

$$F = q (\mathbf{u} \times \mathbf{B})$$

Charge $\perp \mathbf{u}$

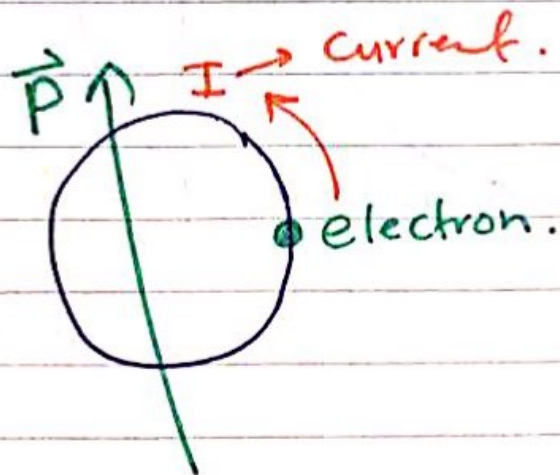
$$F \perp B$$

$$F \perp u$$

$$V_{emf} = \frac{\partial \lambda}{\partial t} = -N \frac{\partial \Phi}{\partial t} \rightarrow \text{flux.}$$

$$\Phi = \int \mathbf{B} \cdot d\mathbf{s} \Rightarrow \text{in closed surface} = 0$$

$$\mathbf{u} (\mathbf{L} \times \mathbf{B})$$

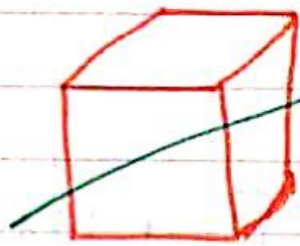


$$\Phi = \int \mathbf{B} \cdot d\mathbf{s}$$

$$= \int \mu H \cdot d\mathbf{s} = \int \mu K \mathbf{I} \cdot d\mathbf{s}$$

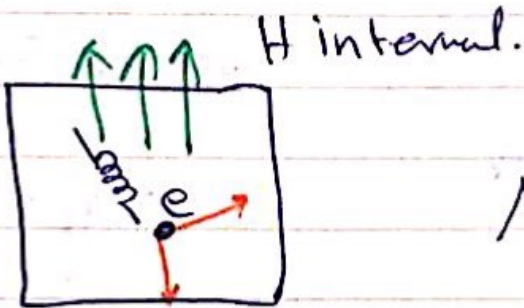
\mathbf{I} constant.

□



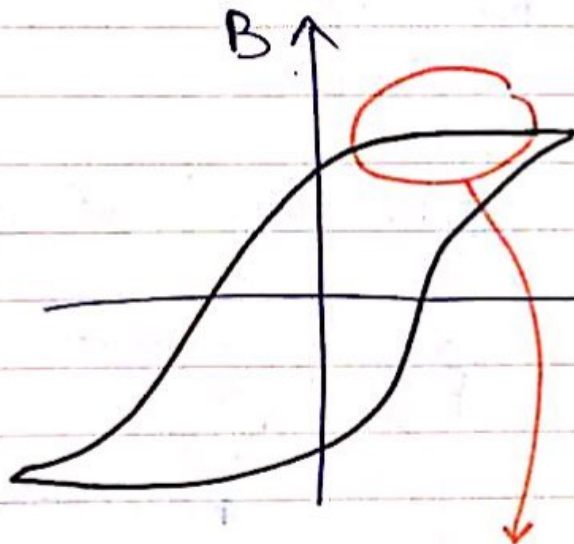
H (magnetic field)

at $t=0$ → time varying
 ↳ force on electrons.



$$M = M_0 M_r$$

$$M_r \geq 1$$



Hysteresis loop.

H ← +ve
 -ve
 up and down

rise $H \uparrow$ → use the transformer pulse ~~res~~ width modulation.

$\uparrow f$, Churny H .



and gate.

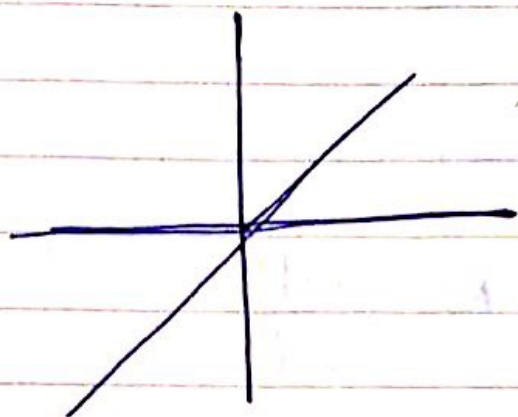
* from low to high ON } differential
 " high " low OFF } btw volt

⇒ Noise margin.

2

20_{year}erse

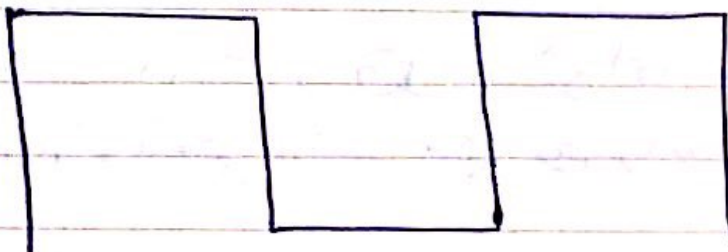
↑ area → ↑ loss in energy.



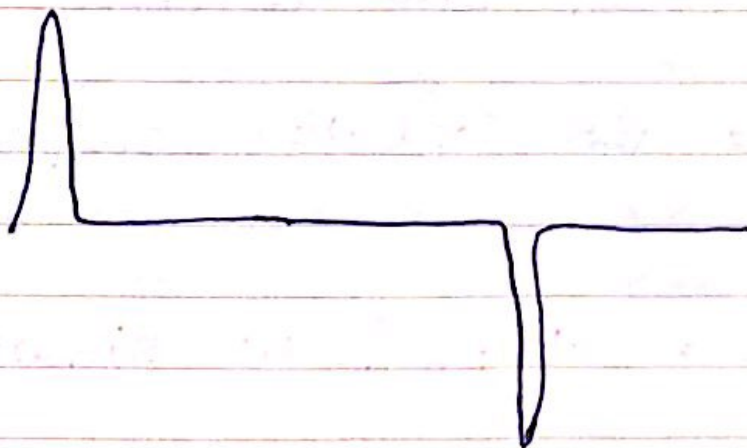
linear H.L

$$H = H_0 \sin(\omega t).$$

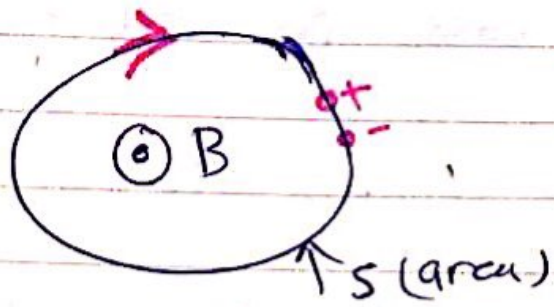
$$\frac{\Delta \bar{I}}{\Delta t}$$



$$\bar{e}^{\wedge} \ell$$



Ex



$$V_{emf} = -\frac{\partial \lambda}{\partial t} = -N \frac{\partial \Phi}{\partial t}$$

* إذا لفيت ال coil حول الوالد في loop
فرق بين أول لف وأخر لف ← يسمى break
down.

"break down btw different coil in a loop"

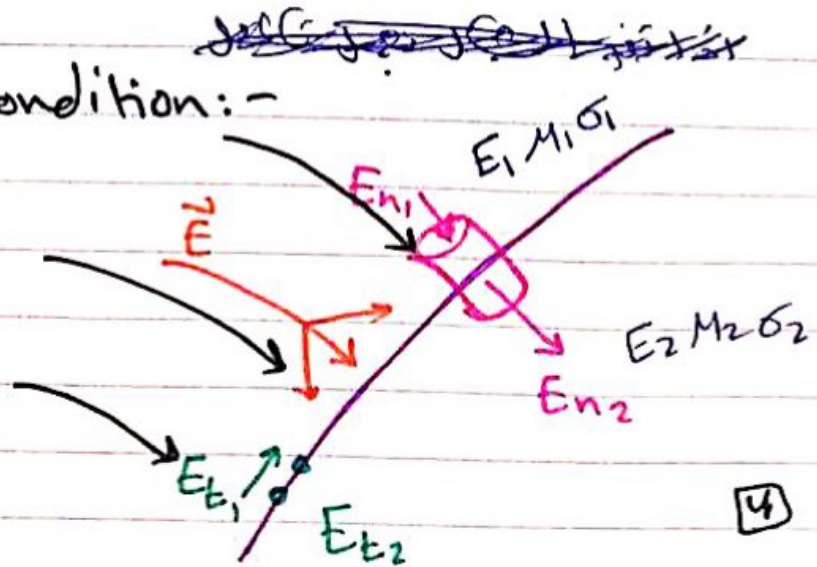
$B = B_0 \cos(\omega t)$ simple harmonic function.

$V_{emf} = + B_0 S \omega \sin(\omega t)$

B \vec{r}

* Boundary condition:-

$E_{t1} = E_{t2}$



4

magnetic field ← *
 electric. " ← *

normal ———— \vec{D}_1 ———— \vec{D}_2 ———— \vec{E} ————
 tangent ————

$$\vec{J} = \sigma \vec{E}$$

* electric field

In the transient. → electron move. *
 on component. → produce current
 → after relaxation time. →
 remove tangent and normal \vec{J}

normal component: (in area).

$$\int D_{n1} ds = q_{\text{inside}}$$

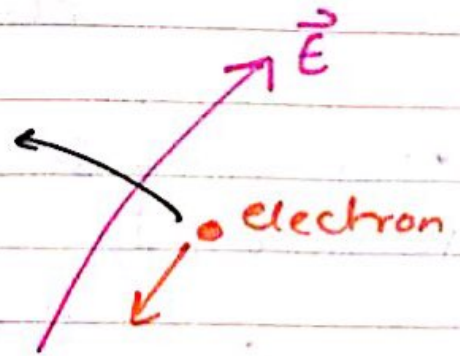
$$-D_{n1} + D_{n2} = \frac{q}{S} = \rho_s$$

$$D_{n2} - D_{n1} = \rho_s$$

5

$\epsilon \uparrow \rightarrow \vec{E} \downarrow \rightarrow \uparrow \text{Capacitance}$

كثافة المجال الكهربائي \vec{E} و ϵ و الجهد الكهربائي



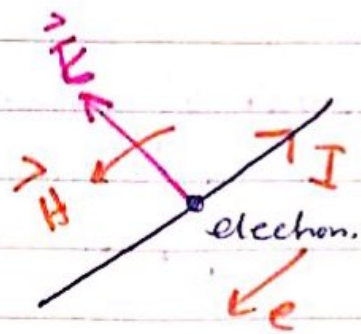
* Capacitor \Rightarrow breakdown voltage.

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t} \rightsquigarrow \vec{E} \cdot \epsilon_0$$

$$E = E_0 \cos(\omega t)$$

$$\nabla \times \vec{H} = \epsilon \frac{\partial \vec{E}}{\partial t}$$



$$\nabla \times \vec{H} = \epsilon \frac{\partial \vec{E}}{\partial t}$$

$$\nabla \times \vec{E} = -\mu \frac{\partial \vec{H}}{\partial t}$$

6

$$E = g(\alpha) \Rightarrow (t, \underline{x, y, z}) \propto \beta$$

$$E = g(\beta)$$

↑
time

↓
space.

$$= \cos(\beta)$$

$$= \cos(at + B(x, y, z)).$$

$$= \cos(\omega t - kr)$$



25/7/
Tue

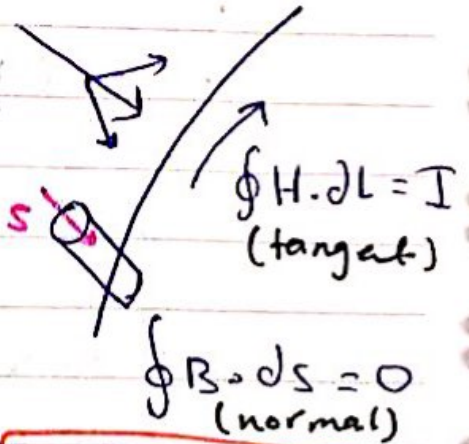
$$H_{t1} - H_{t2} = -K$$

wave equation:

$$E = E_0 e^{-\alpha r} \cos(\omega t - \beta r) \vec{a}_e$$

$$H = H_0 e^{-\alpha r} \cos(\omega t - \beta r) \vec{a}_h$$

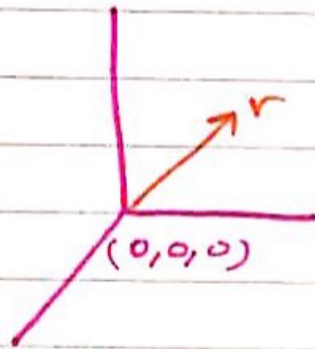
Phase shift. ↙



$$B_{n2} = B_{n1}$$

Complex ← vector ↘ \vec{r} quantity.

$$\vec{a}_e \times \vec{a}_h = \vec{a}_r$$

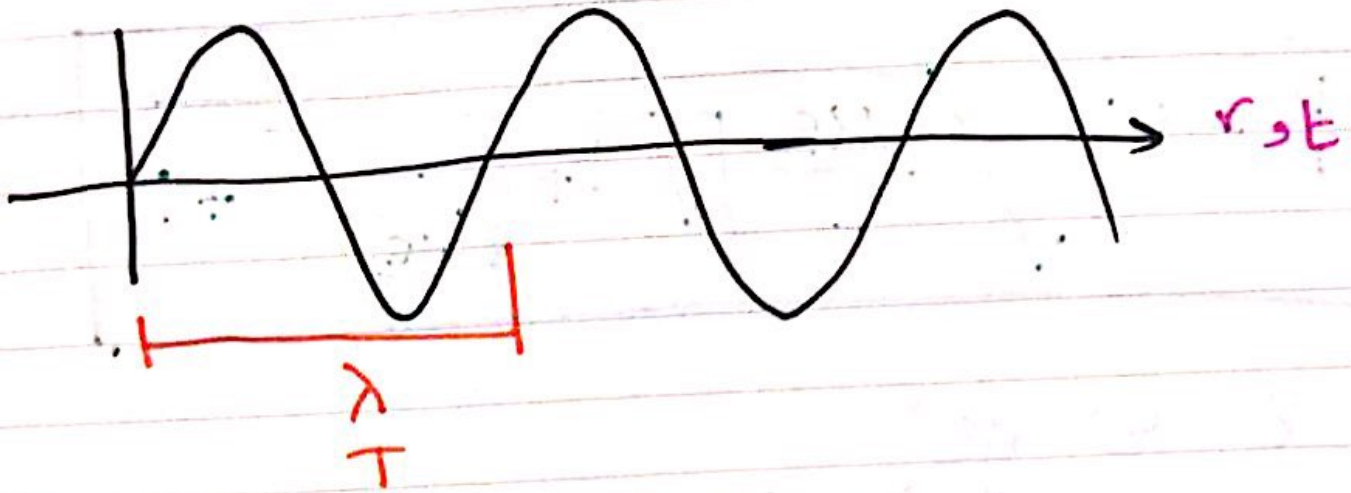


magnetic field. $\vec{a}_e \times \vec{a}_h = \vec{a}_r$

Phasor in (r) direction not in E or H field.

direction
X, Y ~~direction~~ ↘ electric, magnetic ~~direction~~ ↘ Phase x
↙ propagation.

8



$$\beta = \frac{2\pi}{\lambda}$$

$$\omega = \frac{2\pi}{T}$$

$\alpha \uparrow \rightarrow E \downarrow \rightsquigarrow \alpha \approx 0$

$E \sim \frac{1}{r} \sim \frac{1}{\sqrt{r}} \sim \frac{1}{\sqrt{t}}$

if $\beta \approx 100$ $e^{-100} \rightsquigarrow E \approx 0$.

$$\nabla^2 E - \delta^2 E = 0.$$

$$\delta^2 = (\sigma + j\omega\epsilon) j\omega\mu$$

$$= \alpha + j\beta$$

$$\alpha = \omega \sqrt{\frac{\mu\epsilon}{2} \left[\sqrt{1 + \left(\frac{\sigma}{\omega\epsilon}\right)^2} - 1 \right]}$$

$$\beta = \omega \sqrt{\frac{\mu \epsilon}{2} \left[\sqrt{1 + \left(\frac{\sigma}{\omega \epsilon} \right)^2} + 1 \right]}$$

$$\epsilon = \epsilon' + j\epsilon''$$

↘ effect of break down.

$$\mu = \mu' + j\mu''$$

↘ heat or real power dissipated in the material.

ϵ'' ~~part~~ → in water (الجزء الخيالي من العازل)

$$\text{loss tangent} = \frac{\sigma}{\omega \epsilon}$$

$$E = \gamma L H$$

γ ≡ Characteristic Impedance of Space.

$$\gamma = \sqrt{\frac{j\omega\mu}{\sigma + j\omega\epsilon}} = |\gamma| \angle \theta_\gamma$$

* Speed of propagation in r direction.

$$u = \frac{1}{\sqrt{\mu \epsilon}} = \frac{1}{\sqrt{\mu_0 \mu_r \epsilon_0 \epsilon_r}} = \frac{c}{\sqrt{\epsilon_r \mu_r}}$$

$$\frac{2\pi f}{T} = \frac{2\pi}{\lambda} r$$

$$\frac{\lambda}{T} = \frac{r}{t} = v \quad \left[\begin{array}{l} \text{distance} \\ \text{time} \end{array} = \text{Speed} \right]$$

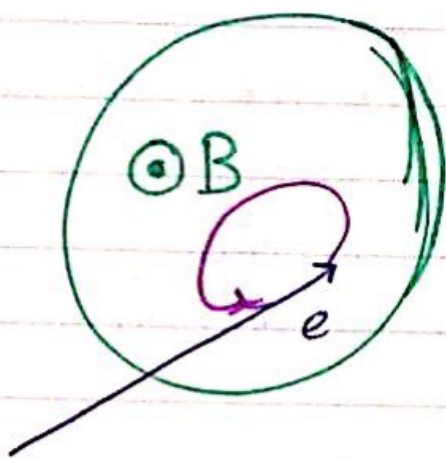
$\frac{1}{T} = \text{freq}$

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = 3 \times 10^8 \text{ m/s.}$$

$$\tan(2\theta) = \frac{\sigma}{\omega \epsilon}$$

$\sigma = 0 \rightarrow \gamma = \text{complex}$
 \hookrightarrow special case. $\alpha = 0.$





\rightarrow magnetic field

electron



$$v = E \cdot dl$$

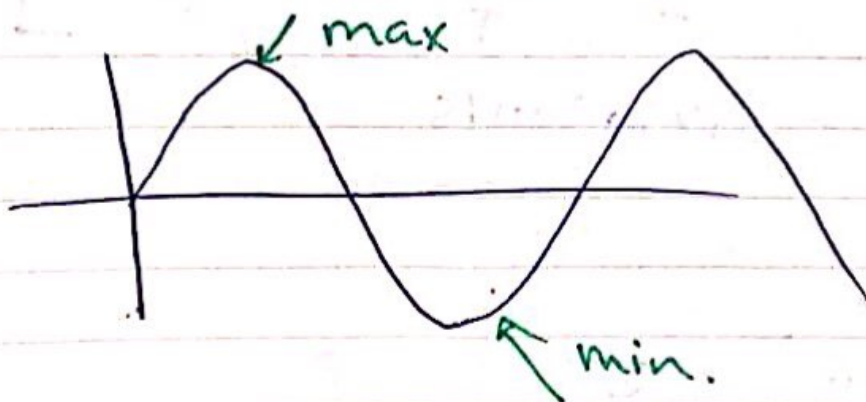
magnetic field

magnetic field



max

min.



not coherent pure Sine wave

Ex]

$$E = E_0 e^{-\alpha r} \cos(\omega t - \beta r) \vec{a}_x$$

$$E = E_0 e^{-\alpha z} \cos(\omega t - \beta z) \vec{a}_x$$

↳ unit (volt/meter)

$$H = H_0 e^{-\alpha z} \cos(\omega t - \beta z) \vec{a}_y$$

$$\frac{E_0}{\mu}$$

elect field. \perp magnetic field

$$H = \frac{E_0}{\mu} e^{-\alpha z} \cos(\omega t - \beta z) \vec{a}_y$$

↳ unit (ampere/meter)

\vec{P} Power or average Poinling

propagation direction

$$\vec{P} = \vec{E} \times \vec{H}$$

$$\boxed{\overline{P} = \frac{1}{2} |E| |H|}$$

W/m² "power density"

Ex

$$\sigma = 0.01, \quad \epsilon_r = 4, \quad \mu_r = 1$$

$$E_0 = 10 \text{ V/m}, \quad f = 6 \text{ GHz}$$

$$E \text{ in } +ve \text{ } x \text{ direction} \Rightarrow (-\beta)$$

$$P \text{ in } +ve \text{ } z \text{ direction}$$

Find: $u, \lambda, \gamma, \alpha, \beta, \bar{P}$

Sol:

$$\mu_0 = 4\pi \times 10^{-7}$$

$$\epsilon_0 = 8.85 \times 10^{-12}$$

$$\textcircled{1} \quad u = \frac{c}{\sqrt{\mu_r \epsilon_r}} = \frac{3 \times 10^8}{\sqrt{4 \cdot 1}} = 150 \times 10^6$$

$$\textcircled{2} \quad \lambda = \frac{u}{f} = \frac{c/2}{6 \times 10^9} = 0.025 = 2.5 \text{ cm}$$

$$\textcircled{3} \quad \alpha = \omega \sqrt{\frac{\mu \epsilon}{2} \left(\sqrt{1 + \left(\frac{\sigma}{\omega \epsilon}\right)^2} - 1 \right)}$$

$$\frac{\sigma}{\omega \epsilon} = \frac{10^{-2}}{4 \times 2\pi \times 6 \times 10^9 \times 8.85 \times 10^{-12}} = 7.49 \times 10^{-3}$$

$$\omega = 2\pi f$$

$$\alpha = \frac{\omega}{u} \sqrt{\frac{1}{2} \left(\sqrt{1 + \left(\frac{\sigma}{\omega \epsilon}\right)^2} - 1 \right)}$$

14

$$\alpha = 0.941$$

$$(4) \beta = 251.5$$

$$(5) \gamma = \sqrt{\frac{j\omega M}{\sigma + j\omega\epsilon}} = \frac{\cancel{120\pi}}{\cancel{A}}$$

$$\gamma = \frac{\gamma_0}{\sqrt{\epsilon_r}} = \frac{120\pi}{\sqrt{4}} = 188.5$$

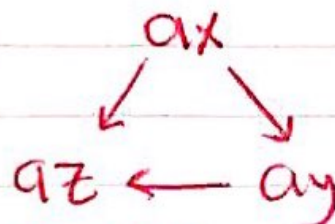
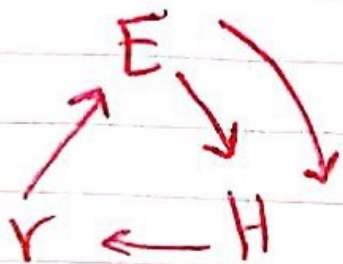
$$\gamma = 188.5 \left[\frac{1}{2} \tan^{-1}(7.5 \times 10^{-3}) \right]$$

$$= 188.5 / 0.215^\circ$$

$$(6) \cancel{P = \frac{1}{2} \frac{E_0^2}{\eta}}$$

$$\bar{P} = \frac{1}{2} \frac{E_0^2}{\eta} = \frac{1}{2} \cdot \frac{(10)^2}{188.5}$$

$$= 0.265 \text{ watt/meter.}$$



$$a_x \times a_y = +ve a_z$$

$$a_y \times a_x = -ve a_z$$

15

20erse

27/7/
THUR

Quiz 1 Find pointing vector. in freespace.
if:

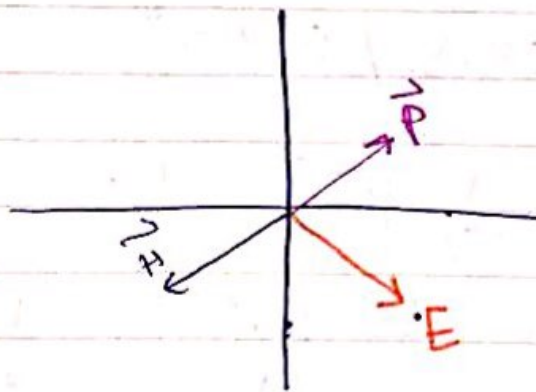
$$E = 8 \cos(\omega t - \beta r) \hat{a}_y$$

$$H = H_0 \cos(\omega t - \beta r) \hat{a}_x$$

$$P = -\frac{64}{377} \hat{a}_z$$

② Find \vec{H} :

$$E = 10 \cos(\omega t + \beta z) \left(\frac{1}{\sqrt{2}} \hat{a}_x - \frac{1}{\sqrt{2}} \hat{a}_y \right)$$



$$\vec{H} = \frac{10}{377} \cos(\omega t + \beta z) \left(\frac{-1}{\sqrt{2}} \hat{a}_x - \frac{1}{\sqrt{2}} \hat{a}_y \right)$$

16

* (∫) solution more stable.

$$\boxed{\text{Ex}} \quad \alpha = \pm 0.94$$

$$\beta = 251.4$$

$$\gamma = 188.5 \angle 0.215^\circ$$

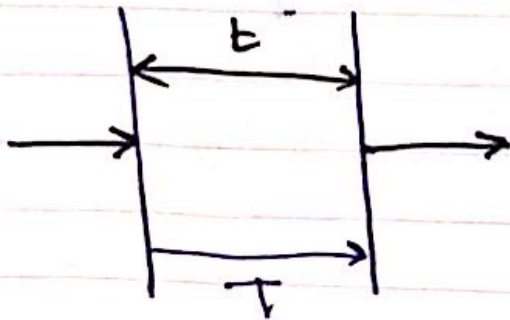
$$u = c/2$$

$$\lambda = 2.5 \text{ cm.}$$

$$E = 10 e^{-\alpha z} \cos(\omega t - \beta z) \vec{a}_x$$

$$H = \frac{10}{188.5} e^{-\alpha z} \cos(\omega t - \beta z - 0.215^\circ) \vec{a}_y$$

$$\vec{P} = \frac{100}{188.5} e^{-2\alpha z} \cos(\omega t - \beta z) \cos(\omega t - \beta z - 0.215^\circ) \vec{a}_z$$



17

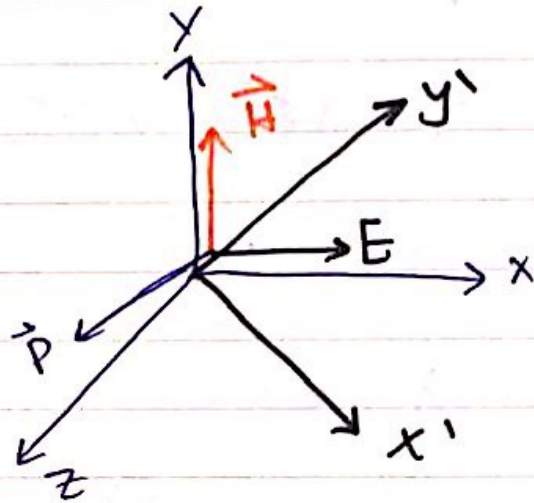
Ex

$$E = 10 \cos(\omega t - \beta z) \vec{a}_x$$

$$H = \frac{10}{\eta_0} \cos(\omega t - \beta z) \vec{a}_y$$

$\eta_0 \leftarrow 377$

$$\left\{ \begin{array}{l} E_0, M_0 \\ \eta = \eta_0 \end{array} \right.$$



$$\vec{V} = V_x \vec{a}_x + V_y \vec{a}_y + V_z \vec{a}_z$$

Rotation matrix in 3 dimension space.

$$\mathcal{R} = \begin{bmatrix} \cos & \sin \\ -\sin & \cos \end{bmatrix}$$

$$\vec{V}' = \vec{V} \mathcal{R}$$

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$$\boxed{\text{Ex}} \quad E = 10 \cos(\omega t - \beta z) \vec{a}_x + 5 \cos(\omega t - \beta x) \vec{a}_y$$

$$H = \frac{10}{377} \cos(\omega t - \beta z) \vec{a}_y + \frac{5}{377} \cos(\omega t - \beta x) \vec{a}_z$$

↳ 2 waves (independent).

