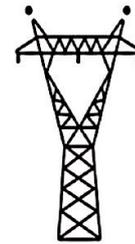




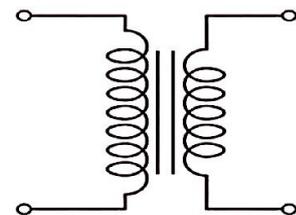
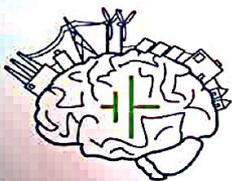
# Communications I

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Handout #1  
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Summary

- Complex exponential Fourier series:  $x(t) = \sum_{n=-\infty}^{\infty} \alpha_n e^{jn\omega_0 t}$  ;  $\omega_0 = \frac{2\pi}{T}$
- $\alpha_n$  found by:  $\alpha_n = \frac{1}{T} \int_T x(t) e^{-jn\omega_0 t} dt$ .
- Fourier Transform:  $X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$  ,  $x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega) e^{j\omega t} d\omega$

- Fourier
- $\cos \omega_0 t \rightarrow \pi [\delta(\omega + \omega_0) + \delta(\omega - \omega_0)]$
  - $\sin \omega_0 t \rightarrow j\pi [\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$
  - $e^{\pm j\omega_0 t} \rightarrow 2\pi \delta(\omega \mp \omega_0)$
  - $\text{rect}(t/\tau) \rightarrow \tau \text{sinc}(\frac{\omega\tau}{2\pi})$
  - $\Delta(t/\tau) \rightarrow \tau \text{sinc}^2(\frac{\omega\tau}{2\pi})$
  - $\text{sinc}(t/2\pi) \rightarrow 2\pi \text{rect}(\omega)$

- $\text{saw}(t/\tau) \rightarrow \frac{-2j}{\omega} [\text{sinc}(\frac{\omega\tau}{2\pi}) - \cos(\frac{\omega\tau}{2})]$
- $\delta(t) \rightarrow 1$
- $1 \rightarrow 2\pi \delta(\omega)$
- $\text{rep}[p(t)] \rightarrow \sum 2\pi \alpha_n \delta(\omega - n\omega_0)$
- $u(t) \rightarrow \pi \delta(\omega) + 1/j\omega$
- $\text{sgn}(t) \rightarrow 2/j\omega$
- $e^{-t^2/2} \rightarrow \frac{1}{\sqrt{2\pi}} e^{-\omega^2/2}$

- Properties:
- $x^*(t) \rightarrow X^*(-\omega)$
  - $X(t) \rightarrow X(\omega)$  (even, real) ;  $X(t) \rightarrow -X(\omega)$  (odd, imag.)
  - $X(t) \rightarrow 2\pi x(-\omega)$

- $x(t \pm t_0) \rightarrow X(\omega) e^{\pm j\omega t_0}$
- $x(t) e^{\pm j\omega_0 t} \rightarrow X(\omega \mp \omega_0)$
- $\frac{dX(t)}{dt} \rightarrow j\omega X(\omega)$
- $\int_{-\infty}^{\infty} x(\tau) d\tau \rightarrow \frac{X(\omega)}{j\omega} + \pi X(0) \delta(\omega)$

PSD:  $\text{PSD} \equiv S(\omega) = \lim_{T \rightarrow \infty} \frac{1}{T} |X_T(\omega)|^2 \Rightarrow P = \frac{1}{2\pi} \int_{-\infty}^{\infty} S_x(\omega) d\omega$

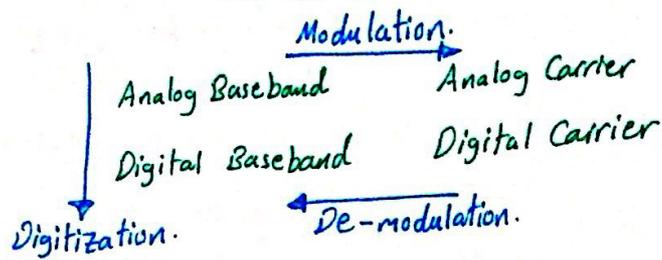
Pavg:  $P_{\text{avg}} = \frac{1}{T} \int_T |x(t)|^2 dt$  ; Avg:  $X_{\text{avg}} = \frac{1}{T} \int_T x(t) dt$  ; RMS:  $X_{\text{rms}}^2 = \frac{1}{T} \int_T x^2(t) dt$

