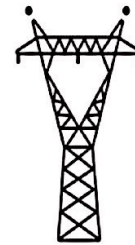



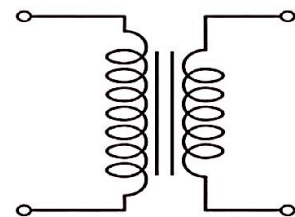
Communications I

F_{all017}



Dr. **M**hmd **H**awa 

 By: **M**hmd **A**buhashya



Powerunit-ju.com

Mohammad
Abu Hashya.

24

9/17/2017

Lecture 1: Introduction to Communication Systems

Dr. Mohammed Hawa
Electrical Engineering Department
The University of Jordan

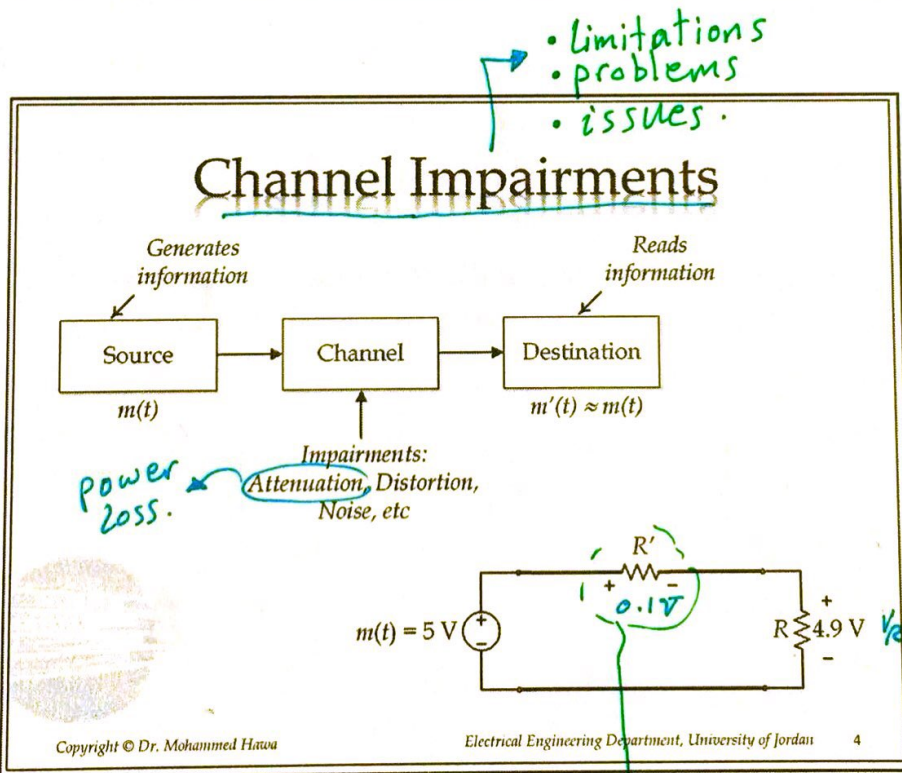
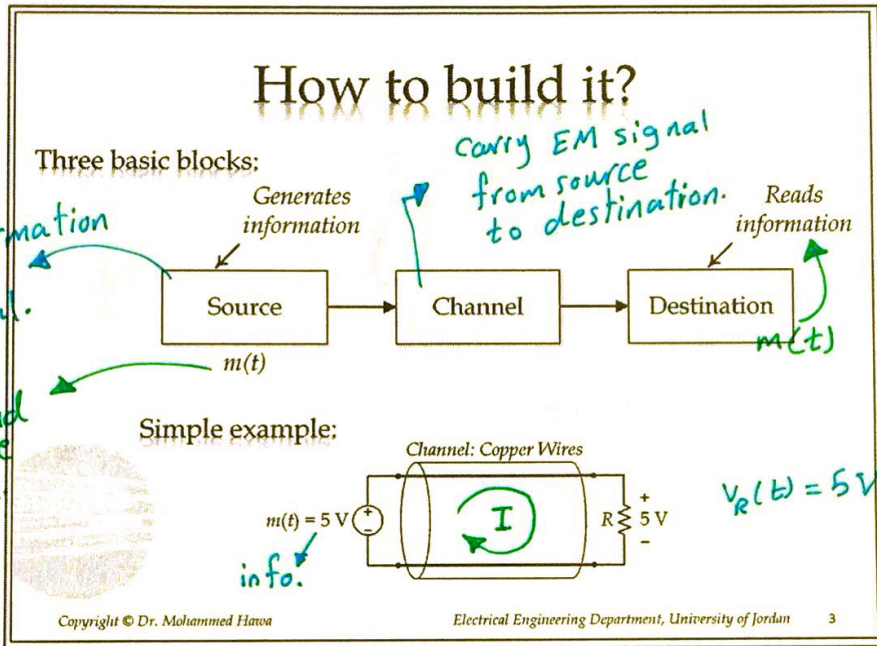
EE421: Communications I.

A Communication System

- Purpose of a communication system:
Carry information from one point to another.
- A typical communication system consists of three main components:
 - Source
 - Channel
 - Destination

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will absorb power
 → convert it to heat
 , this heat can't be recovered back.
 , so power loss.
 This called Attenuation.

the difference is the losses.

$V_{DC} = 5V \rightarrow P_{av} = DC^2 = 25W \Rightarrow \text{Average value} = DC = 5$
 $V_{AC} = 4\cos(\omega t) \rightarrow P_{av} = \frac{4^2}{2} = 8W \rightarrow \text{Average} = DC = \text{Zero.}$
 $V_{out_{DC}} = 4.9 \text{ volt} \rightarrow P_{av} = 4.9^2 W.$

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$$m(t)_{\text{average}} = DC = \frac{1}{T} \int m(t) dt.$$

$$P_{av \text{ in } m(t)} = \frac{1}{T} \int m^2(t) dt.$$

$rms = \sqrt{\frac{1}{T} \int m^2(t) dt}$
 $rms = \sqrt{P_{av}}$
 $rms^2 = P_{av}$

amplitude. \uparrow
 freq. (Hz) \uparrow
 $A \cos(2\pi f t + \theta)$
 $= \omega_1$
 angular freq. (rad/sec) \uparrow
 phase-shift or angle.

Channel Impairments

1. Attenuation: As the signal travels through the channel it loses some of its energy (power) as heat in the internal resistance of the channel. We say the signal is attenuated.

signal attenuated.

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Attenuation

- Attenuation can be problematic for long distance communications (say cross-country).

each time multiply by 0.9. $(0.9)^{300}$

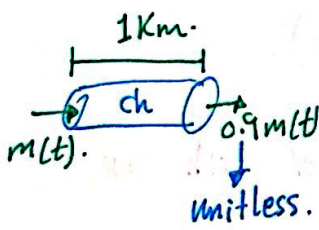
Amman. Agaba.

$V_{out}(t)?$

$(0.9)^{300} \times m(t) = 1.874 \times 10^{-14} \times m(t) \approx \text{Zero.}$

Almost Nothing reach Agaba. (Need solutions!)

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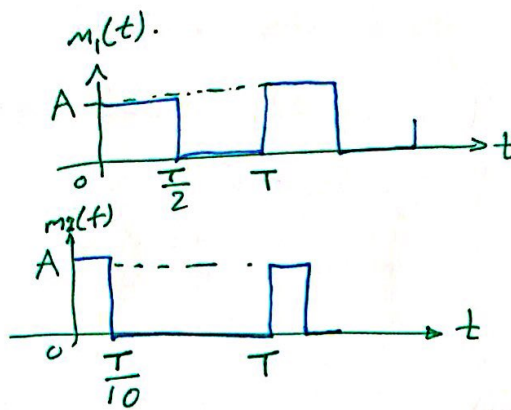
$$dB = 10 \log_{10} (\text{unitless})$$

*

Home work:

1) Find P_{av} & Average for:

2) Find P_{av} & Ave. for:



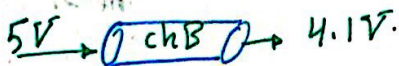
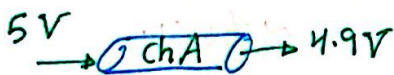
Answers:

1) $A_v = \frac{A}{2}$ & $P_{av} = \frac{A^2}{2}$

2) $A_v = \frac{A}{10}$ & $P_{av} = \frac{A^2}{10}$

**

1. Attenuation exists for all signal types.
2. = = = all channel types, But its level depends on the exact channel. used.
3. Attenuation level increases as the channel length increases. (Why?) → Because R' increases.



* Which channel has more attenuation?

CH B → more attenuation.
(more power loss).

* We care for the channel with less attenuation.

**

* memorize the following:

more expensive. ↓

wireless
copper wires
coax cable
waveguide & optical fiber.

↑ more Attenuation.

But should be used wisely.

voltage gain = $\frac{1}{(0.9)^{300}}$
 $= 5.3 * 10^{13}$
 (This will cause a large cost).
 ∞

Solutions to Attenuation

(a) Use Amplifiers:

(b) Use channels with smaller attenuation levels (e.g., optical fiber) - such channels are usually more expensive.

(c) Digital signals are less susceptible to attenuation (because of threshold detection at the receiver).

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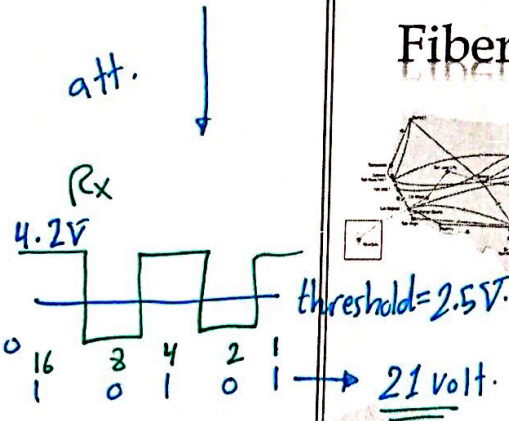
gain = $\frac{1}{(0.9)^{10}}$
 $= 2.868$

Rx don't care for the 5V & 0V.

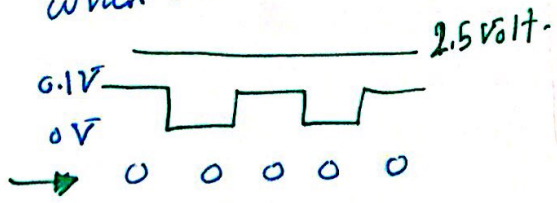


Fiber Cables for Long Distance

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Problem when use:

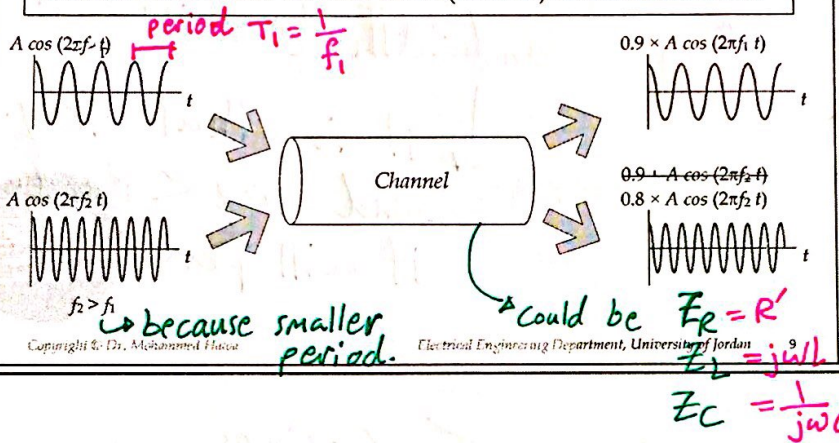


* Memorize the following:

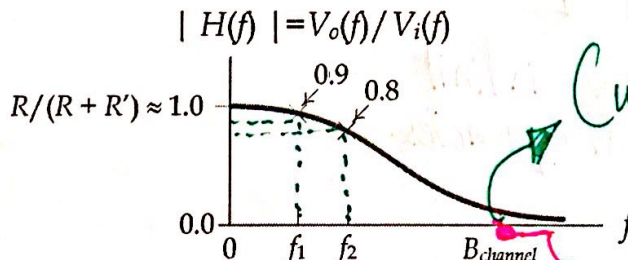
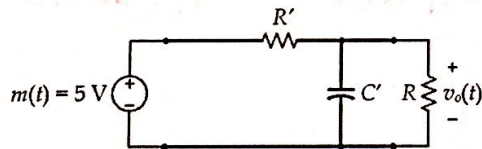
- For Copper wires you need an amplifier every 5-10Km.
- For Optical fiber you need an amplifier every 50-100Km.

Channel Impairments

2. Linear Distortion: The channel attenuation changes according to the transmitted signal frequency. Usually higher frequencies are attenuated more. Hence, the channel acts as a LPF that attenuates high frequencies, thus distorting the signal. We say the channel is a filter that has finite (limited) channel bandwidth.



Linear Distortion: Cause



Cutoff frequency.

Bandwidth of the channel is (always in) Hz.

Low freq $\Rightarrow Z_C \uparrow \Rightarrow$ open cct.
 High freq $\Rightarrow Z_C \downarrow \Rightarrow$ short cct.

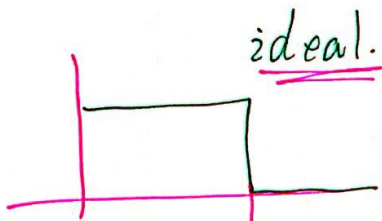
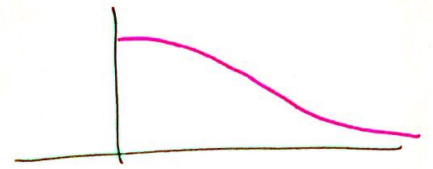
\Rightarrow LPF.
 Low freq \Rightarrow pass
 High freq \Rightarrow rejected.
 The signal is attenuated. (all of it).

The previous curve called:

* Attenuation Level:

or freq. Response function.

or freq. Transfer function.



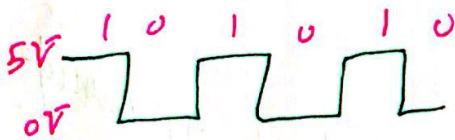
↓
cutoff = Bandwidth. (memorize).

↳ it is that freq., when you send $\text{freq} < \text{Bandwidth}$ it will pass, o.w reject.

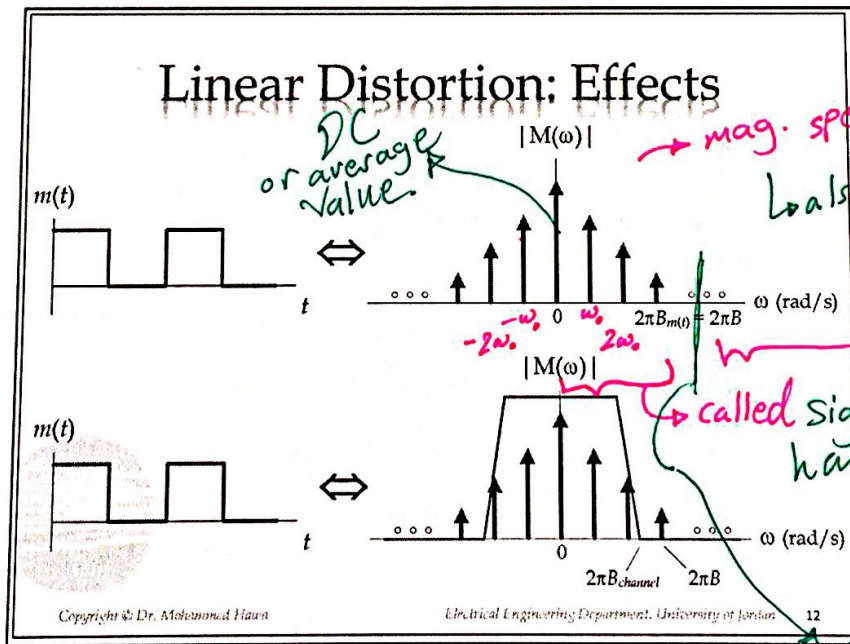
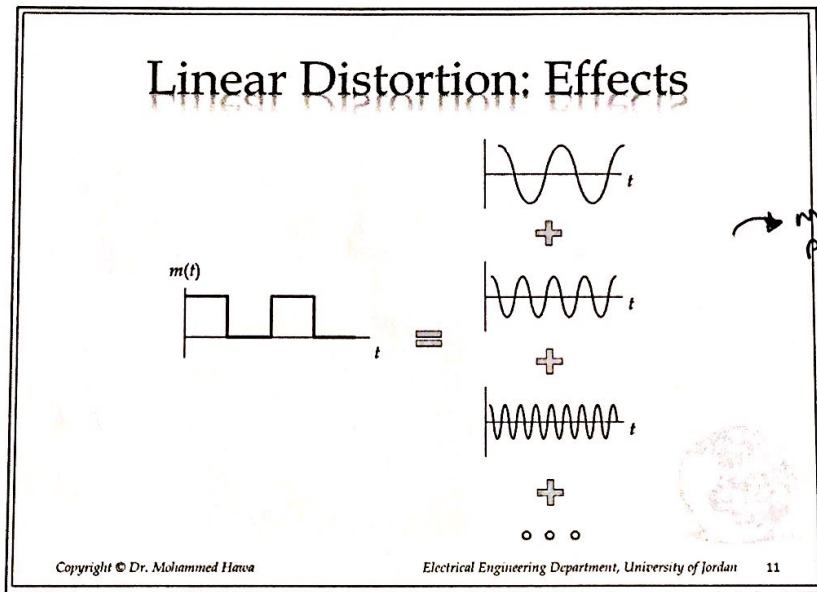
* Fourier:

$$m(t)_{\text{Periodic}} = \sum_{\infty} \text{Cosines.}$$

$\cos(\omega_0 t)$ $\cos(2\omega_0 t)$ $\cos(3\omega_0 t) \dots$



↳ has infinite frequencies.



* if we remove one of the insig. signals (No big change).

* " " " " " sig. " (Big change).

↳ Distortion.

Bandwidth of the signal.
 $m(t) = \int_{-B}^B m(t) dt$

Note that: there is bandwidth of the channel. $B_{channel}$.
 // // // // // signal. $B_{m(t)}$.

optical fiber \rightarrow BPF.

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Linearly-Distorted Signals

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To Summarize:

- Channel Bandwidth $B_{channel}$:
 - A property of the channel.
 - You read it from the data sheet of the channel.
 - The frequency after which the channel presents very high attenuation.
- Signal Bandwidth $B_{m(t)} = B$:
 - A property of the signal.
 - You figure it out from the Fourier transform of the signal.
 - The frequency above which $m(t)$ has insignificant (negligible) harmonics.
- **Rule of thumb:** signal bandwidth should be less than or equal to channel bandwidth.

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Bandwidth
of the channel.



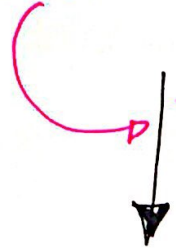
- Copper wires about 1 Km
- Coax cable. " "
- Optical fiber. " "

1-2 MHz.

1-2 GHz.

several THZ.

more
expensive.



Two advantages:

- less att. & - bigger Bchannel.

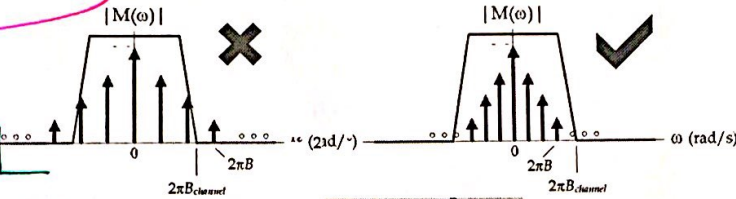
Solutions to Linear Distortion

(a) The message should fit in the channel bandwidth (either send at smaller data rate or use a better channel)

95%

send

instead of



(b) Use an Equalizer

complex device (expensive) used at the RX performs inverse gain

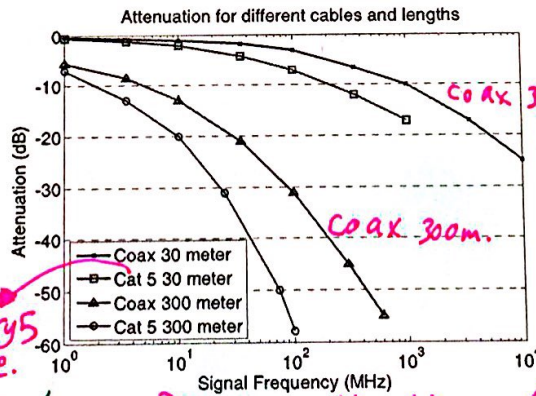


of ch. attenuation. (Need to know 4 things)

memorize.

(c) Pre-distortion @ Tx.

Channel bandwidth depends on channel type and channel length



more distance. more att.

category 5 cable. = Ethernet copper } higher att. than Coax.

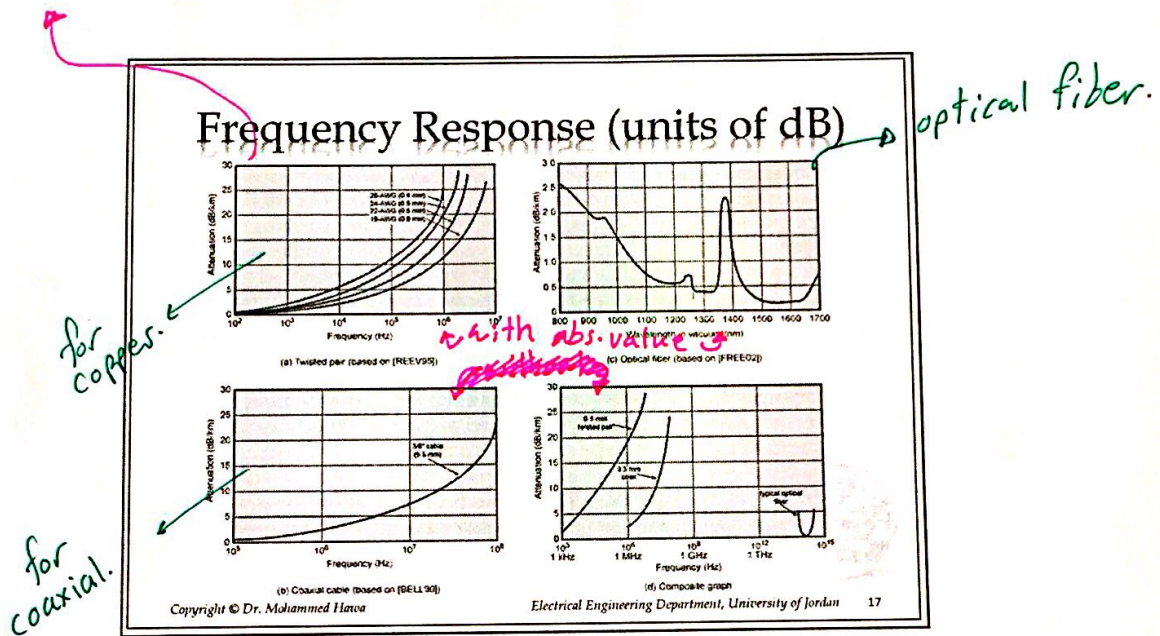
$\frac{P_{out}}{P_{in}} < 1$
 $10 \log_{10} \left(\frac{P_{out}}{P_{in}} \right) < 0$ dB.
 -ve

att \Rightarrow more att. \rightarrow Pout smaller \rightarrow Log₁₀ more negative.

Higher att. \rightarrow lower curve \rightarrow less B_{channel}.

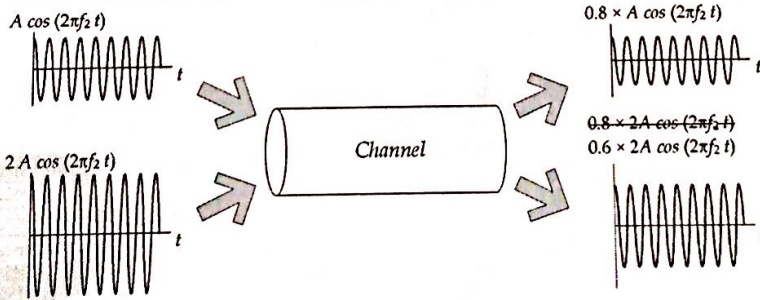
* Attenuation, always negative dB.
 Ex. what is Att of copper at 10^5 Hz?
 -5 dB/Km.

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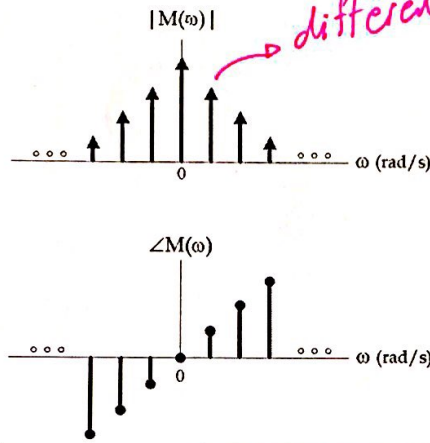
Channel Impairments

3. Non-Linear Distortion: The channel attenuation changes according to the transmitted signal amplitude and/or phase. Usually higher amplitudes are attenuated more. This causes distortion to the signal.



amp \uparrow \Rightarrow att \uparrow (depends on the physics of the channel).

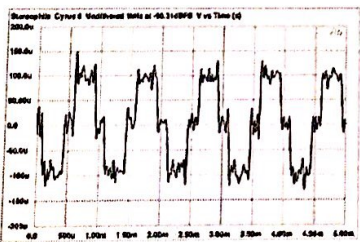
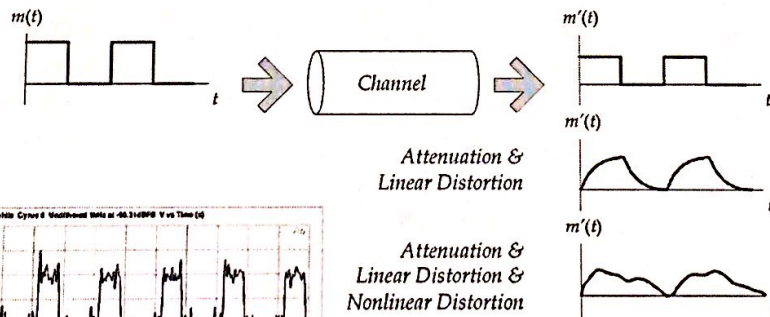
Fourier Transform Again!



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Non-Linearly-Distorted Signals



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Distorted signals are not desired!



- Solutions to Non-Linear Distortion: Use an Equalizer.

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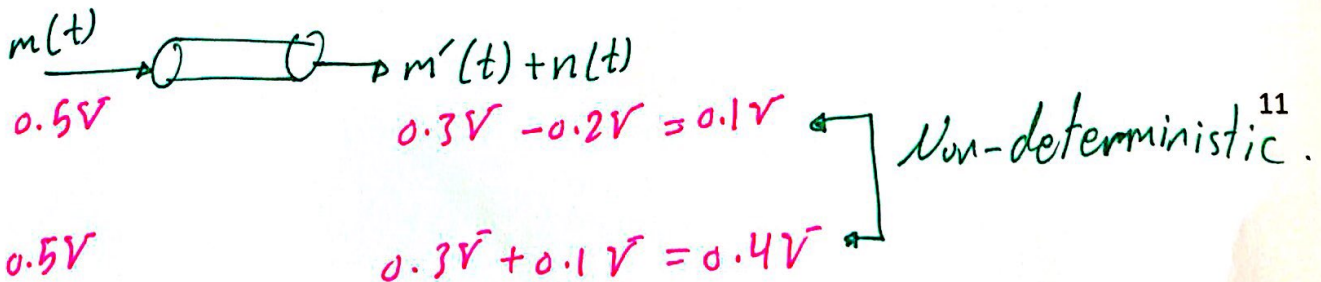
Channel Impairments

4. Noise: All the undesired signals (not part of the original signal) that are added by the channel. Noise is a random (*non-deterministic*) signal generated by external and internal sources.

- **External Sources:** interference from signals transmitted on nearby channels (crosstalk), interference generated by contact switches, automobile ignition radiation, fluorescent lights, natural noise from lightning, solar radiation, etc.

