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3

$\phi = \sqrt{Z}$

Q	Mark
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2	13/13
3	6/18
4	4/16
35/60	

University of Jordan
Electrical Eng. Dept

EE 0933481 Power Systems (1)

Second Exam.
17-4-2016

الاسم: [Redacted] رقم التفقد (6) الرقم الجامعي: [Redacted]

Q1) a-The series impedance of the equivalent circuit of a long transmission line has a value of $Z = 187/79^\circ \Omega$. If the product of line's length and propagation constant equal $0.5/85^\circ$, evaluate the characteristic impedance of the line. [8]

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7/8 = 0.878 $\angle 1.25^\circ$

$\delta l = 0.5 \angle 85^\circ$

$A = D = \cos(\delta l) = \frac{1}{2} (e^{\delta l} + e^{-\delta l})$

$e^{\delta l} = e^{0.013 j 0.5} = 1.04 \angle 28.6^\circ$
 $e^{-\delta l} = 0.96 \angle -28.6^\circ$

$\delta l = \sqrt{ZY} = 0.5 \angle 85^\circ = 0.5 e^{j 85^\circ} \Rightarrow ZY = 0.25 \angle 170^\circ$

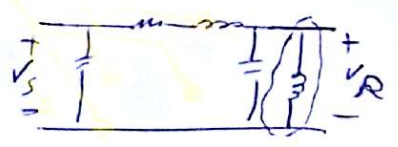
$\Rightarrow Y = 1.33 m \angle 91^\circ$

$B = Z_c \sinh(\delta l); Z_c = 374.9 \angle -6^\circ; B = 180 \angle 79.8^\circ$

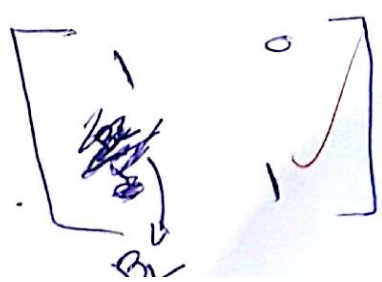
$C = \frac{1}{Z_c} \sinh(\delta l) = 1.28 \times 10^{-3} \angle 91.8^\circ$

b-Evaluate the parameter matrix of a compensation network with 80% compensation factor located at the end of a lightly loaded transmission line which has series impedance of $180/75^\circ \Omega$ and shunt admittance of $j 0.0012 S$. [5]

$0.8 = \frac{B_L}{B_C}, B_C = j 0.0012 S$



$B_L = -j 9.6 \times 10^{-4} S$



$Z = \frac{X}{2}$

$$V_1 = V_f \left(1 - \frac{Z_{13}}{Z_{33}} \right)$$

Q2) A power system has 4 buses. For a balanced 3-ph at bus 3, the pu fault current was $5.118 \angle -90^\circ$ and the voltages at busbars 1, 2 and 4 were 0.209, 0.235 and 0.465 respectively all in pu.

a-Evaluate ΔV_1

[5]

$$I_f'' = \frac{V_f}{Z_{33}} \Rightarrow Z_{33} = 0.195 \angle 90^\circ$$

$$I_f'' = \frac{V_f}{Z_{33}} \Rightarrow V_f = 1 \angle 0^\circ$$

$$\Delta V_1 = -V_f \frac{Z_{13}}{Z_{33}} \Rightarrow -0.7897$$

$$V_1 = V_f \left(1 - \frac{Z_{13}}{Z_{33}} \right) \Rightarrow \frac{Z_{13}}{Z_{33}} = +0.791 = + \frac{Z_{13}}{Z_{33}} \Rightarrow Z_{13} = 0.154 \angle 90^\circ$$

b-If the line between buses 3 and 4 has an impedance equal Numerically to the element Z_{43} in the Z_{bus} matrix, evaluate the current I_{34} .

[8]

$$V_4 = V_f \left(1 - \frac{Z_{43}}{Z_{33}} \right) \Rightarrow \frac{Z_{43}}{Z_{33}} = +0.535 = + \frac{Z_{43}}{0.195 \angle 90^\circ}$$

$$Z_{43} = 0.104 \angle 90^\circ$$

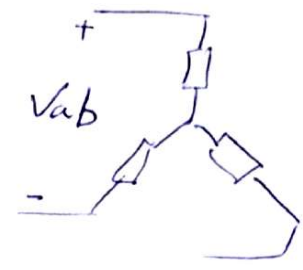
$$I_{34} = \frac{V_3 - V_4}{Z_{43}} = \frac{0 - 0.465}{0.104 \angle 90^\circ} = 4.47 \angle 90^\circ$$

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Q3)a- Prove that for a Y-connected system, its line voltages have NO Zero sequence components. [5]