$x(t)$ rept.	DC	$B_x(t)$	$\alpha_n$	$\angle \alpha_n$	figure
$A \text{rect}(t/\tau)$	$A\tau/T$	$1/\tau$	$\frac{A\tau}{T} \text{sinc}(\frac{n\omega_0\tau}{2\pi})$	Zero.	
$2A \text{rect}(\frac{t}{\tau}) - A$	0	$2/\tau$	$A \text{sinc}(\frac{n}{2})$	Zero.	
$A \Delta(t/\tau)$	$\frac{A\tau}{T}$	$1/\tau$	$\frac{A\tau}{T} \text{sinc}^2(\frac{n\omega_0\tau}{2\pi})$	Zero	
$2A \Delta(t/\tau) - A$	0	$2/\tau$	$A \text{sinc}^2(\frac{n}{2})$	Zero	
$A \text{saw}(t/\tau)$	0	$3/\tau$	$\frac{-j2A}{n\omega_0 T} [\text{sinc}(\frac{n\omega_0\tau}{2\pi}) - \cos(\frac{n\omega_0\tau}{2})]$	$\pm 90^\circ$	
$A \text{saw}(t/T)$	0	$3/T$	$jA \frac{\cos(n\pi)}{n\pi}$	$\pm 90^\circ$	

Best of  
 \* \* \*  
 \* \* \*  
 Luck.

# Summary

\* 4-Types of comm sys. :



\* Advantages of Digital over Analog:

- 1) Immunity to NOISE Because —
  - ① threshold detection @ Rx.
  - ② Availability of Regenerative Repeaters.
- 2) Allow Multiplexing —
  - @ Baseband Level: TDM.
  - @ Carrier Level: FDM, CDMA, OFDMA.
- 3) Use spread spectrum tech. help to overcome Jamming & Interference & impairments such as Fading which increase transmission Rate.
- 4) Source Coding tech. ⇒ reduce amount of transmitted bits ⇒ increase Bandwidth.
- 5) Channel Coding tech. ⇒ reduce bit errors ⇒ improves SNR.
- 6) Exchanging SNR for Bandwidth.
- 7) Digital Hardware is flexible, allows  $\mu$ processor to perform DSP.
- 8) Digital signal storage is easy & inexpensive.

\* A/D Conversion: Sampling → Quantization → Mapping → Encoding & pulse-shaping.

\*\* Sampling :

\* convert  $m(t)$  from Continuous to discrete separated by  $T_s$ : sampling time.

\* Nyquist-Shannon sampling theorem:  $f_s \geq 2B$  ⇒ No aliasing  $f_s = \frac{1}{T_s}$  sampling freq.

\* if  $f_s < 2B$  aliasing will occur.

Ex. Voice ( $B=4\text{KHz} \Rightarrow$  sampled @  $8\text{KHz}$ ) & CD(Audio) ( $B=20\text{KHz} \Rightarrow$  sampled @  $44.1\text{KHz}$ )

\* practically its hard to have impulse, so we use pulses.

\* Types of Sampling: ideal/practical/Natural.

### \* Quantization :

- \* Samples approximated to a small set of discrete quantization levels.
- \* Quantization Error:  $\Delta V = \frac{2mp}{L}$ 
  - peak of  $m(t)$
  - # of levels.
- ↳ it is decreased by 2-methods:  $L \uparrow$  OR rounded off method.

# of bits =  $\log_2 L$

- Voice: (8-bits)  $\Rightarrow L = 256$  levels.
- CD: (16-bits)  $\Rightarrow L = 65536$  levels.