* wave polarization :-

① linear :- "Space" & "elect field"

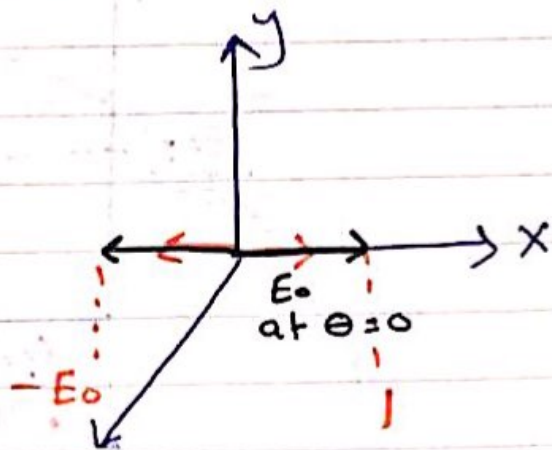
$$E = E_0 \cos(\omega t - \beta z) \vec{a}_x$$

$$\theta = 0$$

$$E =$$

at $\theta = 45$

$$E = \frac{E_0}{\sqrt{2}}$$

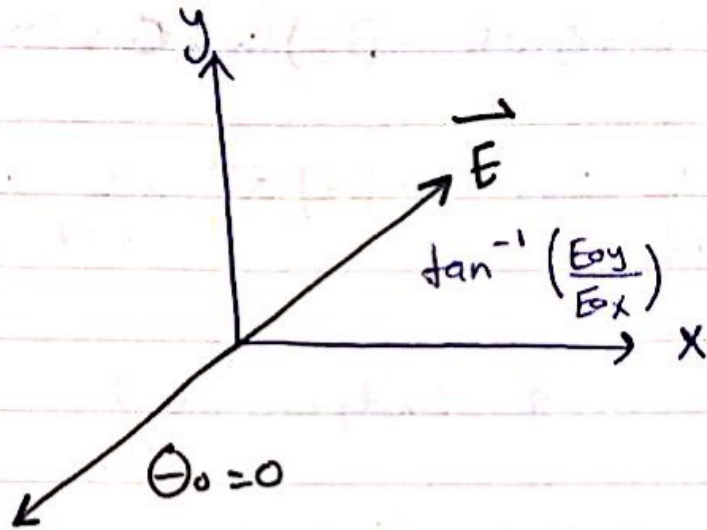


$$E = E_0 \cos(\omega t - \beta z) \left(\frac{\vec{a}_x}{\sqrt{2}} + \frac{\vec{a}_y}{\sqrt{2}} \right)$$

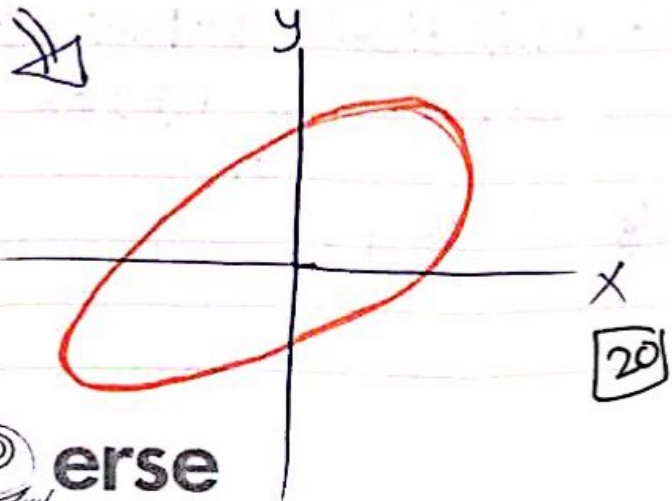
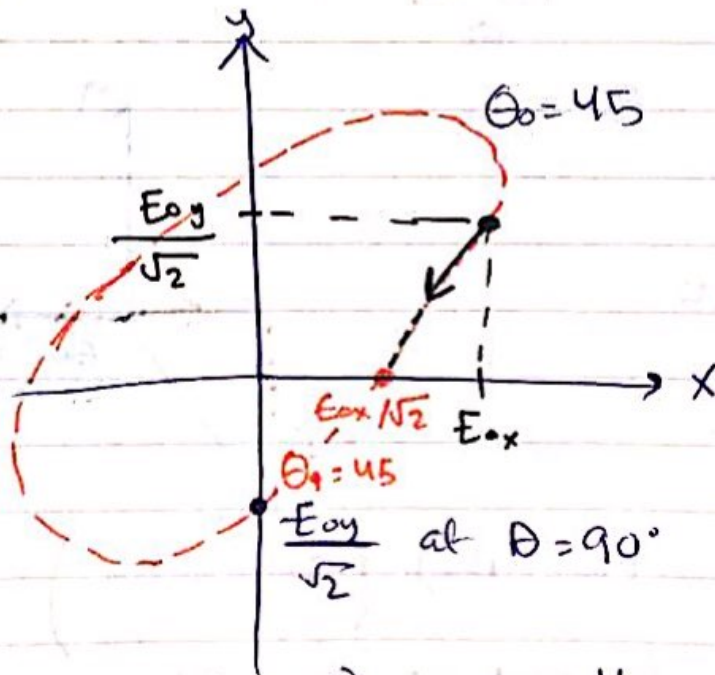
3- elliptical polarization :-

$$\vec{E} = E_0 \cos(\omega t - \beta z) \vec{a}_x + E_0 \cos(\omega t - \beta z + \theta_0) \vec{a}_y$$

$$\theta_0 = 45$$

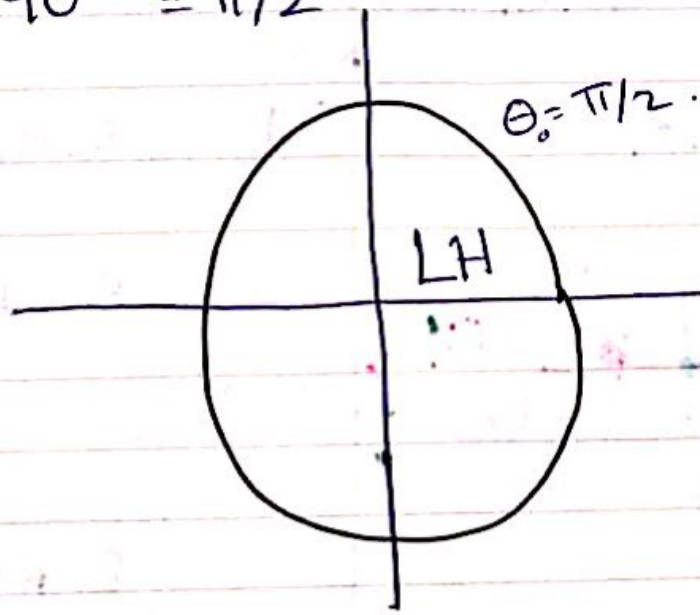


~~Handwritten scribbles and text, possibly indicating a correction or a specific condition.~~



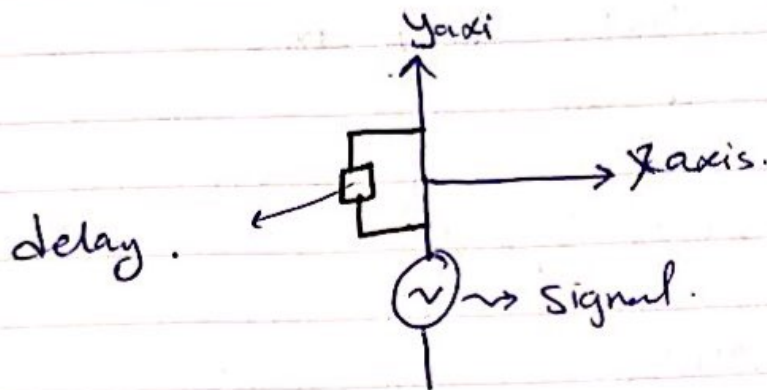
20erse

at $\theta_0 = 90^\circ = \pi/2$



LH \equiv left Hand.

2 Circular Polarization :-
 $\theta_0 = \pi/2$.



$$E_r = \Gamma E_i$$

$$E_t = \tau E_i$$

$$\Gamma = \frac{\gamma_2 - \gamma_1}{\gamma_2 + \gamma_1}$$

$$\tau = 1 + \Gamma$$

$$\tau = \frac{2\gamma_2}{\gamma_2 + \gamma_1}$$

$$\gamma = \sqrt{\frac{\mu}{\epsilon}}$$

at lossless ~~medium~~ $\sigma = 0$

Ex

free space

$$\begin{cases} \sigma = 0 \\ \epsilon_r = 1 \\ \mu_r = 1 \end{cases}$$

media 2

$$\begin{cases} \mu_r = 1 \\ \epsilon_r = 4 \\ \sigma_2 = 0 \end{cases}$$

Sol:

$$\gamma_1 = \gamma_0 = 120\pi = 377 \Omega.$$

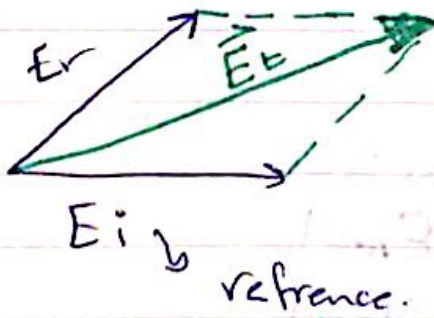
$$\gamma_2 = \sqrt{\frac{\mu}{\epsilon}} = \cancel{\dots} = 60\pi$$

reflected $\Gamma = \frac{60\pi - 120\pi}{180\pi} = -\frac{6}{18} = -\frac{1}{3}$

180° phase

$$E_r = -\frac{1}{3} E_i$$

for amplitude. $= \frac{E_0}{3} \cos(\omega t + \beta_2 z) \vec{a}_x \Rightarrow -v \vec{a}_x$



transmitted $\tau = \frac{2}{3}$, $E_t = \tau E_i$

$$E_t = \frac{2}{3} E_0 \cos(\omega t - \beta_2 z) \vec{a}_x$$

24

$$-1 < \Gamma < +1$$

$$0 < \tau < 2$$

$$\lambda_1 = \frac{c}{f}$$

$$\lambda_2 = \frac{c/2}{f}$$

$$u = \frac{1}{\sqrt{\mu\epsilon}}$$

$$\rightarrow B_2 = 2 B_1$$

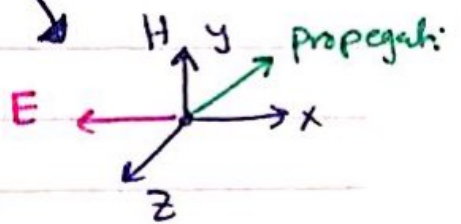
Free space

$$H_i = \frac{E_0}{\eta_0} \cos(\omega t - \beta_1 z) \vec{a}_y$$

$$H_r = \frac{1}{3} \frac{E_i}{\eta_0} \cos(\omega t + \beta_1 z) \vec{a}_y$$

media 2

$$H_t = \frac{2E_0}{3\eta_2} \cos(\omega t - \beta_2 z) \vec{a}_y$$



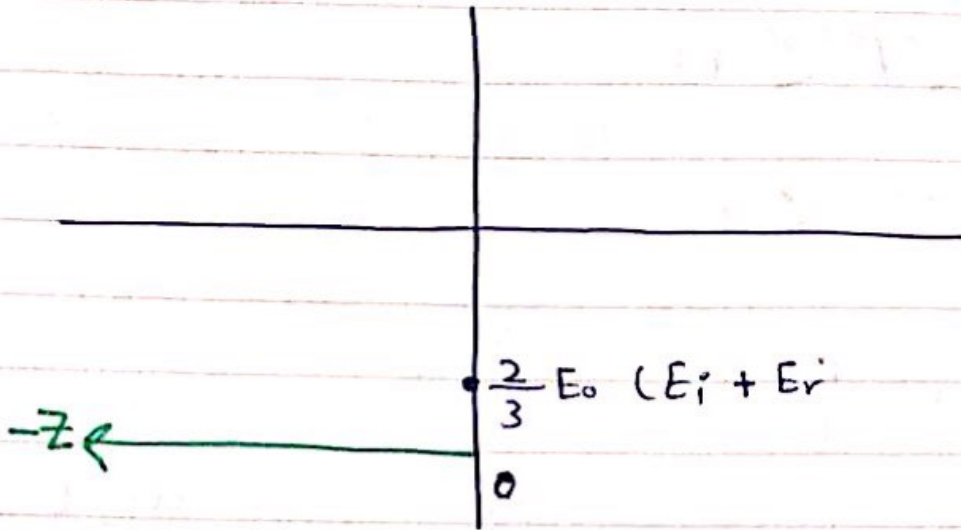
$E \rightarrow -x$ axis.

$\Gamma \rightarrow -ve z$.

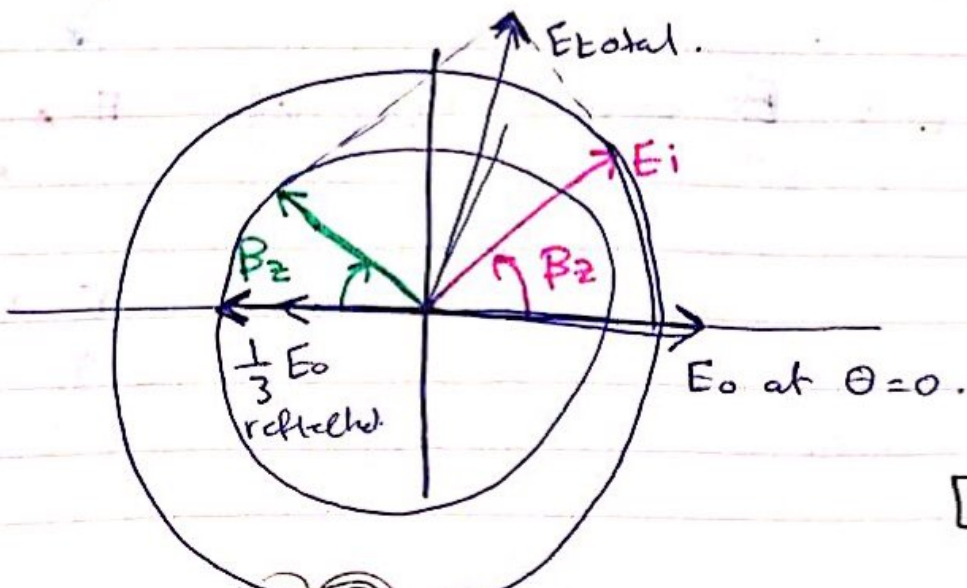
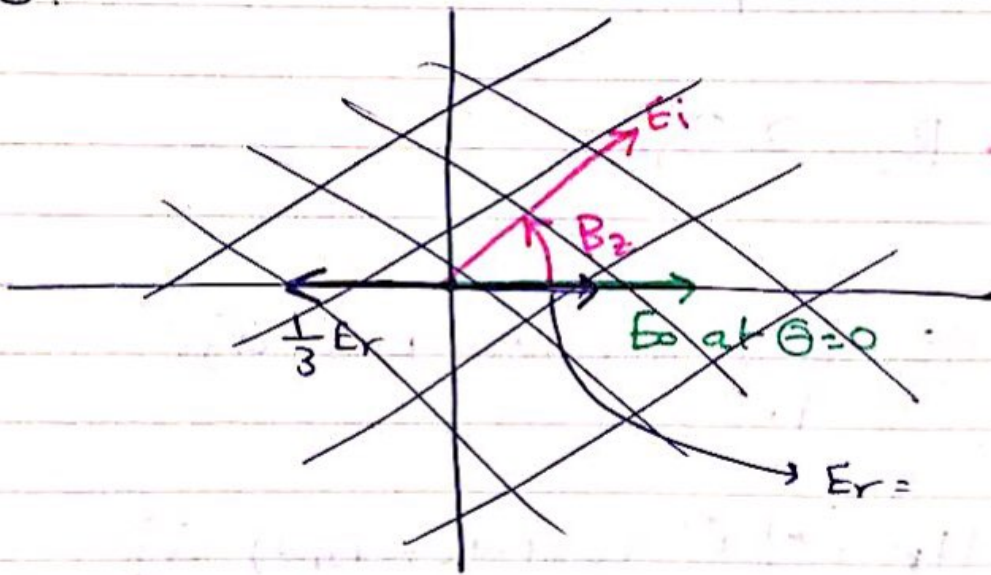
$H \rightarrow +ve y$.

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* 2 waves

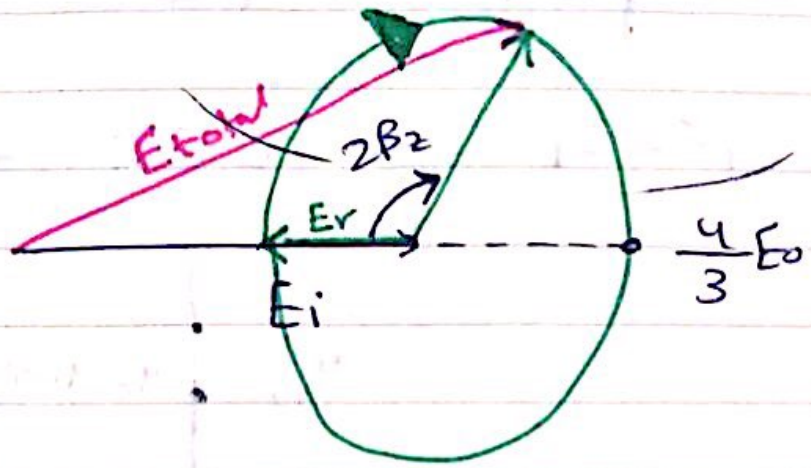


at $t=0$.



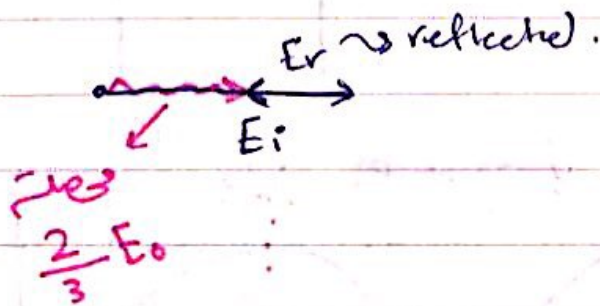
26

erse

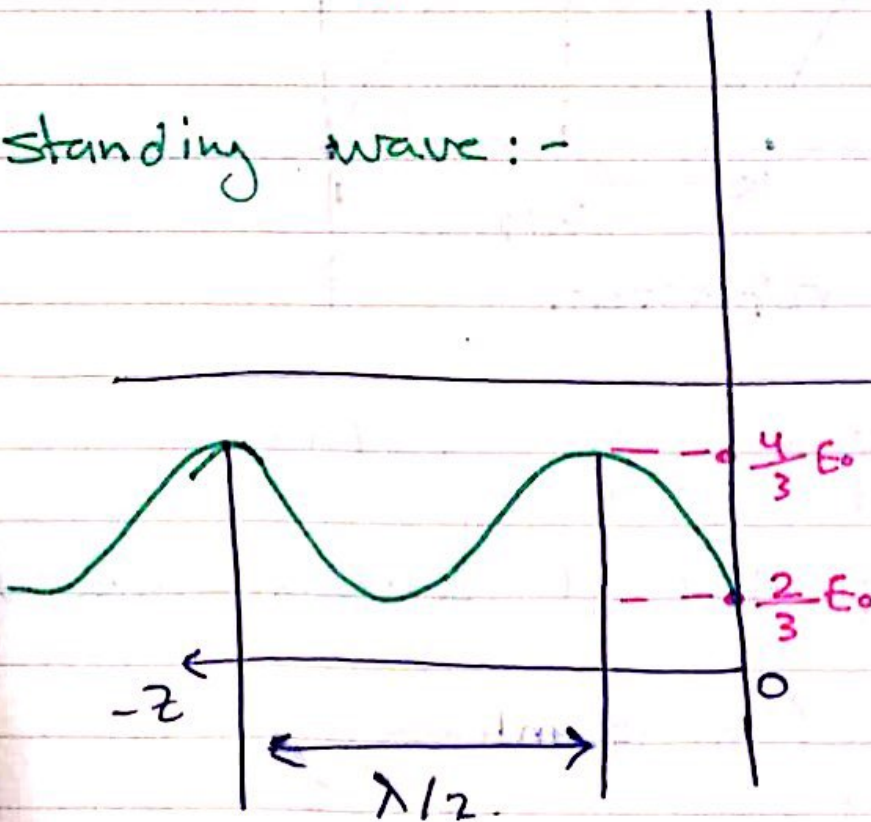


at $\theta = 0$.

$z = 1, \dots$



standing wave :-



reflection
 ↳ standing wave

every $\lambda/2$ we see 2 peaks.

27

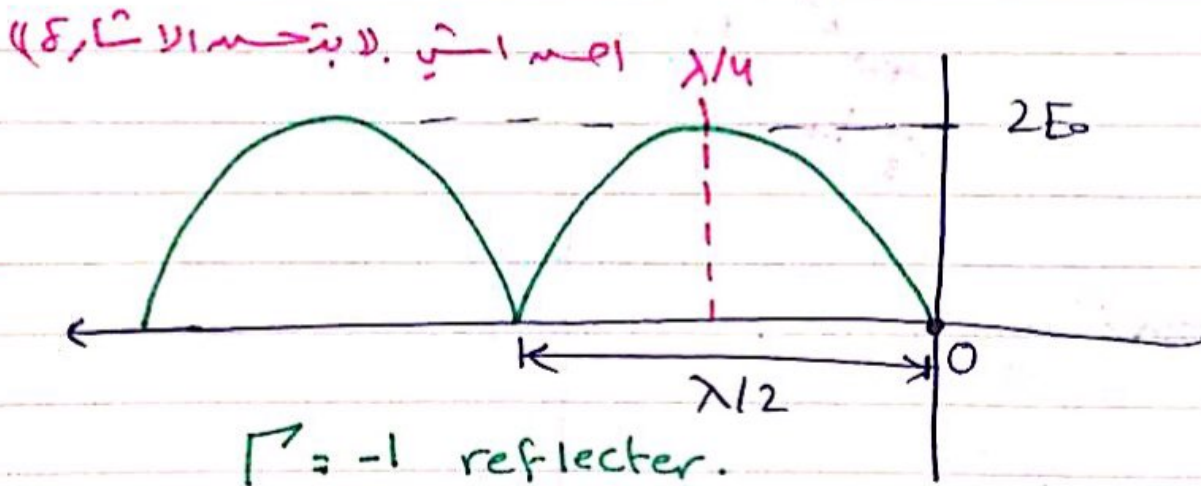
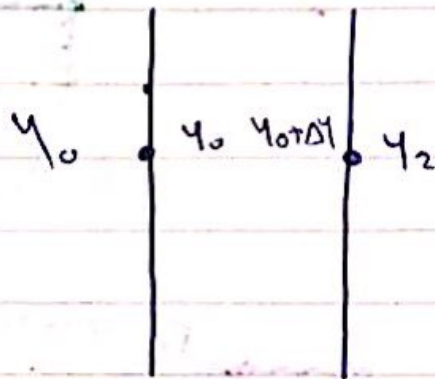
رسالة

↗ -ve → min
 ↘ +ve → max.

erse

max power \rightarrow match the 2 media.

$\Gamma = -1 \Rightarrow T = 0 \rightarrow$ no reflection.



AM $\lambda = \frac{c}{f} = \frac{3 \times 10^8}{801 \text{ KHz}} = 374 \text{ m}$

$\lambda/4 = 93 \text{ m}$ (antenna)

effect channel \Rightarrow in antenna.
Tx, Rx

SAR \equiv Specific absorption ~~rate~~.
Radio

31/8/17
MON

Ex

$$Y_1 = Y_0$$

$$Y_2 = 200 - j100$$

$$E_i = 5 \cos(\omega t - \beta_1 z) \hat{a}_y$$

$$\Gamma = \frac{Y_2 - Y_1}{Y_2 + Y_1}$$

$$= \frac{200 - j100 - 377}{200 - j100 + 377}$$

$$= \frac{-177 - j100}{577 - j100}$$

$$= 0.34 \angle -140^\circ$$

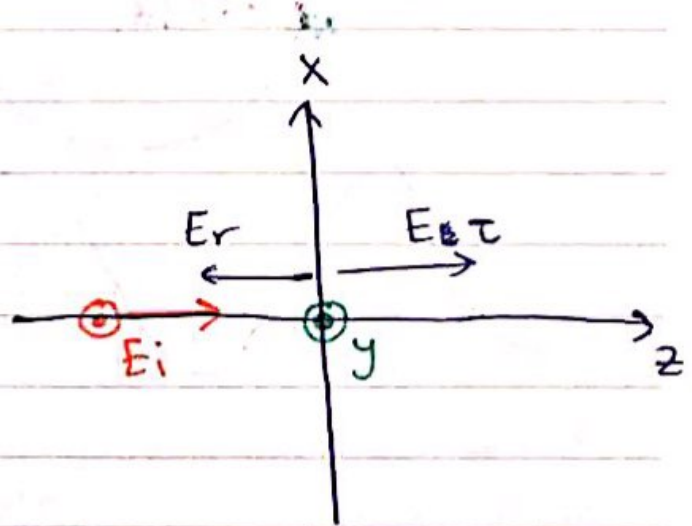
$$\tau = 1 + \Gamma$$

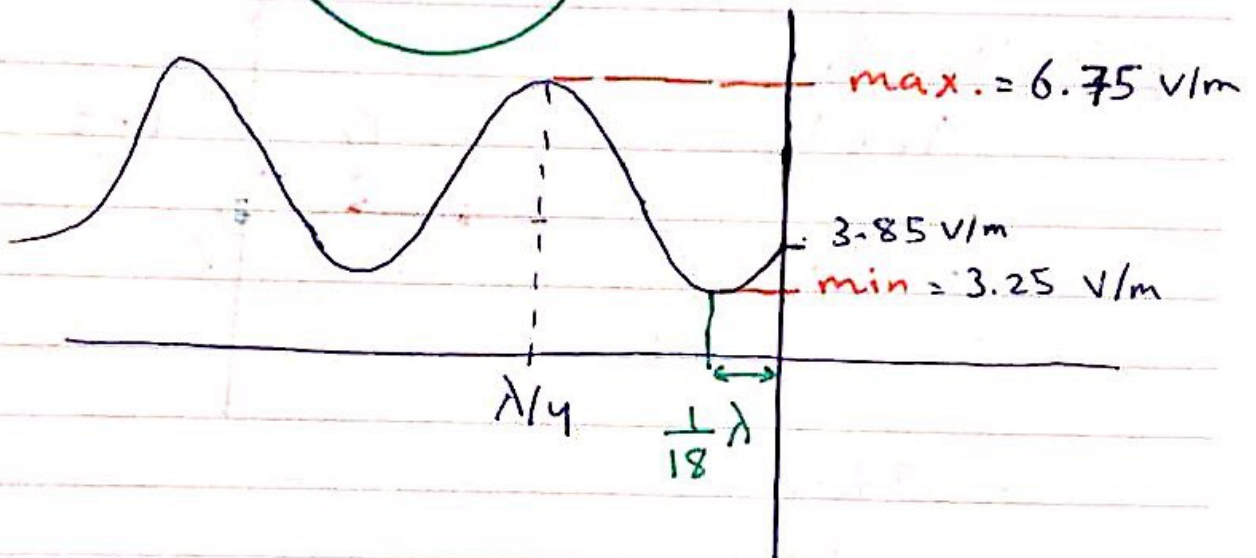
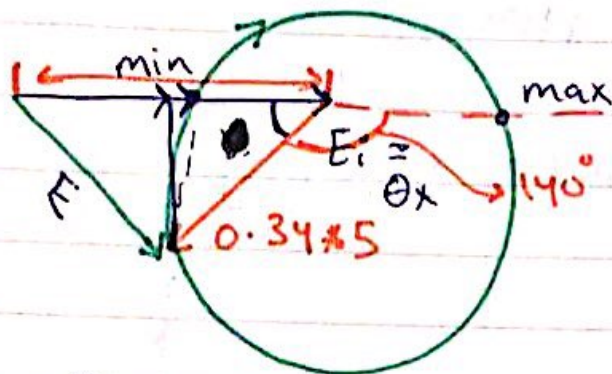
$$= 0.76 \angle -16.7^\circ$$

$$E_r = 0.34 * 5 \cos(\omega t + \beta_1 z + 140^\circ) \hat{a}_y$$

$$E_t = 0.76 * 5 \cos(\omega t - \beta_2 z + 16.7^\circ) \hat{a}_y$$

29





$$\rightarrow \Gamma E_0 \sin(\theta_r)$$

$$\text{min} = E_0 (1 - \Gamma)$$

$$\rightarrow E_0 + \Gamma E_0 \cos(\theta_r)$$

$$\text{max} = E_0 (1 + \Gamma)$$

$$E = E_0 \sqrt{(\Gamma \sin(\theta_r))^2 + (1 + \Gamma \cos(\theta_r))^2}$$

$$E = E_0 \sqrt{(\Gamma \sin(\theta_x))^2 + (1 + \Gamma \cos(\theta_r))^2}$$

$$\bullet 180 - \theta_x = 40$$

$$\frac{40}{360} * \frac{\lambda}{2} = \frac{1}{18\lambda}$$

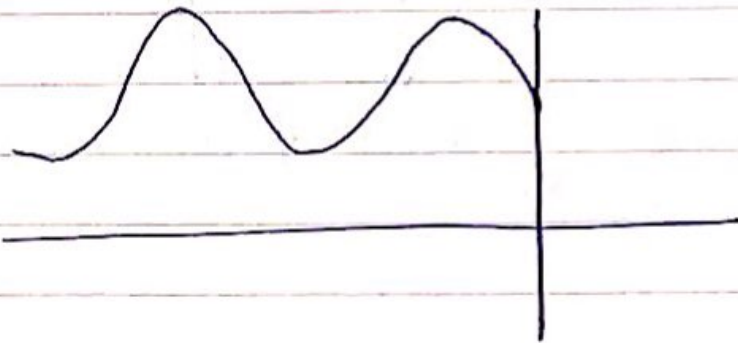
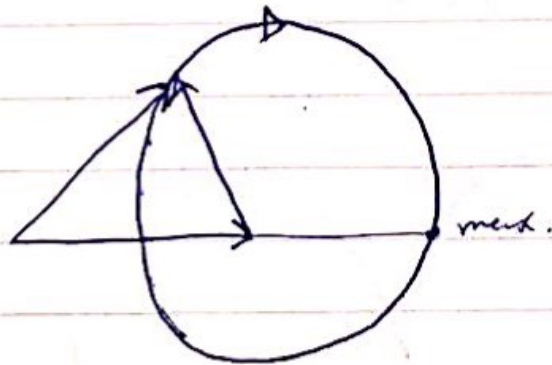
30

22erse

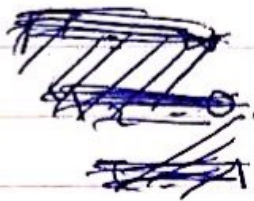
$$E = E_0 \sqrt{(\Gamma \sin(-140)) ^2 + (1 + \Gamma \cos(-140)) ^2}$$

$$= 3.85 \text{ V/m}$$

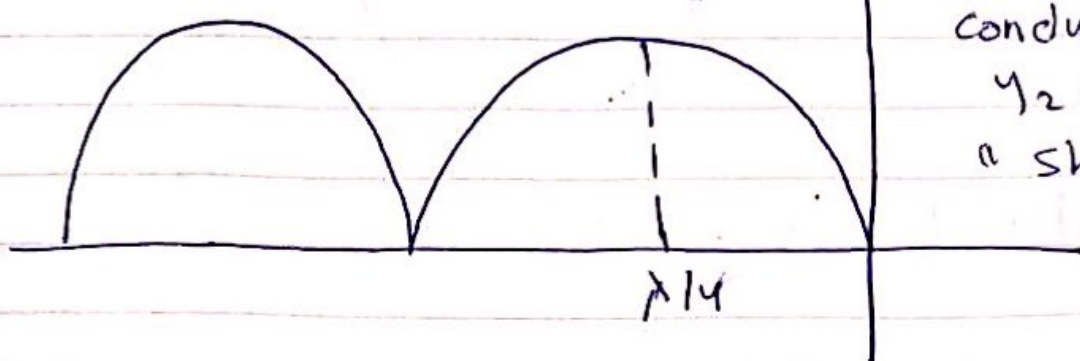
if Γ +ve.



