th} = \frac{-5 + 1000}{150}$$

في المخطط الثاني



input loop 1 :- $-5 + \vec{I}_{E1} R_{E1} + 0.7 + \vec{I}_{B1} \vec{R}_{th} + \vec{V}_{th} = 0 \Rightarrow R_{E1} = 2.93 \text{ k}\Omega$

output loop 1 :- $-5 + \vec{I}_{E1} \vec{R}_{E1} + \vec{V}_{CE1} + R_{C1} (\vec{I}_{C1} - \vec{I}_{B2}) - 5 = 0 \Rightarrow R_{C1} = 520 \text{ k}\Omega$

input loop 2 :- $-(5) - R_{C1} (\vec{I}_{C1} - \vec{I}_{B1}) + \vec{V}_{CE2} + \vec{I}_{E2} R_{E2} - 5 = 0 \Rightarrow R_{E2} = 4.25 \text{ k}\Omega$

output loop 2 :- $-5 + \vec{I}_{C2} R_{C2} + \vec{V}_{CE2} + \vec{R}_{E2} \vec{I}_{E2} - 5 = 0 \Rightarrow R_{C2} = 3.215 \text{ k}\Omega$

3

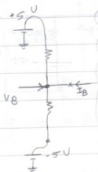
another solution:- 'without V_{th} '

$$I_1 = \frac{5 - V_B}{50}$$

$$I_1 + I_{B1} = \frac{V_B - (-5)}{100}$$

$$\frac{5 - V_B}{50} + I_{B1} = \frac{V_B + 5}{100}$$

$$\rightarrow V_B = \dots$$



input loop:-

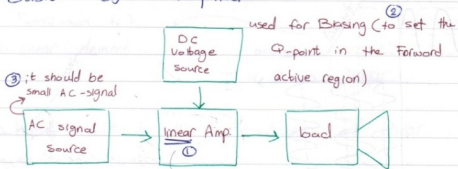
$$-5 + I_{B1} R_{E1} + V_{EB} + V_B = 0$$

BJT - MOS → control the Biasing → Q-point position

25-2/2014 Tue.

(4)

• Basic BJT Amplifier:-

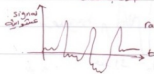


eg: microphone
CD player
U Card & Gmp

we can apply super position
& DC-analysis
& AC-analysis

speaker

DC-analysis kill to AC-sfcs
والتحليل للتيار المستمر لا يؤثر على التحليل للتيار المتردد



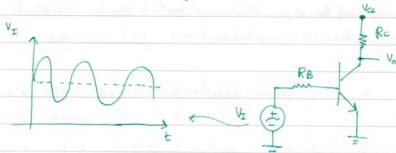
random → take it as a f'n. Design

we use sin signal → Random signal
نستخدم إشارة جيبية بدلاً من الإشارة العشوائية
sin... + sin... + ...

linear amp → output = const * Input

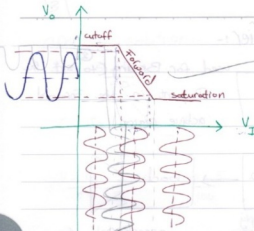
O/I constant
إخراج ثابت

1. The transistor in Amplifier circuit should be in the forward-active Region. why?!



$v_i = 3 + 2 \sin \omega t$

[5]



if it non-linear

بغير جزء يتغير مقدار من جبهة
ومن الجهد الثانيه بيتغير مقدار

تأني!



عند V_o

لانه غيرا مكان ال point
مجزء من ال signal
مع يطلع مع صيقت ال cutoff
الصلن قا بيتغير بصير من صت
مثلا س حسب الموقع!

• في حالة ال Saturation & cutoff يكون $V_o = 0$ ثابت

او في Forward active Mode يوجد علاقة جبهة \rightarrow بصير بقدر العمل amplification ال signal.

• لازم تكون Linear Relationship

• باعز small-AC-signal لانه يتكون اقرب ال linear



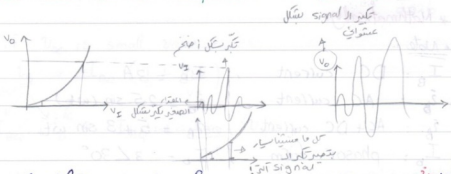
1

2. we need a linear amplifier, why?

⇒ linear element: $I \propto V$ is linear.

⇒ linear circuit: all its components are linear.

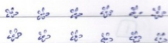
⇒ linear Amplifier: means that the Relation between V_I and V_O is linear. "to get linear amplifier we need all its components to be linear."



• Amplifier consists of: $I \propto V$ (linear), $I \propto V$ (linear), and a non-linear transistor.

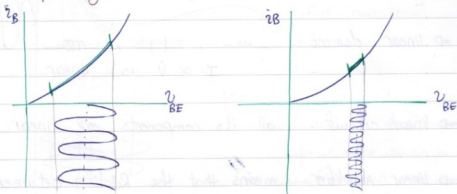
3. we need small AC-signal to get a linear transistor. How?





2

* Graphically :-



* Mathematically :-

* Note :-

 I_B : DC current , $I_B = 3A$ i_b : AC current , $i_b = 2.5 \sin(\omega t)$ i_B : AC + DC current , $i_B = 5 + 3 \sin \omega t$ I_b : phasor form , $I_b = 3 \angle 30^\circ$

Reverse saturation current is

$$\rightarrow \text{We know that } i_B = \frac{I_s \exp\left(\frac{v_{BE}}{V_T}\right)}{1 + \beta}$$

$$= \frac{I_s}{1 + \beta} \exp\left(\frac{V_{BEQ} + v_{be}}{V_T}\right)$$

$$\rightarrow i_B = \underbrace{\frac{I_s}{1 + \beta} \exp\left(\frac{V_{BEQ}}{V_T}\right)}_{I_{BQ}} \cdot \exp\left(\frac{v_{be}}{V_T}\right)$$

(3)

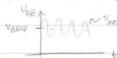
$$i_B = I_{BQ} \cdot \exp\left(\frac{v_{be}}{V_T}\right)$$

Note:-

Taylor Series: $e^{\theta} = \frac{\theta^0}{0!} + \frac{\theta^1}{1!} + \frac{\theta^2}{2!} + \frac{\theta^3}{3!} + \dots$

if $\theta \ll 1 \Rightarrow e^{\theta} \approx 1 + \theta$ linear Relationship exponential Relationship

$\Rightarrow e^{\frac{v_{be}}{V_T}} \approx 1 + \frac{v_{be}}{V_T}$ if $\frac{v_{be}}{V_T} \ll 1$



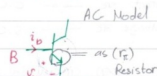
$v_{be} \ll V_T$
0.026

if v_{be} is small value :-

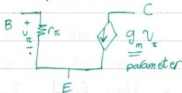
$$i_B \approx I_{BQ} \left(1 + \frac{v_{be}}{V_T}\right)$$

$I_{BQ} + i_b \approx I_{BQ} + \frac{I_{BQ}}{V_T} v_{be}$

$i_b = \frac{I_{BQ}}{V_T} v_{be}$ \Rightarrow So linear relationship



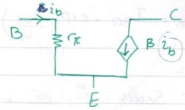
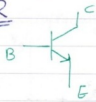
\therefore small signal Hybrid- π equivalent cct.



\downarrow transistor \downarrow linear ckt

4

OR



- $r_{\pi} = \frac{V_T}{I_{BQ}}$ " diffusion resistance " [Ω]
- $g_m = \frac{I_{CQ}}{V_T}$ " transconductance " A/V [S]
- $r_{\pi} \times g_m = \beta$

* procedure: DC analysis then AC analysis *

A-parameter Model: X غير مطلوب

* General steps to Solve an Amplifier circuit :-

① DC-analysis :-

- Draw DC-equivalent cct
- kill all AC-sources
 $\left\{ \begin{array}{l} \text{current src} \rightarrow \circ - \circ \text{ O.C} \\ \text{voltage src} \text{ --- } \text{S.C} \end{array} \right.$
- replace all capacitors by open circuit
 $\left\{ \begin{array}{l} \text{سلسلة} \\ \text{S.C بى خارج سلسلتها} \end{array} \right.$
- keep all DC-sources.
- then find I_{BQ}, I_{CQ}, V_{CEQ}



② AC-analysis:-

- Draw the AC-equivalent cct.:-
- 1- Replace the transistor by the Hybrid- π equivalent
- 2- Kill all DC-sources
- 3- Replace all capacitor by short-circuit

• Find voltage gain $A_v = \frac{v_o}{v_i}$

$$i_b, i_c, v_{ce}, R_i, R_o$$

4-then by using super position :-

find result = AC + DC

$$i_B = i_b + I_{BQ}$$

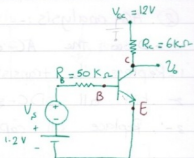
* Ex 6.1

$\beta = 100, V_{BE(ON)} = 0.7 \text{ V}$

Find the voltage gain

$A_v = \frac{v_o}{v_s}$

$v_s = 0.25 \sin \omega t$



• DC-analysis :-

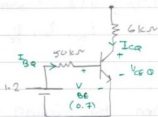
⇒ DC equivalent ckt :-

∴ input loop :-

$-1.2 + I_{BQ}(50) + 0.7 = 0$

$I_{BQ} = 10 \mu\text{A}$

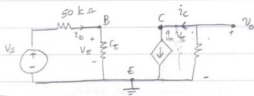
$I_{CQ} = \beta I_{BQ} = 1 \text{ mA}$



• AC-analysis :-

⇒ AC equivalent ckt :-

$A_v = \frac{v_o}{v_s}$



$v_o = -g_m v_{\pi} R_C \rightarrow [1]$

$v_{\pi} = v_s \frac{r_{\pi}}{r_{\pi} + R_B} \rightarrow [2]$

2-3-2014 Sunday

Sub (2) in (1):-

$$v_o = -g_m R_c * \frac{v_s r_\pi}{r_\pi + R_B}$$

$$\therefore A_v = \frac{v_o}{v_s} = \frac{-g_m R_c r_\pi}{r_\pi + R_B}$$

$$r_\pi = \frac{V_T}{I_{BQ}} = \frac{0.026}{10 \times 10^{-6}} = 2.6 \text{ k}\Omega$$

$$\rightarrow g_m = \frac{I_{CQ}}{V_T} = 38.5 \text{ mA/V}$$

$$A_v = -11.4$$

-ve sign:- phase shift = 180° between v_s and v_o

Find and Draw

i_B , i_C , v_{CE} if $v_s = 0.25 \sin \omega t$

From AC-cct

$$i_B = \overset{\uparrow}{i_b} + I_{BQ}$$

$$i_B = \frac{v_s}{50} + 10 \mu$$

so far

$$i_B = \frac{0.25 \sin \omega t}{50 + 2.6} + 10 \mu$$

$$i_B = 4.75 \sin \omega t \mu + 10 \mu$$

$$\tilde{i}_c = i_c + I_{CQ}$$

$$\tilde{i}_c = \beta i_b + I_{CQ}$$

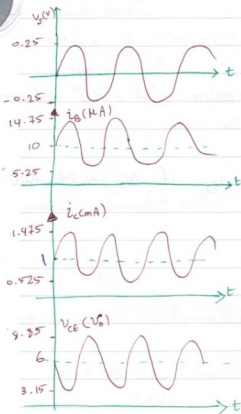
$$i_c = 0.475 \sin \omega t + 1 \text{ mA}$$

$$v_{CE} = v_{ce} + V_{CEQ}$$

$$v_{CE} = -i_c R_c + 12 - I_{CQ} \times 6$$

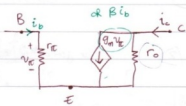
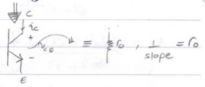
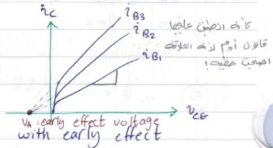
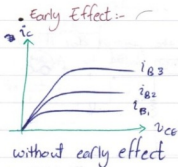
$$v_{CE} = -2.85 \sin \omega t + 6 \text{ V}$$

where $V_{CE} = V_0$



Because there's different units

* Hybrid π - equivalent model including the Early Effect:



→ the AC-equivalent with early effect.

* early effect $\rightarrow r_o$ parallel to β

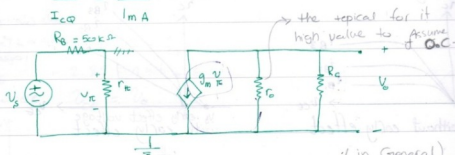
$$r_o = \frac{V_A}{I_{CQ}}$$

* the early effect reduce the (gain voltage).

Ex :- consider the last example :-

Find $A_v = \frac{v_o}{v_i}$, if $V_A = 50V$.

$$r_o = \frac{V_A}{I_{CQ}} = \frac{50}{1mA} = 50 k\Omega$$



$$A_v = \frac{v_o}{v_s}$$

(in General)
early effect
↓
reduce / decrease the
Gain

$$v_o = -g_m v_{\pi} (R_C // r_o) \dots (1)$$

$$v_{\pi} = v_s \frac{r_{\pi}}{r_{\pi} + R_B} \dots (2)$$

Sub (2) in (1).

$$v_o = -g_m (R_C // r_o) v_s \frac{r_{\pi}}{r_{\pi} + R_B}$$

$$A_v = -g_m (R_C // r_o) \frac{r_{\pi}}{r_{\pi} + R_B}$$

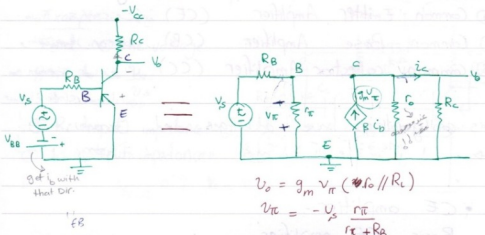
$A_v = -10.2$ The early effect reduces the Gain.

nPN → pNP : Biasing → V_{BE} و V_{CE}
 - Alternating current V_{BE} و V_{CE}
 مع V_{BE} و V_{CE}
 مع V_{BE} و V_{CE}

4-3-2014 Tue

* PnP - transistor :

Account for the early effect

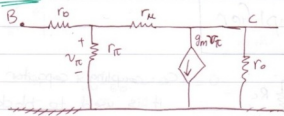


$$V_o = g_m V_{\pi} (r_o \parallel R_C)$$

$$V_{\pi} = -V_s \frac{r_{\pi}}{r_{\pi} + R_B}$$

same as npn ← $A_v = -\frac{g_m (r_o \parallel R_C) r_{\pi}}{r_{\pi} + R_B}$

* Note *



$r_o \approx 0 \rightarrow$ very small value \rightarrow S.C
 $r_{\pi} = \infty \rightarrow$ very high value \rightarrow O.S
 we can negligible it.

* Basic Transistor Amplifier configuration:-

- ① Common Emitter Amplifier (CE) من ال 0 / 3 مشتركة
- ② Common Base Amplifier (CB) واطببق هو ال common
- ③ Common collector Amplifier (CC) ال common هو الفرع البخر مشترك على اي شيء!

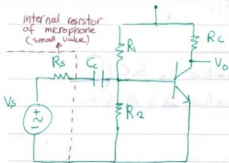
these configurations have advantages and Disadv...

→ البحر عن التمر من مشترك! (multistage)

• CE amplifier:-

- 1 - Basic CE amplifier
- 2 - Basic CE amplifier with Emitter resistor
- 3 - Basic CE amplifier with Emitter resistor and Bypass capacitor.
- 4 - Advanced CE amplifier

1. Basic CE Amplifier



C_c : coupling capacitor
 it is used to block any DC component from the user. SO, the position of Q-point is independent on the DC component from the user.

user sign from microphone

Basic CE Amplifier:-

Example:-

Find: ① the voltage

gain $A_v = \frac{v_o}{v_{is}}$

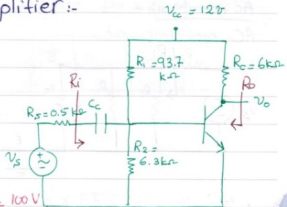
Amplification factor

② R_i "input impedance"

③ R_o "output impedance"

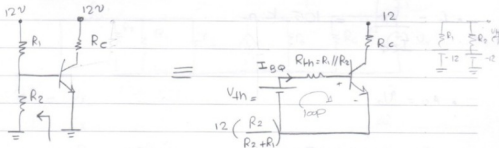
$\beta = 100$

$V_{BE} = 0.7$ $V_{CC} = 100V$



DC analysis:-

DC equivalent ckt:-



$-V_{th} + R_{th} I_{BQ} + 0.7 = 0$

$I_{BQ} = 9.5 \mu A$

$I_{CQ} = \beta I_{BQ} = 0.95 mA$

$V_{ceQ} = 12 - I_{CQ} R_c = 6.31 V$ $\approx \frac{1}{2} (V_{CC}) \rightarrow$ Best value!

Qpt 100

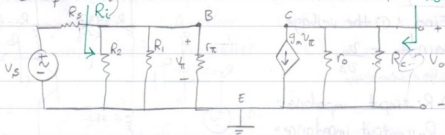
Best value to get good Amplification

$\frac{12 - 12}{2} = -12 \text{ V}$

AC-analysis:-

AC-equivalent ckt:-

s.c. $\rightarrow R_o$



$$\bullet r_{\pi} = \frac{V_T}{I_{BQ}} = 2.74 \text{ k}\Omega$$

I_{BQ}

$$\bullet g_m = \frac{I_{CQ}}{V_T} = 36.5 \text{ mA/V}$$

$$\bullet r_o = \frac{V_A}{I_{CQ}} = 105 \text{ k}\Omega$$

I_{CQ}

$$\bullet A_v = \frac{V_o}{V_s}$$

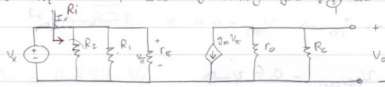
$$\rightarrow V_o = -g_m V_{\pi} (R_c \parallel r_o) \rightarrow (1)$$

$$\rightarrow V_{\pi} = V_s \frac{(R_1 \parallel R_2 \parallel r_{\pi})}{R_1 \parallel R_2 \parallel r_{\pi} + R_s} \rightarrow (2)$$

Sub (2) in (1)

$$A_v = \frac{V_o}{V_s} = \frac{-g_m (R_c \parallel r_o) (R_1 \parallel R_2 \parallel r_{\pi})}{(R_1 \parallel R_2 \parallel r_{\pi}) + R_s} = -163$$

to find R_i indep sources sig killing sig v_x src v_x

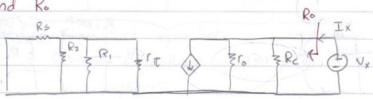


$$R_i = \frac{V_x}{I_x} \text{ , using Vth}$$

$$-V_x + I_x (R_1 \parallel R_2 \parallel r_E) = 0$$

$$R_i = \frac{V_x}{I_x} = R_1 \parallel R_2 \parallel r_E = 1.87 \text{ k}\Omega$$

to find R_o



$$R_o = \frac{V_x}{I_x}$$

$$\Rightarrow R_o = r_o \parallel R_C$$

$$= 5.68 \text{ k}\Omega$$

Advantage:- high A_v

Disadvantage:- 1. very sensitive to $V_{BE(on)}$ \rightarrow (unstable performance)

المقاومة تؤثر على $V_{BE(ON)} = 0.7V \Rightarrow$

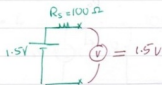
$I_{BQ} \rightarrow I_{CQ} \rightarrow V_{CEQ} = 6.31V$ "Forward"

if $V_{BE(ON)} = 0.6V \Rightarrow$

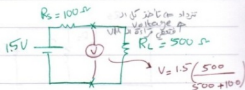
$I_{BQ} \rightarrow I_{CQ} \rightarrow V_{CEQ} = -3.6V$ "Not Forward"

2. high loading effect:-

loading effect:



src without load



src with load $= 1.25V$
 $1.25 < 1.5$

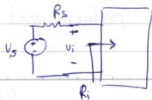
\rightarrow To reduce the loading effect ($v_o \approx v_s$)
 R_L should be $\gg R_s$

\rightarrow in our example:

$R_i = 1.87 k\Omega$

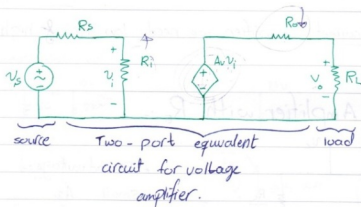
$R_s = 0.5 k\Omega$

$R_s \ll R_i$



$$v_i = v_s \frac{R_i}{R_i + R_s}$$

$$v_i = 0.789 v_s$$



$$\bullet v_i = v_s \frac{R_i}{R_i + R_s}$$

To reduce the loading effect on the input circuit ($v_i \approx v_s$) we need high R_i

$$\bullet v_o = A_v v_i \frac{R_L}{R_L + R_o}$$

To reduce the loading effect on the output

circuit ($v_o \approx A_v v_i$) we need low R_o $v_i R_i$ is Voltage in v_i

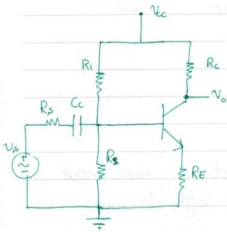
• (High R_i and low R_o) Good voltage \rightarrow Voltage Amp.

voltage Amp \rightarrow Voltage \rightarrow Good current \rightarrow Current Amp.



\rightarrow For current amplifier we need low R_i & high R_o

• CE-Amplifier with R_E :-



* Disadvantage :-

Small A_v

* Advantages :-

1. A_v is less dependent on β (stable gain)
2. small loading effect.

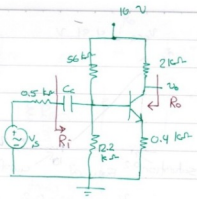
* Example *

$\beta = 100$, $V_A = \infty$ (no early effect, $r_o = \infty$ open ckt),

$V_{BE(on)} = 0.7 \text{ V}$

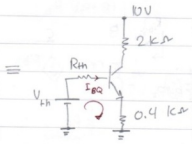
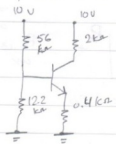
Find :-

- ① A_v ② R_i ③ R_o



• DC analysis :-

DC equivalent ckt:



$$R_{th} = 56 // 12.2$$

$$R_{th} = 10 \text{ k}\Omega$$

$$V_{th} = 1.78 \text{ V}$$

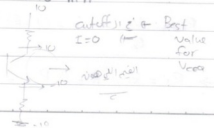
* input loop :-

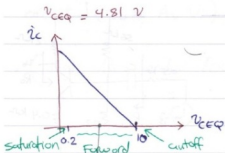
$$-V_{th} + R_{th} I_{BQ} + 0.7 + 0.4(1 + \beta) I_{BQ} = 0$$

$$I_{BQ} = 0.0216 \text{ mA} = 21.6 \mu\text{A}$$

$$I_{CQ} = \beta I_E = 100 \times 21.6 \mu\text{A} = 2.16 \text{ mA}$$

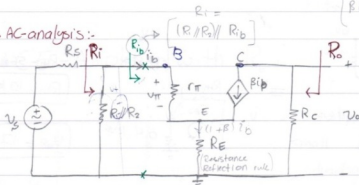
$$V_{CEQ} = 4.81 \text{ V}$$





mid point
 $V_{ceq} = \frac{10 + 0.2}{2} = 5.1$ Best value for V_{ceq}

• AC-analysis:



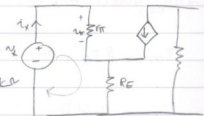
$\beta i_b \rightarrow$ with R_E
 R_E \rightarrow $\frac{0 + I_x}{\beta i_b}$
 \rightarrow $\frac{V_x}{\beta i_b}$

$$R_{ib} = \frac{V_x}{I_x}$$

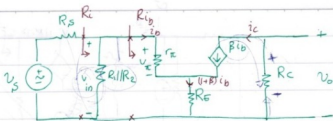
$$-V_x + I_x r_{\pi} + (1 + \beta) I_x R_E = 0$$

$$R_{ib} = \frac{V_x}{I_x} = (r_{\pi} + (1 + \beta) R_E) = 41.6 \text{ k}\Omega$$

$$\rightarrow R_i = R_1 // R_2 // R_{ib} = 8.06 \text{ k}\Omega$$



11-3/2014 Tue



$$R_i = R_1 // R_2 // R_{ib}$$

$$R_{ib} = r_{\pi} + (1 + \beta) R_E$$

$$A_v = \frac{v_o}{v_s}$$

$$\rightarrow v_o = -\beta i_b R_C \quad \text{--- (1)}$$

$$v_i = v_s \frac{R_i}{R_i + R_s}$$

$$i_b = \frac{v_i}{R_{ib}} = v_s \frac{R_i}{R_{ib} (R_i + R_s)} \quad \text{--- (2)}$$

use 1 & 2:-

$$A_v = \frac{v_o}{v_s} = \frac{-\beta R_C}{r_{\pi} + (1 + \beta) R_E} \left(\frac{R_i}{R_i + R_s} \right)$$

$$\boxed{A_v = -4.53} \text{ exact value.}$$

approximate value of $A_v \approx \frac{-R_c}{R_E}$ نقد، تقريبا، قيمته
but up this is exam

Because:-

- $(1 + \beta) R_E \gg r_e$
- $R_i \gg R_s$

Disadvantage:- small $A_v = -4.53$

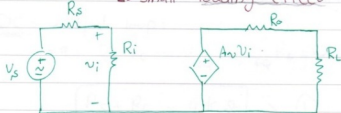
Advantage :- 1. A_v is less dependent on β

في النسبة والاعتماد
 يتغيروا سواء تغيرت β

β	A_v
50	-4.41
100	-4.53
150	-4.57

A_v stable & remains constant.

2. small loading effect



جاءت $\uparrow R_i$
 في A_v
 loading effect
 جلت

$V_i = V_s \frac{R_i}{R_i + R_s} \rightarrow 8.06$
 $R_i + R_s \rightarrow 0.5 k\Omega$

npn or pnp
 نفس المبدأ

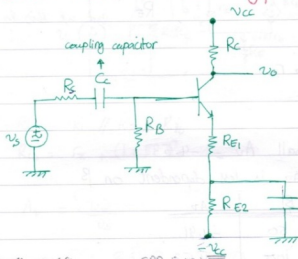
$V_i = 0.942 V_s$

for stability use *
 this design CE with R_E
 but the gain \rightarrow multistage

loading effect \rightarrow Buffer \rightarrow R_L & R_o \rightarrow R_E

11-3-2014 / TUE

3. CE with R_E and Bypass Capacitor:-



(S.C)

$$A_v = \frac{R_C}{R_E} \text{ in AC}$$

$\rightarrow R_E = R_{E1} + R_{E2}$

DC analysis $R_E \uparrow$
 high ω \rightarrow low gain
 $\rightarrow R_E = R_{E1} + R_{E2}$ (open ckt)

$C_E \rightarrow$ Bypass capacitor
 parallel with R_{E1} or R_{E2}

there's no s.c to get i_b \leftarrow GRD \rightarrow v_{cc}

C_E : Bypass capacitor \rightarrow To satisfy the AC and DC requirement.

\rightarrow simplify Design & Analysis

Example consider a CE amplifier with R_C . Use the approximate gain $A_s = -\frac{R_C}{R_E}$. Assume that

$$I_{CQ} = 1 \text{ mA} = I_{EQ}$$

$$V_{CE} = 5 \text{ V}$$

$$V_{CC} = 9 \text{ V}$$

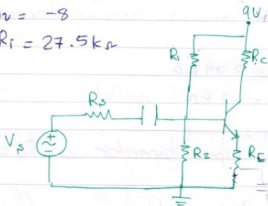
$$\beta = 99$$

$$R_1 \parallel R_2 \approx \infty$$

Find R_C & R_E such that:

① $A_v = -8$

② $R_i = 27.5 \text{ k}\Omega$



DC requirements:

$$I_{CQ} = 1 \text{ mA}$$

$$V_{CEQ} = 5 \text{ V}$$

AC requirements:

$$A_v = -8$$

$$R_i = 27.5 \text{ k}\Omega$$

DC: output loop:

$$-9 + I_{CQ} R_C + V_{CEQ} + I_{EQ} R_E = 0$$

$$R_C + R_E = 4 \text{ k}\Omega \rightarrow \textcircled{1}$$

AC: $A_v = -8 = -\frac{R_C}{R_E} \rightarrow R_C = 8 R_E \rightarrow \textcircled{2}$

16-3/2014

$$R_i = 2.75 \text{ k}\Omega$$

$$R_i = R_1 \parallel R_2 \parallel R_{ib}$$

$$27.5 = r_{\pi} + (1 + \beta) R_E$$

$$\frac{V_{BE}}{I_{BQ}} = 2574$$

$$R_E = 0.25 \text{ k}\Omega$$

From ①: $R_C = 3.75 \text{ k}\Omega$

From ②: $R_C = 2 \text{ k}\Omega$ conflict. ! ok

Solution:- use bypass capacitor on R_E or R_C

• Bypass capacitor on R_E :-

DC : $\sum V + I_{CQ} R_C + V_{CEQ} + I_{EQ} (R_{E1} + R_{E2}) = 0$

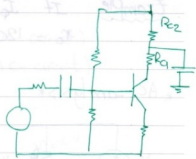
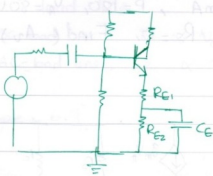
$$R_C + R_{E1} + R_{E2} = 4 \text{ k}\Omega \quad \dots \text{①}$$

AC : $A_v = 8 = \frac{-R_C}{R_{E1}} \rightarrow R_C = 8 R_{E1} \dots \text{②}$

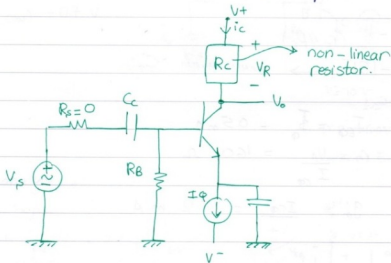
$$R_i = r_{\pi} + (1 + \beta) R_{E1} \rightarrow R_{E1} = 0.25 \text{ k}\Omega$$

from ②: $R_C = 2 \text{ k}\Omega$

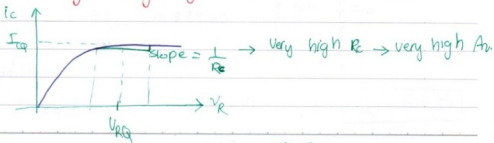
from ①: $R_{E2} = 1.75 \text{ k}\Omega$



• Advanced common Emitter amplifier CE:



Advantage :- very high A_v



Example If $I_Q = 0.5 \text{ mA}$, $\beta = 120$, $V_A = 80 \text{ V}$
 $r_c = 120 \text{ k}\Omega$, $R_S = 0$, Find (A_v):

* AC analysis *



$$A_v = -g_m (r_o \parallel R_C)$$

$$= -1317 \rightarrow \text{very high Gain.}$$

where $I_{EQ} = I_Q = 0.5 \text{ mA}$

$$r_o = \frac{V_A}{I_{CQ}} = 160 \text{ }\Omega$$

$$g_m = \frac{I_{CQ}}{V_T} = 19.2 \text{ mA}$$

• AC-load line:-

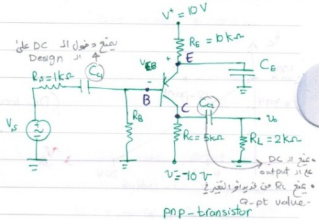
- DC-load line: $I_c \propto V_{ce}$ (DC-circuit)
- AC-load line: $i_c \propto v_{ce}$ (AC-circuit)

* Example :- 6.9

$\beta = 150$

$V_A = \infty$

$V_{BE(ON)} = 0.7 V$



PNP-transistor
common Emitter Amp.

