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**Questions # 1 (10 marks) SHOW YOUR CALCULATIONS**

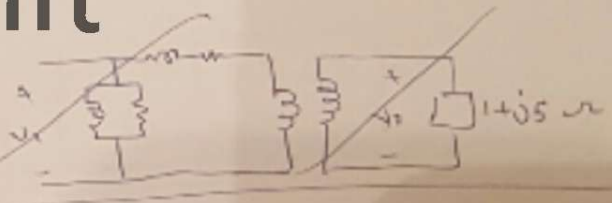
A single-phase 10 kVA, 7500/250 V, transformer has the following approximate equivalent circuit parameters:

$Z_{eq} = 0.02 + j0.08 \text{ pu}$ ,  $R_c = 50 \text{ pu}$ ,  $X_m = 20 \text{ pu}$

Determine the transformer voltage regulation using the per-unit equivalent circuit assuming a rated voltage is applied to the transformer primary while a load of  $Z_L = 1 + j5 \Omega$  is connected to the secondary.

PF: 0.19 %VR = 8.23 %

# Power Unit

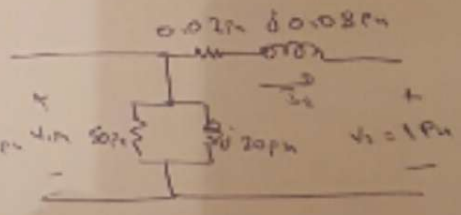


$S_{rated} = 10 \text{ kVA}$

$V_{p1} = 7500 \text{ V}$

$V_{p2} = 250 \text{ V}$

$V_{pru} = \frac{V_2}{V_{p2}} = \frac{250}{250} = 1 \text{ pu}$



$|I_{2pu}| = \frac{S_{rated}}{V_2} = 1 \text{ pu}$

$I_2 = 1 \angle -78.7 \text{ pu}$

$V_{pru} = V_{sec} + I_2 (0.02 + j0.08)$

$V_{pru} = 1 + (1 \angle -78.7)(0.02 + j0.08)$

$V_{pru} = 1.0823 \angle -0.02$

$VR = \frac{V_{pru} - V_{rated}}{V_{rated}} \times 100\% = \frac{1.0823 - 1}{1} \times 100\% = 8.23\%$

$VR = 8.23\%$

# Power Unit

Questions 2 (15 mark)

SHOW YOUR CALCULATIONS

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A 25 kV/600 V, 60 Hz, 300 kVA 3-phase transformer is connected as shown in Fig. Q2. The typical per unit parameters of the primary and secondary windings and the magnetizing branch as provided by the manufacturer are

$$R_1 = 0.01 \quad X_1 = 0.02 \quad R_2 = 0.01 \quad X_2 = 0.02$$

The magnetizing branch real  $P_c$  and reactive  $Q_m$  power losses are 1% resistive and 1% reactive, respectively.

- Obtain the actual parameters ( $R_1, X_1, R_2, X_2, R_c$  and  $X_m$ ) in Ohms of the three-phase two winding transformer.
- Draw its per-phase approximate equivalent circuit referred to the primary showing the actual values of the parameters.
- Determine the vector group of the 3-ph transformer connection using the clock method. Illustrate your solution using schematic diagram.