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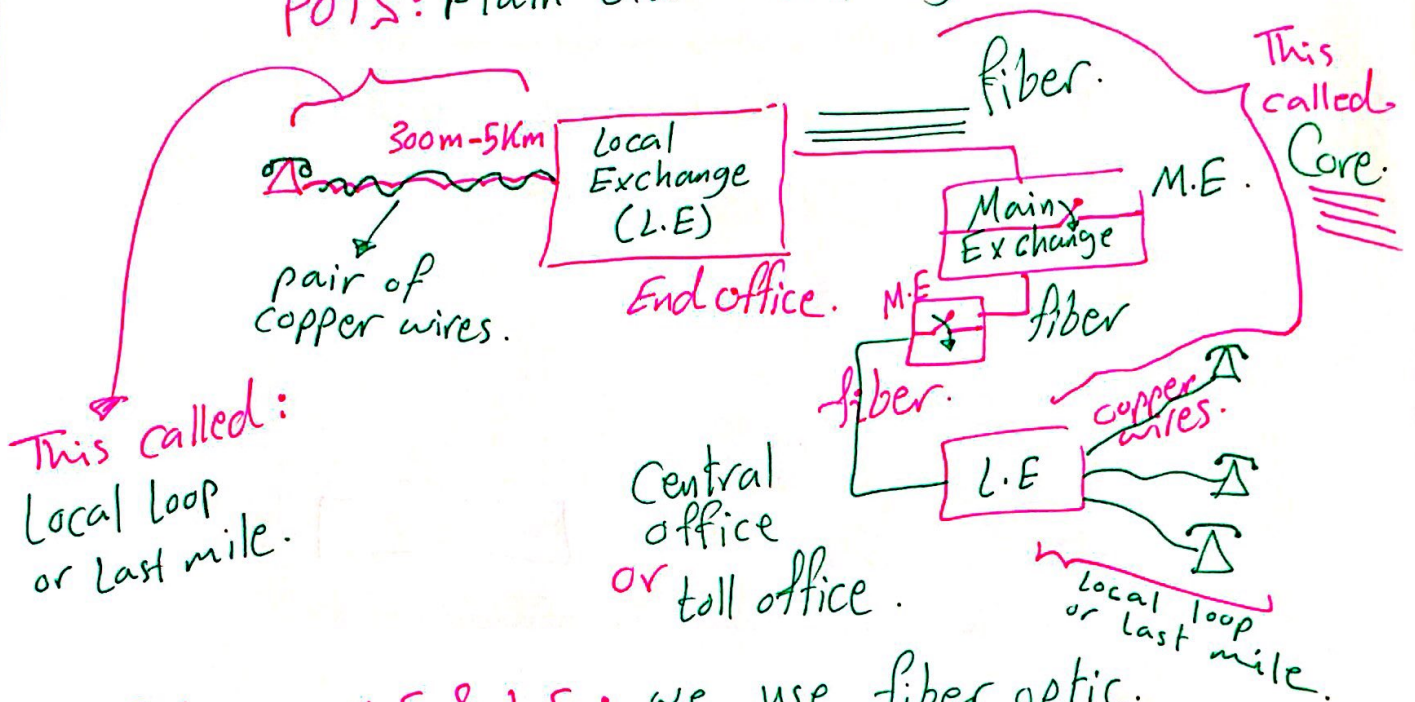
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* Landline Telephony Systems:

↳ PSTN: Public switched Telephony Network.

POTS: Plain Old Telephony Service.



- Between M.E & L.E: we use fiber optic.
- Between L.E & Telephone: we use copper.
- Between 2 Local Exchanges \Rightarrow there's M.E.

Example External Noise: Crosstalk

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L.E

$i_1' + \underbrace{i_2 + i_3 + i_4}_{n(t)}$

Noise

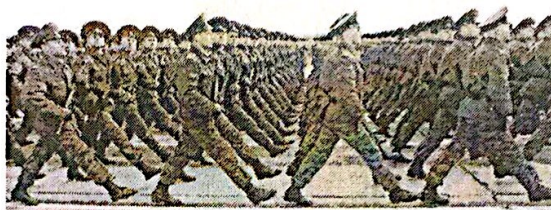
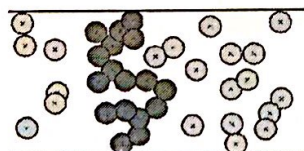
Internal Noise

Thermal Noise.

- Internal Sources:** thermal noise (random motion of electrons in conductors, random diffusion and recombination of charged carriers in electronic devices).

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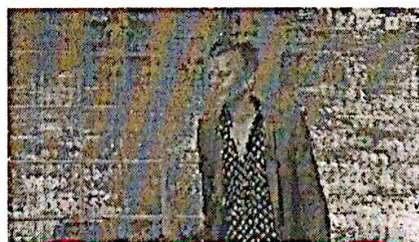
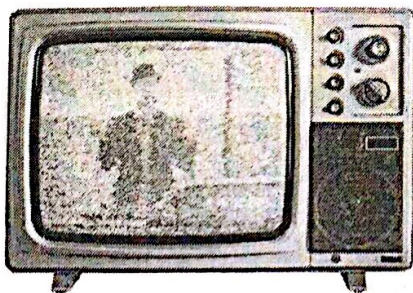
Moving Electrons



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Noisy signals are not desired!



- The effects of external noise can be minimized or eliminated.
- The effects of internal noise can be minimized but never eliminated.

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& cheap & effective.

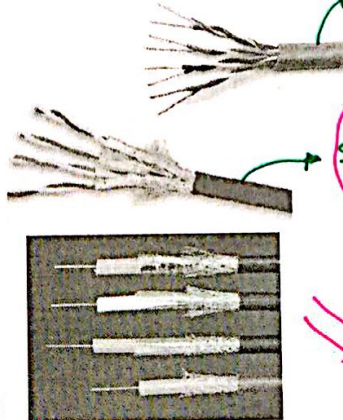
As more as you twisted as more as the vector changes & minimize the magnetic field



very effective But very expensive.

Solutions for External Noise

- a) Shielding or twisting.
- b) A different cable design.
- c) Proper design of the whole system.
- d) Using BPF or LPF at the receiver side.
- e) Use digital transmission.



Unshielded Twisted pair UTP

shielded twisted pair STP

coax & fiber fiber optic

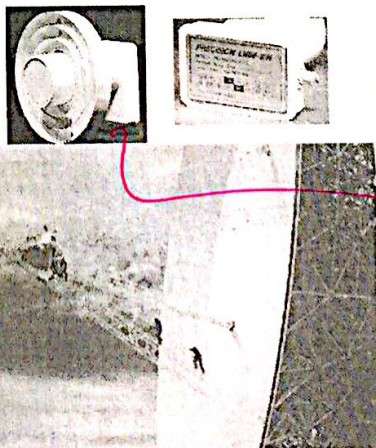
very effective & very cheap.

(d) first solution (e) second solution. & others: depend on the costs & other things.

very effective & becoming cheap.

Solutions for Internal Noise

- a) Cooling.
- b) Using BPF or LPF at the receiver side.
- c) Use digital transmission.



LNA: Low Noise Amplifier. LNB: Low Noise Block.

These two are the top solutions.

cooling: very effective But very expensive.

We need this solution (e.g. satellites).

wifi



$f = 2.4 \text{ GHz}$

interference
between both
of them

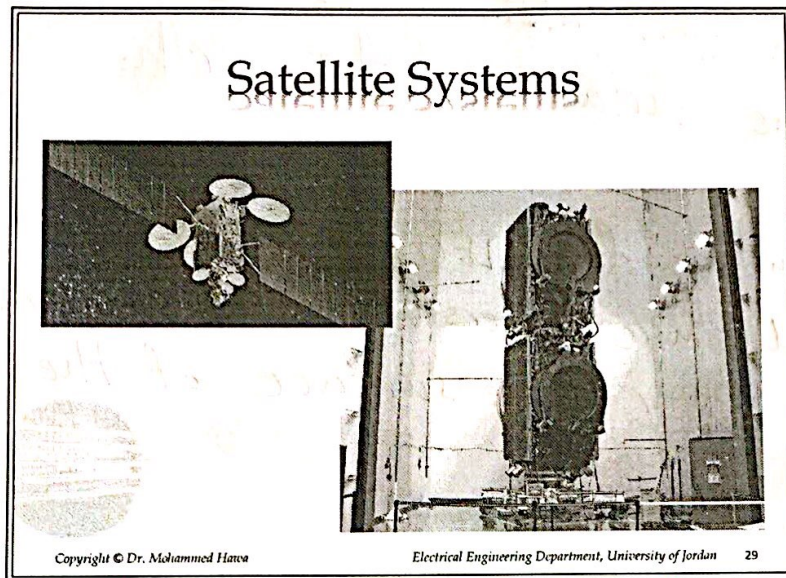
wifi



$f = 2.4 \text{ GHz}$



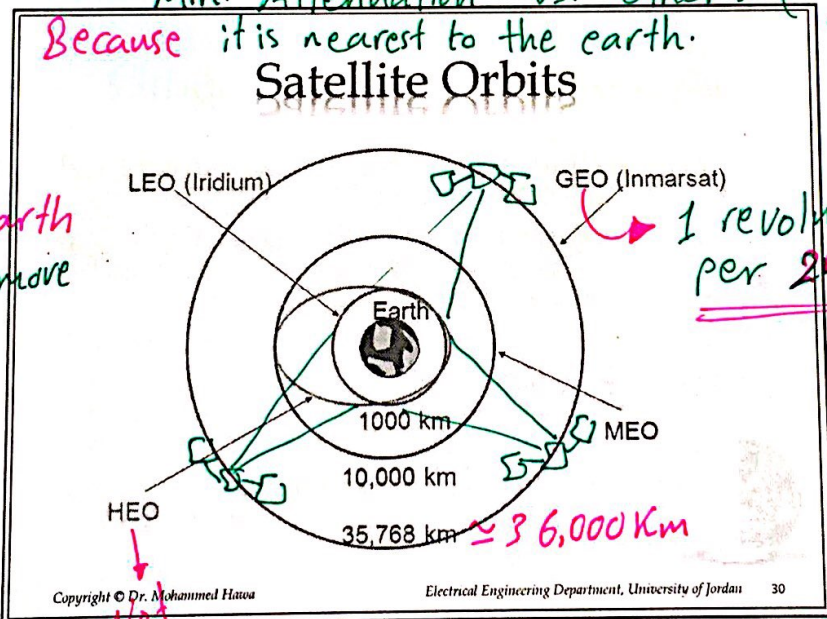
better to move
them away from
each other.



***What is the advantage of LEO?**

Min. Attenuation vs. others. (Min Att. & external noise)

Because it is nearest to the earth.



*if you are closer to earth the satellites move faster.

min. number of satellites for GEO: 3

1 revolution per 24 hours.

memorize:

- 1,000 km → LEO: Low Earth Orbit.
- 10,000 km → MEO: Medium Earth Orbit.
- 36,000 km → GEO: Geostationary (Geosynchronous) Earth Orbit.

* Advantages of GEO:

1) Easier To install Rx.

2) Min # of satellites is 3. to cover the surface of the earth.

* Disadvantage for LEO:

• Need more numbers of satellites than GEO To cover the surface of the earth.

* LEO: (Iridium), (Global Star), (ISS)

* MEO: (GPS), (GLONASS), (Galileo).

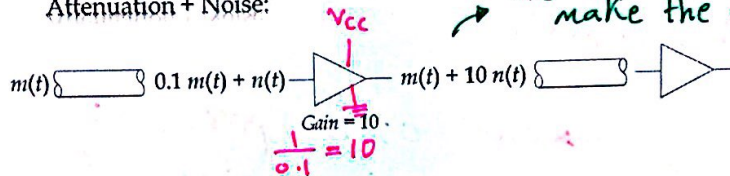
↓
international
space
station.

* GEO: (Inmarsat), (Thuraya), (TV Broadcasting)

↳ (Nilesat, Badr, Hotbird).

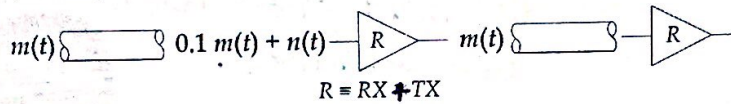
Impairments ALL Together

Attenuation + Noise:



we solve one issue, but we make the other one much worse.

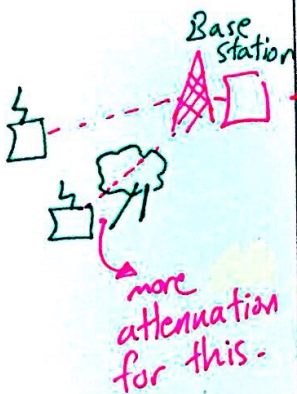
We need new solutions: Regenerators (Digital Transmission)



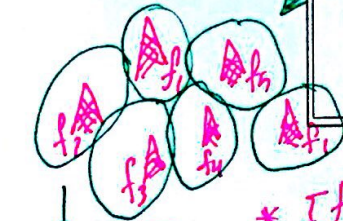
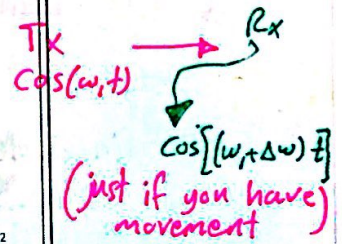
Memorize each one of them & for what specific wires. (channels)

Other Channel Impairments

5. **Fading:** Variable attenuation with time of day and receiver location (wireless systems).
6. **Doppler Shift:** Shift in the frequency of the transmitted signal. Shows up when we have a wireless channel and fast moving objects.
7. **Frequency-reuse interference:** Shows up in wireless systems when we re-use the same frequencies at multiple nearby locations to increase system capacity.
8. **Chromatic Dispersion:** Specific to optical fiber channels.

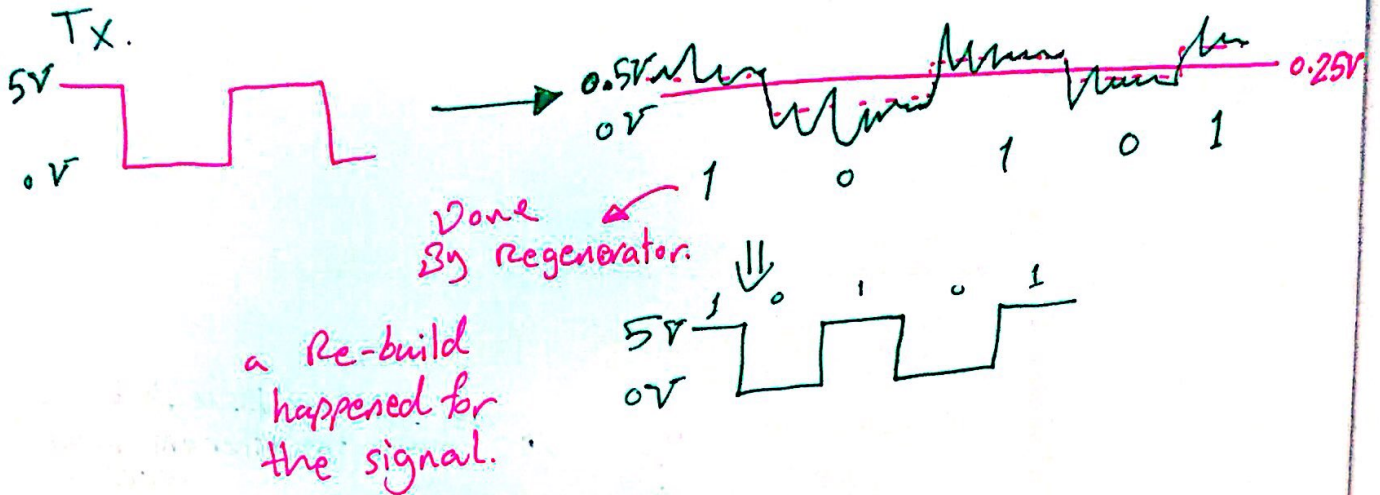


e.g. (wireless) satellites & Airplanes.



we reuse To increase system Capacity

* If he asked about Impairments for fiber optic? it will be 5 impairments. & so on for others. => for wireless: 7 impairments. (Doppler just if there) is movement



→ one of the problems:

is that if a regen. do a mistake the next other regen. will do the same mistakes.

Disadvantage for Regen:

It very Difficult to Build (Need multiple Transistors) unlike the amplifier (Need one Transistor).

* Regen. : it is Transmitter & Receiver.

* The Range of the sent. digital signal

could be increased But as long as it increased it will face more Non-linear distortion.

remember the following: $\log_2(x) = \log_2 10 \log_{10}(x) \approx 3.322 \log_{10}(x)$.

9/17/2017

Shannon's Limit

$C = B_{ch} \times \log_2(1 + SNR)$

finite Number.

- C: Capacity of the channel in bits/second (bps)
- B_{ch} : Channel bandwidth (units of Hz)
- SNR: Signal-to-Noise Ratio (unitless)(not dB)

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Capacity: the maximum (bps) that you can send through the channel.

if $B_{ch} \downarrow \Rightarrow \Rightarrow C \downarrow$

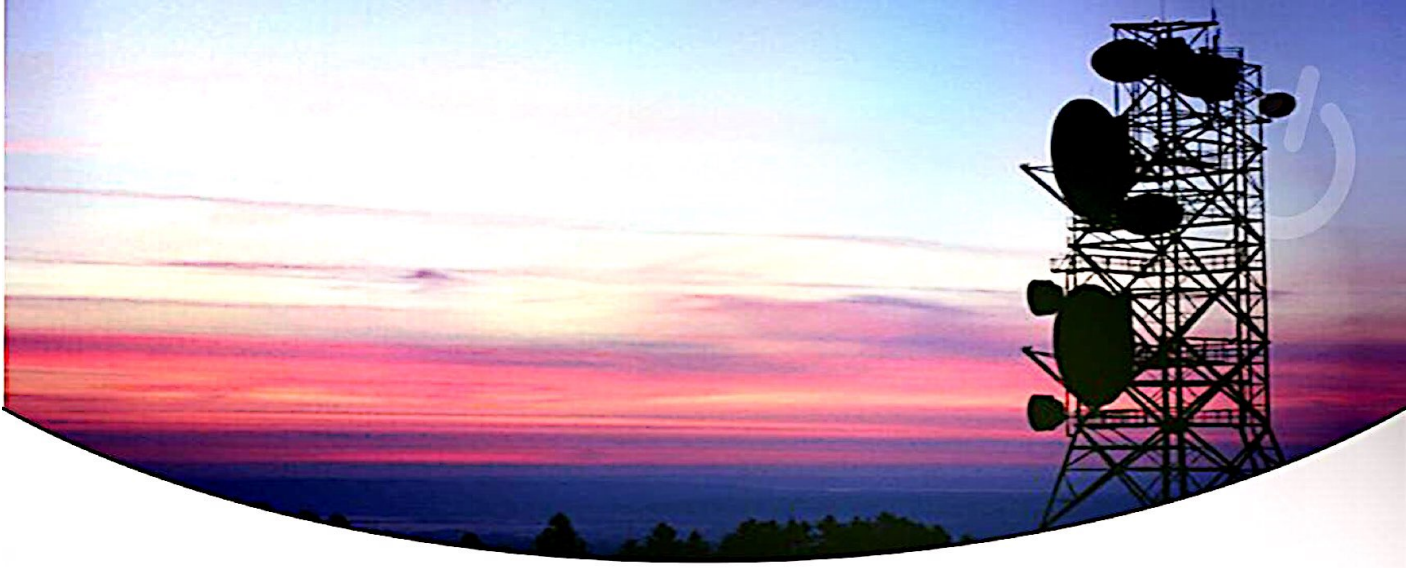
$$SNR = \frac{\text{signal power}}{\text{noise power}}$$

more att. \uparrow
 \hookrightarrow signal power \downarrow
 \hookrightarrow SNR \downarrow
 \hookrightarrow C \downarrow

also More Noise power $\uparrow \Rightarrow SNR \downarrow \Rightarrow C \downarrow$

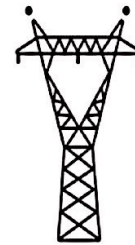
* if we were given that SNR = 30 dB
 \Rightarrow We want to find C \Rightarrow You have to Convert dB to unitless.

SNR = 1000 unitless.




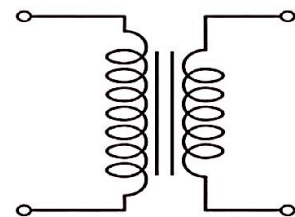
Communications I

Fall 2017



Dr. **M**hmd **H**awa 

 By: **M**hmd **A**buhashya



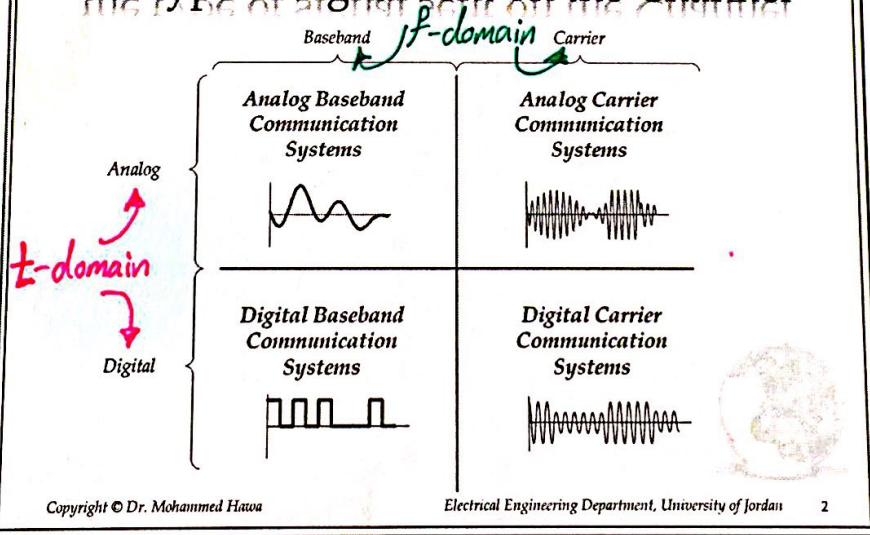
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Lecture 2: Classification of Communication Systems

Dr. Mohammed Hawa
Electrical Engineering Department
The University of Jordan

EE421: Communications I

Comm Systems are classified based on the type of signal sent on the Channel



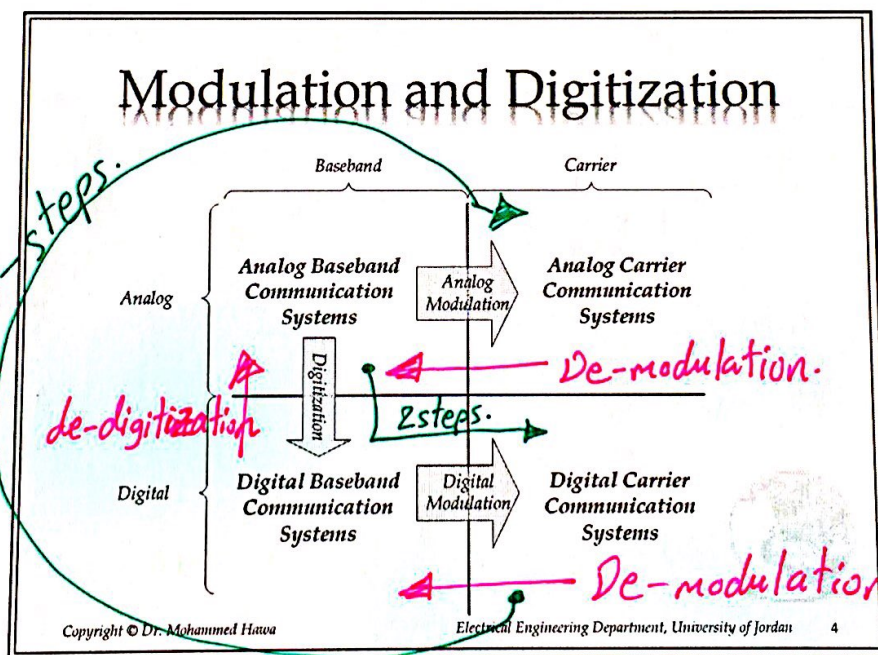
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Each system has its advantages!

<p style="text-align: center;"><i>Analog Baseband</i></p> <ul style="list-style-type: none"> • Simplest system to build • Inexpensive 	<p style="text-align: center;"><i>Analog Carrier</i></p> <ul style="list-style-type: none"> • Allows use of Antennas • Allows Multiplexing (FDM) • Allows exchanging SNR for Bandwidth
<p style="text-align: center;"><i>Digital Baseband</i></p> <ul style="list-style-type: none"> • Immunity to Noise • Allows Multiplexing at baseband level (TDM) • More bandwidth efficient • Allows exchanging SNR for Bandwidth • For more, see Handout 	<p style="text-align: center;"><i>Digital Carrier</i></p> <ul style="list-style-type: none"> • Allows use of Antennas • Allows Multiplexing (FDM) • Allows exchanging SNR for Bandwidth • Also the advantages of digital baseband

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- **Analog Modulation** : the process that take you from Analog Baseband to Analog Carrier. 2
- **De-Modulation** : The Reverse process (Analog carrier to Analog Baseband).

* Analog vs. Digital t-domain (As shown in previous slides.)

* Baseband vs. Carrier f-domain.

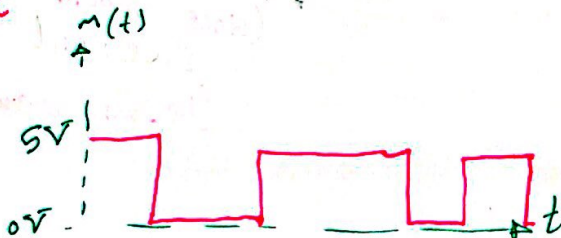
* Periodic vs. aperiodic } t-domain.
 } f-domain.
 we know if repeats itself or Not.
 we know from smooth curve or impulses.
 aperiodic
 periodic.

Ex.1



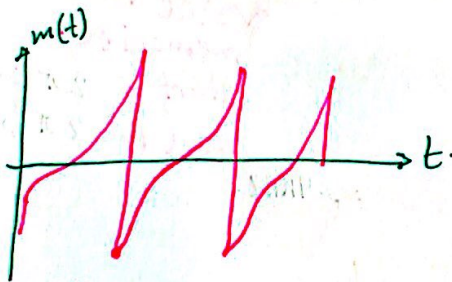
it is Digital & periodic.

Ex.2



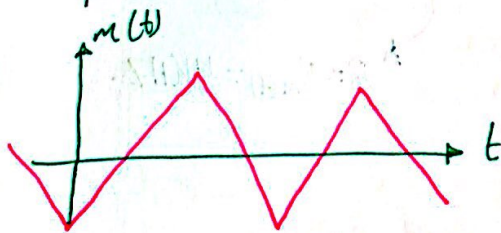
it is Digital But aperiodic.

Ex.3



it is Analog & periodic.

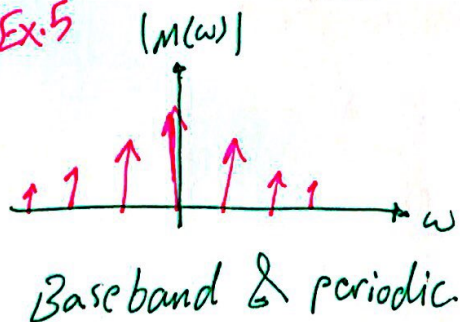
Ex.4



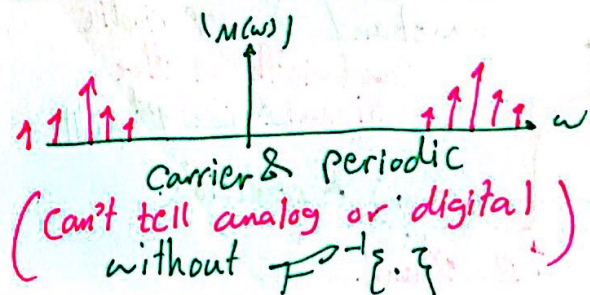
periodic.
 => Analog OR Digital

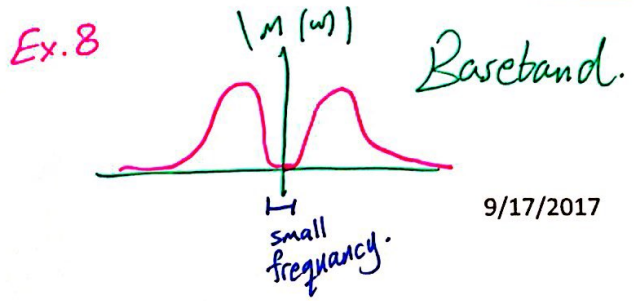
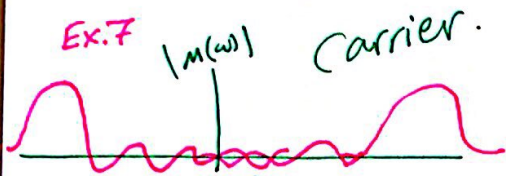
(look at Rx threshold).
 if it use threshold (Digital)
 if Not, and reads voltages (Analog).