~~$V_{ab} + V_{bc} + V_{ca}$~~

~~$(V_{ab}^0 + V_{ab}^1 + V_{ab}^2) + (V_{bc}^0 + V_{bc}^1 + V_{bc}^2) + (V_{ca}^0 + V_{ca}^1 + V_{ca}^2)$~~



$\begin{bmatrix} V_{ab} \\ V_{bc} \\ V_{ca} \end{bmatrix} = A \begin{bmatrix} V_{ab}^0 \\ V_{ab}^1 \\ V_{ab}^2 \end{bmatrix}$

$\rightarrow I_a^0 = 0$

b-A balanced Y-connected load with isolated neutral has a pu impedance of $1/20^\circ$ per phase. If its pu voltages are given as:

$V_{ab}^{(1)} = 0.98/75^\circ$ $V_{ab}^{(2)} = 0.23/220^\circ$

Use the concept of symmetrical components to evaluate the complex power supplied to load. [13]

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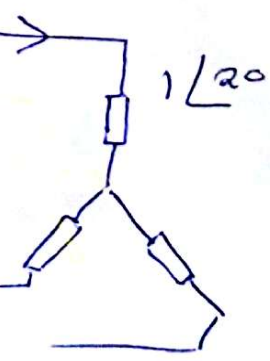
$S = (V_a^0 I_a^{0*} + V_a^1 I_a^{1*} + V_a^2 I_a^{2*})$

$V_{ab}^1 = \sqrt{3} \angle -30^\circ V_{an}^1 \Rightarrow V_{an}^1 = 0.56 \angle 105^\circ$

$V_{ab}^2 = \sqrt{3} \angle 30^\circ V_{an}^2 \Rightarrow V_{an}^2 = 0.133 \angle -170^\circ$

$I_a^1 = \frac{0.56 \angle 105^\circ}{1 \angle 20^\circ} = 0.56 \angle 85^\circ$

$I_a^2 = \frac{0.133 \angle -170^\circ}{1 \angle 20^\circ} = 0.133 \angle 170^\circ$



$S \equiv 0.331 \text{ Pu} \angle 11^\circ$

Q4) Fig. 1 shows the pu zero sequence network of a given power system, Where between each indicated 2 points there is one component.

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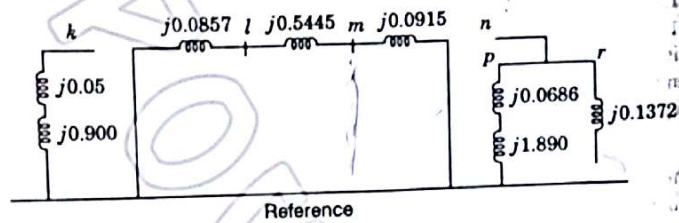
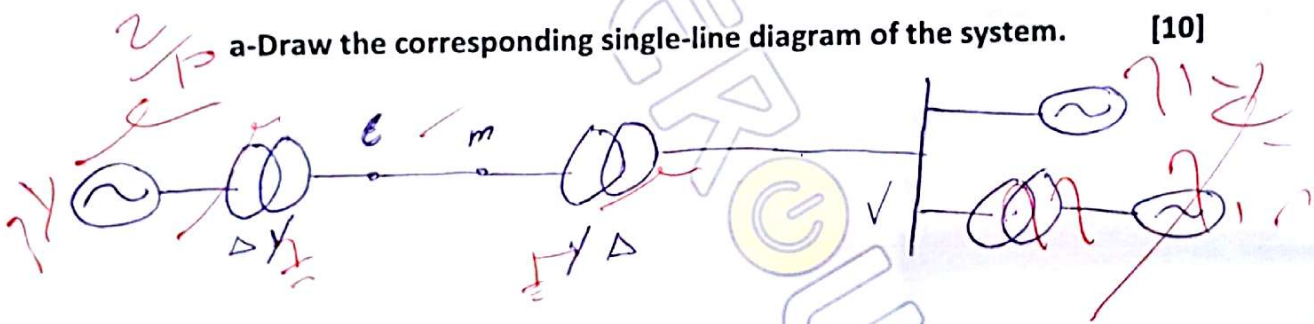


Fig. 1

a-Draw the corresponding single-line diagram of the system. [10]



b-If for a fault at point m, $I^{(0)} = 0.5 \angle 30^\circ$ PU, evaluate $V^{(0)}$. [6]

Handwritten solution for part b:

$I^0 = I^1 = I^2 = 0.5 \angle 30^\circ$

$V_\theta^0 = -I^0 Z_0$

$V^0 = 0.27225 \angle 120^\circ$

$Z_0 = j0.5445$