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25/5  
31.3/15  
4/13/15

$\frac{56}{60} = \frac{28}{3}$

University of Jordan  
Electrical Eng. Dept

EE 0933481 Power Systems (1)

2nd Exam.  
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الرقم الجامعي: 0129244

اسم: بتول سليمان محمد الدردسي  
رقم التفتد: 38

الاسم: بتول الدردسي

Q1) a-A 25 MVA, 13.8 kV 3-ph generator with  $X''=15\%$  is connected through a 3-ph transformer rated at 25 MVA, 13.8/6.9 kV,  $X=10\%$  to a busbar which supplies two identical 3-ph motors, where each motor is rated at 5 MVA, 6.9 kV and  $X''=20\%$ . The motors are drawing rated power at 0.8 pf lagging when a balanced 3-ph fault occur at the busbar of the motors. By using thevenin's Theorem evaluate the contribution of the generator and motors (taking into account the load) to fault current and using Base Quantities of 25 MVA and 13.8 kV. [15]

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$G \circ 0.15 \times \frac{25}{25} \times \frac{(13.8)}{(13.8)^2} = 0.15$

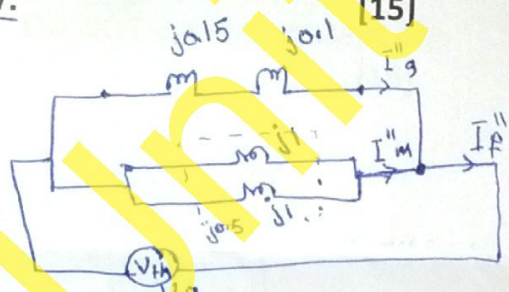
$T \circ x = 0.1 \quad | \quad M \circ x = 0.2 \times \frac{25}{5} = j1$

$Z_{th} = j \frac{0.25 \times 0.5}{0.25 + 0.5} = j0.167$

$I''_f = \frac{V_{th}}{Z_{th}} = \frac{120}{j0.167} = -j6 \text{ p.u.}$

$I''_g = -j6 \times \frac{j0.5}{j0.5 + j0.25} = -j4 \text{ p.u.}$

$I''_m = -j6 \times \frac{j0.25}{j0.5 + j0.25} = -j2 \text{ p.u.}$



$I_L = I_{m1} + I_{m2} = 2 \times \frac{25}{\sqrt{3} \times 6.9} = 86.87$

$= \frac{10}{\sqrt{3} \times 8.9} \times \frac{25}{\sqrt{3} \times 6.9} = 0.4 \angle -36.87 \text{ p.u.}$

$I''_g = -j4 + 0.4 \angle -36.87 = 4.25 \angle -85.7 \text{ p.u.} = 4.415 \angle -85.7 \text{ KA}$

$I''_m = -j2 + 0.4 \angle -36.87 = 1.79 \angle -100.3 \text{ p.u.} = 3.74 \angle -100.3 \text{ KA}$

b-When a balanced 3-ph fault occur on busbar number 2 of a 4-bus system, the fault current and the bus voltages during the fault were as follows:  $I''_f = -j4.357$ ,  $V_1 = 0.156$ ,  $V_3 = 0.349$ ,  $V_4 = 0.344$ .

Evaluate the corresponding column of the  $Z_{bus}$  matrix.

[10]

$I''_f = \frac{V_p}{Z_{22}}$

$-j4.357 = \frac{120}{Z_{22}}$

$\Rightarrow Z_{22} = j0.2295 \text{ p.u.}$

$V_1 = 120 - I''_f Z_{12}$

$0.156 = 1 - (-j4.357) Z_{12}$

$Z_{12} = j0.1937 \text{ p.u.}$

$V_3 = 120 - (-j4.357) Z_{32} = 0.349$

$Z_{32} = j0.1494 \text{ p.u.}$

$V_4 = 120 - (-j4.357) Z_{42} = 0.344$

$Z_{42} = j0.1506 \text{ p.u.}$

$Z_{bus} = \begin{bmatrix} j0.1937 \\ j0.2295 \\ j0.1494 \\ j0.1506 \end{bmatrix}$

