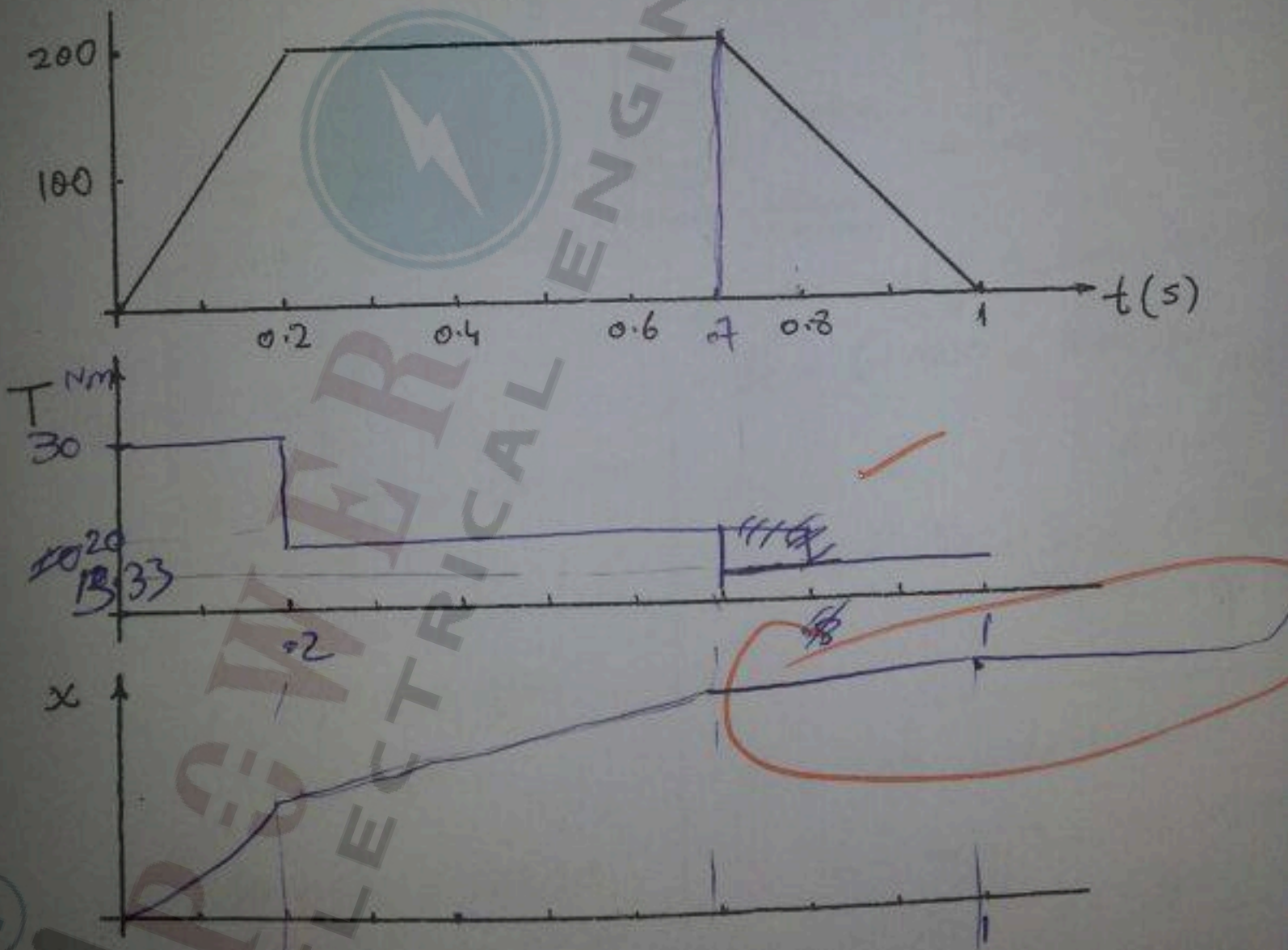


Name (in Arabic)

Student No. مكود مكي عبد عرايبي 0094338

1. Given the speed variation with time for certain load. Draw the variation of the Torque and position with time. Given that the constant torque is  $20\text{Nm}$  and the motor load inertia  $J = 0.01\text{kgm}^2$ . 4marks



$$T_e = T_L + J \frac{d\omega}{dt}$$

$t = 0 \rightarrow 0.2$

for  $t = 1 \rightarrow \infty$   
 $\frac{d\omega}{dt} = 0 \rightarrow T_e = T_L = 20$