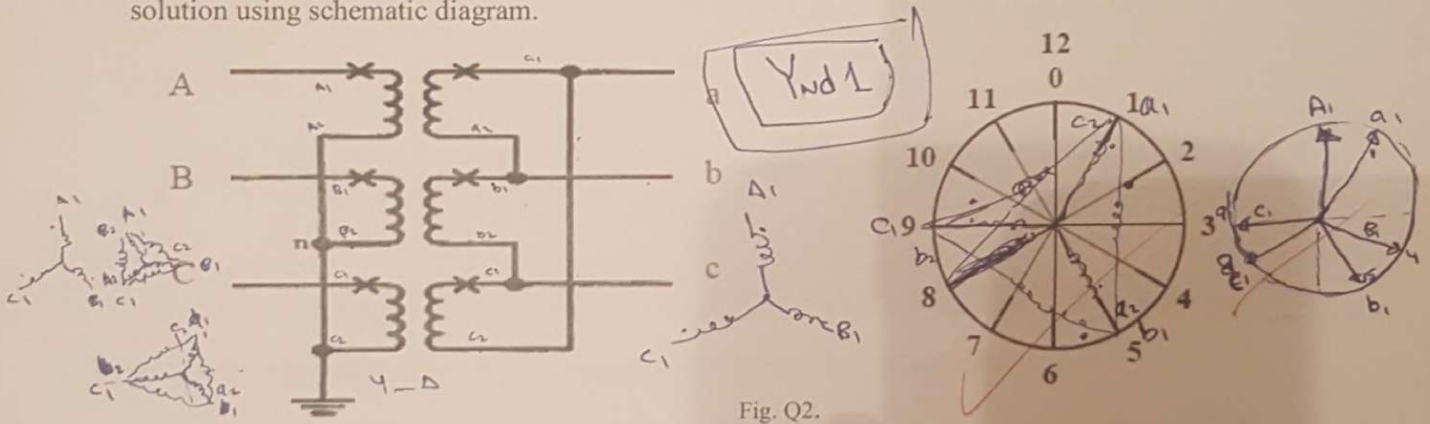


Fig. Q2.

$$S_b = 100 \text{ KVA}$$

$$V_{b1} = 14.43 \text{ kV}$$

$$V_{b2} = 600 \text{ V}$$

$$Z_{b1} = \frac{(V_{b1})^2}{S_{b1\phi}} = 2083.3 \Omega$$

$$Z_{b2} = \frac{(V_{b2})^2}{S_{b2\phi}} = 3.6 \Omega$$

$$R_1 = Z_{b1} \times 0.01 = 20.833 \Omega$$

$$R_2 = Z_{b2} \times 0.01 = 0.036 \Omega$$

$$X_1 = Z_{b1} \times 0.02 = 41.66 \Omega$$

~~$$R_c = \frac{1}{0.01} = 100 \Omega$$~~

$$R_c = \frac{1}{0.01} = 100 \Omega$$

$R_1 =$	20.833	$\Omega$
$R_2 =$	0.036	$\Omega$
$X_1 =$	41.66	$\Omega$
$X_2 =$	0.072	$\Omega$
$R_c =$	208.3	k $\Omega$
$X_m =$	208.3	k $\Omega$
$R_{eq}' =$	41.66	$\Omega$
$X_{eq}' =$	83.3	$\Omega$

$$R_{eq}' = R_1 + R_2 \times 578.4$$

$$X_{eq}' = X_1 = X_2 \times 578.4$$

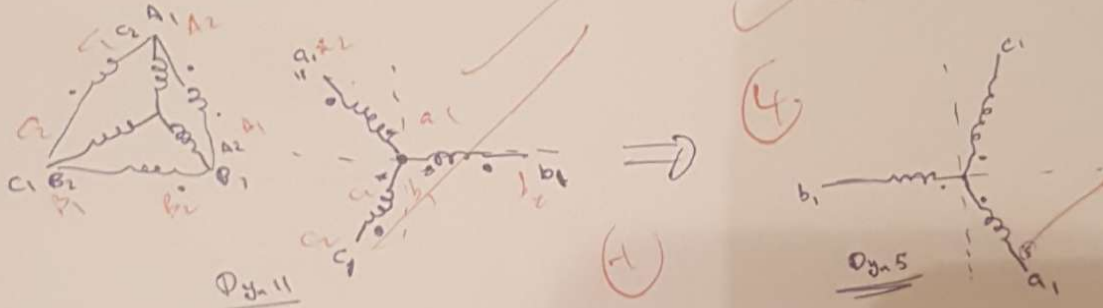
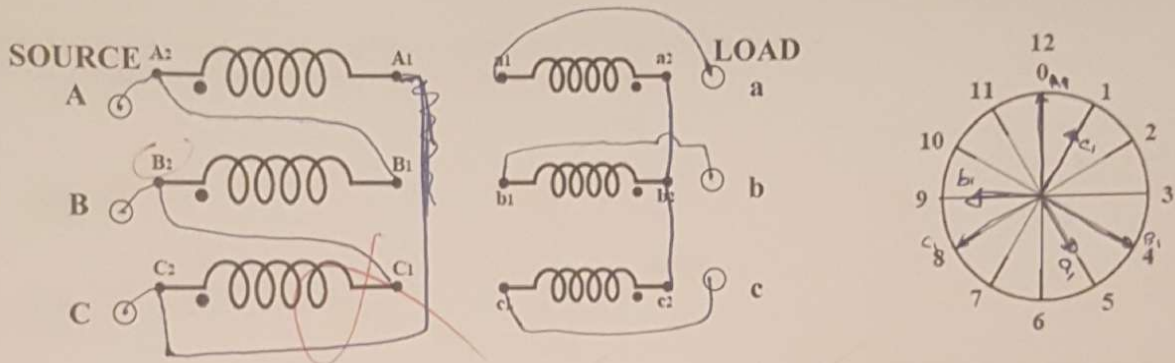
# Power Unit