Ex.5

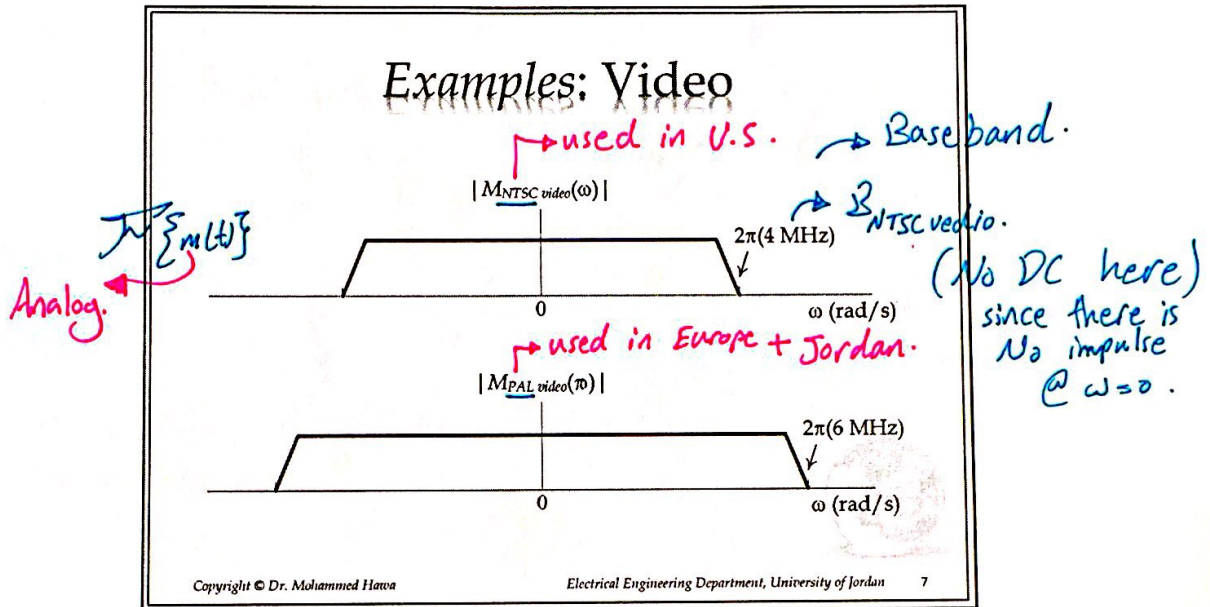


Ex.6





9/17/2017



Analog Baseband Systems

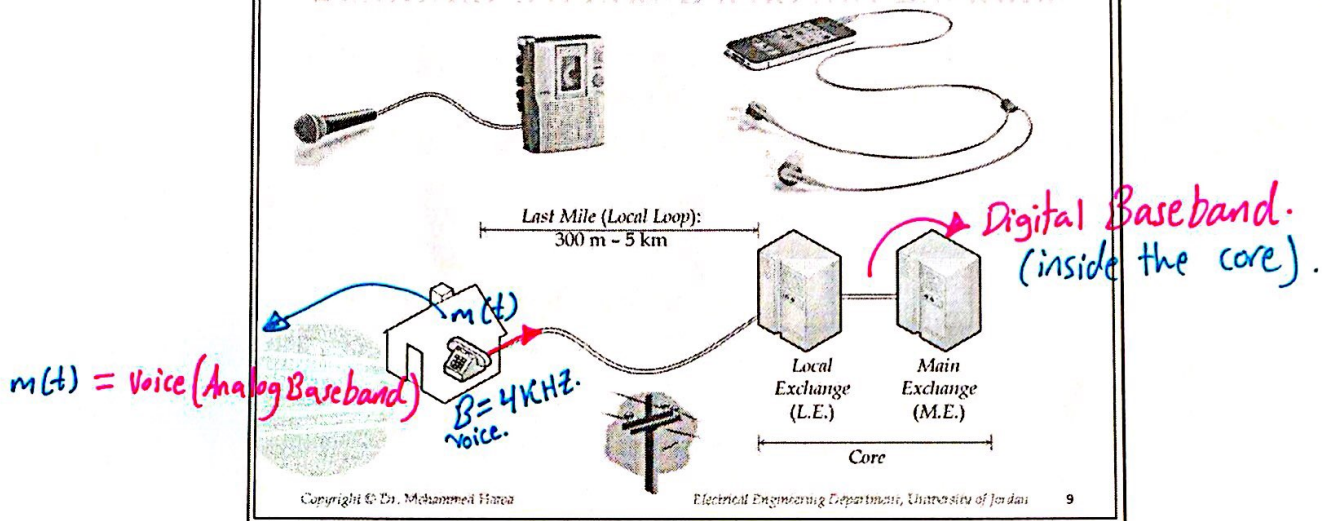
- An analog baseband system sends the analog baseband signal $m(t)$ as is (without any modifications).
- Advantages:
 - Simplest possible system.
 - Inexpensive to build.
- Usually used for short-distance communications.
- Examples of such systems in the next slide.

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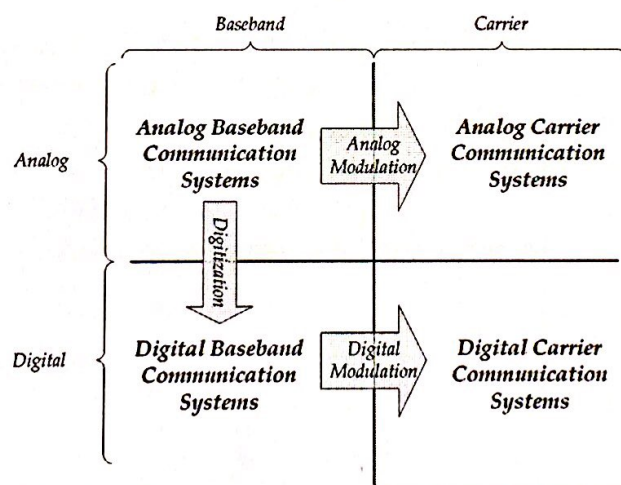
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Example Analog Baseband Systems



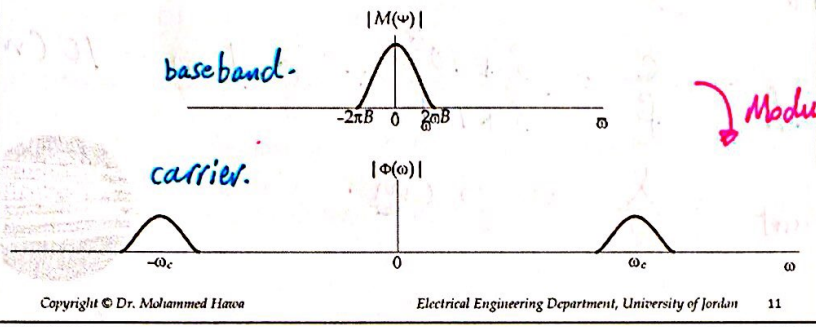
Modulation and Digitization



Modulation

- In modulation, the signal $m(t)$ is combined with a high-frequency signal called the carrier.
- Hence, frequencies are shifted.

shift \equiv Modulation.



Modulation. De-modulation.

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FDM: Frequency Division Multiplexing.

Multiplexing: sending multiple signals simultaneously over the same channels, without interference.

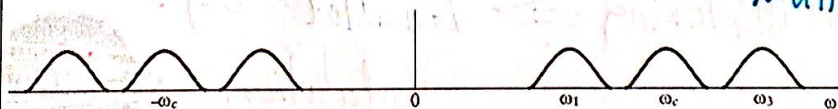
Analog and Digital Carrier Systems

- Modulation (i.e., analog and digital carrier systems) advantages:

- Allows the use of reasonable antenna lengths. (necessary for wireless channel).
- Allows Multiplexing (FDM). As well as CDMA and OFDMA in digital systems.
- Allows exchanging SNR for Bandwidth.

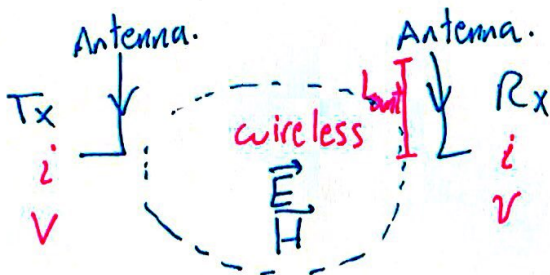
Code Division Multiple Access.

next page



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$L_{ant} = \frac{\lambda}{2}$ → wave length.

$\lambda = \frac{c}{f}$ → speed of light.
→ freq. of signal (HZ).

* human voice. (• take a freq. = 3000 Hz).
for easier calculations.

$$\lambda_{\text{voice}} = \frac{c}{f} = \frac{300,000 \text{ Km/s}}{3000 \text{ Hz}} = \underline{\underline{100 \text{ Km}}}$$

$$L_{\text{ant}} = \frac{\lambda}{2} = \underline{\underline{50 \text{ Km}}}$$

* Wifi (f = 2.4 GHz \rightarrow \sim 3 GHz)

$$\lambda_{\text{wifi}} = \frac{c}{f} = \frac{3 \times 10^8}{3 \times 10^9} = 0.1 \text{ m} = \underline{\underline{10 \text{ cm}}}$$

$$L_{\text{ant}} = \frac{\lambda}{2} = \underline{\underline{5 \text{ cm}}}$$

** We can't do Wireless Without Antenna.

memorize :

CDMA: Code Division Multiple Access.

OFDMA: orthogonal Frequency Division Multiple Access.

For Multiplexing \Rightarrow Enabled by:
Modulation & Digitization.

* always Wireless. use modulation.

9/17/2017

Example Carrier Systems

- Examples of **analog carrier systems**:
 - AM and FM radio broadcasting.
 - Analog TV broadcasting (NTSC and PAL).
- Examples of **digital carrier systems**:
 - Digital radio broadcasting (DAB).
 - Digital TV broadcasting (DVB-S, DVB-T, ATSC)
 - WiMAX metropolitan area network.
 - Wi-Fi wireless local area network.
 - Cellular Telephony (2nd, 3rd and 4th generations).
 - Bluetooth, Zigbee and NFC
 - Old dial-up modems.
 - ADSL modems.

AM: Amplitude Modulation.
FM: Frequency //

DAB → memorize the shortcut.

DVB: Digital Video Broadcasting
S- for satellites.

Not wireless.
(wired).

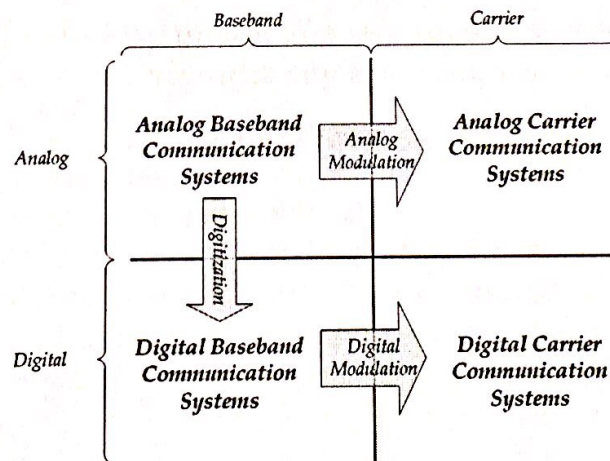
digital modulation.

e.g. connecting modem with the Telephone.

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Modulation and Digitization



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Digitization

- To convert the analog baseband signal into a digital baseband signal :

- ① - Sampling.
- ② - Quantization.
- ③ - Mapping.
- ④ - Encoding (coding).
- ⑤ - Pulse Shaping.

memorize the 5 of them respectively.

- Digital baseband Advantages:
 - Immunity to Noise, and Attenuation.
 - Allows Multiplexing at baseband level (TDM).

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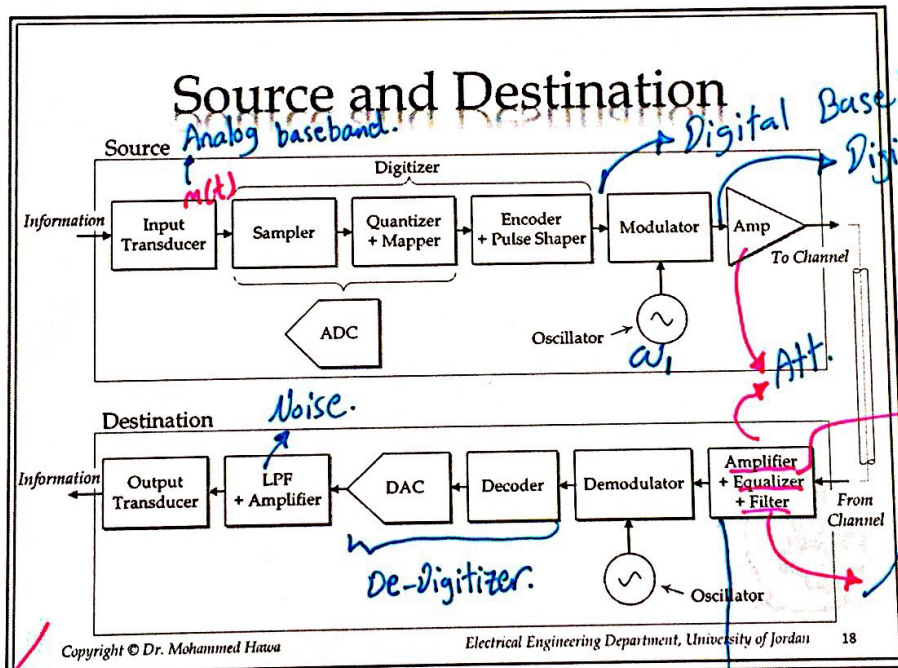
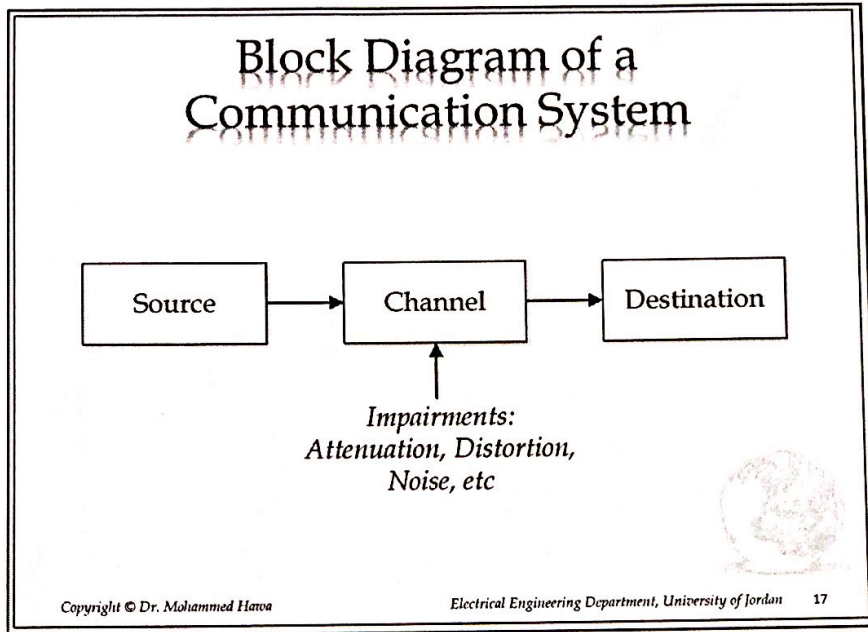
TDM: Time Division Multiplexing.
↳ enabled by Digitization.

Example Digital Baseband Systems

- Digital baseband Advantages (Continue):
 - More bandwidth efficient (compression and line coding).
 - Allows exchanging SNR for Bandwidth at the baseband level.
 - For more, see Handout.
- Examples of digital baseband systems:
 - Serial (RS-232) and USB port connections.
 - Ethernet (a popular local area network).
 - Telephony (between local exchanges), such as the T-1, T-2, ..., E1, E2, ... etc PDH carriers. (in the core).

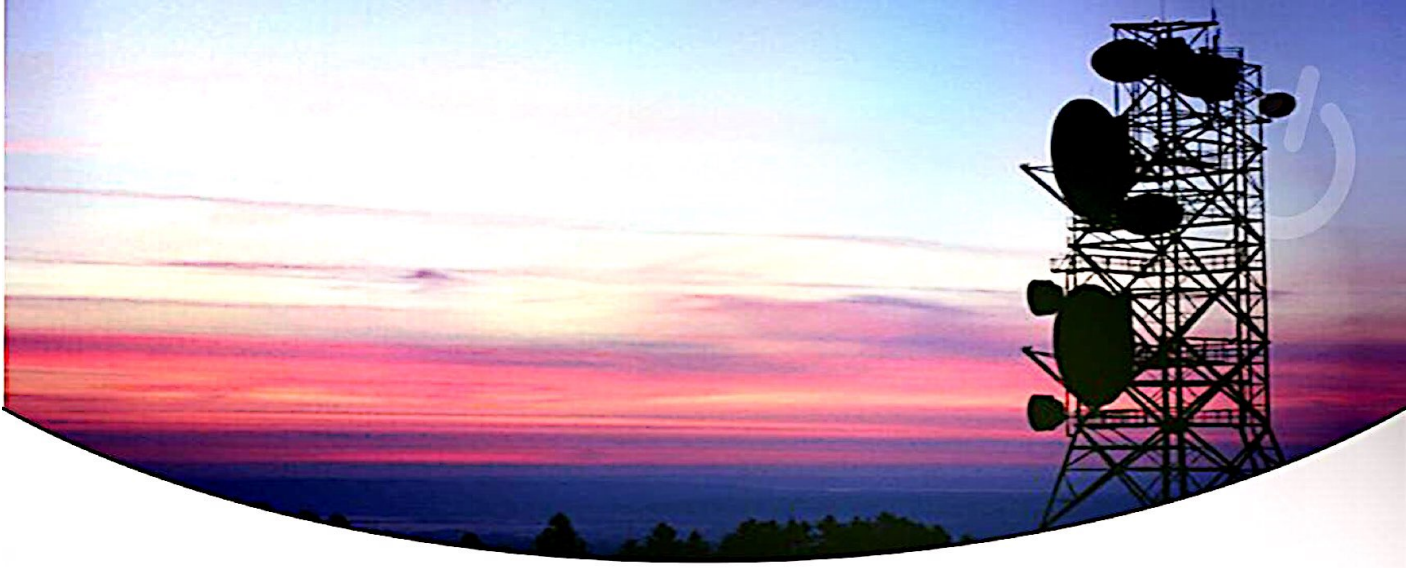
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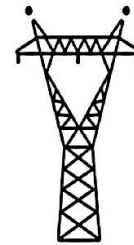
This system classification:

- Digital Carrier. (since it sent by the channel!).
- To make it Digital Baseband (remove Modu. & De-modu.)
- To make it Analog Baseband (" " " also digitizer & De-Dig.)




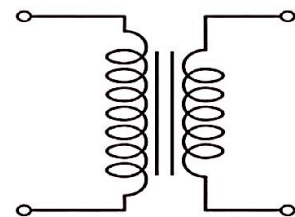
Communications I

Fall 2017



Dr. **M**hmd **H**awa 

 By: **M**hmd **A**buhashya



Powerunit-ju.com

Lecture 3: Review of Signal Analysis Basics

Dr. Mohammed Hawa
Electrical Engineering Department
University of Jordan

EE421: Communications I

Exponential vs. Compact

Complex exponential form:

$$\rightarrow x(t) = \sum_{n=-\infty}^{\infty} \alpha_n \cdot e^{jn\omega_0 t}, \quad \omega_0 = \frac{2\pi}{T}$$

\rightarrow complex exp. fourier series Coefficient.

$$x(t) = \frac{c_0}{2} + \sum_{n=1}^{\infty} c_n \cos(n\omega_0 t - \theta_n), \quad \omega_0 = \frac{2\pi}{T}$$

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Memorize:

$$\omega_0 \equiv \text{Fundamental Frequency} = \frac{2\pi}{T} \neq 2\pi * \text{Bandwidth of } m(t) = 2\pi B$$

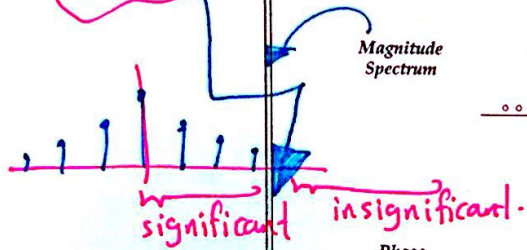
* Fourier: • Fourier Series $\rightarrow x(t)_{\text{periodic}} = \sum_{\infty} \text{Cosines.}$

* Why we use the mag. spectrum?
To find the Bandwidth
of the signal.

Need to describe
three things:

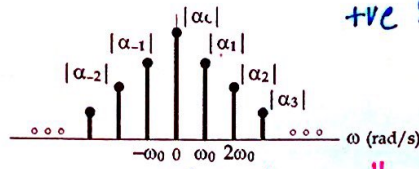
- Amplitude.
- Frequency.
- Phase shift.

Bandwidth of the signal.
 $2\pi B_m(t)$



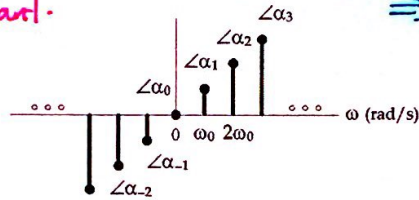
Exponential Fourier Series

Magnitude Spectrum



+ve & -ve ⇒ gives cosine

Phase Spectrum



Always the 1st harmonic (first freq) ⇒ Fundamental.

found by $\frac{2\pi}{T}$.

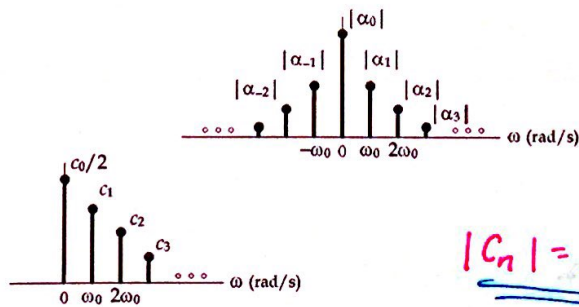
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3

1

Single-Sided vs. Double-Sided



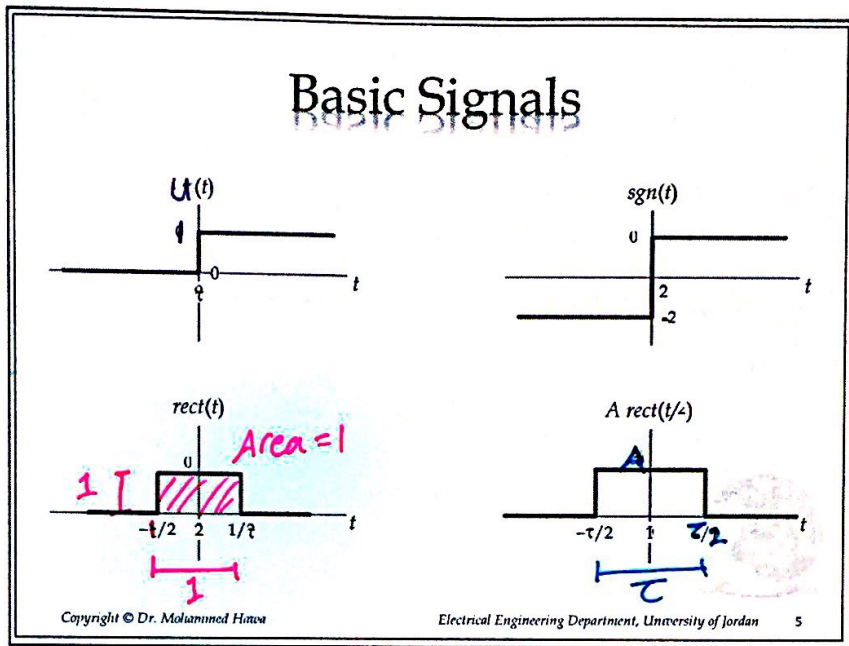
$|c_n| = 2|\alpha_n|$

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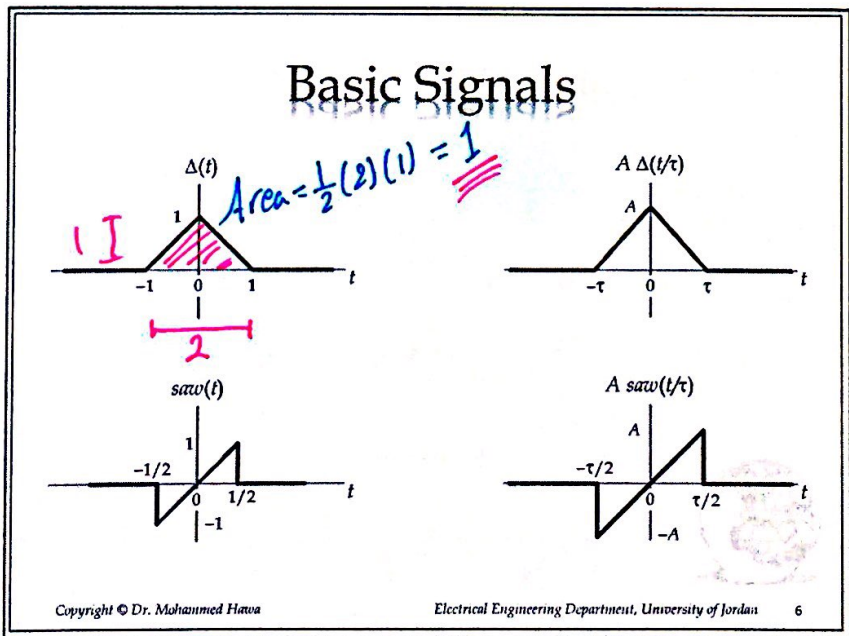
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2

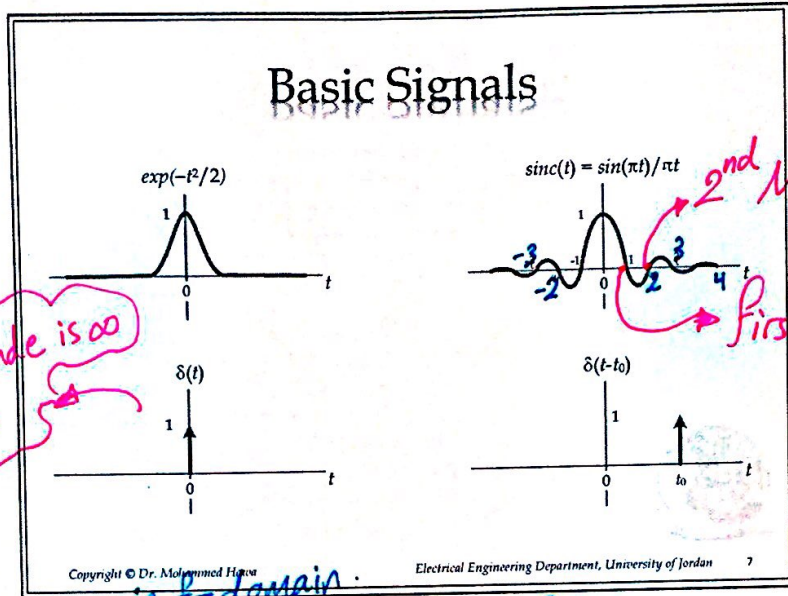


Always the area should be (1).

