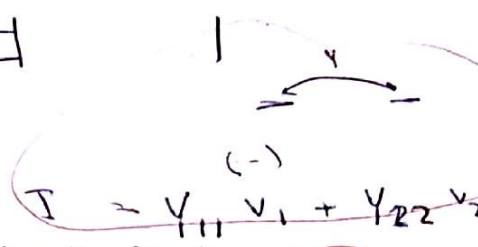


$$V_R = AV_f + BI_f$$

$$I_R = \frac{C V_f + D I_f}{A V_f + B I_f}$$



University of Jordan  
Electrical Eng. Dept

13/22

Q	Mark
1	3 / 19
2	4 / 16
3	7 / 15
4	17 / 20
5	8 / 10
Total	39 / 60

EE 0933481 Power Systems (1)

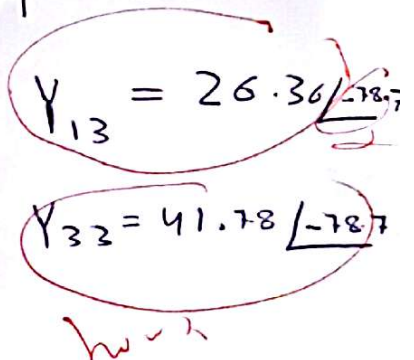
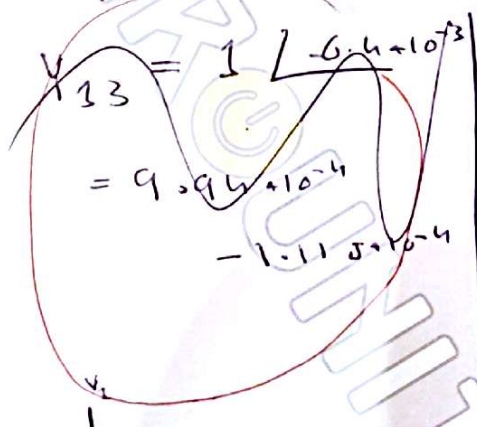
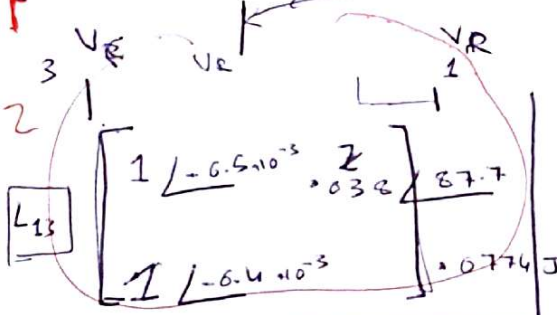
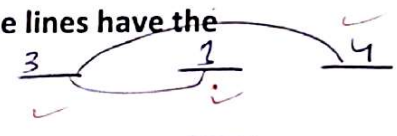
Firs Exam.  
8-11-2015

الاسم: [redacted] رقم التفقد: (17) الرقم الجامعي: [redacted]

Q1) A 4 busbar system has busbar number 3 connected to busbars 1 and 4 by means of medium length transmission lines. The lines have the following total Z (Ω) and Y(S):

Line 3-1: Z=0.0074+j 0.0372 , Y=j0.0775  
Line 3-4: Z=0.0127+j 0.0636 , Y=j0.1275

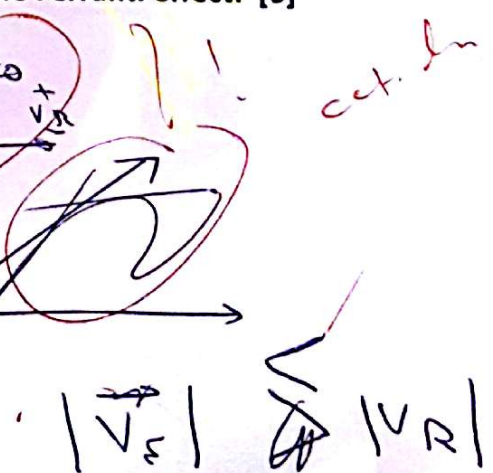
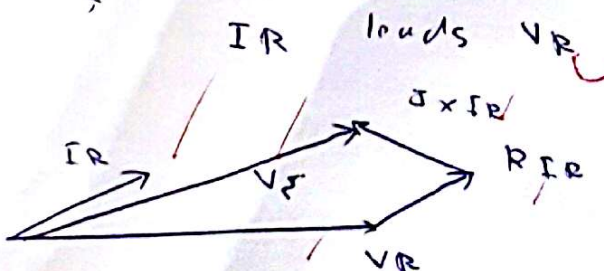
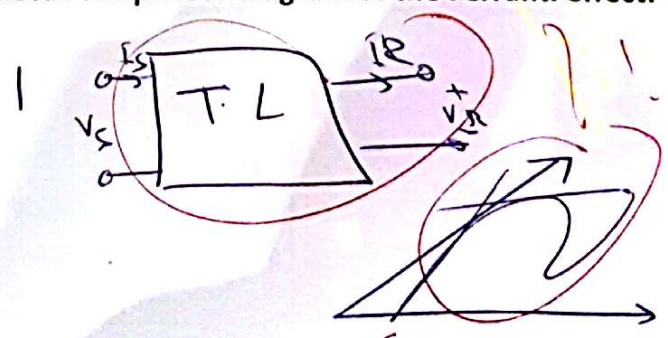
Evaluate the elements Y<sub>13</sub> and Y<sub>33</sub> in the Bus Admittance Matrix of this system. [9].