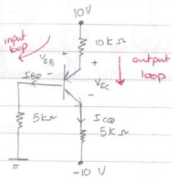
* DC-analysis *

input loop:-

$$-10 + I_{BQ} \times 10 + 0.7 + 5 I_{BQ} = 0$$

$\rightarrow I_{BQ} = 5.96 \mu A$

$I_{CQ} = \beta I_{BQ} = 0.894 mA$



output loop:-

$$-10 + I_{CQ} R_E + V_{CEQ} + I_{CQ} R_C - 10 = 0 \rightarrow V_{CEQ} = 6.53V$$

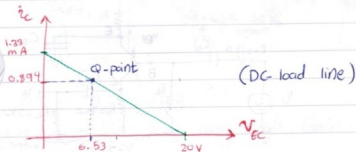
DC-load line:-

$$-V^+ + R_E \left\{ \frac{(1+\beta) I_C}{\beta} \right\} + V_{EC} + I_C R_C + V^- = 0$$

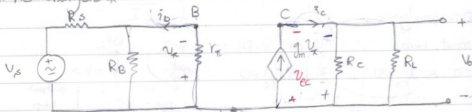
$\left(\frac{(1+\beta) I_C}{\beta} \right) \rightarrow I_{EQ}$

$$I_C = \frac{V^+ - V^-}{R_C + \left(\frac{1+\beta}{\beta}\right) R_E} - \frac{V_{EC}}{R_C + \left(\frac{1+\beta}{\beta}\right) R_E}$$

Note: operation of operation By default is Forward



* AC-analysis *



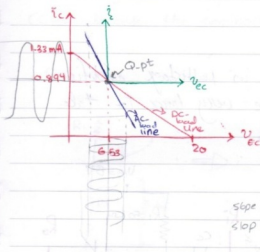
$\frac{1}{s} E$
 s.c $\leftarrow C_E$
 ground $\leftarrow V^+$ and $\leftarrow V^-$
 $\leftarrow R_E$
 E \leftarrow ground
 ground \leftarrow

sign \leftarrow
 E
 \leftarrow
 ground?

• AC-load line:-

$$v_{ce} = -i_c (R_c \parallel R_L)$$

$$i_c = -\frac{1}{R_c \parallel R_L} v_{ce} \rightarrow \text{AC-load line eqn.}$$



Zero in i_c & v_{ce}

DC v_{ce} & i_c line

AC-load line

Gain v_{ce}/i_c

AC-circuit

Bypass-C $\rightarrow \mu$

AC $\parallel i_c$ DC $\parallel R_c \parallel R_L$

slope AC

slope DC

\rightarrow slope $\parallel i_c$ $\parallel R_c \parallel R_L$

• AC-load line helps in visualizing the relationship between the small signal response and the transistor characteristics.

* R_{ib} should be high because $R_i = R_1 // R_2 // R_{ib}$
 R_i High يعني R_1 و R_2 و R_{ib} High
 parallel ان يوصلوا

20-3-2014

* Common Collector Amplifier:- (Emitter follower / buffer).

* Features:-

1. High $R_i \rightarrow$ loading effect is small in the input $\rightarrow V_o = V_i$
2. Low $R_o \rightarrow$ as $\Sigma C \Rightarrow$ small loading effect in the output
3. $A_v \approx +1$
4. $A_i \approx 1 + \beta$
5. its used as a final stage in multistage amplifiers
6. R_1 & R_2 should be very large to take the advantage of high R_{ib} .

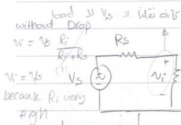
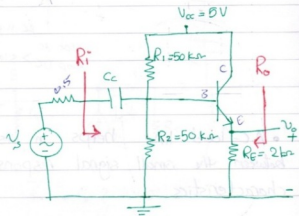
* Ex *

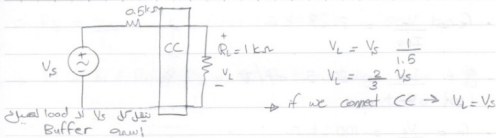
$\beta = 100$

$V_A = 80V$

Find $A_v = \frac{V_o}{V_s}$

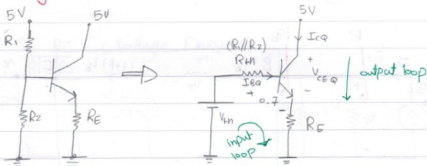
$R_i, R_o, A_i = \frac{I_o}{I_{in}}$





and the voltage in E follows the input voltage (in Mag & phase)
 CC → because the common is collector.

- DC-analysis :-



input loop: $-2.5 + I_{BQ} (25) + 0.7 + R_E (1 + \beta) I_{BQ} = 0$

$I_{BQ} = 7.929 \mu A$

$I_{CQ} = \beta I_{BQ} = 0.793 \text{ mA}$

output loop: $-5 + V_{CEQ} + R_E I_{CQ} = 0$

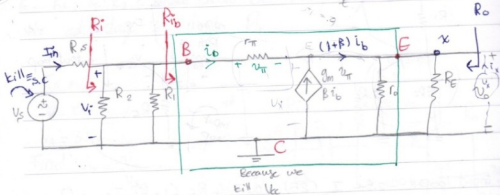
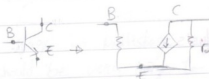
$V_{CEQ} = 3.5 \text{ V}$

$r_{\pi} = \frac{V_T}{I_{BQ}} = 3.28 \text{ k}\Omega$

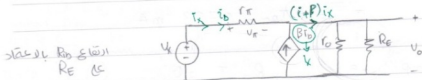
$g_m = \frac{I_{CQ}}{V_T} = 30.5 \text{ mA/V}$

$r_o = \frac{V_A}{I_{CQ}} = 100 \text{ k}\Omega$

AC-analysis:-



$R_i = R_1 // R_2 // R_{iB} \rightarrow$ i_x & v_x \bar{v}_x jawab R_{iB} pinter



kop $\rightarrow -v_x + i_x r_{\pi} + (1+\beta) i_x (r_o // R_E) = 0$

$$\therefore R_{ib} = \frac{v_x}{i_x} = r_{\pi} + (1+\beta)(r_o \parallel R_E) = 201 \text{ k}\Omega$$

$$\rightarrow R_i = R_1 \parallel R_2 \parallel R_{ib} = 22.2 \text{ k}\Omega \quad (\text{High value with respect to } R_s)$$

should be high
↑ high

$$A_v = \frac{V_o}{V_s} \quad V_s \text{ is } V_{in} \text{ in circuit diagram}$$

$$V_o = (1+\beta) i_b (r_o \parallel R_E)$$

$$V_{in} = \frac{V_s R_i}{R_i + R_s} \quad (\text{voltage Division})$$

$$i_b = \frac{V_{in}}{R_{ib}}$$

$$\rightarrow A_v = \frac{V_o}{V_s} \left(\frac{r_{\pi} + R_1 \parallel R_2 \parallel R_s}{1+\beta} \right) \parallel R_E \parallel r_o$$

$$= +0.962 \approx 1$$

$$R_o = \frac{v_x}{i_x}$$

KCL at node X:-

$$I_x + g_m v_{\pi} = \frac{v_x}{R_E} + \frac{v_x}{r_o} + \frac{v_x}{r_{\pi} + R_S \parallel R_1 \parallel R_2} \rightarrow (1)$$

$$v_x = -v_{\pi} \frac{r_{\pi}}{r_{\pi} + R_S \parallel R_1 \parallel R_2} \rightarrow (2)$$

sub (2) in (1):

$$R_o = \frac{v_x}{i_x}$$

$$= \left(\frac{r_{\pi} + (R_1 \parallel R_2 \parallel R_S)}{1 + \beta} \right) \parallel R_E \parallel r_o \rightarrow \text{it can give a difference}$$

$R_o = 36.6 \Omega$ "very low value"

$$A_i = \frac{i_o}{i_{in}}$$

$$i_o = (1 + \beta) i_b \frac{r_o}{r_o + R_E} \rightarrow (1)$$

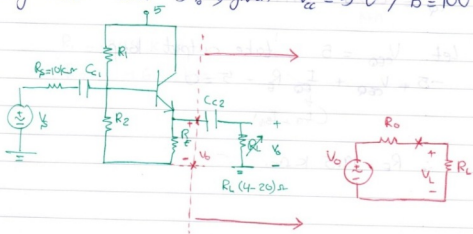
$$i_b = i_{in} \frac{R_1 \parallel R_2}{R_1 \parallel R_2 + R_{ib}} \rightarrow (2)$$

use ① & ②:

$$A_i = \frac{i_o}{i_{in}} = (1+B) \left(\frac{R_1 \parallel R_2}{R_1 \parallel R_2 + R_{ib}} \right) \left(\frac{r_o}{r_o + R_E} \right)$$

Typically/usually $r_o \gg R_E$ $r_o = 100k\Omega$
 $R_E = 2k\Omega$
 $R_1 \parallel R_2 \gg R_{ib}$ in this ex. isn't typical
 $\rightarrow A_i \approx 1+B = \beta$

Example :- Design a common collector amp. (CC) that connects a voltage source (microphone) with $R_s = 10k\Omega$ with a load that has R_L changes from $4k\Omega$ to $20k\Omega$, we want to design CC amplifier such that the output voltage doesn't vary more than 5%, given $V_{cc} = 5V / \beta = 100$



$$0.95 v_o \leq v_L \leq v_o$$

$$0.95 v_o = v_o \frac{R_L}{R_L + R_o} \Rightarrow R_o = 200 \Omega$$

↑
 at $R_L = 4 k\Omega$ (cause it will give the least v_L)

- For CC:

$$R_o = \left(\frac{r_{\pi} + R_1 // R_2 // R_s}{1 + \beta} \right) // R_E // r_o$$

usually $R_1 // R_2 \gg R_s$

$$\frac{r_{\pi} + R_1 // R_2 // R_s}{1 + \beta} \ll R_E // r_o$$

$$\left. \begin{array}{l} R_o \approx \frac{r_{\pi} + R_s}{1 + \beta} \\ r_{\pi} = 10.2 k\Omega \end{array} \right\}$$

$$r_{\pi} \approx \frac{V_T}{I_{BQ}} \rightarrow I_{BQ} = \frac{0.076}{10.2k} \approx 2.55 \mu A$$

$$I_{CQ} = 0.255 \text{ mA}$$

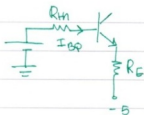
Let $V_{CEQ} = 5$, take output loop:

$$-5 + V_{CEQ} + \underbrace{I_{CQ} R_E}_{(I_{CQ} + I_{BQ})} - 5 = 0$$

$$\therefore R_E = 19.5 k\Omega$$

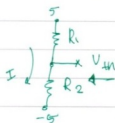
23-3/2014

→ For stability $R_{th} = 0.1(1+\beta)R_E$ "Rule"
 $R_{th}(= R_1 // R_2) = 198 \text{ k}\Omega$



$$-V_{th} + R_{th} I_{BQ} + 0.7 + I_{EQ} R_E - 5 = 0$$

→ we can find V_{th} .



$$V_{th} = \left(\frac{R_2}{R_1 + R_2} \right) (10) - 5$$

* $\frac{R_1}{R_1}$ * $\frac{R_2}{R_1}$ * $\frac{R_2}{R_1 + R_2}$

$$= \underbrace{\frac{R_1}{R_1}}_{R_{th}} \left(\frac{R_2}{R_1 + R_2} \right) (10) - 5$$

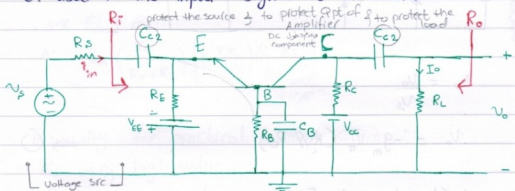
$\therefore R_1 = 344 \text{ k}\Omega$

$R_2 = 467 \text{ k}\Omega$

* Common Base Amplifier (CB) :-

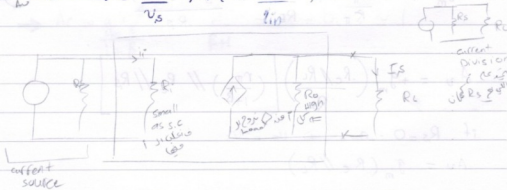
* Features :-

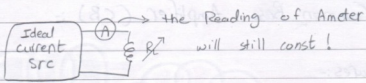
1. $A_v > 1$
2. $A_i \approx 1$
3. small R_i
4. high R_o
5. CB - Amplifier \equiv Ideal current source. (without R_s)
6. used if the input signal is a current.



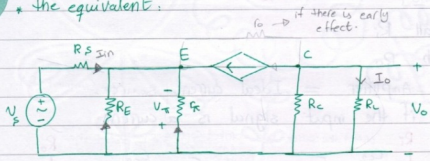
Voltage src
 give the low value

Find : $A_v = \frac{v_o}{v_s}$, $A_i = \frac{i_o}{i_{in}}$, R_o , R_i





• the equivalent:



$$A_v = \frac{V_o}{V_s}$$

$$V_o = -g_m V_{\pi} (R_c // R_L) \rightarrow (1)$$

• KCL at node E \Rightarrow

$$g_m V_{\pi} + \frac{V_{\pi}}{R_{\pi}} + \frac{V_{\pi}}{R_E} + \frac{V_s - (-V_{\pi})}{R_s} = 0 \rightarrow (2)$$

$$A_v = +g_m \left(\frac{R_c // R_L}{R_s} \right) \left[\left(\frac{r_{\pi}}{1+\beta} \right) // R_E // R_s \right]$$

if $R_s = 0 \Omega \Rightarrow V_{\pi} = -V_s$

$$A_v = g_m (R_c // R_L)$$

25-3/2014. Tue.

$$A_i = \frac{I_o}{I_{in}}$$

$$I_o = -g_m V_{\pi} \frac{R_c}{R_c + R_L} \quad (\text{current division}) \rightarrow (1)$$

KCL at Emitter:

$$I_{in} + g_m V_{\pi} + \frac{V_{\pi}}{r_{\pi}} + \frac{V_{\pi}}{r_E} = 0$$

$$V_{\pi} = -I_{in} \left[\left(\frac{r_{\pi}}{1+\beta} \right) \parallel R_E \right] \rightarrow (2)$$

. use (1) & (2):

$$A_i = g_m \left(\frac{R_c}{R_c + R_L} \right) \left[\left(\frac{r_{\pi}}{1+\beta} \right) \parallel R_E \right]$$

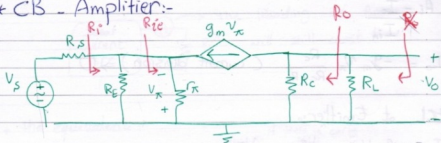
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المعاد
بتظهر

* usually for practical common CB:-

 R_E very high value. R_L very small value.

$$\rightarrow A_i \approx \frac{g_m r_{\pi}}{1+\beta} = \frac{\beta}{\beta+1} = \alpha = 0.99 \approx 1$$

* CB - Amplifier :-



$$R_i = R_E // R_{ie}$$

loop
current Division
Voltage Division



$$R_{ie} = \frac{V_x}{i_x}$$

* find R_o in this

KCL at node E :-

ct. +

$$i_x + \frac{V_x}{r_x} + g_m V_x = 0$$

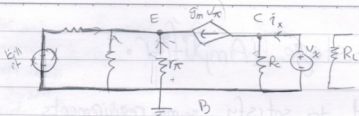
[Δ -equivalent circuit then gains...]

but $V_x = -V_x$

$$\Rightarrow i_x - \frac{V_x}{r_x} - g_m V_x = 0$$

$$R_{ie} = \frac{V_x}{i_x} = \frac{r_x}{1 + \beta g_m} = \frac{r_x}{\beta} \rightarrow \text{small value.}$$

• $R_i = R_E // R_{ie}$ "small value"



KCL at C:-

$$i_x - \frac{v_x}{R_c} - g_m v_x = 0 \rightarrow \textcircled{1}$$

KCL at E:-

$$g_m v_x + \frac{v_x}{R_c} + \frac{v_x}{R_E} + \frac{v_x}{R_S} = 0$$

$$\rightarrow v_x \left(g_m + \frac{1}{R_c} + \frac{1}{R_E} + \frac{1}{R_S} \right) = 0 \quad \therefore v_x = 0$$

$$\therefore \text{from } \textcircled{1}: \frac{R_c}{I_x} = \frac{v_x}{I_x} = R_c.$$

* (لك صفة مادة الامتحان) *

Multi-stage Amplifier.

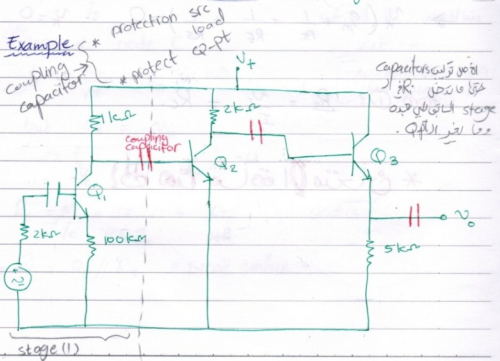
تلبية
requirement
المتطلبات
1-stage.

it is used to satisfy some requirements that can not be satisfied by single stage.

Example * CE without R_E \rightarrow has a high A_v but unstable.

* CE with R_E \rightarrow has low A_v but stable.

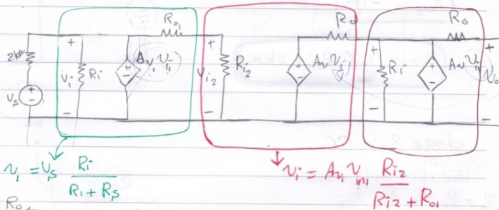
* CC has $A_v = 1$ but high R_i and R_o



For Q_1 : $\beta = 100$, $r_x = 1 \text{ k}\Omega$

For Q_2 & Q_3 : $\beta = 100$, $r_x = 0.5 \text{ k}\Omega$

Find $A_v = \frac{v_o}{v_s}$:



$$v_i = v_s \frac{R_i}{R_i + R_s}$$

$$v_i = A_{v1} v_{i1} \frac{R_{i2}}{R_{i2} + R_{o1}}$$

A_v → *دائرة مكمل و كل stage في جيبه ! اقله اقله اقله اقله اقله*
Av & Ro stage

* Solution :-

stage 1: $A_{v1} = \frac{-\beta R_c}{r_x + (1+\beta)R_E} \left(\frac{R_i}{R_i + R_s} \right)$

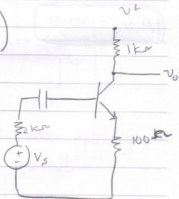
$$R_i = [r_x + (1+\beta)R_E] \parallel R_1 \parallel R_2$$

$$\therefore R_i = r_x + (1+\beta)R_E$$

Sub \rightarrow

$$A_{v1} = -7.63$$

$$R_{o1} = R_c = 1 \text{ k}\Omega$$

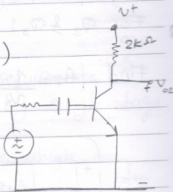


stage 2:- CE without R_E .

$$A_{v2} = -g_m \left(\frac{R_1 // R_2 // r_\pi}{R_1 // R_2 // r_\pi + R_{s1}} \right) (r_o // R_C)$$

$$A_{v2} = -133$$

$$R_{o2} = r_o // R_C = 2k\Omega$$

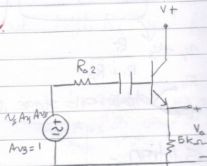


stage 3:- CC

$$V_o = V_s A_{v1} A_{v2} A_{v3}$$

$$A_v = \frac{V_o}{V_s} = A_{v1} A_{v2} A_{v3}$$

\swarrow \swarrow \swarrow
 -7.63 -133 1

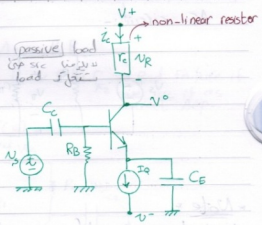


$$A_v = 1010$$

High gain ≈ 1000

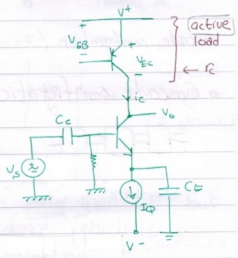
* Active load:

advantage:
high r_c , so
high A_v



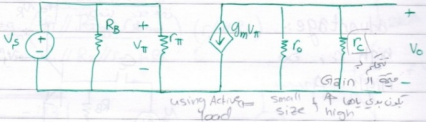
advantages:-

1. small size, so can be used in ICs.
2. r_c is high, so high A_v .
3. we don't need bypass capacitor.



This is an example of using the npn & pnp transistors in the same circuit.

AC-circuit:-

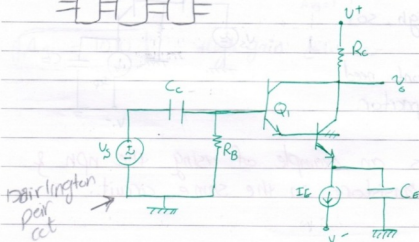


* Note *

Multistage Amplifier could be cascade configuration OR cascode configuration.
 as parallel.
 output of the 1st stage is input to the second stage (as series)

cascade configuration (Ex: Darlington pair circuit)

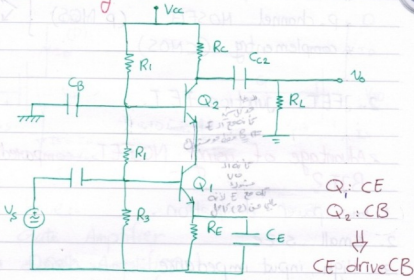
• Cascade configuration:-



Features:-

- 1. High current gain : $A_i \approx \beta_1 \beta_2$
- 2. High input resistance : $R_i \approx 2\beta_1 r_{\pi 2}$ → Bad Feature if we use it as current Amp.

* Cascode configuration:-



* Advantage :-

- CB stage has a bandwidth wider than CE, but CB has low ^(Bad) input impedance which is a limitation in many application. CE → high input Z

But cascode configuration has a wide Bandwidth and high input impedance!

CB input, output, CE input, output

* Field Effect Transistor (FET) Amplifiers *

FET:- *Feld Effect Transistor*

1. MOSFET: metal-oxide-semiconductor FET.

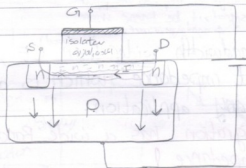
- * n-channel MOSFET (nMOS)
 - * p-channel MOSFET (pMOS)
 - * complementary (CMOS)
- } $\begin{cases} \text{Enhancement} \\ \text{Depletion} \end{cases}$

2. JFET: junction FET.

جوزنشن فیلڈ ٹرانزیستور

Advantage of using MOSFET compared with BJT?

1. low power dissipation.
2. small size.
3. High input impedance. \rightarrow because there is isolator

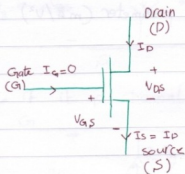


- holes will move with the direction of Field \rightarrow majority of n-channel
- $I_G = 0$, $I_S = I_D$

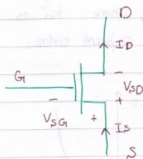
$(V_{DS} > V_{GS})$ good \leftarrow loading effect

But: $g_{m(\text{BJT})} \gg g_{m(\text{FET})}$ Gain. μ_{eff} is low
 so that $A_{v(\text{BJT})} \gg A_{v(\text{FET})}$ by using μ_{eff} is low
 Multistage.

n-channel MOSFET



p-channel MOSFET



• we will have:-

- 1- common Gate Amplifier
- 2- Common Drain Amplifier
- 3- Common Source Amplifier

* The Transistor should be in **Saturation Mode** to work as Amplifier.

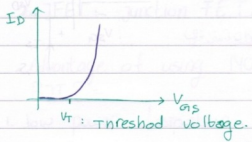
• DC-analysis :-

- 1. Draw DC-equivalent cct, $-1-: o.c$
 Finding it from input loop AC-src: S/c
 then use eqn

2. use $I_{DQ} = K_n (V_{GSQ} - V_{TN})^2$

• where K_n is the conduction parameter (mA/V^2)

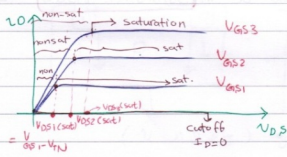
• Q-point value: I_D, V_{GS}, V_{DS}
 controller



→ if $V_{DSQ} > V_{DS(sat)}$, then saturation Mode.

↳ Finding it from output loop.

$$V_{DS(sat)} = V_{GSQ} - V_{TN}$$

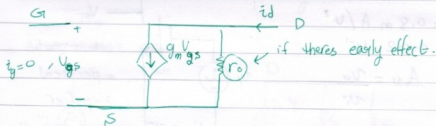


sat ↓ ⇔ ↑ V_{GS}
 saturation: output
 V_{GS} is the gate voltage
 BJT is like an
 active V_{GS} control of
 the sat

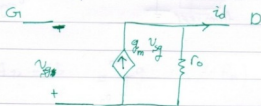
* AC-analysis *

+ Draw AC-equivalent cct:

• if it n-channel:-



• if it p-channel:-



$$\rightarrow g_m = 2kn \left(v_{GSQ} - V_{TN} \right) \rightarrow \text{for n-channel}$$

but $g_m = 2kp (v_{SGSQ} + V_{TP})$ for p-channel

$$\rightarrow r_o = \frac{1}{\lambda I_{DQ}} \quad \bullet \quad \text{where } \lambda \text{ is the channel length modulation parameter.}$$

(+ve value)

$$\rightarrow i_d = g_m v_{gs} = 2kn (v_{GSQ} - V_{TN}) v_{gs}, \quad \text{if } r_o = \infty$$

G-4/20/14 Sunday

* Example :-

Given :

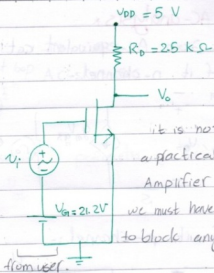
$$V_{TN} = 1V$$

$$k_n = 0.8 \text{ mA/V}^2$$

$$\lambda = 0.02 \text{ V}^{-1}$$

$$\text{find } A_v = \frac{v_o}{v_i}$$

• it is common source.



DC-analysis:-

$$V_{GSQ} = V_{GS} = 2.12V$$

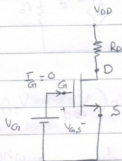
$$I_{DQ} = k_n \left(\frac{V_{GSQ} - V_{TN}}{1} \right)^2$$

$$I_{DQ} = 1 \text{ mA}$$

$$V_{DSQ} = \frac{V_{DD}}{5} - I_D R_D = 2.5V$$

$$V_{DSQ} \stackrel{?}{>} (V_{DS(sat)}) = \frac{V_{GS}}{1} - V_{TN} \quad \checkmark \quad (\text{saturation})$$

so we can use the transistor as amplifier

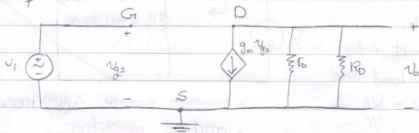


AC-analysis:-

$g_m = 2k_n(v_{gs} - V_{th}) = 1.79 \text{ mA/V}$

$r_o = \frac{1}{\lambda I_{DQ}} = 50 \text{ k}\Omega$ (early effect)

→ Ac-equivalent ckt:-



$A_v = \frac{v_o}{v_i} = -g_m (r_o // R_D)$

$A_v = -4.26$ (BJT is direct ← small value)

• use the same circuit in the previous example, but with p-channel MOSFET ^{gain}

$\begin{cases} V_{DD} = -5 \text{ V} \\ \text{and } + (2.12) \text{ OR } \frac{1}{-} (-2.12) \end{cases}$

$A_v = -g_m (r_o // R_D)$ & it is the same value.

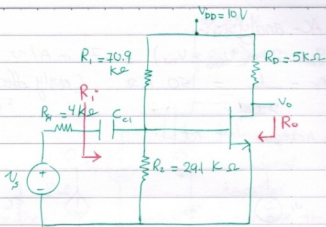
6-4-2014

Example:-

$$V_{TN} = 1.5V$$

$$k_n = 0.5 \text{ mA/V}^2$$

$$\lambda = 0.01 \text{ V}^{-1}$$



Find :-

1. Q-point value

2. DC-load line

$$3. A_v = \frac{V_o}{V_i}$$

- common source Amplifier.
- practical amplifier.