### \* Mapping :

- \* Gives 1's & 0's for the discretized signal.
- \* Bit Time:  $T_0 = \frac{T_s}{\log_2 L} \Rightarrow f_0 = f_s \log_2 L \Rightarrow \underline{f_s = 2B_m}$
- \* PCM  $\equiv$  Pulse Code Modulation. (includ sampling + Quan. + Mapping).
- \* a% above Nyquist Rate  $\Rightarrow (a/100 + 1) * f_s ; f_s = 2B_m$ .

### \* Encoding :

- Source Coding: Compression Data.
  - $\Rightarrow$  Examples: ① Shannon code. ② Huffman Code. ③ Lempel-Ziv coding.
  - ④ RLE (Run length Encoding). ⑤ LPC (Linear Prediction Coding) ⑥ CELP (Code Excited Linear prediction).
  - ⑦ Arithmetic Coding. ⑧ MPEG-4 video Coding.
- Channel Coding: Error Correcting.  $C = B_{ch} * \log_2(1+SNR)$ 
  - $\Rightarrow$  Examples: ① Hamming Codes. ② Turbo Codes. ③ Convolution Codes ④ Reed-Solomon Codes.
- Line Coding:
  - \* represent the final bit (1 & 0) in form of voltage or current.

### \* The need of Line Coding:

- ① self clocking @ Rx.
- ② Control the DC component (its BAD to have DC value)  $\Rightarrow$  Noise.
  - \* Codes which eliminate DC: Zero-DC, DC equalized.
- ③ To transmit @ high data Rate (which require small B).
- ④ Increase  $P_{signal} \Rightarrow$  increase SNR.
- ⑤ To Reduce amount of power @ low f. (important in telephony).

Line Coding	Procedure.	Bandwidth	Applications (3)
Unipolar	NRZ 1 → +P(t) 0 → Zero	$f_0$	TTL Logic.
	RZ same NRZ But it goes to 0 @ the middle of the bit time.	$2f_0$	
Polar	NRZ 1 → +P(t) 0 → -P(t)	$f_0$	computer motherboard & Ethernet (1000 Base-Sx & LX)
	RZ same but goes to zero @ the middle.	$2f_0$	
NRZI	1 → +P(t), -P(t), +P(t), ... 0 → No Transition.	$f_0$	CD, USB-port & Ethernet (100-Base Fx)
Bipolar (AMI)	1 → +P(t), -P(t), +P(t), ... 0 → Zero.	$f_0$	BBS, HDB3 & E <sub>1</sub> -system.
Darbinary	1 → +P(t) if # of 0's even. 1 → -P(t) if # of 0's odd. 0 → Zero.	$0.5f_0$	40 Gbit/s & 20 Gbit/s fiber Tx system.
MLT-3	1 → +P(t), 0 → -P(t), +P(t), ... 0 → NO Transition.	$0.9f_0$	Ethernet (100 Base Tx)
Manchester	1 → High to Low. 0 → Low to High.	$2f_0$	IEEE 802.3 & 802.4 Ethernet (10 Base-T)
M-ary	It make a table with number M-bits & gives them values (see Ex.).	$f_{\text{symbol}} = \frac{f_0}{\log_2 M}$	—

• Main disadvantage for Unipolar ⇒ has a DC value.

• Main advantage for all other types ⇒ has 0-DC value.

• Unipolar :   
 → Advantages: compatible with TTL logic (NRZ better than RZ).   
 → Disadvantages: → No self clocking & there is DC.

• Polar :   
 → Advantages: polar has  $P_{signal} > P_{signal}$  for unipolar ⇒ Better SNR   
 & polar NRZ has  $P_{signal} > P_{signal}$  of polar RZ   
 → Disadvantages: polar NRZ it is lack clock info.

• Bipolar (AMI) : → Disadvantage: when transmits along run of 0's, it produces No transition (suffers a Drawback).