Question #3 (10 marks)

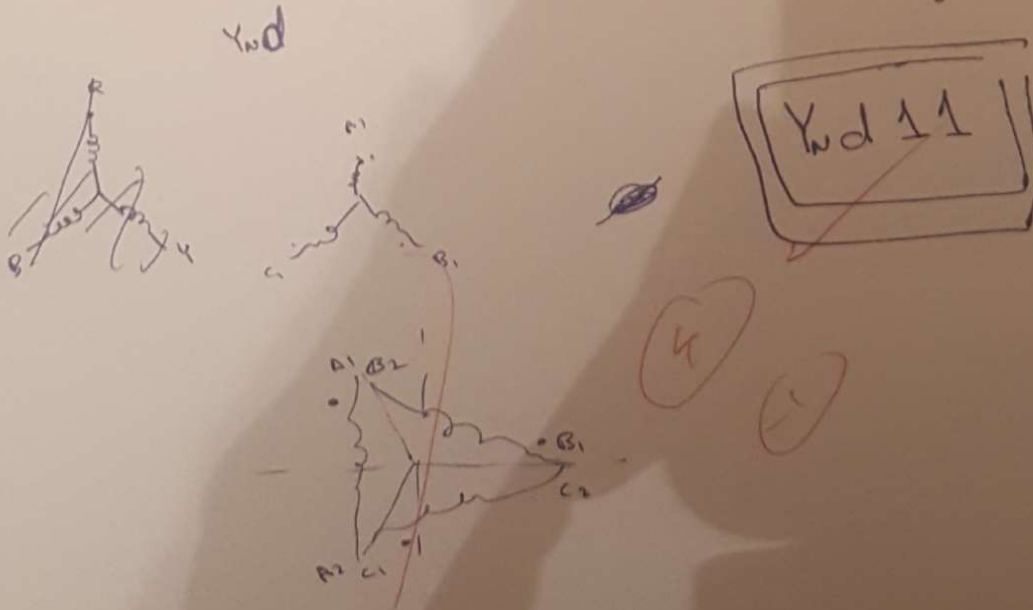
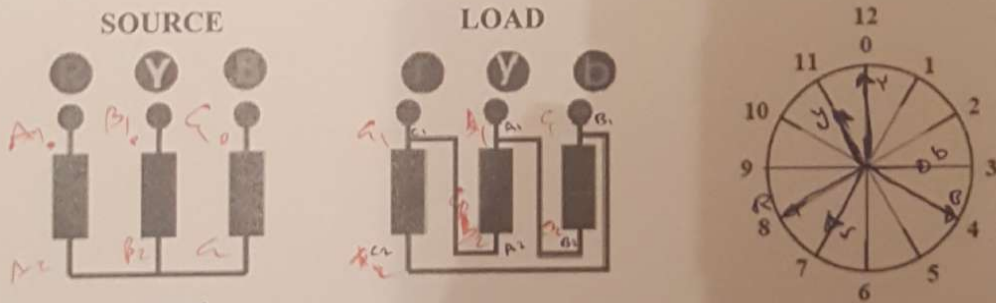
SHOW YOUR CALCULATIONS

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a. Draw a schematic connection diagram of a 3-phase transformer with Dyn5 vector group.



b. What is the vector group for the following 3-phase transformer connection?





# Power Unit

(5)

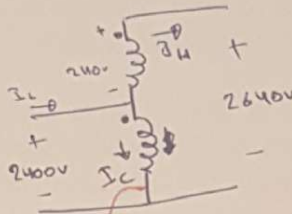
Question #4 (10 marks)

SHOW YOUR CALCULATIONS

- A 10-kVA, 60-Hz, 2400—240-V distribution transformer is reconnected for use as a step-up autotransformer with a 2640-V output and a 2400-V input. Draw the connection diagram and determine:
- the rated primary current  $I_L$  and secondary current  $I_H$  when connected as an autotransformer.
  - the advantage factor,  $A_f$ .
  - the apparent-power rating  $S_{I/O}$  when connected as an autotransformer.
  - power transferred by induction  $S_{ind}$  and conduction  $S_{cond}$ .