4. R_i

5. R_o (load resistor) $i_{DQ} = I_{DQ}$ V_{DSQ}

DC-analysis:-

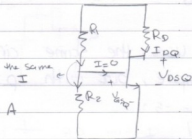
voltage DIVISION

$$V_{GSQ} = 10 \times \frac{R_2}{R_2 + R_1} = 2.91 \text{ V}$$

$$I_{DQ} = k_n (V_{GSQ} - V_{TN})^2 = 1 \text{ mA}$$

$$V_{DSQ} = 10 - I_{DQ} R_D = 5 \text{ V}$$

$$V_{DSQ} > (V_{DS(sat)}) = V_{GSQ} - V_{TN} \quad \checkmark \quad (\text{saturation})$$



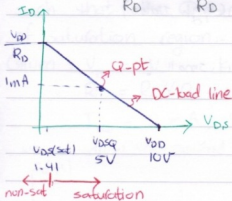
6-4-2019

DC-load line:- $I_D \propto V_{DS}$

$$-V_{DD} + I_D R_D + V_{DS} = 0$$

$$I_D = \frac{V_{DD}}{R_D} - \frac{V_{DS}}{R_D}$$

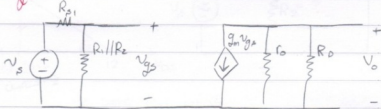
$$\text{slope: } -\frac{1}{R_D}$$

Best value for V_{DSQ} :

$$\frac{10 + 1.41}{2}$$

$$= 5.705 V$$

* AC-analysis:-



$$A_v = \frac{v_o}{v_i}$$

$$v_o = -g_m v_{gs} (r_o \parallel R_L)$$

$$v_{gs} = v_s \frac{R_1 \parallel R_2}{R_1 \parallel R_2 + R_{S1}}$$

$$A_v = -g_m (r_o \parallel R_o) \left(\frac{R_1 \parallel R_2}{R_1 \parallel R_2 + R_s} \right) = -0.562$$

$$R_i = R_1 \parallel R_2 = 20.6 \text{ k}\Omega \quad (\text{High value})$$

$$R_o = r_o \parallel R_o = 4.76 \text{ k}\Omega \quad \text{small!}$$

Design Example:-

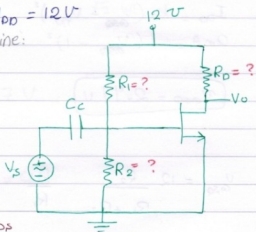
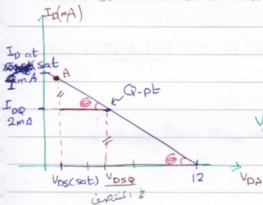
Design the bias of MOSFET (common source) such that the Q-point is in the middle of saturation region:-

Given : $V_{TN} = 1V$, $k_n = 1 \text{ mA/V}^2$, $\lambda = 0.015 \text{ V}^{-1}$

$R_i = R_1 // R_2 = 100 \text{ k}\Omega$

$I_{DQ} = 2 \text{ mA}$, $V_{DD} = 12V$

we will draw the DC-load line:



the same tan of C.

at point A : $I_D = 4 \text{ mA}$

$$I_{D_A} = k_n (V_{GS_A} - V_{TN})^2$$

$$\rightarrow V_{GS_A} = 3V$$

$$\Rightarrow V_{DS(sat)} = V_{GS_A} - V_{TN} = 2V$$

[the same of at pt A]

$$V_{DSQ} = \frac{12 + 2}{2} = 7 \text{ V} \quad \text{Best value.}$$

$$-12 + I_{DQ} R_D + V_{DSQ} = 0$$

$$R_D = 2.5 \text{ k}\Omega$$

$$I_{DQ} = k_n (V_{GSQ} - V_{TN})^2$$

$$2 \text{ mA} = 1 (V_{GSQ} - 1)^2$$

$$V_{GSQ} = 2.41 \text{ V}$$

$$V_{GSQ} = 12 \frac{R_2}{R_1 + R_2} \frac{R_1}{R_1}$$

$$V_{GSQ} = 12 \frac{R_1 R_2}{R_1 + R_2} \cdot \frac{1}{R_1}$$

$$2.41 = 12 \frac{(R_1 // R_2)}{100} \frac{1}{R_1}$$

$$R_1 = 498 \text{ k}\Omega$$

$$R_2 = 125 \text{ k}\Omega$$

• another solution:-

$$V_{GSP} = 12 \frac{R_i}{R_1} = \frac{1200}{R_1}$$

$$I_{DQ} = k_n (V_{GSP} - V_{TN})^2$$

$$2 = 1 \left(\frac{1200}{R_1} - 1 \right)^2$$

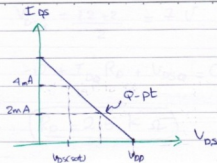
$$\sqrt{2} + 1 = \frac{1200}{R_1} \rightarrow R_1 = \frac{1200}{\sqrt{2} + 1}$$

$$V_{D(sat)} = 1.41 \text{ V}$$

$$V_{DQ} = \frac{12 + 1.41}{2} = 6.7 \text{ V}$$

$$-12 + I_{DQ} R_p + V_{DQ} = 0$$

$$R_p = 2.65 \text{ k}\Omega$$



$$I_{D(sat)} = kn(V_{GS(sat)} - V_{TN})^2$$

$$V_{GS(sat)} = 3V$$

$$V_{DS(sat)} = V_{GS(sat)} - V_{TN} = 2V$$

$$V_{DSQ} = \frac{V_{DD} + V_{DS(sat)}}{2} = 7$$

from the output loop:

$$-\frac{V_{DD}}{12} + \frac{I_{DQ}}{2mA} R_D + \frac{V_{DSQ}}{7} = 0$$

$$\rightarrow R_D = 2.5 k\Omega$$

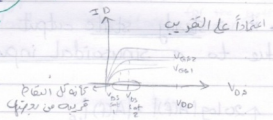
$$I_{DQ} = kn(V_{GSQ} - V_{TN})^2$$

$$V_{GSQ} = 2.41V$$

$$V_{QDQ} = V_{DD} * \frac{R_2 R_1}{R_1 + R_2} \cdot \frac{1}{R_1}$$

$$\rightarrow R_1 = 498 \text{ k}\Omega$$

$$R_2 = 125 \text{ k}\Omega$$



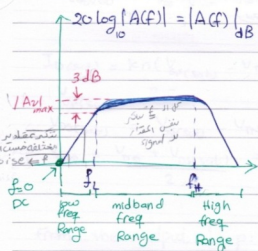
10-4/2014 Thu.

New Chapter

Frequency Response

Gain as a fn of f

- it is steady state output of a linear sys. due to a sinusoidal input.



$f = 0$: DC

$f > 0$: AC

f_L : low corner - frequency

low 3dB frequency

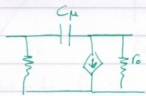
break - point frequency

- Bandwidth (BW) = $f_H - f_L$ Gain indep. on freq if it wide \Rightarrow Good Amplifier.

AMP → user's load
3 Amplifier load

Types of capacitors:-

- 1. Coupling and bypass capacitors $\parallel R_C / \parallel R_E$ → the same behavior for the both. (Group 1)
- 2. Transistor and load capacitors (Group 2)



Transistor capacitor



Load capacitor

capacitor $\left\{ \begin{array}{l} \text{--- a ---} \\ \text{--- s.c ---} \\ \text{--- s.c ---} \end{array} \right.$
have impedance.

• In DC ($f=0$) → all capacitors are open ckt.

$$Z_c = \frac{1}{j2\pi f C} = \infty \Omega$$

AMP → user's load

• In low frequency range:

Group (1): $Z_c = \frac{1}{j2\pi f C}$
as balanced $\Rightarrow \downarrow f \Rightarrow j2\pi f C \uparrow, \infty$

Group (2): ∞ open ckt

$$Z_c = \frac{1}{j2\pi f C} \Rightarrow Z_c: \text{high value} \Rightarrow \infty \text{ o.c}$$

• In midband Range:

Group (1): s.c

New Chapter

Group (2): open. cct

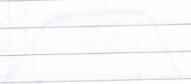
Group (1): High value

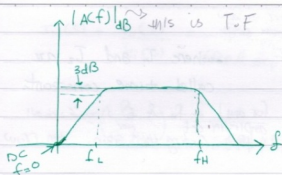
• High frequency range:

Group (1): short cct

Group (2): Low value
 $j\omega Z_c = \omega C$

$$\text{Group (2): } Z_c = \frac{1}{j\omega C}$$





$$BW = f_H - f_L$$

Note: the values of capacitors in graph 1 \gg values of capacitors in graph 2.

• Transfer Function: $A(f)$

→ S-Domain:

$$S = j\omega = j 2\pi f \quad (\text{complex frequency})$$

$$Z_c = \frac{1}{j\omega C} = \frac{1}{sC}$$

$\frac{s}{+}$
From
Laplace.

In general, $\underbrace{T(s)}_{\text{Transfer function}} = \frac{k(s-z_1)(s-z_2)\dots(s-z_n)}{(s-p_1)(s-p_2)\dots(s-p_m)}$

z_1, z_2, \dots, z_n : Zeros of Transfer function

p_1, p_2, \dots, p_m : poles of Transfer function.

k : constant.

→ To draw $A(f)$ of amplifier, we will consider only two forms of TCS.

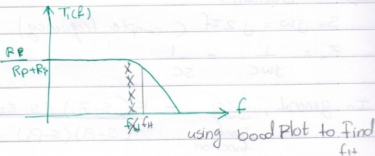
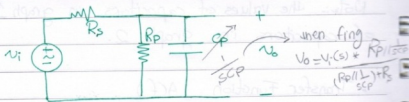
① $T_1(s) = k_1 \frac{1}{1 + sT_1}$ corner frequency

• where T_1 and T_2 are called time constant.

② $T_2(s) = k_2 \frac{sT_2}{1 + sT_2}$ right corner

for any amplifier ckt then finding the \uparrow Gain. then Draw

• $T_1(s)$: This is transfer function of the following ckt:



$$T_1(s) = \frac{V_o(s)}{V_i(s)}$$

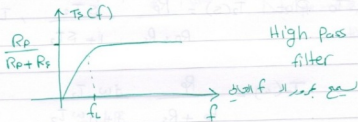
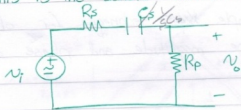
$$V_o(s) = V_i(s) \times \frac{R_p // \frac{1}{sC_p}}{(R_p // \frac{1}{sC_p}) + R_s}$$

$$T_1(s) = \frac{V_o(s)}{V_i(s)} = \frac{R_p // \frac{1}{sC_p}}{(R_p // \frac{1}{sC_p}) + R_s}$$

$$= \left(\frac{R_p}{R_p + R_s} \right) \frac{1}{1 + s(R_p // R_s) C_p}$$

$$\rightarrow K_1 = \frac{R_p}{R_p + R_s} \quad \& \quad T_1 = (R_p // R_s) C_p$$

• $T_2(s)$: This is the transfer function of this ckt.



$$T_2(s) = \frac{V_o(s)}{V_i(s)}$$

$$V_o(s) = V_i(s) * \frac{R_p}{R_p + R_s + \frac{1}{sC_s}}$$

$$T_2(s) = \frac{S C_s R_p}{1 + (R_p + R_s) C_s s}$$

$$T_2(s) = \left(\frac{R_p}{R_p + R_s} \right) \cdot \frac{s (R_s + R_p) C_s}{1 + (R_s + R_p) C_s s}$$

where $k = \frac{R_p}{R_p + R_s}$ & $T = (R_s + R_p) C_s$

* Bode Plot:

it is a simple ~~technique~~ technique for obtaining approximate plots of the magnitude and ~~phase~~ phase of transfer function.

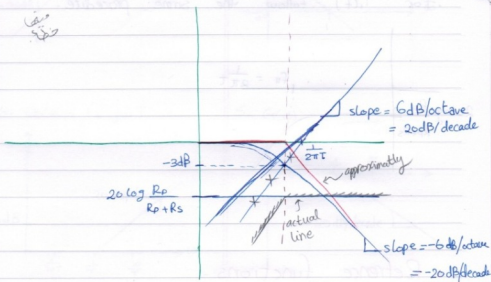
To Plot $T_2(s) = \frac{R_p}{R_p + R_s} \frac{s T_2}{1 + s T_2}$, $T_2 = (R_s + R_p) C_s$

$$\rightarrow T_2(\omega) = \frac{R_p}{R_p + R_s} \frac{j\omega T_2}{1 + j\omega T_2}$$

$$|T_2(\omega)| = \frac{R_p}{R_p + R_s} \frac{\omega T_2}{\sqrt{1 + (\omega T_2)^2}}$$

$$|T_2(f)| = \frac{R_p}{R_p + R_s} \cdot \frac{2\pi f T_2}{\sqrt{1 + (2\pi f T_2)^2}}$$

$$|T_2(f)|_{dB} = 20 \log \frac{R_p}{R_p + R_s} + 20 \log 2\pi f T_2 - 20 \log \sqrt{1 + (2\pi f T_2)^2}$$



• Octave:-

$$\begin{aligned} 20 \log 2 &= 6 \text{ dB} \\ 20 \log 4 \left(\times 2 \right) &= 12 \text{ dB} \left(+ 6 \text{ dB} \right) \\ 20 \log 8 \left(\times 2 \right) &= 18 \text{ dB} \left(+ 6 \text{ dB} \right) \\ 20 \log 16 \left(\times 2 \right) &= 24 \text{ dB} \left(+ 6 \text{ dB} \right) \end{aligned}$$

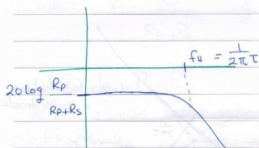
• decade:

$$20 \log 10 = 20 \text{ dB}$$

$$20 \log 100 \stackrel{\times 10}{=} 40 \text{ dB} \quad \leftarrow +20$$

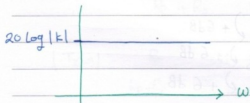
$$20 \log 1000 \stackrel{\times 10}{=} 60 \text{ dB} \quad \leftarrow +20$$

• For $T_c(f)$ follow the same procedure.

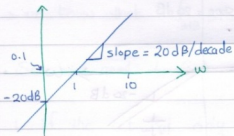


• Reference functions:-

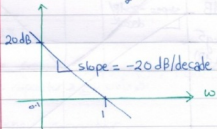
1. $T(\omega) = k$



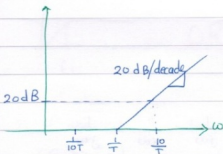
$$2. T(\omega) = j\omega$$



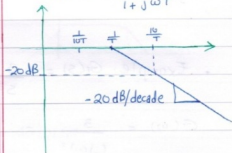
$$3. T(\omega) = \frac{1}{j\omega}$$



$$4. G(\omega) = 1 + j\omega T$$



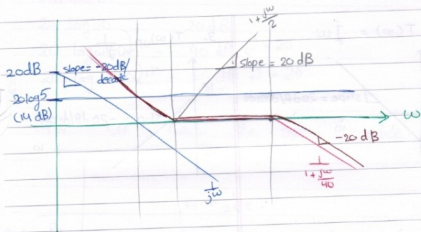
$$5. G(\omega) = \frac{1}{1 + j\omega T}$$



• Example:- Plot the following: $G(s) = \frac{100(s+2)}{s(s+40)}$

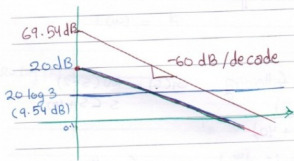
$$G(j\omega) = \frac{100(j\omega + 2)}{j\omega(j\omega + 40)}$$

$$G(j\omega) = \frac{100 \times 2 \left(1 + \frac{j\omega}{2}\right)}{j\omega \times 40 \left(1 + \frac{j\omega}{40}\right)} = \frac{5 \left(1 + \frac{j\omega}{2}\right)}{\left(1 + \frac{j\omega}{40}\right)}$$



• Example: $G(s) = \frac{3}{s^3}$

$$G(\omega) = \frac{3}{(j\omega)^3} = 3 \cdot \frac{1}{j\omega} \cdot \frac{1}{j\omega} \cdot \frac{1}{j\omega}$$



• Short circuit and Open circuit time const.

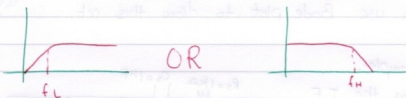
→ we know that $f_{3dB} = \frac{1}{2\pi T}$

• So, we need to find T (Time constant), How?
 - capacitor → شحنه و تفريغ

1. if the cct has only one capacitor:

$T = R_{eq} C$

↳ seen by C.



2. if the cct has two capacitors:-

$(C_1 \gg C_2)$



$T_L = R_{eq} C_1$, $Z_C = \frac{1}{j2\pi f C_2} \approx \infty$

where C_2 will be open cct

$$\Rightarrow f_L = \frac{1}{2\pi T_L}$$

$$T_H = R_{eq} C_2 \quad , \quad Z_C = \frac{1}{j2\pi f C} \rightarrow \infty \approx 0$$

3. if the cct has more than two capacitor.
or $(C_1 = C_2)$

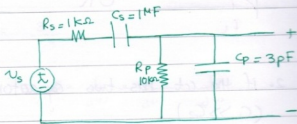
→ we need to find the transfer function $\frac{V_o(s)}{V_s(s)}$
then use Bode plot to draw this cct.

- Example:-

Draw the T.F

$\frac{V_o(f)}{V_s(f)}$ and Find

the Band width
of the Given cct:



17-4/2014

$$\cdot f_L = \frac{1}{2\pi T_L}, \quad T_L = R_{eq} C_s \quad (C_p = 0.0)$$

$$T_L = (R_s + R_p) C_s = 1.1 \times 10^{-2} \text{ sec}$$

$$f_L = 14.5 \text{ Hz}$$

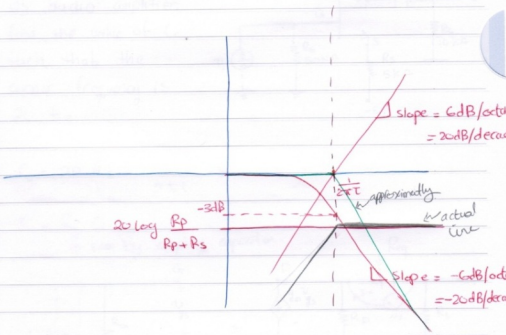
$$\cdot f_H = \frac{1}{2\pi T_H}, \quad T_H = R_{eq} C_p \quad (C_s: \text{S.C.})$$

$$T_H = (R_s \parallel R_p) C_p = 2.73 \times 10^{-9} \text{ sec}$$

$$f_H = 58.3 \text{ MHz}$$

$$\cdot \text{BW} = f_H - f_L = 58.3 \text{ MHz}$$

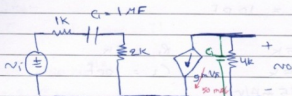
القوة والقدرة



Lecture

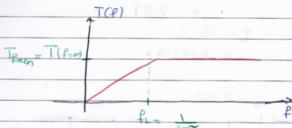
20-4-2014

Ex:



Sketch the bode plot of the transfer function magnitude

Diagram of transfer function.



$$\Rightarrow T_{\text{max}}(f) = T(f=0) = \frac{V_o}{V_i}$$

\downarrow
 C_1 is short circuit

$$V_o = -g_m V_x \times 4$$

$$V_x = V_i \frac{2}{2+1}$$

$$\Rightarrow \frac{V_o}{V_i} = -g_m \times R_L \times \frac{2}{2+1} = -133$$

$$|T(f)| = 133$$

$$\Rightarrow f_L = \frac{1}{2\pi\tau}$$

$$\tau = R_{\text{eq}} \cdot C$$

$$= 53.1 \text{ Hz}$$

$$= (1+2) \times 1\mu$$

$$= 3 \text{ m sec}$$

Ex: Same example, without C_1 , assume C_L parallel with $R_L = 10 \mu\text{F}$

$$R_s = 0.5 \text{ k}$$

$$R_L = 5 \text{ k}$$

$$V_s = 1.5 \text{ V}$$

$$C_L = 10 \mu\text{F}$$

$$g_m = 75 \text{ mA/V}$$

$$|T_{\text{max}}(f)| = |T(f_{\text{co}})| = g_m \times R_L \times \frac{1.5}{1.5 + 0.5}$$

$$= \boxed{281}$$

$$f_H = \frac{1}{2\pi\tau}$$

$$\tau = R_L C_L$$

$$= 3.18 \text{ MHz}$$

Ex 3



Sketch the Bode plot of the transfer function magnitude

$$\Rightarrow C_s \gg C_L$$

$$\text{at low freq} \Rightarrow Z_C = \frac{1}{2\pi f C_L} \quad C_L \text{ \& open circuit}$$

$$C_s \text{ \& has an effect}$$

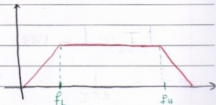
$$f_L = \frac{1}{2\pi\tau_L}$$

$$\tau_L = R_{\text{eq}} C_s \quad (C_L \text{ open ckt})$$

$$= 2.25 \times 10^3 \times 2 \times 10^{-6}$$

$$= 4.5 \text{ } \mu\text{sec}$$

$$\therefore f_L = 35.4 \text{ Hz}$$



$$f_H = \frac{1}{2\pi\tau_H}$$

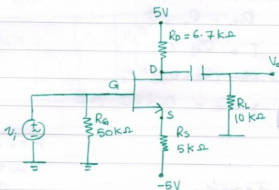
$$\tau_H = R_{eq} C_L \quad (C_s : \text{short circuit})$$

$$\begin{aligned}\tau_H &= 4 \times 10^3 \times 50 \times 10^{-12} \\ &= 0.2 \mu\text{sec}\end{aligned}$$

$$f_H = 0.796 \text{ MHz}$$

Example:-

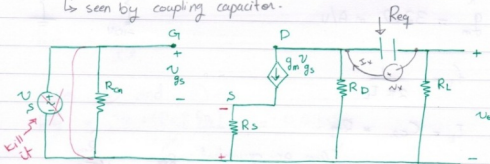
This circuit is used as audio amplifier, find the value of C_c such that the corner frequency is 20 Hz.



$$f_c = 20 \text{ Hz} = \frac{1}{2\pi T} \rightarrow T = 7.96 \text{ msec}$$

$$T = R_{eq} C_c$$

↳ seen by coupling capacitor.



$$v_{gs} = -R_S * g_m v_{gs}$$

$$v_{gs} (1 + R_S g_m) = 0$$

$$\boxed{v_{gs} = 0}$$

$$R_{eq} = R_L + R_D$$

$$T = R_{eq} C_c$$

$$7.69m = (R_D + R_L) C_c$$

2.5 Capacitor at corner

$$\rightarrow C_c = 0.477 \mu F$$

$$\frac{1}{\sqrt{2} \pi f c t} = 0$$

Example:-

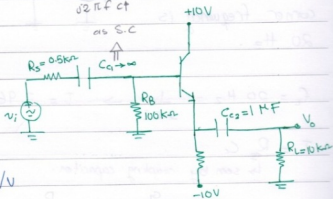
$$B = 100$$

$$V_A = 120 V$$

$$C_{c2} = 1 \mu F$$

$$r_{\pi} = 3.10 k\Omega$$

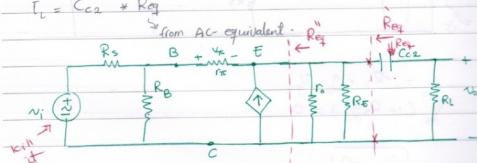
$$g_m = 32.2 \text{ mA/V}$$



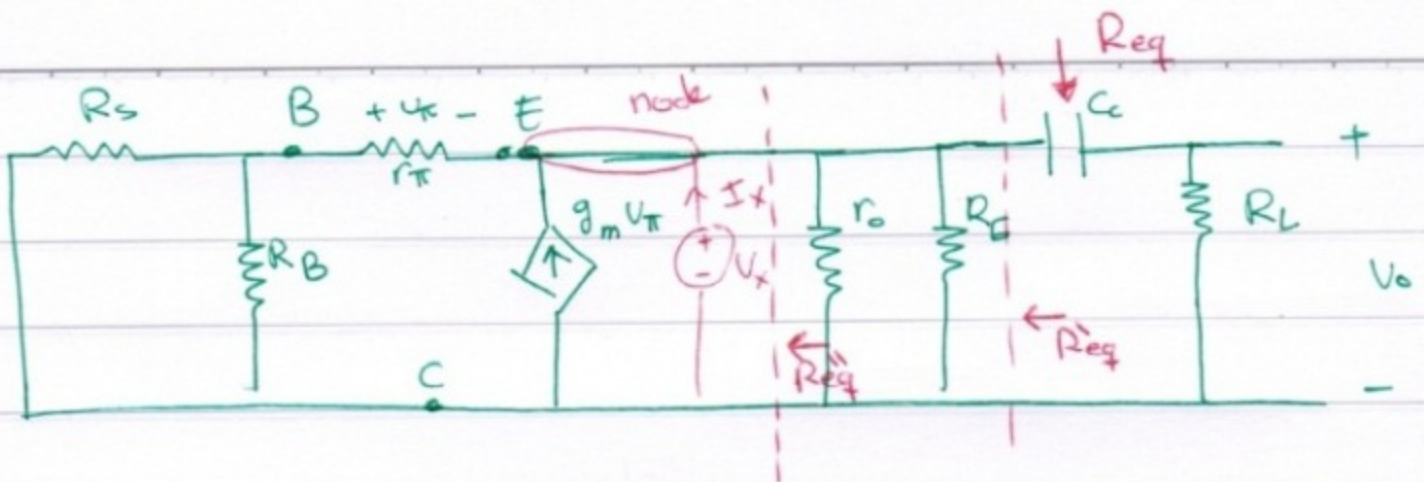
$$f_L = \frac{1}{2\pi T_L}$$

$$T_L = C_{c2} * R_{eq}$$

from AC equivalent



22-4/2014



$$R_{eq} = R_L + R_{eq}$$

KCL at node E:

$$I_x + g_m v_{\pi} = -\frac{v_{\pi}}{r_{\pi}} \rightarrow (1)$$

$$v_{\pi} = -v_x \frac{r_{\pi}}{r_{\pi} + (R_B \parallel R_s)} \rightarrow (2)$$

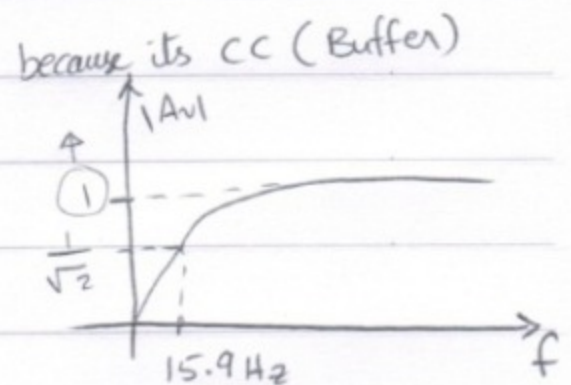
$$R_{eq}'' = \frac{v_x}{I_x}$$

from (2) and (1) \rightarrow

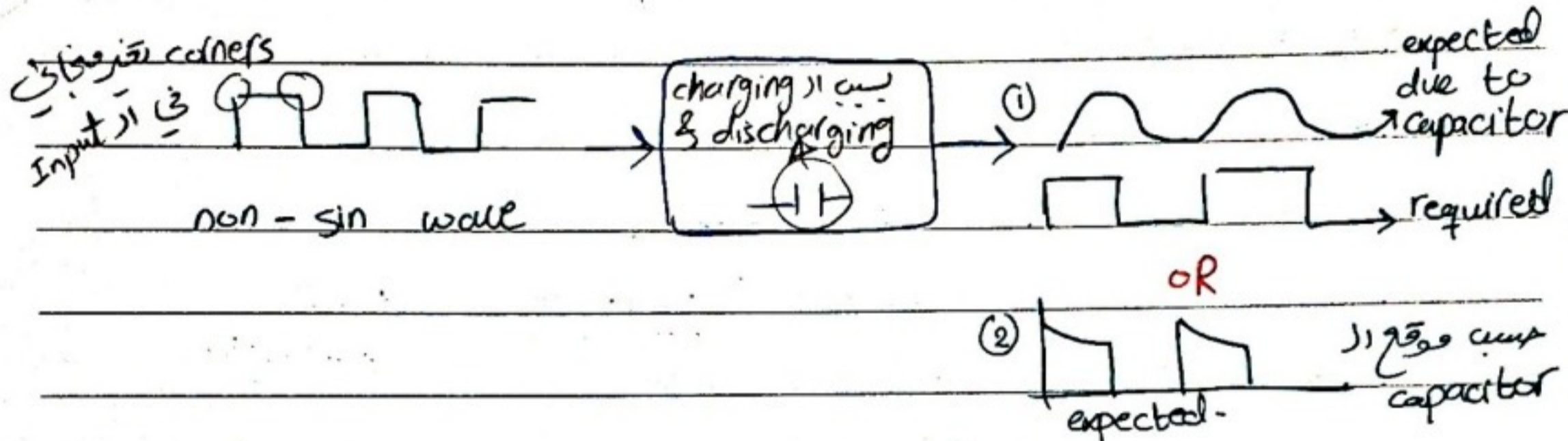
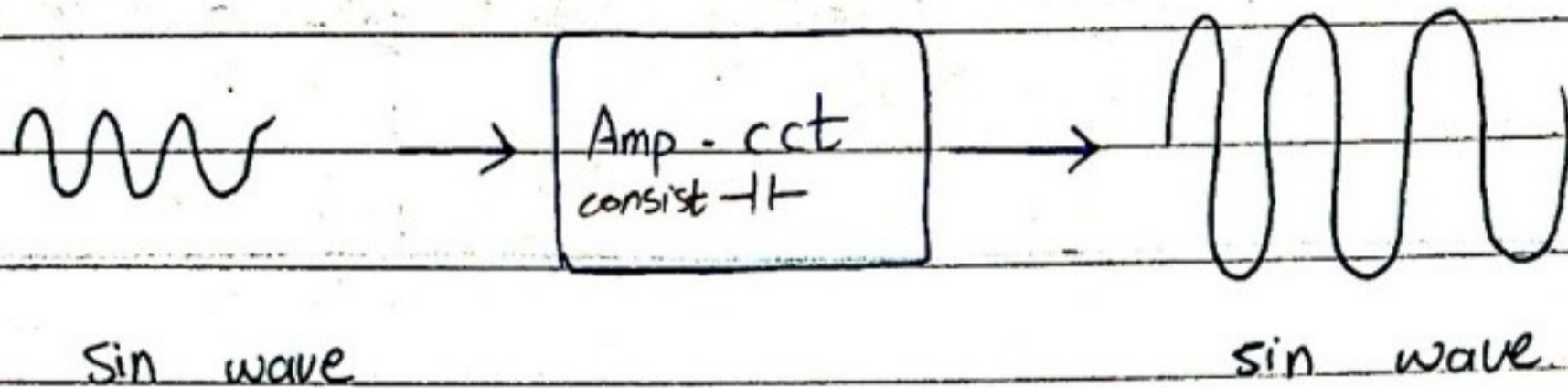
$$R_{eq}'' = \frac{v_x + (R_s \parallel R_B) v_x}{1 + \beta} = 0.0356$$

$$\rightarrow R_{eq} = 35.5 \Omega$$

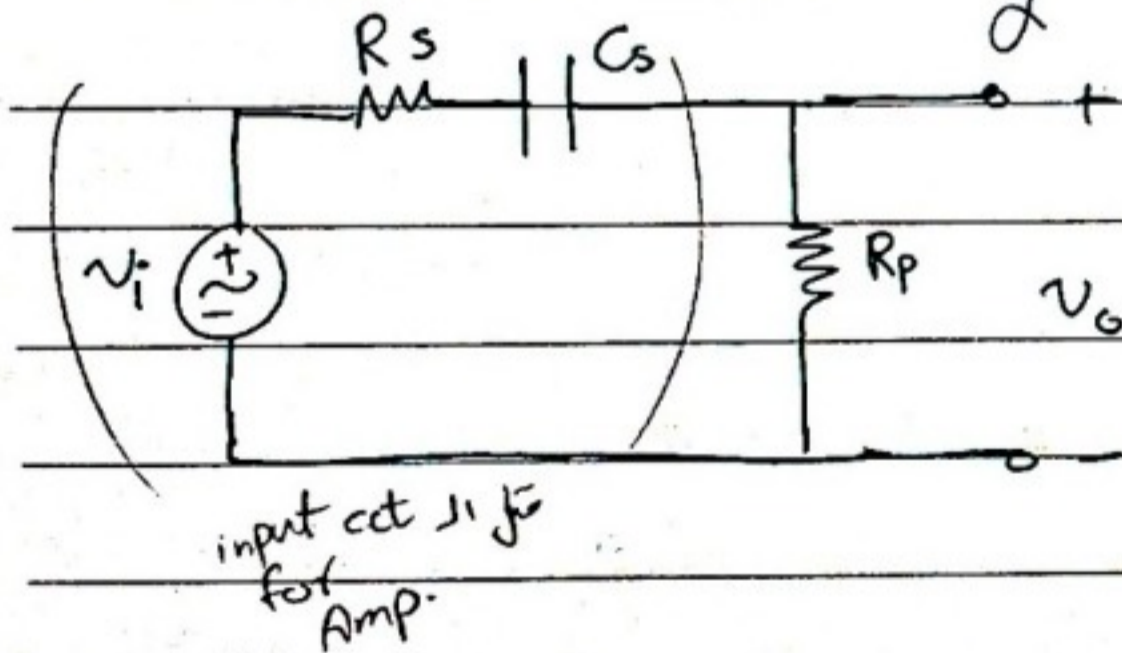
$$f_L = \frac{1}{2\pi \tau_L} = 15.9 \text{ Hz}$$