$$V_f = AV_R + BI_R$$

$$I_f = CV_R + DI_R$$

Q2) By drawing the electrical circuit showing on it all necessary voltages and currents, sketch the phasor diagram of the Ferranti effect. [6]



Q3) The components of the power system shown in Fig. 1, has the following reactance in pu referred to the same base:

Component:	$G_1$	$G_2$	$T_1$	$T_2$	TL12	TL13	TL23
Reactance :	0.2	0.2	0.05	0.05	0.1	0.1	0.1

a- If the transmission lines of short length, draw the detailed pu reactance diagram of the system by assuming positive phase sequence. [6]

b- If the current into busbar 5 is  $0.9 \angle -120^\circ$  pu and the voltage at busbar 5 is  $0.8 \angle -30^\circ$ , then by using (a) above evaluate the current into busbar 2 and the voltage at busbar 2. [9]

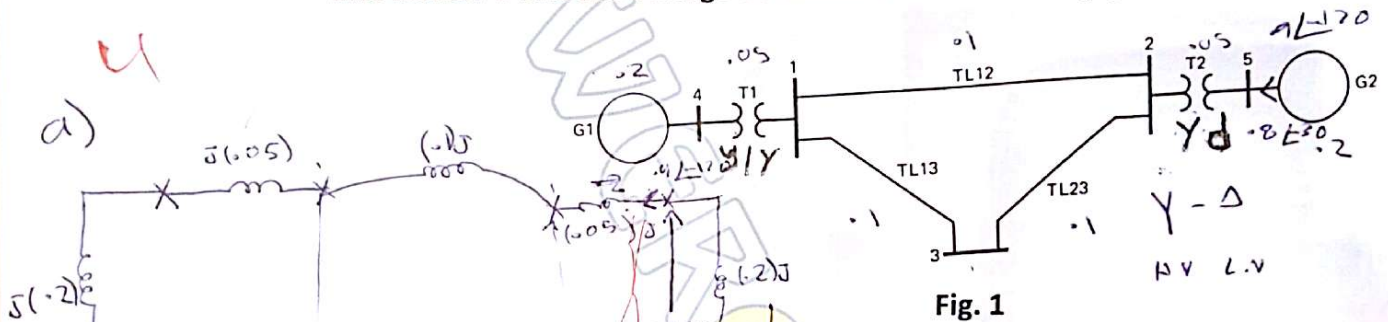
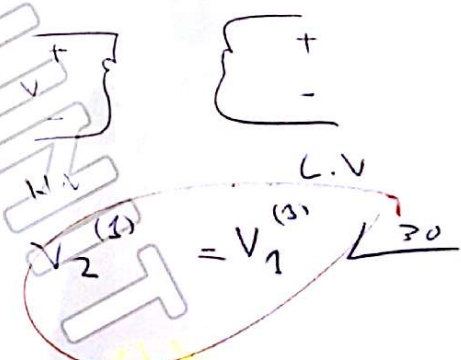
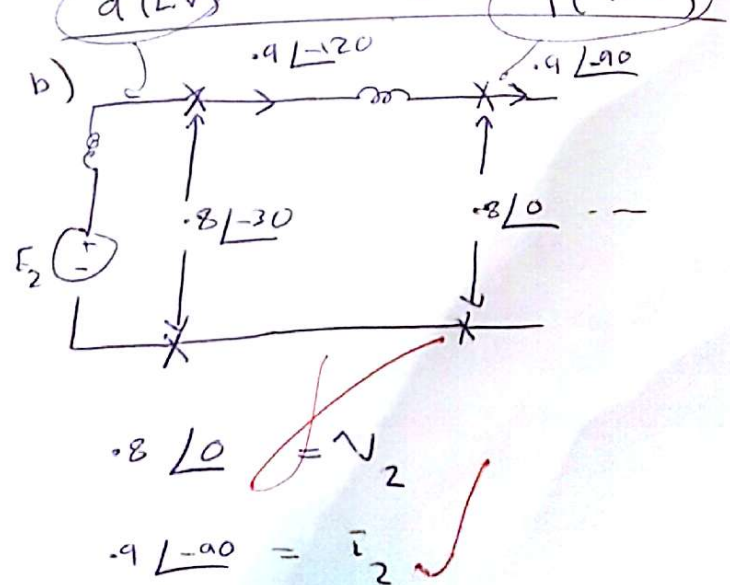
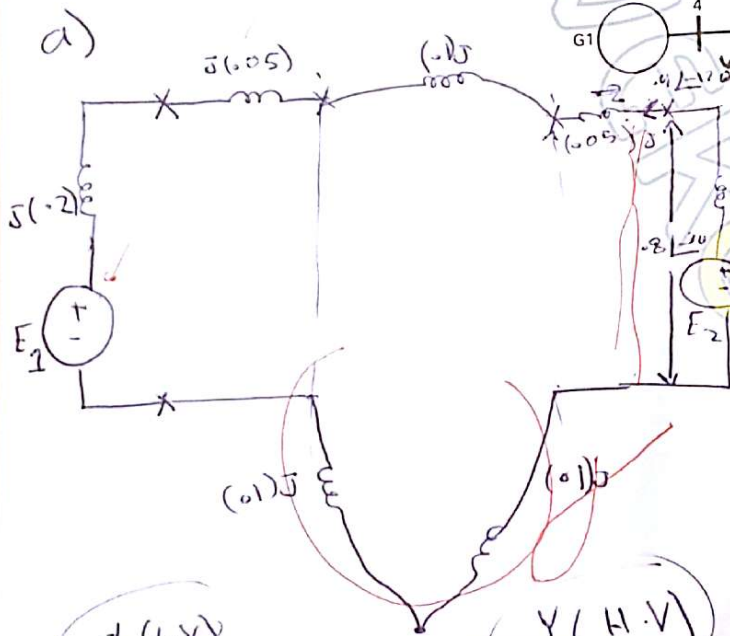


Fig. 1



1 → 100  
..

$$\begin{matrix} \cosh \delta L & Z_c \sinh \delta L \\ \frac{1}{Z_c} \sinh \delta L & \cosh \delta L \end{matrix}$$

Long  
Q4) A 50 Hz, 300 km transmission line has its phase conductors equally spaced with distance between centers = 1.5 m. The line has the following data:

$D_s = 0.387$  cm, radius of conductor = 0.8 cm,  $R = 0.237 \Omega/\text{km}$ .

Given  $\epsilon = 8.85 \times 10^{-12}$ , evaluate the A constant of this line. [20]