~~$I_L =$~~   
rated

$$I_H = \frac{10000}{240} = 41.67 \text{ A}$$



$$A_f = \frac{240 + 2400}{240} = 11$$

$$S_{ind} = 1000 \text{ kVA}$$

$$S_{I/O} = 11 \times 1000 = 11000 \text{ kVA}$$

$$S_{cond} = S_{I/O} - S_{ind} = 10000 \text{ kVA}$$

$$I_L = \frac{10000}{2400} = 4.167 \text{ A}$$

$$I_H = 41.67 \text{ A}$$

$$\frac{2640}{2400} = \frac{I_L}{41.67}$$

$I_L =$	458.37	A
$I_H =$	416.7	A
$A_f =$	11	
$S_{I/O} =$	1100	kVA
$S_{ind} =$	100	kVA
$S_{cond} =$	1000	kVA

(-2)

# Power Unit

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Question #5 (15 marks)

SHOW YOUR CALCULATIONS

Three 10 kVA, 1330/230 V, 60 Hz single-phase transformers are connected to form a three-phase 2300/230 V Yd1 transformer bank. The equivalent impedance of each transformer referred to the LV side is  $Z_{eqLV} = 0.12 + j0.25 \Omega$  and the magnetizing branch is neglected. The transformer bank supplies a 230 V, 27 kVA three-phase load at PF of 0.9 lagging. The transformer connected to a three-phase source through a feeder line with an impedance of  $Z_f = 0.5 + j2 \Omega$  per phase as shown in Fig. Q5.

- Draw the per phase equivalent circuit with all values referred to the HV side and determine
- the magnitudes of the HV- and LV- winding currents ( $I_{HV}$  and  $I_{LV}$ ) when the transformer bank supplies the above load at 230 V,
  - the magnitude of the line-to-line voltage at the HV side of the transformer,  $V_{HVLL}$ ,
  - the magnitude of the line-to-line source voltage at the three-phase source,  $V_{sLL}$ ,
  - the apparent power supplied by the source,  $S_{source}$  and power factor,  $PF_{source}$ .

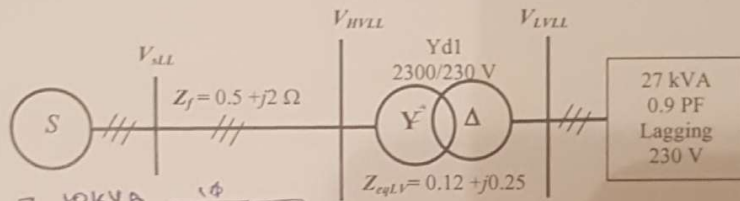


Fig. Q5

$S_{rated} = 10 \text{ kVA}$  (per phase)

$S_{1\phi} = 9 \text{ kVA}$

PF = 0.9 lagging

$I_H = \frac{9 \text{ k}}{230} \angle -\cos^{-1}(0.9)$

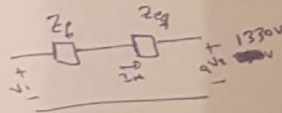
$I_H = 39.13 \angle -25.8^\circ \text{ A}$

$Z_{eqHV} = Z_{eqLV} \times \left(\frac{1330}{230}\right)^2$

$V_{HP} = 1330 + Z_H \times (I_{eqHV})$

$Z_{eq} =$

$\phi \angle -25.8^\circ$   
 $\phi \angle -25.8^\circ$



$Z_{eqHV} =$	$9.4 + j8.36 \Omega$
$I_{HV} =$	$39.13 \angle -25.8^\circ \text{ A}$
$I_{LV} =$	$39.13 \angle -25.8^\circ \text{ A}$
$V_{HVLL} =$	$2389.6 \text{ V}$
$V_{sLL} =$	$2405.8 \text{ V}$
$S_{source} =$	$9.4 \text{ kVA}$
$PF_{source} =$	$0.59 \approx 0.6$

Final Answer

$V_{HVLL} = 2389.6 \text{ V}$

$V_{sLL} = 2405.8 \text{ V}$

2405.8 V