Time Response:-



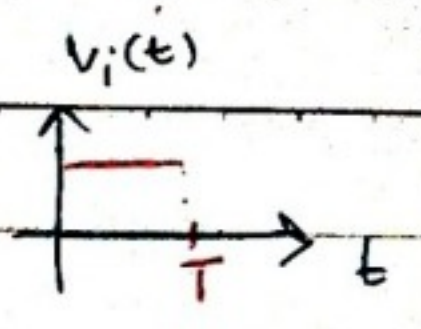
Consider the following ckt:-



$$\frac{V_o(s)}{V_i(s)} = \frac{R_p}{R_p + R_s} = \frac{S(R_s + R_p)C_s}{1 + S(R_s + R_p)C_s}$$

$$T(s) = \frac{V_o(s)}{V_i(s)} = k_2 \frac{S T_2}{1 + S T_2}$$

if $V_i(t) = u(t)$: unit step function.



what is $V_o(t)$?!

$$V_o(s) = V_i(s) T(s)$$

$$V_o(s) = \left(\frac{1}{s}\right) \cdot k_2 \frac{T}{1 + sT_2}$$

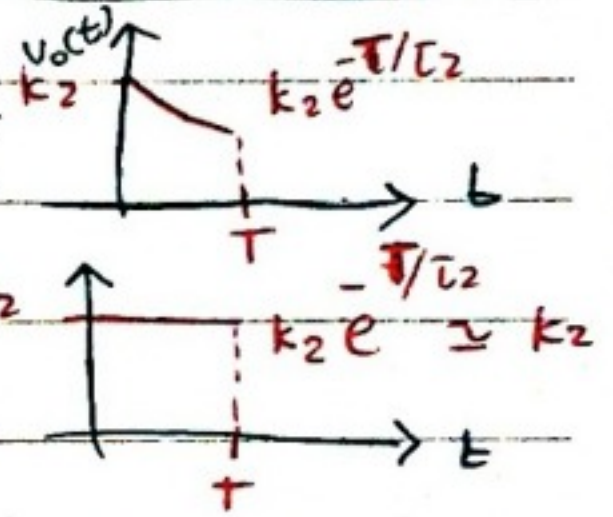
by Laplace Transform $1 + sT_2$

$$V_o(s) = \frac{k_2 T}{1 + sT_2}$$

inverse Laplace Transform

$V_o(t) = k_2 e^{-t/T_2}$

كل تازان T_2 عملية التفريغ أكبر T
 تاخذ زوفاً طويلاً
 أو أقل



But the required $V_o(t)$: and

to get it \Rightarrow
 $k_2 \approx k_2 e^{-T/T_2}$

$$e^{-T/T_2} \approx 1$$

$\frac{T}{T_2}$ very small value.

min value to get

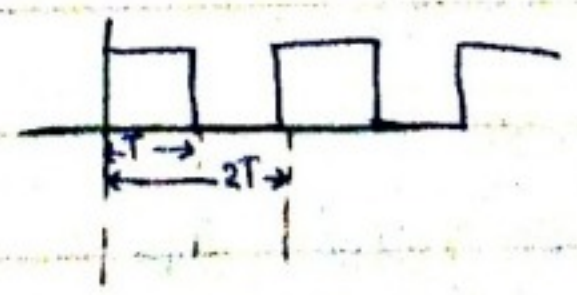
$$T_2 = 10T$$

$$\Rightarrow T_2 \gg T$$

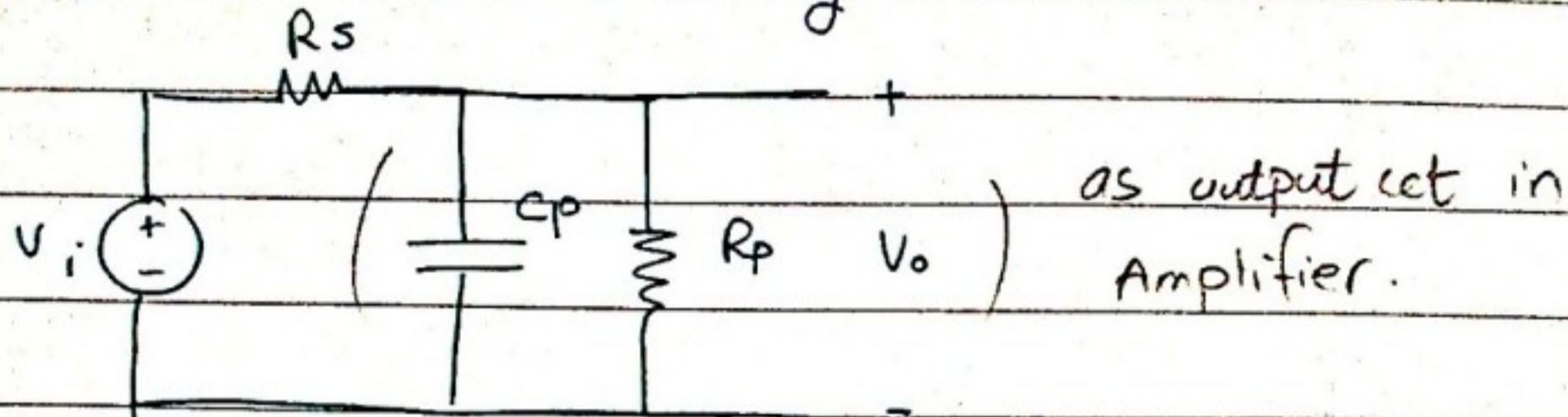
$C_s(R_s + R_p) \gg T$
 \rightarrow should be very large.

$T_2 \gg 10(T)$

 $\rightarrow f_{vi} = \frac{1}{2T}$



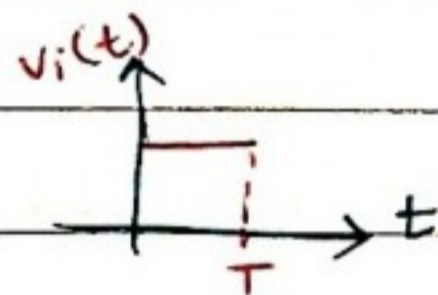
• consider the following cct: -



$$\frac{V_o(s)}{V_i(s)} = \frac{R_p}{R_p + R_s} \cdot \frac{1}{1 + s(R_s \parallel R_p)C_p}$$

$$= K_1 \frac{1}{1 + sT_1}$$

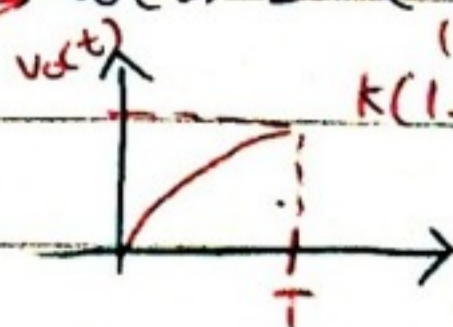
→ if the input $V_i(t) = u(t)$
what is the output?



$$V_o(s) = V_i(s) \cdot T(s)$$

$$= \frac{1}{s} \cdot \frac{K_1}{1 + sT_1}$$

$$V_o(s) = \frac{K_1}{s} \cdot \frac{1}{1 + sT_1} \xrightarrow[\text{Transform}]{\text{inverse Laplace}} V_o(t) = K_1 \left(1 - e^{-t/T_1} \right)$$

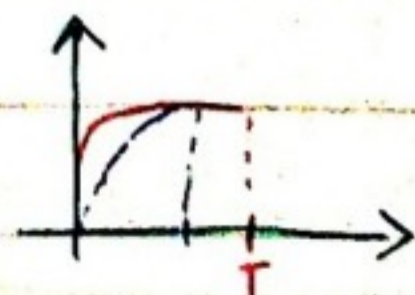


• To get the required $V_o(t)$:

$$T_1 \ll T$$

$$C_p (R_p \parallel R_s) \ll T$$

↳ we need C_p to be very small value.



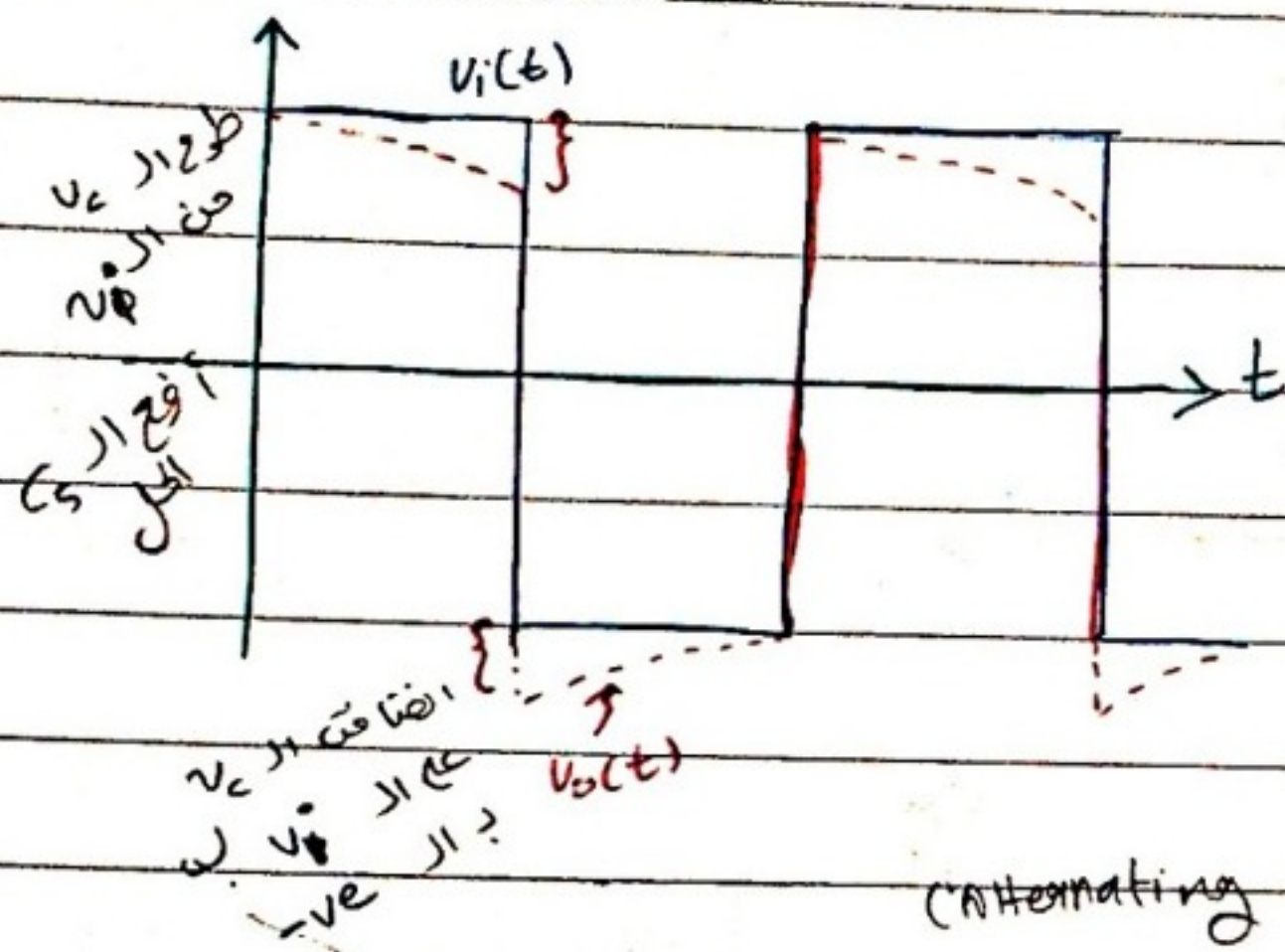
Time Response & frequency Response.

$$\tau \ll \frac{T}{10}$$

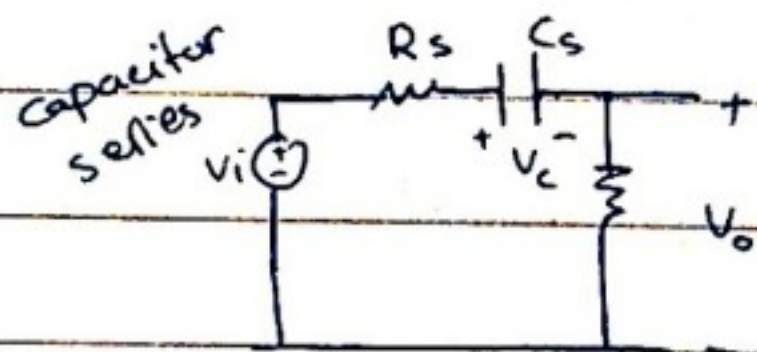
Time Response $\tau \ll \frac{T}{10}$



T.F. $\tau \ll \frac{T}{10}$ $\omega \ll \frac{1}{\tau}$

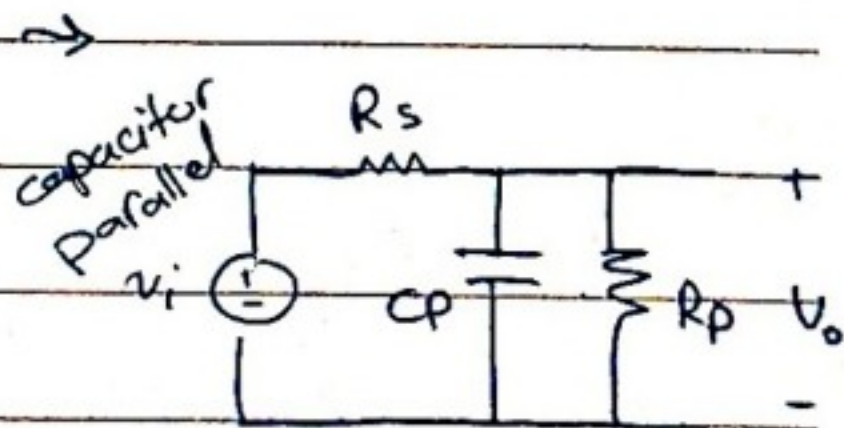
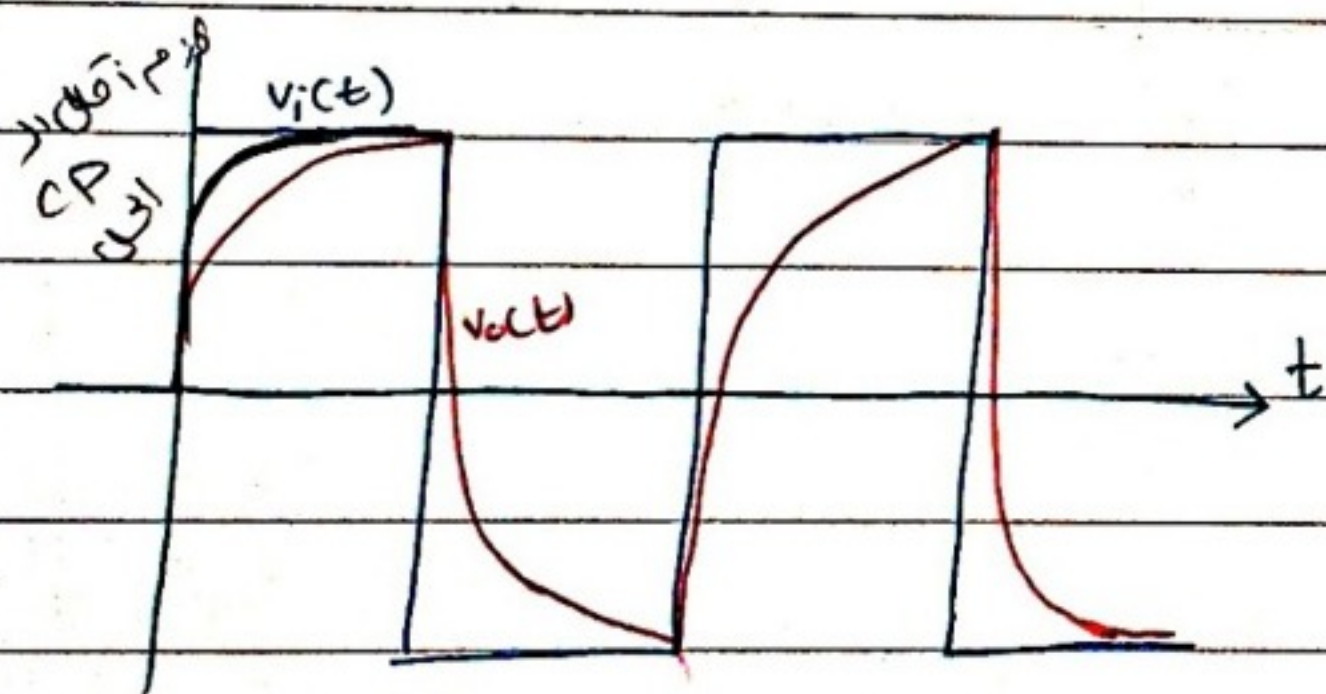


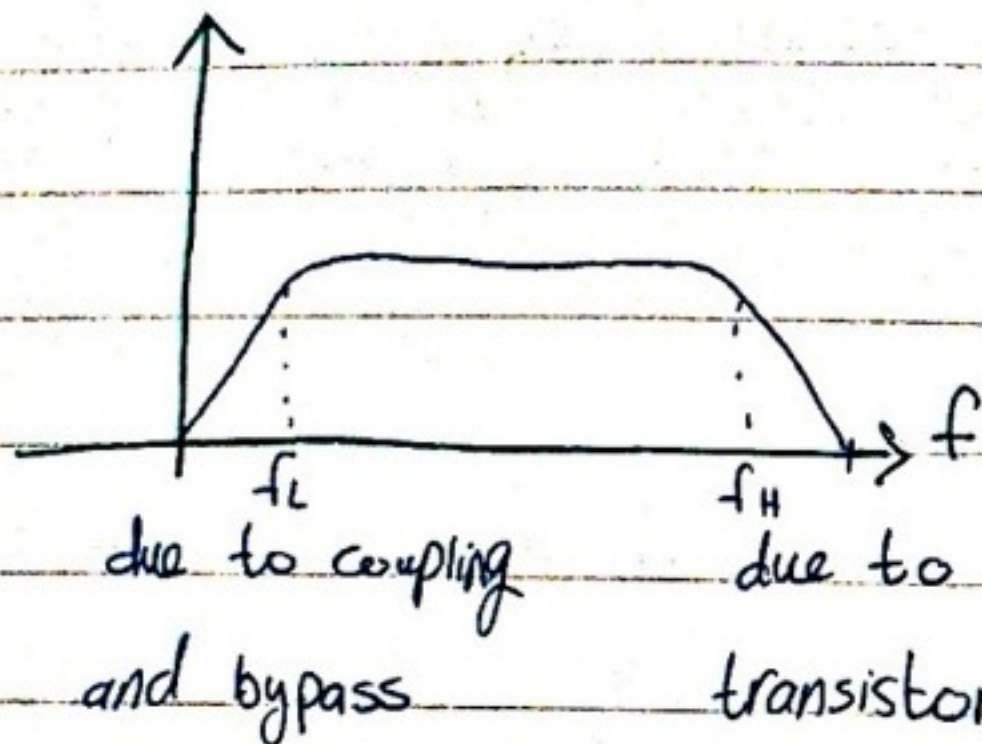
for the first ckt:



$$-v_i + v_c + v_o = 0$$

$$v_o = v_i - v_c$$

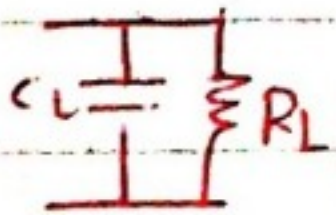




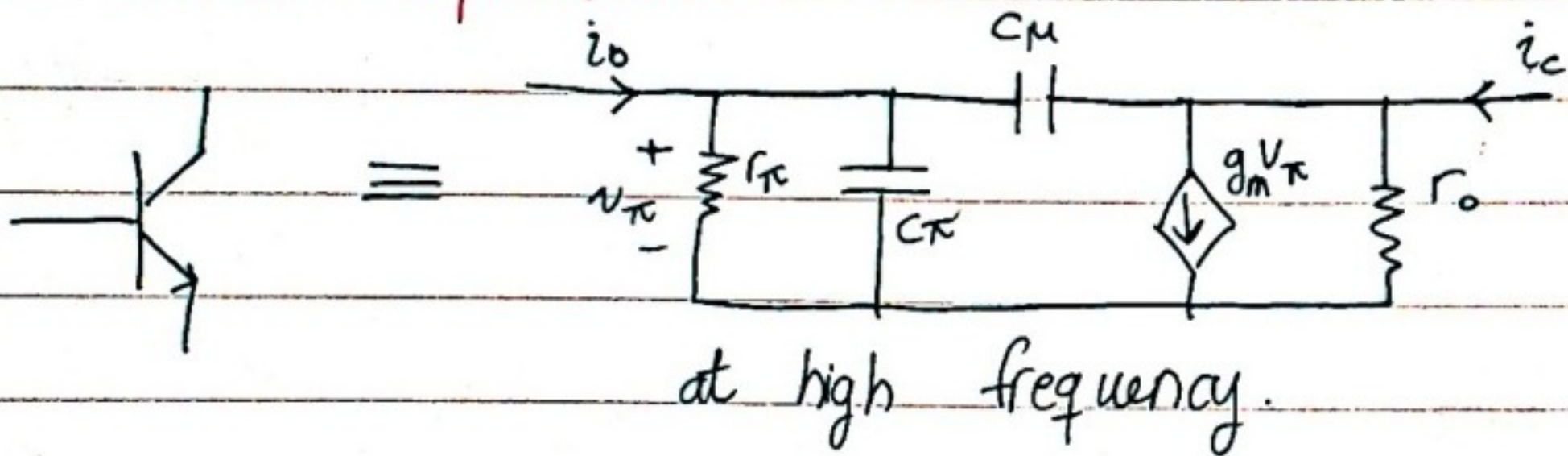
due to coupling and bypass capacitor

due to transistor and load capacitor

parallel to R_L



• Transistor capacitor:-



at high frequency.

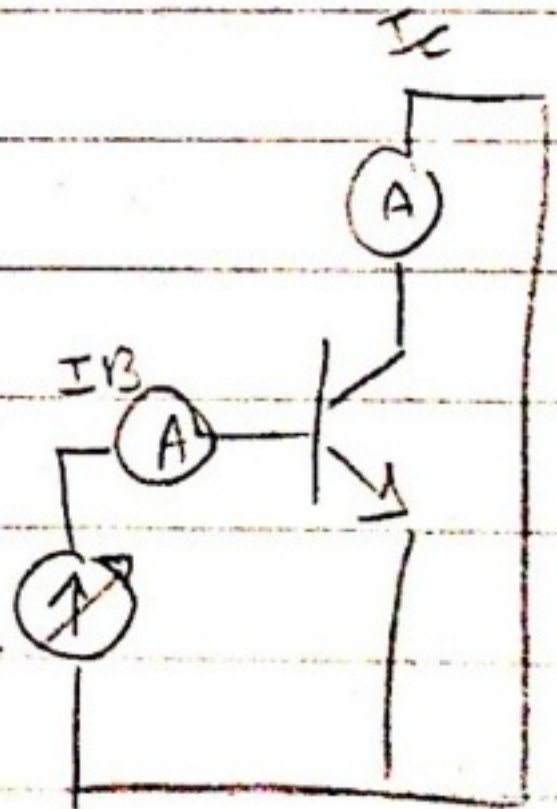
→ DC, low, mid frequency ranges:

$$i_c = \beta i_b$$

at high frequency: $i_c = h_{fe} i_b$

where h_{fe} : small signal current gain.

or ~~small~~ short-cct current gain

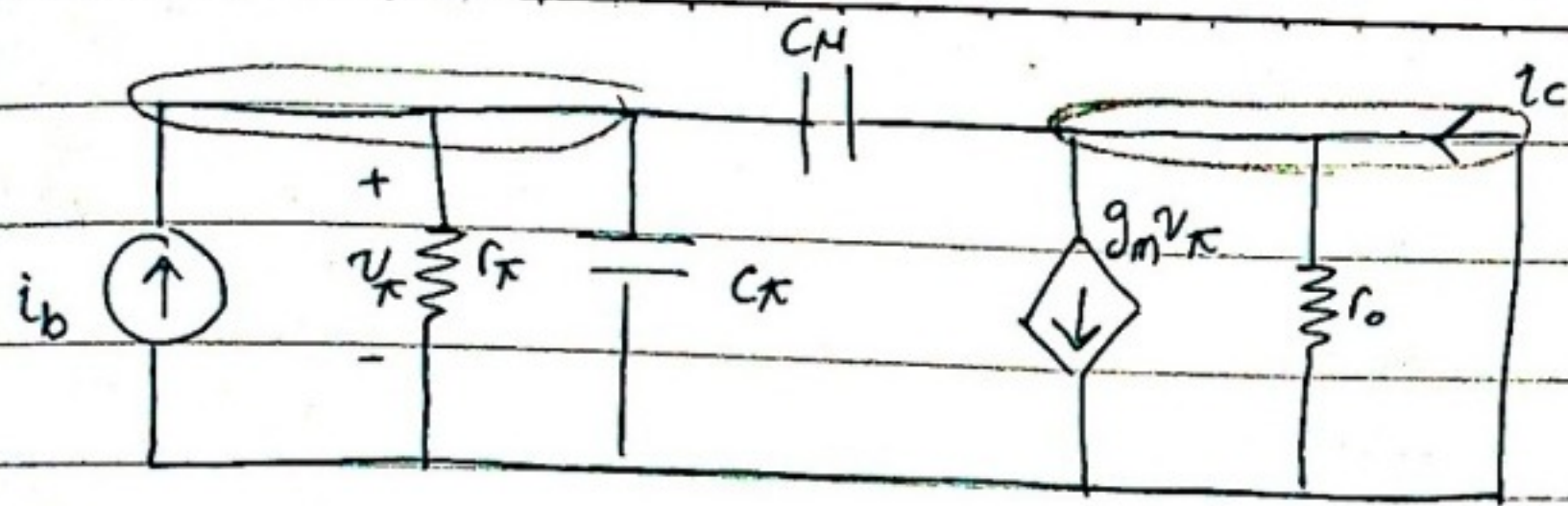


$$\beta = \frac{\Delta I_c}{\Delta I_B}$$



27-4/2014 Sun.