• Doubinary :   
 → Advantages: smallest Bandwidth since  $(\frac{f_c}{2})$ .   
 ↳ Detection Errors without additional bits for that.   
 → Disadvantage: Low freq. Components.

• MLT-3 : → Advantages:   
 ↳ Emitting less EM interference.   
 ↳ small Bandwidth =  $0.9f$ .

• Manchester :   
 → Advantages: self clocking & zero-DC.   
 → Disadvantages: very long Bandwidth =  $2f$ .

• M-ary : → Advantage: it reduce the Bandwidth by  $\log_2 M$  ( $f_{sym} = \frac{f_0}{\log_2 M}$ ).

\*  $f_{symbol}$  &  $f_0$  :   
 → for all types without M-ary ⇒  $f_{sym} = f_0$ .   
 → for M-ary ⇒  $f_{sym} = \frac{f_0}{\log_2 M}$

\*\*Pulse Shaping:

⇒ We use it for:   
 ① Control PSD.      ② Decrease Bandwidth   
 ③ Reducing high freq.      ④ Eliminate Distortion like ISI (Inter symbol Interference).

\* Bandwidth for Raised Cosine:  $B = \frac{f_0}{2} (1 + \alpha)$    
 ↳  $f_0$  found After using the encoding type (polar, unipolar, manchester, ...).   
 ↳ Roll-off Factor.



Summary

\* All Abbreviations in this Handout provided as follows:

- ASK  $\equiv$  Amplitude Shift Keying.
- FSK  $\equiv$  Frequency Shift Keying.
- PSK  $\equiv$  Phase shift Keying.
- QAM  $\equiv$  Quadrature Amplitude Modulation.
- OOK  $\equiv$  On OFF Keying;
- BPSK  $\equiv$  Binary Phase Shift Keying.
- QPSK  $\equiv$  Quadrature (Quaternary) phase shift Keying.
- TCM  $\equiv$  Trellis Coded Modulation.
- AWGN  $\equiv$  Additive White Gaussian Noise.
- CCK  $\equiv$  Complementary Code Keying;
- OFDM  $\equiv$  Orthogonal Frequency Division Multiplexing.
- DVB  $\equiv$  Digital Video Broadcasting.
- DVB-T  $\equiv$  Digital Video Broadcasting for Terrestrial Television.
- DAB  $\equiv$  Digital Audio Broadcasting.
- DMT  $\equiv$  Discrete Multi-Tone Modulation.
- DQPSK  $\equiv$  Differential Quadrature Phase Shift Keying;

\* Shannon's Limit:  $C = B \log_2(1+SNR)$   $\rightarrow$  bps.

$C \equiv$  Channel Capacity: it is the Maximum number of binary bits that can be transmitted per second with probability of error as bitrarily close to Zero.

- Major Modulation Techniques : ASK - FSK - PSK - QAM.

(7)

### 1] ASK :

- for example send  $2A\cos\omega t \rightarrow$  logic 1 &  $A\cos\omega t \rightarrow$  logic 0
- special case of ASK: "OOK"  
it send  $A\cos\omega t \rightarrow 1$  & zero voltage  $\rightarrow 0$
- Polar NRZ + AM = ASK.
  - \* AM with  $m < 1 \Rightarrow$  ASK.
  - \* AM with  $m = 1 \Rightarrow$  OOK.
- $B_{ASK} = 2f_0$
- ASK  $\rightarrow$  (Advantages): simplest kind of modulation to generate & detect.  
 $\rightarrow$  (Disadvantages): Big BW =  $2f_0$  & used just @ very high SNR.

### 2] FSK :

- Mark frequency  $\rightarrow$  logic 1 & space frequency  $\rightarrow$  logic 0.
- Polar NRZ + FM = FSK.
- $B_{FSK} = 2\Delta f + 2f_0 = 2f_0(\beta + 1)$
- FSK (Advantages)  $\rightarrow$  vs. ASK the carrier has a constant amplitude, FSK has immunity to non-linearities, rapid fading, adjacent channel interference. it has ability to exchange SNR for BW. used in early slow dial-up modems.