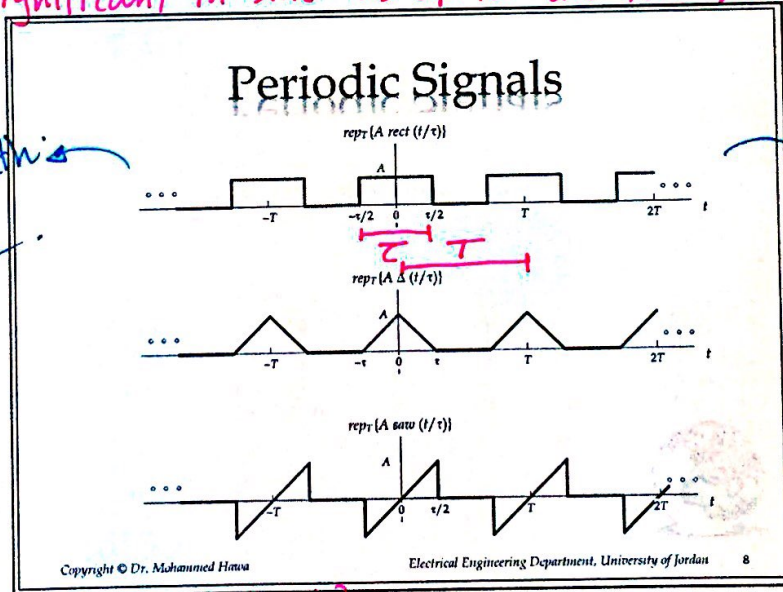


* Sinc: $\text{sinc}(t) = \frac{\sin \pi t}{\pi t}$ \Rightarrow Always use this form.
 $\text{sinc}(t) = \frac{\sin(t)}{t}$

9/28/2016



* whenever you see $\text{sinc}(\cdot)$, $\text{sinc}^2(\cdot)$ or $\text{sinc}^n(\cdot)$ in f -domain \Rightarrow The first Null is the Bandwidth.
 "significant in sinc is up to the first Null"



$$\alpha_n = \frac{A\tau}{T} \text{sinc}\left(\frac{n\omega_0\tau}{2\pi}\right)$$

$$\alpha_0 = \frac{A\tau}{T}$$

$$\alpha_1 = \frac{A\tau}{T} \text{sinc}\left(\frac{\omega_0\tau}{2\pi}\right)$$

$$\downarrow$$

$$\text{Sinc } x = \frac{\sin \pi x}{\pi x}$$

$$|\alpha_0| = \frac{A\tau}{T}$$

$$\alpha_0 = 0 \text{ (real number)}$$

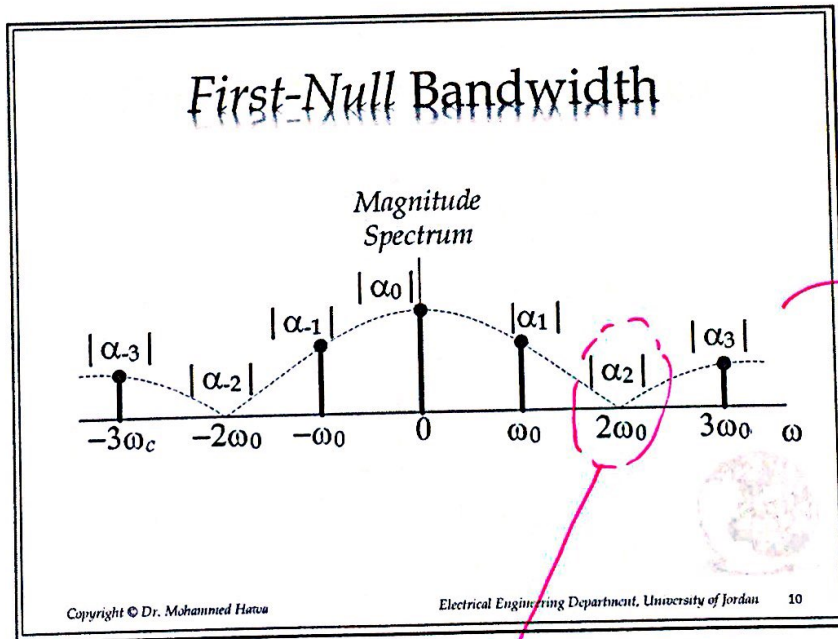
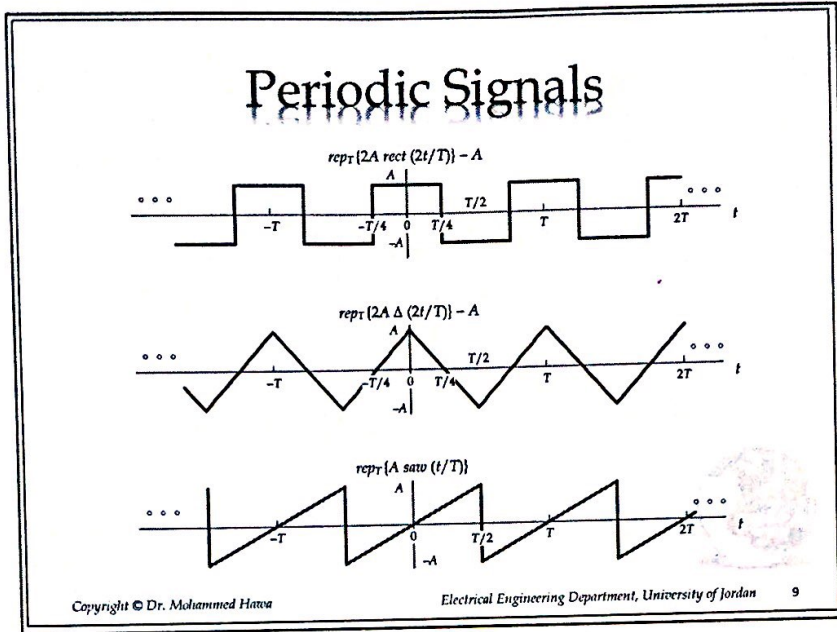
* How To find first null?

$$\alpha_n = \frac{A\tau}{T} \text{sinc}\left(\frac{n\omega_0\tau}{2\pi}\right)$$

@ $\frac{n\omega_0\tau}{2\pi} = 1 \Rightarrow$ first Null. (Bandwidth).

$$\text{Bandwidth} = n\omega_0 = \frac{2\pi}{T} \text{ rad/s.}$$

$$\Rightarrow \text{B}_{Hz} = \frac{1}{T}$$



Note:
 Always +ve.
 ↓ if there is a negative it will be shown in the phase spectrum.

Bandwidth of $m(t)$ since it is 1st Null.
 $\alpha_3 = -5$ → $|\alpha_3| = 5$
 ~~$\alpha_3 = 180^\circ$~~

- Fourier series: ONLY periodic

- Fourier Transform: periodic & aperiodic.

9/28/2016

Fourier Transform

$$X(\omega) = \mathcal{F}\{x(t)\} = \int_{-\infty}^{\infty} x(t)e^{-j\omega t} dt$$

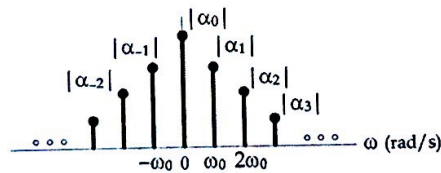
$$x(t) = \mathcal{F}^{-1}\{X(\omega)\} = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega)e^{j\omega t} d\omega$$

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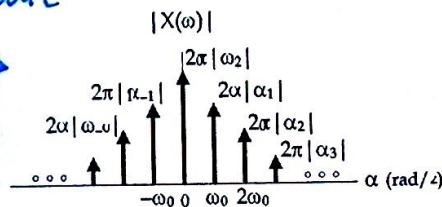
Fourier Series vs. Transform

series.



Same periodic signal.

Transform.



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$$\mathcal{F}\{\cos(\omega_0 t)\} = \pi \delta(\omega - \omega_0) + \pi \delta(\omega + \omega_0)$$

come from $2\pi * \frac{1}{2}$
 \downarrow
 fourier series coefficient of cosine
 $\alpha_1 = \alpha_{-1} = \frac{1}{2}$

$$\mathcal{F}\{\sin(\omega_0 t)\} = -j\pi \delta(\omega - \omega_0) + j\pi \delta(\omega + \omega_0)$$

$$\mathcal{F}\{\text{rect}(t)\} = \text{sinc}\left(\frac{\omega}{2\pi}\right) \rightarrow \mathcal{F}\left\{A \text{rect}\left(\frac{t}{T}\right)\right\} = AT \text{sinc}\left(\frac{\omega T}{2\pi}\right)$$

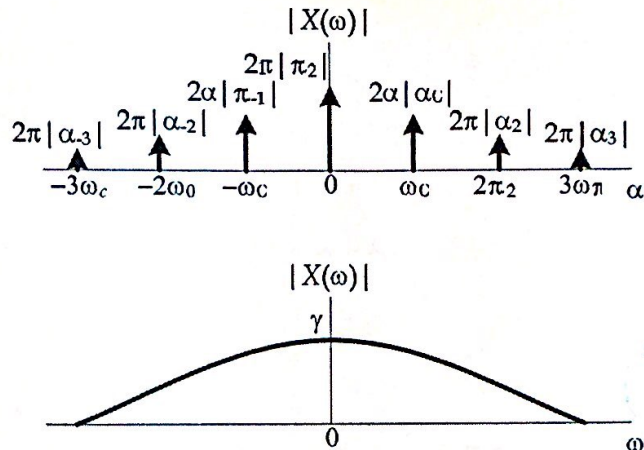
we can use it to find

α_n for $A \text{rect}\left(\frac{t}{T}\right)$:

$$\alpha_n = \frac{AT}{T} \text{sinc}\left(\frac{\omega T}{2\pi}\right) \xrightarrow{n\omega_0}$$

"Divide by T, replace ω by $n\omega_0$ "

Periodic vs. Aperiodic



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DC vs. Average Power

The DC value or average value of the signal $x(t)$ is:

TD: $DC = \overline{x(t)} = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} x(t) dt$

FD: $DC = \overline{x(t)} = \alpha_0 \rightarrow$ *Fourier Series Coefficient.*

The average power in the signal $x(t)$ is:

TD: $P_x = \overline{x^2(t)} = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} |x(t)|^2 dt$

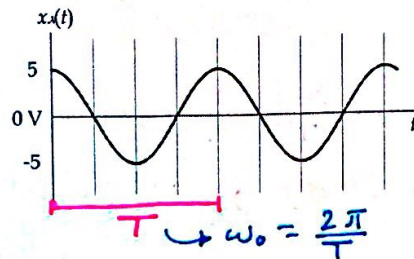
FD: $P_x = \overline{x^2(t)} = \frac{1}{2\pi} \int_{-\infty}^{\infty} S_x(\omega) d\omega$

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DC vs. Average Power



$DC = \text{avg} = \overline{x_1(t)} = 0$

$\hookrightarrow \text{Av. power} = \frac{5^2}{2} = 12.5 \text{ W.}$
 $\hookrightarrow \frac{A^2}{2}$



$\Rightarrow \text{peak} = 2.5$

$x_2(t) = 2.5 \cos(4t) + 7.5$

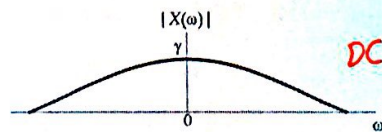
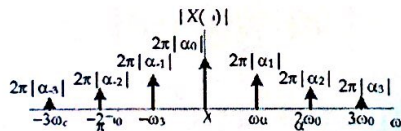
\Rightarrow Always write the Mathematical expression.

$\Rightarrow DC = 0 + 7.5 = 7.5$

$\text{Av. power: } P_{av.} = \frac{(2.5)^2}{2} + (7.5)^2 = 59.375 \text{ W.}$

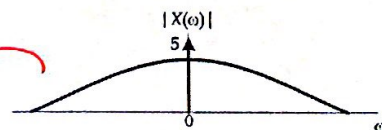
~~We Can't use~~ Super position for power.

DC from Frequency Domain



$DC \neq \gamma$

\hookrightarrow DC found from the impulse @ $\omega = 0$



$DC \neq 5$

So DC = 0

EXCEPT in this case: (orthogonality).

see Ex. \rightarrow

$DC = \alpha_0 \Rightarrow 2\pi|\alpha_0| = 5$

so $\alpha_0 = DC = \frac{5}{2\pi}$

Be careful.

Ex. of Orthogonality:

① $\cos(\omega t)$ & $\sin(\omega t)$. ("same freq.")

② AC & DC ("different freq") \rightarrow Like the previous example.

③ Cosines of multiple freq.
 $\cos(\omega t), \cos(2\omega t), \cos(3\omega t) \dots$

$x(t) = 2.5 \cos(\omega t) + 7.5$ "orthogonal"

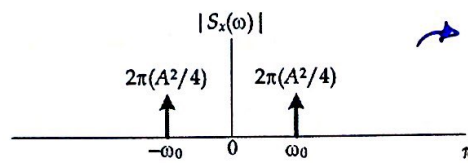
$x(t) = 5.5 + 4 \cos(2\omega t) + 5 \cos(2\omega t)$ "Not orthogonal"

$x(t) = 5.5 + 4 \cos(2\omega t) + 5 \sin(2\omega t)$ "orthogonal"

Power Spectral Density

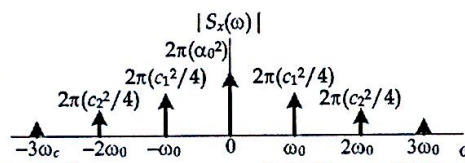
$$\text{PSD} = S_x(\omega) = \lim_{T \rightarrow \infty} \frac{1}{T} |X_T(\omega)|^2 = \mathcal{F}\{R_{xx}(\tau)\}$$

Auto correlation for $x(t)$.



$$P_{av} = \frac{1}{2\pi} \int_{-\infty}^{\infty} S_x(\omega) d\omega$$

$$= \frac{1}{2\pi} \times \text{Area.}$$



$$= \frac{1}{2\pi} (2\pi) \frac{A^2}{2}$$

$$\Rightarrow P_{av} = \frac{A^2}{2} \text{ W.}$$

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17

Quick Review of Filters

- There are three main filter types that you studied in signal analysis:
 - LPF: Low-Pass Filter
 - BPF: Band-Pass Filter
 - HPF: High-Pass Filter
 - BSF: Band-Stop Filter.

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Ex1: Find $R_{xx}(\tau)$ and then $S_x(\omega)$ for $x(t) = A \cos(\omega_0 t)$
Then Find Pav. ? see figure(1) slide(17).

Ex2: Find $R_{xx}(\tau)$, $S_x(\omega)$, $\overline{x^2(t)}$ for $x(t) = \text{rept} \left\{ A \text{rect} \left(\frac{t}{T} \right) \right\}$?
see figure(2) slide(17).

Low-Pass Filter (LPF)

• Symbol:

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Frequency-response function

$$H(\omega) = \frac{V_o(\omega)}{V_i(\omega)}$$

$|V_o(\omega)| = |H(\omega)| \times |V_i(\omega)|$

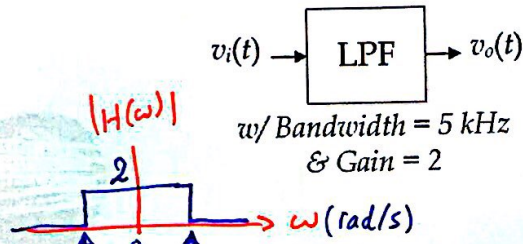
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impulses @ the edges will pass.

Bandwidth of the filter.

Characteristics

- **Always** centered at 0 rad/s.
- Bandwidth = Cut-off frequency = ω_1 rad/s
- Gain = k.



Always draw the filter at first & show its char.

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$2\pi(5\text{kHz})$
 $2\pi(-5\text{kHz})$

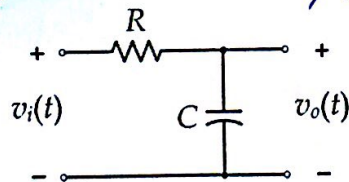
$\text{width} = 2 * \text{Bandwidth}$.

** In Bandwidth Calculations Consider only positive freq.*

** For Power Calculations Consider Both +ve & -ve freq.*

Memorize:

Example Circuit



1st order LPF. passive filter.

$f \downarrow \Rightarrow C \text{ open } v_o = v_i$

$f \uparrow \Rightarrow C \text{ short } v_o = 0$

$$B_{LPF} = \frac{1}{2\pi RC} \text{ Hz}$$

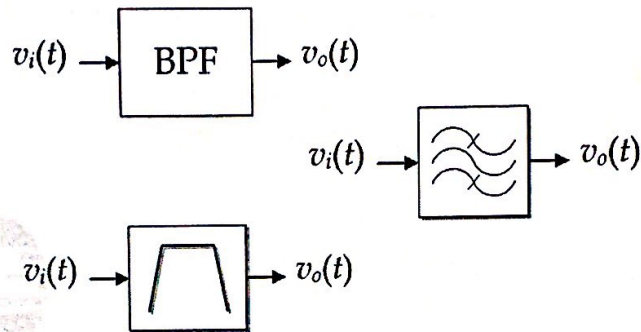
$$\text{Gain} = 1$$

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Band-Pass Filter (BPF)

- Symbol:

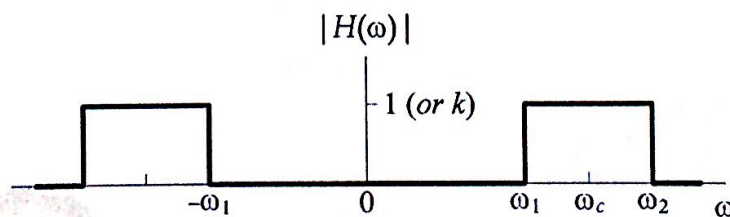


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Frequency-response function

$$H(\omega) = \frac{V_o(\omega)}{V_i(\omega)}$$



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Characteristics

- Centered around center frequency ω_c rad/s.
- Bandwidth of Filter = $\omega_2 - \omega_1$ rad/s
- Gain = k.



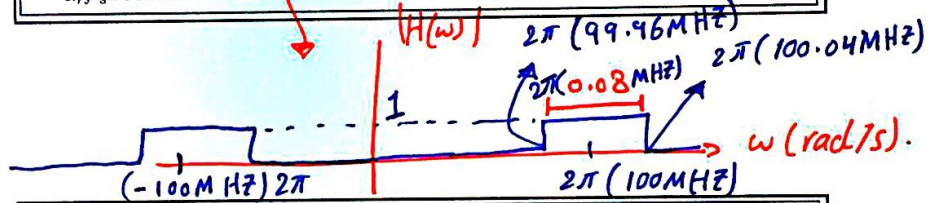
w/ Bandwidth = 80 kHz
Center Frequency = 100 MHz
& Gain = 1

Be careful for the units.



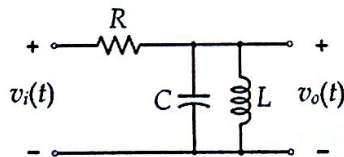
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Example Circuit

2nd order BPF.



$$f_c = f_{res} = \frac{1}{2\pi\sqrt{LC}} \text{ Hz}$$

$$B_{BPF} = \Delta f = \frac{R}{2\pi L} \text{ Hz}$$

$$\text{Gain} = 1$$

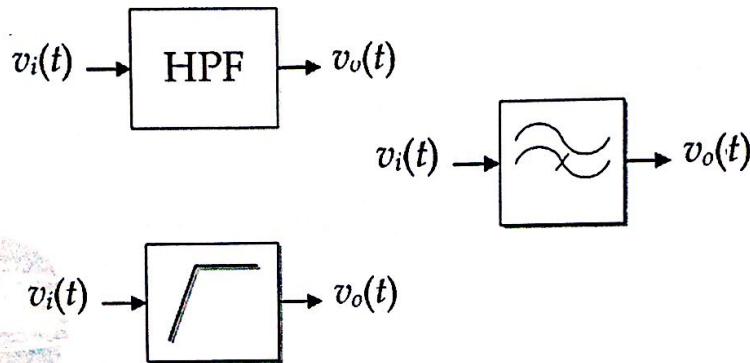


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High-Pass Filter (HPF)

- Symbol:

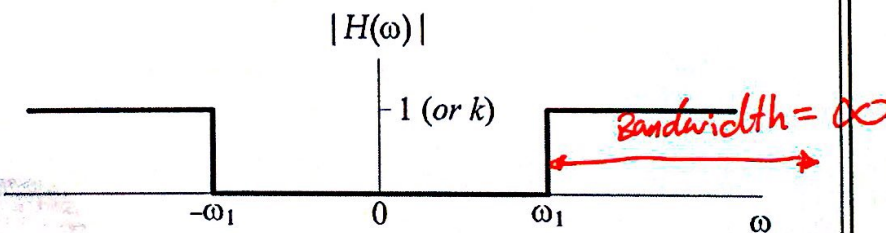


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Frequency-response function

$$H(\omega) = \frac{V_o(\omega)}{V_i(\omega)}$$



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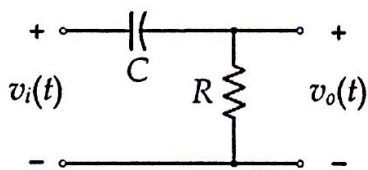
Characteristics

- Cut-off frequency = ω_1 rad/s.
- Gain = k.
- No *bandwidth* defined.

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Example Circuit


 $f \uparrow \Rightarrow C \text{ open}$
 $V_o = 0$

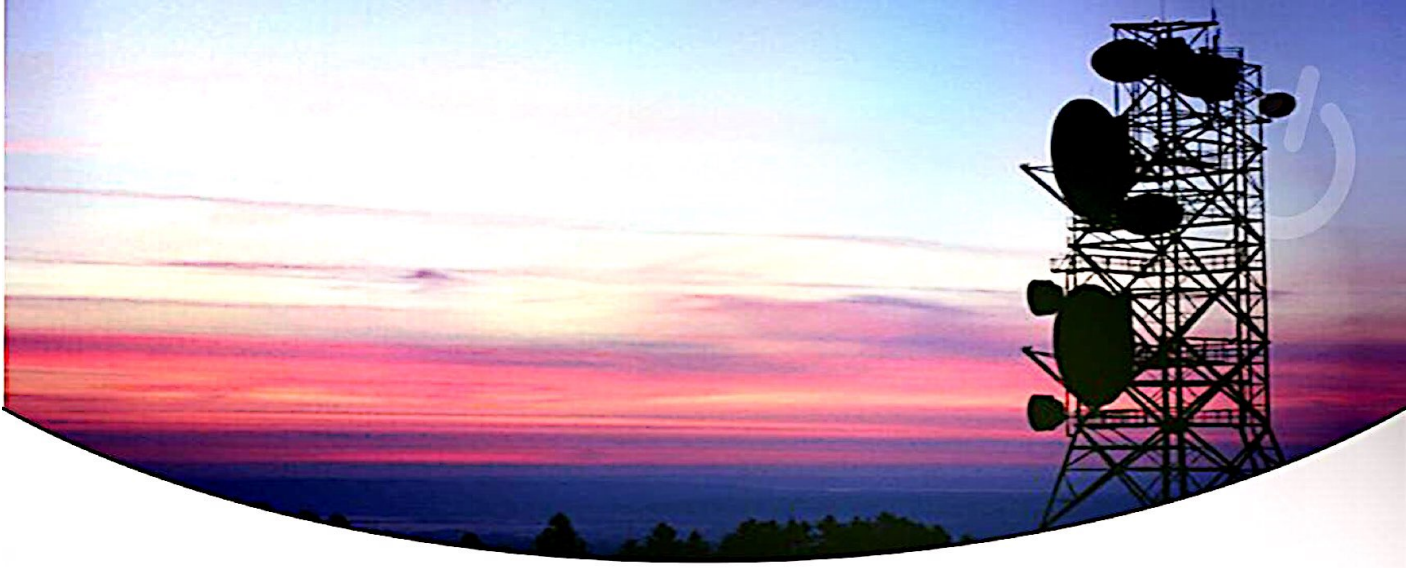
$$f_{\text{cut-off}} = \frac{1}{2\pi RC} \text{ Hz}$$

 $f \downarrow \Rightarrow C \text{ short}$
 $V_o = V_i$

$$\text{Gain} = 1$$

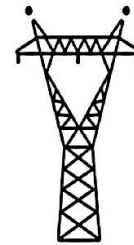
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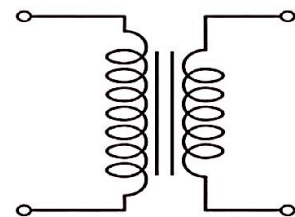
Communications I

Fall 2017



Dr. **M**hmd **H**awa 

 By: **M**hmd **A**buhashya



Powerunit-ju.com

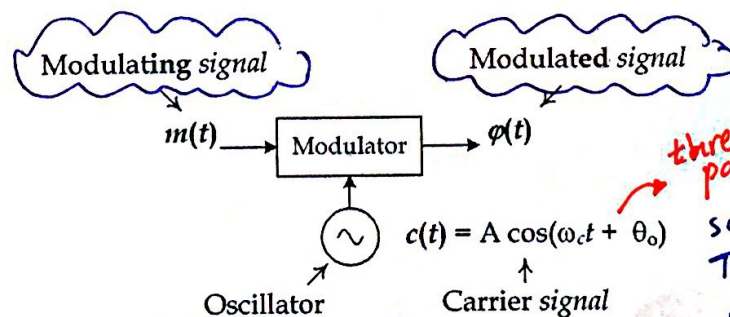
Lecture 4: Amplitude Modulation (Double Sideband Suppressed Carrier, DSB-SC)

Dr. Mohammed Hawa
Electrical Engineering Department
University of Jordan

EE421: Communications I

→ Memorize it.

Notation



→ three basic parameters so three types of modulations.

* If $c(t)$ is cosine, it is called:
CW (continuous wave) modulation.

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* **Modulation**: is a process that causes a shift of frequencies of the signal from Baseband to Carrier.

* **Modulation is achieved by**: changing one of the basic parameters of a high frequency periodic signal (called the carrier $c(t)$) in proportion to the baseband message signal $m(t)$.

Three Modulation Types

- $A \propto m(t)$; $\omega_c = \text{constant}$; $\theta_o = \text{constant}$
 - Amplitude Modulation (AM) \rightarrow in Analog Modulation.
 - Amplitude Shift Keying (ASK) \rightarrow in Digital Modulation.
- $A = \text{constant}$; $\omega_c \propto m(t)$; $\theta_o = \text{constant}$
 - Frequency Modulation (FM)
 - Frequency Shift Keying (FSK)
- $A = \text{constant}$; $\omega_c = \text{constant}$; $\theta_o \propto m(t)$
 - Phase Modulation (PM)
 - Phase Shift Keying (PSK)

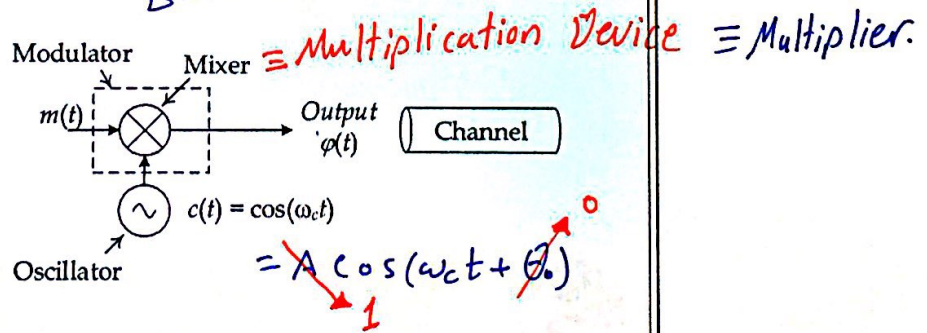
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* When we say just (AM): we mean DSB-FC. Double sideband larger carrier.

DSB-SC Modulator; Mixer Balanced Modulator.



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$$o/p = \phi(t) = m(t) \cdot c(t)$$

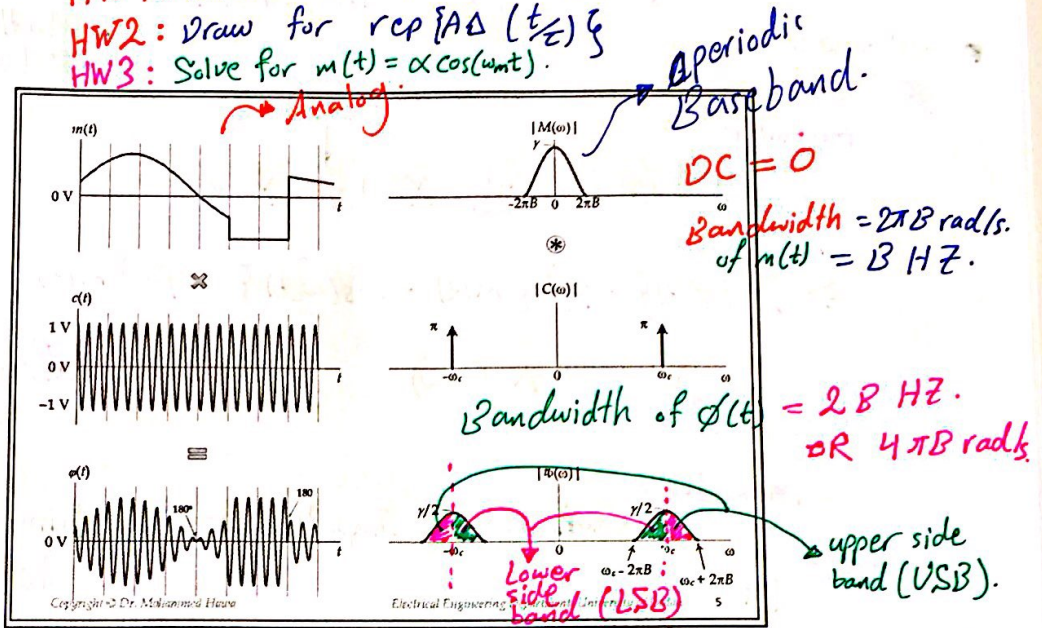
DSB-SC

$$\Rightarrow \phi(t) = m(t) \cos(\omega_c t)$$

$A \propto m(t)$ Const. Const.

2

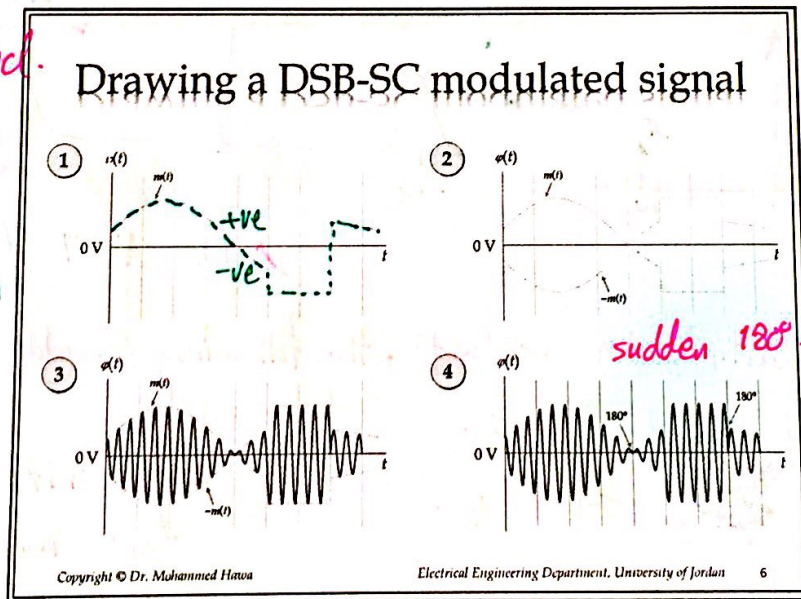
- HW1: Draw for rep $\{ \text{rect}(\frac{t}{T}) \}$
- HW2: Draw for rep $\{ A \Delta(\frac{t}{T}) \}$
- HW3: Solve for $m(t) = \alpha \cos(\omega_m t)$.