3. A 300 V dc shunt motor drives a certain load at a speed of 1000 rpm. The armature resistance =  $0.5\Omega$  and the field current = 2A. The motor draws a total current of 82A. The load torque is proportional to square of the speed. The speed control for this motor is performed by field current control. Calculate the field current to drive the load at 1200rpm. What is the value of the armature current then?

$$V_T = 300 \text{ V}$$

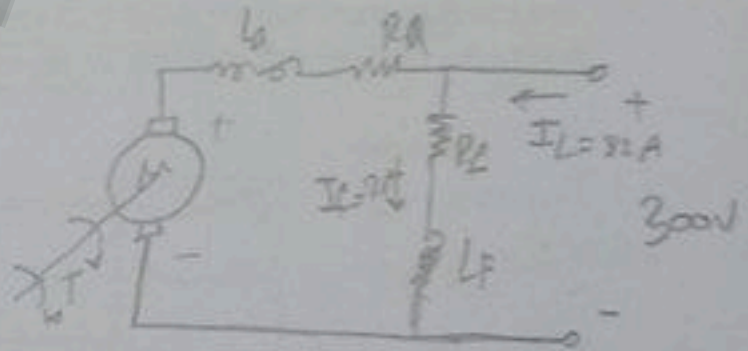
$$n_1 = 1000 \text{ rpm}$$

$$R_a = 0.5 \Omega$$

$$I_{f_1} = 2 \text{ A}$$

$$T_L = K n^2$$

6marks



\* find  $I_{f_2}$  at  $n_2 = 1200 \text{ rpm}$

$$I_{a_1} = I_L - I_{f_1} = 82 - 2 = 80 \text{ A}$$

$$V_T = E_{a_1} + I_{a_1} R_a$$

$$E_{a_1} = 300 - (80) \times 0.5 = 260 \text{ V}$$

$$T_1 = K \Phi I_{a_1}$$

$$T = K \omega^2$$

4. A dc. Separately excited motor is driving a load torque composed of two components as given in the equation:

$$T = 25 + 0.1 \omega^2$$

The armature circuit of the motor is connected to a full-wave, ac/dc SCR converter. The input voltage to the converter is 300V (rms). The armature resistance of the motor is  $5 \Omega$ , and the field constant ( $k\phi$ ) is 2.5 V sec. Assume that the armature current is always continuous. Calculate the range of the triggering angle to operate the motor at a speed range of 0 to 600 rpm.

at  $\omega = \frac{600 \times 2\pi}{60} = 62.9 \text{ rad/sec}$  6marks  $\frac{T}{k\phi}$

$$\alpha = \cos^{-1} \left[ \frac{T}{2V_{max}} (R_a + I_a r_f + k\phi) \right]$$

$$\alpha = \cos^{-1} \left[ \frac{T}{2 \times \sqrt{2} \times 300} (0.5 * (25 + 0.1 \omega^2)) \right]$$

$$\alpha = \cos^{-1} \left[ 3.7 \times 10^{-3} (0.5 * (168.26)) \right]$$

$$\alpha = 26.73^\circ \text{ for } \omega = 62.9$$

for  $\omega = 0$

$$\alpha = \cos^{-1} \left[ \frac{T}{2 \sqrt{2} \times 300} \left[ 0.5 \left( \frac{25}{2.5} \right) \right] \right]$$

$$Q3 \quad I_a = 82 - 2 = 80 A \quad \rightarrow \quad E_a = 300 - 80 \left(\frac{1}{2}\right) = 260 \text{ volt}$$

$$T = k\phi I_a \Rightarrow \frac{I_{f2} I_{a2}}{I_{f1} I_{a1}} = \left(\frac{n_2}{n_1}\right)^2$$

$$\left(\frac{1200}{1000}\right)^2 = \frac{I_{f2} I_{a2}}{I_{f1} I_{a1} \rightarrow 80} \Rightarrow E_a = k\phi\omega$$

$$\frac{E_{a2}}{260} = \frac{I_{f2} \times 1200}{2 \times 1000} \quad \cancel{E_{a2} =}$$