### 3] PSK :

- BPSK: cosine with phase shift 0  $\rightarrow$  logic 1 & cosine with phase shift 180  $\rightarrow$  logic 0.
- Polar NRZ + PM = BPSK.
- Peak phase deviation  $\equiv \Delta\theta = \frac{\pi}{2}$   
 $\Rightarrow \theta_{max} - \theta_{min} = 2\Delta\theta = \pi$
- $B_{BPSK} = 2f_0$
- 4-ary + PM = QPSK.
- $B_{QPSK} = f_0$

### \* Constellation Diagram:

$\Rightarrow$  Axis are called I (in-phase) & Q (quadrature).

- BPSK: 2-points.
  - QPSK: 4-points
- } we take them with constant freq. & constant Amplitude.

- Highest order PSK: 8-PSK. "Highest practically".
- more than 8-phases: error-rate becomes too high.
- in PSK points are positioned in a circle:  
 Because:
  - gives Maximum phase separation.
  - best immunity to noise.
  - gives same carrier amplitude.

$$B_{M-PSK} = 2 \text{ Band Rate} = \frac{2f_0}{\log_2 M}$$

4] QAM:
 

- Analog QAM.
- Digital QAM.

- Analog QAM: used in NTSC & PAL where I & Q carry the components of chrominance information.

$$B_{QAM} = 2B$$

$$B_{M-QAM} = \frac{2f_0}{\log_2 M}$$

- Points must be closer to each other: for more susceptible to noise But results higher BER, so higher order-QAM deliver less reliably than lower order unless SNR is increased.
- Non-square Constellation: achieve better performance BUT harder to modulate and demodulate.
- TCM: it is the type Modulation that use an extra bit for parity not for data. [e.g send 7 bits → 6 bits for data → 1 bit for parity].

\* Performance of digital modulation techniques in presence of Noise:

- SNR  $\propto$  BER
- Good Quality: BER  $\leq 10^{-6}$
- The variance of the Noise ( $\sigma^2$ )  $\equiv$  Average Power of the Noise.
- $X \sim (0,1)$ :  $f(x) = \frac{1}{\sqrt{2\pi}} e^{-x^2/2} \Rightarrow Q(x) = 1 - F(x)$
- Use the table to find Q(x), if it is NOT in the table, Then do interpolation.

$$K = \log_2 M$$

$$T_{\text{symb}} = K T_0$$

Modulation with AWGN	BER
ASK	$Q\left(\sqrt{\frac{E_b}{N_0}}\right)$
FSK	$Q\left(\sqrt{\frac{E_b}{N_0}}\right)$
BPSK	$Q\left(\sqrt{\frac{2E_b}{N_0}}\right)$
QPSK	$Q\left(\sqrt{\frac{2E_b}{N_0}}\right)$

\* Comparison of Digital Modulation schemes:

• ON the BER curves: to the left "for the same  $E_b/N_0$ "  
less BER, need less SNR, better immunity to Noise.

\* Bandwidth for BPSK, QPSK, M-PSK, M-QAM found by:  $BW = 2 \times \frac{\text{Baud Rate}}{\log_2 M} = \frac{2 f_0}{\log_2 M}$

⇒ The following Table could be observed:

Modulation	Bandwidth	Modulation	Bandwidth
ASK	$2 f_0$	16-PSK	$f_0/2$
FSK	$2\Delta f + 2B = 2f_0(P+1)$	16-QAM	$f_0/2$
BPSK	$2 f_0$	64-QAM	$f_0/3$
QPSK	$f_0$	256-QAM	$f_0/4$
8-PSK	$2 f_0/3$		

\* Applications of Digital Modulation techniques:

- 1] IEEE 802.11 (Wi-Fi). "CCK"
- 2] IEEE 802.16 (Wi-MAX). "OFDM".
- 3] DVB "standard in Europe".
- 4] DAB "it use DQPSK".
- 5] ADSL "it use DMT".

Best of \* \* \* \*  
\* \* \* \* Luck.