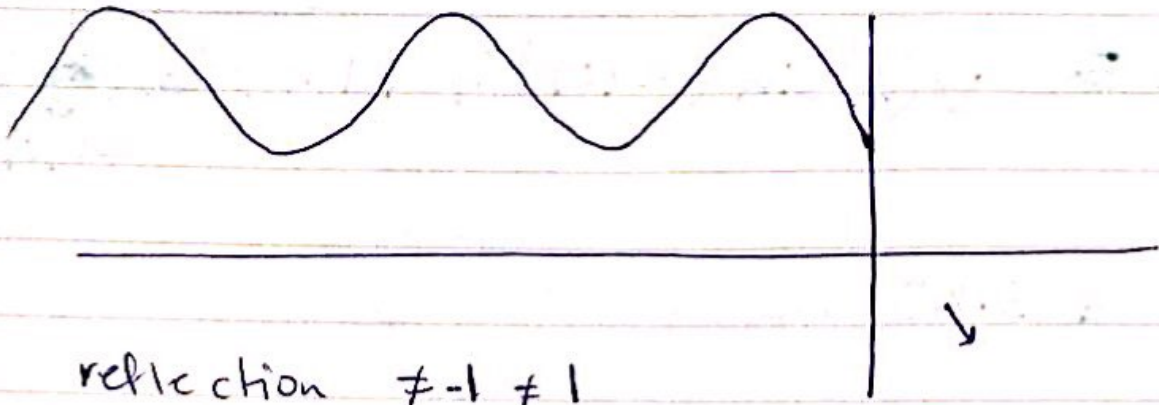
no \hat{u}
max \hat{u} is



if perfect conductor.
 $\Gamma = -1$, $\gamma_2 = 0$, $\tau = 0$

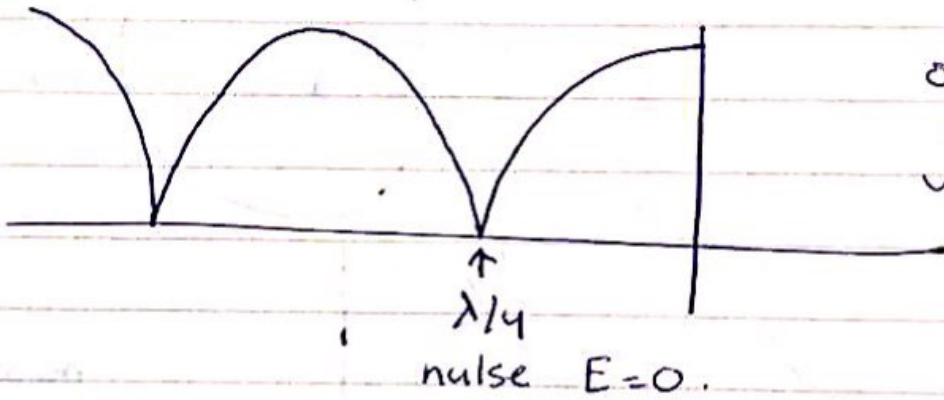


conductor
 $\gamma_2 = 0$
 (short ckt)



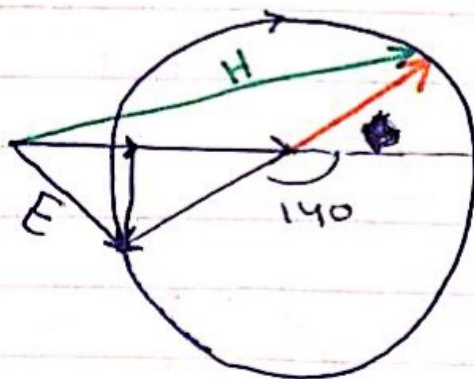
reflection coefficient $\neq -1 \neq 1$

perfect conductor

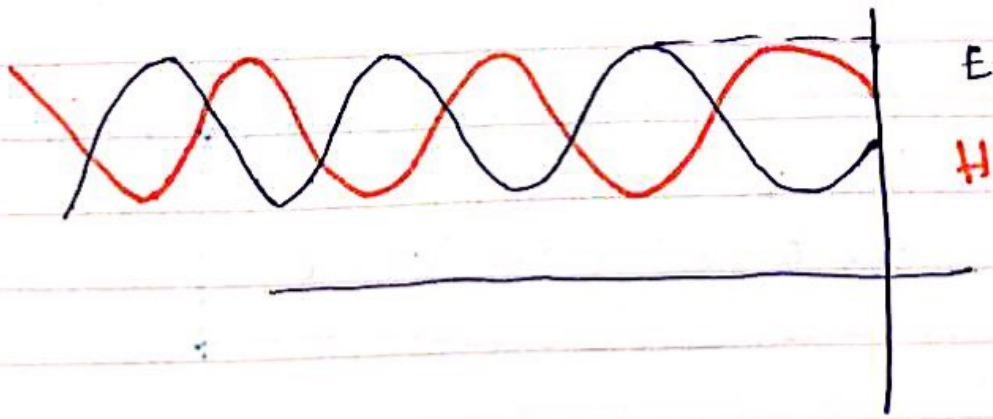


open circuit
 $\gamma_2 \rightarrow \infty$

$\lambda/4$ node $E=0$



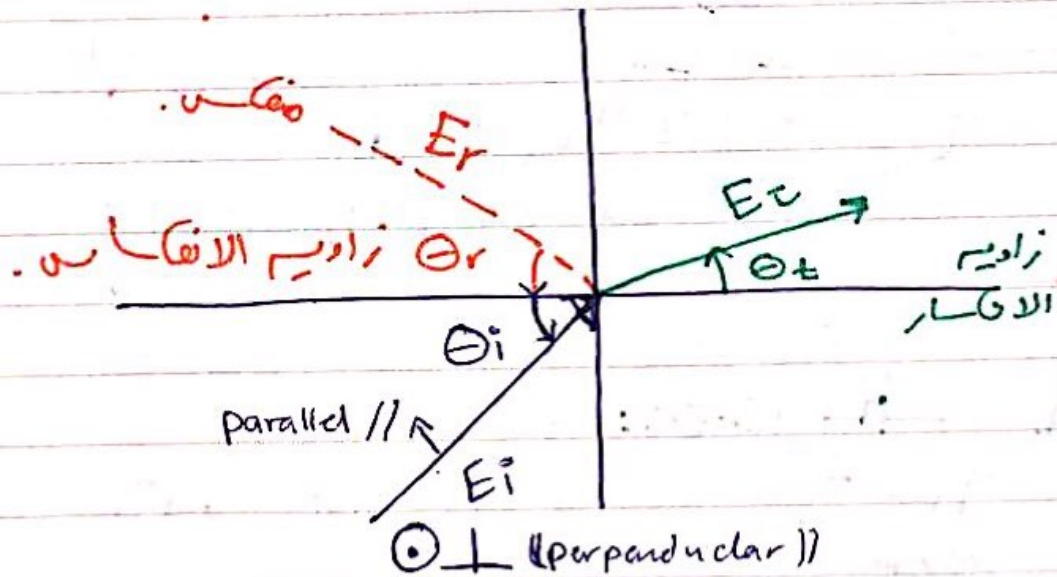
$H \perp E$ in space.



H reflection E.

stand wave H \propto \cos stand wave E

* Oblique Incidence Δ



$$n_1 \sin \theta_i = n_2 \sin \theta_t$$

$$n = \sqrt{\mu_r \epsilon_r}$$

\perp direction

$$\Gamma_{\perp} = \frac{\mu_2 \cos \theta_i - \mu_1 \cos \theta_t}{\mu_2 \cos \theta_i + \mu_1 \cos \theta_t}$$

$$\tau_{\perp} = \frac{2\mu_2 \cos \theta_i}{\mu_2 \cos \theta_t + \mu_1 \cos \theta_i}$$

// 8 -

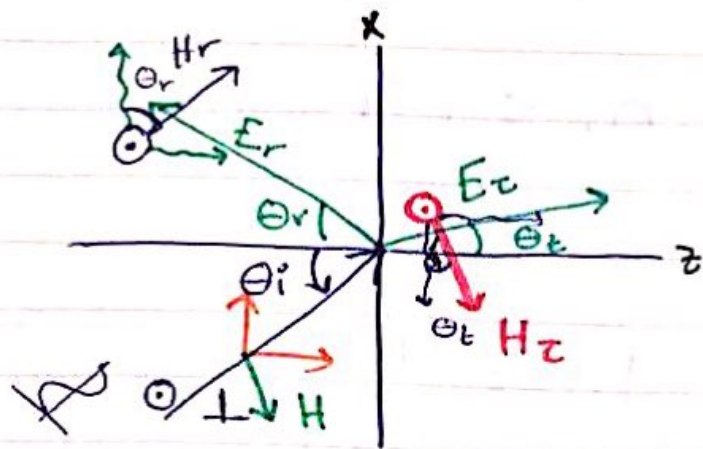
$$\Gamma_{\parallel} = \frac{\mu_2 \cos \theta_t - \mu_1 \cos \theta_i}{\mu_2 \cos \theta_t + \mu_1 \cos \theta_i}$$

$$\tau_{\parallel} = \frac{2\mu_2 \cos \theta_i}{\mu_2 \cos \theta_t + \mu_1 \cos \theta_i}$$

Ex - Case: -

$\mu_1 = 200$, $\mu_2 = 100$, $\theta_i = 30^\circ$

$\Gamma_{\perp} = ?!$



$$E_i = E_0 \cos(\omega t - Br) \hat{a}_y$$

34

propagation direction (زاویه انتشار)

$$\frac{2\pi}{\lambda} (\cos(\theta_i) z + \sin(\theta_i) x) = \beta = \frac{2\pi}{\lambda}$$

z axis
زاویه انتشار

x axis
زاویه انتشار

$$E_i = E_0 \cos(\omega t - \beta_1 (\cos(\theta_i) z + \sin(\theta_i) x)) \vec{a}_y$$



$$E_r = \Gamma_{\perp} E_0 \cos(\omega t - \beta_1 (-\cos(\theta_r) z + \sin(\theta_r) x)) \vec{a}_y$$

$$\epsilon_{r1} = 3.55 \rightarrow \gamma = \frac{\gamma_0}{\sqrt{\epsilon_r}} \Rightarrow \epsilon_r = \left(\frac{\gamma_0}{\gamma}\right)^2 = \left(\frac{120\pi}{200}\right)^2 = 3.55$$

$$\epsilon_{r2} = 14.2 \rightarrow \left(\frac{120\pi}{100}\right)^2 = 14.21$$

$$\sqrt{\epsilon_{r1}} \sin(30) = \sqrt{\epsilon_{r2}} \sin(\theta_t)$$

$$\sin \theta_t = \sqrt{\frac{3.55}{14.2}} \sin 30$$

$$\theta_t = 14.4^\circ$$

$$\Gamma_{\perp} = \frac{1 - \sqrt{\epsilon_{r2}} \sin \theta_t}{1 + \sqrt{\epsilon_{r2}} \sin \theta_t} = -0.38$$

$$\tau = 0.62$$

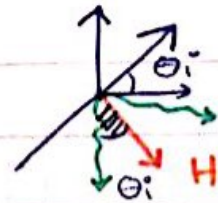
$\tau = 1 + \Gamma$ in \perp correct.

$\tau \neq 1 + \Gamma$ in \parallel

$$E_{\tau} = \tau E_0 \cos(\omega t - \sqrt{\frac{\epsilon_{r2}}{\epsilon_{r1}}} \beta_1 (\cos \theta_t z + \sin \theta_t x)) \vec{a}_y$$

Ex

⊙ E → y



$$H_i = \frac{E_0}{\eta_1} \cos(\omega t - \beta_1 (\cos \theta_i z + \sin \theta_i x))$$

$$* (-\cos \theta_i \vec{a}_x + \sin \theta_i \vec{a}_z)$$

$$H_r = \frac{\Gamma_1 E_0}{\eta_1} \cos(\omega t - \beta_1 (-\cos \theta_i z + \sin \theta_i x))$$

$$* (\cos \theta_r \vec{a}_x + \sin \theta_r \vec{a}_z)$$

$$H_{\tau} = \frac{\tau E_0}{\eta_2} \cos(\omega t - \beta_2 (\cos \theta_t z + \sin \theta_t x))$$

$$* (-\cos \theta_t \vec{a}_x + \sin \theta_t \vec{a}_z)$$

1/8/
Tue.

Ex

$$\eta_1 = 200 \rightsquigarrow \epsilon_{r1} = 3.5$$

$$\eta_2 = 300 \rightsquigarrow \epsilon_{r2} = 1.579$$

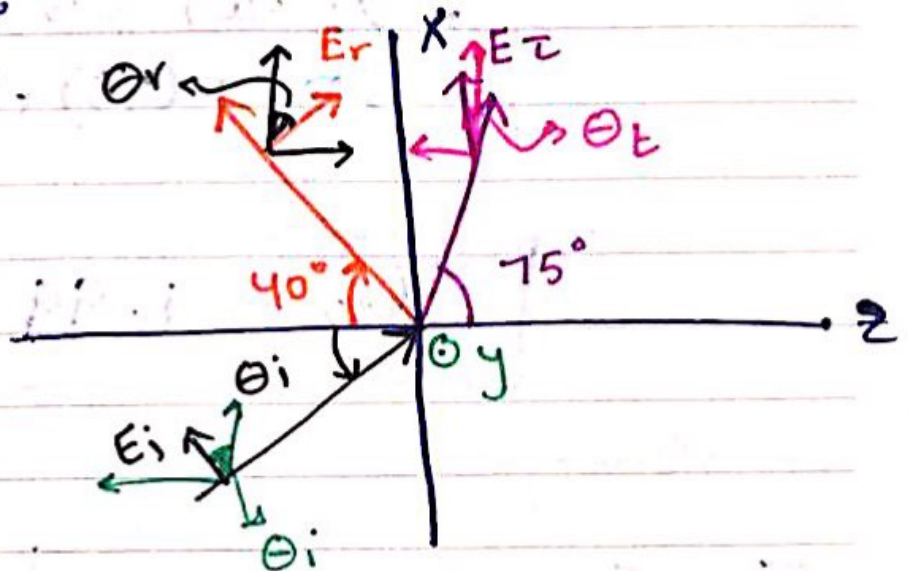
$f = 2.4 \text{ GHz}$ (freq for wireless)

$$\theta_i = 40^\circ$$

$$\eta = \eta_0 \sqrt{\frac{\mu_r}{\epsilon_r}}$$

$$\epsilon_{r1} = \left(\frac{\eta_0}{\eta_1} \right)^2$$

$$\epsilon_{r1} = 3.55$$



$$\sqrt{\epsilon_{r1}} \sin \theta_i = \sqrt{\epsilon_{r2}} \sin \theta_t$$

$$\sin \theta_t = \sqrt{\frac{\epsilon_{r1}}{\epsilon_{r2}}} \sin \theta_i$$

$$\theta_t = 75^\circ$$

$$\Gamma_{||} = \frac{\eta_2 \cos(75^\circ) - 200 \cos(40^\circ)}{300 \cos(75^\circ) + 200 \cos(40^\circ)}$$

$$\Gamma_{||} = -0.327$$

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$$\begin{aligned}
 T_{11} &= \frac{2 Y_2 \cos \theta_i}{Y_2 \cos \theta_e + Y_1 \cos \theta_i} \\
 &= \frac{2(300) \cos(40)}{300 \cos(75) + 200 \cos(40)}
 \end{aligned}$$

$$T_{11} = 1.99$$

$$* E_i = E_0 \cos\left(\omega t - \frac{2\pi * 100}{6.6} (\cos \theta_i z + \sin \theta_i x)\right)$$

* $(\cos \theta_i \vec{a}_x - \sin \theta_i \vec{a}_z)$

$$B_i = \frac{2\pi}{\lambda}$$

$$\lambda = ?$$

$$u_i = \frac{c}{\sqrt{\epsilon_r \mu_r}} \quad \text{if } \mu_r = 1$$

$$u_i = \frac{c}{\sqrt{\epsilon_r}} \Rightarrow \lambda = \frac{u}{f} = \frac{c}{\sqrt{\epsilon_r}} \cdot \frac{1}{f} \quad (38)$$

ARSA

$$\lambda_1 = \frac{3 \times 10^8}{\sqrt{3.55}} \cdot \frac{1}{2.4 \times 10^9} = 6.6 \text{ cm.}$$

$$\lambda_2 = \frac{3 \times 10^8}{\sqrt{1.57}} \cdot \frac{1}{2.4 \times 10^9} = 9.9 \text{ cm.}$$

* $E_r = ?!$ $\rightarrow E_r = \Gamma E_0 i$

$$E_r = -E_0 * 0.32 \cos\left(\omega t - \frac{2\pi * 100}{6.6} (-\cos\theta r z + \sin\theta r x)\right) * (\cos\theta r \vec{a}_x + \sin\theta r \vec{a}_z)$$

* $E_t = \tau E_0 i$

$$E_t = 1.99 E_0 \cos\left(\omega t - \frac{2\pi * 100}{9.9} (\cos\theta_t z + \sin\theta_t x)\right)$$

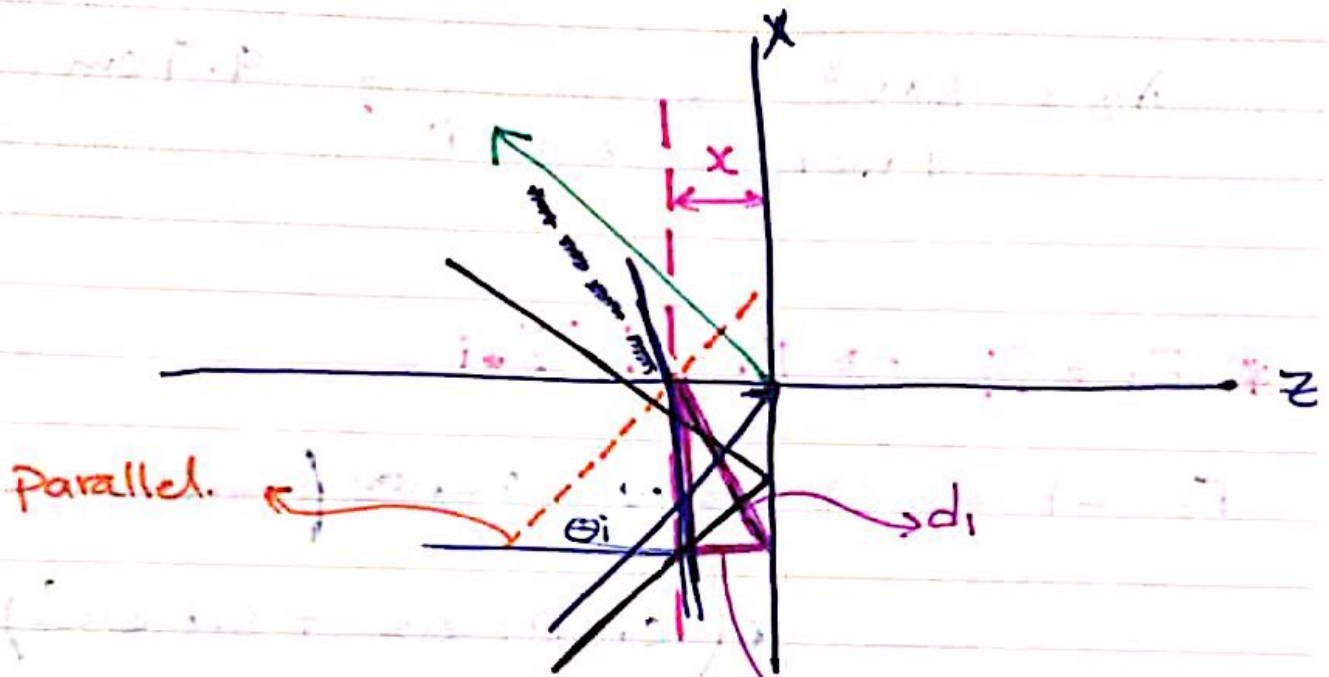
$$* (\cos\theta_t \vec{a}_x - \sin\theta_t \vec{a}_z)$$

$$\Rightarrow H_i = \frac{E_0}{\eta_1} \cos(\text{---}) \vec{a}_y$$

$$\Rightarrow H_r = \frac{E_0 * 0.32}{\eta_1} \cos(\text{---}) \vec{a}_y$$

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$$\Rightarrow H_z = \frac{1.99 E_0}{\gamma_2} \cos(\dots) \hat{a}_y$$



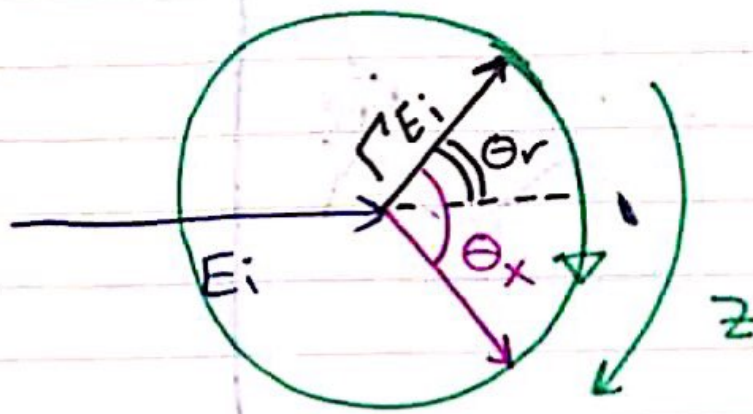
Phase shift btw $i_o r$ d_2

$$d_1 = \frac{z}{\cos \theta_i}$$

$$d_2 = d_1 - 2 \sin^2 \theta_i$$

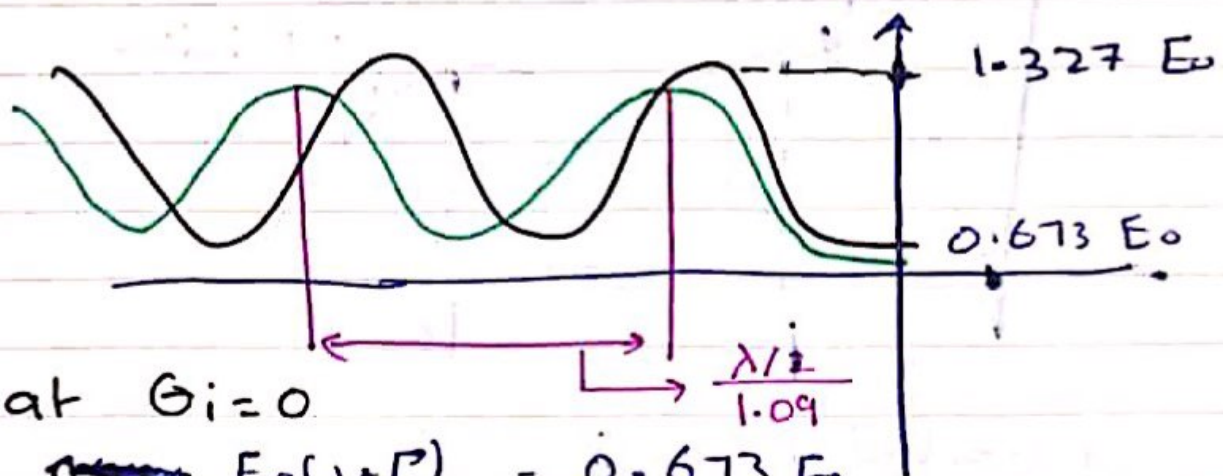
$$d_2 = \frac{z}{\cos \theta_i} - z \sin^2 \theta_i$$

5



$$\theta_x = (d_1 + d_2) * \frac{2\pi}{\lambda}$$

$$= z \left(\frac{2}{\cos \theta_i} - \frac{\sin^2 \theta_i}{2} \right) * \frac{2\pi}{\lambda}$$



at $\theta_i = 0$

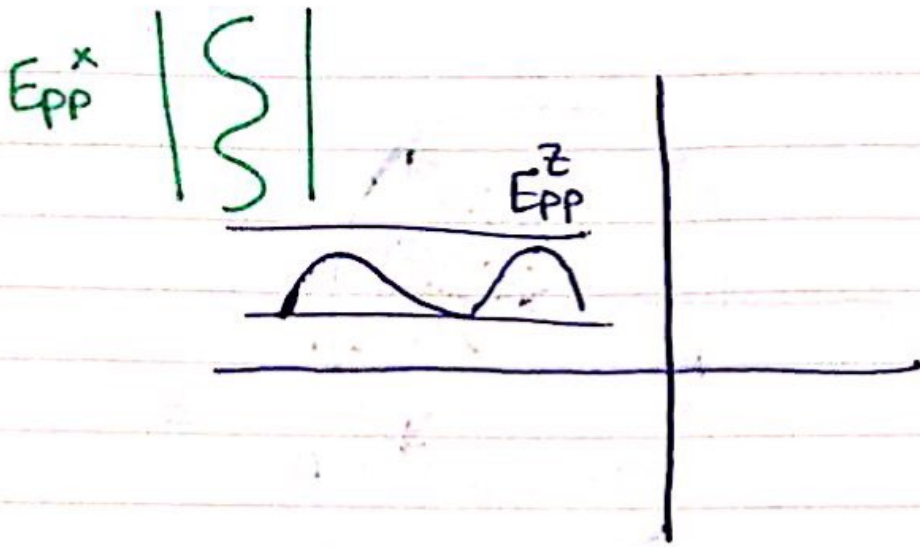
$$E_0(1 + P) = 0.673 E_0$$

$$E_0(1 - P) = 1.327$$

at $\theta_i = 40$

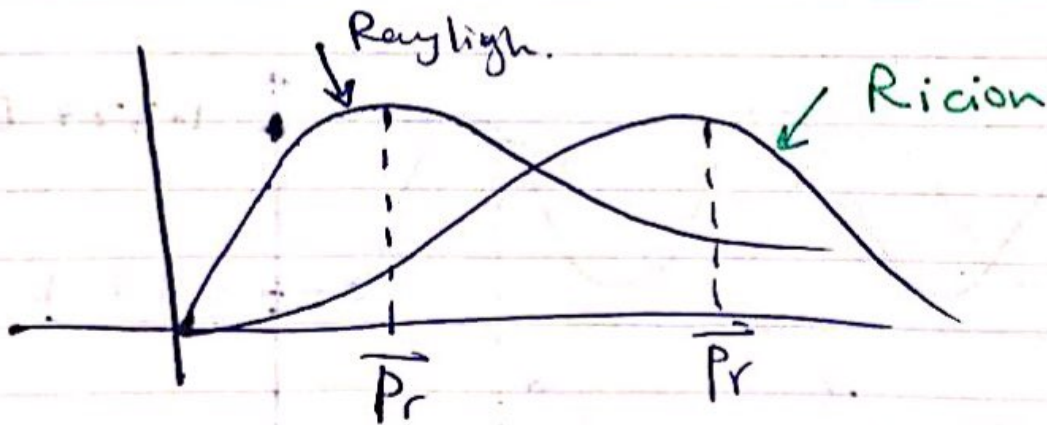
$$\left(\frac{1}{\cos \theta_i} - \frac{\sin^2 \theta_i}{2} \right) = 1.098 \Rightarrow \text{expanded}$$

91



$$\theta_i = \tan^{-1} \left(\frac{E_{PP}^x}{E_{PP}^z} \right)$$

Nulling \leftarrow ω is π or 2π or 4π *



reflected *

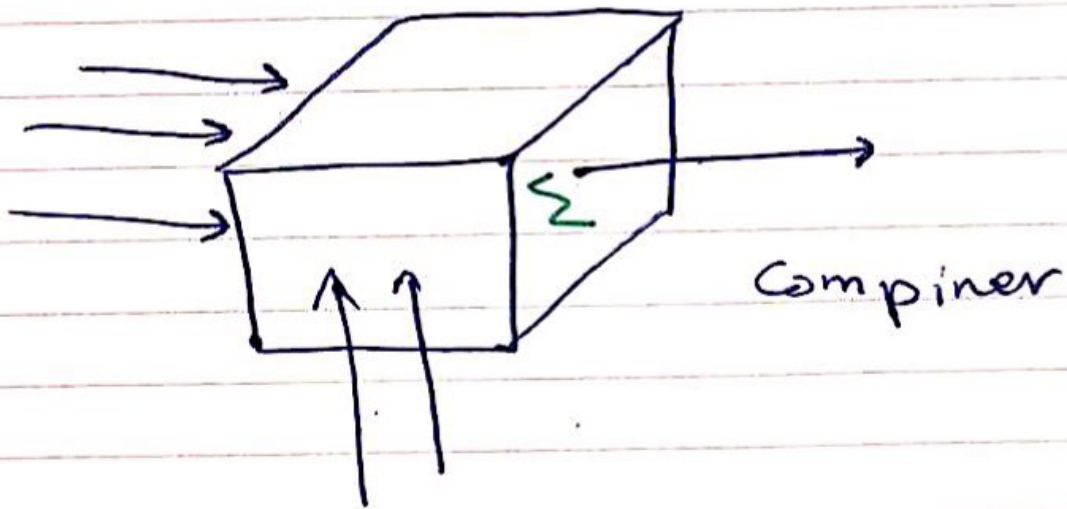
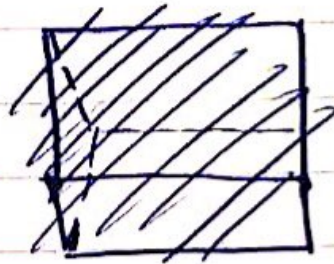
$$E_{r \text{ total}}(\text{space}) = \sum_{i=1}^N |\Gamma_i| E_0 e^{j\theta_i}$$

delay \leftarrow

$(\omega t - \beta r)$ \leftarrow ω is π

$$H(z) = \sum |r_i| z^{-i}$$

↳ in z transformer.