Q2) If a circuit breaker has a rated S/C MVA of 2386 at a voltage of 73 kV and K factor equal to 1.2, evaluate the maximum current which the breaker can interrupt and its corresponding voltage. [5]

$$2386 \text{ M} = \sqrt{3} \times 73 \text{ kV} \times I_{sc} \times 10^{-3}$$

$$I_{sc} = 18.87 \text{ kA}$$

$$I_{\text{interrupt max.}} = 1.2 \times 18.87 \text{ kA} = \boxed{22.644 \text{ kA}}$$

$$K = 1.2 = \frac{V_{\text{rated max}}}{V_{\text{lower limit}}} \Rightarrow V_{\text{lower limit}} = \frac{73 \text{ kV}}{1.2} = \boxed{60.83 \text{ kV}}$$

Q3) The line currents flowing to the Y-side of 10 MVA, 66 Y/13.2 Δ kV transformer are:  $I_a = 100 \angle 0^\circ$ ,  $I_b = 141.4 \angle 225^\circ$ ,  $I_c = 100 \angle 90^\circ$ .

By using the concept of symmetrical components in pu, evaluate the currents flowing in the lines from the Δ-side. DO NOT use the concept of turns ratio. [15]

$$I_{\text{base}} = \frac{10 \text{ M}}{\sqrt{3} \times 66 \text{ k}} = 87.48 \text{ A}$$

Y :

$$I_A = 100 \angle 0^\circ \text{ A}$$

$$= 1.143 \angle 0^\circ \text{ p.u.}$$

$$I_B = 1.616 \angle 225^\circ$$

$$I_C = 1.143 \angle 90^\circ$$

$$\begin{bmatrix} I_A^{(0)} \\ I_A^{(1)} \\ I_A^{(2)} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & 1 & 1 \\ 1 & a & a^2 \\ 1 & a^2 & a \end{bmatrix} \begin{bmatrix} 1.143 \angle 0^\circ \\ 1.616 \angle 225^\circ \\ 1.143 \angle 90^\circ \end{bmatrix}$$

$$\therefore I_A^{(0)} = 0, \quad I_A^{(1)} = \frac{1}{3} (I_A + I_B + I_C) \neq 0$$

$$I_A^{(1)} = 1.275 \angle -15^\circ \text{ p.u.}$$

$$I_A^{(2)} = 0.3414 \angle 105^\circ \text{ p.u.}$$

Δ :

$$I_a^{(0)} = 0$$

$$I_a^{(1)} = 1.275 \angle -15^\circ - 30^\circ = 1.275 \angle -45^\circ \text{ p.u.} = 111.557 \text{ A}$$

$$I_a^{(2)} = 0.3414 \angle 105^\circ + 30^\circ = 0.3414 \angle 135^\circ \text{ p.u.} = 29.87 \text{ A}$$

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} 0 \\ 111.557 \angle -45^\circ \\ 29.87 \angle 135^\circ \end{bmatrix}$$