$i_c = g_m v_{\pi}$
 C_M



$$h_{fe} = \frac{i_c}{i_b}$$

• KCL at the input node:

$$i_b = \frac{v_{\pi}}{r_{\pi}} + \frac{v_{\pi}}{(1/j\omega C_{\pi})} + \frac{v_{\pi}}{(1/j\omega C_M)}$$

$$i_b = v_{\pi} \left(\frac{1}{r_{\pi}} + j\omega (C_{\pi} + C_M) \right) \rightarrow (1)$$

• KCL at the output node:

$$g_m v_{\pi} = i_c + \frac{v_{\pi}}{(1/j\omega C_M)}$$

$$v_{\pi} = \frac{i_c}{(g_m - j\omega C_M)} \rightarrow (2)$$

Sub (2) in (1) :-

$$h_{fe} = \frac{g_m - j\omega C_M}{\frac{1}{r_{\pi}} + j\omega (C_{\pi} + C_M)} = \frac{i_c}{i_b}$$

for typical values :-

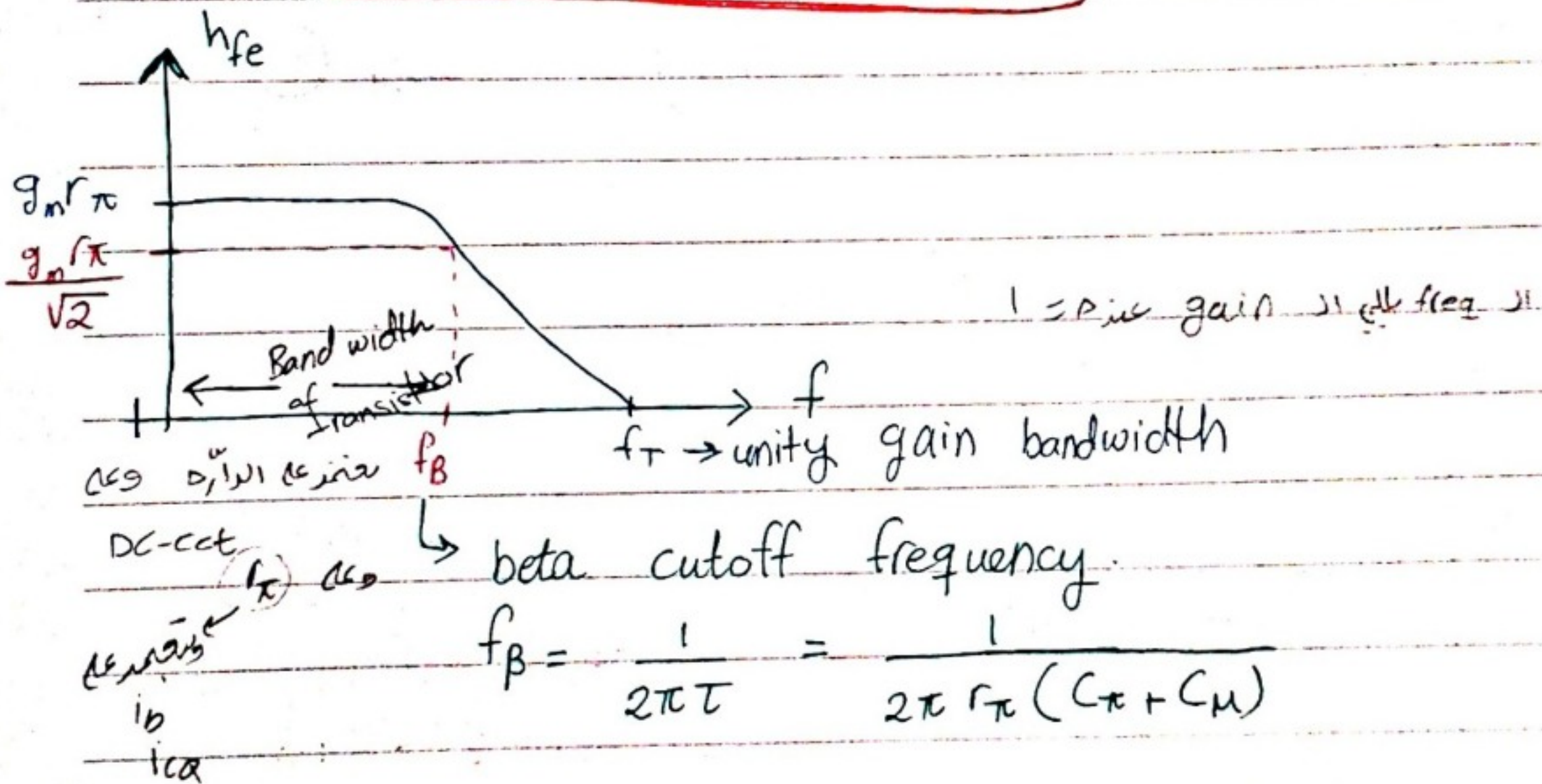
$$C_M = 0.2 \text{ pf}$$

$$g_m = 50 \text{ mA/V}$$

$$f_{\text{max}} = 100 \text{ MHz}$$

$$\Rightarrow \omega C_M \ll g_m$$

$$\text{So, } h_{fe} \approx \frac{g_m r_\pi}{1 + j\omega r_\pi (C_\pi + C_M)} \approx \frac{1}{1 + sT}$$



• f_T ?!

$$|h_{fe}(f_T)| = 1$$

$$\left| \frac{g_m r_\pi}{1 + j \left(\frac{f_T}{f_\beta} \right)} \right| = 1$$

$$\frac{g_m R}{\sqrt{1 + \left(\frac{f_T}{f_B}\right)^2}} = 1$$

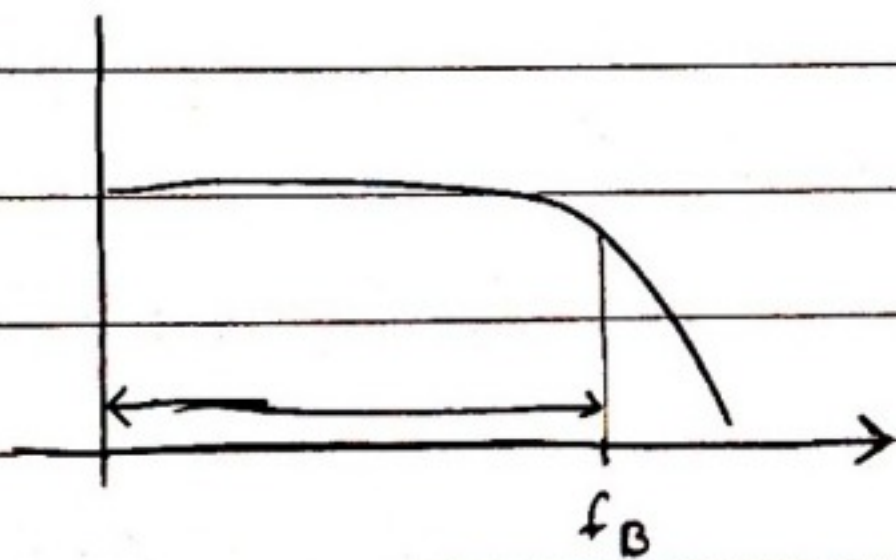
$$\begin{aligned} \cdot \frac{j f_T}{f_B} &= j \frac{f_T}{\frac{1}{2\pi R (C_T + C_M)}} \\ &= j 2\pi R (C_T + C_M) f_T \end{aligned}$$

usually $f_T \gg f_B \Rightarrow$

$$\frac{f_T}{f_B} = \beta$$

gain * Bandwidth = const.

$$\therefore \boxed{f_T = \beta f_B}$$



(Beta - cutoff - freq)

Bandwidth of
transistor

small size

$f_B \uparrow$

$\Rightarrow C_M \& C_T \downarrow$

29-4/2014 Tue

Example Find the 3dB freq of the short ckt current gain of BJT with $r_{\pi} = 2.6 \Omega$, $C_{\pi} = 2 \text{ pF}$

$$C_M = 0.1 \text{ pF}$$

$$f_B = \frac{1}{2\pi r_{\pi} (C_{\pi} + C_M)} = 29.1 \text{ MHz}$$

Example Find C_{π} for the BJT given that:

$$I_{CQ} = 1 \text{ mA}$$

$$f_T = 500 \text{ MHz}$$

$$\beta = 100$$

$$C_M = 0.3 \text{ pF}$$

$$f_T = \beta f_B \rightarrow f_B = 5 \text{ MHz}$$

$$f_B = \frac{1}{2\pi r_{\pi} (C_{\pi} + C_M)} \rightarrow C_{\pi} = 11.9 \text{ pF}$$

$$\frac{\beta V_T}{I_{CQ}} = V_T = 0.026 \text{ V}$$

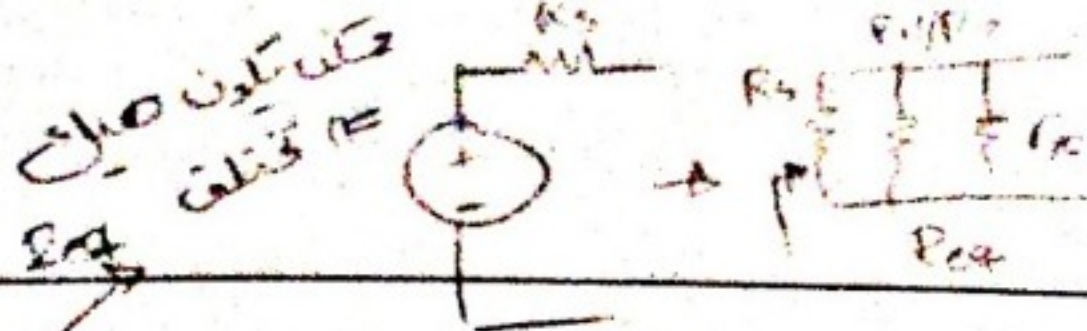
Note:-

1. $f_T \gg f_B$

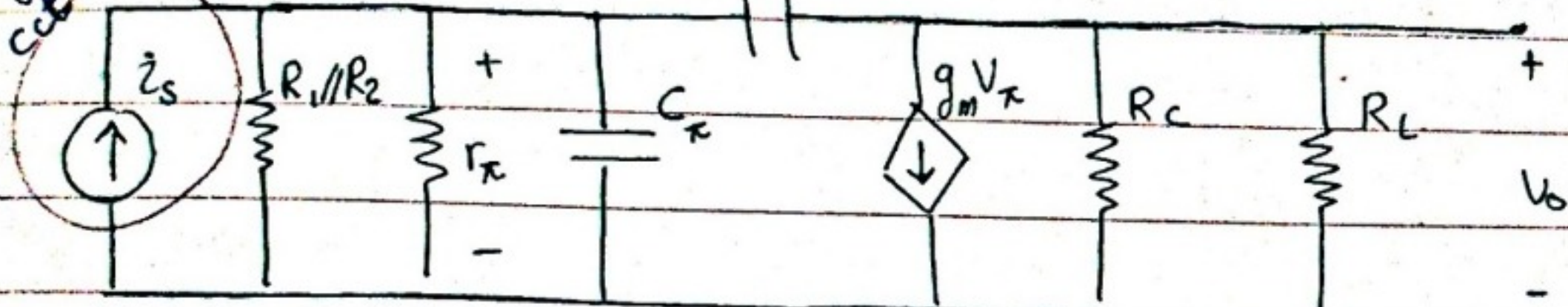
2. $C_M \ll C_{\pi}$

* $C_M \ll C_{\pi}$; But we can't neglect C_M due to Miller effect.

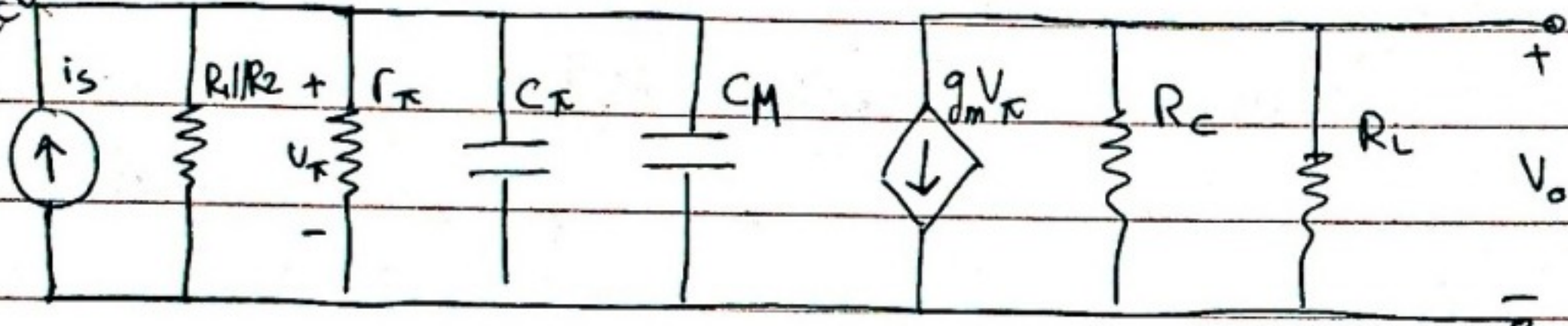
29-4/2014 Tue.



original cct



equivalent cct



$$C_M = C_{\mu} * [1 + g_m (R_c // R_L)]$$

Miller effect (OR feedback effect)
Miller Capacitance

$$f_{3dB} = \frac{1}{2\pi \tau}, \quad \tau = R_{eq} C_{eq}$$

* Example * If $R_c = R_L = 4 \text{ k}\Omega$, $r_{\pi} = 2.6 \text{ k}\Omega$

$R_1 // R_2 = 200 \text{ k}\Omega$, $C_{\pi} = 4 \text{ pF}$, $C_{\mu} = 0.2 \text{ pF}$

$g_m = 38.5 \text{ mA/V}$, Find: f_{3dB} for this cct.

① if we consider the Miller effect:

$$f_{3dB} = \frac{1}{2\pi \tau} = \frac{1}{2\pi R_{eq} C_{eq}}$$

$$= \frac{1}{2\pi (R_1 // R_2 // r_{\pi}) (C_{\pi} + C_M)} = 3.16 \text{ MHz}$$

$\hookrightarrow 15.6 \text{ pF}$

cut
Trans.
FR

f_{3dB} \uparrow \downarrow

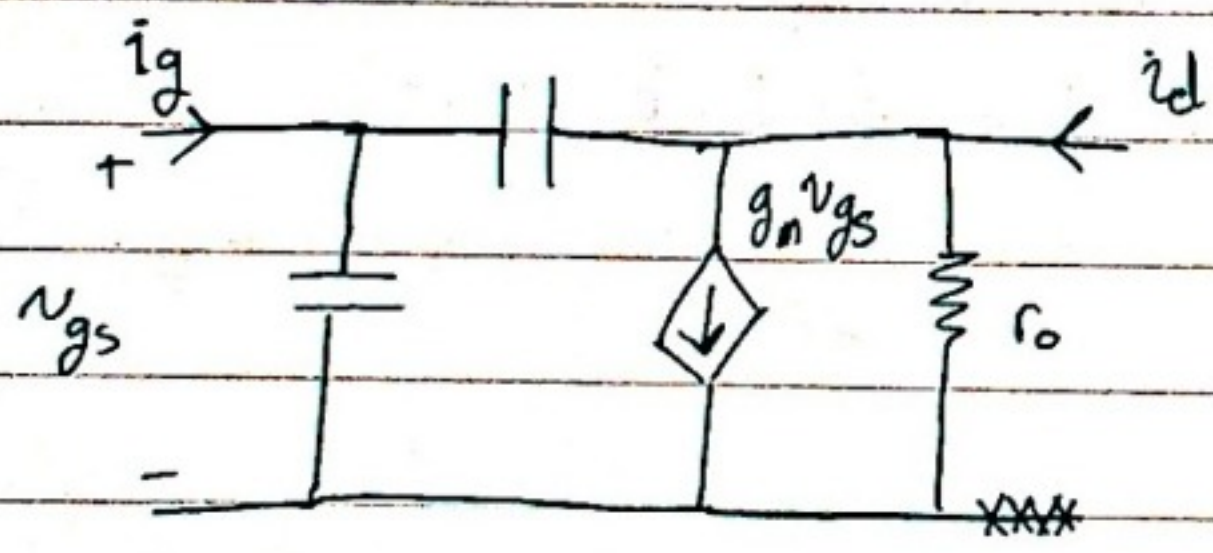
do not \uparrow consider the Miller effect ($C_M = 0$)

$$f_{3dB} = \frac{1}{2\pi(R_1 \parallel R_2 \parallel r_\pi)C_\pi} = 15.5 \text{ MHz}$$

$C_\mu : O.C$
 $\rightarrow C_M = C_\mu \cdot (\dots)$
 $\Rightarrow C_M = 0$

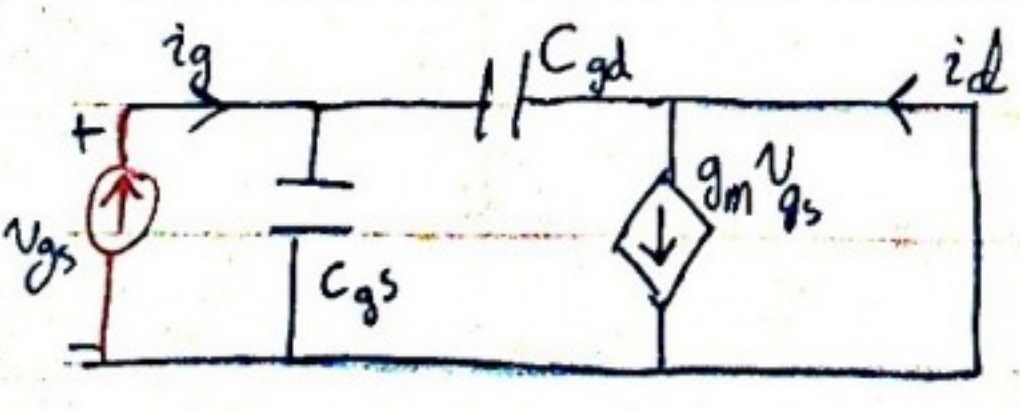
$f_{3dB} \text{ Miller} \ll f_{3dB} \text{ without Miller}$ Mid \uparrow \downarrow

FET at high frequency :-



- in DC $\rightarrow I_G = 0$
- low & Midband $\rightarrow I_G = 0$
- high frequency $\rightarrow ?!$

* We calculate the short cct current gain:



$$A_i = \frac{i_d}{i_g}$$

29-4/2014 Tue

$$A_i = \frac{v_d}{v_g} = \frac{g_m - j\omega C_{gd}}{j\omega (C_{gs} + C_{gd})}$$

if we consider the typical values $C_{gd} = 0.05 \text{ pF}$

$$g_m = 1 \text{ mA/V}$$

$$\rightarrow g_m \gg \omega C_{gd}$$

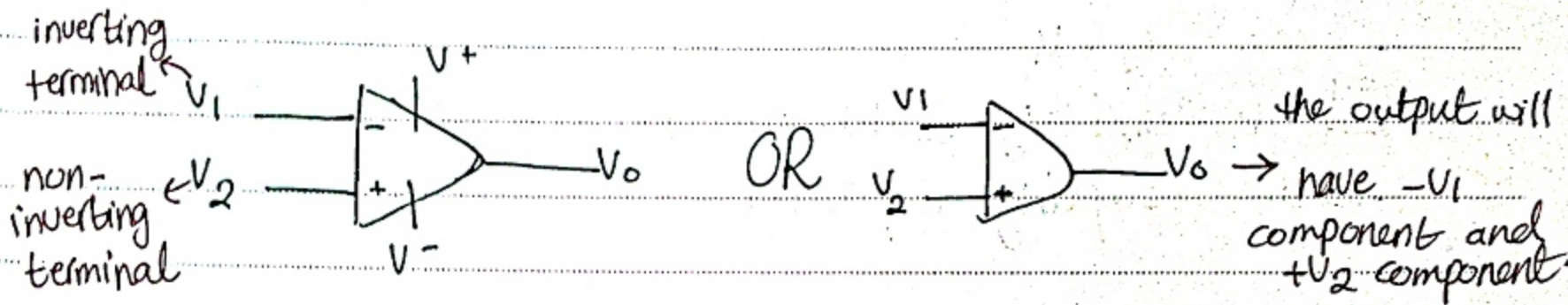
$$A_i = \frac{g_m}{j\omega (C_{gs} + C_{gd})}$$

\rightarrow unity gain bandwidth:-

$$f_T = \frac{g_m}{2\pi (C_{gs} + C_{gd})}$$

Operational Amplifier (op-amp)

it is an integrated ckt (IC) that amplifies the difference between two input voltage produces a signal output.



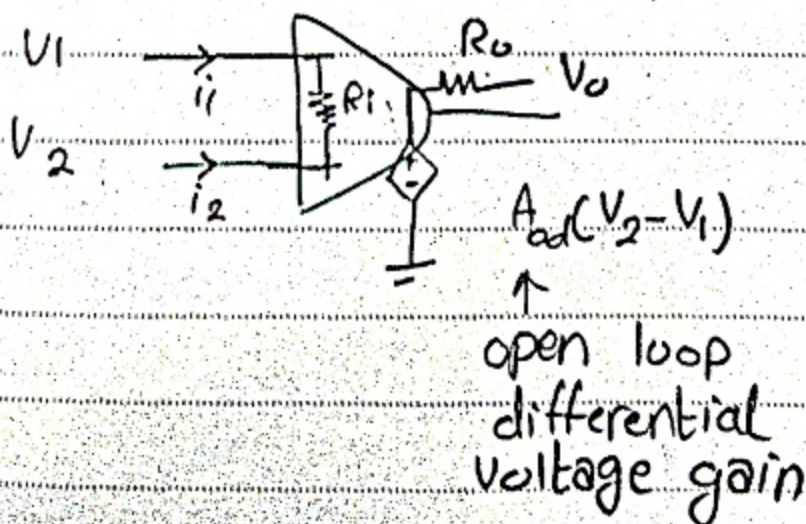
Name, why "operational"?

it was used in analog computers to perform mathematical operations to solve differential and integral equations.

* Ideal op-amp \rightarrow will be considered usually.

* non-ideal op-amp

Ideal op-amp:-



$$\textcircled{1} R_i = \infty \Omega$$

$$\textcircled{2} R_o = 0 \Omega$$

$$\textcircled{3} i_1 = i_2 = 0 \text{ A}$$

$$\textcircled{4} A_{od} = \infty$$

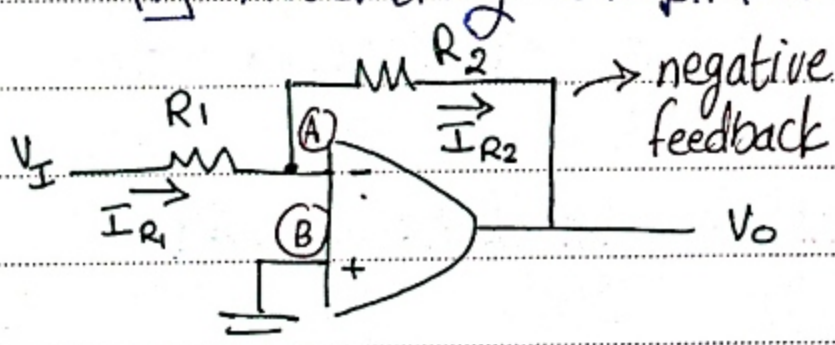
$$\Rightarrow V_2 - V_1 = 0$$

$$\therefore V_2 = V_1$$

$\textcircled{5}$ V_1 and V_2 could be DC or AC, and we need coupling capacitor.

• OP-amp Applications-

$\textcircled{1}$ inverting amplifier.



• at A: $V_1 = 0$
 $i_1 = 0$

• at B: $V_2 = V_1$
 $I_2 = 0$

$$I_{R1} = I_{R2}$$

$$\frac{V_I - 0}{R_1} = \frac{0 - V_o}{R_2}$$

$$\rightarrow \frac{V_o}{V_I} = -\frac{R_2}{R_1}$$

$$V_o = V_I \left(-\frac{R_2}{R_1} \right)$$

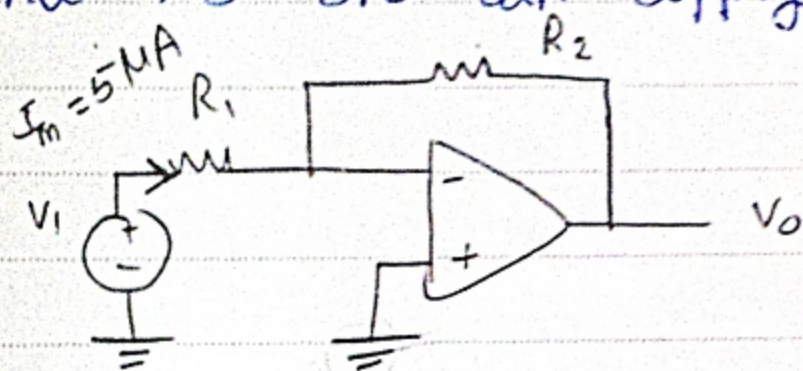
* Point (A) is:
an actual ground
cause it gave $V_1 = 0$
 $\neq I_1 = 0$

• feedback:-

negative feedback: it result in stable circuit

positive feedback: it is used to produce oscillators.

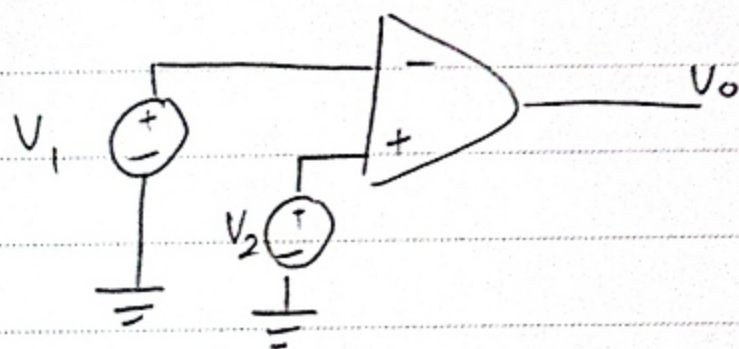
Example:- Design an inverting amp. such that the voltage gain $A_v = -5$, knowing that this ~~set~~ ^{set} is connected with a src that have $V_s = 0.1 \sin \omega t$ V and this src can supply maximum current of 5 mA.



$$A_v = -\frac{R_2}{R_1} = -5$$

$$R_2 = 5R_1$$

$$I_m = \frac{V_{s(max)} - 0}{R_1}$$



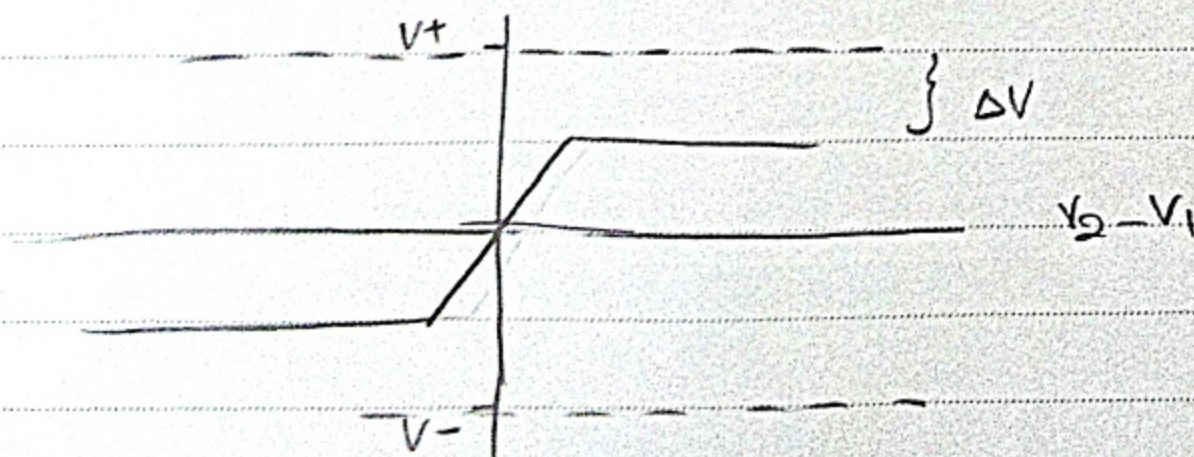
$$\rightarrow R_1 = 20 \text{ k}\Omega$$

$$\therefore R_2 = 100 \text{ k}\Omega$$

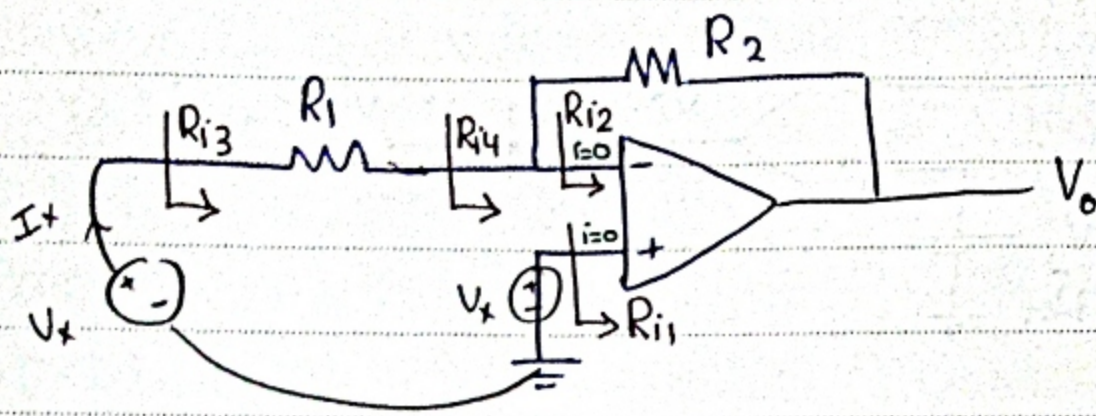
(comparator)

if $V_2 > V_1 \rightarrow V_0 = +V_c$

if $V_2 < V_1 \rightarrow V_0 = -V_c$



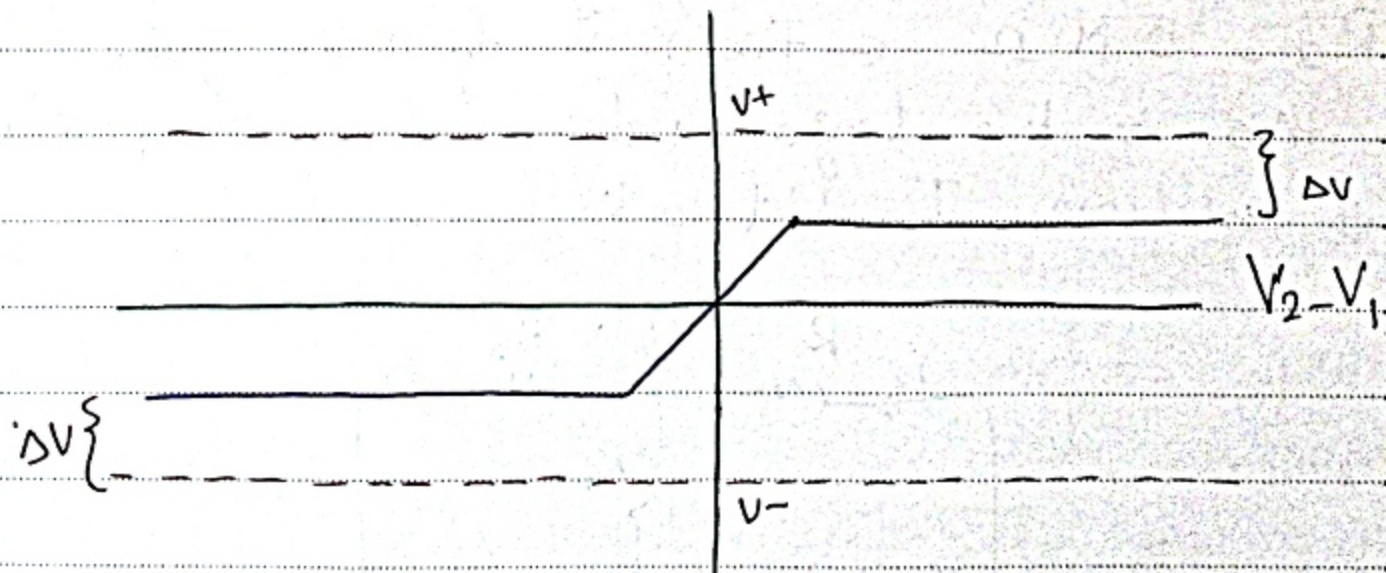
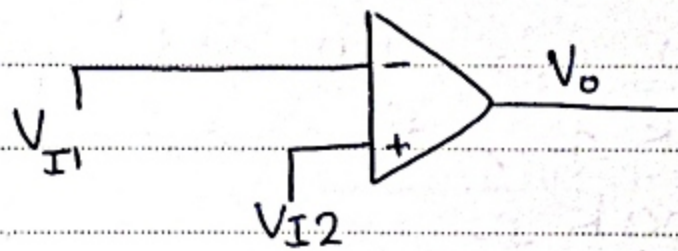
8/5/2014