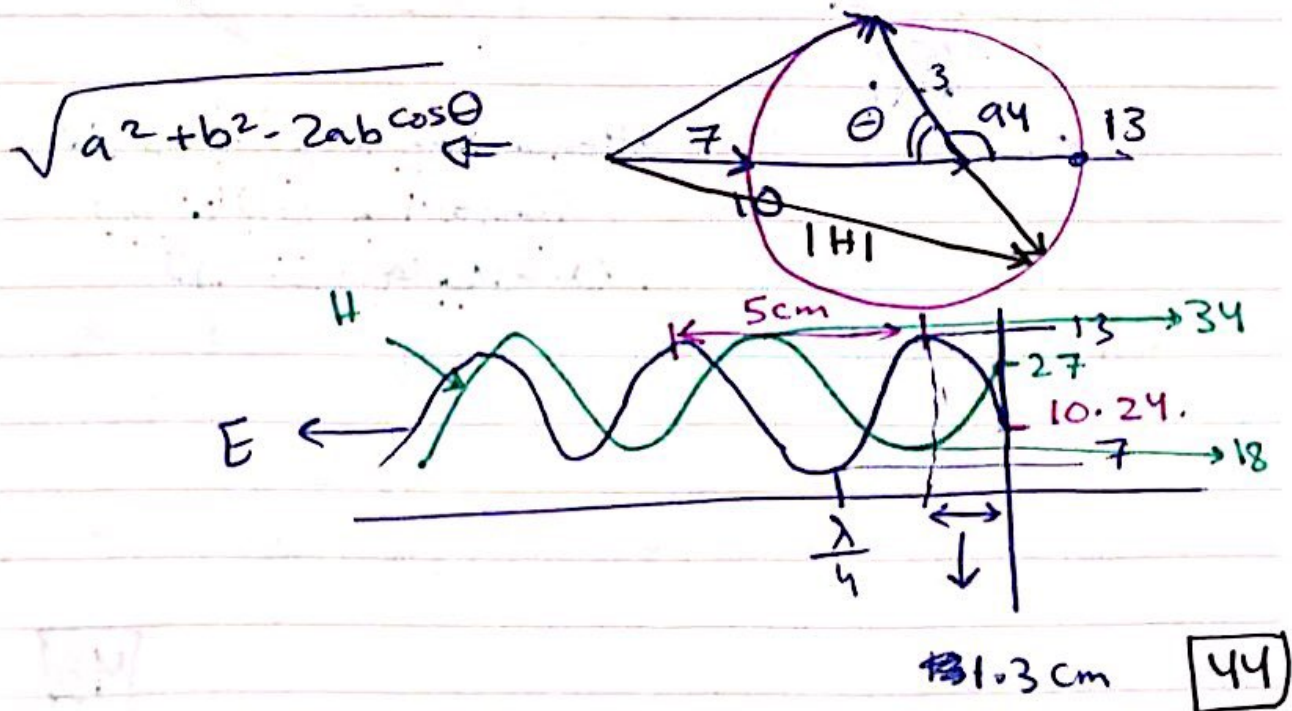
$$\tau_{\perp} = 1 + \Gamma_{\perp}$$

$$\tau_{\parallel} = (1 + \Gamma_{\parallel}) \frac{\cos \theta_i}{\cos \theta_t}$$

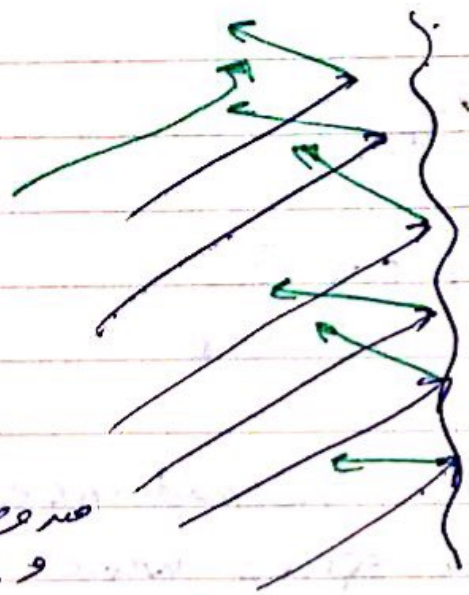
Quiz 2:

for normal incidence from free space wave into $\mu_2 = 300 + j200$; Draw the E & H standing waves $E_i = 10 \cos(\omega t - 20\pi z) \hat{a}_y$

Sol: $\Gamma = \frac{300 + 200j - 377}{300 + 200j + 377} = 0.3 \angle 94.6$

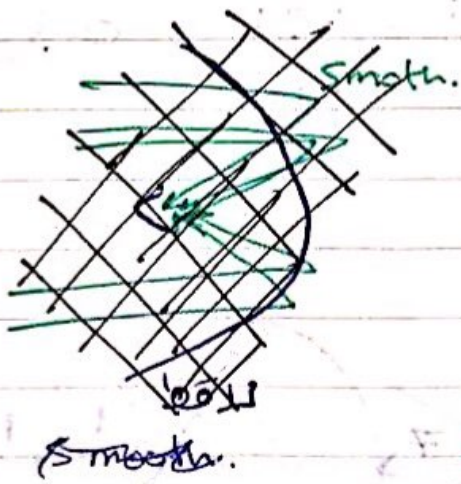


wave في
 random



wave incident.
 (far source)

if far source → far field. → wave propagation
 if near → near field.



attenuation في اتجاه
 scattering
 لكل نقطة

smooth and scattered.



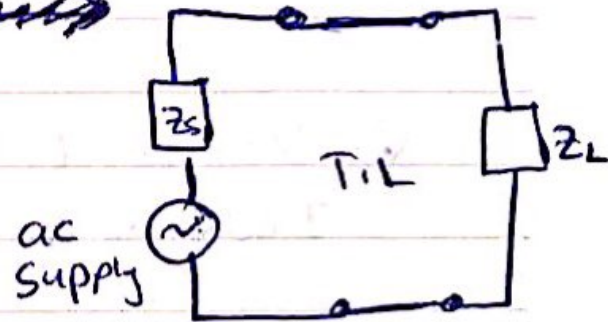
smooth signal

Transmission line :-

Signal track



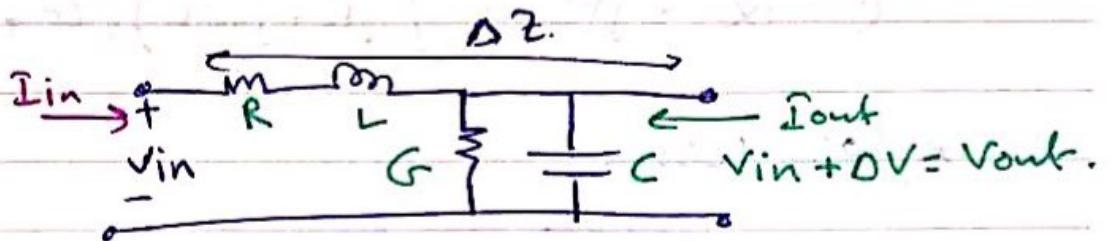
VCC
ground



equivalent
circuit
behaviour

all T.L we use lossless.

↳ 2 conductor circuit.



2 port network

$$\frac{\partial V(z)}{\partial z} = (R + j\omega L) I(z)$$

$$-\frac{\partial I(z)}{\partial z} = (G + j\omega C) V(z)$$

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Handwritten signature and a pink heart symbol.

20erse

$$\begin{aligned} \nabla^2 V &= \gamma^2 V \\ \nabla^2 I &= \gamma^2 I \end{aligned}$$

$$V = V_0 \cos(\omega t - \beta z)$$

2 conductor بين V و I لا يوافق ω في الالاتي ω

$$I = I_0 \cos(\omega t - \beta z)$$

$$\frac{V_0}{I_0} = Z_{T.L}$$

$$\gamma = \alpha + j\beta = \sqrt{(R + j\omega L)(G + j\omega C)}$$

* loss less :

$$\beta = \omega \sqrt{LC}$$

$$L = H/m$$

$$C = F/m$$

$$v = \frac{1}{\sqrt{LC}}$$

speed $< c$ (سرعة $< c$)

parameter.

$$Z_{T.L} = \sqrt{\frac{L}{C}}$$

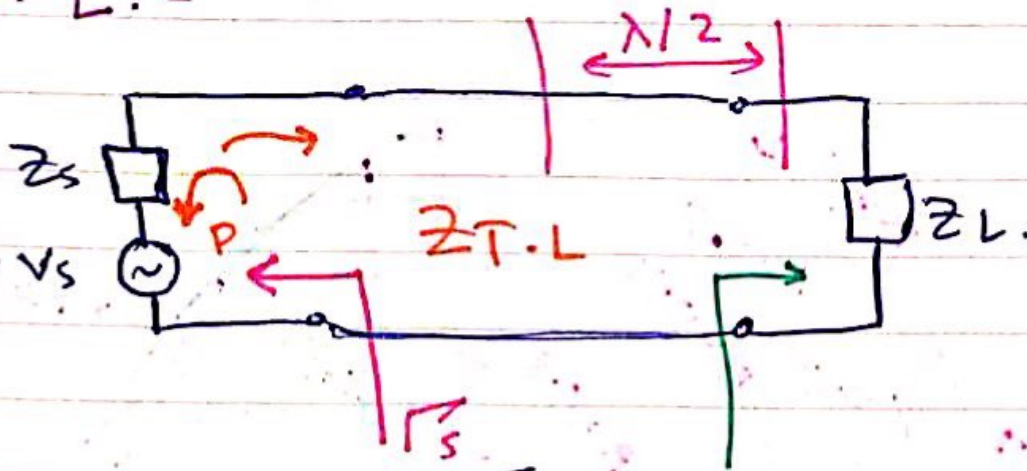
47

2020 erse

Mid (13/8) SUNDAY

3/8/
THU

T.L:-



$$\Rightarrow Z_{T.L} = \sqrt{\frac{L}{C}}$$

$$\Gamma_L = \frac{Z_L - Z_{T.L}}{Z_L + Z_{T.L}}$$

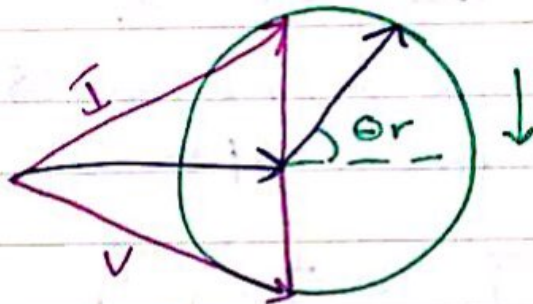
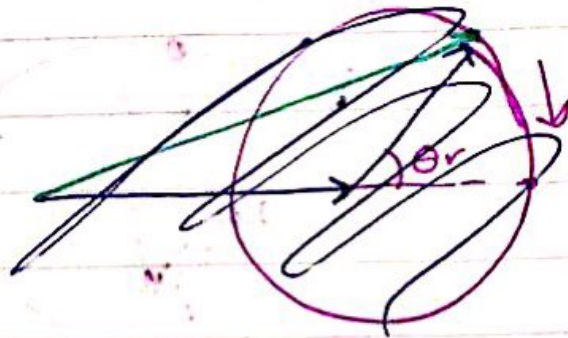
$$\Rightarrow u = \frac{1}{\sqrt{LC}}$$

$$\Rightarrow V_s = V_0 \cos(\omega t)$$

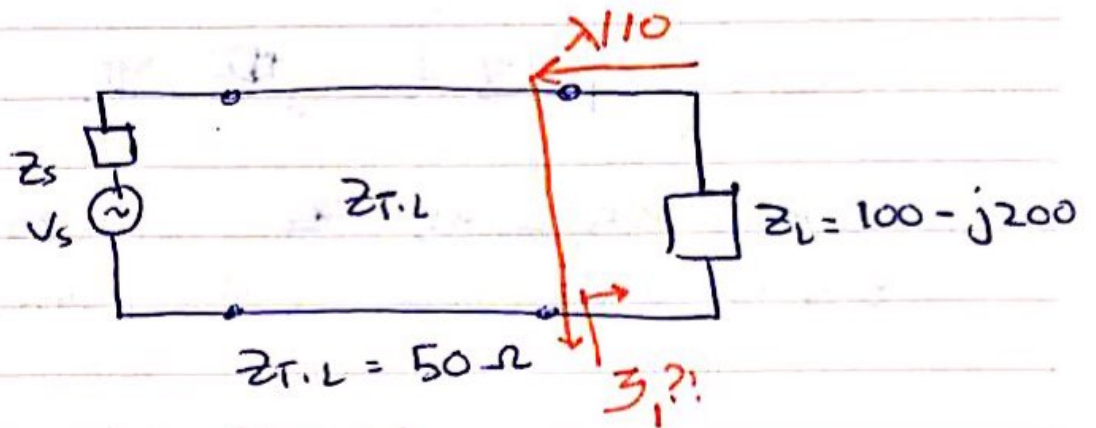
$$* \Gamma_s = \frac{Z_s - Z_{T.L}}{Z_s + Z_{T.L}}$$

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matching point center of T.L.



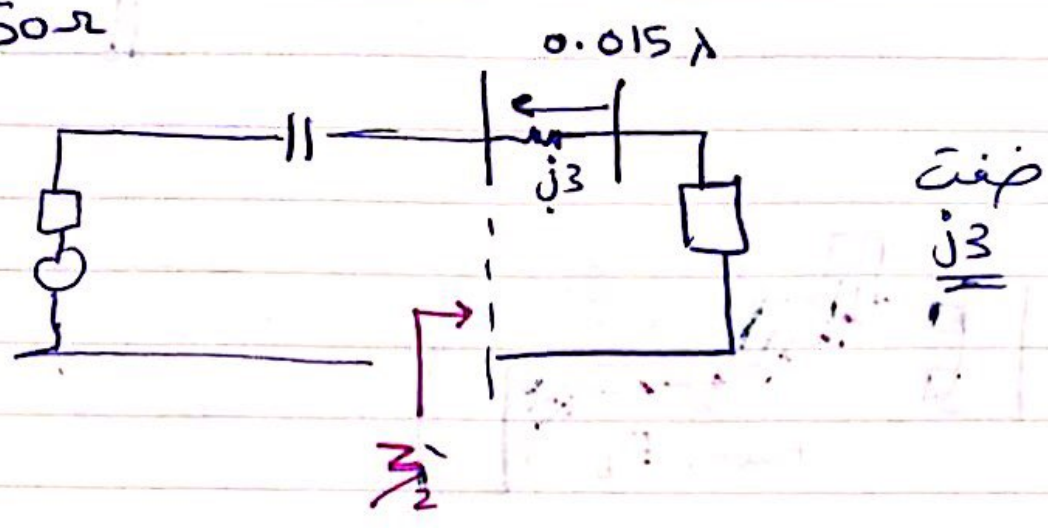
Ex1



T.L charging and discharging $Z_s C$

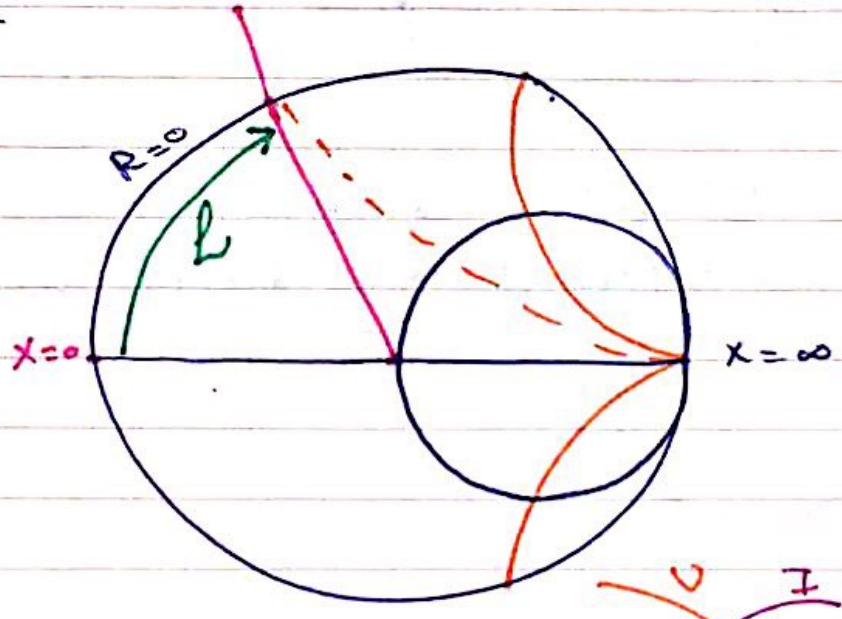
50

$Z_1' = 50 \Omega$

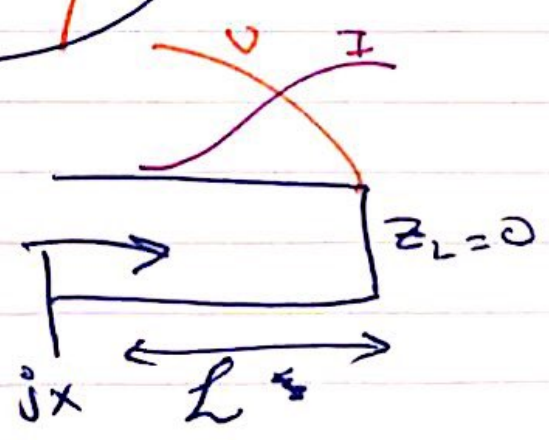


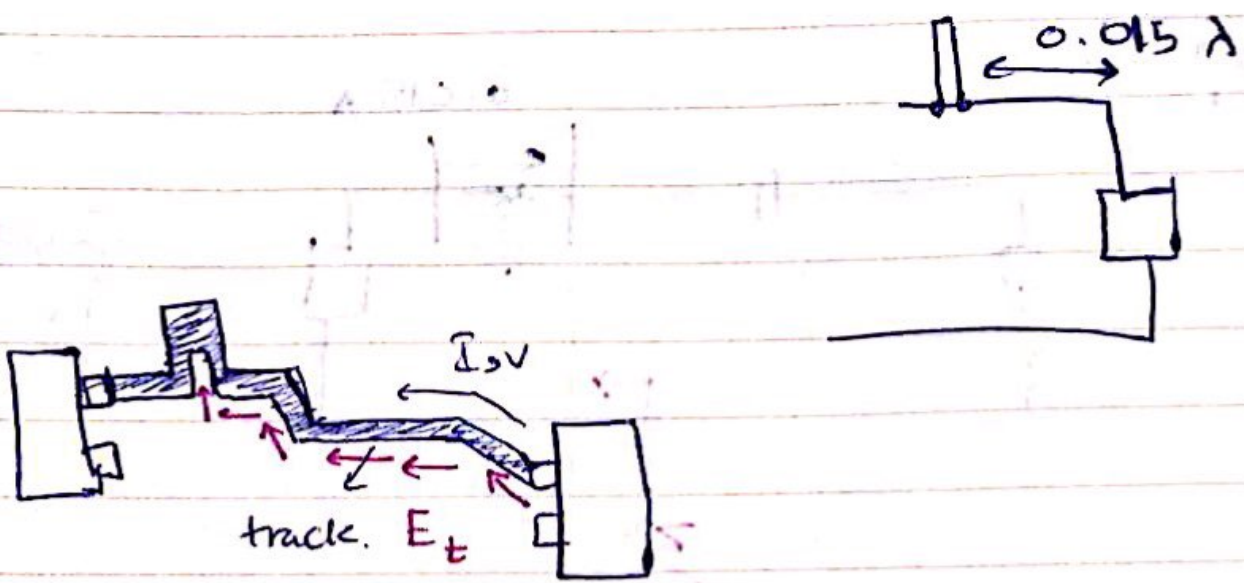
$\Gamma_2' = 1 \rightarrow Z = 50 \Omega$

Stub:

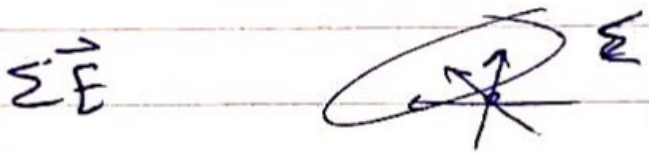


$jx = j3$
 $L = 0.198 \lambda$





$$\vec{J} = \nabla \times \vec{E}$$



DC path. اذا تاليري. $\lambda/4 \leftarrow$ SC و OC فرق بين

6/8/
50N

Ex

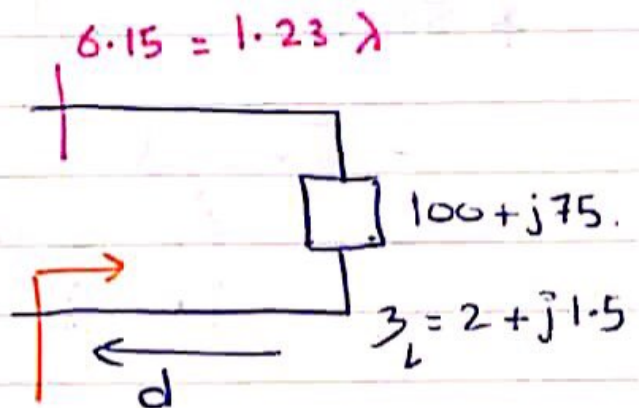
$$Z_L = 100 + j75$$

$$Z_{T.L} = 50 \Omega$$

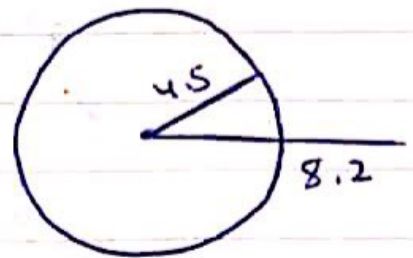
$$\lambda = 50 \text{ cm}$$

Find Z at 6.15 cm from load ?!

Sol:



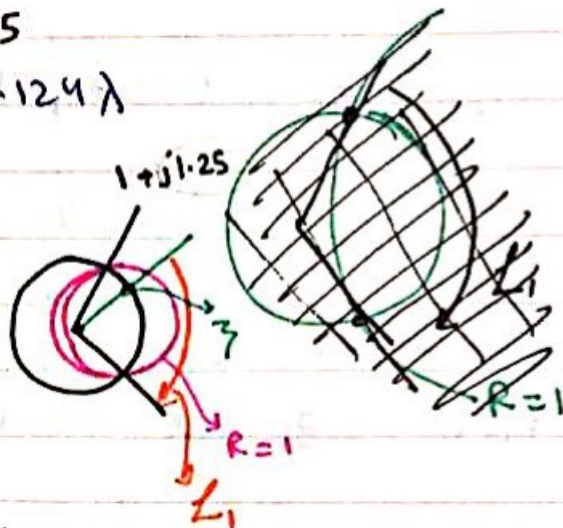
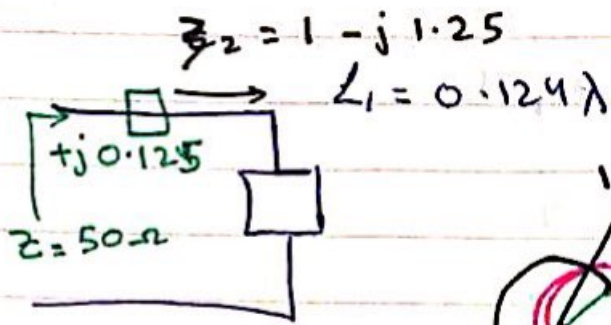
$$\frac{4.5}{8.2} = 0.54 \angle 30$$



$$Z_1 = 50 * (0.35 - j0.38)$$

$$Z_1 = 17.5 - j19$$

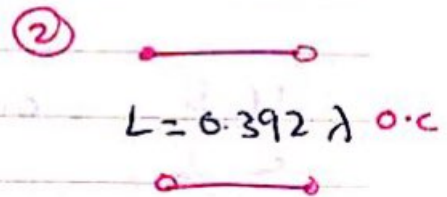
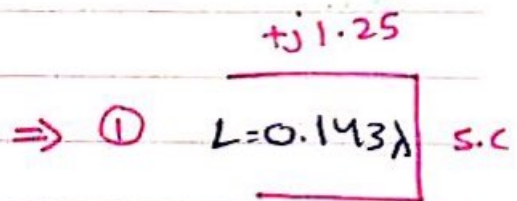
54



Case 1:

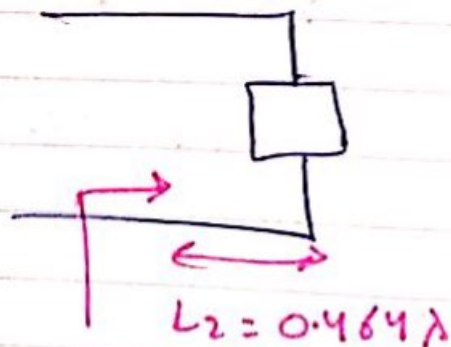
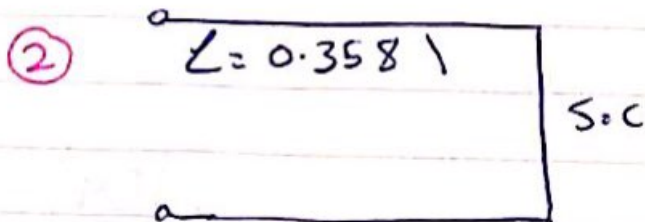
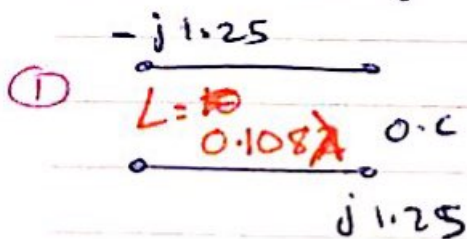
* Series Matching:

- Inductive:
 $L_1 = 0.124 \lambda$
 $(jX = j1.25)$

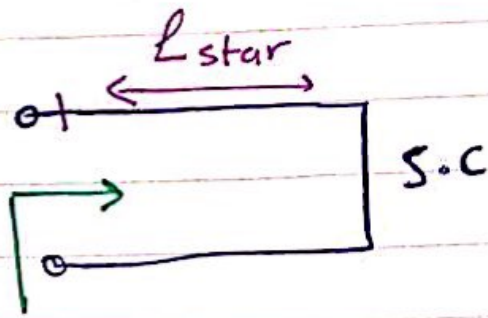


- Capacitive:

$L_2 = 0.464 \lambda$
 $jX = -j1.25$



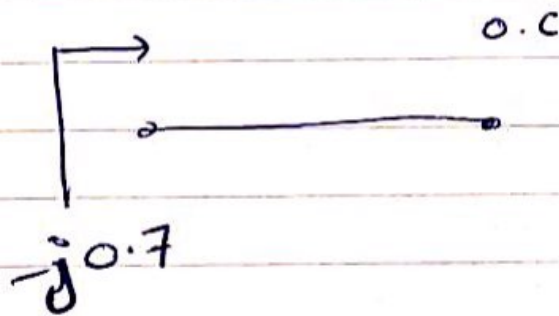
EX



$-j0.7$ (series capacitor \rightarrow (series inductor
freq))