* $B_{DSB-SC} = 2B$ (this is a disadvantage because it will be more expensive.)

* Because LSB & USB we call it Double Side Band (DSB).

* It is called Suppressed Carriers because No impulses in freq. domain were shown (but actually they are existed.)



sudden 180° phase shift in $\phi(t)$.

* Bandwidth found in f-domain.

* Sudden phase-shift found in t-domain.

This happens when $m(t)$ changes from +ve \rightarrow -ve or otherwise around. -ve \rightarrow +ve.

* Sketch $\phi(t)$ in t-domain.

* $\Rightarrow \Phi(\omega) = \mathcal{F}\{\phi(t)\}$ in f-domain.

• F-Domain:

* Graphically:

remember:

$$\mathcal{F}\{x(t)y(t)\} = \frac{1}{2\pi} X(\omega) \star Y(\omega)$$

$$\Rightarrow \mathcal{F}\{\phi(t)\} = \mathcal{F}\{m(t) \cdot \cos(\omega_c t)\} = \mathcal{F}\{m(t) \cdot c(t)\}$$

$$= \frac{1}{2\pi} M(\omega) \star C(\omega)$$

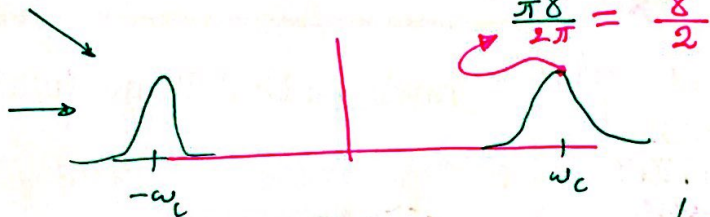
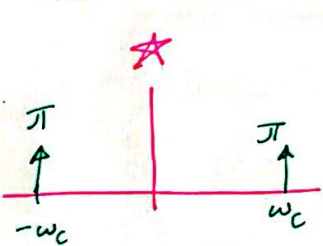
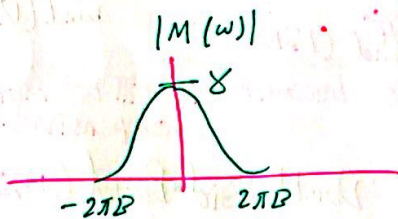
$$** \mathcal{F}\{c(t)\} = \mathcal{F}\{\cos(\omega_c t)\} = \pi \delta(\omega - \omega_c) + \pi \delta(\omega + \omega_c)$$

remember:

something \star Impulse = Something

with shift (by shift of impulse)

& scale (by area of impulse).



DO NOT forget $\left(\frac{1}{2\pi}\right)$.

* if you multiply by $\cos(\omega_c t)$, the following should be done:

- 1- Shift Right by ω_c .
- 2- shift left by ω_c .

3- Multiply by $\frac{1}{2}$.

4- $B_{DSB-SC} = 2B$

5- $\overline{\phi_{DSB-SC}^2(t)} = \frac{1}{2} \overline{m^2(t)}$

$\hookrightarrow P_{av}$ in $\phi(t)$

$\hookrightarrow P_{av}$ in $m(t)$

• Memorize this fast method.

\Rightarrow Continue

Example: Assume $m(t) = \alpha \cos(\omega_m t)$ Find $m^2(t)$?

for DSB-SC.

$$\hookrightarrow = \boxed{\frac{\alpha^2}{2}}$$

$$\phi(t) = m(t) \cdot c(t) \\ = \alpha \cos(\omega_m t) \cos(\omega_c t)$$

$$\Rightarrow \overline{\phi^2(t)} = \boxed{\frac{\alpha^2}{4}}$$

So $\overline{\phi^2(t)} = \frac{1}{2} \overline{m^2(t)}$

Mathematically:

$$\Phi(\omega) = \mathcal{F}\{\phi(t)\} = \mathcal{F}\{m(t) \cos(\omega_c t)\}$$

$$= \mathcal{F}\left\{ \frac{1}{2} m(t) e^{j\omega_c t} + \frac{1}{2} m(t) e^{-j\omega_c t} \right\}$$

$$= \frac{1}{2} \mathcal{F}\{m(t) e^{j\omega_c t}\} + \frac{1}{2} \mathcal{F}\{m(t) e^{-j\omega_c t}\}$$

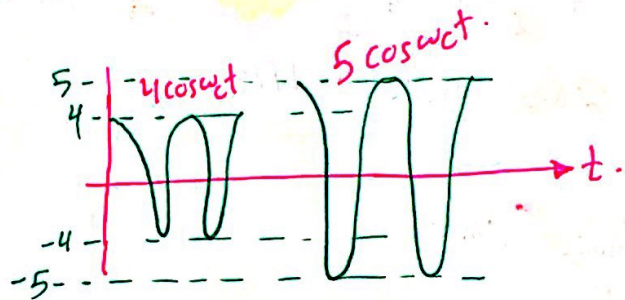
"frequency" shift property

$$\Phi(\omega) = \frac{1}{2} M(\omega - \omega_c) + \frac{1}{2} M(\omega + \omega_c)$$

\downarrow shift right. \downarrow shift left.

• T-Domain:

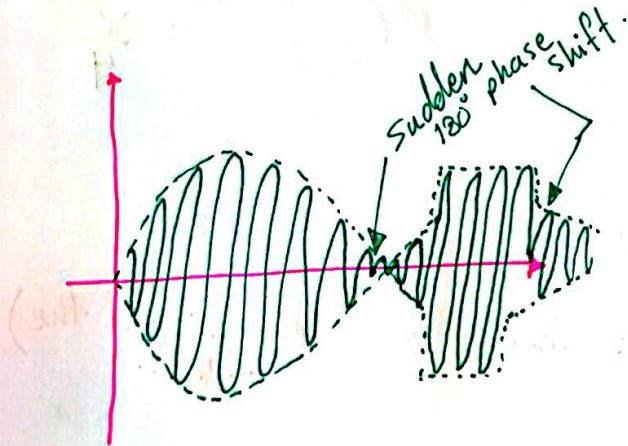
Draw $4\cos\omega_c t$ & $5\cos\omega_c t$



* Now for $m(t) \cos\omega_c t = \phi(t)$.

we draw a dashed lines for $m(t)$ & $-m(t)$
Then we draw the cosine inside it.

for $5\cos\omega_c t$
 $-5\cos\omega_c t = 5\cos(\omega_c t - 180^\circ)$
 $\hookrightarrow 180^\circ$ -phase shift.



Sketch $x(t)$ & $y(t)$ in t -domain.
& $X(\omega)$ & $Y(\omega)$ in f -domain.

DSB-SC Demodulator: Mixer again!

$$\phi(t) = m(t) \cos(\omega_c t)$$

$$x(t) = \phi(t) \cdot c(t)$$

$$X(\omega) = \mathcal{F}\{\phi(t) \cdot c(t)\}$$

$$= \mathcal{F}\{m(t) \cos^2(\omega_c t)\}$$

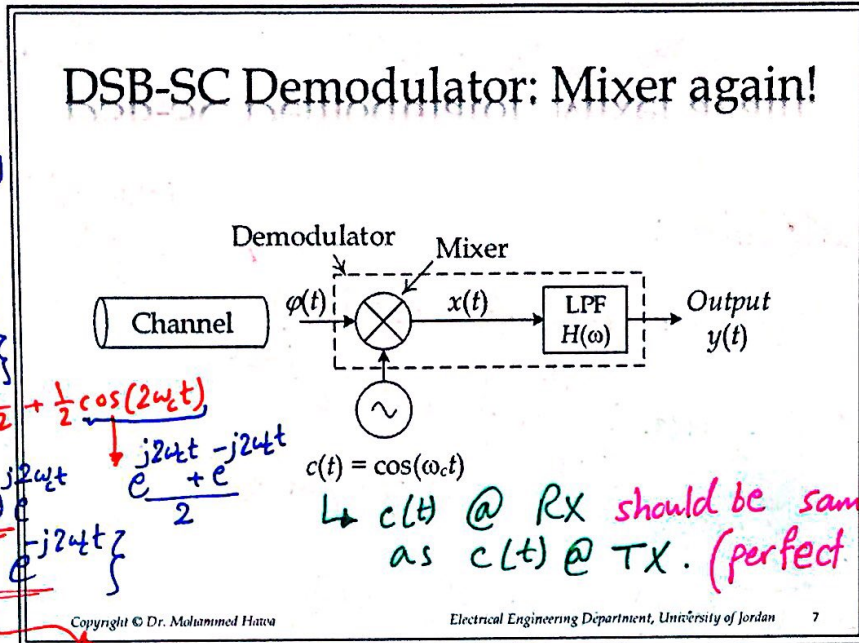
$$= \mathcal{F}\left\{ \frac{1}{2} m(t) + \frac{1}{4} m(t) e^{j2\omega_c t} + \frac{1}{4} m(t) e^{-j2\omega_c t} \right\}$$

$$= \frac{1}{2} M(\omega) + \frac{1}{4} M(\omega - 2\omega_c) + \frac{1}{4} M(\omega + 2\omega_c)$$

① ② ③

② & ③ rejected by LPF.

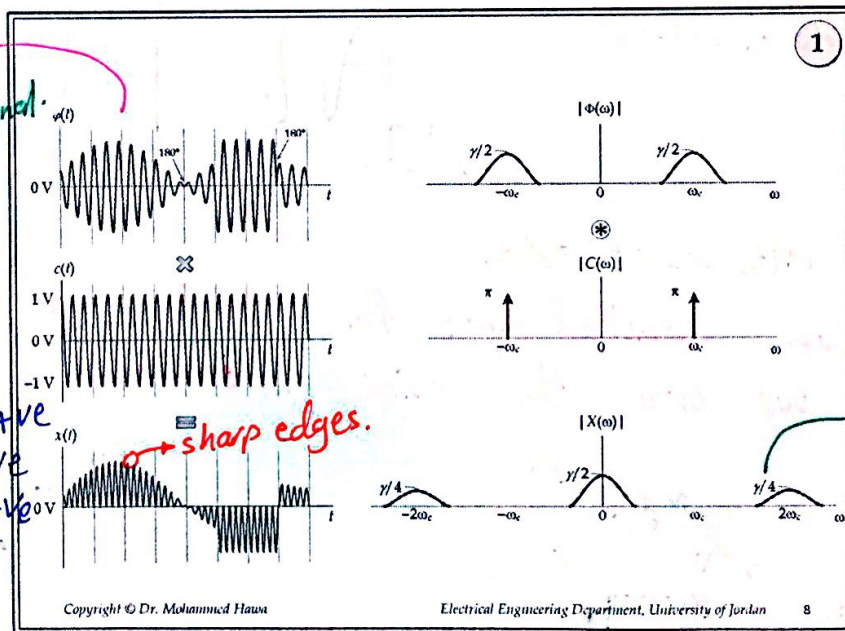
$$\Rightarrow Y(\omega) = \frac{1}{2} M(\omega) \rightarrow \text{Gain}_{\text{LPF}} = 1$$



$c(t)$ @ RX should be same freq. & phase. as $c(t)$ @ TX. (perfect Synchronization)

- Modulated signal.
- AM.
- DSB-SC.

+ve x +ve = +ve
-ve x -ve = +ve
-ve x +ve = -ve

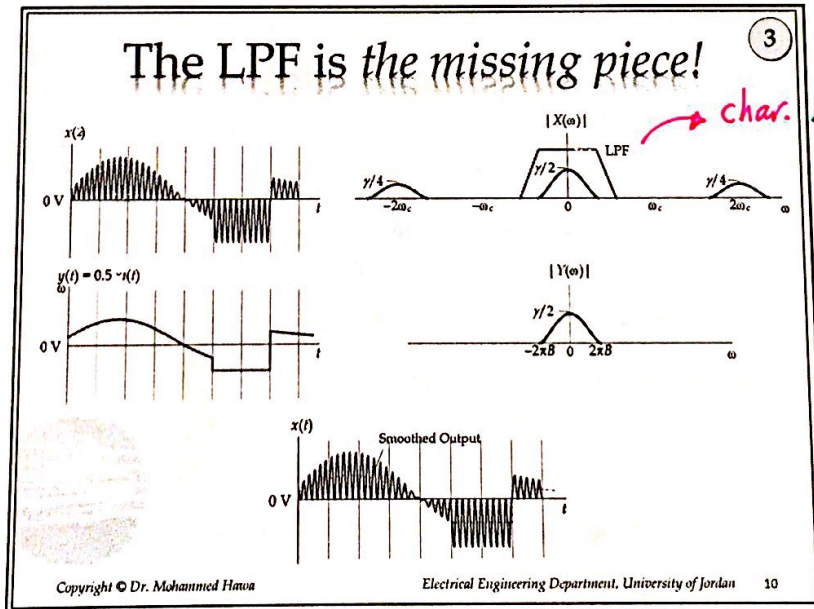
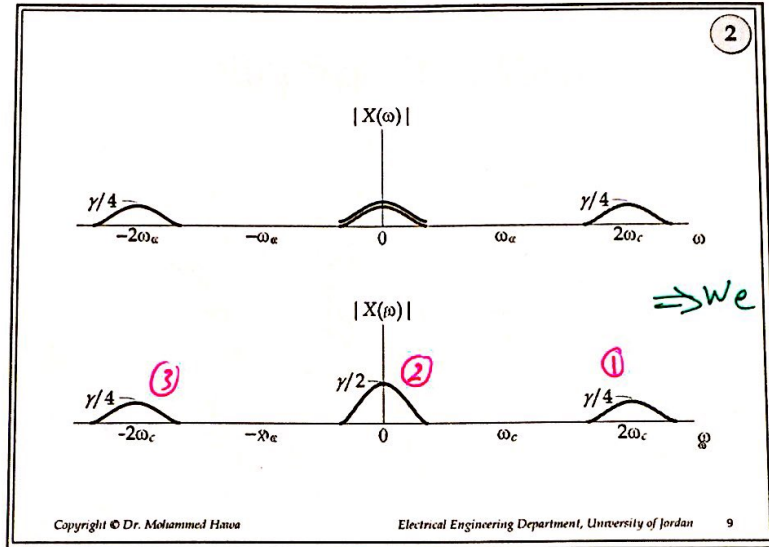


$$\mathcal{F}\{\phi(t) \cdot c(t)\} = \frac{\Phi(\omega) * C(\omega)}{2\pi}$$

Note:

Sharp edges \equiv High Freq.

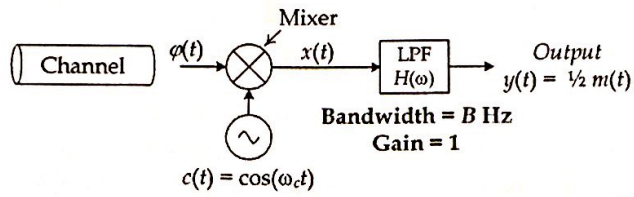
\Rightarrow LPF removes sharp edges. (smooths out the signal.)



for gain = 1 ⇒ $y(t) = \frac{1}{2} m(t)$.
 for gain = 5 ⇒ $y(t) = \frac{5}{2} m(t)$.

"Be careful"

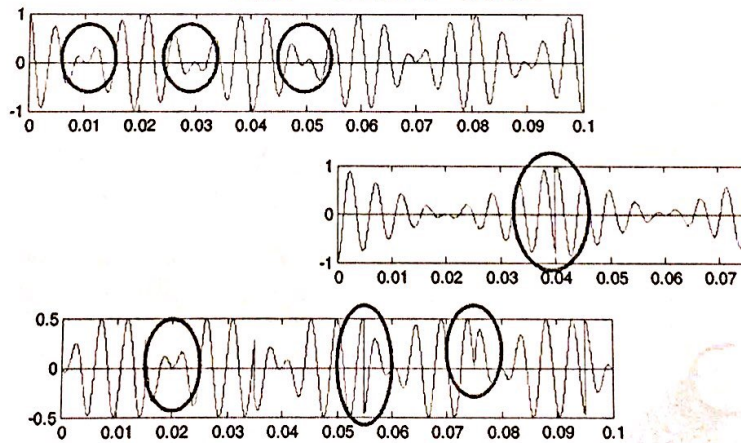
Filter Specifications!



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180° Phase Shift



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* always Tone Modulation means that $m(t) = \alpha \cos(\omega_m t)$.
 (Memorize it).

2/15/2017

Example

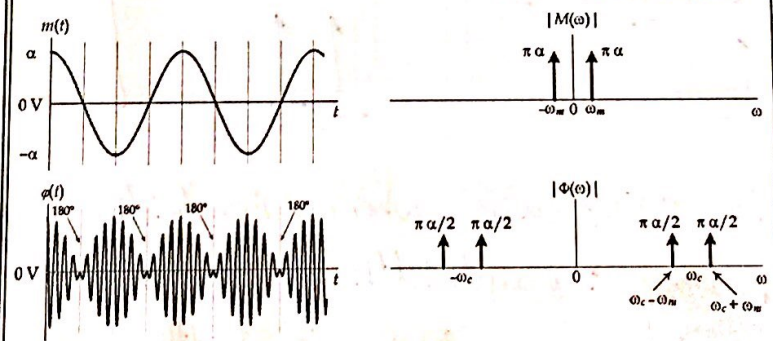
- Assume we perform DSB-SC modulation for the baseband signal $m(t) = \alpha \cos(\omega_m t)$ [the case of tone modulation], where $\omega_c \gg \omega_m$:
 - Sketch the time-domain modulated signal $\phi(t)$.
 - Sketch the Fourier transform of the modulated signal $\Phi(\omega)$ [frequency domain].
 - Find the bandwidth of $m(t)$ and $\phi(t)$. *→ found from Freq. domain.*
 - Find the average power in both $m(t)$ and $\phi(t)$. *→ found from Time domain.*
 - Show the demodulator hardware.
 - Sketch $x(t)$ and $y(t)$ in the demodulator.

see slide (11)

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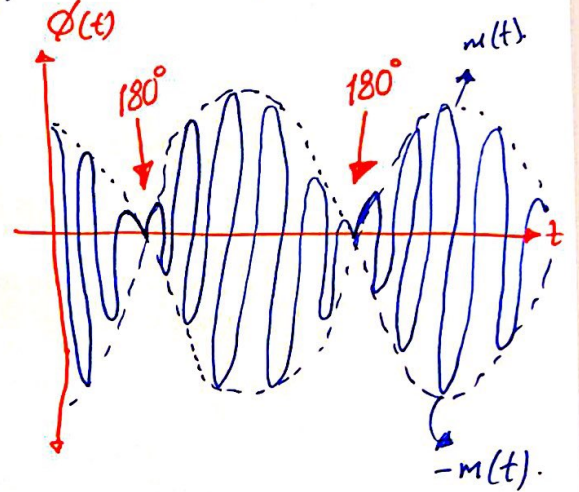
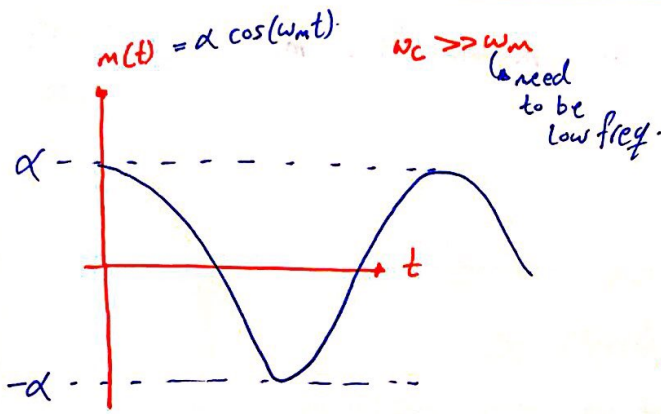
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Solution



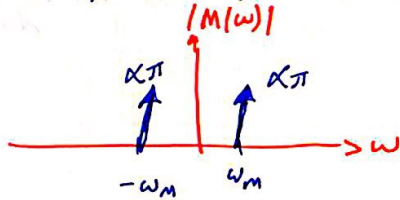
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$$\Phi(\omega) = \frac{1}{2} M(\omega - \omega_c) + \frac{1}{2} M(\omega + \omega_c)$$

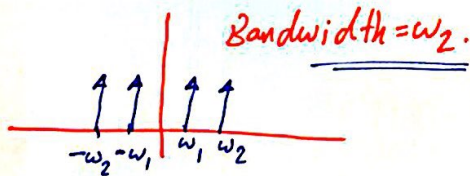
$$M(\omega) = \mathcal{F}\{m(t)\} = \mathcal{F}\{\alpha \cos \omega_m t\} = \alpha \pi [\delta(\omega - \omega_m) + \delta(\omega + \omega_m)]$$



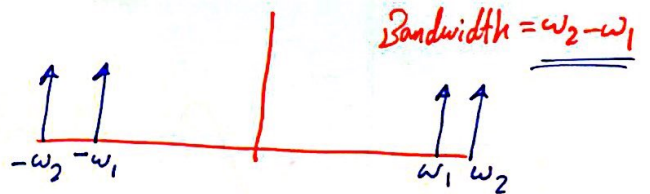
Bandwidth of $m(t) = \omega_m \text{ rad/s.}$
 $= \frac{\omega_m}{2\pi} = f_m \text{ Hz.}$

* Note:

if $M(\omega)$ Baseband:

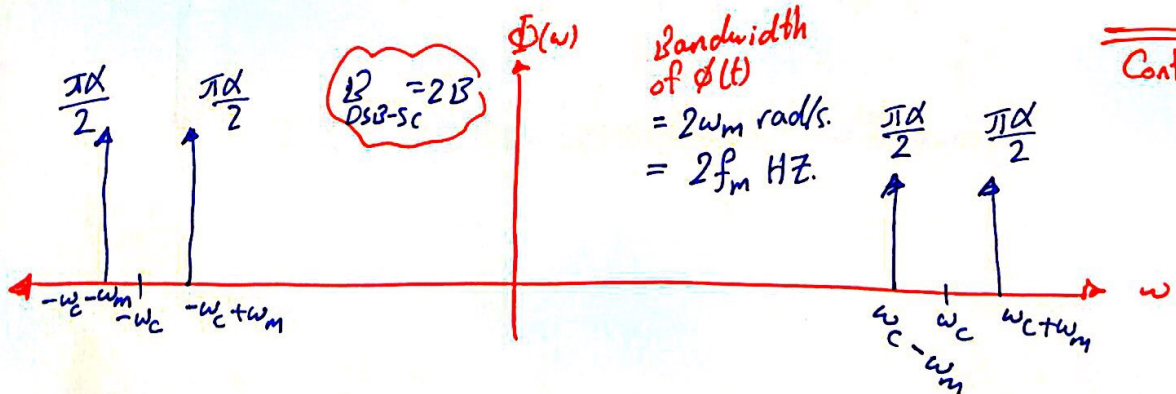


if $\Phi(\omega)$ modulated Carrier:



* Tone Mod.: is ONLY case where Bandwidth = fundamental.

all other cases: Bandwidth \neq fundamental.



Continue

for the average power:

found from time-domain.

$$\overline{m^2(t)} = \frac{1}{T} \int_T m^2(t) dt.$$

$$m(t) = \alpha \cos(\omega_m t)$$

$$\Rightarrow \boxed{\overline{m^2(t)} = \frac{\alpha^2}{2}}$$

Now for $\phi(t)$:

$$\overline{\phi^2(t)} = \frac{1}{T} \int_T \phi^2(t) dt.$$

OR

$$\overline{\phi^2(t)} = \frac{1}{2} \overline{m^2(t)}$$

$$\Rightarrow \boxed{\overline{\phi^2(t)} = \frac{\alpha^2}{4}}$$

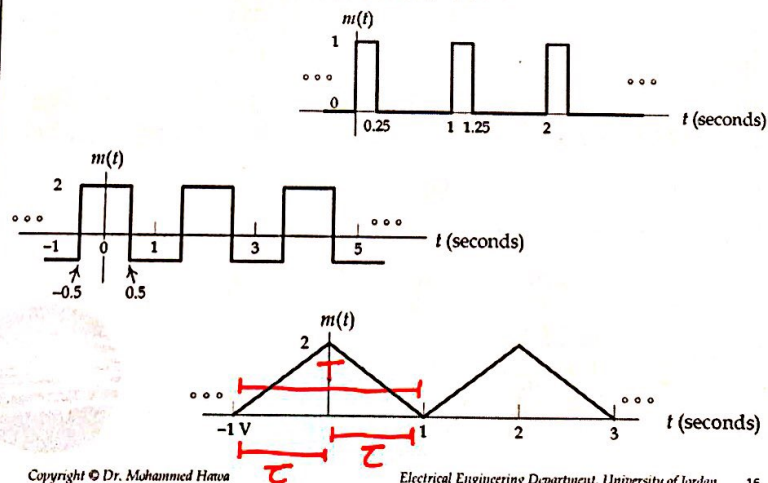
Homework

- For the following signals $m(t)$, sketch:
 - The modulated signal $\varphi(t)$ at the modulator
 - The Fourier transform $\Phi(\omega)$
 - The signals $x(t)$ and $y(t)$ at the demodulator
 - The Fourier transform $X(\omega)$ and $Y(\omega)$
- Find the average power and bandwidth for the signals $\varphi(t)$ and $y(t)$.
- Are there any phase shifts in $\varphi(t)$? If so, where?
- Determine the DC value in $m(t)$, $\varphi(t)$ and $y(t)$.

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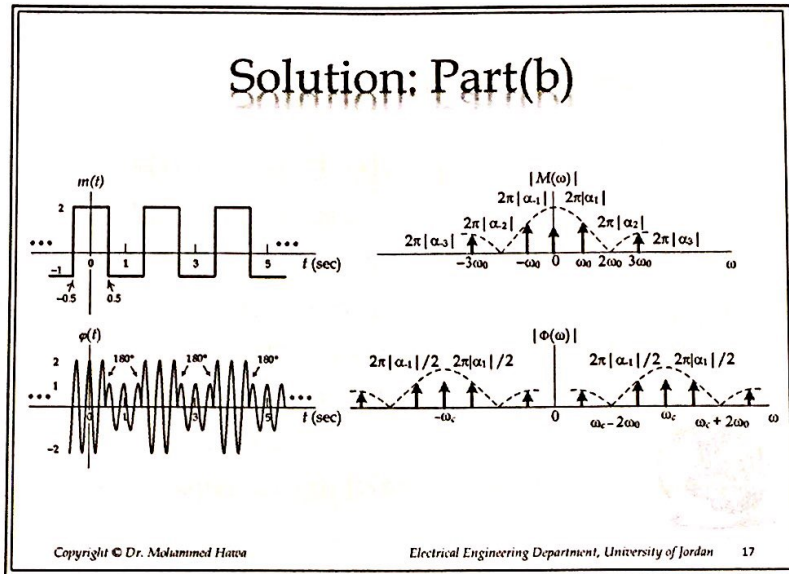
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Homework



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very important.

Homework

- For the following circuit, sketch $x(t)$ and $y(t)$, along with the Fourier transform $X(\omega)$ and $Y(\omega)$.

$c(t) = \cos(\omega_c t)$ $c(t) = \sin(\omega_c t) = \cos(\omega_c t - 90^\circ)$

Bandwidth = B Hz
 Gain = 1

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How to build a Mixer?

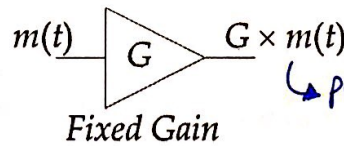
- Variable Gain Amplifier
 - The basic design.
- Gilbert Cell (e.g., MC 1496)
 - Popular (used in Integrated Circuits).
 - Uses variable gain differential amplifiers.
- Switching Modulator
 - Uses diodes.
 - Cheaper design (was popular before ICs).

is built using 8 transistors configured as 3 differential amplifiers.