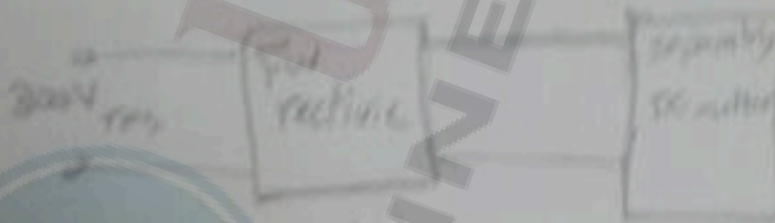
$$E_{a2} = 300 - I_{a2} \left(\frac{1}{5}\right) \Rightarrow I_{a2} = 1.39 A$$

$$I_{a2} = 165 A \quad X$$

4. A dc. Separately excited motor is driving a load torque composed of two components as given in the equation:

$$T = 25 + 0.1 \omega^2$$

The armature circuit of the motor is connected to a full-wave, ac/dc SCR converter. The input voltage to the converter is 300V (rms). The armature resistance of the motor is 0.5  $\Omega$ , and the field constant ( $k\phi$ ) is 2.5 V/ase. Assume that the armature current is always continuous. Calculate the range of the triggering angle to operate the motor at a speed range of 0 to 600 rpm.



6marks

$$r_a = 0.5 \Omega$$

$$k\phi = 2.5 \text{ V/ase}$$

Continuous Ia

$$T = k\phi I_a$$

at  $\omega = 0$

$$T_1 = 25 + 0.1 \times (0)^2 = 25 \text{ Nm}$$

$$I_{a1} = \frac{T}{k\phi} = \frac{25}{2.5} = 10 \text{ A}$$

$$E_{a1} = k\phi \omega_1 = 0$$

$$\frac{2 V_{max}}{\pi} \cos(\alpha) = E_a + r_a I_a$$

$$\frac{2 \times 300 \times \sqrt{2}}{\pi} \cos(\alpha) = 0 + 0.5 \times 10$$

$$270.1 \cos(\alpha) = 5$$

$$\alpha = \cos^{-1} \left( \frac{5}{270.1} \right) = 89.93^\circ$$

$$\omega_2 = 600 \text{ rpm}$$

$$\omega_2 = 600 \times \frac{2\pi}{60} = 62.83 \text{ rad/sec}$$

$$T_2 = 25 + 0.1 \times (62.83)^2 = 419.8 \text{ Nm}$$

$$I_{a2} = \frac{T_2}{k\phi} = \frac{419.8}{2.5} = 167.92 \text{ A}$$

$$E_{a2} = k\phi \omega_2 = 2.5 \times 62.83 = 157.1 \text{ V}$$

$$\frac{2 \times 300 \sqrt{2}}{\pi} \cos(\alpha) = 157.1 + 0.5 \times 167.92$$

$$270.1 \cos(\alpha) = 241.06$$

$$\alpha = \cos^{-1} \left( \frac{241.06}{270.1} \right) = 26.81^\circ$$

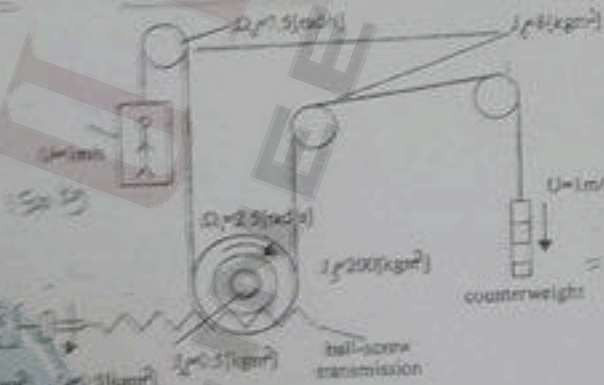
\* range of  $\alpha$

$$(26.81^\circ - 89.93^\circ)$$

6

2. The figure below shows an elevator drive with multiple mechanical transmission and counterweight. The motor is a 4 pole motor operating at a slip of 0.05 and an efficiency of 85% from a 3-phase supply of 400V, 50 Hz. The counterweight = 1000kg and the elevator load is 1500kg. 5 marks

Calculate the torque and the electromagnetic power without counterweight

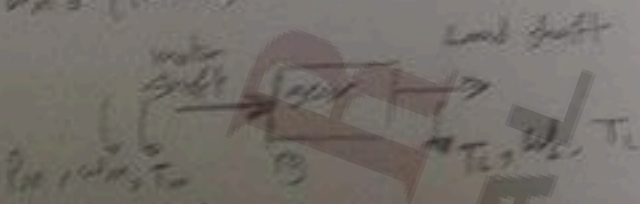


5

$$\omega_s = \frac{2\pi \times 50}{4} = 785.4 \text{ rad/s}$$

$$500 \text{ rpm} = 52.36 \text{ rad/s}$$

$$\omega_m = (1 - 0.05) \times 52.36 = 49.74 \text{ rad/s}$$



referred to motor shaft

$$J_1 = \frac{J_2}{\omega_2} = \frac{33}{149.2}$$

$$J_3 = \frac{J_4}{\omega_4} = \frac{33}{149.2}$$

$$J_T = J_1 + J_2 + J_3 + J_4 = 3 \times \left(\frac{33}{149.2}\right) + J_4$$

$$J_T = \frac{1000 \times 9.81 \times 1}{149.2} + 3 \times \left(\frac{33}{149.2}\right) = 6.67 + 0.66 = 7.33 \text{ kgm}^2$$