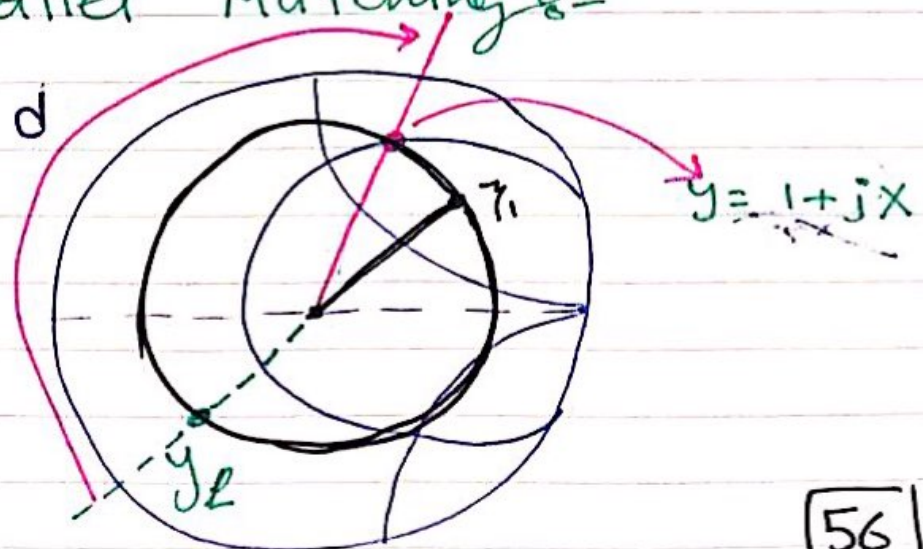
$L_{star} = \cancel{0.403} \lambda \quad 0.403 \lambda$

$L_{star} = 0.153$



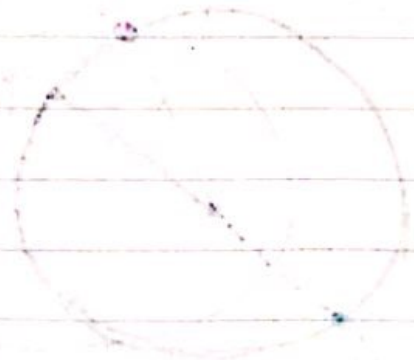
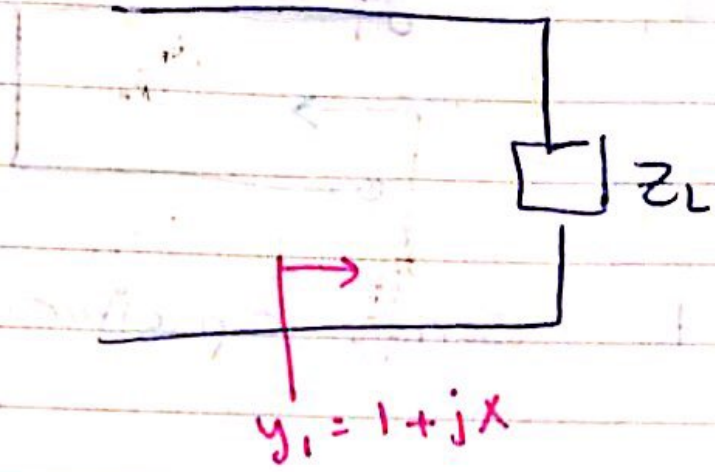
Case 2:-

* Parallel Matching:-

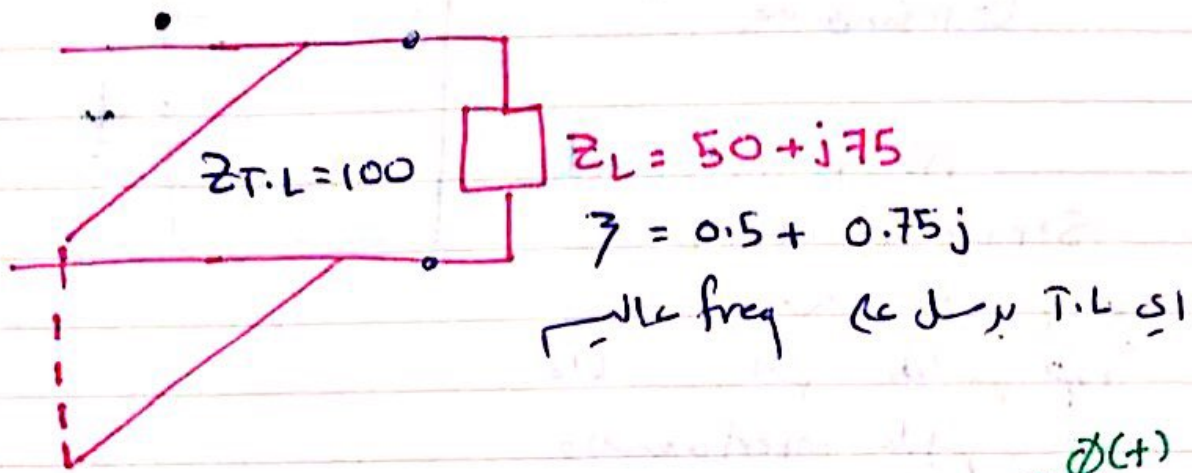


56

2020 erse

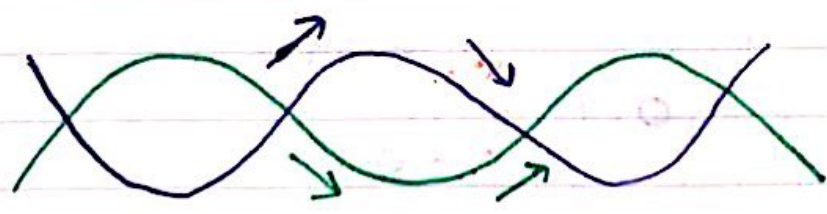
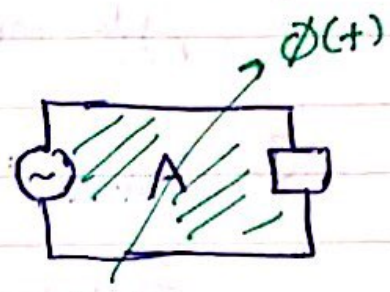


Parallel Matching :-



$$n(t) = \frac{\partial A \phi(t)}{\partial t}$$

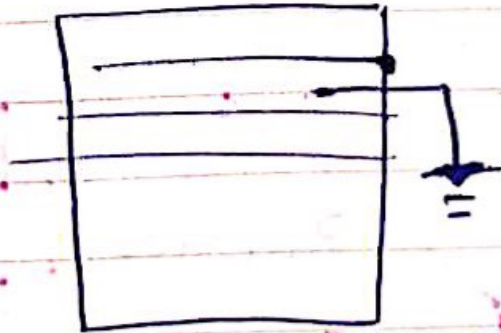
↳ [Interference]



They will almost cancelled each other and end up with Almost Zero interference.

* Another sol:-

Grounding



Strip و Strip
 thickness ال مع ال
 interference و

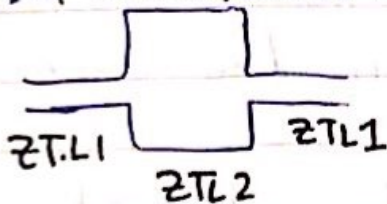
① $Y_{stub} = -j1.3$

$Z_{stub} = +j0.76$
 s.c. 0.102λ
 o.c. 0.352λ

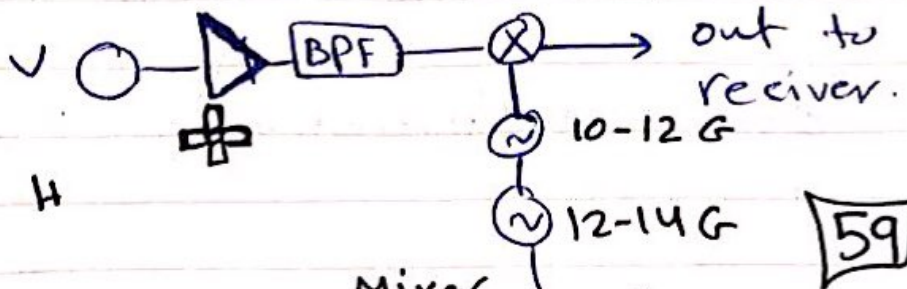
② $Y_{stub} = +1.3j$

$Z_{stub} = -j0.76$
 s.c. 0.398λ
 o.c. 0.148λ

$\lambda/4$ transformer



* L-M 7806 regulator



Mixer balanced

59



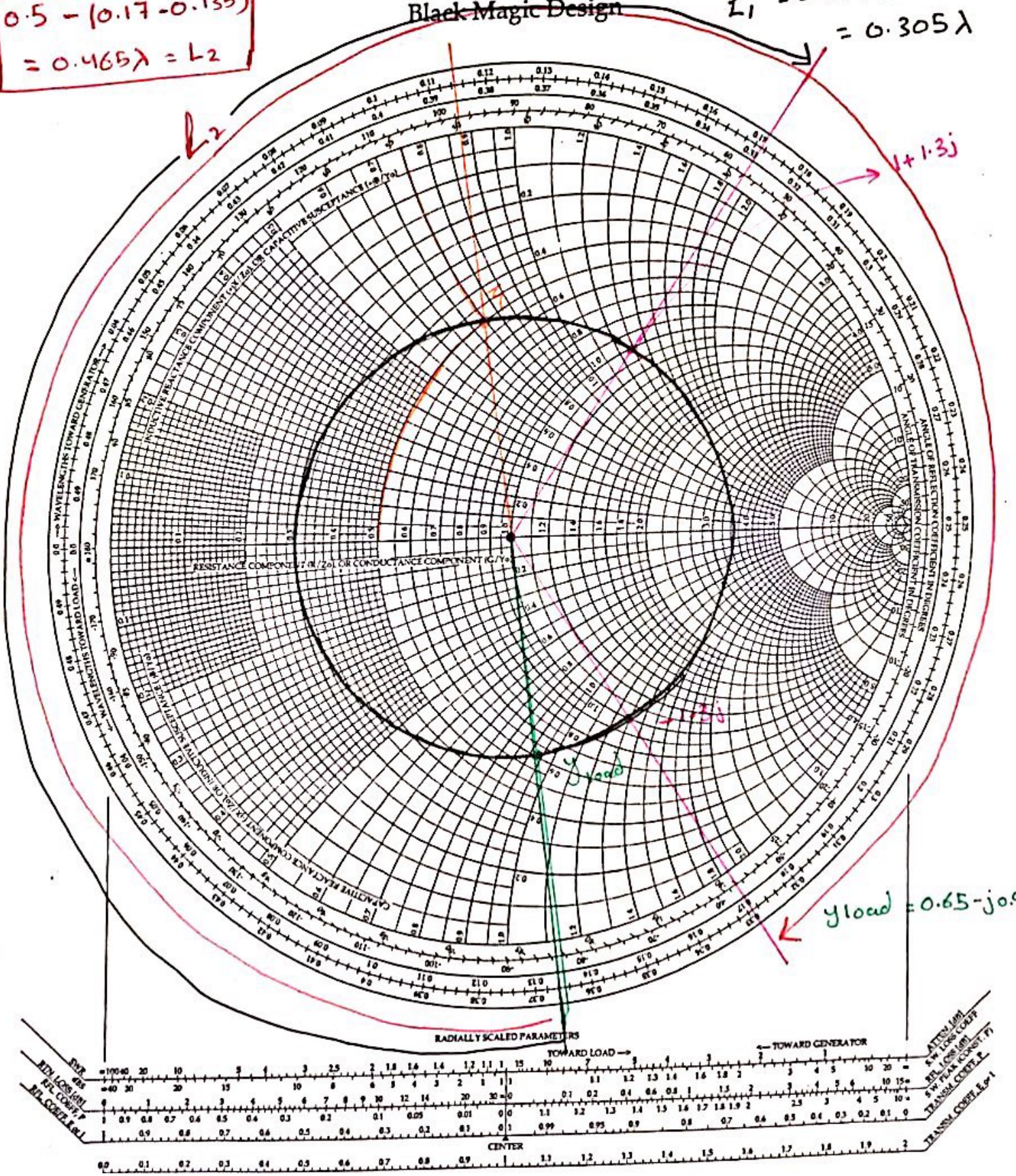
EX 7/8 MON

Parallel Matching

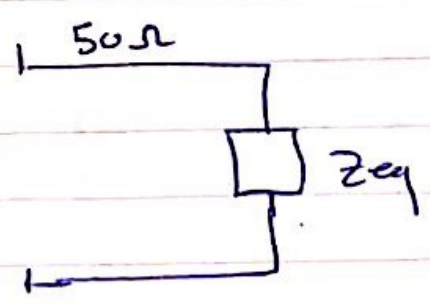
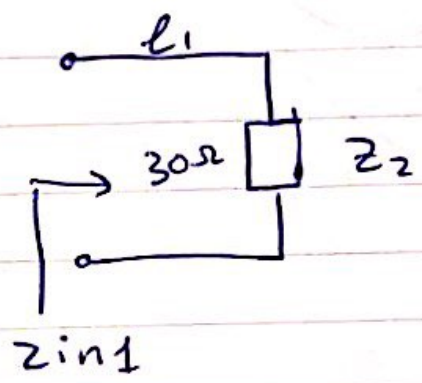
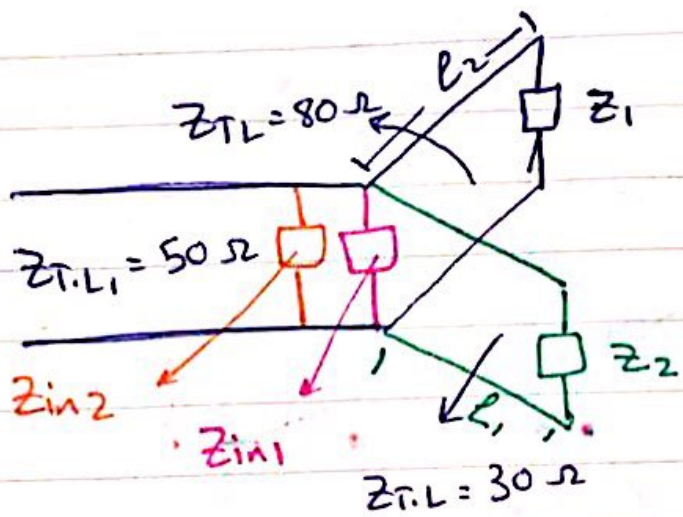
$0.5 - (0.17 - 0.135)$
 $= 0.465\lambda = L_2$

The Complete Smith Chart Black-Magic Design

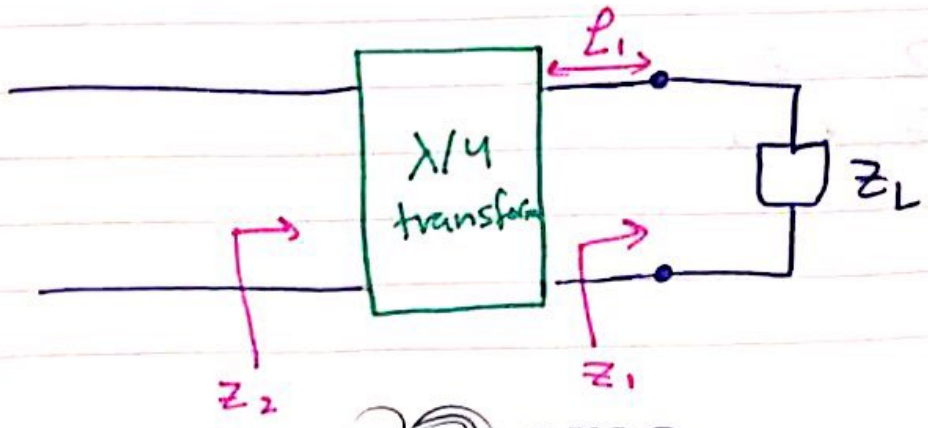
$L_1 = 0.17 + 0.135$
 $= 0.305\lambda$



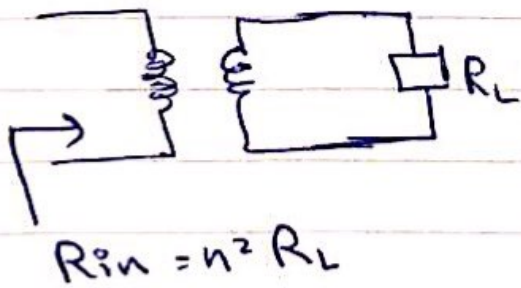
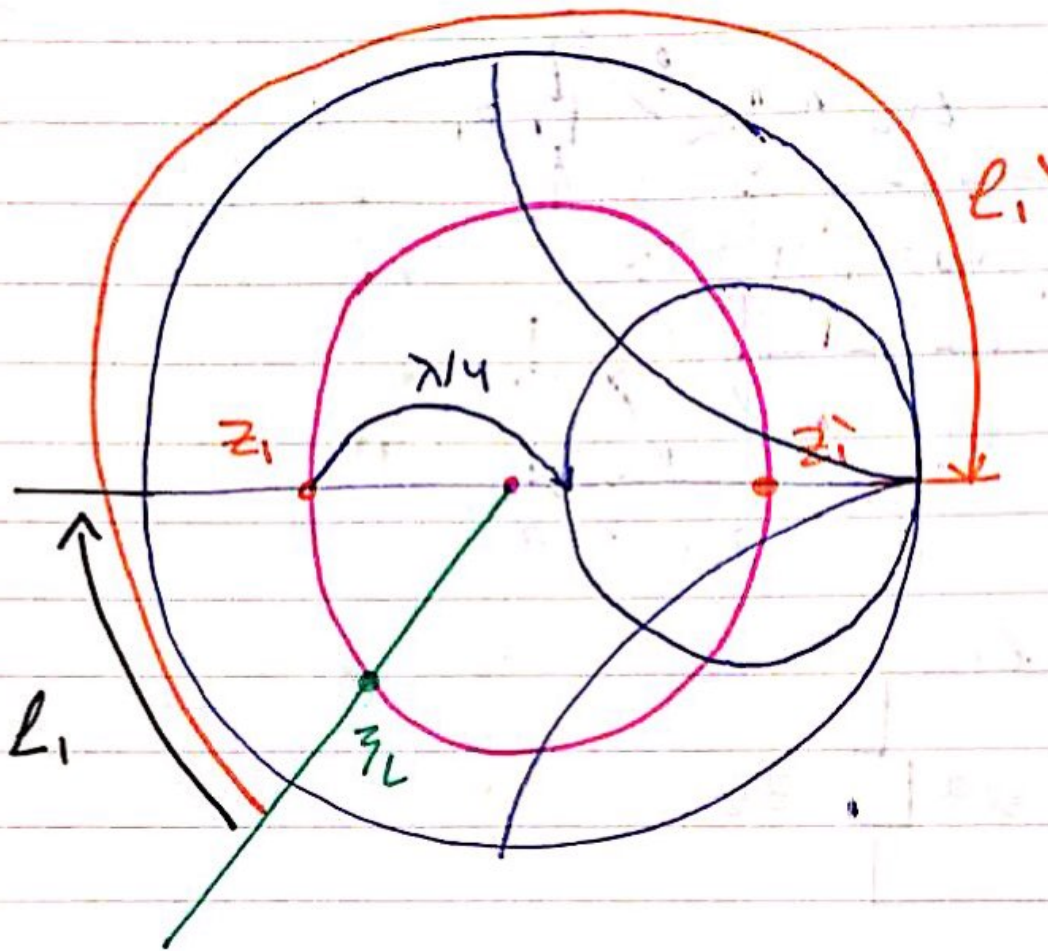
8/8/
Tue



* $\lambda/4$ Transformer:-



60

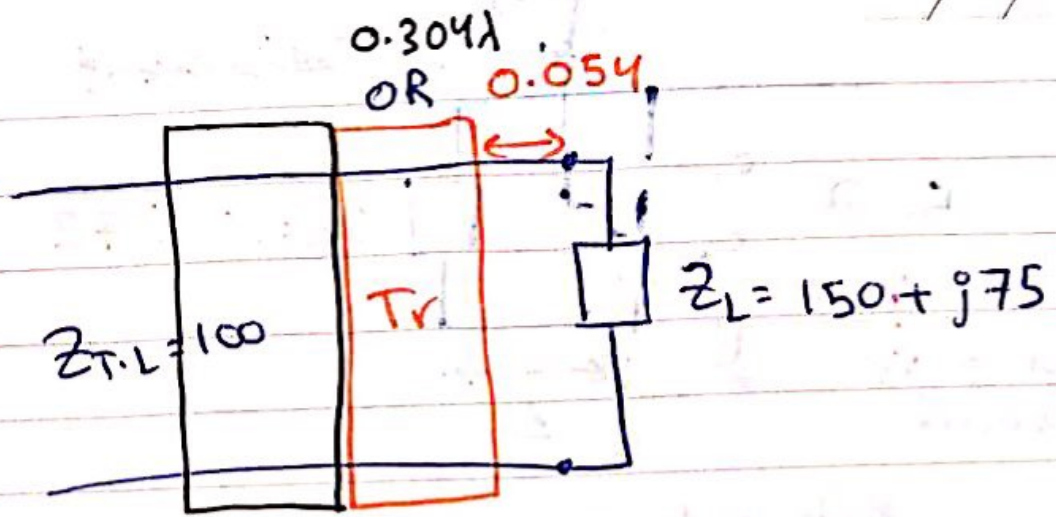


$$Z_{\lambda/4} = \sqrt{Z_2 \cdot Z_1}$$

$$Z_2 = Z_{T.L}$$

$$Z_1 = \text{real}$$

Ex 1



$$Z_L = 1.5 + j0.75$$

$$0.25 - 0.196 = 0.054 \lambda$$

$$Z_1 = 1.95$$

$$Z_1 = 195 \Omega$$

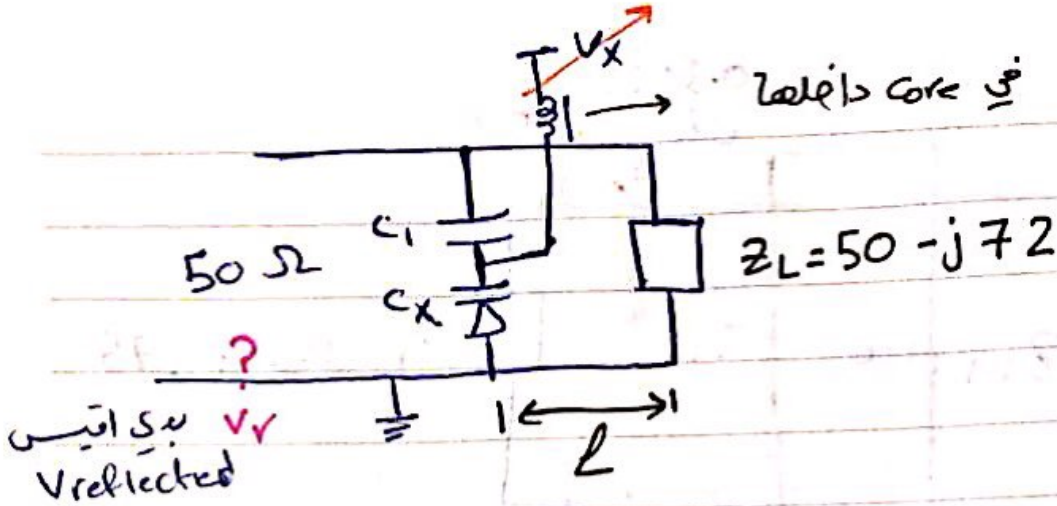
$$Z_{Tr} = \sqrt{100 * 195} = 139 \Omega$$

$$l_1' = 0.304 \lambda$$

$$Z_{Tr}' = \sqrt{100 * 50} = 70.7 \Omega$$

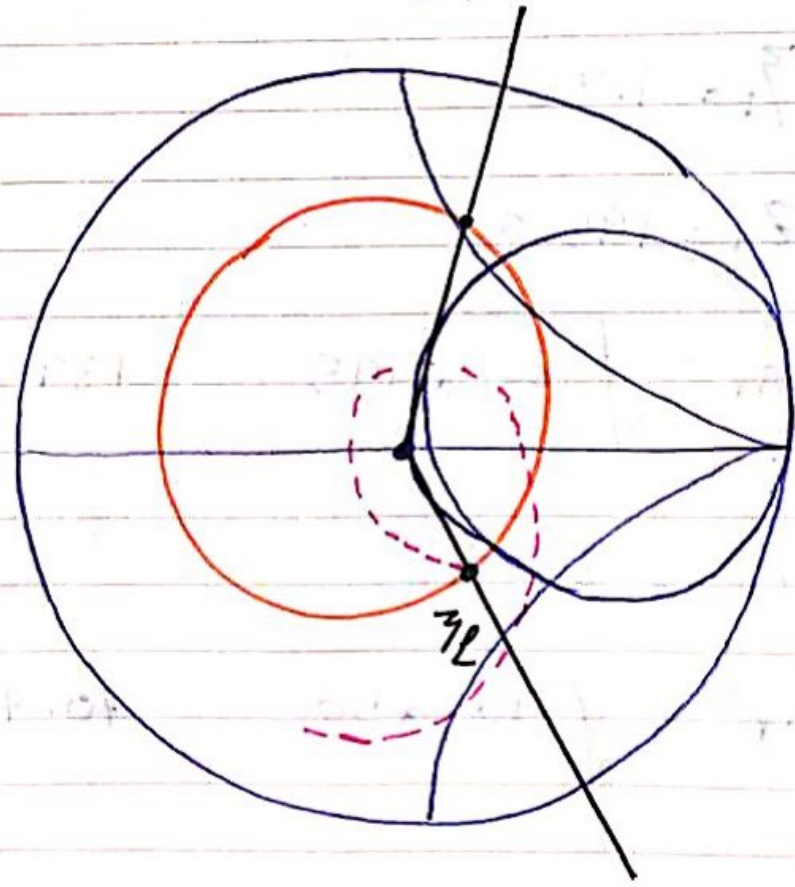
* Directional Coupler D.C :

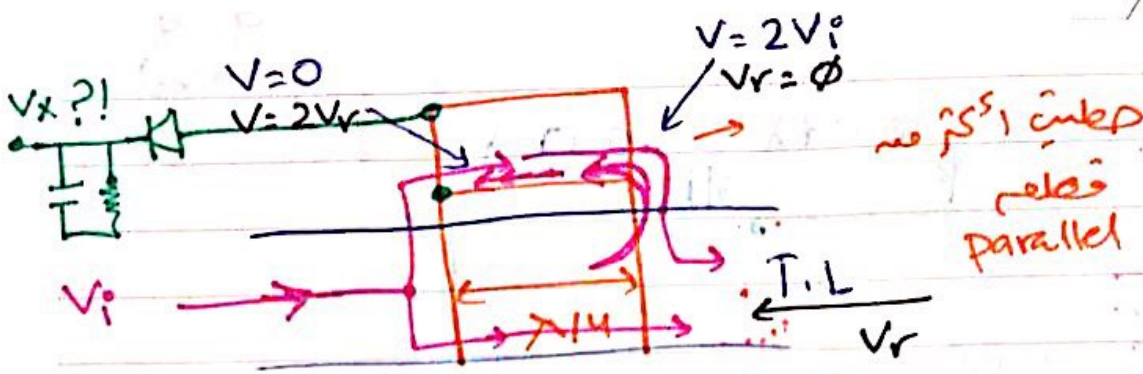
62



not a linear inductance we can't use for communication.