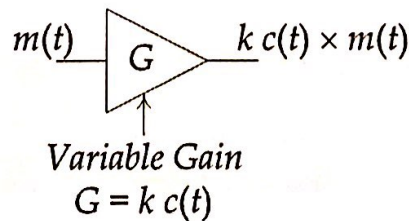
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Variable Gain Amplifier

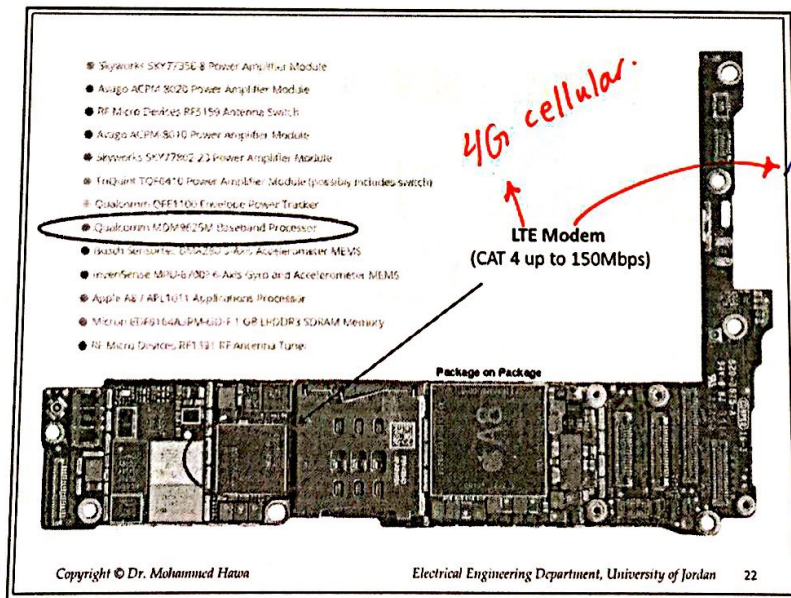
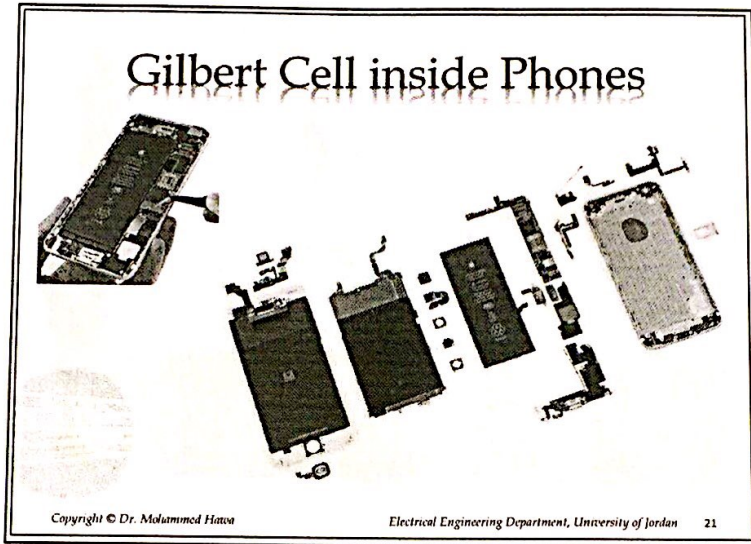


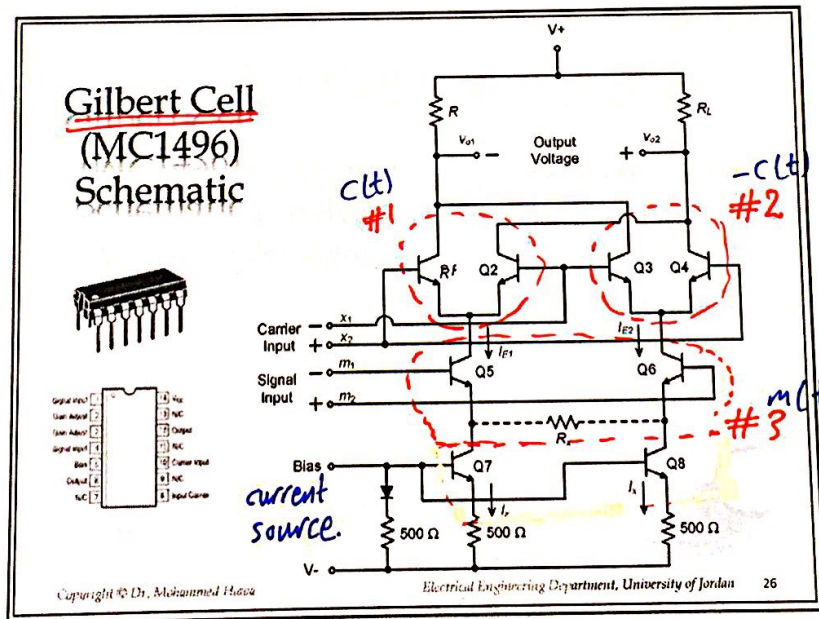
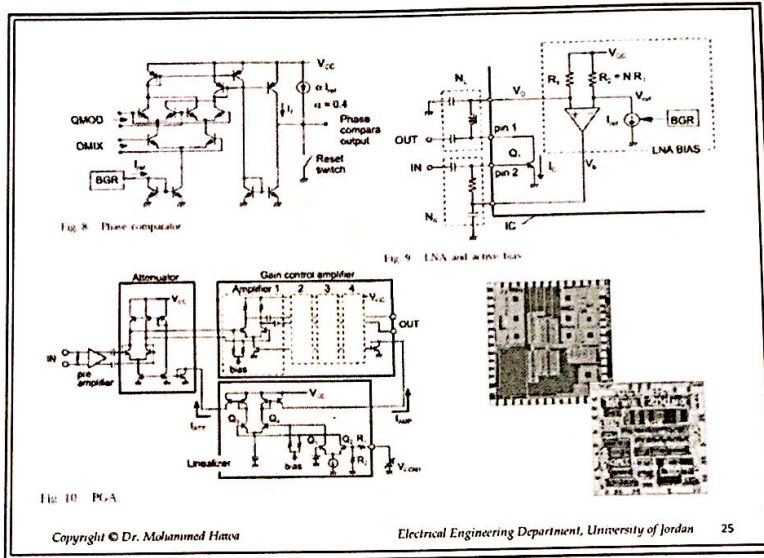
power = power_{in} * G^2



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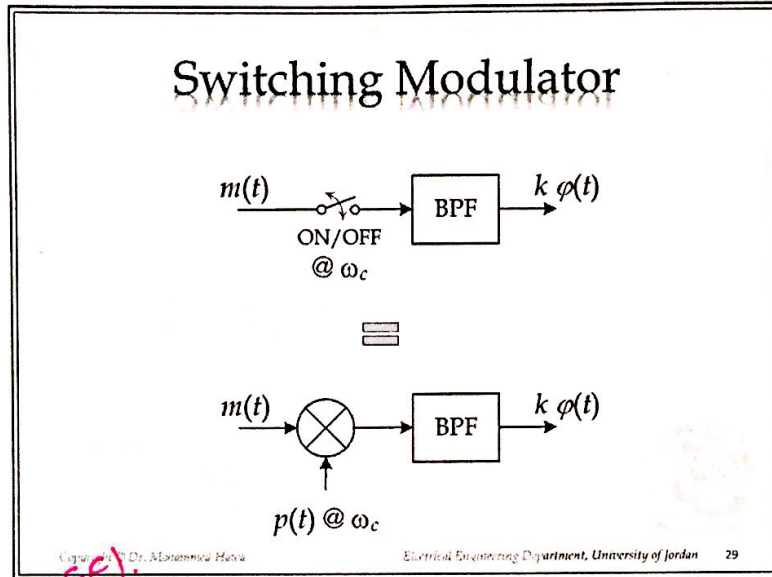
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switching \equiv Multiplying by $p(t) = \text{rep}\{\text{rect}(t)\}$

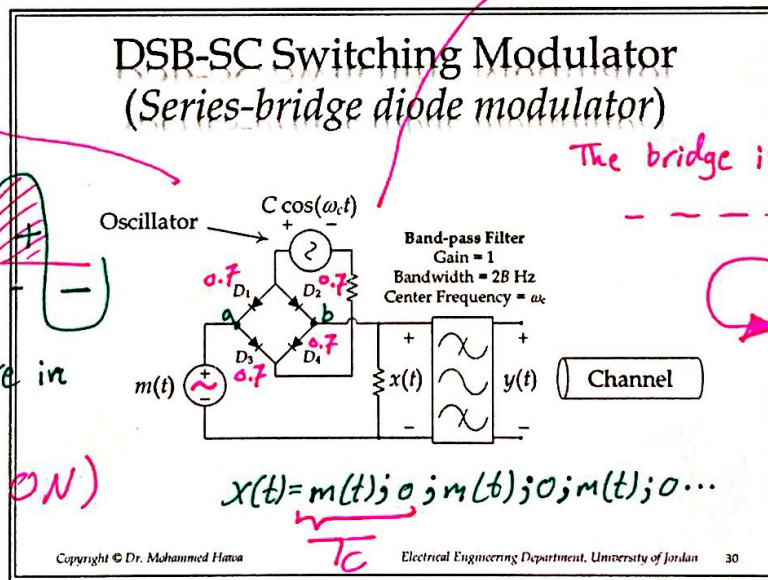
2/15/2017



in (-ve) cycle:
all diodes reverse biased (All diodes are OFF).
 $x(t) = 0$

Diodes = switch.

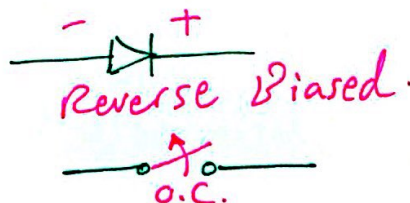
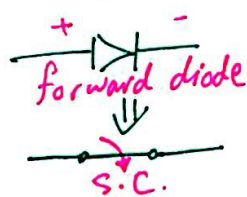
in (+ve) cycle.
The diodes will work as a S/C between a & b:
 $-0.7 + 0.7 + 0.7 - 0.7 + V_{ab} = 0$
 $V_{ab} = 0$

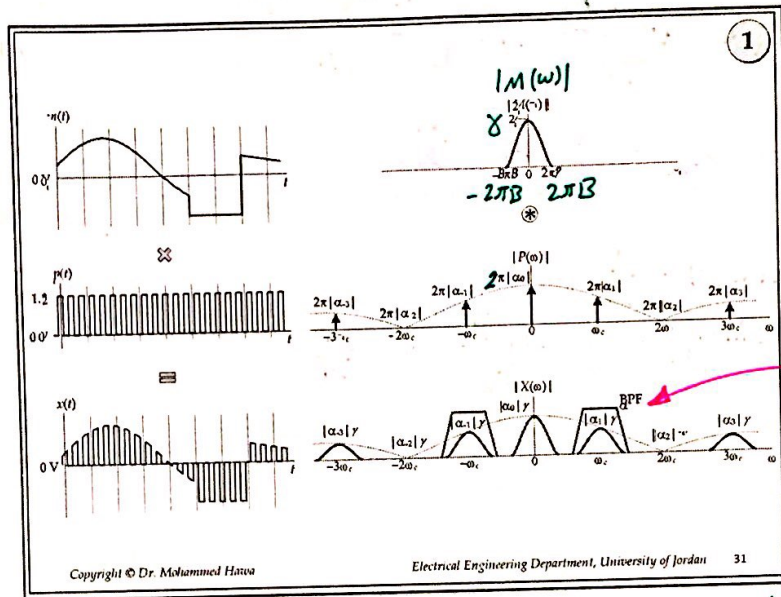


All the diodes are in forward biased (All diodes are ON)
 $x(t) = m(t)$.

The bridge is used as a switch.
 $C \gg m(t)$
 $C \gg 1$
 $C \gg 1.4$
To control the diode & also have a voltage higher than 0.7 volt.

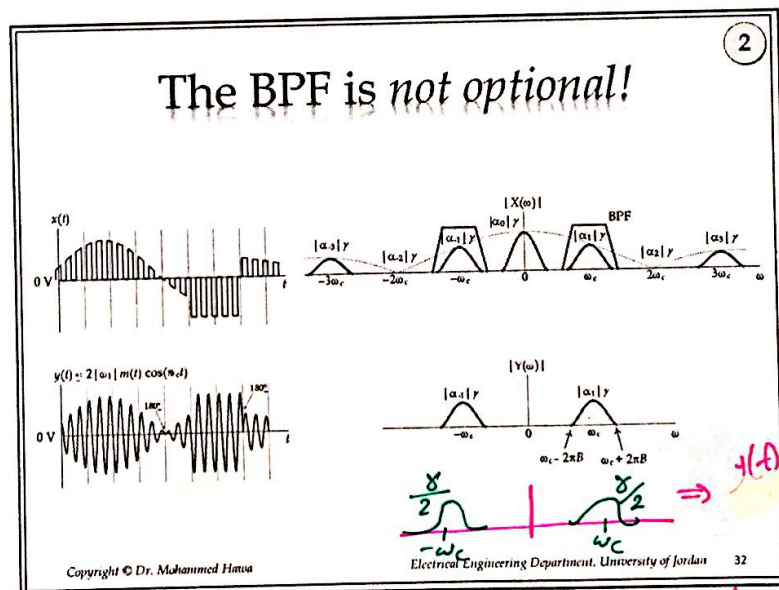
states of diode:





$$\frac{\gamma \cdot 2\pi|\alpha_1|}{2\pi} = \gamma|\alpha_1|$$

BPF → center = $\omega_c \text{ rad/s} \approx \frac{1}{T_c} \text{ Hz}$
 → Bandwidth = $2B \text{ Hz} = 4\pi B \text{ rad/s}$
 → Gain



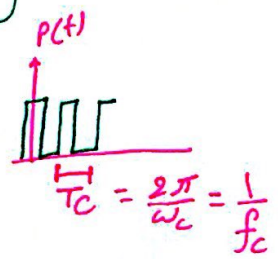
Gain = 1	$ \alpha_1 $	$\frac{1}{2 \alpha_1 }$
$y(t) = 2 \alpha_1 m(t)\cos(\omega_c t)$	$y(t) = 2 \alpha_1 ^2 m(t)\cos(\omega_c t)$	$y(t) = m(t)\cos(\omega_c t)$

$$\mathcal{F}\{m(t) \cdot p(t)\} = \frac{1}{2\pi} M(\omega) \star P(\omega)$$

$$\alpha_n = \frac{AT}{T} \operatorname{sinc}\left(\frac{n\omega_c T}{2\pi}\right) \Rightarrow \text{from } p(t) \Rightarrow A=1$$

$$\Rightarrow \alpha_n = \frac{1.0\left(\frac{T_c}{2}\right)}{T_c} \operatorname{sinc}\left(\frac{n\left(\frac{2\pi}{T_c}\right)\left(\frac{T_c}{2}\right)}{2\pi}\right)$$

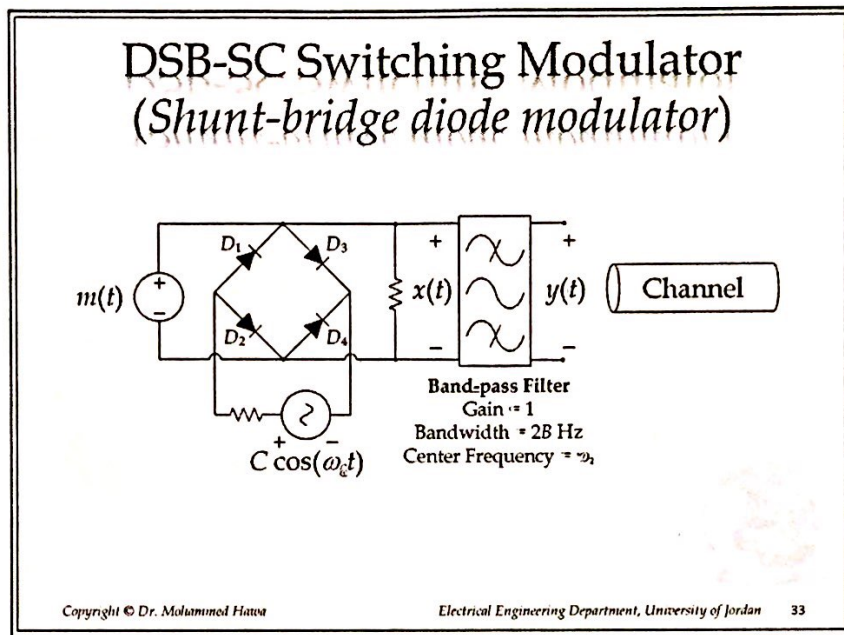
$$\Rightarrow \underline{\underline{\alpha_n = \frac{1}{2} \operatorname{sinc}\left(\frac{n}{2}\right)}}$$



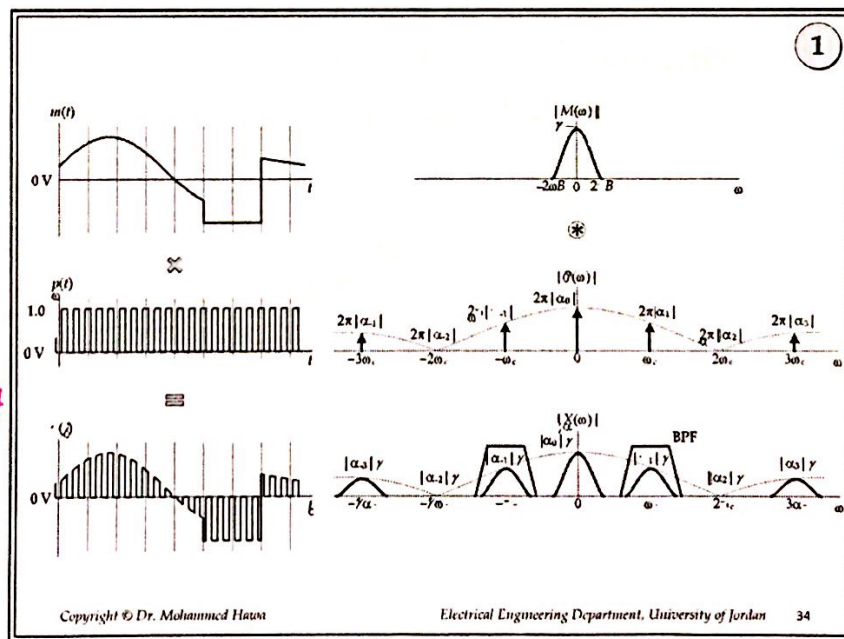
see the figures
slide (31).

$$\alpha_0 = \frac{1}{2} \operatorname{sinc}(0) = \frac{1}{2}$$

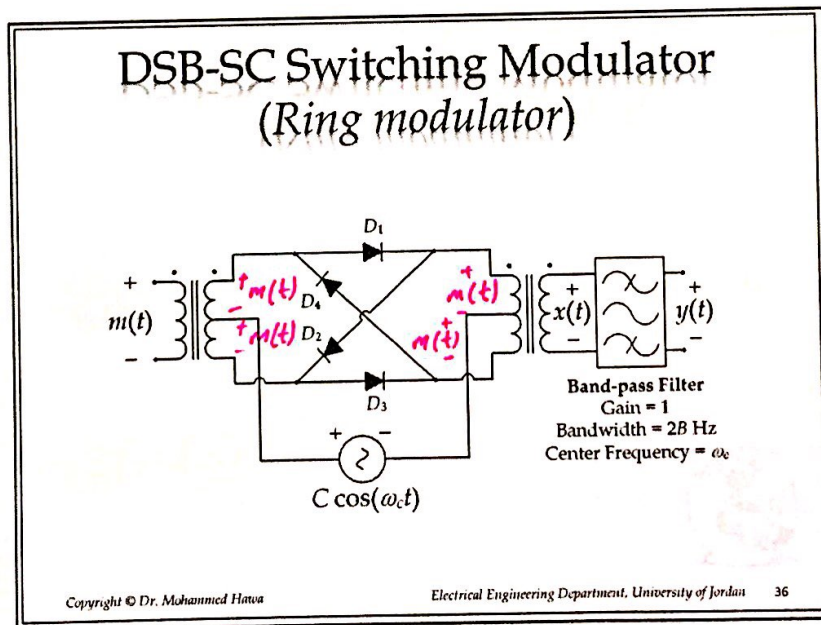
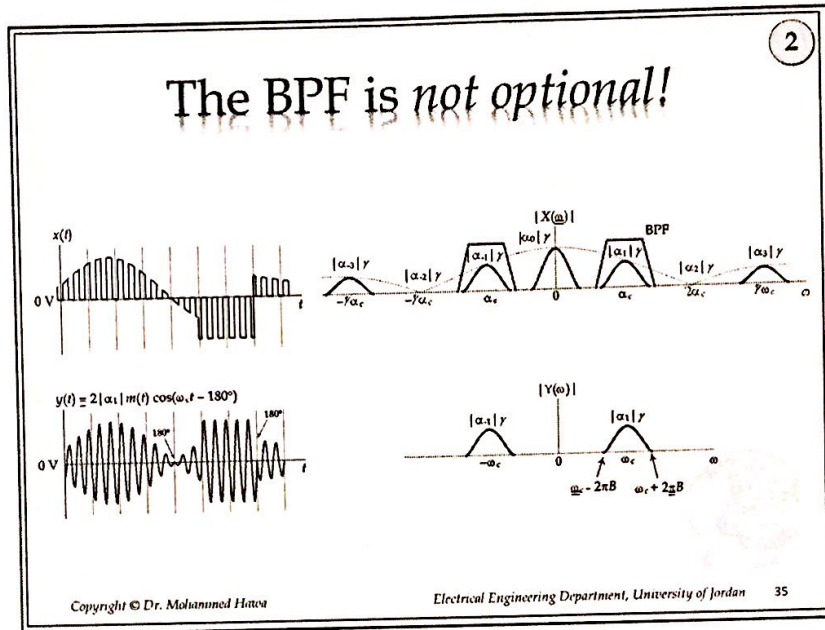
$$\alpha_1 = \frac{1}{2} \operatorname{sinc}\left(\frac{1}{2}\right) = \frac{1}{2} \frac{\sin \frac{\pi}{2}}{\frac{\pi}{2}} = \frac{1}{\pi}$$



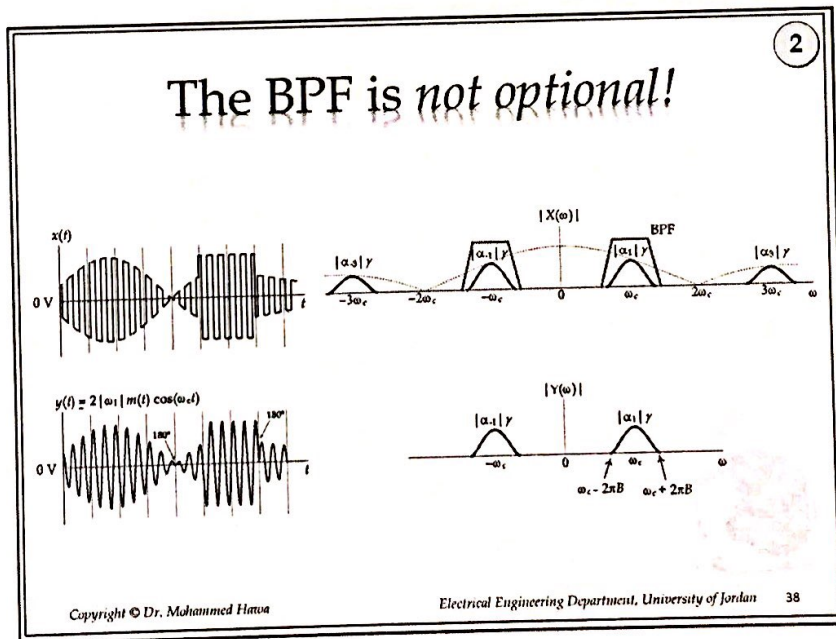
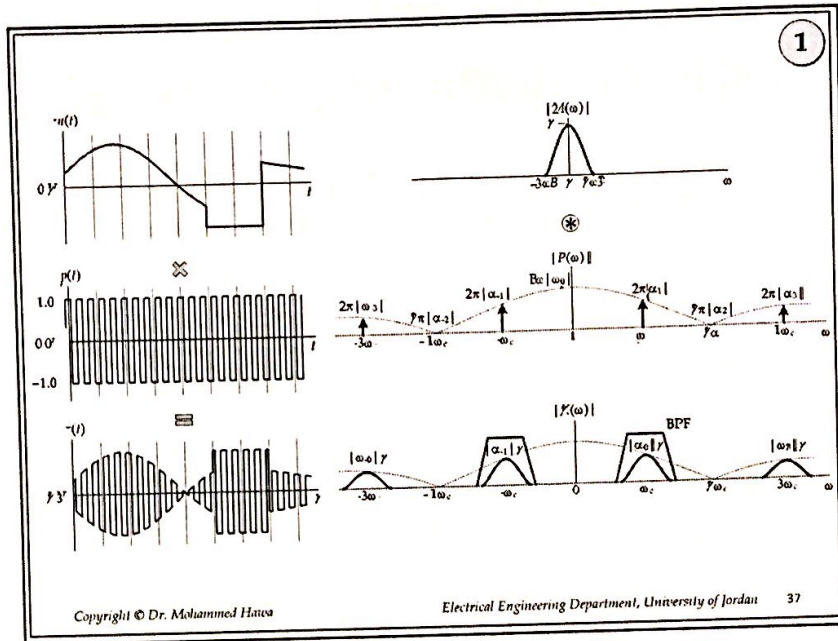
a shift in time
for the rect →
so a phase shift
will happen
in the freq.
domain.



$$x(t) = 0; m(t); 0; m(t) \dots$$

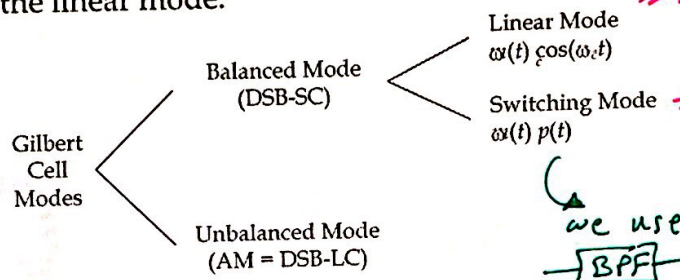


$$x(t) = m(t) ; -m(t) ; m(t) ; -m(t) ; \dots$$



Gilbert Cell as Switching Modulator

- It is recommended to use the Gilbert Cell (MC1496) in the switching mode, rather than the linear mode.

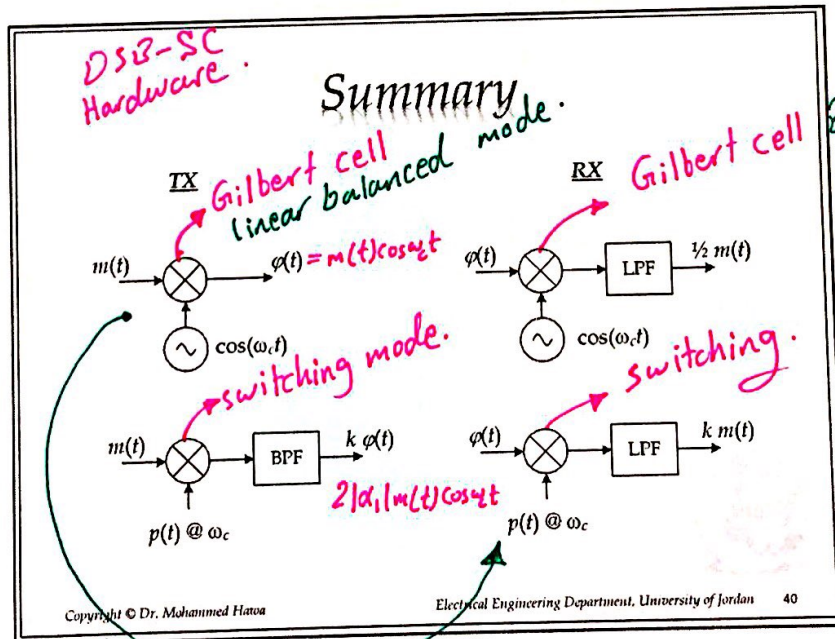


doesn't use BPF
⇒ gives less power.

this is the recommended one.

⇒ gives more power.

Two way To build the mixer. ⇒



Balanced linear mode

we could use them together as Tx & Rx.

Homework

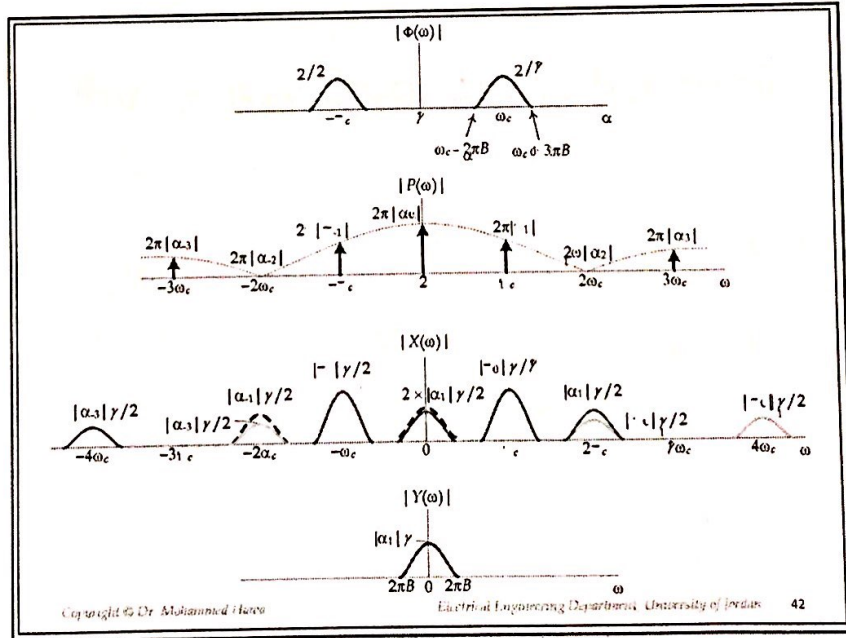
- If we use a switching demodulator (say a series-bridge diode demodulator), answer the following:

- What are the specifications of the filter? *LPF with*
- What is the value of k in the output $y(t) = k m(t)$ if the input is $\phi(t) = m(t) \cos(\omega_c t)$
- What is the value of k in the output $y(t) = k m(t)$ if the input is $\phi(t) = 2 |\alpha_1| m(t) \cos(\omega_c t)$
- Sketch the Fourier transform of the solution.