[inverting Amp]
 $|Gain| = \left| \frac{R_2}{R_1} \right|$

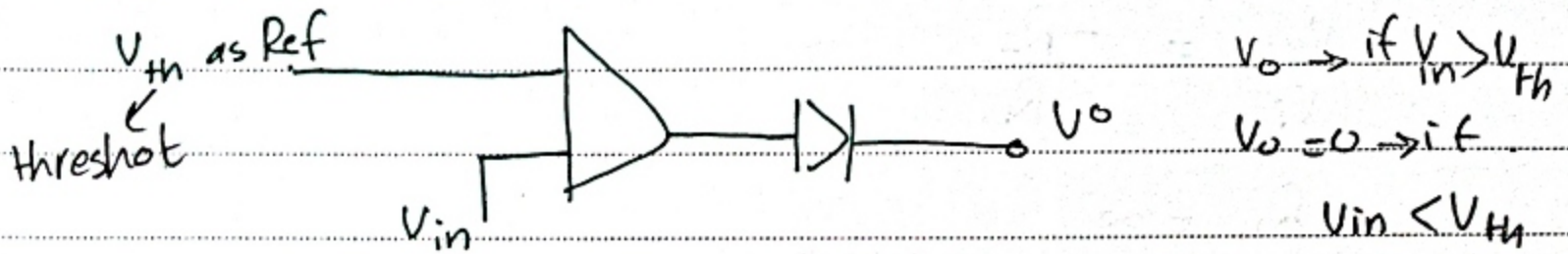
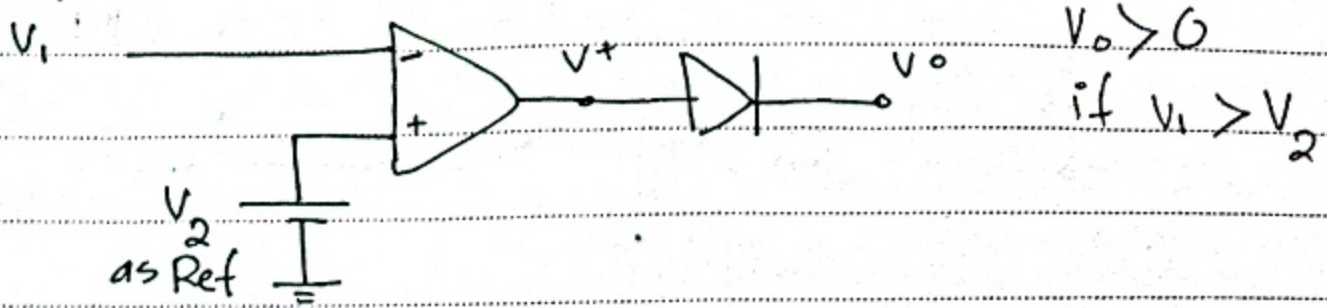
$$\frac{V_o}{V_i} = -\frac{R_2}{R_1}$$

- $R_{i1} = \infty$
- $R_{i2} = \infty$, $\frac{V_x}{I_x} = \frac{V_x}{0} = \infty$
- $R_{i3} = R_1$
- $R_{i4} = \frac{V_x}{I_x} = 0$



V_o of an op-amp ckt is always between
 $V^- + \Delta V < V_o < V^+ - \Delta V$

* Comparator :-



• Application:- Amplifier with T-Network.

why do we need T-Network?!

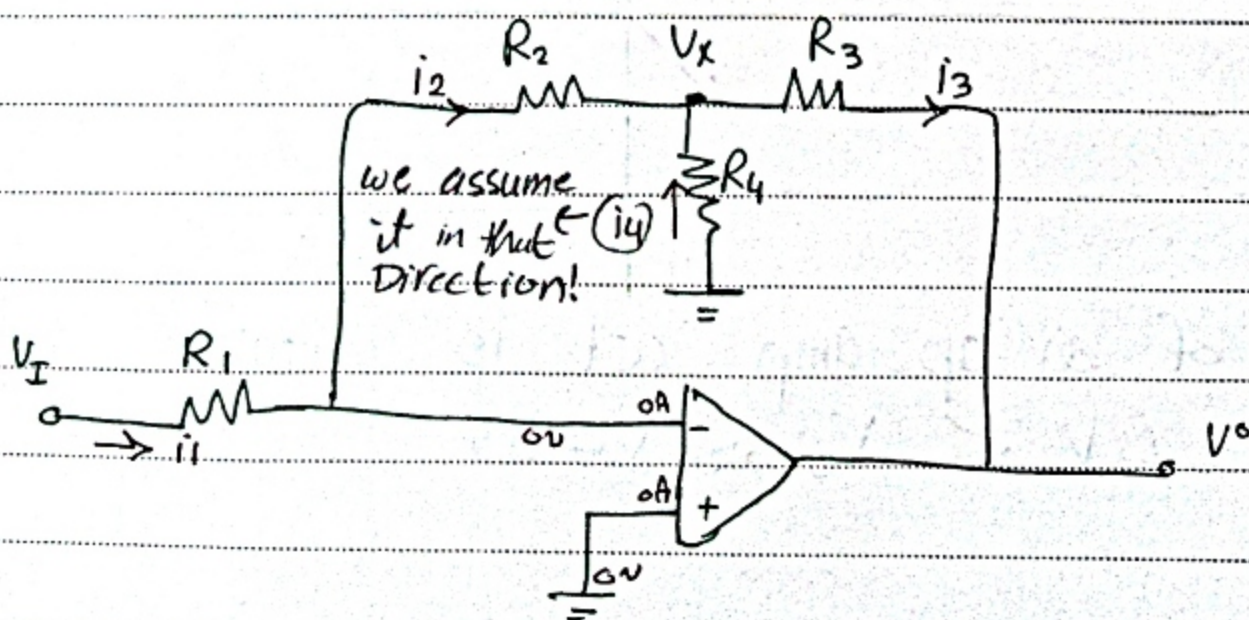
answer: if we want to design an inverting amplifier with $A_v = -100$ and input impedance of $R_i = 50\text{ k}\Omega$, then we need:

$R_1 = R_i = 50\text{ k}\Omega$

$R_2 = 5\text{ M}\Omega$ ← Finding it from the gain.

→ this is too large value for most practical ckt.

⇒ solution: T-Network



$$i_2 = i_1$$

$$\frac{V_I}{R_1} = \frac{0 - V_x}{R_2}$$

$$\rightarrow V_x = \frac{-R_2}{R_1} V_i \rightarrow (1)$$

requirements $\left. \begin{array}{l} \text{Gain } \uparrow \\ R_i \uparrow \end{array} \right\} \rightarrow \text{loading effect } \downarrow$
 $\therefore R_2$ will be \uparrow

@ node x:

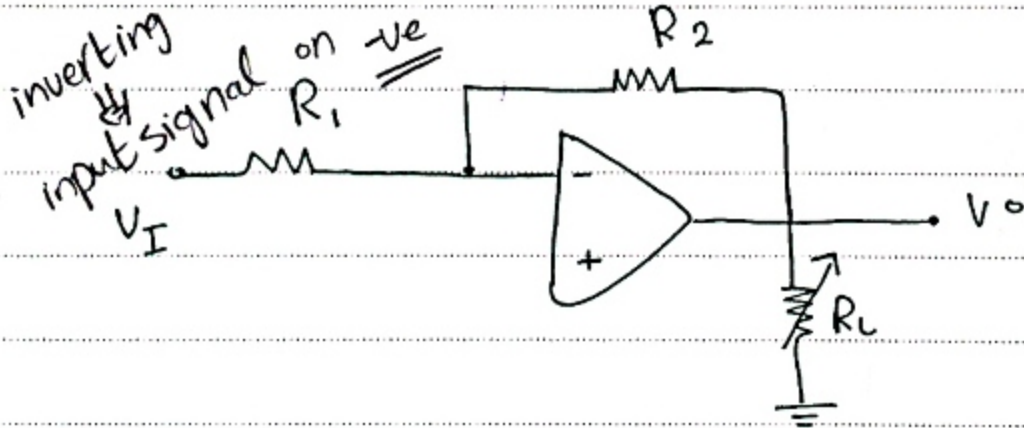
$$i_2 + i_4 = i_3$$

$$-\frac{V_x}{R_2} - \frac{V_x}{R_4} = \frac{V_x - V_o}{R_3}$$

$$V_x = \left(\frac{1}{R_2} + \frac{1}{R_4} + \frac{1}{R_3} \right) = \frac{V_o}{R_3} \rightarrow (2)$$

sub (2) in (1):

$$A_v = \frac{V_o}{V_i} = \frac{-R_2}{R_1} \left(1 + \frac{R_3}{R_4} + \frac{R_3}{R_2} \right)$$



$$\boxed{A_v} = \frac{-R_2}{R_1}$$

will not change
with R_L

non-ideal $A_{od} = \infty$ $R_i = \infty$ $R_o = 0$

Ideal OP-amp:- if is assumed to simplify the analysis and design non-ideal op-amp but the final will be similar to the non-ideal op-amp.

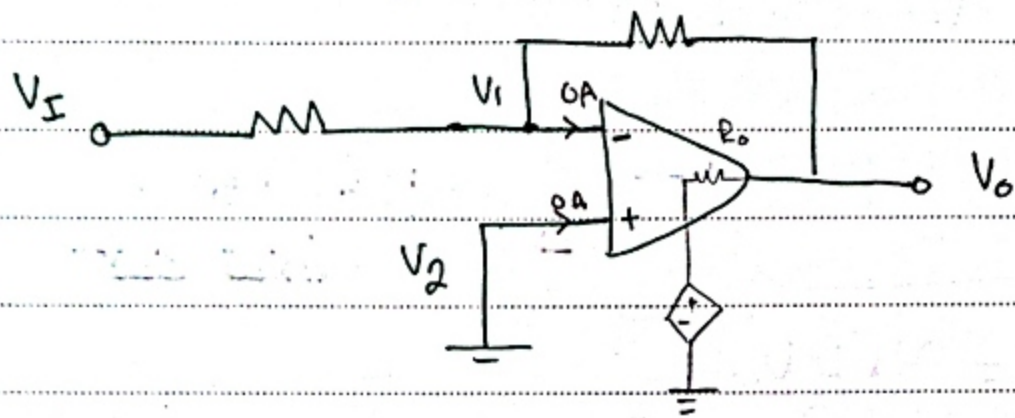
→ also coupling capacitor at input and output !!

8/5/2014

• Example:- if we assume that $A_{od} \neq \infty$

→ $V_2 \neq V_1$ $R_i = \infty$ $R_o = 0$

Find the gain of an inverting amp:-



neither completely ideal nor non-ideal.

$R_i = \infty \rightarrow i_1 = i_2 = 0$

$i_{R1} = i_{R2}$

• $\frac{V_I - V_1}{R_1} = \frac{V_1 - V_O}{R_2} \rightarrow \text{---}$

• $V_O = A_{od} (V_2 - V_1) = -A_{od} V_1$

→ $V_1 = \frac{-V_O}{A_{od}}$

Sub (2) in (1)

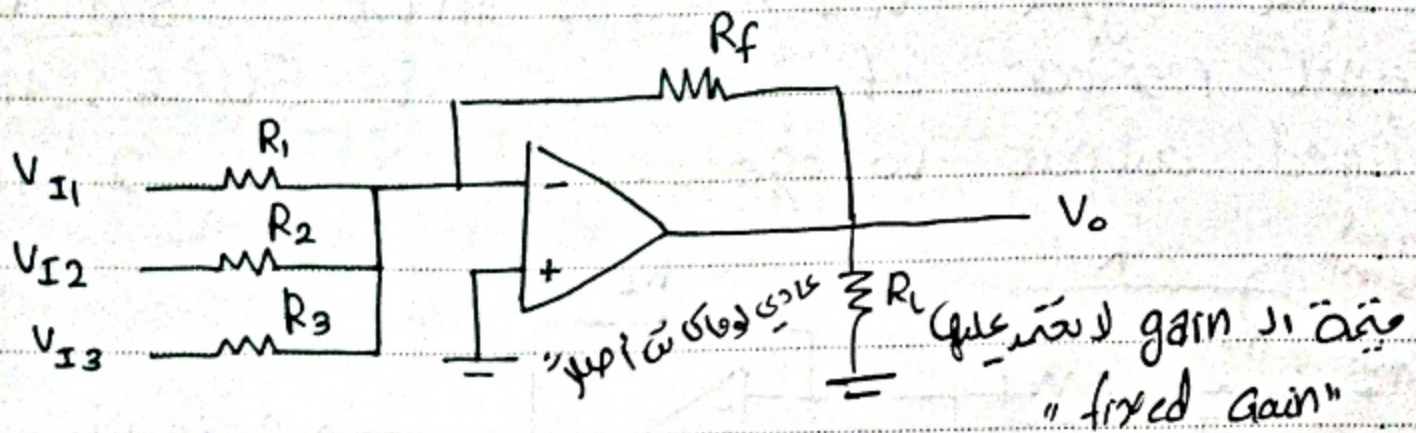
$A_v = \frac{-R_2}{R_1} \left(1 + \frac{1}{A_{od}} \left(1 + \frac{R_2}{R_1} \right) \right)$

if $R_2 = 100 \text{ k}\Omega$ $R_1 = 10 \text{ k}\Omega$

	A_{od}	A_v
	10^2	-9.01
non-ideal	10^3	-9.89
	10^4	-9.989
	10^5	-9.999
	10^6	-9.9999
	ideal case	∞

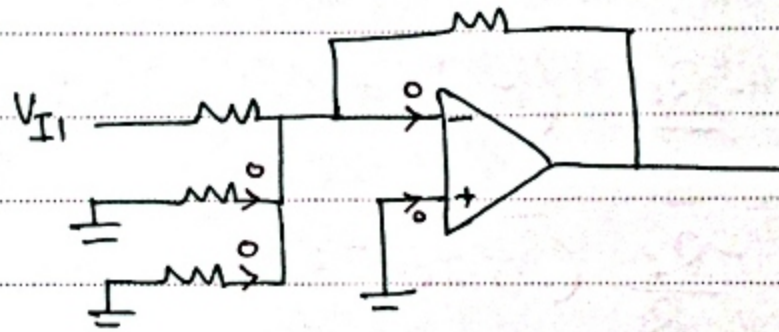
→ the same result.

• summing amplifier:



use super position technique:-

$V_o' = V_o$ due to V_{I1} only:-



$$\therefore V_o' = \frac{-R_f}{R_1} * V_{I1}$$

$$V_o'' = \frac{-R_f}{R_2} * V_{I2}$$

$$V_o''' = \frac{-R_f}{R_3} * V_{I3}$$

$$\therefore V_{total} = -R_f \left(\frac{V_{I1}}{R_1} + \frac{V_{I2}}{R_2} + \frac{V_{I3}}{R_3} \right)$$

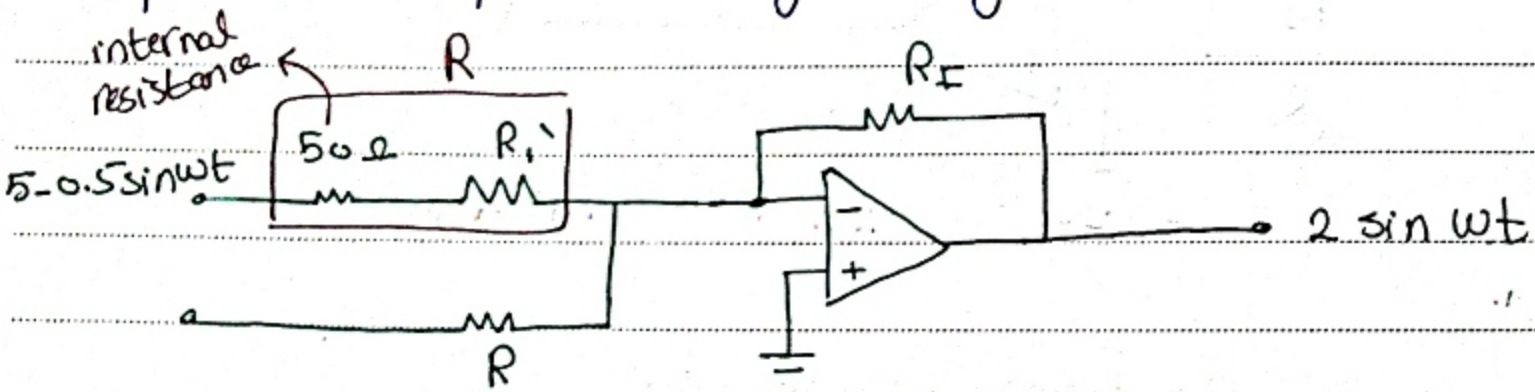
if $R_1 = R_2 = R_3 = R$

$$\rightarrow V_o = \frac{-R_f}{R} (V_{I1} + V_{I2} + V_{I3})$$

$V_o = -(V_{I1} + V_{I2} + V_{I3})$: just if all Resistors are equal to each other

11/15/2014

• Example:- Design a summing Amplifier that has an input signal $V_i = 5 - 0.5 \sin \omega t$ and the internal resistor of the source is 50Ω , the required output voltage signal is $V_o = 2 \sin \omega t$



$$V_o = -\frac{R_f}{R} (V_{I1} + V_{I2})$$

$$2 \sin \omega t = -\frac{R_f}{R} (5 - 0.5 \sin \omega t + V_{I2})$$

$$2 \sin \omega t = -\frac{R_f}{R} (5 - 0.5 \sin \omega t + (-5))$$

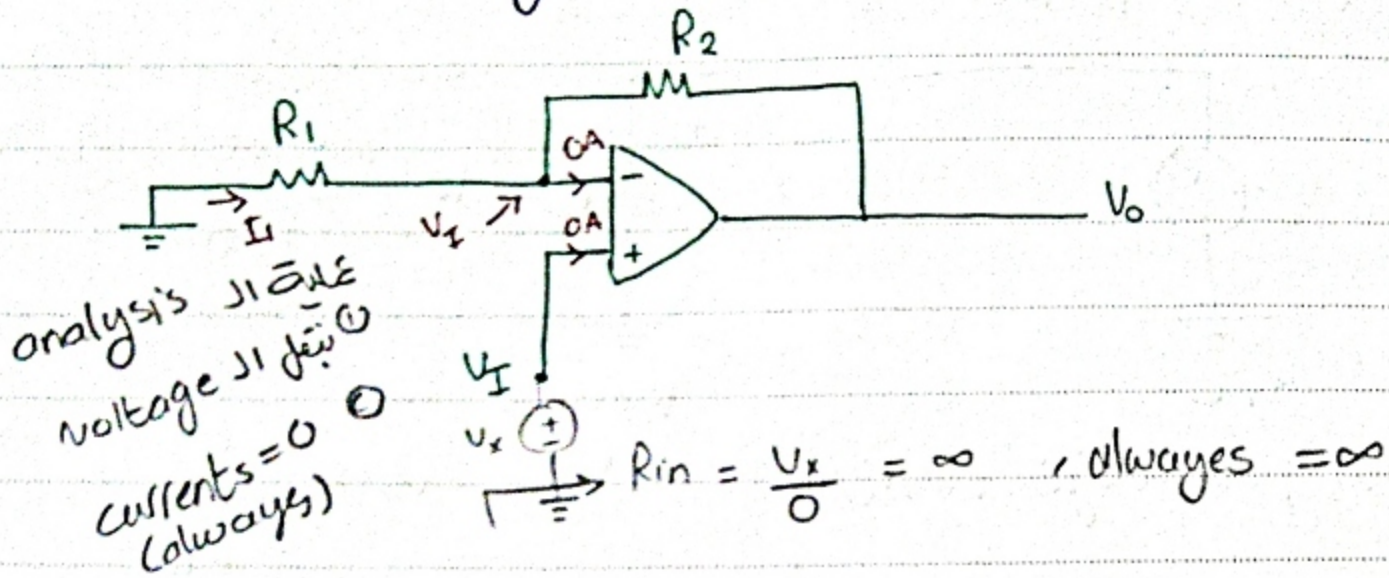
$$2 = -\frac{R_f}{R} (-0.5)$$

$$\rightarrow \frac{R_f}{R} = 4 \Rightarrow \boxed{R_f = 4R} \quad \therefore \text{any two values verified this ratio.}$$

$$\text{Let } R_f = 120 \text{ k}\Omega \rightarrow R = 30 \text{ k}\Omega$$

$$R_i' = 30 \text{ k}\Omega - 50 \Omega$$

• Non-inverting amplifier:-

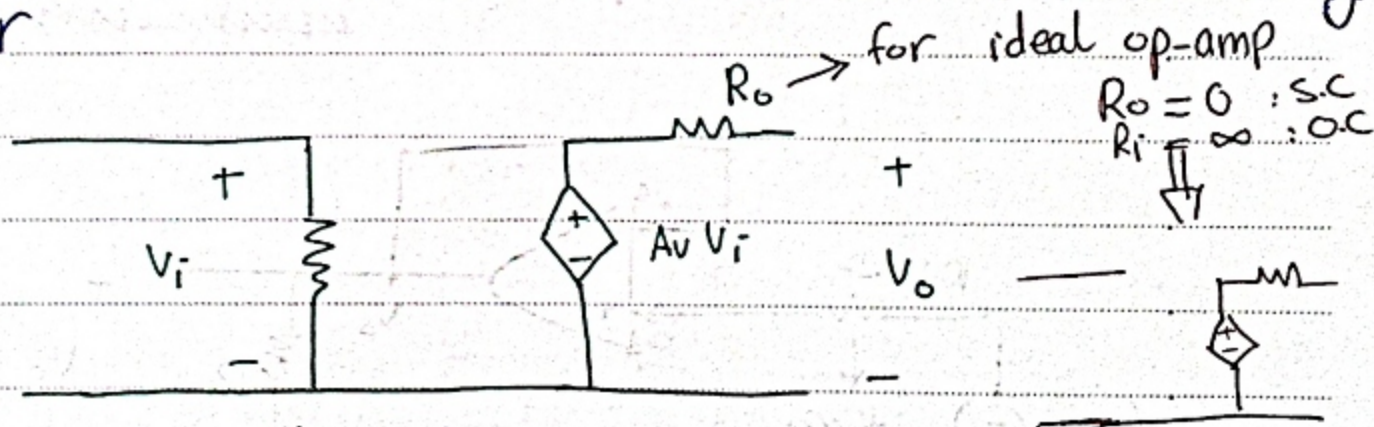


$I_1 = I_2$

$\frac{0 - V_I}{R_1} = \frac{V_I - V_O}{R_2}$

$A_v = \frac{V_O}{V_I} = 1 + \frac{R_2}{R_1}$ (Here > 1)

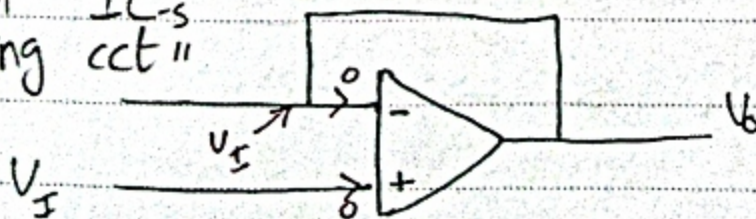
• Equivalent two-port Network of non-inverting amplifier



$A_v < 1$ when $R_2 < R_1$!

loading effect
output follows V_I mag & phase.
• Voltage follower (Buffer / impedance transformer)

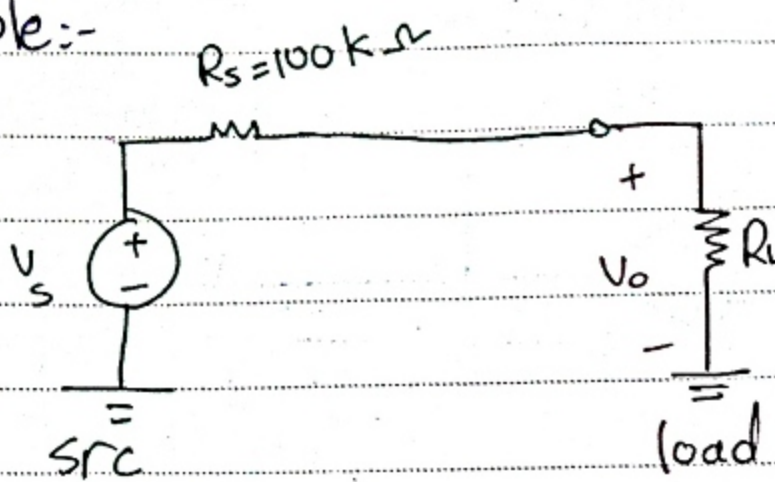
using in IC-s
"integrating cct"



$A_v = \frac{V_O}{V_I}$

$A_v = 1$

• Example:-



src مع load \rightarrow
without using
Buffer.

using voltage division:
$$V_o = V_s \times \frac{1}{1 + 100}$$

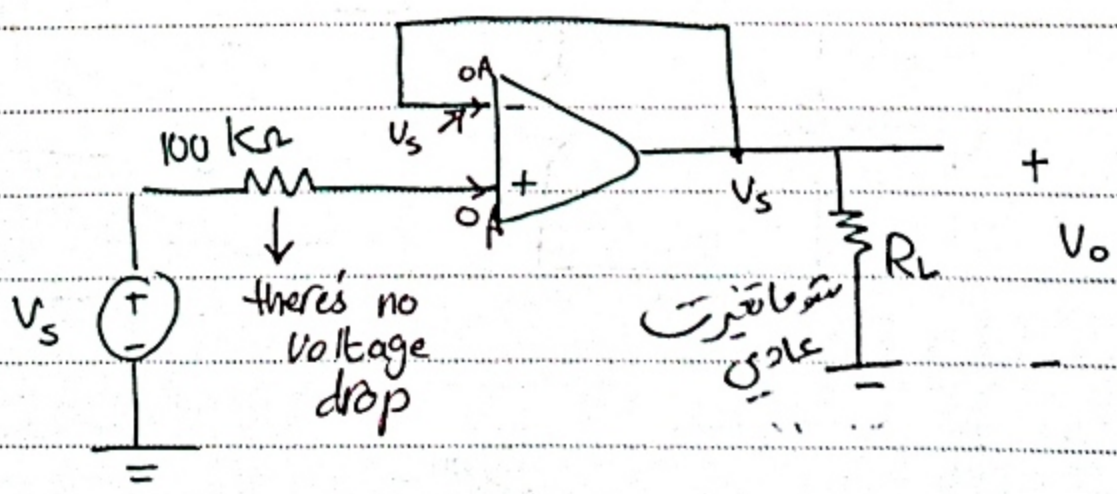
\rightarrow High loading effect
problem.

But without loading effect (without load) \rightarrow

$V_o = V_s$

\Rightarrow with load V_o changed.