* بتوہم Capacitance بتوہم V_x

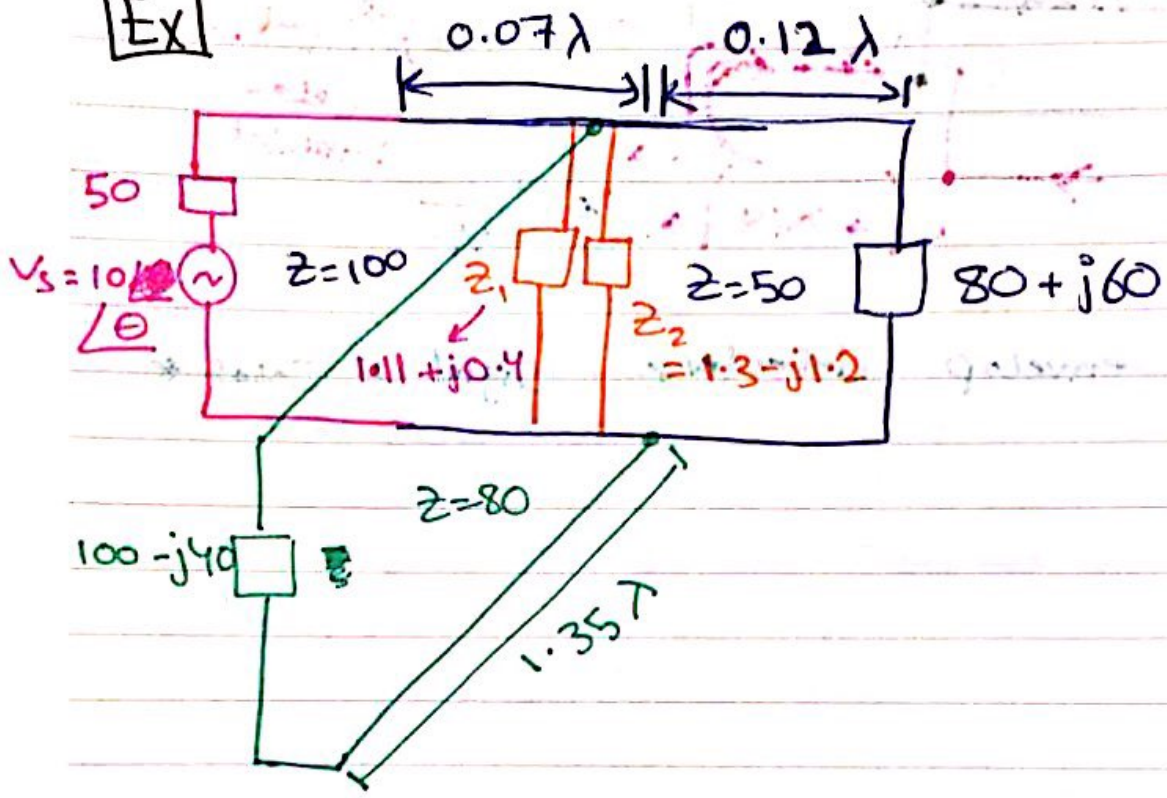




envelop detector ← signal w mas *

9/8/
Wed

Ex



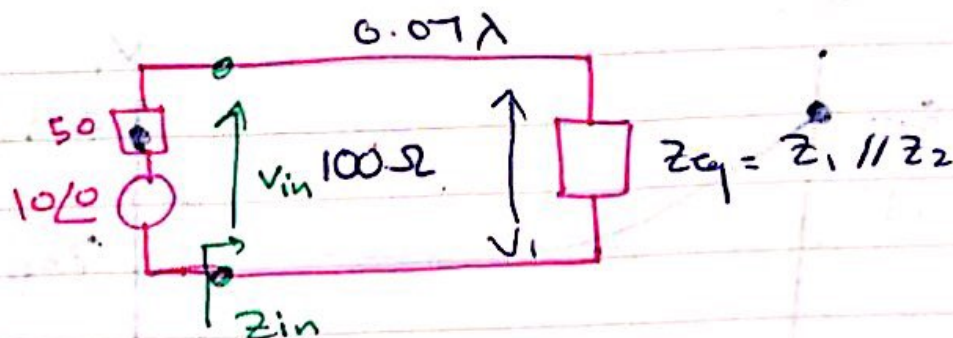
$$\frac{80 + j60}{50} = 1.6 + j1.2 \quad Z_1$$

$$\frac{100 - j40}{80} = 1.25 - j0.5 \quad Z_2$$

$$Z_2 = 65 - j60$$

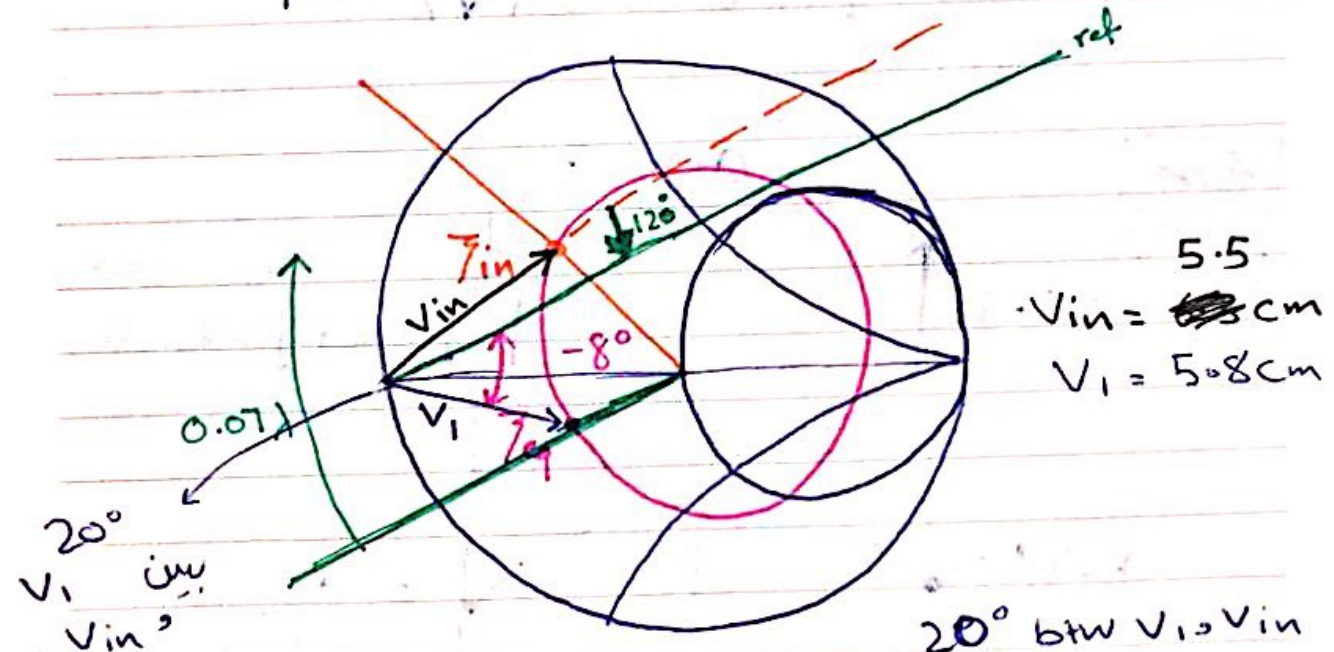
$$Z_1 = 88.8 + j32j$$

65



$$Z_{eq} = 52.13 - j11.6$$

$$\Gamma_{eq} = 0.52 - j0.11$$



$$V_{in} = 5.5 \text{ cm}$$

$$V_1 = 5.8 \text{ cm}$$

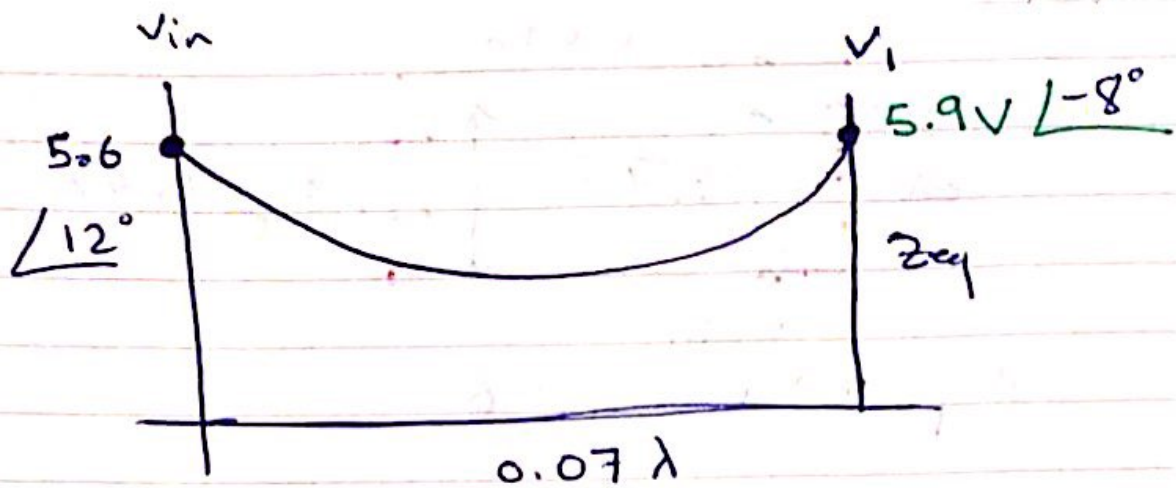
$$\Gamma_{in} = 0.55 + j0.28$$

20° btw V_1 و V_{in}
 الزاوية بين V_1 و ref
 $12 - 20 = -8^\circ$

$$Z_{in} = \Gamma_{in} * 100$$

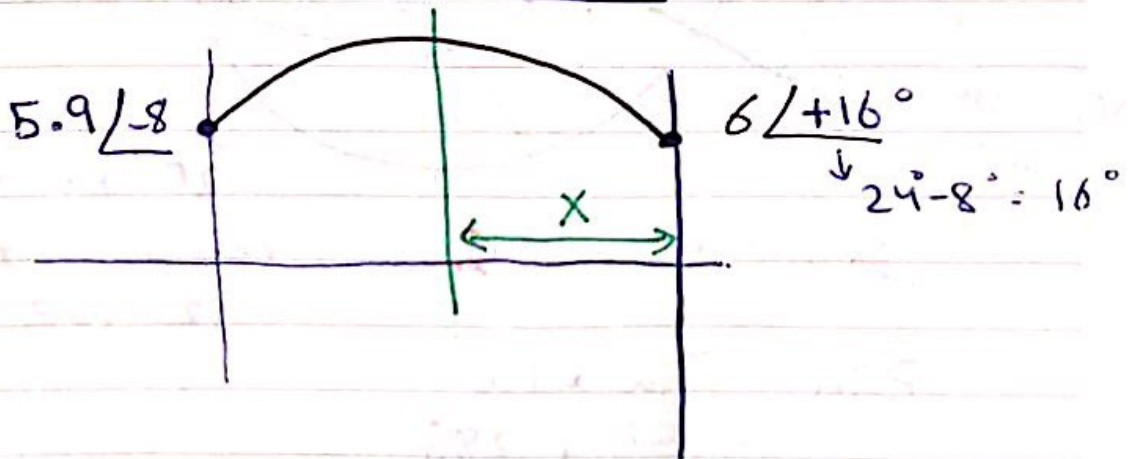
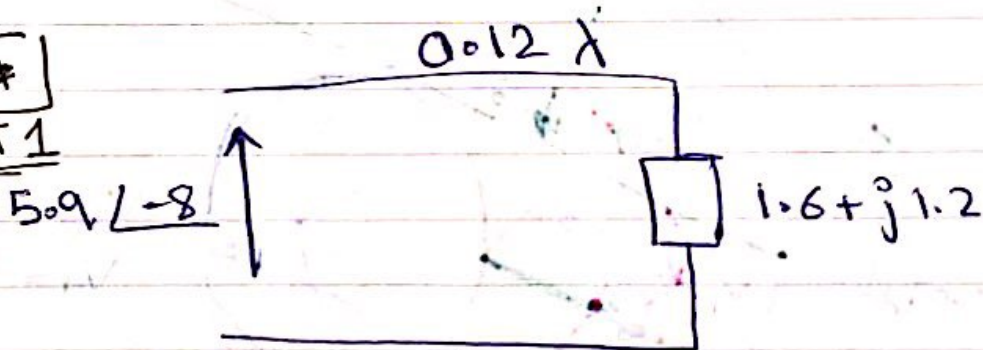
$$= 55 + 28j$$

$$V_{in} = \frac{10 \angle 0 * 55 + j28}{55 + j28 + 50} = 5.6 \angle 12^\circ$$



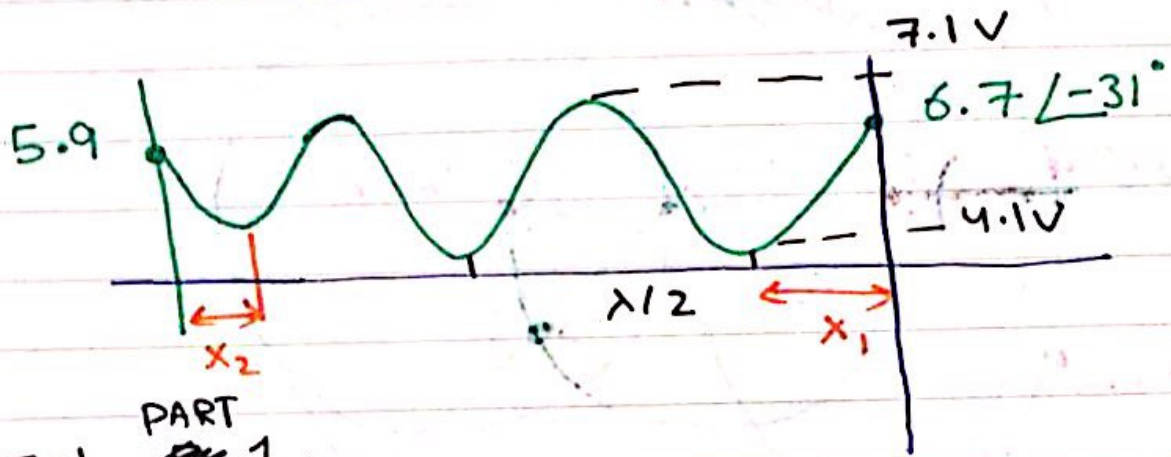
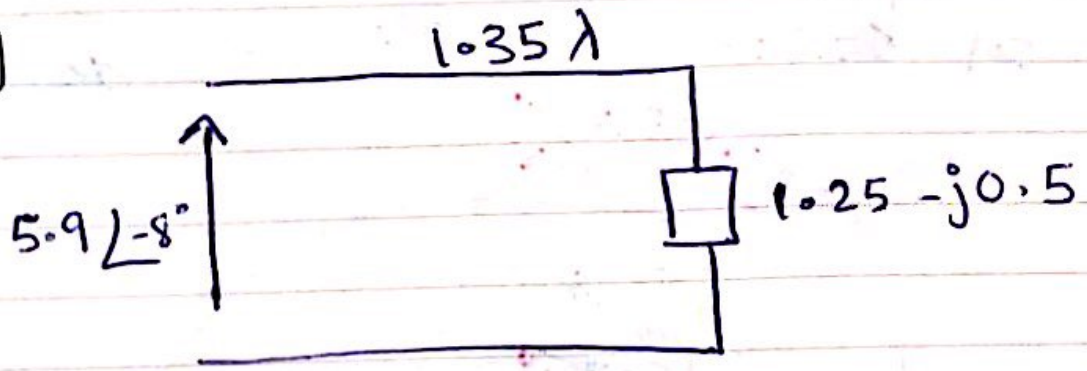
$$V_1 = \frac{5.8}{5.5} * 5.6 = 5.9V \angle -8^\circ$$

~~Part 1~~
PART 1



67

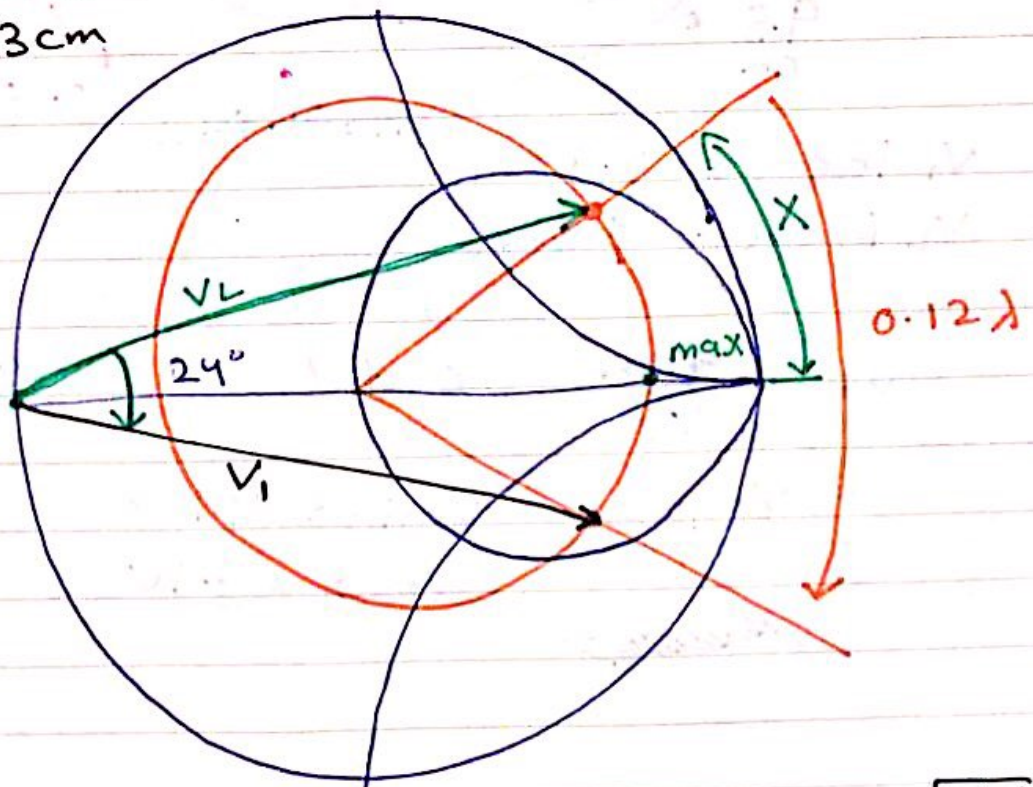
EX 2
PART



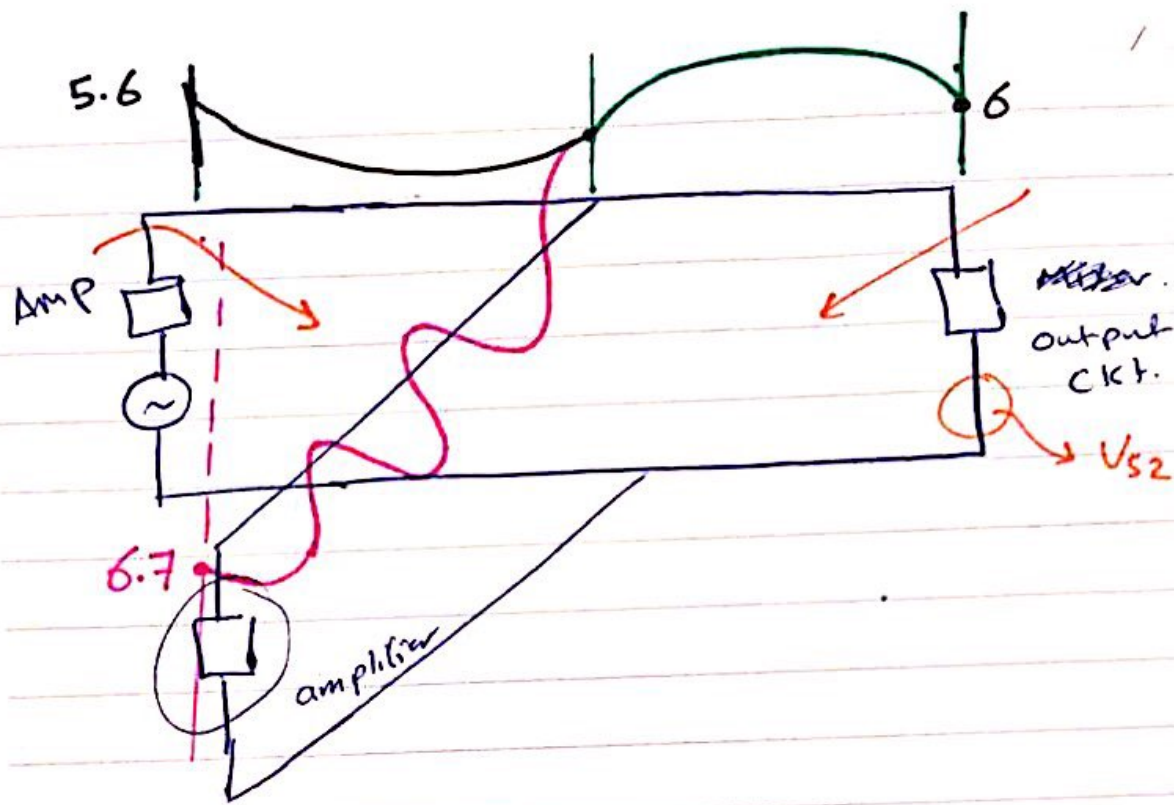
Sol PART 1 :-

$V_L = 10.9 \text{ cm}$

$V_1 = 10.3 \text{ cm}$



68

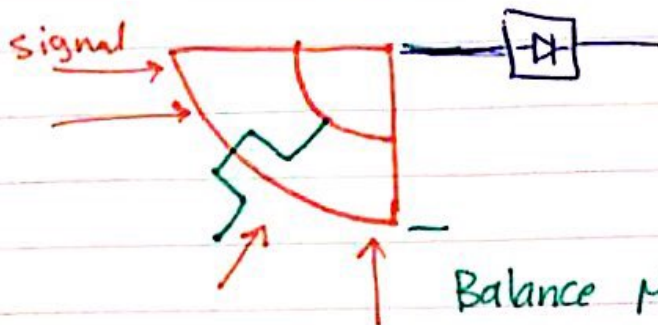


$$VSWR = \frac{V_{max}}{V_{min}}$$

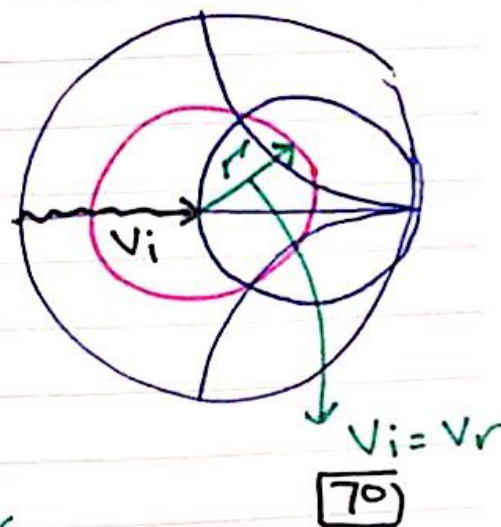
البرقنة و
الفرقنة
Ratio btw

$$VSWR = \frac{7.1}{4.1} = 1.73 \geq 1$$

$$VSWR = \frac{V_i + V_r}{V_i - V_r}$$



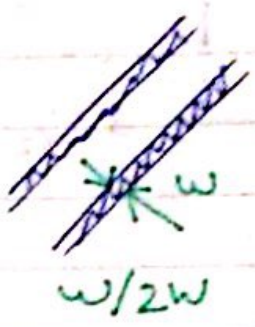
Balance Mixer



20_{sept}erse

10/8/19
Thur

In Inductive admittance $j\omega L = +ve$
 $Y = \frac{1}{jX} = -ve$ in parallel

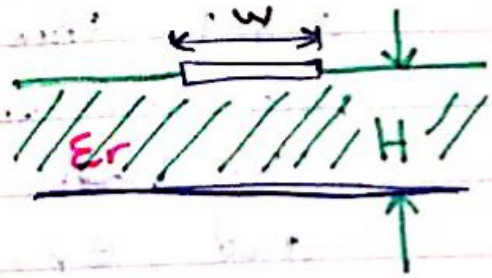


$w \rightarrow 2w$ is not a bus

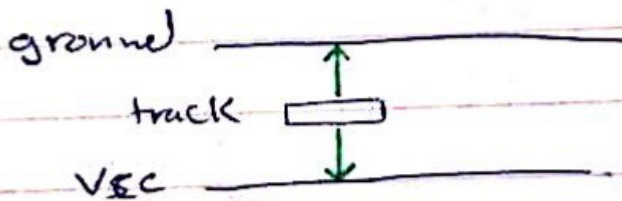
$w \rightarrow$ track
 \downarrow
ground

Micro strip:-

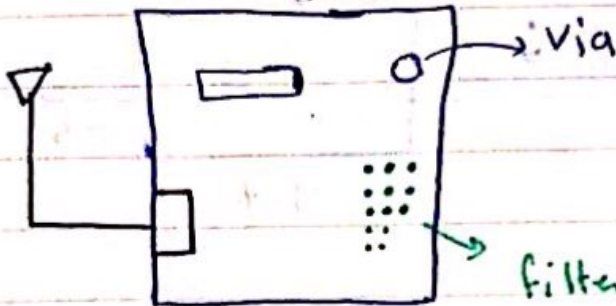
$$Z = \frac{377}{\sqrt{\epsilon_r} \left(\frac{W}{H} + 2 \right)}$$



H btw ground and track.



* FR4 $\Rightarrow \epsilon_r = 4.4$



\uparrow size \rightarrow \downarrow resonance freq.

Size $\propto \lambda$

filter to reject certain freq

Oscillator \Rightarrow freq $\uparrow \rightarrow$ there size \downarrow

16/8/
Wed

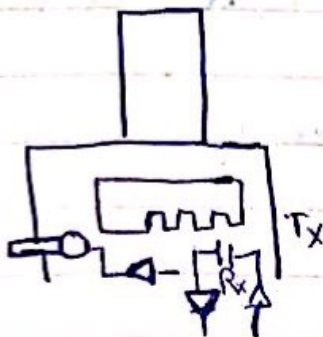
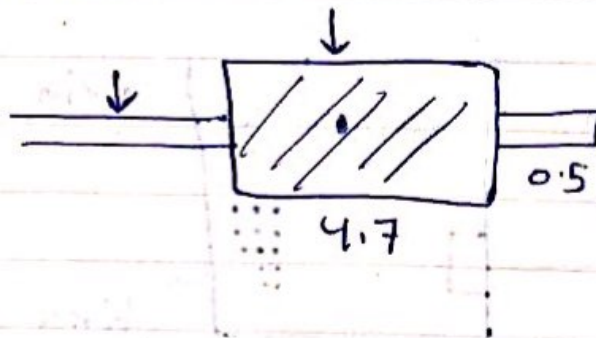
Quiz 5:-

a $\lambda/4$ transformer has $Z_{Tr} = \cancel{377} 35 \Omega$
find the width of the track if
the board height is 1.5 mm
and $\epsilon_r = 4.4$?