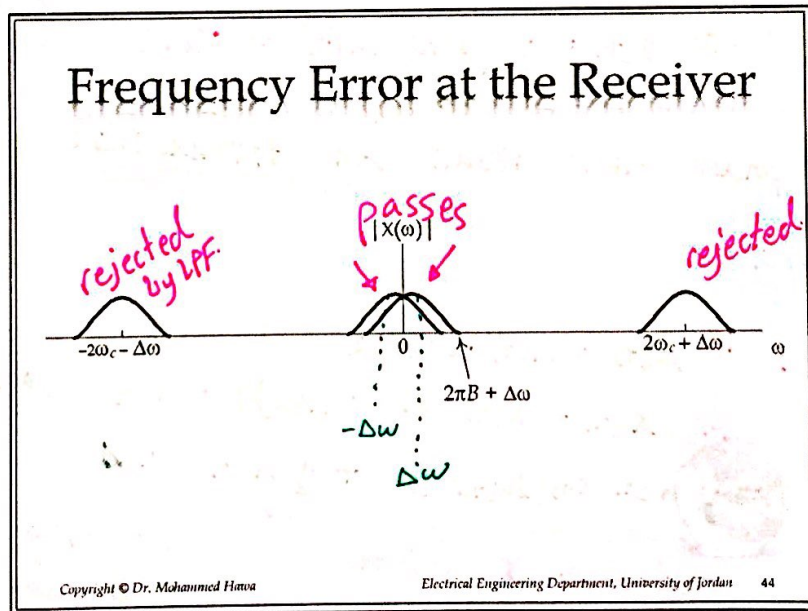
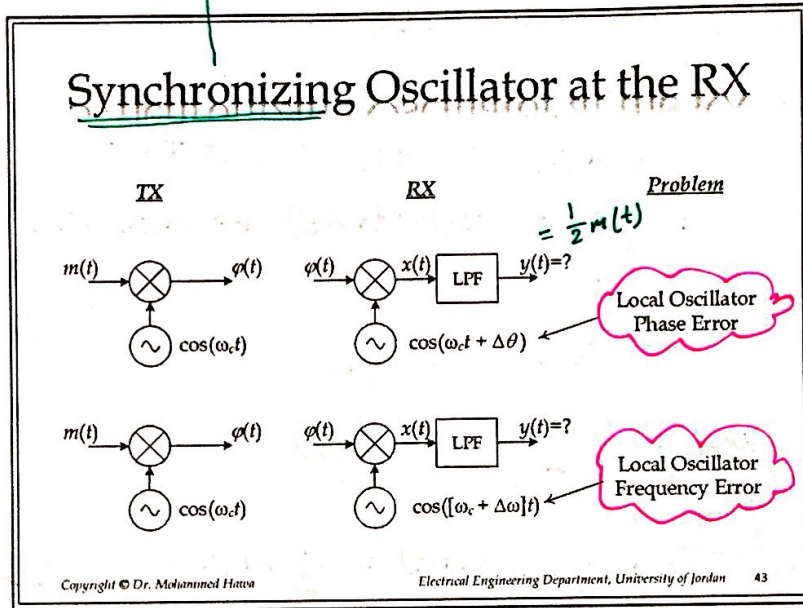
*gain = 1
bandwidth = B Hz
or $2\pi B$ rad/s.*

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same freq. & phase @ Rx & Tx



if we have phase & freq. errors together then we will have Attenuation & Distortion.

* Phase Error:

Find $y(t)$:

Solution: Tx $\phi(t) = m(t) \cos(\omega_c t)$

Rx $x(t) = \phi(t) \cos(\omega_c t + \Delta\theta)$

$$= m(t) \cos(\omega_c t) \cos(\omega_c t + \Delta\theta)$$

$$= \frac{1}{2} m(t) \cos(2\omega_c t + \Delta\theta) + \frac{1}{2} m(t) \cos(\Delta\theta)$$

High freq. @ $2\omega_c$
rejected by LPF.

Low freq passes. LPF.

$$\Rightarrow y(t) = \frac{1}{2} \cos(\Delta\theta) m(t)$$

No error $\Delta\theta = 0 \Rightarrow y = \frac{1}{2} \cos(0) m(t) = \frac{1}{2} m(t) \rightarrow < 1$

$\Delta\theta = 30^\circ \Rightarrow y(t) = \frac{1}{2} \cos(30) m(t) = \frac{1}{2} \cdot \frac{\sqrt{3}}{2} m(t)$

$\Delta\theta = 60^\circ \Rightarrow y(t) = \frac{1}{2} \cos(60) m(t) = \frac{1}{2} \cdot \frac{1}{2} m(t)$

worst case $\Delta\theta = 90^\circ \Rightarrow y(t) = \frac{1}{2} \cos(90) m(t) = \text{Zero}$ (No signal).

* so phase error result "An Attenuation"

* Frequency Error:

solve for $y(t)$: Tx $\phi(t) = m(t) \cdot \cos(\omega_c t)$

Rx $x(t) = \phi(t) \cos(\omega_c + \Delta\omega)t = m(t) \cos \omega_c t \cos(\omega_c + \Delta\omega)t$

$$= \frac{1}{2} m(t) \cos(2\omega_c + \Delta\omega)t + \frac{1}{2} m(t) \cos(\Delta\omega)t$$

High freq. so rejected
by LPF.

Low freq. so it passes
through LPF.

$$\Rightarrow y(t) = \frac{1}{2} m(t) \cos(\Delta\omega t)$$

* so freq. error result
"Distortion"



To avoid problems due to phase and frequency errors

new.

- Solution #1: Use a PLL (Phase-Locked Loop) at the RX. A PLL can, by observing $\phi(t)$, recover the exact frequency and phase of the carrier at the TX, and hence use these values at the RX. The PLL is called a **carrier-recovery circuit** (complex and expensive). The receiver in this case is known as a **synchronous or coherent** receiver.

old.

- Solution #2: Do not generate a carrier at the RX. Rather, let the TX send an extra copy of the carrier (e.g., DSB-LC) to help the RX demodulate $\phi(t)$. The RX is known as **asynchronous or incoherent** receiver (cheaper), but the TX is power inefficient.

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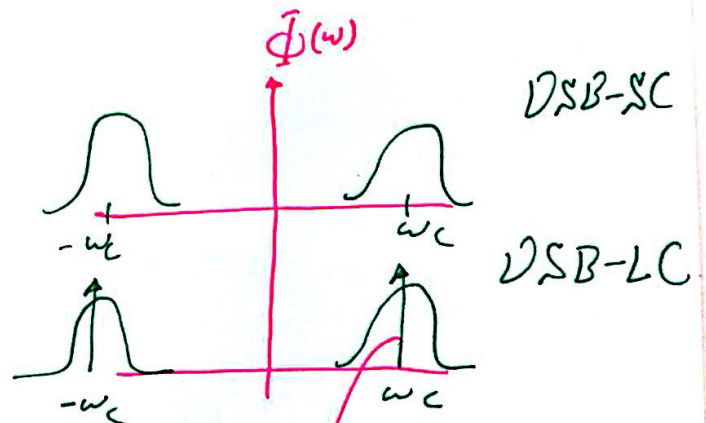
45

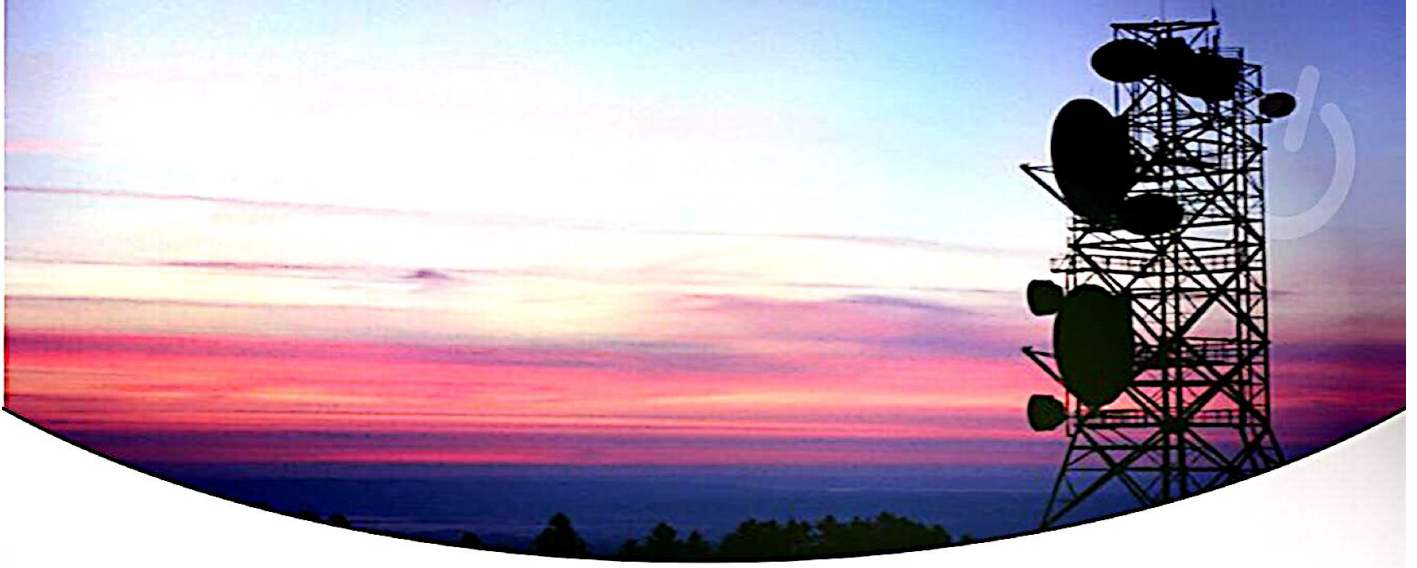
*very important (memorize): $\{ \text{PLL} \equiv \text{phase-locked loop} \}$

$\text{CLK}_{tx} \rightarrow \text{CLK}_{rx}$

must be synchronized

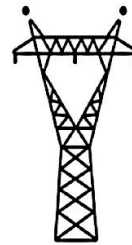
by using clock-recovery circuit (PLL).






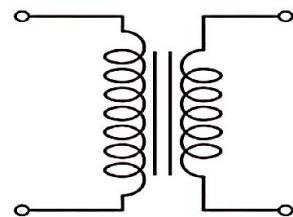
Communications I

Fall 2017



Dr. **M**hmd **H**awa 

 By: **M**hmd **A**buhashya



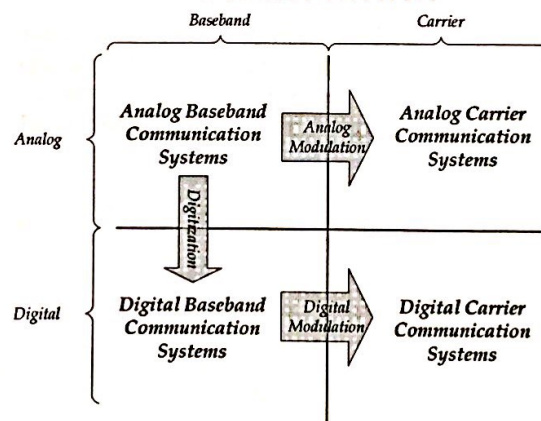
Powerunit-ju.com

Lecture 5a: Sampling and Quantization

Dr. Mohammed Hawa
Electrical Engineering Department
University of Jordan

EE421: Communications I

Digitization



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Digital Systems Advantages

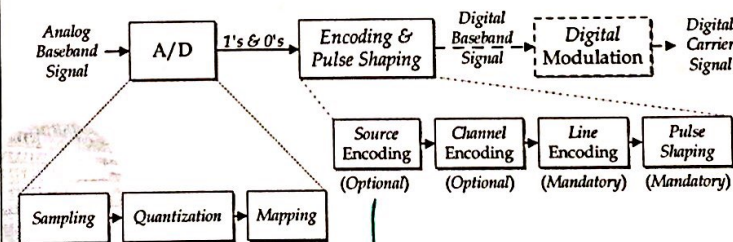
- Immunity to noise (threshold detection; regenerative repeaters).
- Multiplexing at the baseband level (e.g., TDM) and carrier level (e.g., FDM, CDMA and OFDMA).
- Spread spectrum techniques and orthogonality.
- Channel coding (i.e., error correcting codes).
- Source coding techniques (i.e., compression). Also Encryption.
- Exchanging SNR for bandwidth.
- Using microprocessors and DSP.
- Digital signal storage is relatively easy and inexpensive.

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Rigitization

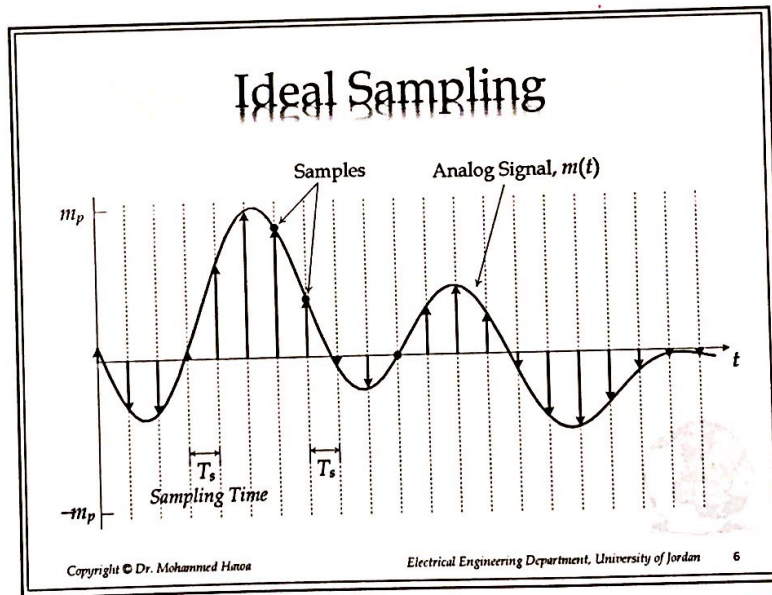
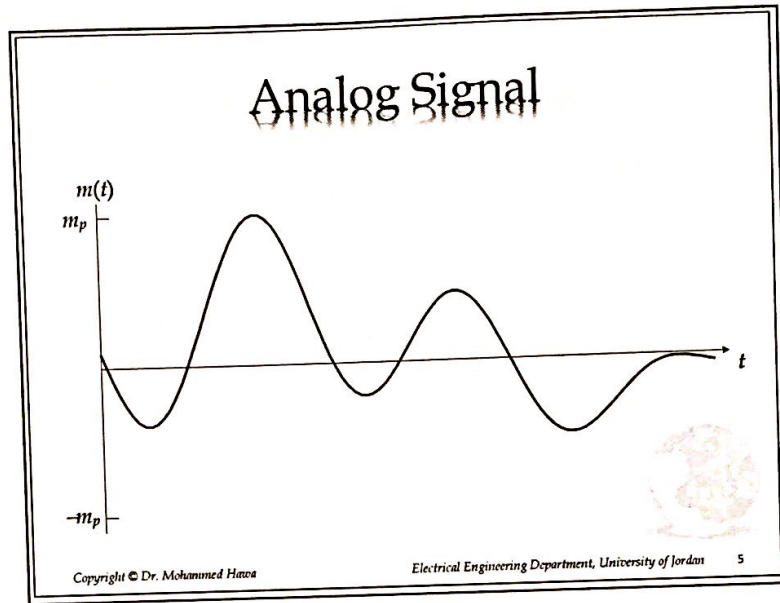
- Sampling (discrete analog signal).
- Quantization (quantized discrete signal)
- Mapping (stream of 1's and 0's).
- Encoding and Pulse Shaping (digital baseband signal).



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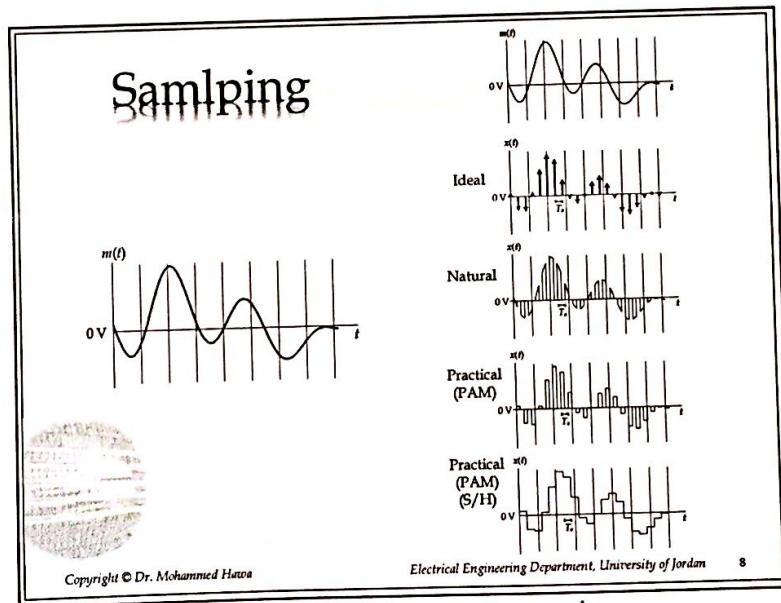
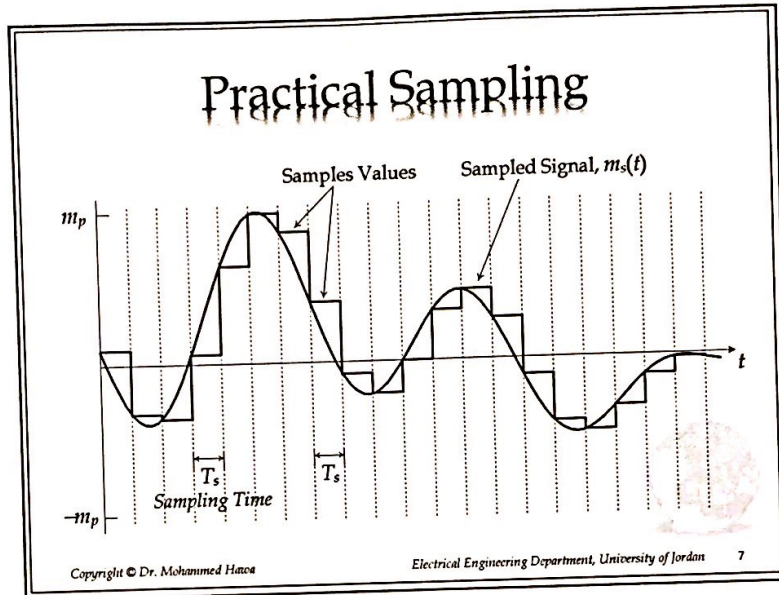
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optional because its complex & expensive.
But most new systems using them.



(f_s) sampling freq. = $\frac{1}{T_s}$, $\omega_s = \frac{2\pi}{T_s}$

$T_s, T_{\text{sym.}}, T_0$ are all different.

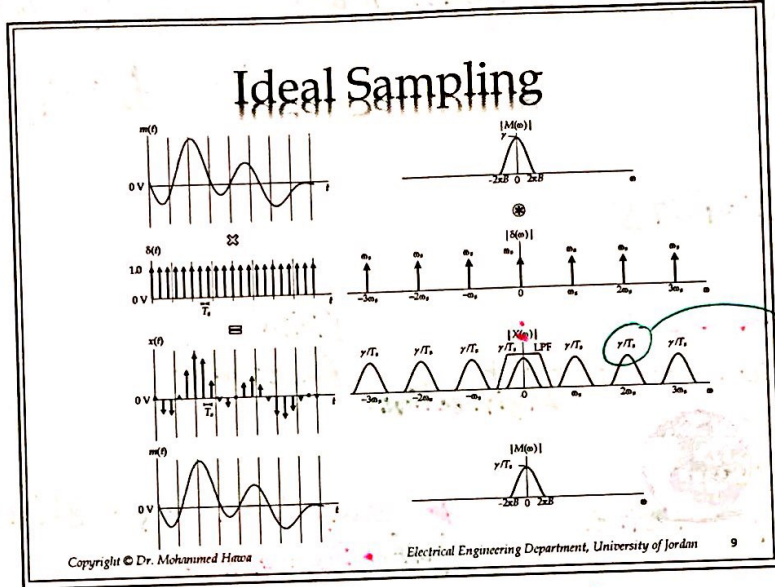


memorize:
 PAM \equiv Pulse Amplitude Modulation.
 \rightarrow This is just a name (it is NOT Modulation)
 it is a practical Sampling (included in Digitization)
 S/H \equiv Sample & Hold. \equiv practical sampling with max pulse width.

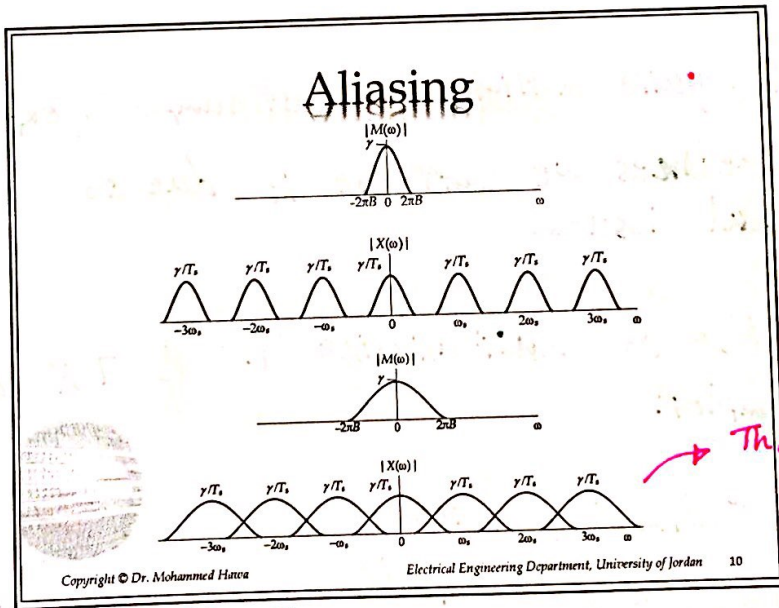
find $F\{x(t)\} = F\{\text{ideally-sampled version of } m(t)\} = F\{m(t) \cdot \text{rep}_{T_s}\{\delta(\cdot)\}\}$

$$= \frac{M(\omega) \star \Gamma(\omega)}{2\pi}$$

2/15/2017



$\omega_s \cdot \frac{1}{2\pi}$
 $= \frac{2\pi}{T_s} \cdot \frac{1}{2\pi}$
 $= \frac{1}{T_s}$



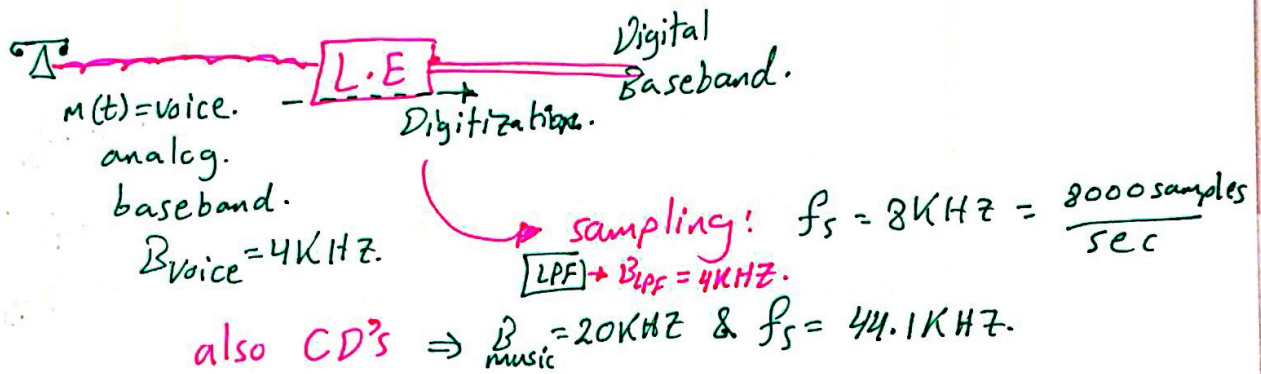
→ This overlap called Aliasing.

Bandwidth = B Hz
 or = $2\pi B$ rad/s
 gain = 1

* To avoid the problem of Aliasing?

- Sol #1: follow Nyquist Rate $\omega_s \geq 4\pi B$ rad/s.
or $f_s = \frac{1}{T_s} \geq 2B$ Hz

Ex1: PSTN = POTS



* Solution 1 require a High number of samples (expensive)
so sometimes we can't use it due to practical issues.

- Sol #2: Use an Anti-aliasing LPF @ TX before the sampler.