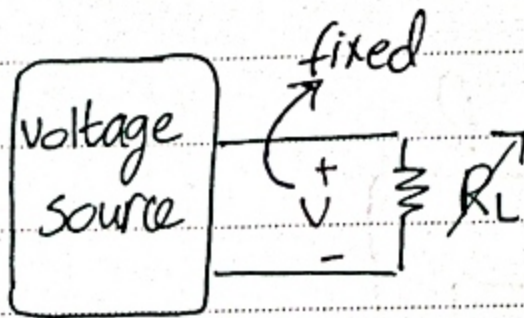
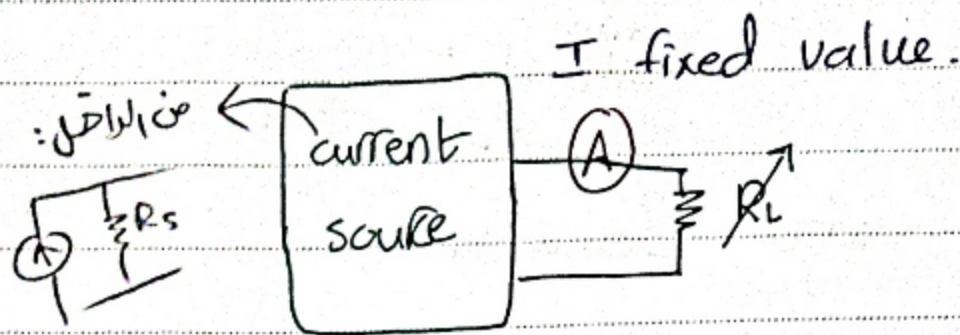
to solve this problem using Buffer



$\rightarrow V_o = V_s$ "no loading effect"

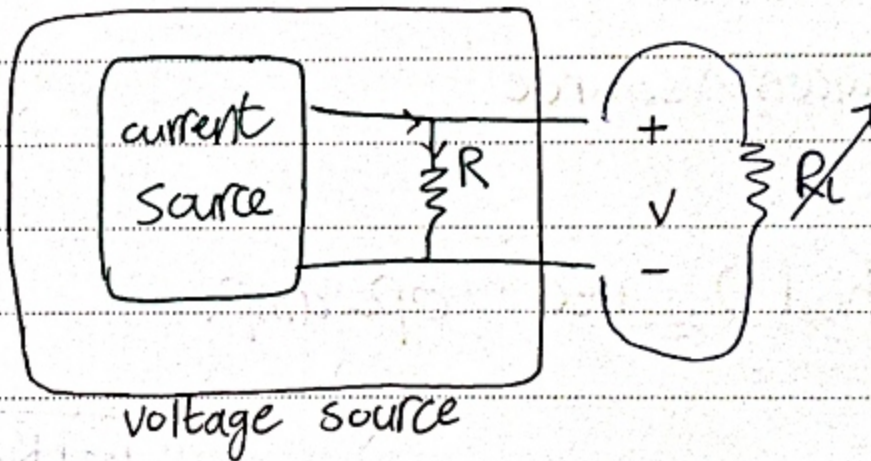
if $R_L : SC \rightarrow V_o = 0$

• current - to - voltage converter:-



→ current to voltage converter:-

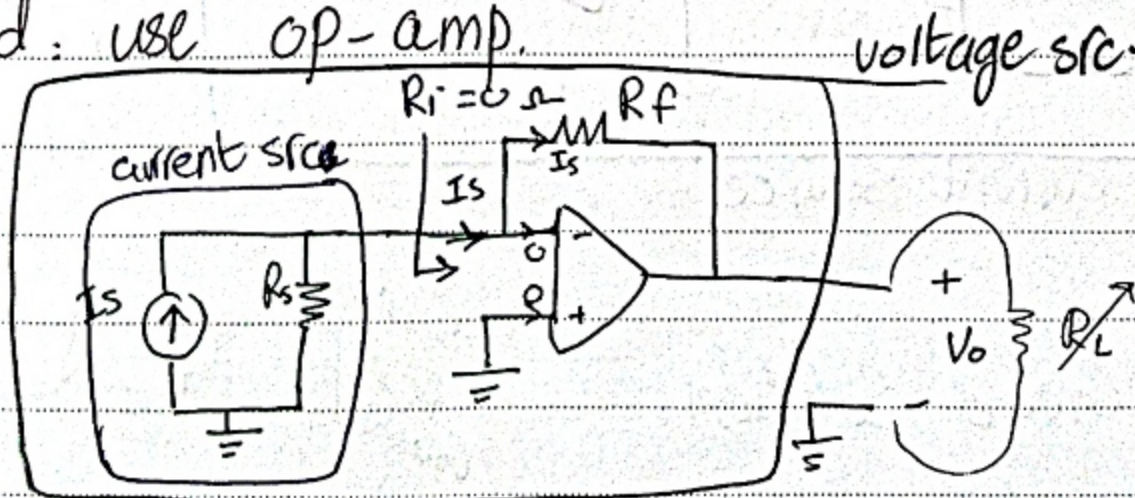
* Method: use \$R\$.



\$V\$ will change with \$R_L\$ so it is bad solution.

* Method: use op-amp.

R_s internal resistor of the source



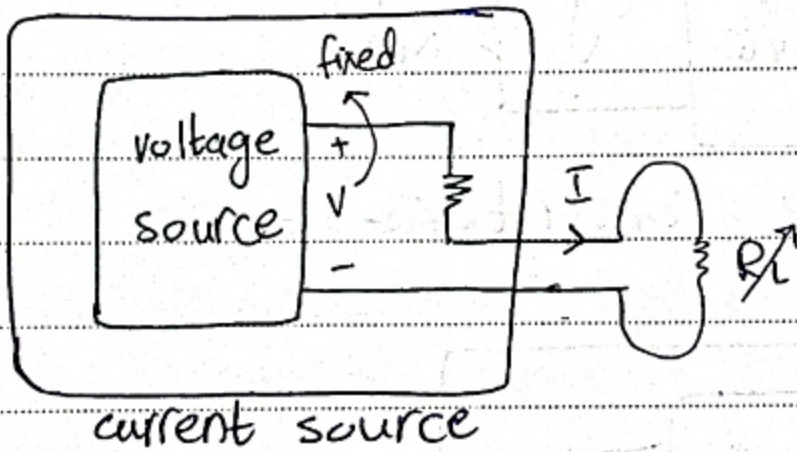
$$I_s = \frac{0 - V_o}{R_f} \rightarrow V_o = -R_f I_s$$

fixed independent on R_L

→ Good Solution.

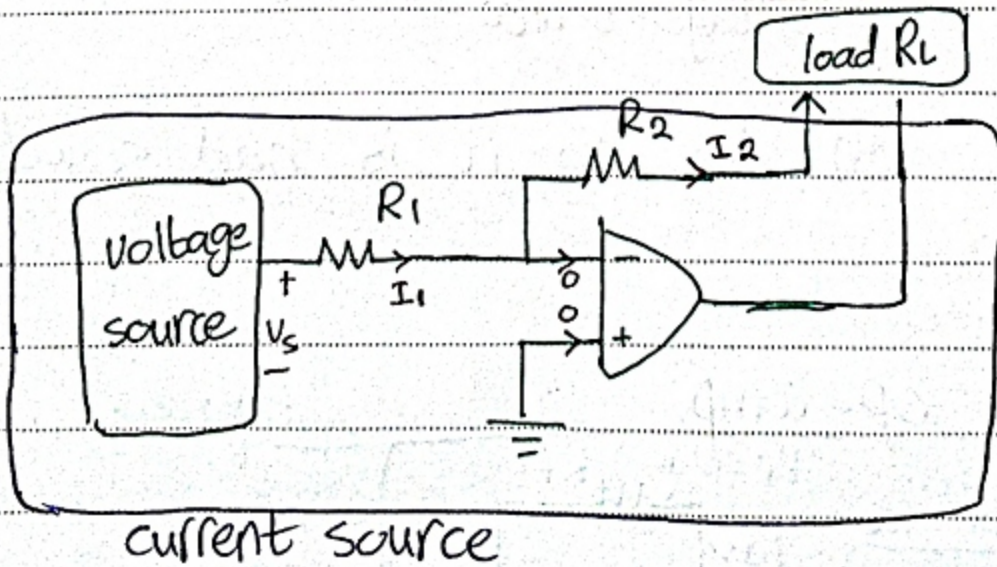
* Voltage-to-current inverter:-

• Method 1: use R_f :



→ Bad solution since I changes with R_L

• Method 2: use op-amp:



$$I_2 = I_1 = \frac{V_s}{R_1}$$

fixed

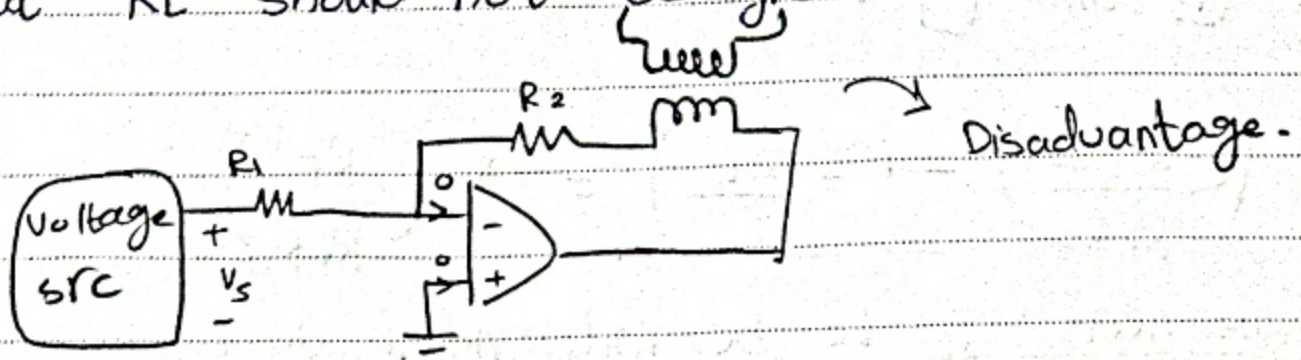
I_2 fixed, ind. on R_2

→ Good Solution.

لا تصنع انو R_L تكون Grounded!

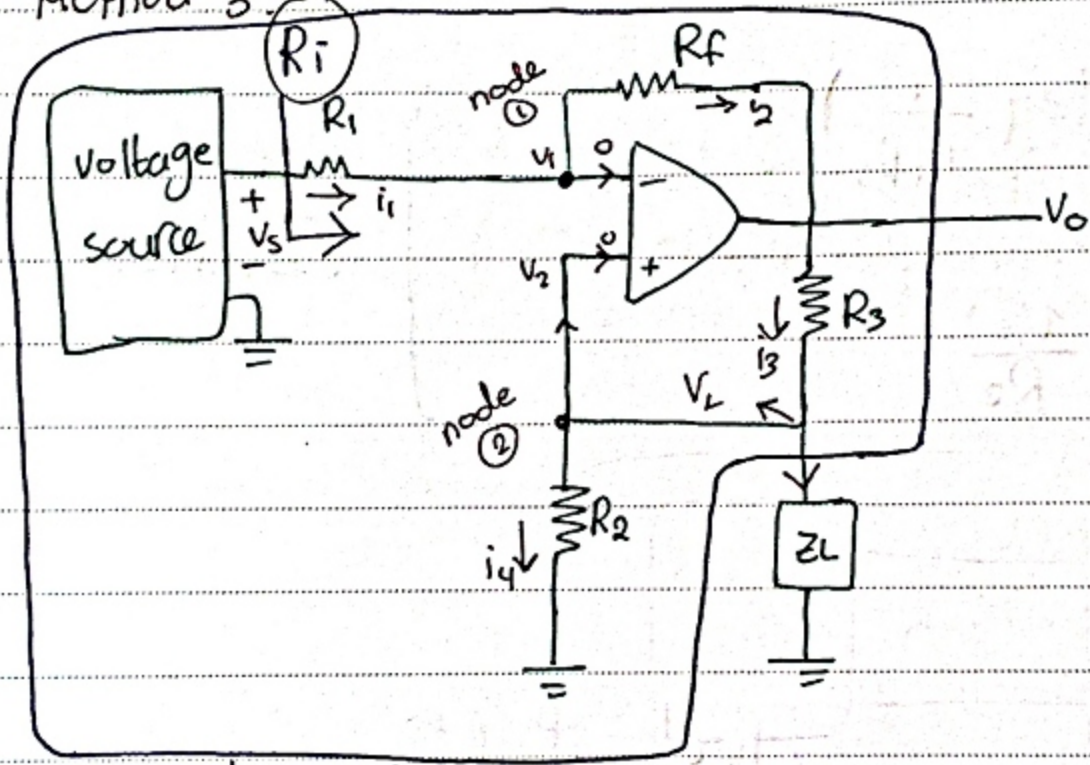


• But R_L should not be grounded



مع افتراض عتق الربط
على صفة ال i_L ؟!

Method 3:



current source

$\rightarrow v_1 = v_2 = v_L = i_L Z_L$
 $\rightarrow i_1 = i_2$ from node (1)

$$\frac{V_s - i_L Z_L}{R_1} = \frac{i_L Z_L - v_o}{R_f} \rightarrow \boxed{1}$$

(i_L صفة ال i_L بد v_L صفة ال v_L)

$\rightarrow i_3 = i_L + i_4$ from node (2)

$$\frac{v_o - i_L Z_L}{R_3} = i_L + \frac{i_L Z_L}{R_2} \rightarrow \boxed{2}$$

use [1] and [2] :-

$$i_L \left(\frac{R_f Z_L}{R_1 R_3} - 1 - \frac{Z_L}{R_2} \right) = v_s \left(\frac{R_f}{R_1 R_3} \right)$$

→ we need i_L to be independent on Z_L →

$$\frac{R_f}{R_1 R_3} = \frac{1}{R_2}$$

→ من أجل أن تكون التيار مستقل عن Z_L !

$$\left. \begin{array}{l} \rightarrow i_L = -v_s \left(\frac{R_f}{R_1 R_3} \right) \\ \text{(current fixed, independent on } Z_L) \\ \rightarrow i_L = -\frac{v_s}{R_2} \end{array} \right\} \text{Good Solution.}$$

→ Finding R_i :

$$R_i = \frac{R_1 R_2}{R_2 + Z_L}, \text{ check it !?}$$

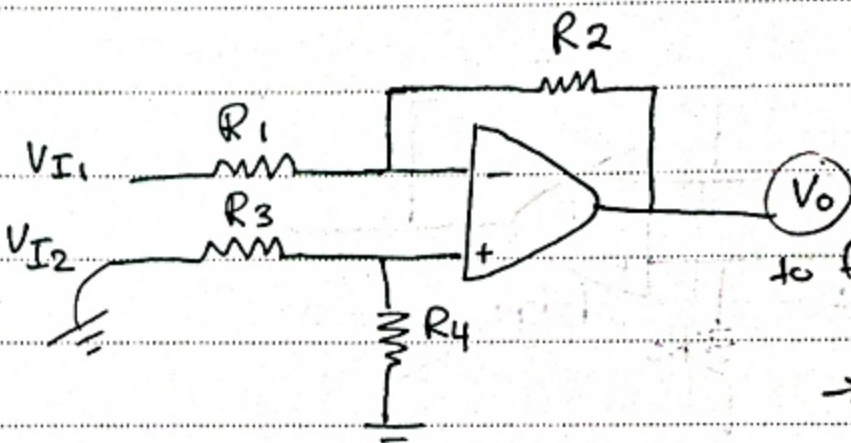
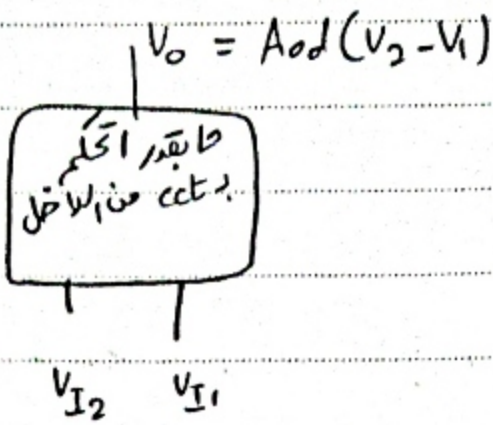
→ من شرط أن تكون
هذه القيمة cct

op-amp: $V_o = A_{od}(V_2 - V_1)$

هون بقلم بقیه ال gain

ما بقدر انا اقول
عنه ال output
ال output ال
ال output ال

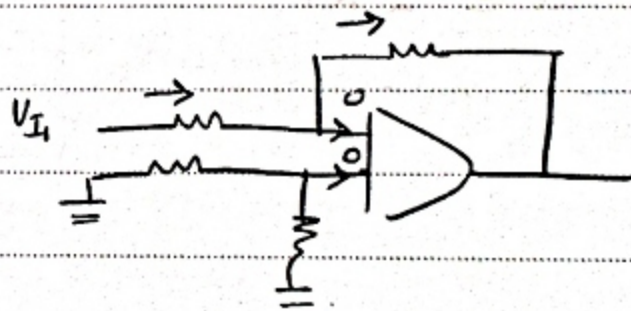
Difference Amplifier: -> to take the difference between two voltages and amplify it.



to find it with r. to V_{I1} & V_{I2}
-> using super position.

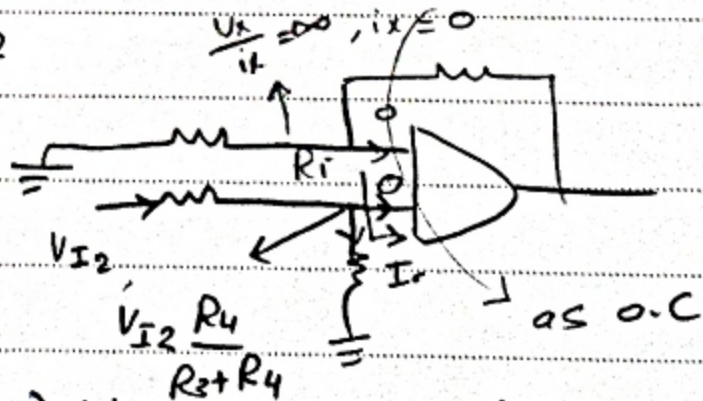
• By super position:-

$$V_o' = -\frac{R_2}{R_1} V_{I1}$$



$$V_o'' = \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_4}{R_4 + R_3}\right) V_{I2}$$

inverting - amp.



$$\rightarrow V_o = -\frac{R_2}{R_1} V_{I1} + \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_4}{R_4 + R_3}\right) V_{I2}$$

-> voltage division between R_3 & R_4

$$V_o = \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_4/R_3}{1 + R_4/R_3}\right) V_{I2} - \frac{R_2}{R_1} V_{I1}$$

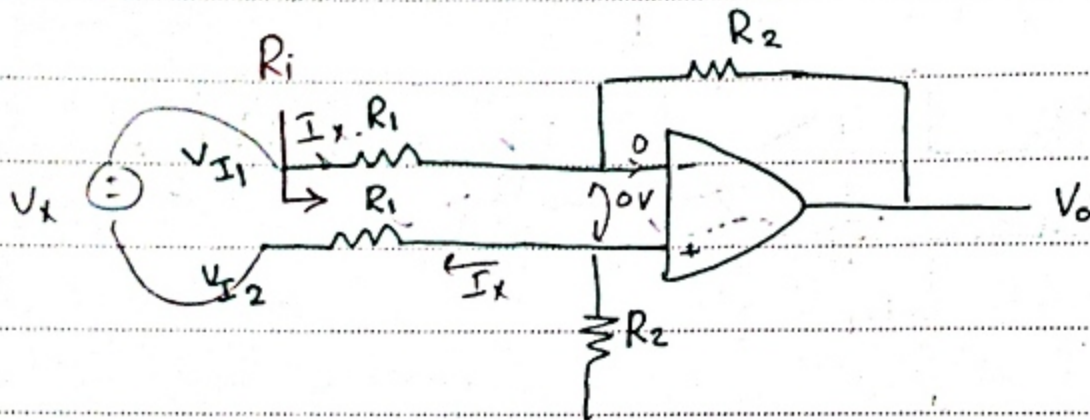
• if $V_{I1} = V_{I2}$ then V_o should be = zero

$$\text{So } \frac{R_2}{R_1} = \frac{R_4}{R_3}$$

$$= \boxed{V_o = \frac{R_2}{R_1} (V_{I2} - V_{I1})}$$

موضحة توضح
النسبة بين
Ratio

به النسبة



$$R_i = 2R_1$$

$$-V_x + R_1 I_x + R_1 I_x + 0 = 0$$

$$2R_1 = \frac{V_x}{I_x}$$

* Instrumentation Amplifier:-

we know that for difference amplifier:-

$$\bullet \text{ Gain} = \frac{R_2}{R_1}$$

$$\bullet R_i = 2R_1$$

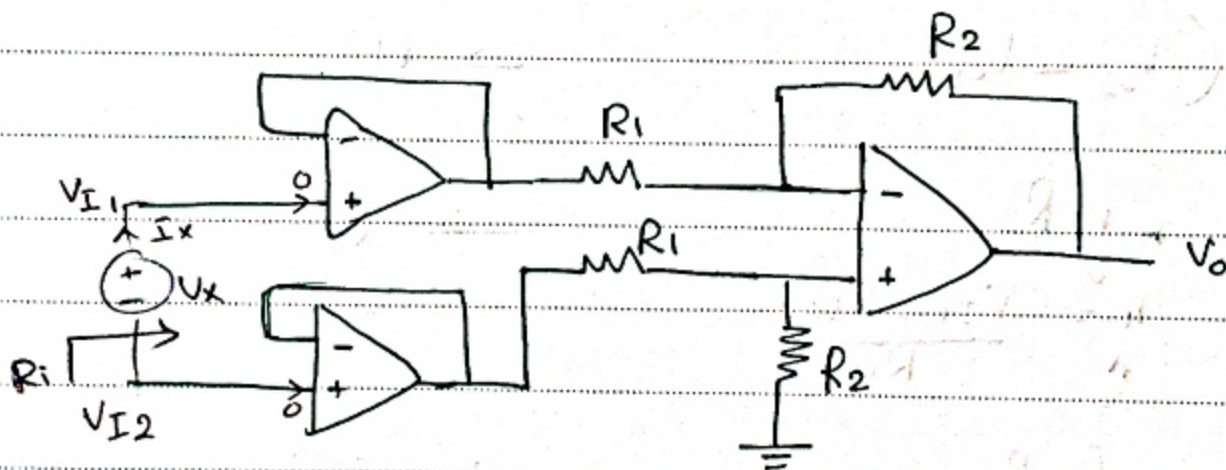
loading effect ← only R_1 on

↓ Gain

! Gain ↓ ⇔ ↑ R_1 ⇔ ↑ R_i

→ problem:- Both R_i and gain are dependent on R_1

→ solution:- ① use Buffer.



$$\Rightarrow \boxed{R_i = \infty}$$

⇒ But there is another problem!

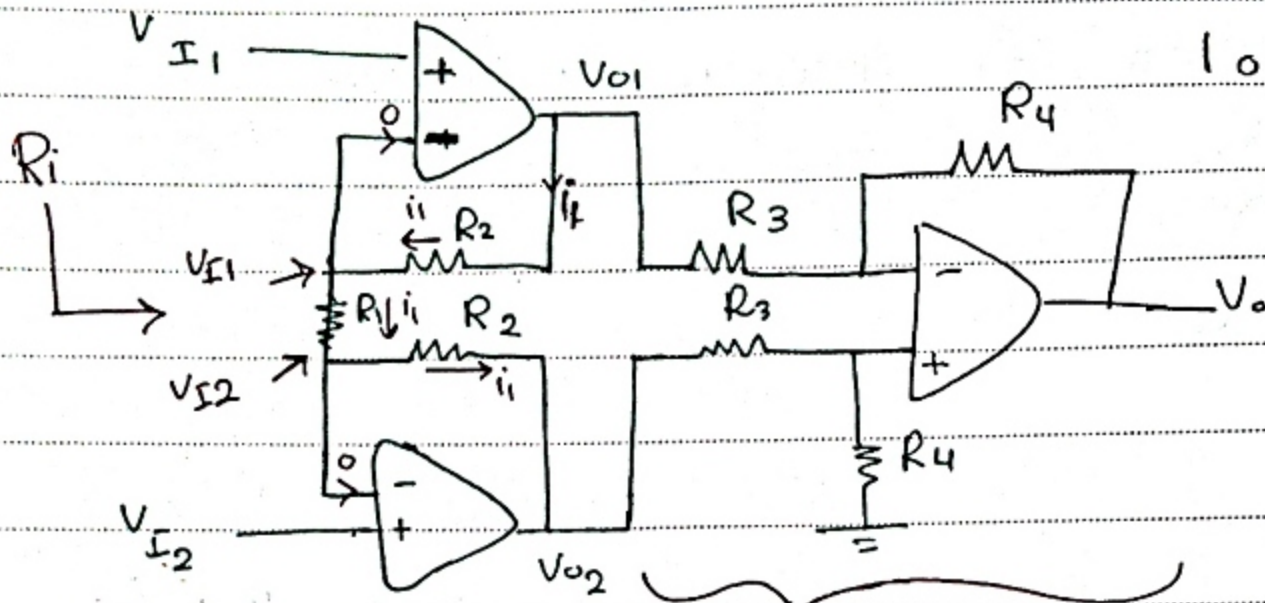
if we need to change the gain we have to change two resistor.

using potentiometer ← 2-resistor user can use

the change must be equally → This is a practical problem.

②: using Instrumentation Amplifier.

2 inputs
1 output



Difference Amp → الشرح بالخطوط

$$V_o = \frac{R_4}{R_3} (V_{o2} - V_{o1}) \rightarrow (1)$$

$$V_{o1} = V_{I1} + i_1 R_2 \rightarrow (2)$$

$$i_1 = \frac{V_{I1} - V_{I2}}{R_1}$$

$$V_{o2} = V_{I2} - i_1 R_2 \rightarrow (3)$$

use (2) and (3) in (1):-

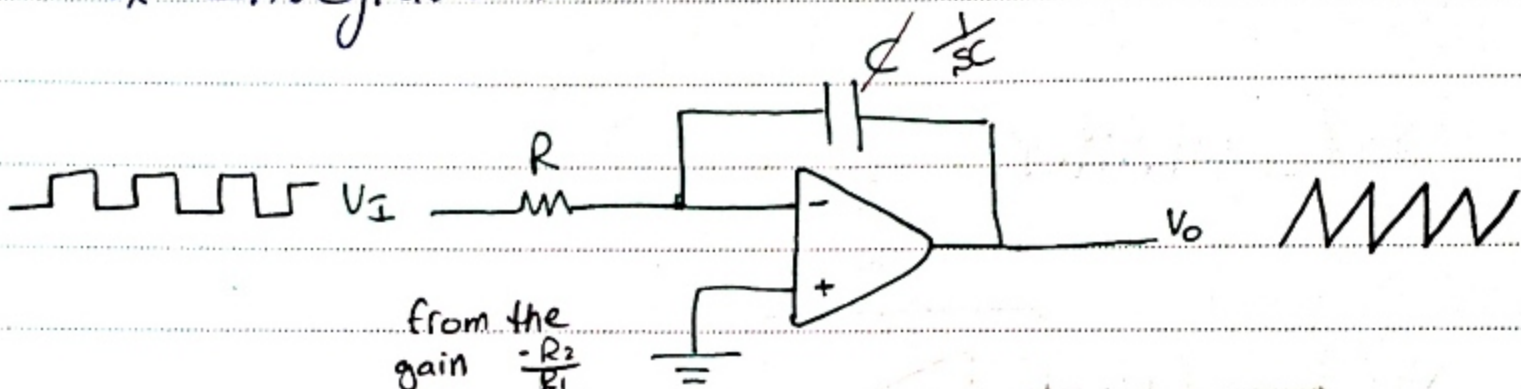
$$V_o = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_1} \right) (V_{I2} - V_{I1})$$

↑ fixed
↑ fixed
↓ fixed
↓ fixed
↑ R₁

• advantages:-

1. $R_i = \infty$
2. The gain can be changed using one resistor (R_i)

* Integrator:-



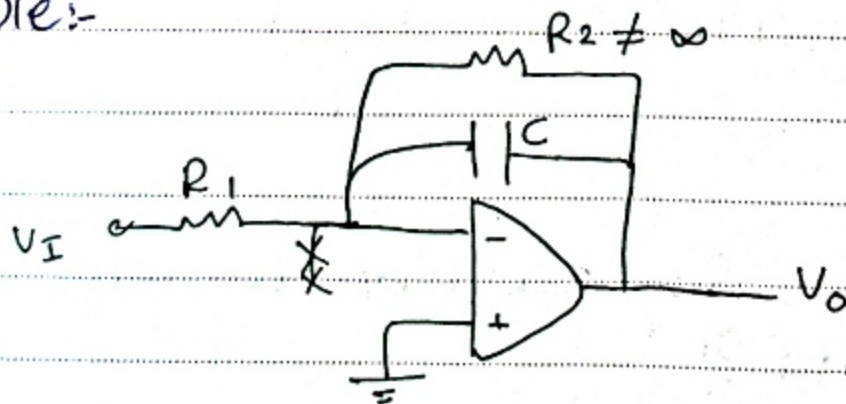
from the gain $\frac{-R_2}{R_i}$
 $R_2 \rightarrow Z_C$

$$V_O(s) = V_I(s) * \frac{-Z_C}{R} = -\frac{1}{sRC} \cdot V_I(s) \quad (\text{s-domain})$$

output = input * T.F
 T.F: Transfer function \rightarrow Gain

$$V_O(s) = V_C(0) - \frac{1}{RC} \int_0^t V_I(t') dt' \quad (\text{time-domain})$$

• Example:-



• what is the condition for making this ckt an integrator

$$V_O(s) = -\frac{R_2 \parallel \frac{1}{sC}}{R_1} V_I(s) = -\frac{R_2}{R_1} \cdot \frac{1}{1 + R_2 s C} V_I(s)$$

$$\left(-\frac{R_2}{R_1} \cdot \frac{1}{1 + R_2 s C} \right) \approx \left(-\frac{1}{sRC} \right)$$

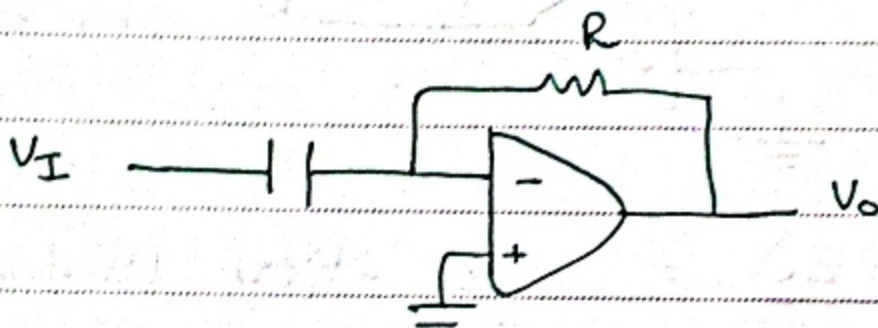
بدي 2-terms سينيوي

→ the condition: $R_2 C S \gg 1$

$$\rightarrow \frac{-R_2}{R_1} \cdot \frac{1}{R_2 C S} = \frac{-1}{R_1 C S} \neq \downarrow j2\pi f$$

⇒ this cct can be used as integrator at high frequency.