Sol:-

$$35 = \frac{377}{\sqrt{4.4} \left(\frac{w}{h} + 2 \right)}$$

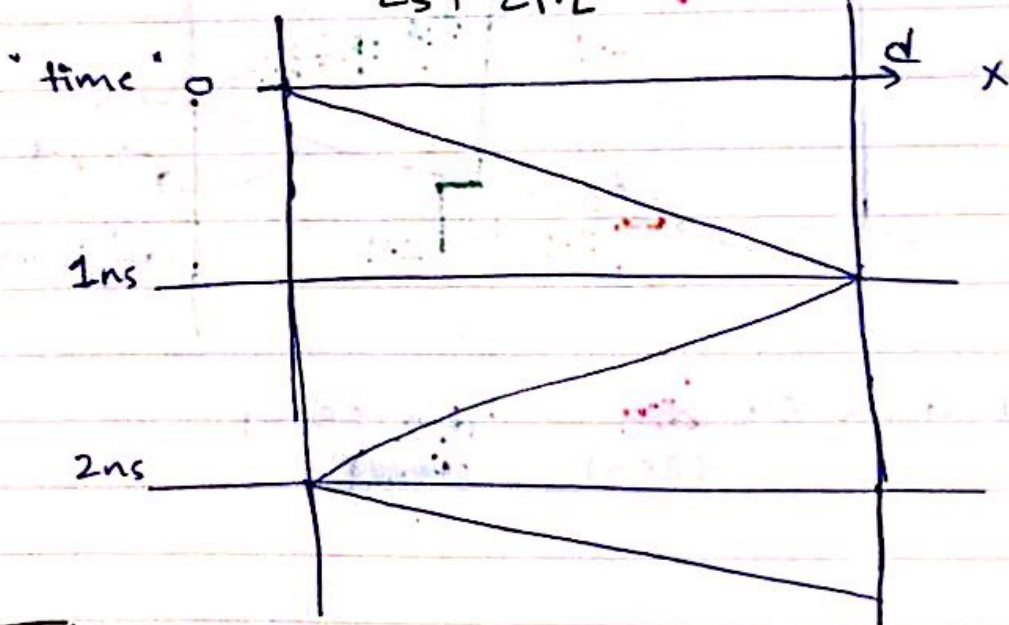
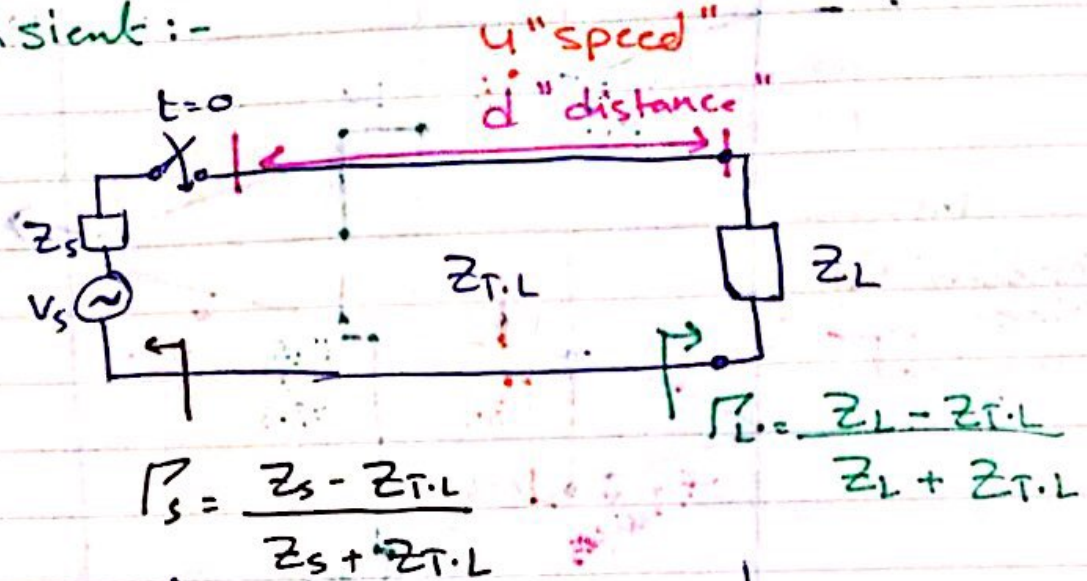
$$w = 4.7 \text{ mm.}$$



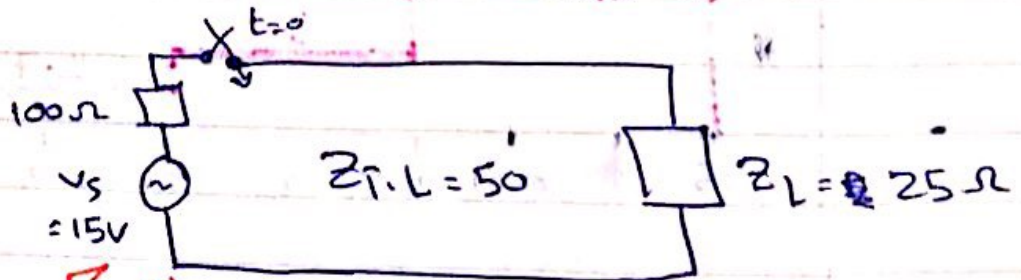
73

ARSO

* Transient :-



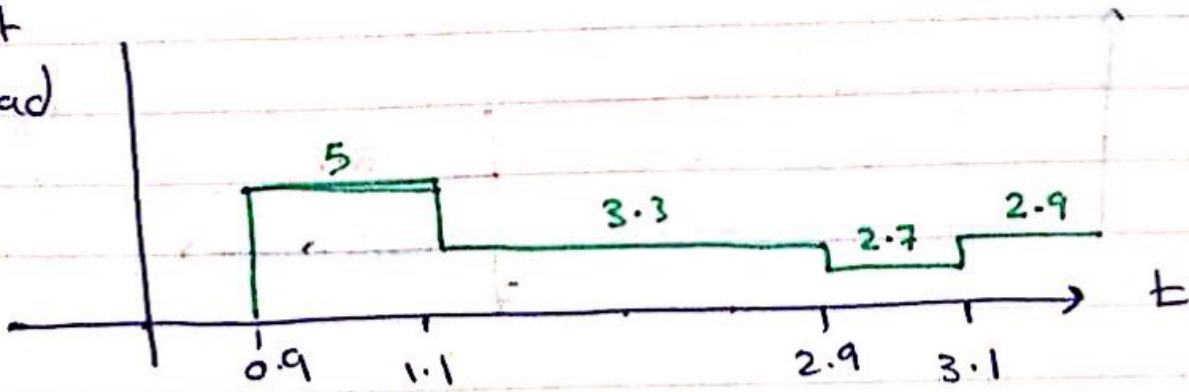
Ex if $d = 10 \text{ cm}$ $u = c/3$



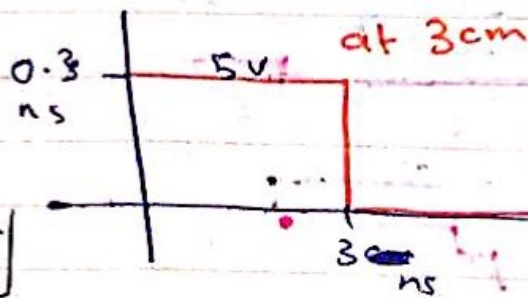
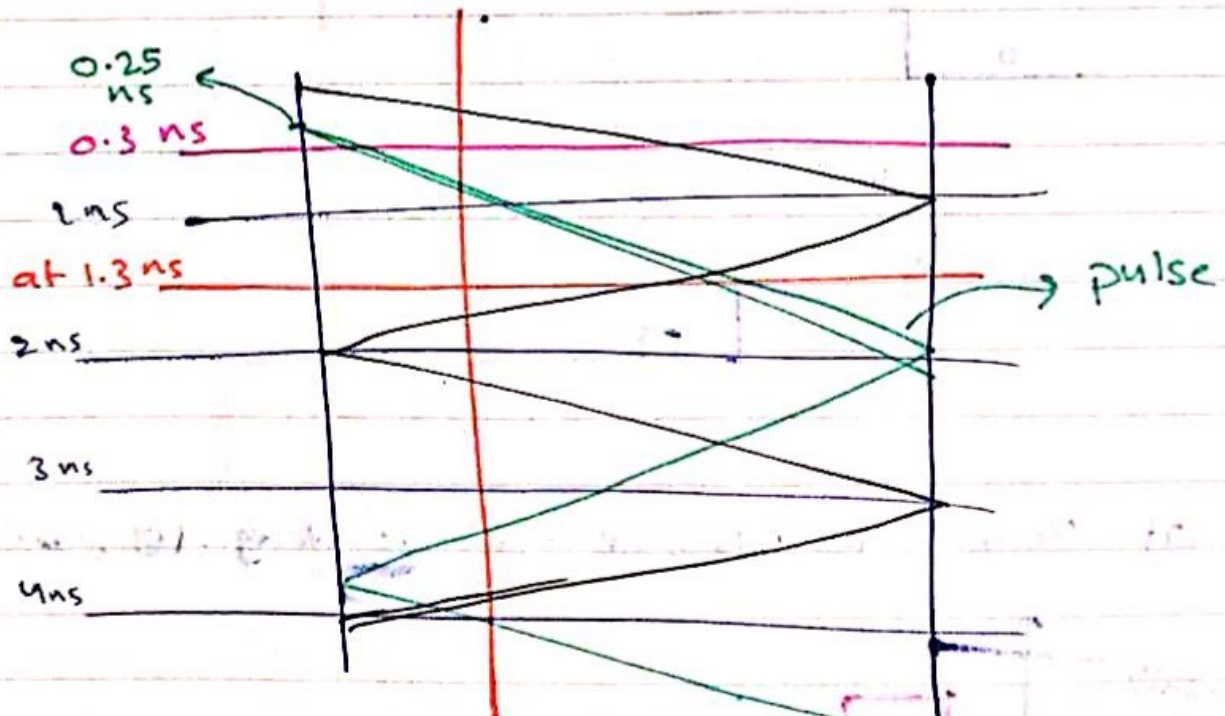
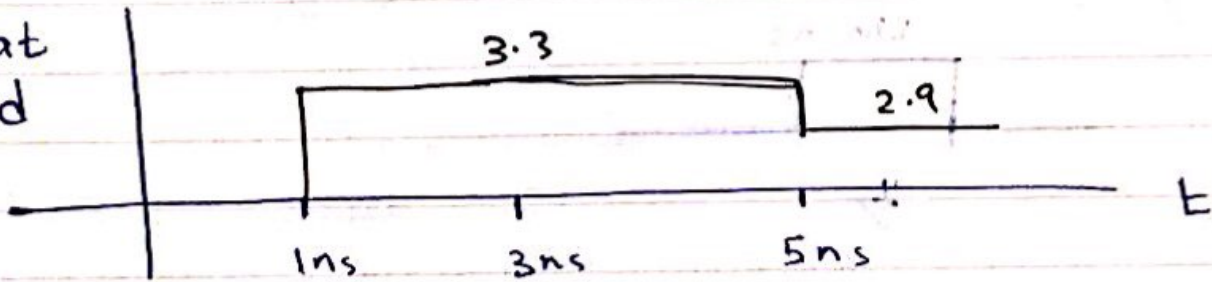
Sol: $\Gamma_s = +\frac{1}{3}$ $\Gamma_L = -\frac{1}{3}$
 $T = 1 \text{ ns}$

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at load



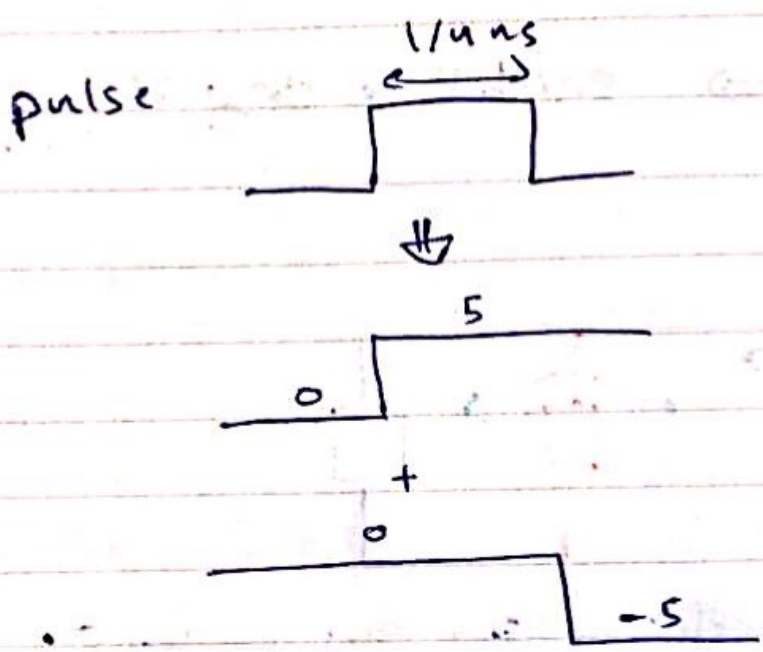
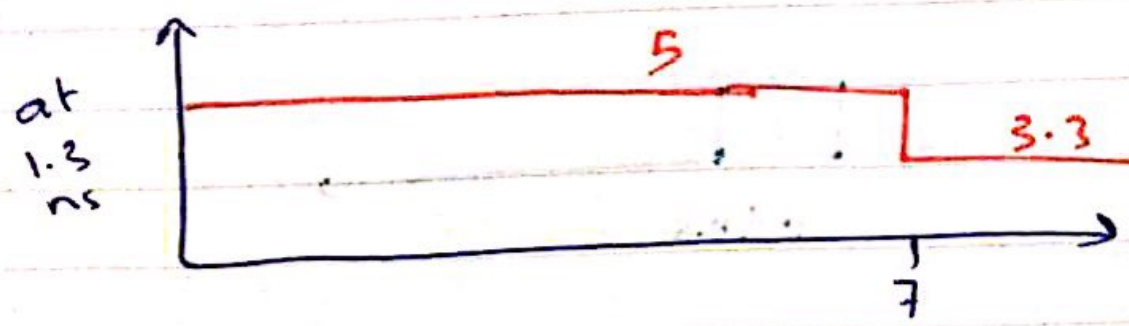
at d



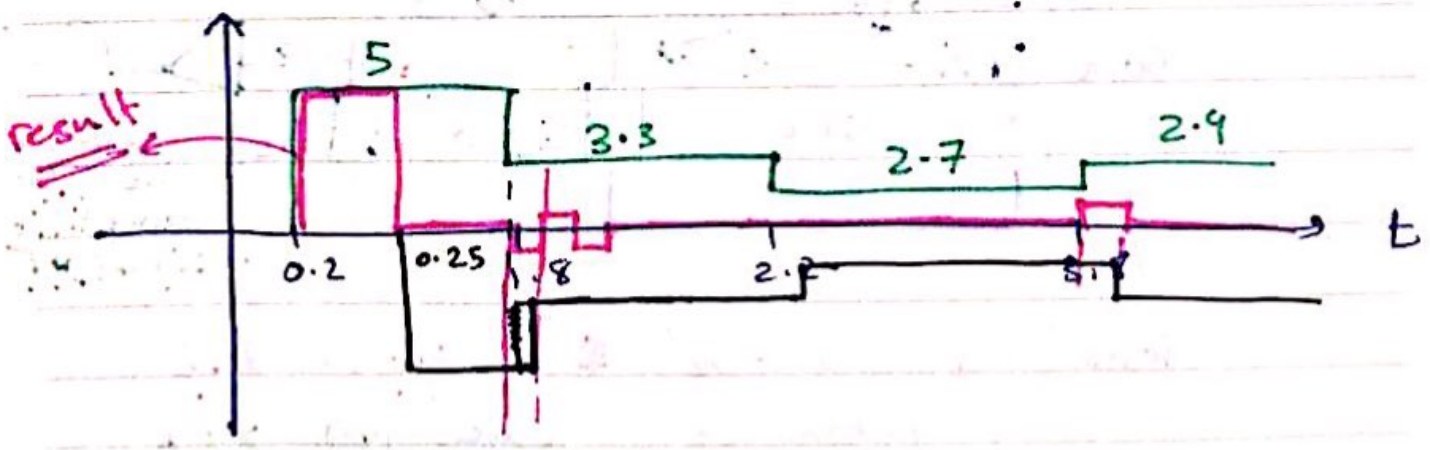
بنيو لى
نوفو لى

Signal 11
~~Signal 11~~

76

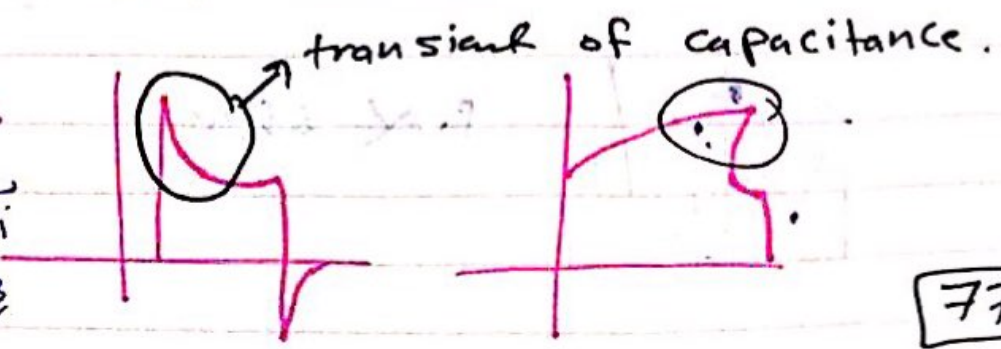


at 2cm \Rightarrow $t_{d, \text{max}} = 0.25$ ns delay

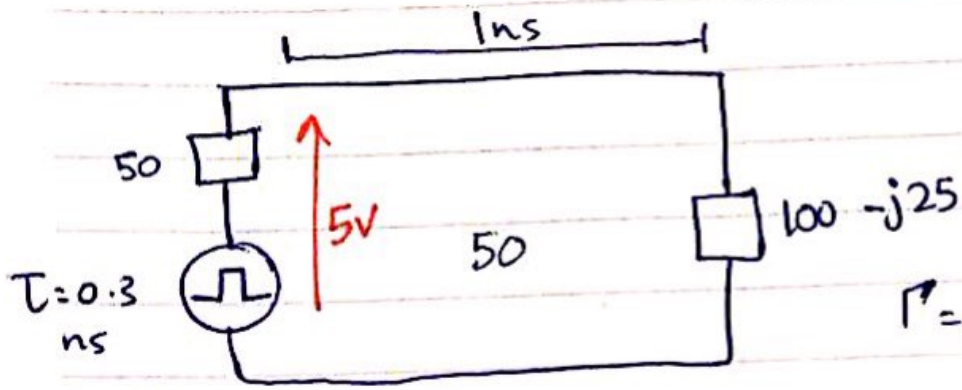


TDR:

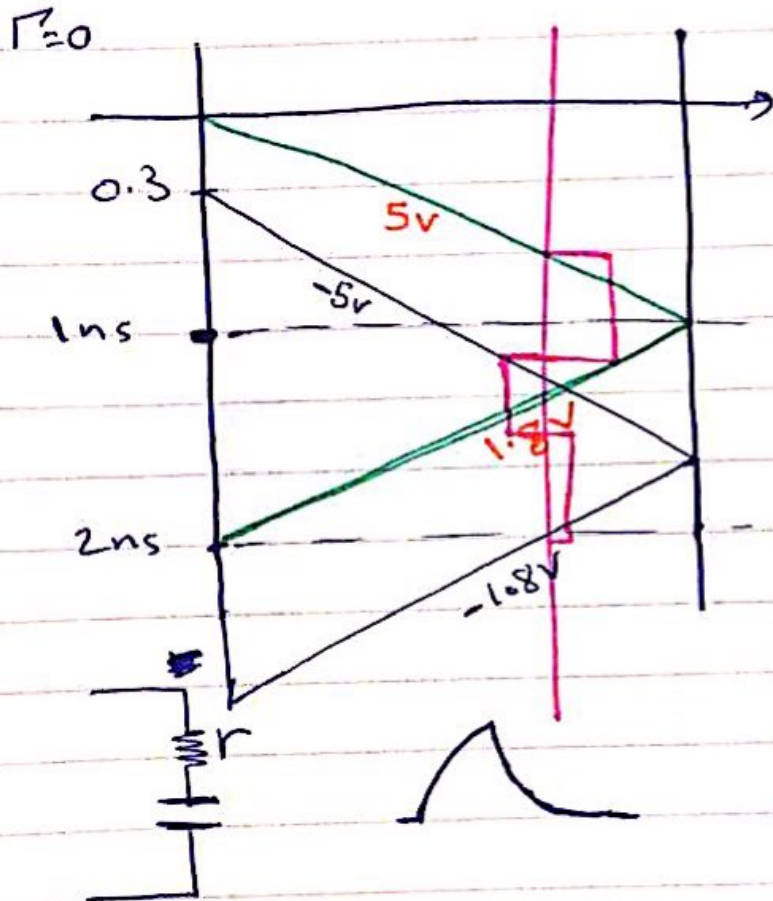
تقسیم علامت
اعرف من اكل
في الكيل



77

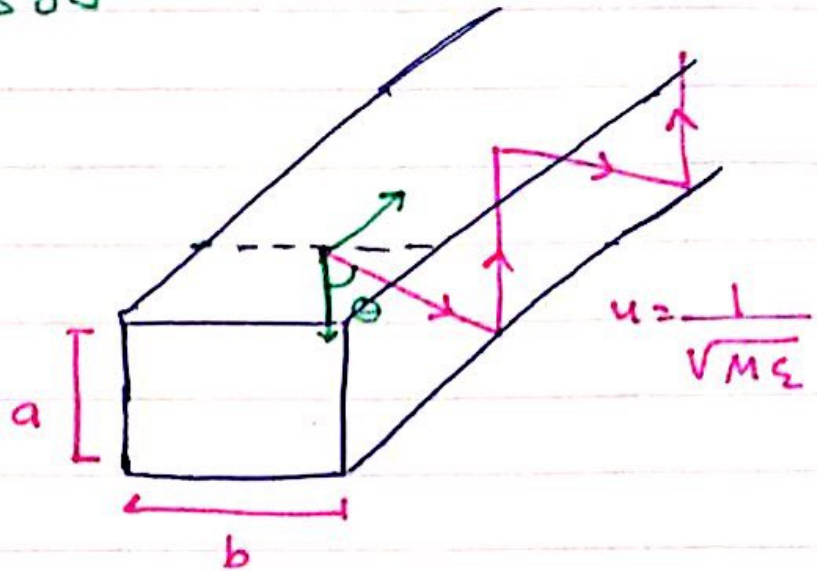


$$\Gamma = \frac{50 - j25}{150 - j25} = 0.36 \angle -17^\circ$$



splitter type

Wave Guides



$$b \gg \lambda/2$$

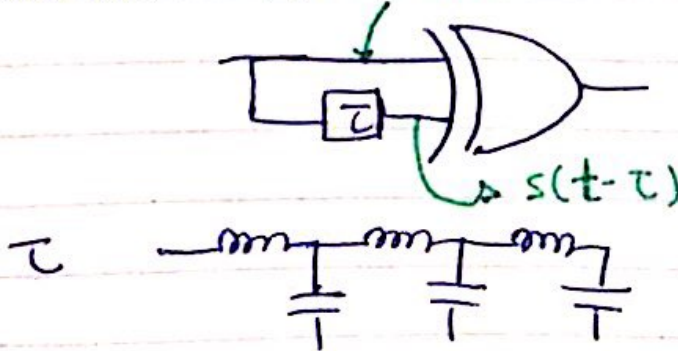
f_{cutoff}

(min freq which \Rightarrow
 $(\lambda/2 = b)$)

$$u = \frac{1}{\sqrt{\mu\epsilon}} \sqrt{1 - \left(\frac{f_c}{f}\right)^2}$$

$$u = \frac{1}{\sqrt{\mu\epsilon}} \sqrt{1 - \left(\frac{f_c}{f}\right)^2}$$

* differential RX:- $s(t)$

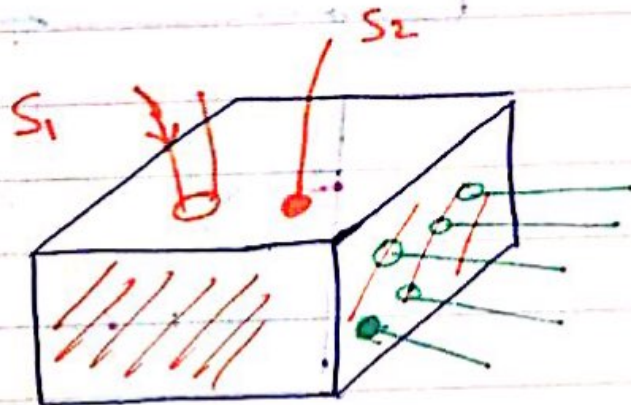
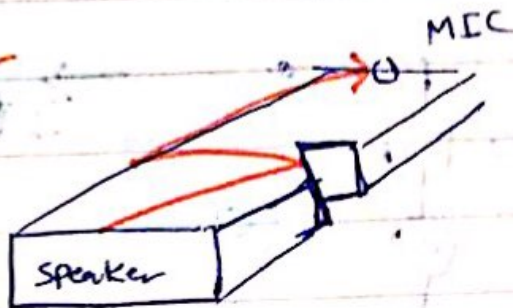


80

erse

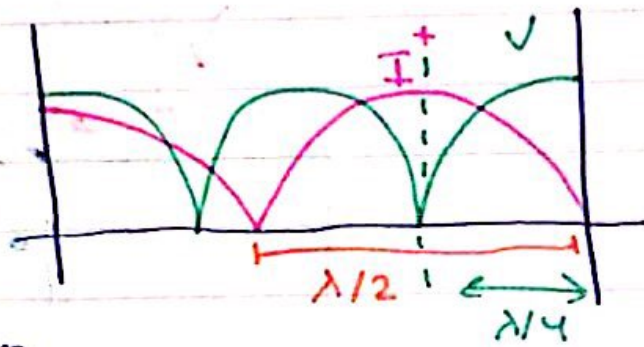
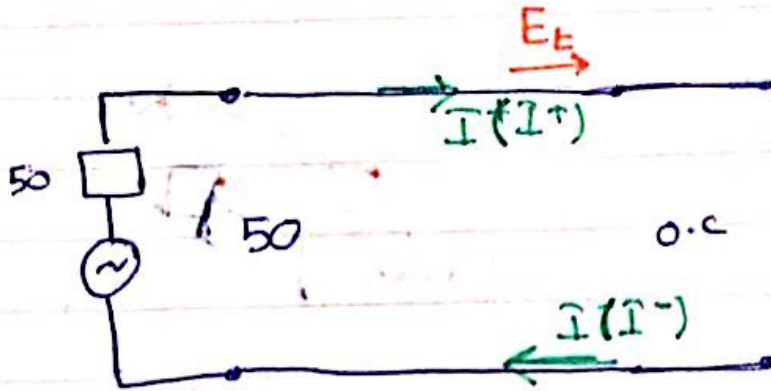
$$y(t) = \sum \alpha_i \cdot s(t - \tau_i)$$

* SAW Filters :-



$$\sum \alpha_i s_1(t - \tau_i) + \beta_i s_2(t - \tau_i)$$

Antennas :-

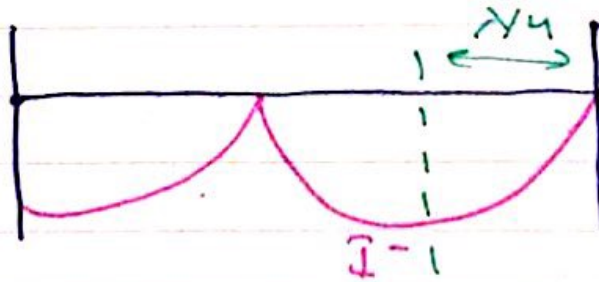


minimum = 0

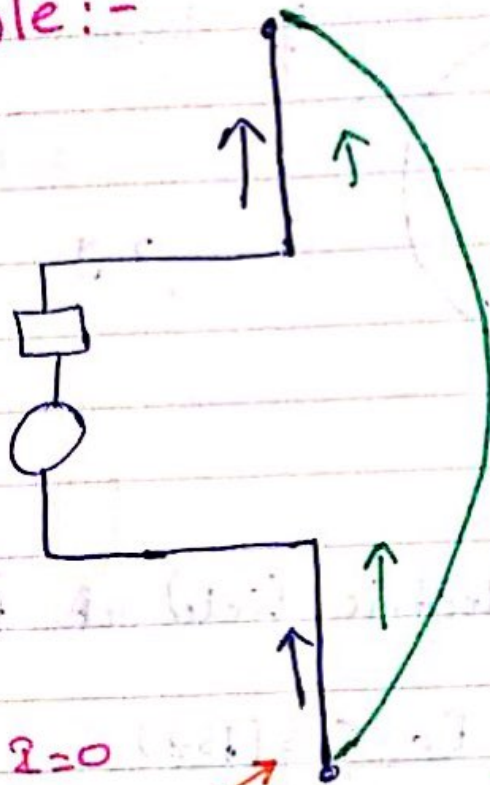
current → give electric field

voltage → current, $\vec{E} \perp \vec{I}$ antenna

$\vec{E} \perp \vec{I}$ rebo

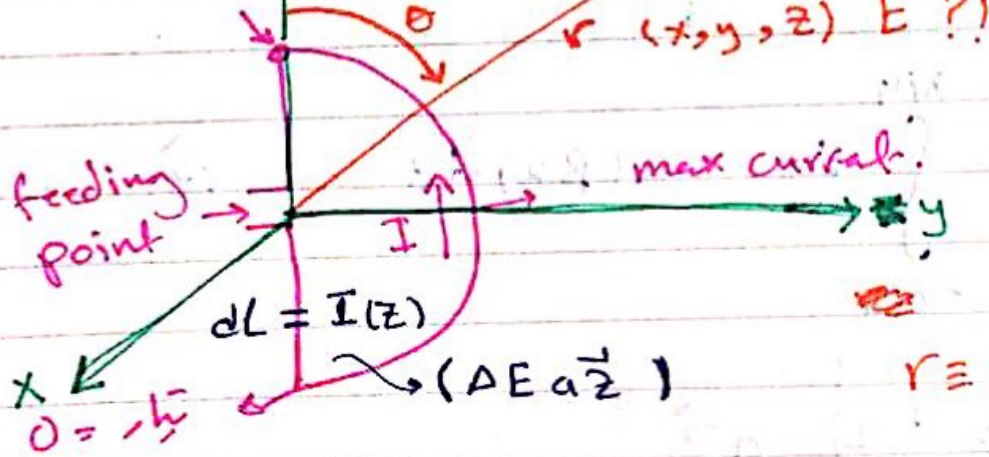


$\lambda/2$ dipole :-



دائرة LC
 دره support
 صاف تيار
 نتي
 الاتجاه

at this point $I=0$

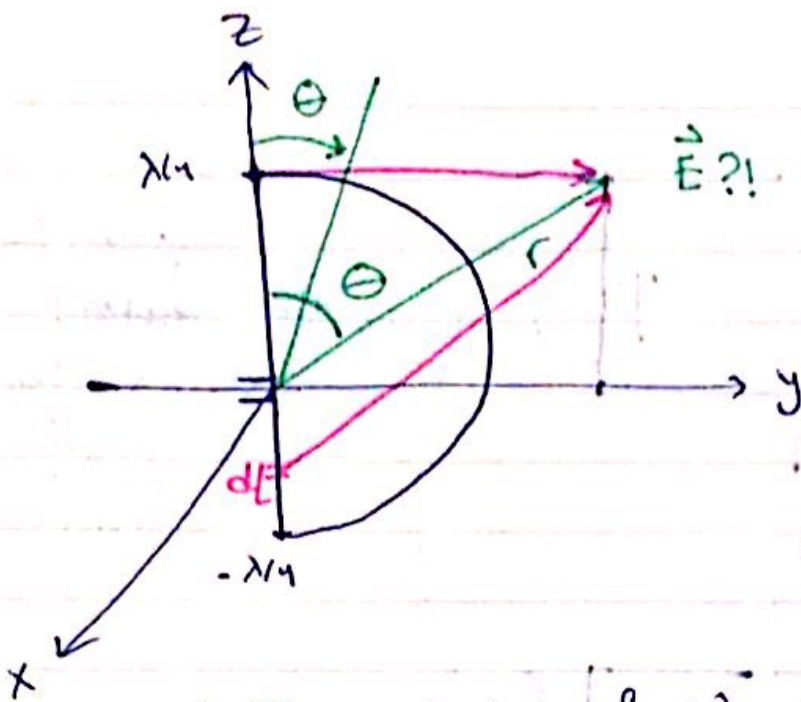


~~...~~
 $r \equiv$ distance from origin

$$\Delta E \vec{a}_z = I(z) E_0 \vec{a}_z$$

$$I(z) = \cos(\beta z)$$

$$\Delta E = E_0 \cos(\beta z)$$



~~dE~~ electric field at $\vec{E} ?!$

$$dE(r) = \frac{E_0 \cos(\beta z)}{r}$$

$$E(r) = \int_{-\lambda/4}^{\lambda/4} \frac{E_0}{r} \cos(\beta z) dz \quad \vec{a}_z$$

$$E(r) = \frac{E_0}{r} \vec{a}_z$$

$$E(r) = \frac{E_0}{r} \vec{a}_z \sin \theta$$

$$E(r, \theta) = \frac{E_0}{r} \sin \theta \vec{a}_z$$

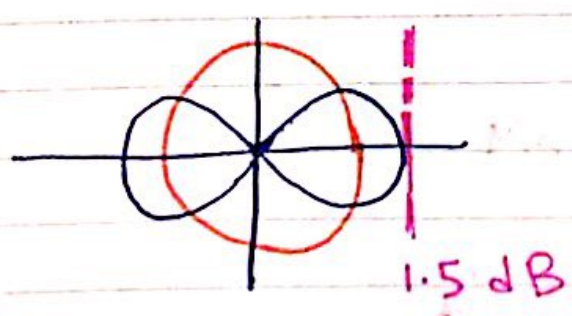
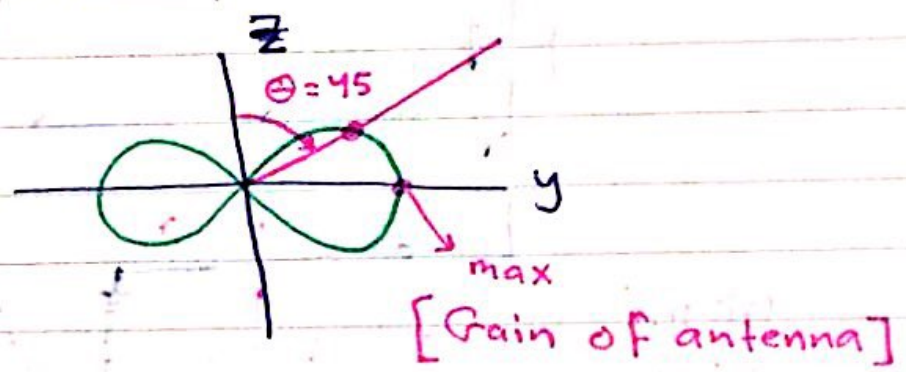
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* اذا كان الشكل في $\sin \theta$ - $\sin \theta$ (في دائرة) E_0

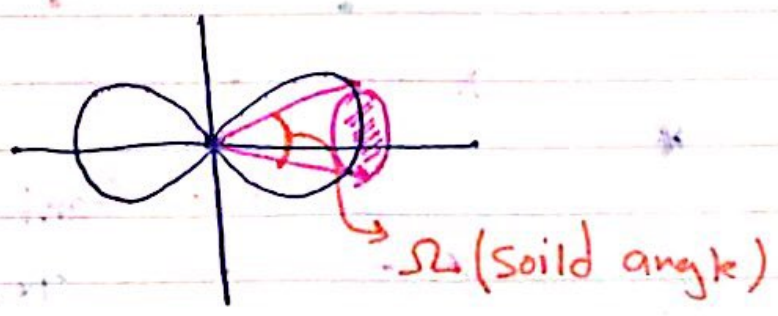
* In Horizontal - plane \rightarrow radiation beam Pattern



* In Vertical - plane...