$\cosh \delta L$

a) Find L:  $2 \times 10^{-7} \ln \left( \frac{D}{D_s} \right)$

$$= 2 \times 10^{-7} \cdot \ln \left( \frac{1.5}{0.387} \right)$$

$$L = 7.3 \times 10^{-7} \text{ H/m}$$

b) Find C:  $\frac{2\pi\epsilon}{\ln \left( \frac{D}{r} \right)}$

$$= \frac{2\pi \cdot 8.85 \times 10^{-12}}{\ln \left( \frac{1.5}{0.8} \right)}$$

$$C = 1.9 \times 10^{-11} \text{ F/m}$$

c)  $X = \omega L$

$$= j2\pi \cdot 50 \cdot 7.3 \times 10^{-7}$$

$$X = 2.3 \times 10^{-4} j \Omega/\text{km}$$

$$Y = j\omega C = j(2\pi \cdot 50 \cdot 1.9 \times 10^{-11})$$

$$= 5.9 \times 10^{-9} j \Omega/\text{km}$$

$$Z_{\text{tot}} = (237 + j69) \Omega$$

$$Y_{\text{tot}} = (1.77 - j10^{-3}) \Omega$$

$$\delta L = \sqrt{(ZC)L}$$

$$\Rightarrow \delta L = \sqrt{(237 + j69) + (1.77 - j10^{-3})}$$

$$= \sqrt{.43691 / 106.2}$$

$$= .660992 / 53.1$$

$$A = \cosh \delta L$$

$$= \frac{e^{\delta L} + e^{-\delta L}}{2}$$

$$e^{\delta L} = .660992 / 53.1$$

$$= e^{-.39687} \cdot e^{-.52858j}$$

$$\Rightarrow 1.487 / 30.3$$

$$e^{-\delta L} = .67242 / -30.3$$

$$A = \frac{1.487 / 30.3 + .67242 / -30.3}{2} = \sqrt{.954596 / 12.431}$$

$$V_F = A V_R + B I_R \Rightarrow \frac{V_F}{B} - \frac{A V_R}{B} = I_R$$

$$\frac{V_F}{B} \angle \beta - \frac{A V_R}{B} \angle \alpha = I_R \angle \gamma$$

Q5) For the transmission line whose equivalent circuit is shown in Fig. 2, if  $V_S = 138 \angle 28^\circ$  kV and  $V_R = 125 \angle 0^\circ$  kV, evaluate:  
 a-the maximum power it can deliver [7]  
 b-Its voltage regulation. [3]

$$\begin{bmatrix} V_R \\ I_R \end{bmatrix} = \begin{bmatrix} 1 + \frac{ZY}{2} & Z \\ Y + \frac{ZY^2}{4} & 1 + \frac{ZY}{2} \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

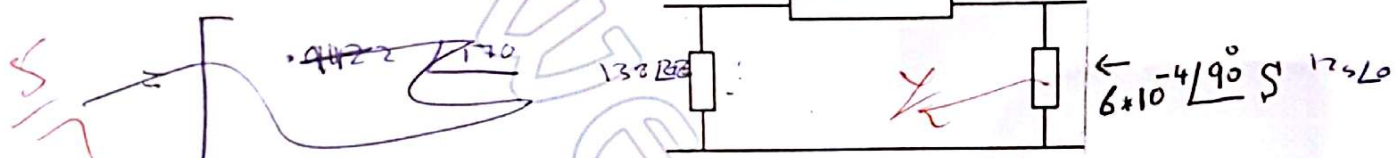


FIG.2

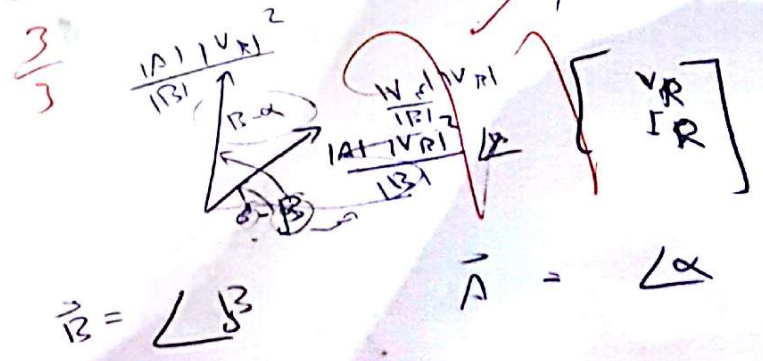
$$1 + \frac{187 \angle 80^\circ + (6 + j10)}{2}$$

$$A \approx D = 0.9448 \angle 0.59$$

$$C = 5.83 \times 10^{-4} \angle 90.3$$

$$B = 187 \angle 80$$

$$\begin{bmatrix} V_F \\ I_F \end{bmatrix} = \begin{bmatrix} 0.9448 \angle 0.59 & 187 \angle 80 \\ 5.83 \times 10^{-4} \angle 90.3 & 0.9448 \angle 0.59 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$



$$\frac{|V_F| |V_R|}{|B|} = \frac{|A| |V_R|^2}{|B| \cos(\beta - \alpha)}$$

$$\frac{138 \times 125}{187} = \frac{0.9448 \times 125^2}{187 \cos(80 - 0.59)}$$

$$P_{max} = 77.7377 \text{ MW}$$

$$\text{VR} = \frac{|V_{Rnl}| - |V_{RFI}|}{|V_{RFI}|}$$

$$V_{Rnl} = \frac{|V_F|}{|A|} = \frac{138}{0.9448} = 146.06$$

$$V_{RFI} = 125$$

$$VR = \left( \frac{146.06 - 125}{125} \right) \times 100 = 16.843\%$$