$$I_a = 81.667 \angle -45^\circ \text{ A}$$

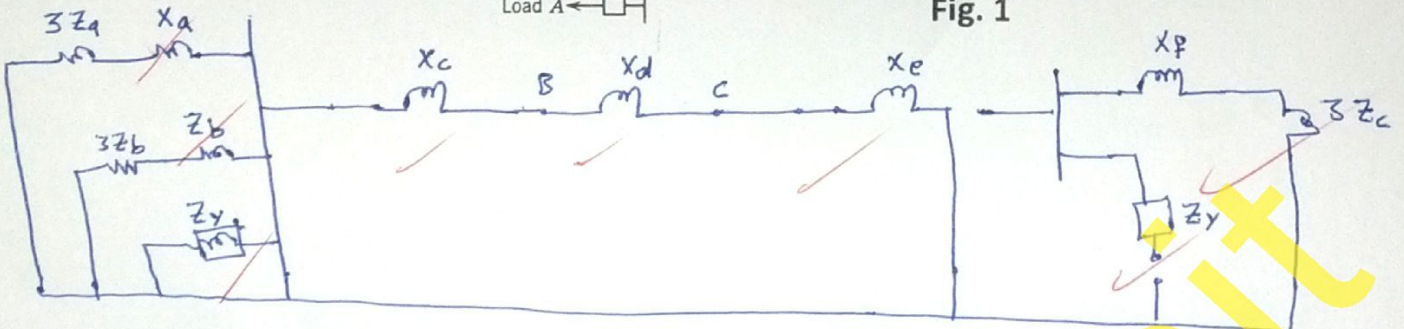
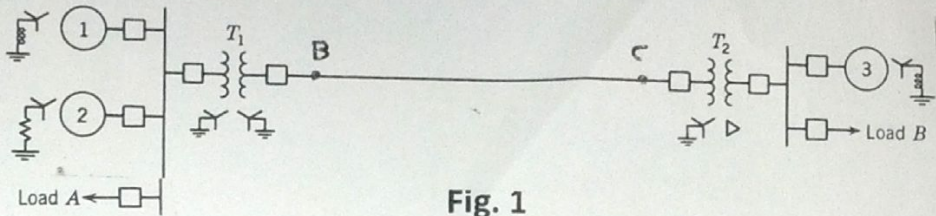
$$I_b = 129 \angle -153.4^\circ \text{ A} \quad 129 \angle -153.4^\circ \text{ A}$$

$$I_c = 129 \angle 63.4^\circ \text{ A}$$

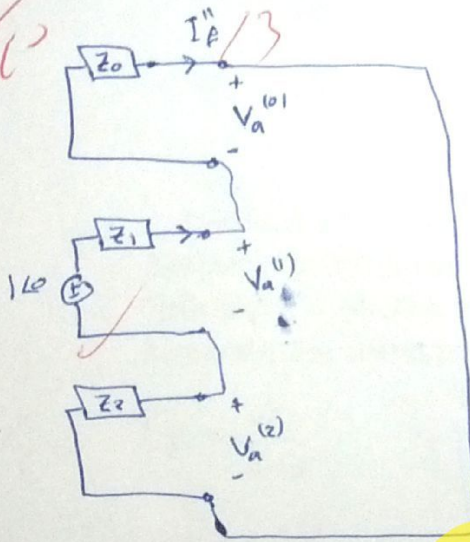
$$I_{\text{base}} = \frac{10 \times 10^6}{\sqrt{3} \times 13.2}$$

Q4)a- Draw the zero sequence network of the system shown in Fig. 1. [5]  
 Given the following zero sequence and earthing impedance values in pu for the elements on the same base:

Parameter	G <sub>1</sub>	G <sub>2</sub>	A	T <sub>1</sub>	T.L <sub>BC</sub>	T <sub>2</sub>	G <sub>3</sub>	B
Z <sub>0</sub>	x <sub>a</sub>	x <sub>b</sub>	z <sub>y</sub>	x <sub>c</sub>	x <sub>d</sub>	x <sub>e</sub>	x <sub>f</sub>	z <sub>y</sub>
Z <sub>n</sub>	z <sub>a</sub>	z <sub>b</sub>	direct	-	-	-	z <sub>c</sub>	isolated



b- A single-line-to ground fault occur at a point Q in a given power system. The fault current  $I_f = -j2.42$ . If the corresponding equivalent sequence impedances in pu were as follows:  $Z_1 = j0.5$ ,  $Z_2 = j0.5$ ,  $Z_0 = j0.24$ , evaluate phase voltages at point Q. [10]



$$V_a^{(0)} = -(-j2.42)(j0.24)$$

$$= -0.5808$$

$$V_a^{(1)} = 1 - (-j2.42)(j0.5)$$

$$= -0.21$$

$$V_a^{(2)} = -(-j2.42)(j0.5)$$

$$= -1.21$$

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} -0.5808 \\ -0.21 \\ -1.21 \end{bmatrix}$$

$$V_a = -2$$

$$V_b = 0.876 \angle -81.5^\circ$$

$$V_c = 0.876 \angle +81.5^\circ$$