In 3D globe
 $\omega = 4\pi$
 0.55 dB

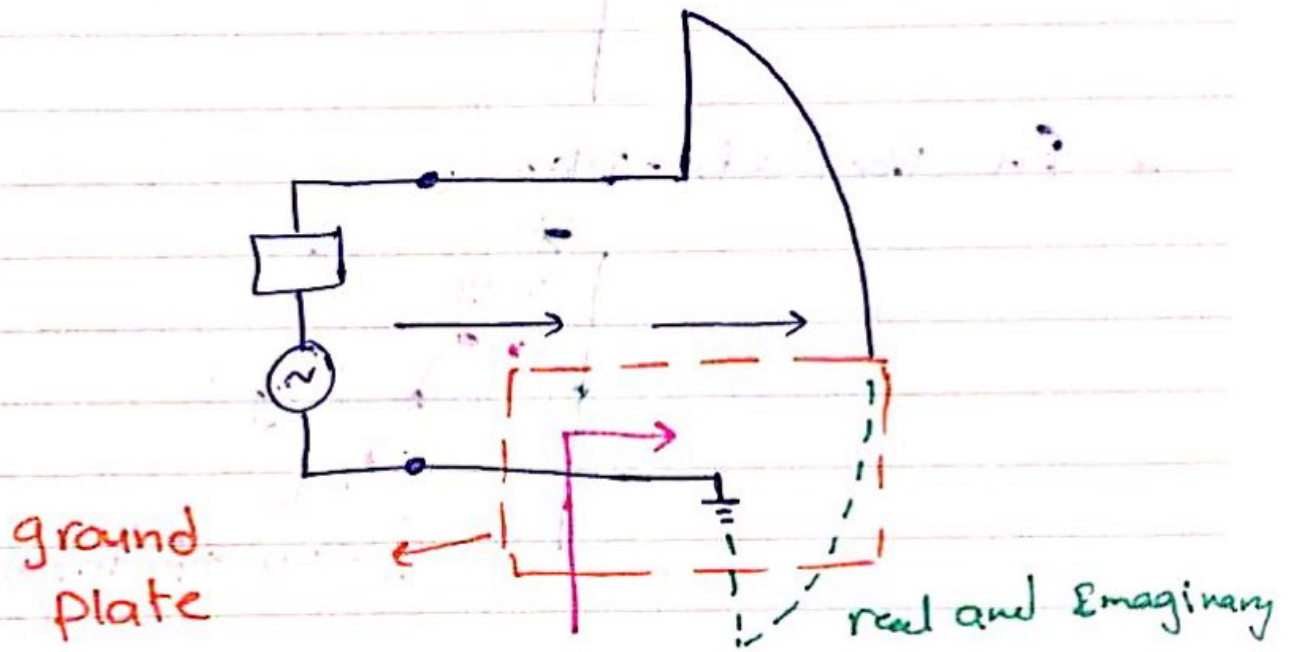


85

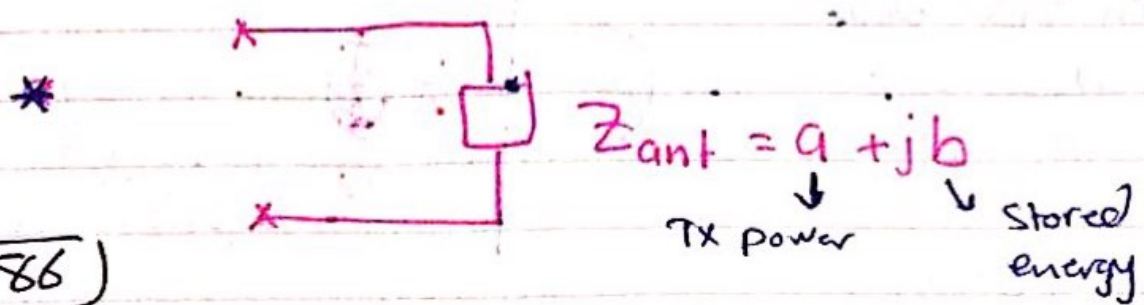
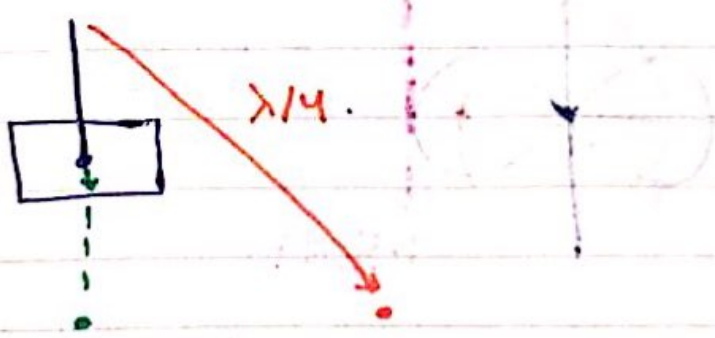
$$P_r = \frac{P_t \cdot G_{ant}}{4\pi r^2}$$

→ free space equation for Tx, Rx power.

• $G_{ant} \rightarrow$ P_t \rightarrow r^2 \rightarrow α^{-1} G

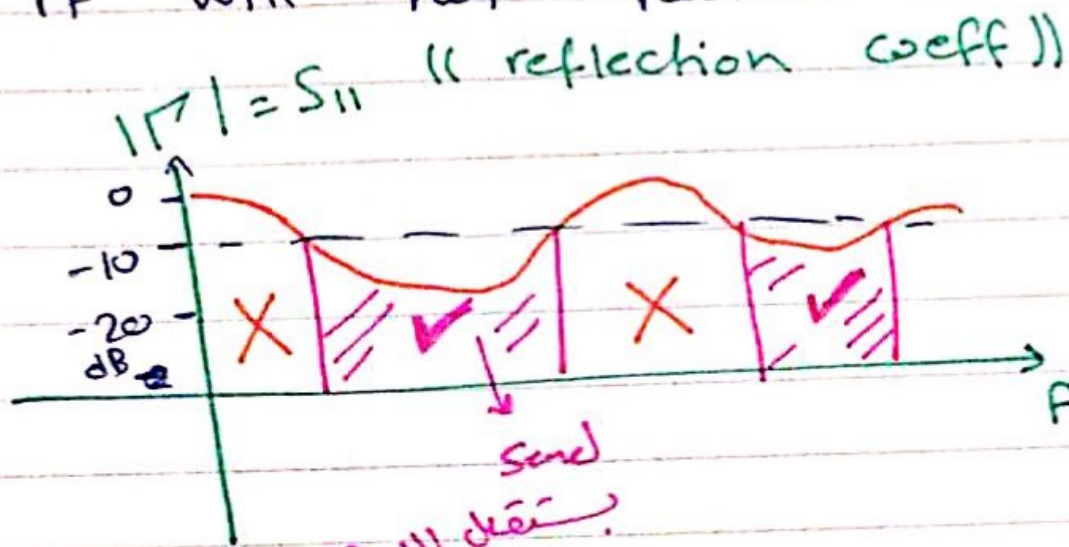


out shadow
See antenna.
⇒ electric dipole.



86

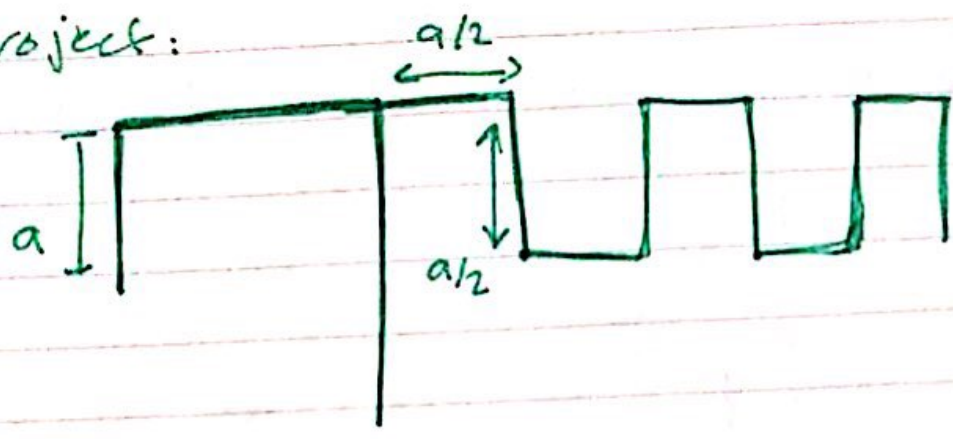
* IF the antenna not match
it will not radiate.



ببقول الـ standing wave
تبقول

22/8
Tue

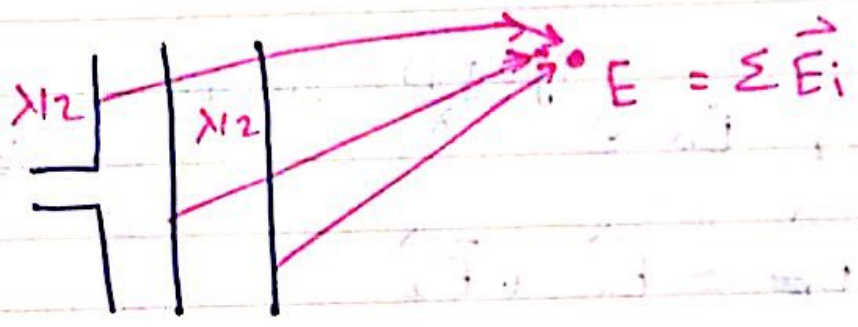
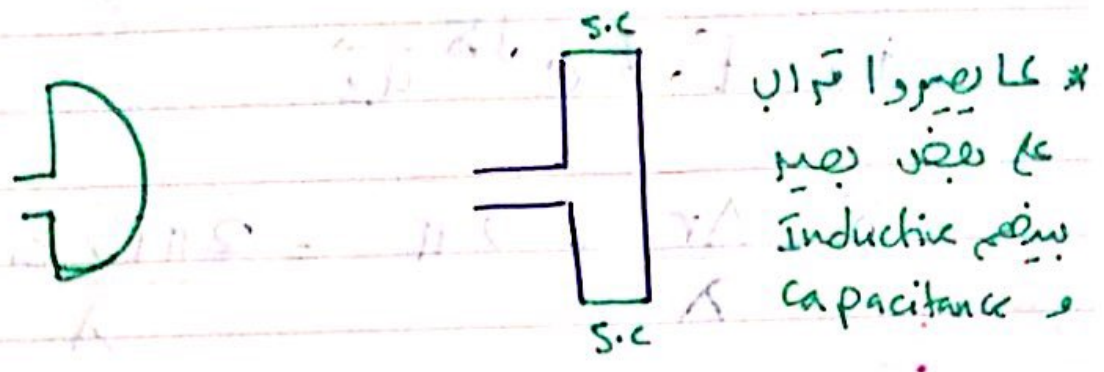
project:



$f = 2.4 \text{ GHz}$
 $f = 3.75 \text{ GHz}$

S11

$\lambda/2$ dipole \rightarrow انواع ال antennas

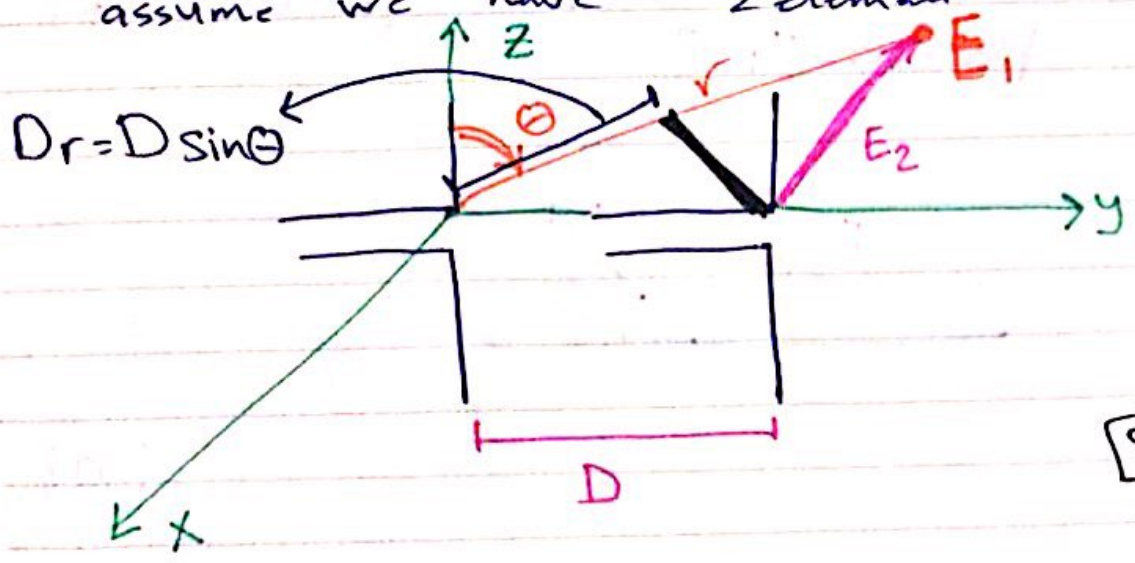


$$E_i = E_0 \angle \theta_i \vec{a}_{ei}$$

$$= E_0 e^{j\theta_i} \vec{a}_{ei}$$

* Antenna arrays :-

assume we have 2 element.



$$E_1 = E_0 \angle \theta \quad \vec{a}_z$$

$$E_2 = E_0 e^{j\delta} \vec{a}_z$$

$$\delta = \frac{\Delta r}{\lambda} * 2\pi = \frac{2\pi D \sin\theta}{\lambda}$$

$$E_2 = E_0 e^{j \frac{2\pi D}{\lambda} \sin\theta} \vec{a}_z$$

$$\vec{E} = \vec{E}_1 + \vec{E}_2$$

$$= E_0 \left(1 + e^{j \frac{2\pi D}{\lambda} \sin\theta} \right) \vec{a}_z$$

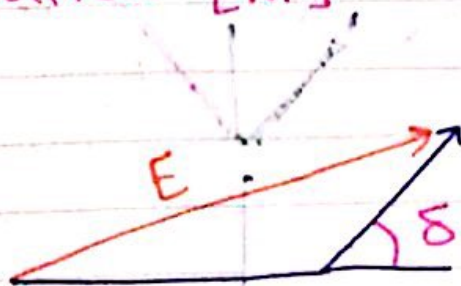
$$\vec{E} = \frac{A}{r} \sin\theta \left(1 + e^{j \frac{2\pi D}{\lambda} \sin\theta} \right) \vec{a}_z$$

radiation

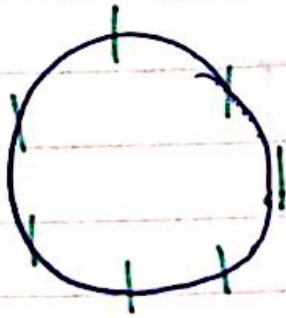
Pattern [RP]

array

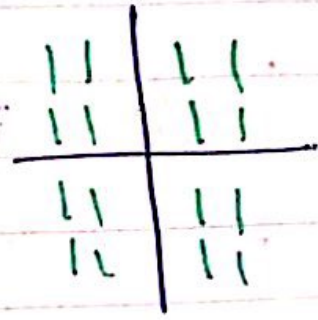
Factor [A.F]



90



circular array



↓
Planer array

$$E = RP(x, y, z) A z$$

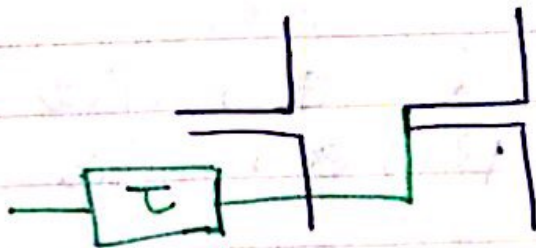
$$= \sum_{i=1}^N e^{j\delta_i}$$

$N =$ elements no

* SUM of vector



dimensional
Space لا تسمى
ليلا تسمى عدد



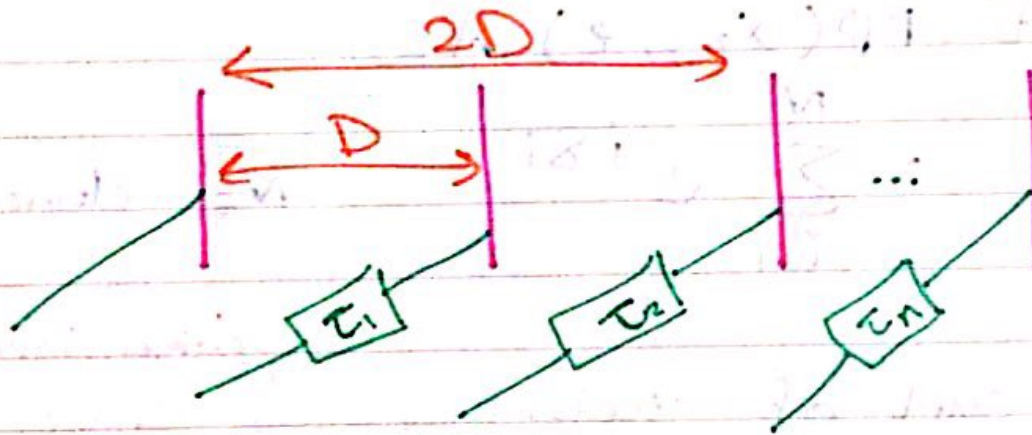
delay circuit

$$E = E_0 \left(1 + e^{j \left(\frac{2\pi D}{\lambda} \sin \theta - \frac{T}{T} 2\pi \right)} \right) \underline{a_z}$$

91

$$\tau_i = \frac{iDT}{\lambda} \sin \Theta$$

* LL غير (τ) لغير ال radiation pattern ← بتحرك
 as a function of Θ.



$$AF = \sum_{i=0}^{N-1} A e^{j \left(\frac{2\pi D i}{\lambda} \sin \Theta - \frac{\tau_i}{T} 2\pi \right)}$$

* in one dimension → Θ
 * in space ⇒ B, Θ

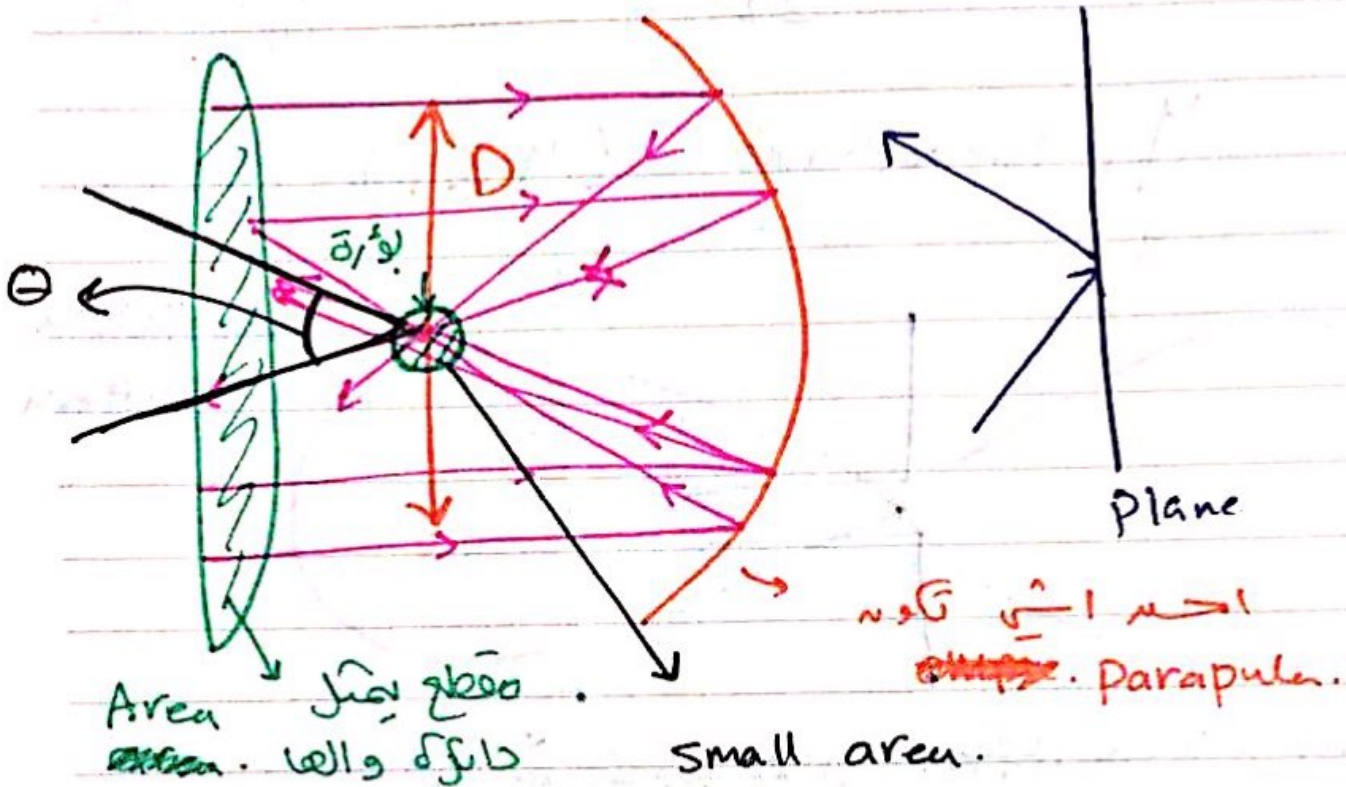
AF at maximum

$$AF = NA$$

↑ Gain ↑ elements.

92

Reflector Antennas:-



$$G \propto \frac{\text{Area}}{\text{area (small)}}$$

$$G = (D \cdot f)^2 \frac{16}{22^2} \Rightarrow \text{for circle}$$

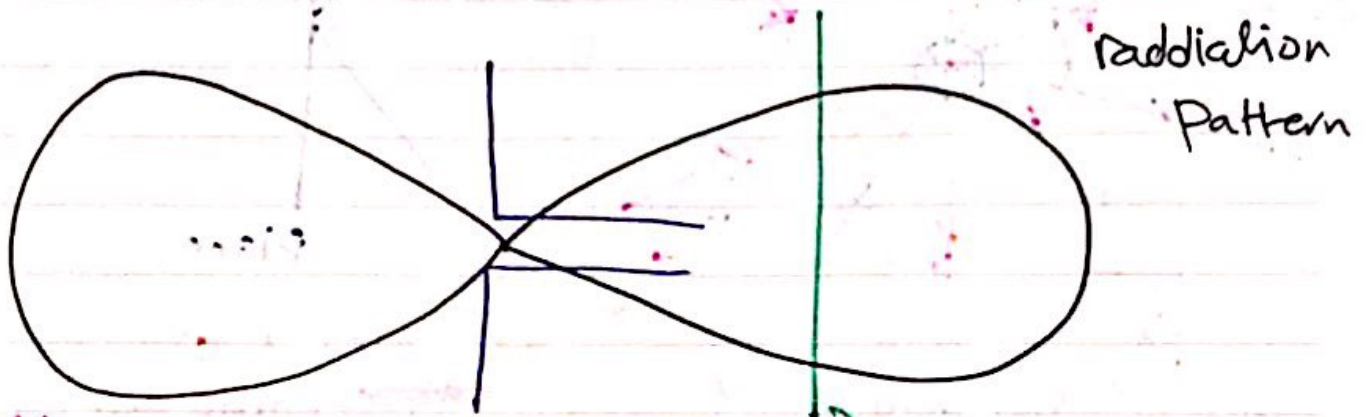


$$G = D_1 D_2 f^2 \cdot \frac{16}{22^2}$$

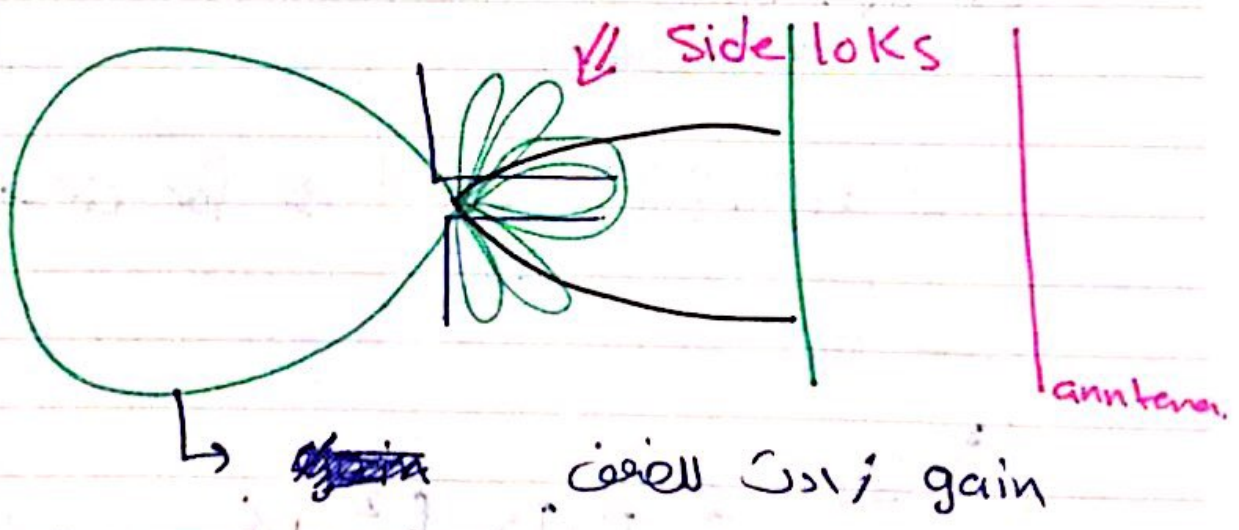
Handwritten notes in Arabic explaining the formula.

$$G = D_1 D_2 F^2 \frac{16}{22^2} \gamma \Rightarrow \text{Cutoff } \frac{1}{\delta} \text{ or } \frac{1}{\epsilon}$$

$\gamma \equiv$ Smoothness ($\gamma \leq 1$)



reflector has no gain
input to give gain



gain

94