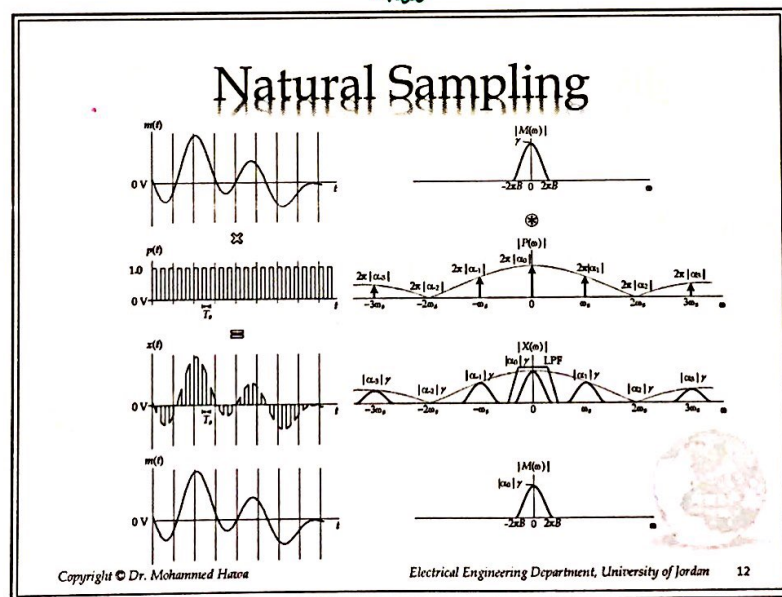
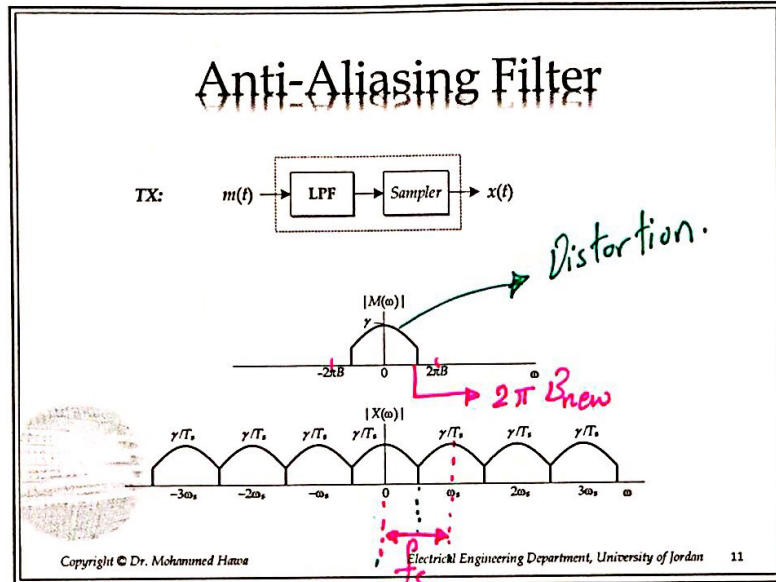
$$B_{LPF} = B_{\text{new}} = \frac{1}{2} f_s \text{ Hz}$$

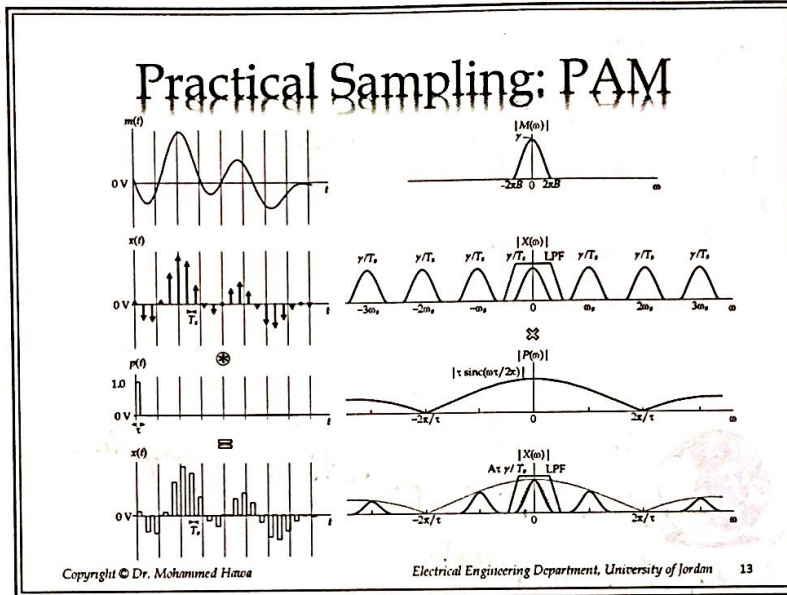
$$2\pi B_{\text{new}} = \frac{1}{2} \omega_s \text{ rad/s.}$$

But here we end-up with distortion

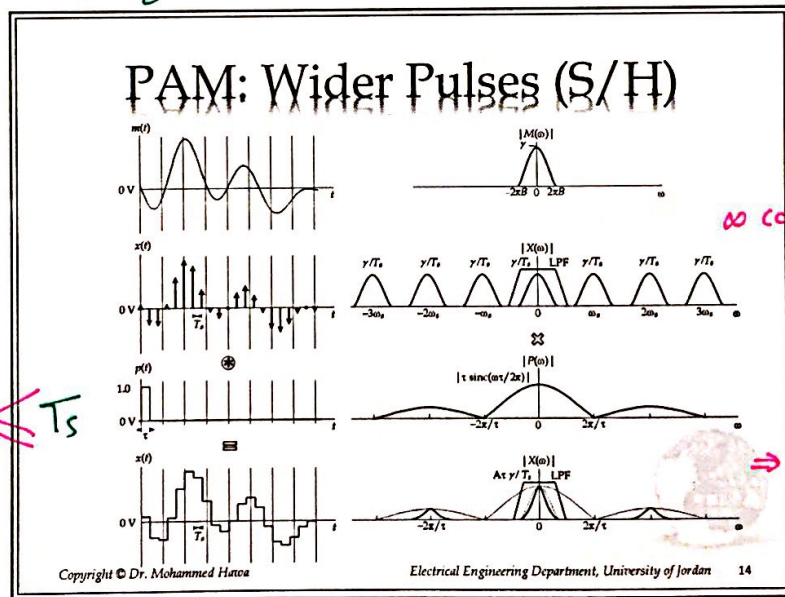
in sol #1:

No-aliasing
No-distortion





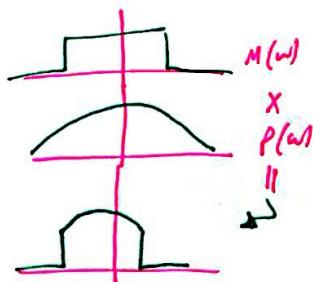
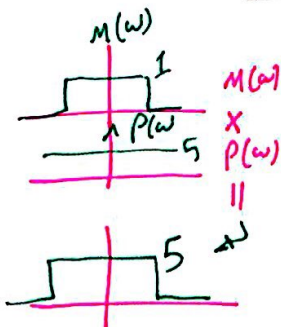
$$\mathcal{F}\{x(t) * y(t)\} = X(\omega) \cdot Y(\omega)$$



τ pulse width $\ll Ts$

∞ copies.

\Rightarrow distorted ∞ copies.



* Solution for Distortion in practical sampling:

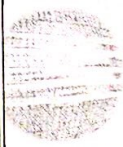
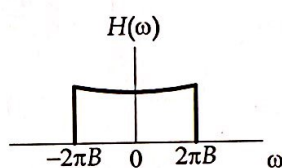
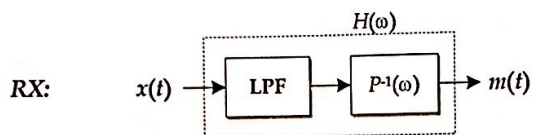
• Sol #1: Narrower Pulse Width.
(expensive). @ Tx.

Time Expansion
⇕
Freq. Compression.

• Sol #2: Equalizer @ Rx.
(expensive).

* So why we use Equalizer?
it is a solution for practical sampling
when distortion happen.

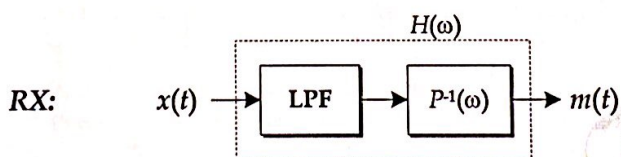
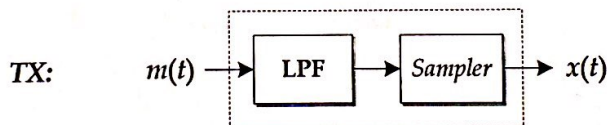
Distortion solved by Equalizer



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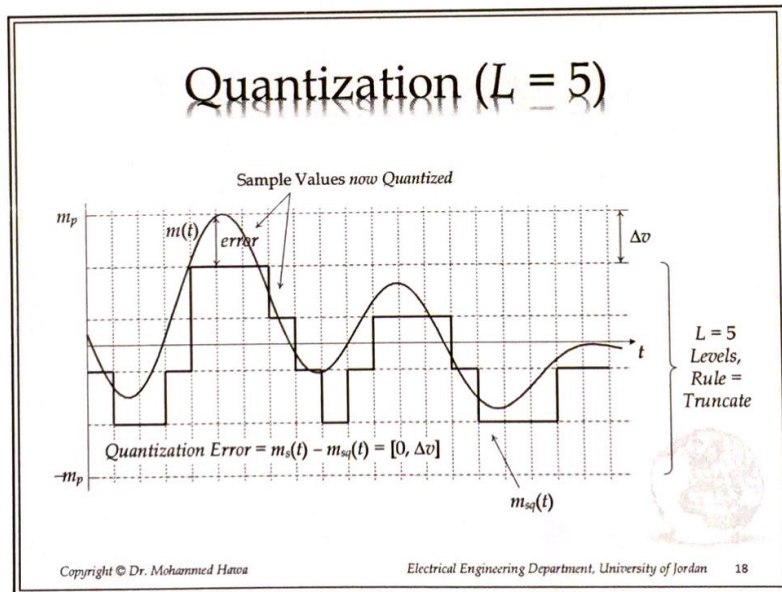
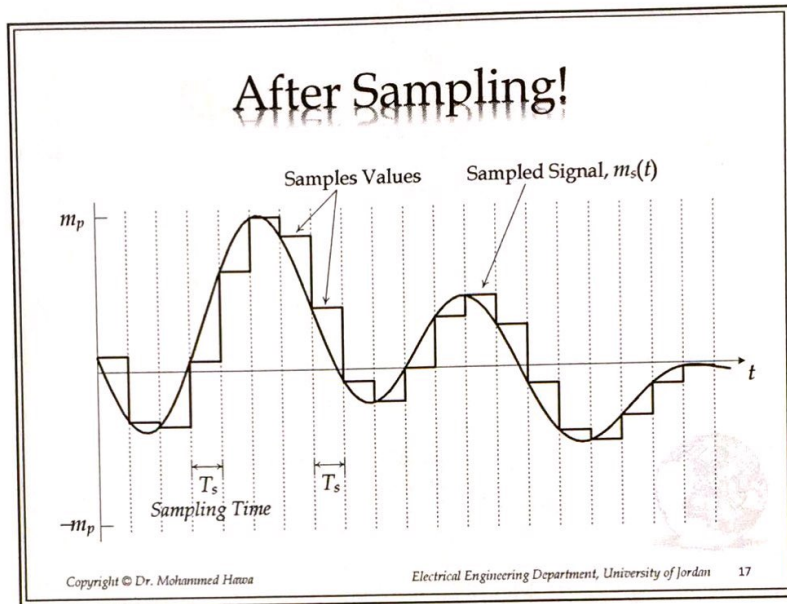
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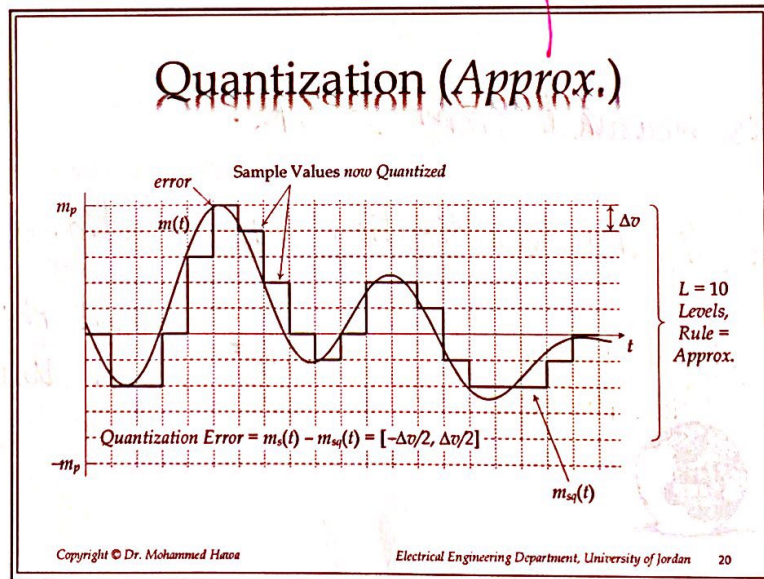
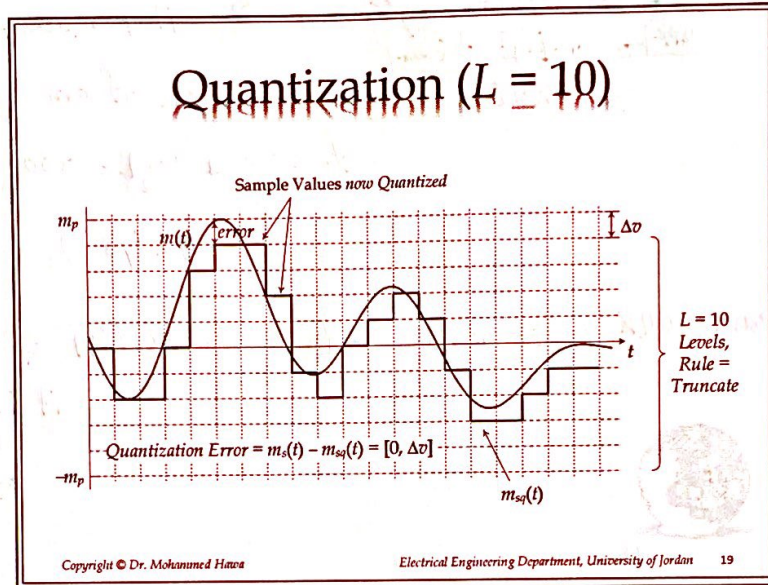
Summary



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if $L=4$ levels.

3V
2V
1V
0V

send 1.6V
 $\approx 2V$ will be sent.
(0.4V) Quant. Error.

if $L=8$ levels.

3.5V
3V
2.5V
2V
1.5V
1V
0.5V
0V

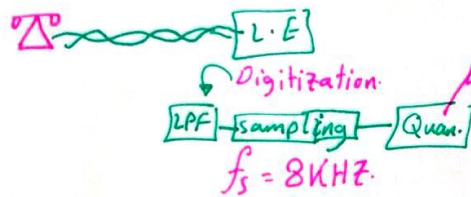
send 1.6V
 $\approx 1.5V$
less error.

Try for $L=16$
& $L=32$.

$L \equiv$ #of Quantization Levels
 $L \uparrow \Rightarrow$ Quantization error \downarrow
 = Noise \downarrow
 Quality \uparrow
 bits Per sample \uparrow
 Expensive. \uparrow

for $L=4$: Need 2-bits to represent.
 $L=8$: 3-bits.
 $L=16$: 4-bits.
 $L=32$: 5-bits.
 ...
 (More Expensive).

Example (1): Telephony. \rightarrow what line coding used in Telephony?
Bipolar.



$L = 256$ Levels.
 8-bit per sample.

Data Rate of one phone call:

$$f_0 = f_s * \log_2 L = 8000 \frac{\text{sample}}{\text{sec.}} * 8 \frac{\text{bits}}{\text{sample}}$$

$$f_0 = 64 \text{ Kbps}$$

* PCM stream (64Kbps) \equiv Pulse Coded Modulation \neq Modulation.

it is digital
 Baseband.
 of one phone call.

Example (2): CD's

$$L = 65,536 = 2^{16}$$

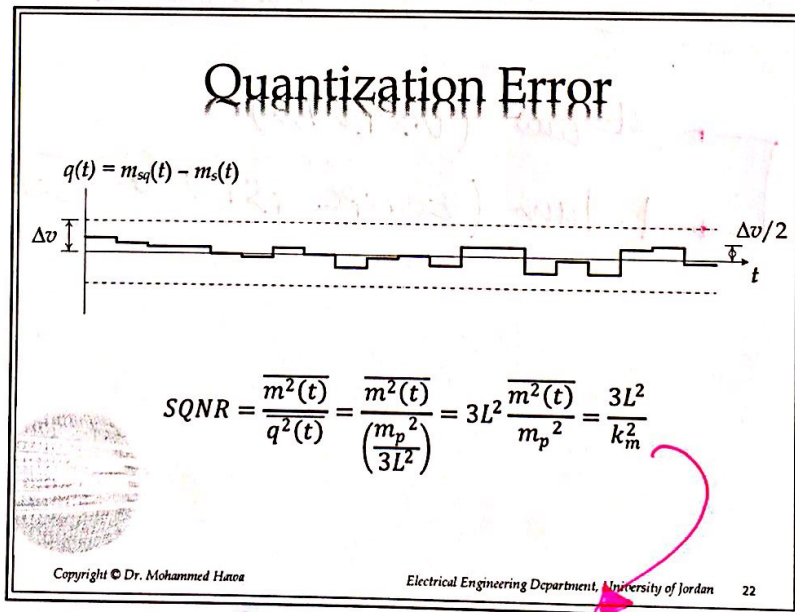
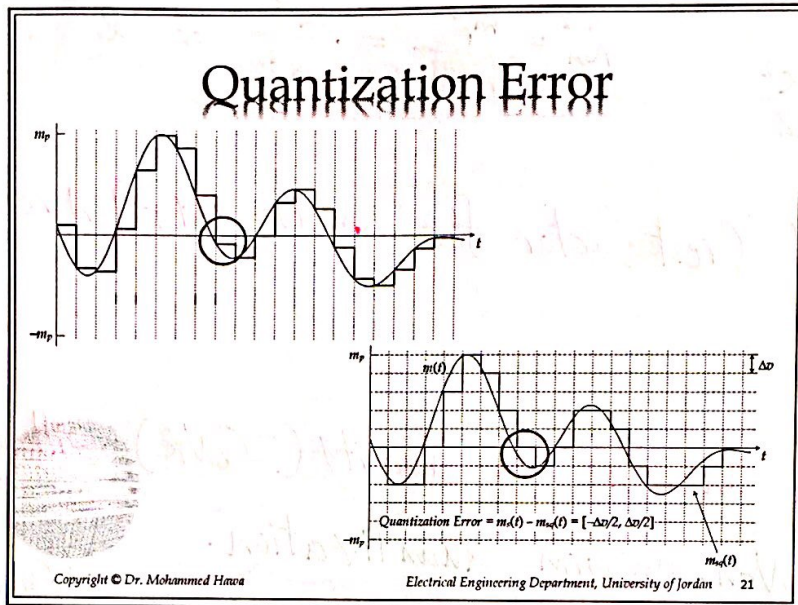
16-bit/sample.

#Quality is measured from SNR.

SQNR \equiv Signal to Quantization Noise Ratio.

$$\text{SNR} = \frac{\text{Signal Power}}{\text{Noise Power}}$$

$$\text{SQNR} = \frac{\text{signal Power}}{\text{Quant. Noise Power.}}$$



$L \uparrow \times 2$

$SQNR \uparrow \times 4$

$L \uparrow \times 5$

$SQNR \uparrow \times 25$

$k_m^2 \equiv$ Crest Factor OR Peak-to-RMS Ratio

$$k_m^2 = \frac{m_p^2}{m_{rms}^2}$$

$$K_m^2 = \frac{m_p^2}{m_{rms}^2} = \frac{m_p^2}{\text{avg. Power}} = \frac{m_p^2}{m^2(t)}$$

Example: find the Crest Factor for $m(t) = \alpha \cos(\omega_m t)$?

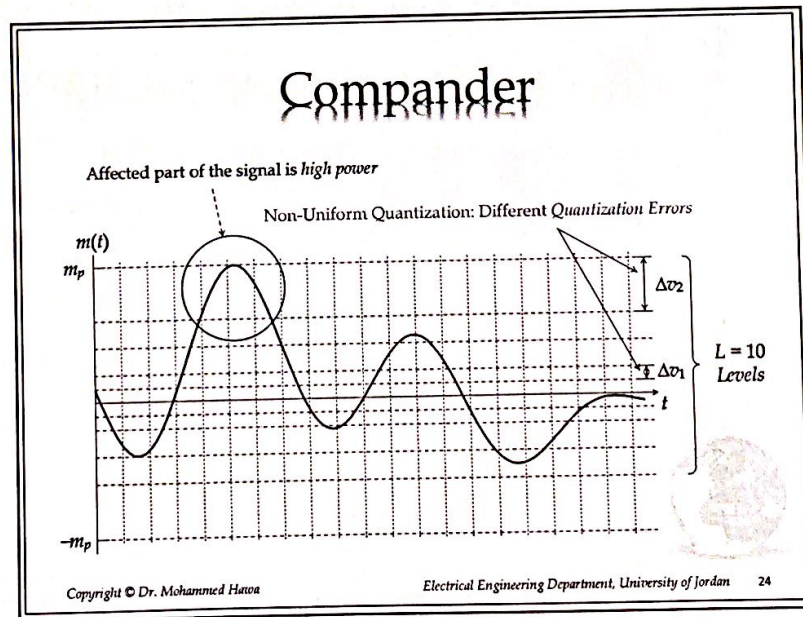
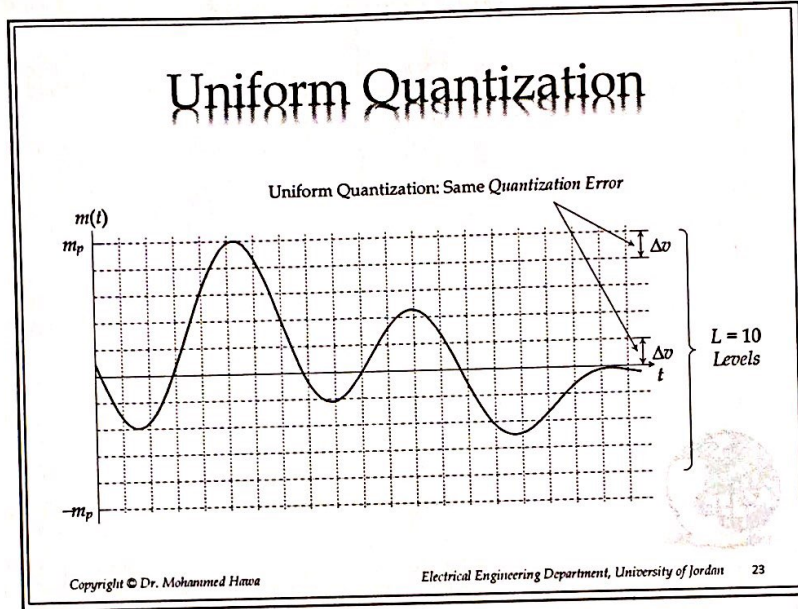
$$\frac{m_p}{m^2(t)} = \frac{\alpha^2}{2} \quad K_m^2 = \frac{m_p^2}{m^2(t)} = \frac{\alpha^2}{\alpha^2/2} = 2$$

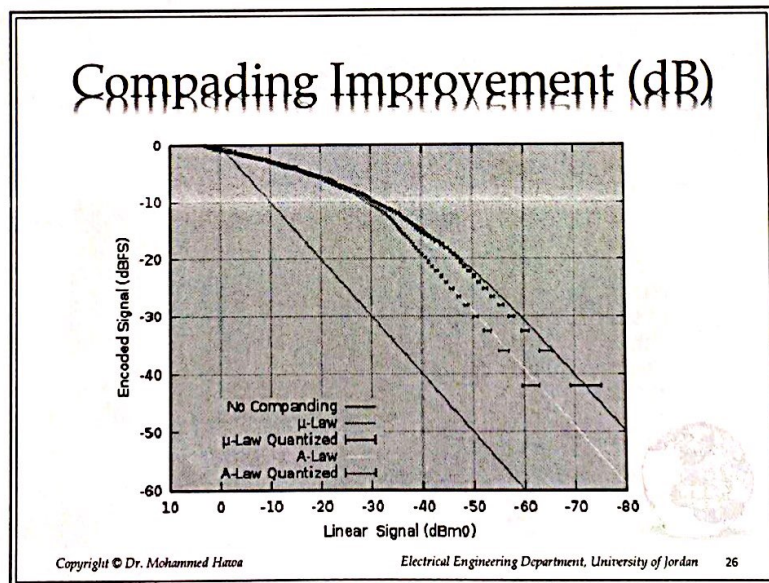
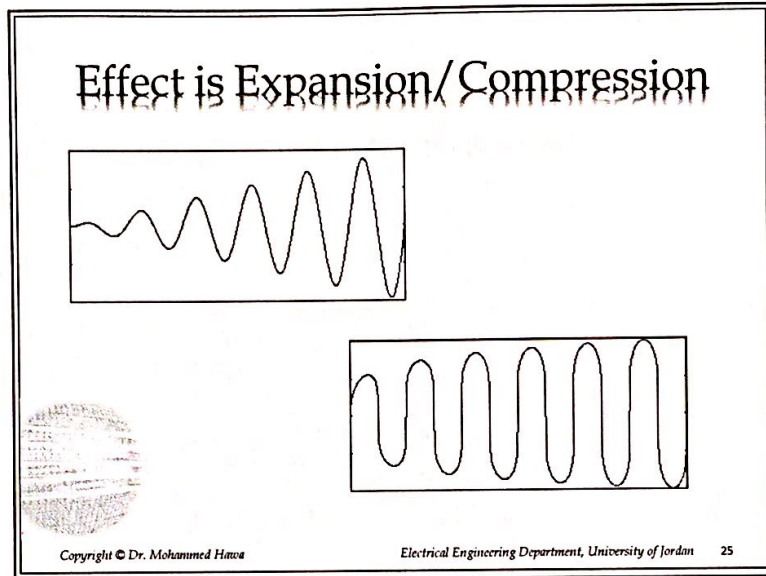
HW: find Crest factor for $m(t) = \text{rect}_T [A \text{rect}(t/T)]$?

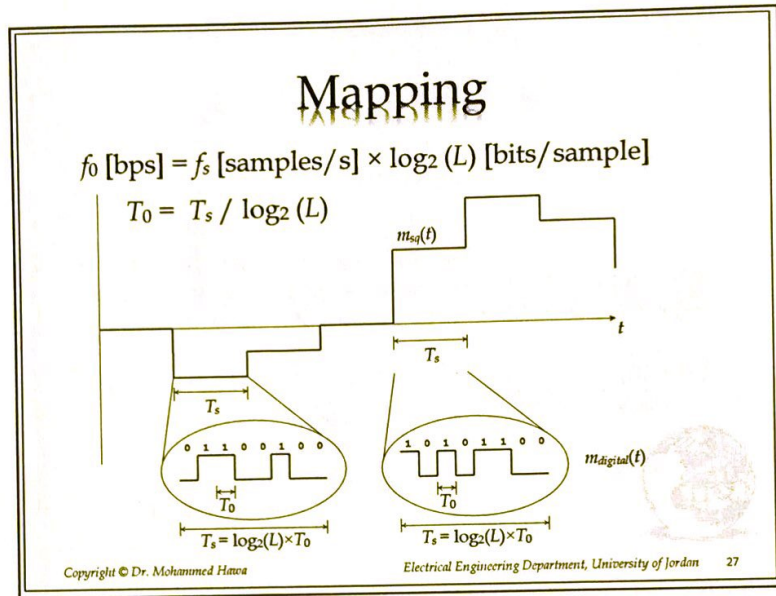
* You Can Increase the Quality (SQNR) without increasing L

Using: Non-uniform Quantization.
 OR \equiv Companding \equiv Compression/Decompression.
 (used in Telephony)

→ μ-law (U.S PSTN)
 → A-law (Europe PSTN & Jordan).



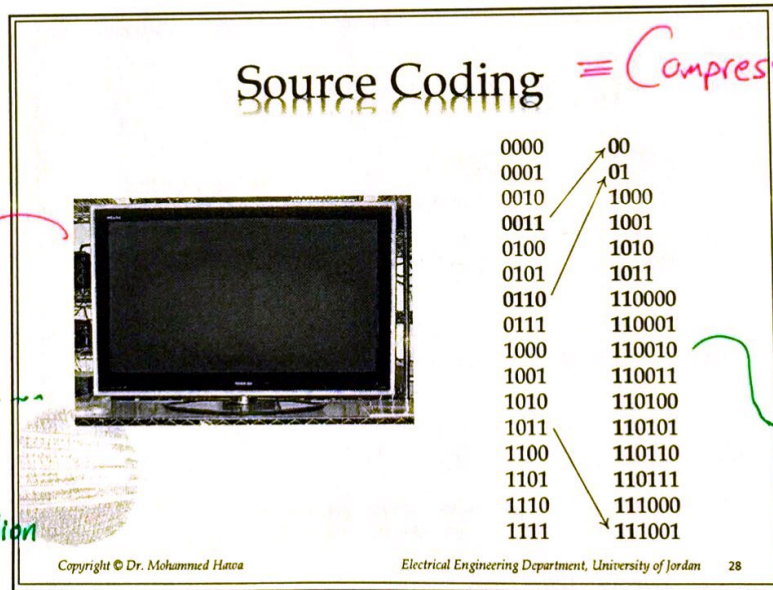




$L=4$

3V	11
2V	10
1V	01
0V	00

2bits
#of bits = $\log_2 L$



pixels.

it will send:

blue blue blue ...
0101 0101 0101 ...

we take 0101
repeat 16 million
times

for 16 possible colors
Need 4 bits.

- RLE: Run-length Encoding.
- Huffman encoding.

popular \Rightarrow short keyword.

16M pixels
 \rightarrow 16 million points.

rare \Rightarrow longer keyword.

Landline: (Doesn't use Compression = source coding).

Cellular: Uses source coding.

2/15/2017

cell phone.

digitization
including
compression.

Audio Compression

- Landline telephony (PCM, no compression)
 - 64 kbps
- Linear Prediction Coding (LPC) vocoder
 - e.g., RPE-LTP (regular pulse excitation, long-term prediction) LPC codec (GSM cellular phones, Full Rate): 13 kbps.
- Code-Excited linear Prediction (CELP) vocoder
 - Algebraic CELP(ACELP) (GSM cellular phones, Enhanced Full Rate) 12.2 kbps
 - FS-1016 (United States Department of Defense): 4.8 kbps

→ Memorize the underlined.

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Video Compression

(memorize).

- MPEG-2: DVD, Digital TV Broadcasting.
- H.261: Videophone.
- H.263: Low bit rate Video Conferencing.
- H.264: Almost everything.

<u>MPEG</u>	<u>ITU-T</u>
MPEG-1	H.261
↓	↓
MPEG-2	H.263
↓	↓
H.264/MPEG-4 Part 10 or AVC (Advanced Video Coding)	
↓	↓
H.265/MPEG-H Part 2 or HEVC (High Efficiency Video Coding)	

- ITU-T: International Telecommunication Union - Telecommunication
- MPEG: Moving Picture Experts Group

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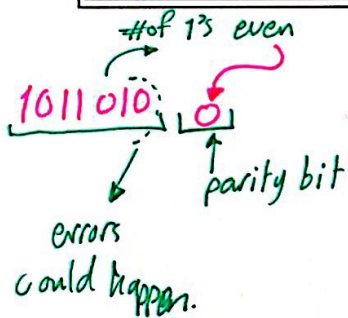
Channel Coding \equiv Bit error detection & Correction.

1110010101111010001010100
 \rightarrow 11100101011110100010101001011
 \rightarrow 11100101011110100010101001011
 \rightarrow 1110010101111010001010100

$C = B_{ch} \times \log_2(1 + SNR)$

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Ex. parity bit.



FEC \equiv Forward Error Correction.

HW: see satellite Receiver (setup \rightarrow menu).