* differentiator: - $C \in R$ $j\omega C$, $R \in C$ ωR



• S-Domain: $V_O(S) = \frac{-R}{(1/SC)} V_I(S)$

$$V_O(S) = -RCS V_I(S)$$

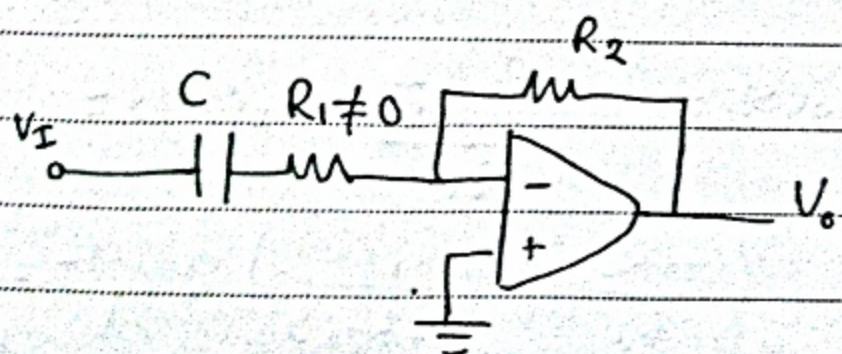
• Time-Domain: $V_O(t) = -RC \frac{dV_I(t)}{dt}$

Example:- what is the condition to make this cct a differentiator?

$$V_O = \frac{-R_2}{R_1 + \frac{1}{SC}} V_I(S)$$

$$V_O(S) = \frac{-R_2 SC}{SCR_1 + 1} V_I(S)$$

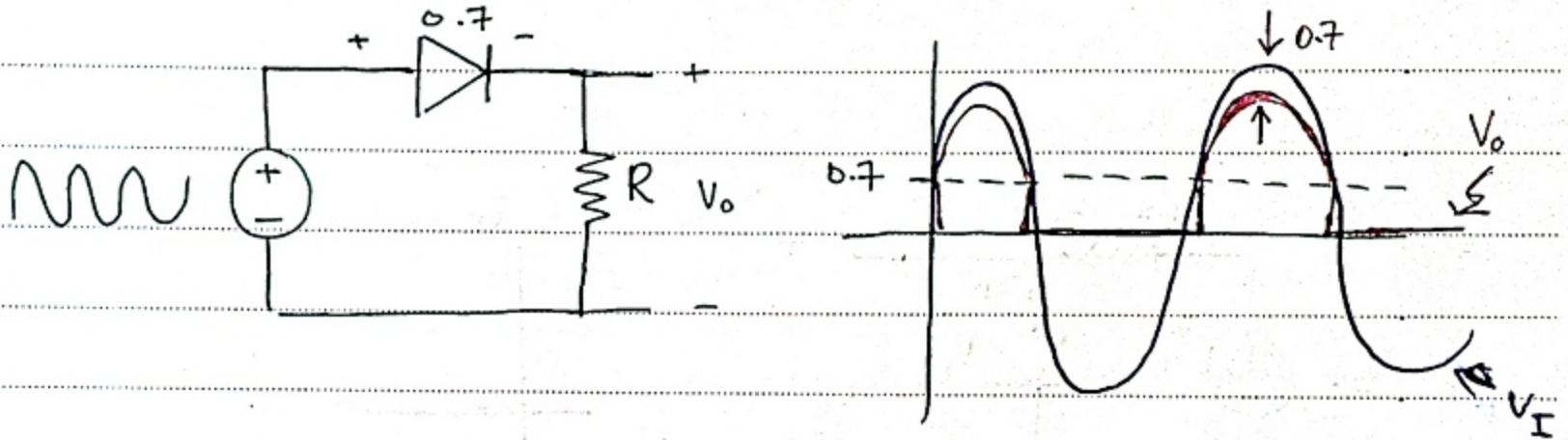
$$\rightarrow SCR_1 \ll 1$$



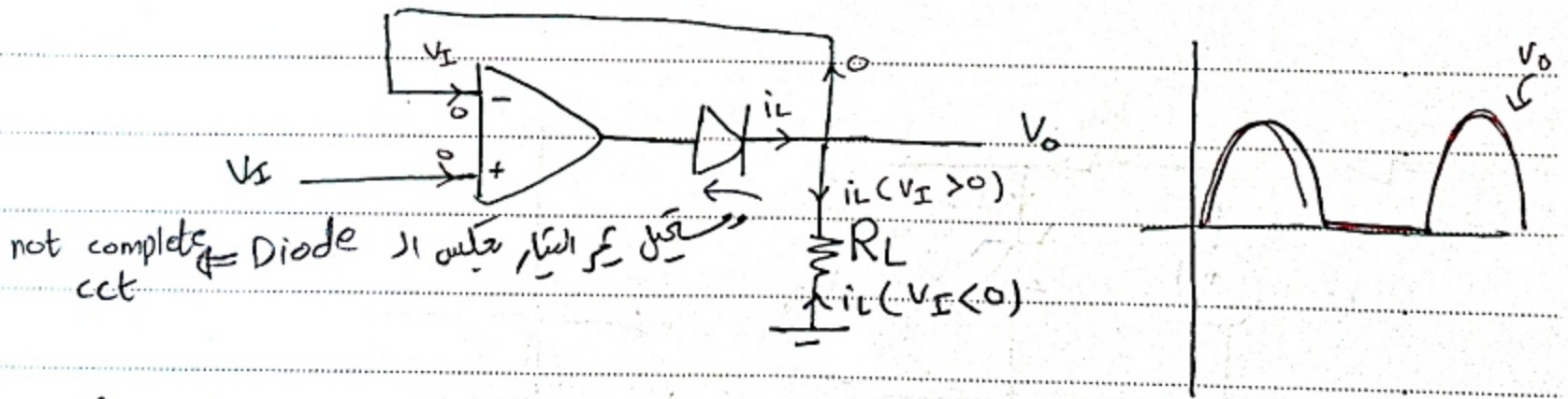
⇒ this cct can be used as differentiator at low frequency.

* Precision half-wave rectifier:-

→ we know that, the diode rectifier, the voltage should be > 0.7 ⁱⁿ



• Precision half-wave rectifier:-



not complete cct = Diode لا يخرج، التيار في اتجاه

• if $V_I > 0 \Rightarrow V_o > 0 \Rightarrow i_L \downarrow$ (Down) \Rightarrow Diode is ON
• buffer ckt

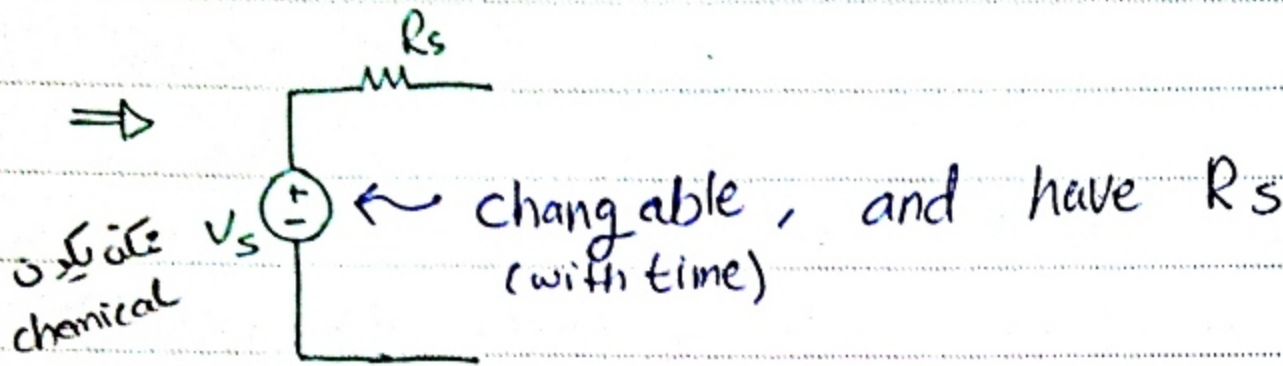
$\therefore V_o = V_I$

• if $V_I < 0 \Rightarrow V_o < 0 \Rightarrow i_L \uparrow$ (up) \Rightarrow Diode is off
• it is not

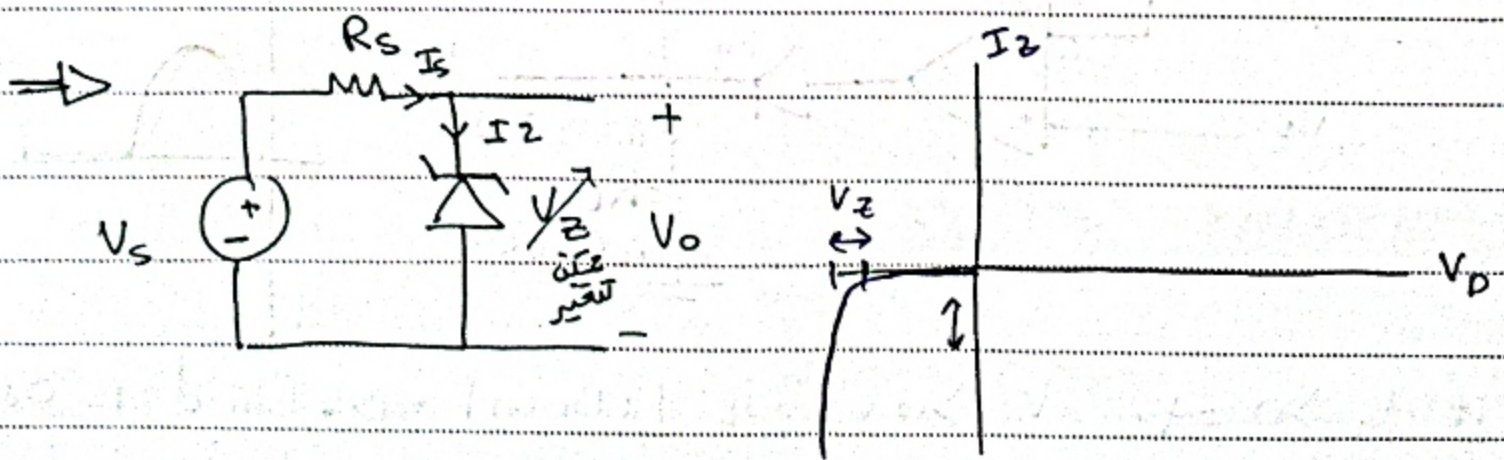
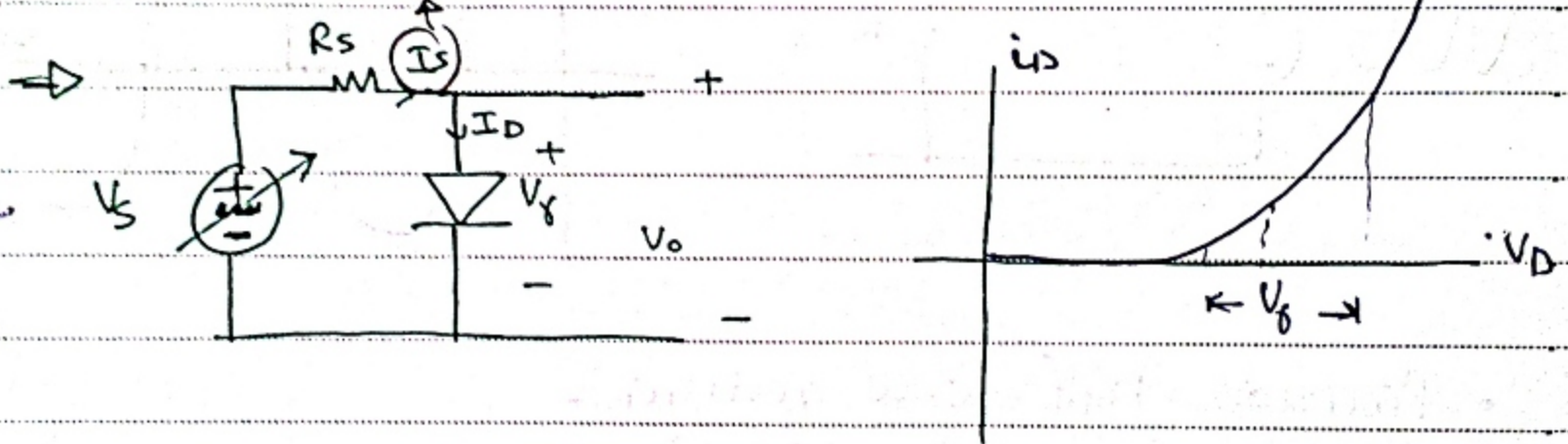
a complete ckt

$\therefore V_o = 0$

* Reference voltage source design:-



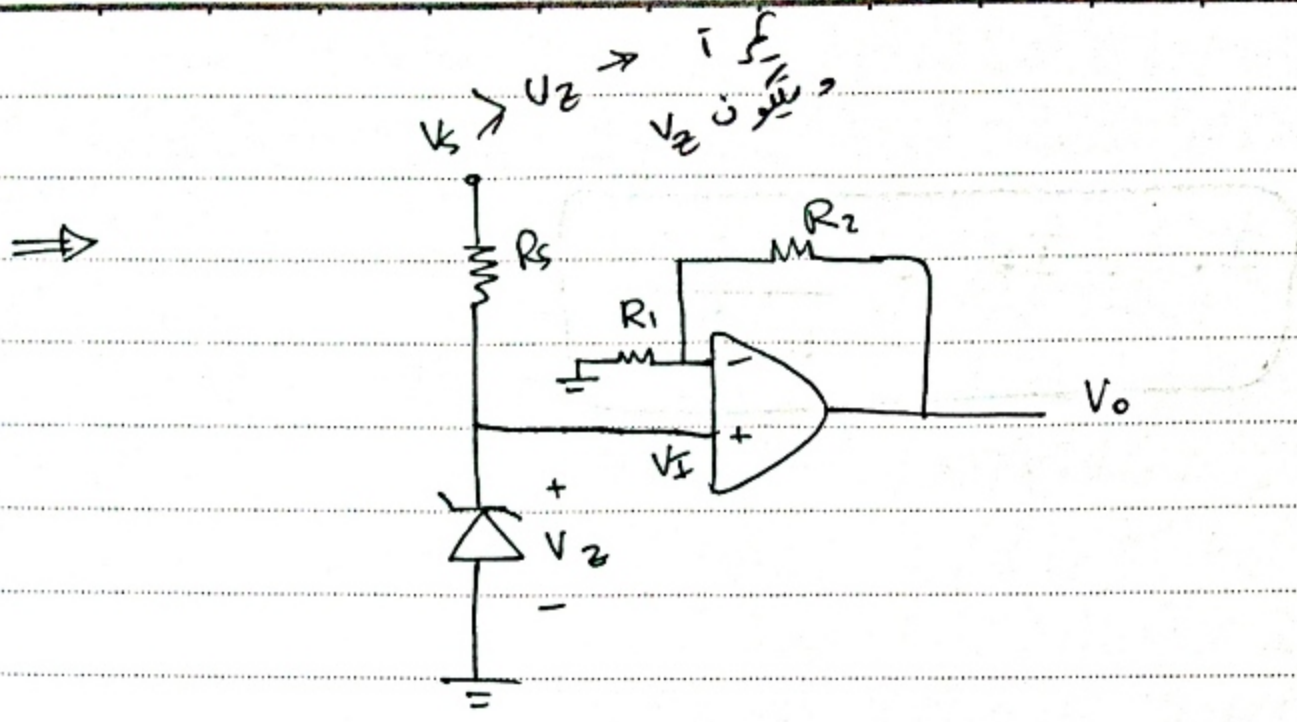
تغير V_s مع تغير I_D مع تغير V_s



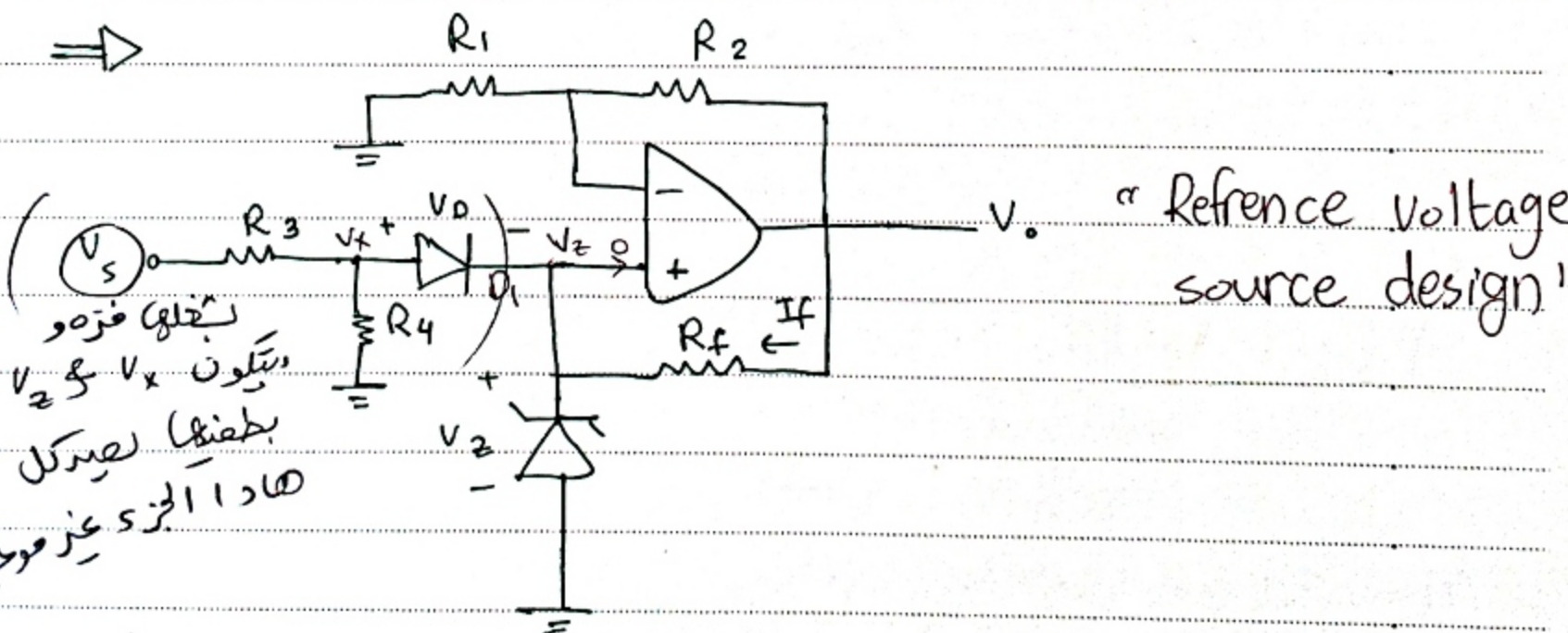
- * problems:-
- ① V_Z changes with V_s
 - ② in some cases we need a reference voltage $\neq V_Z$

$$V_s < V_z \rightarrow i_z = 0$$

15 / 5 / 2014



- if $V_s < V_z \Rightarrow V_I = V_s \rightarrow$ problem
- $V_s \gg V_z \Rightarrow V_I = V_z \rightarrow V_z$ as V_s



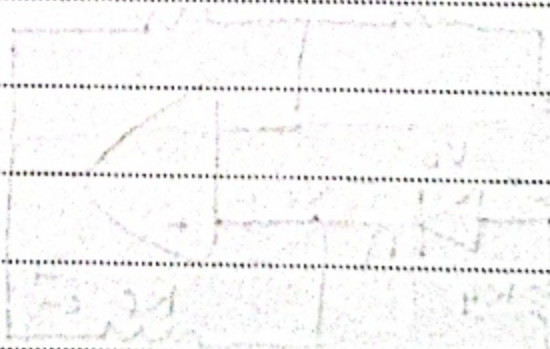
بجمله فزود
دبتون V_x و V_z
بعضه لمدرك
هاد الجزء عز مودود

"Reference voltage source design"

D_i is ON \Rightarrow if $V_x - V_z > V_f$
 $\Rightarrow V_o = V_z \left(1 + \frac{R_2}{R_1} \right)$

$$I_f = \frac{V_o - V_z}{R_f} = \frac{R_2 V_z}{R_1 R_f}$$

$$I_f = I_2 = \frac{R_2 V_2}{R_1 R_f}$$



* feedback and stability:-

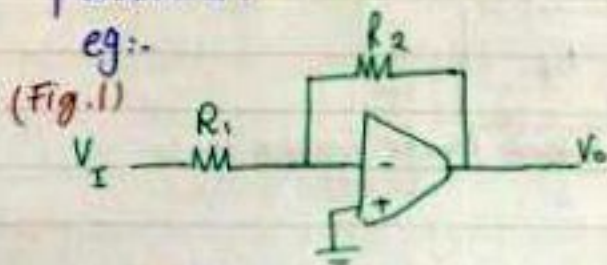
- Type: 1. Positive feedback
2. negative feedback. (*)

• negative feedback:-

Advantage:-

1. stable gain: the gain is independent on transistor parameter.

eg:-



$$\text{Gain} = -\frac{R_2}{R_1}$$

* gain without feedback = A_{od}

2. increases the bandwidth.

3. increases signal to noise ratio.

noise is less

signal power

$$\left(\frac{S}{N}\right) \uparrow \text{increase}$$

noise power

Good

4. reduction of non-linear distortion.

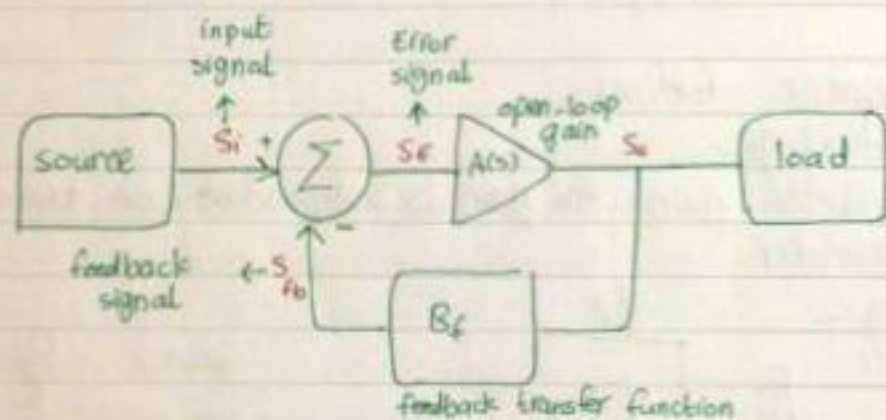
↳ due to large signal → there's non-linear device or large signal to Amp

5. control of input and output impedance level

eg:- in (Fig 1) $Z_i = R_1$

• Disadvantages:-

1. reducing the gain.
2. the ckt may become unstable (oscillate) at high frequencies.



$$S_o = A S_e$$

$$S_{fb} = S_o B_f$$

$$S_e = S_i - S_{fb}$$

$$\therefore S_o = A (S_i - S_o B_f)$$

$$A_f = \frac{S_o}{S_i} = \frac{A}{1+BA} \rightarrow \begin{array}{l} \text{the gain} \\ \text{with feedback} \end{array} \quad \begin{array}{l} \text{the gain} \\ \text{without} \\ \text{feedback.} \end{array}$$

$$A_f = \frac{A}{1+BA}$$

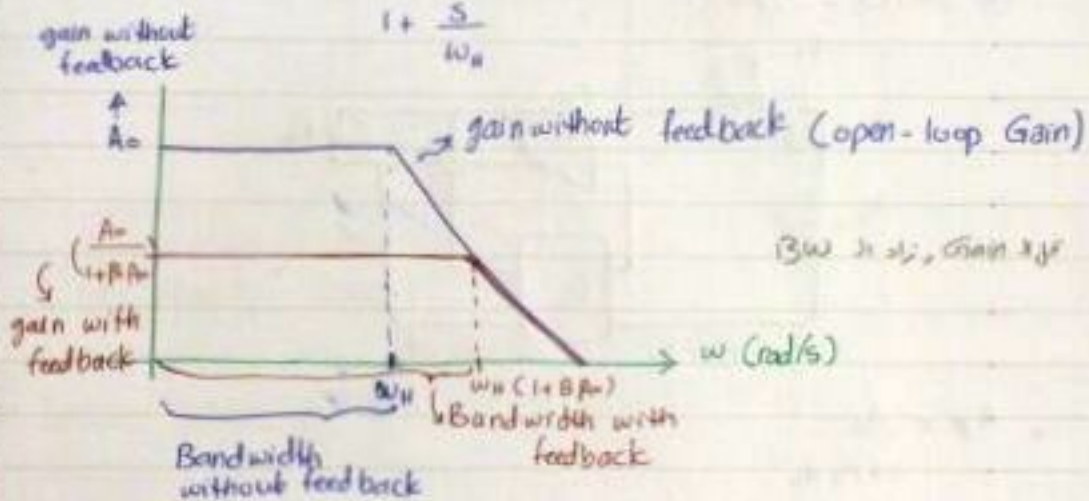
• $A_f < A$ (Disadvantage)

usually $BA \gg 1 \Rightarrow A_f = \frac{1}{B_f} \rightarrow \begin{array}{l} \text{depends on feedback} \\ \text{independent on} \\ \text{op-amp parameter} \end{array}$

↓
stable gain

→ Bandwidth extension:-

$$\text{let } A(s) = \frac{A_0}{1 + \frac{s}{\omega_H}}$$



$$A_f(s) = \frac{A(s)}{1 + BA(s)}$$

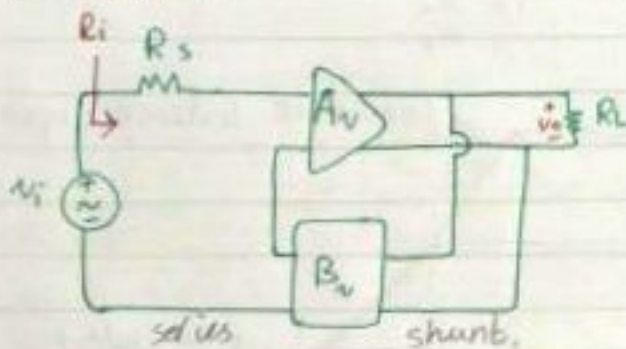
$$A_f(s) = \frac{A_0 / (1 + \frac{s}{\omega_H})}{1 + BA_0 / (1 + \frac{s}{\omega_H})}$$

$$A_f(s) = \left(\frac{A_0}{1 + BA_0} \right) \frac{1}{1 + \frac{s}{\omega_H (1 + BA_0)}}$$

• Gain \downarrow x Bandwidth \uparrow = constant

* Basic feedback configurations:-

(a) series-shunt: ^{as parallel}



$$A_f = \frac{A_v}{1 + B_v A_v}$$

$$R_{if} = R_i (1 + B_v A_v), \quad R_{if}: R \text{ input with feedback}$$

$$R_{of} = \frac{R_o}{1 + B_v A_v}$$

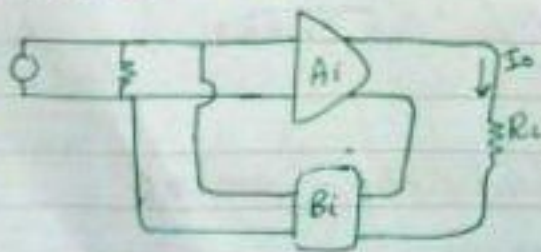
R_i : R input without feedback

$(1 + B_v A_v)$ → β (feedback factor) $\leftarrow R_i$ \leftarrow R_o

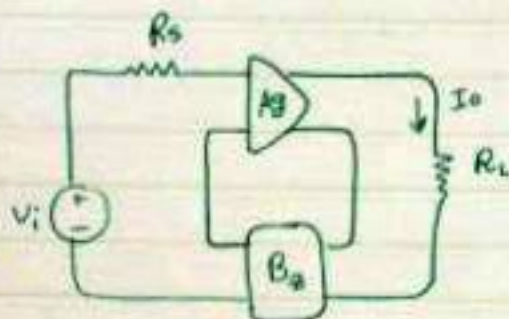
$\leftarrow R_o$

$\leftarrow A$

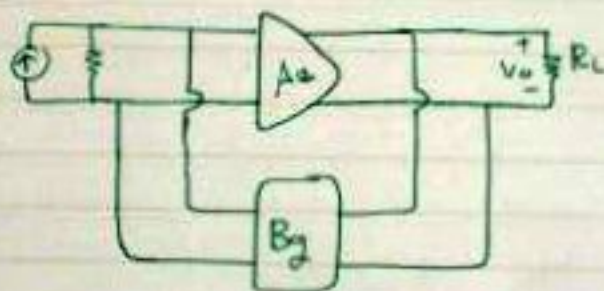
(b) shunt-series:



(c) series-series:-



(d) shunt-shunt:-



• Miller effect of Mosfet \rightarrow $C_M = ?$ v_{ds}