$$J_c = (m_c + m_{cu}) \cdot \frac{u^2}{\omega^2} = (1000 + 1500) \cdot \frac{1}{(149.2)^2}$$

$$J_c = 0.1123 \text{ kgm}^2$$

$$J_T = J_r + J_c = 7.33 + 0.1123 = 7.4423 \text{ kgm}^2$$

$$\Sigma \tau = \alpha \Sigma J$$

$$T_{em} \cdot \omega_m \cdot \eta = m_c \cdot g \cdot u$$

$$T_{em} = \frac{1500 \times 9.81 \times 1}{149.2 \times 0.85} = 116.03 \text{ N.m}$$

$$P_{em} = T_{em} \cdot \omega_m = 116.03 \times 149.2 =$$

$$P_{em} = 17311.576 \text{ W}$$

$$4475 - 128V_i' + 0.092V_i'^2 + 863V_i' - 0.125V_i'^2$$

$$- 0.033V_i'^2 - 4.17V_i' + 443.5$$

$$- 63.18 - j89.2$$

5. A 3-phase, 400V, 50Hz, 6-poles, induction motor is driving a constant load of 80Nm. The parameters of the motor are:

$R_{TH} = R_1 = 0.5\Omega$      
  $R_2 = 0.3\Omega$      
  $X_{TH} = 2\Omega$      
  $X_2 = 2\Omega$      
  $N_1/N_2 = 2$

(i) Calculate the magnitude of the injected voltage that will reduce the motor speed to 700 rpm 7marks

Torque



$$\frac{120 fs}{p} = \frac{120 (50)}{6} = 1000 \text{ rpm}$$

new speed.

$$\frac{n_s - n}{n_s} = \frac{1000 - 700}{1000} = 0.3$$

$$(2) * 2^2 = 8 \quad \sim$$

$$(0.3) * (2)^2 = 1.2 \quad \sim$$

$$8 + 2 = 10 \quad \sim$$

$$T_d = \frac{3}{sU_s} \left[ (I_2')^2 R_2 + V_i' I_2' \cos\theta \right]$$

$$80 = \frac{3}{-3 * \left( \frac{2\pi * 1000}{60} \right)} \left[ (I_2')^2 * (0.3) + V_i' I_2' \cos\theta \right]$$

$$I_2' = \frac{\sqrt{230.94 - \frac{V_i'}{0.3}}}{\sqrt{10.97}} * 3$$

$$I_2' = \left[ \frac{69.28 - V_i'}{3.29} \right]$$

$$80 = \frac{3}{10\pi} \left[ \left( \frac{69.29 - V_i'}{3.29} \right)^2 * 1.2 + V_i' \left[ \frac{69.29 - V_i'}{3.29} \right] \right]$$

$$80 = \frac{3}{10\pi} \left[ \frac{4801.1 - 138.58V_i' + V_i'^2}{3.29} + \frac{69.29 - V_i'}{3.29} \right]$$

A 300 V dc shunt motor drives a certain load at a speed of 1000 rpm. The armature resistance =  $0.5\Omega$  and the field current = 2A. The motor draws a total current of 82A. The load torque is proportional to square of the speed. The speed control for the motor is performed by field current control. Calculate the field current to drive the load at 1200rpm. What is the value of the armature current then?

6marks

$I_{f1}$   
 $82 - 2 = 80A$

A.  
 $= K\phi_1 I_{a1}$   
 $= K\phi_1 (80)$

$K\phi_1 I_{a2}$   
 $\rightarrow (1000 \text{ rpm})^2$   
 $\rightarrow (1200)^2$

$$\frac{\phi_1}{\phi_2} \frac{n_1}{n_2} = \frac{V - I_{a1}R_a}{V - I_{a2}R_a}$$

$$\frac{\phi_1}{\phi_2} = \frac{n_2}{n_1} \left[ \frac{300 - I_{a2}R_a}{300 - I_{a1}R_a} \right]$$

$$\frac{\phi_1}{\phi_2} = \frac{1200}{1000} \left[ \frac{300 - I_{a2}R_a}{300 - 80 \times 0.5} \right]$$

$$\frac{\phi_1}{\phi_2} = \sqrt{2} \frac{31}{300}$$



see table 10.1

10.3

a. @ operating point 1  $\rightarrow T = 40 = \frac{V^2 s_1}{\omega_s R_2}$

$\rightarrow n = \frac{120P}{P} = \frac{120 \times 60}{4} = 1800 \text{ rpm} \rightarrow \omega_s = \frac{2\pi \cdot 1800}{60} = 188.5 \text{ rad/s}$

$\rightarrow 40 = \frac{(480)^2 s_1}{188.5 \times 0.3} \rightarrow s_1 \approx 0.01 \rightarrow I = \frac{V s_1}{\sqrt{3} R_2} = \frac{480 \times 0.01}{\sqrt{3} \times 0.3} = 9.237 \text{ A}$

b. @ operating point 2  $\rightarrow I = \frac{V}{\sqrt{3} X_{eq}} = \frac{480}{\sqrt{3} \times 12} = 23.09 \text{ A}$

c. @ operating point 3  $\rightarrow I = \frac{V}{\sqrt{3} X_{eq}} = 23.09 \text{ A}$

d. @ operating point 4  $\rightarrow T = \frac{V^2 R_2'}{s_3 (-\omega_s) X_{eq}^2} = \frac{(480)^2 \times 0.3}{(1) (-188.5) (12)^2} = -2.546 \text{ NM}$

e. @ operating point 5  $\rightarrow T_6 = T_1 = 40 = \frac{V^2 s_6}{(-\omega_s) R_2'} \rightarrow s_6 = \frac{40 (-\omega_s) (R_2')}{V^2} \approx -0.01$  (feasible)

f.  $T_6 = T_1 = 40 \text{ NM}$

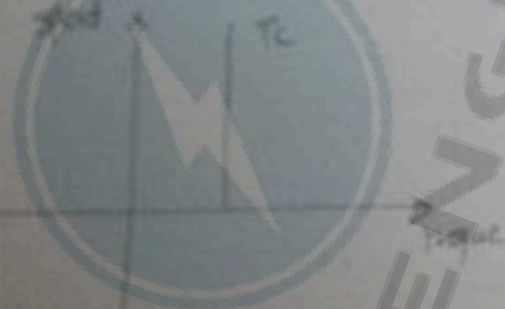
g.  $n_6 = n_s (1 - s_6) = 1800 (1 + 0.01) = 1818 \text{ rpm}$

6. Sketch the relationship of torque speed for

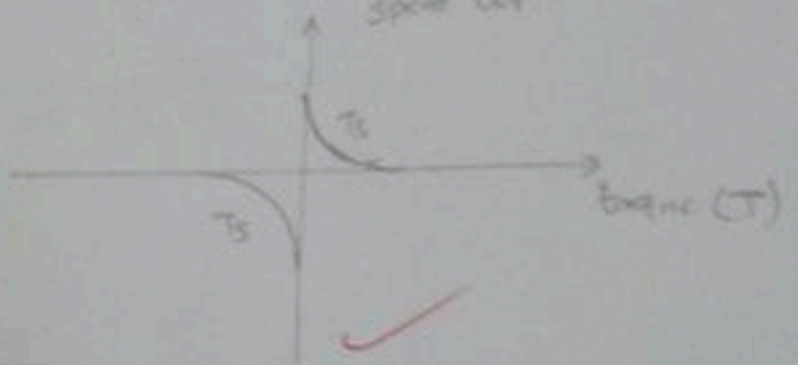
2marks

2

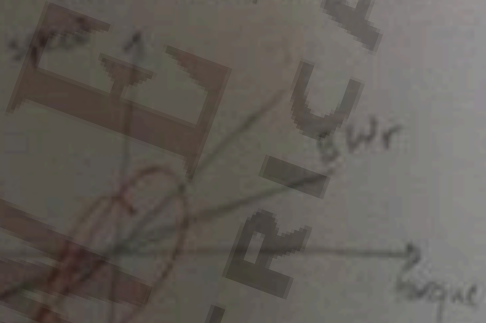
(i) Coulomb friction



(ii) Static friction ( $T_s$ )



(iii) Viscous friction



(iv) Windage friction

